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# IDENTIFICATION OF HEAT RELEASE SHAPES AND COMBUSTION CONTROL OF AN LTC ENGINE 

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# IDENTIFICATION OF HEAT RELEASE SHAPES AND COMBUSTION CONTROL OF AN LTC ENGINE 

By

Radhika Sitaraman

## A THESIS

Submitted in partial fulfillment of the requirements for the degree of MASTER OF SCIENCE

In Mechanical Engineering MICHIGAN TECHNOLOGICAL UNIVERSITY

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This thesis has been approved in partial fulfillment of the requirements for the Degree of MASTER OF SCIENCE in Mechanical Engineering.

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## Dedication

To My Parents \& Sister

## Contents

List of Figures ..... xiii
List of Tables ..... xvii
Preface ..... Xxi
Acknowledgments ..... xxiii
List of Abbreviations ..... XXV
Nomenclature ..... xxix
Abstract ..... Xxxi
1 Introduction ..... 1
1.1 Engine modelling for controls ..... 4
1.2 Machine learning based approach for combustion classification ..... 6
1.3 Machine learning approaches for ICE combustion modeling and con-trol11
1.4 Shortcomings of literature ..... 16
1.5 Scope of Research ..... 16
1.6 Organization of Thesis ..... 18
2 Experimental Setup ..... 20
2.1 Engine Specification ..... 20
2.1.1 Engine Modifications ..... 21
2.2 Data Acquisition ..... 23
2.3 Test data and Analysis ..... 24
2.3.1 Uncertainty Analysis ..... 25
2.4 Heat release rate calculation ..... 26
3 Classification of heat release rate traces ..... 29
3.1 Rule based Classification ..... 31
3.1.1 Characteristics of combustion type ..... 36
3.1.1.1 Peak Cylinder Pressure ..... 36
3.1.1.2 Maximum pressure rise rate ..... 38
3.1.1.3 $\mathrm{CA}_{10}$ ..... 39
3.1.1.4 $\mathrm{CA}_{90}$ ..... 40
3.1.1.5 Maximum in-cylinder temperature ..... 41
3.1.1.6 In-cylinder temperature at Start of main heat release ..... 42
3.1.1.7 In-cylinder temperature at End of main heat release ..... 44
3.1.1.8 Exhaust gas temperature ..... 45
3.1.1.9 Engine out emissions ..... 45
3.2 Supervised learning - Convolutional Neural Network ..... 48
3.2.1 CNN Theory ..... 49
3.2.2 Application of CNN in HRR shaping ..... 52
3.2.2.1 Prediction Accuracy of CNN model ..... 52
3.3 Supervised learning - Decision tree ..... 53
3.3.1 Decision tree theory ..... 54
3.3.2 Application of decision tree in HRR shaping ..... 56
3.3.2.1 Prediction Accuracy of decision tree model ..... 56
3.4 Unsupervised learning - k-means clustering ..... 58
3.4.1 k-means theory ..... 58
3.4.2 Application of k -means in HRR shaping ..... 60
3.4.2.1 Drawbacks of k -means classification ..... 60
4 Identification of combustion classifiers ..... 63
4.1 Scheduling parameter identification ..... 64
4.1.1 Principal Component Analysis (PCA) ..... 64
4.1.2 Multivariable linear regression ..... 67
4.1.2.1 Application of multi variable linear regression ..... 68
5 LPV model Identification with combustion classifiers ..... 72
5.1 Support Vector Machine (SVM) ..... 73
5.1.1 LS-SVM system identification ..... 73
5.1.2 Test data ..... 78
5.1.3 LTC engine modelling ..... 79
5.1.3.1 Model identification results ..... 80
5.1.3.2 System matrices ..... 83
6 Control of combustion phasing and IMEP with MPRR limitation ..... 85
6.1 LPV identification ..... 85
6.1.1 Evaluation of model accuracy ..... 86
6.2 Model Predictive Control ..... 88
6.2.1 Design ..... 89
6.2.2 Application ..... 92
6.2.2.1 Control structure ..... 94
6.2.2.2 Tracking Performance ..... 95
7 Conclusions and Future Work ..... 104
7.1 Summary and Conclusions ..... 104
7.2 Future work ..... 107
7.2.1 Control architecture for a multi-mode engine using HRR clas- sification ..... 107
7.2.1.1 Predictive models ..... 108
7.2.1.2 Algorithm for desired HRR type input ..... 109
7.2.1.3 MPC controller ..... 109
7.2.1.4 Learning Algorithm ..... 110
7.2.2 Other future works ..... 111
References ..... 113
A LTC engine data used for identification of scheduling parameter ..... 123
B LTC engine model data used for LPV-SVM system identification ..... 155
C Mode Frontier ..... 191
C.0.0.1 Optimization of hyper parameters of LS-SVM ..... 191
D Hyper Parameters Used for System Identification ..... 195
E Program and data files summary ..... 197
E. 1 Chapter 1 ..... 197
E. 2 Chapter 2 ..... 198
E. 3 Chapter 3 ..... 199
E. 4 Chapter 4 ..... 201
E. 5 Chapter 5 ..... 202
E. 6 Chapter 6 ..... 203
E. 7 Chapter 7 ..... 205
E. 8 Appendix A ..... 206
E. 9 Appendix B ..... 206
E. 10 Appendix C ..... 206

## List of Figures

1.1 Soot and $\mathrm{NO}_{x}$ in equivalence ratio to Temperature space ..... 2
1.2 Combustion metrics ..... 7
1.3 Thesis Organization ..... 19
2.1 LTC engine setup ..... 22
2.2 LTC Engine Data Acquisition ..... 23
3.1 Heat release rate trace with Start and End of Main HR depicted ..... 31
3.2 Flowchart of Classification Algorithm ..... 33
3.3 Sample heat release rate traces for three main HRR patterns ..... 34
3.4 Distribution of $\mathrm{COV}_{\text {IMEP }}$ ..... 35
3.5 Peak cylinder pressure distribution ..... 37
3.6 Maximum pressure rise rate distribution ..... 38
$3.7 \mathrm{CA}_{10}$ distribution ..... 39
$3.8 \quad \mathrm{CA}_{90}$ distribution ..... 41
3.9 Maximum in-cylinder temperature distribution ..... 42
3.10 In-cylinder temperature at Start of Main distribution ..... 43
3.11 In-cylinder temperature at end of Main distribution ..... 44
3.12 Heat release types ..... 46
3.13 HC emission ..... 46
3.14 CO emission ..... 46
$3.15 \mathrm{NO}_{x}$ emission ..... 47
3.16 Smoke (FSN) ..... 47
3.17 Representation of CNN structure ..... 50
3.18 Data dimensions through layers of CNN ..... 53
3.19 Prediction summary of CNN ..... 54
3.20 Decision tree for the engine HRR classification ..... 57
3.21 Prediction summary of Decision tree ..... 58
3.22 k -means classification of traces ..... 61
4.1 Plot of experimental data ..... 71
5.1 Manipulated variables of the LTC engine ..... 80
5.2 States of the LTC engine ..... 81
5.3 Scheduling parameters of the LTC engine ..... 81
5.4 Comparison of measured and modelled output of LTC engine ..... 82
5.5 $\bar{A}\left(p_{1 k}, p_{2 k}\right)$ matrix elements as a function of scheduling parameters ..... 83
5.6 $\bar{B}\left(p_{1 k}, p_{2 k}\right)$ matrix elements as a function of scheduling parameters ..... 84
5.7 $\mathrm{C}\left(p_{1 k}, p_{2 k}\right)$ matrix elements as a function of scheduling parameters ..... 84
6.1 Predicted $\mathrm{CA}_{50}$ from (a) LPV-SVM model and (b) physics based plant model as function of scheduling parameter p1 and p2 . . . . . . . 87
6.2 Predicted MPRR from (a) LPV-SVM model and (b) physics based plant model as function of scheduling parameter p1 and p287
6.3 Predicted IMEP from (a) LPV-SVM model and (b) physics based plant model as function of scheduling parameter p 1 and p 2
6.4 Schematic of the designed LPV-MPC controller for the LTC engine 93
6.5 Tracking capability of designed controller to follow desired $\mathrm{CA}_{50}$ and IMEP with MPRR limit is $6 \mathrm{bar} / \mathrm{CAD}$
6.6 Tracking capability of designed controller to follow desired $\mathrm{CA}_{50}$ and IMEP. The MPRR limit is $8 \mathrm{bar} / \mathrm{CAD}$99
6.7 Tracking capability of designed controller to follow desired $\mathrm{CA}_{50}$ and IMEP along with measurement uncertainty added in measured outputs of LTC engine. The MPRR limit is 6 bar/CAD
6.8 Tracking capability achieved for $\mathrm{CA}_{50}$ and IMEP with PR as scheduling parameter [49]. MPRR limit is 5.8 bar/CAD
6.9 Maximum tracking capability achieved for IMEP, when increased to 690 kPa and MPRR limit is $6 \mathrm{bar} / \mathrm{CAD}$
6.10 Maximum tracking capability achieved for $\mathrm{CA}_{50}$, when increased to 14 CAD aTDC and MPRR limit is 6 bar/CAD
7.1 Proposed control architecture for a multi-mode engine using HRR clas-
sification ..... 108
C. 1 Work flow of Mode Frontier tool ..... 192
C. 2 Hyper parameters tuned in Mode Frontier for LPV- SVM model from
Section 6.2 ..... 193
C. 3 Hyper parameters tuned in Mode Frontier for LPV- SVM model from
Section 6.2 ..... 194

## List of Tables

2.1 Engine Specifications ..... 21
2.2 Fuel Specifications ..... 22
2.3 Test conditions of engine data ..... 25
2.4 Table of measured parameters and associated uncertainties ..... 26
2.5 Derived parameters and associated uncertainties ..... 26
3.1 Summary of the classified HRR traces ..... 35
3.2 Table of $\mathrm{COV}_{\text {IMEP }}$ distribution ..... 36
3.3 Table of peak cylinder pressure distribution ..... 36
3.4 Table of maximum pressure rise rate distribution ..... 38
3.5 Table of $\mathrm{CA}_{10}$ distribution ..... 39
3.6 Table of $\mathrm{CA}_{90}$ distribution ..... 40
3.7 Table of Maximum in-cylinder temperature distribution ..... 42
3.8 Table of in-cylinder temperature distribution at start of main heat release ..... 43
3.9 Table of in-cylinder temperature distribution at end of main heat re-
lease ..... 44
4.1 Output of PCA on HRR classifier identification ..... 66
4.2 Table of iteration of engine parameters to model fraction of early HR and fraction of late HR ..... 69
6.1 Valid operating region of LPV-SVM model of LTC engine ..... 86
6.2 Summary of constraints applied on manipulated variables and outputs of the adaptive MPC ..... 95
C. 1 Range of hyper parameters defined in Mode Frontier ..... 194
D. 1 Table of hyper parameters for System Identification with $A, B$ and $C$ matrices ..... 196
E. 1 Figure Files ..... 197
E. 2 Visio Files ..... 197
E. 3 Figure Files ..... 198
E. 4 Matlab Data File ..... 199
E. 5 Matlab code Files ..... 199
E. 6 Python code ..... 199
E. 7 Visio Files ..... 200
E. 8 Figure Files ..... 200
E. 9 Matlab Figure Files ..... 200
E. 10 Matlab code ..... 201
E. 11 Figures ..... 201
E. 12 Rstudio data and Code ..... 201
E. 13 Matlab code ..... 202
E. 14 Data file ..... 202
E. 15 Figure files ..... 202
E. 16 Figure files ..... 203
E. 17 Visio files ..... 203
E. 18 Matlab code ..... 203
E. 19 Simulink files ..... 204
E. 20 Matlab Data ..... 204
E. 21 Figure file ..... 205
E. 22 Data file ..... 206
E. 23 Data file ..... 206
E. 24 Figure file ..... 206

## Preface

Work documented is in continuation of research by Kaveh Sadabadi [1], Kaushik Kannan [2], Nitin Kondipati [3], Akshat Raut [4] and Aditya Basina [5]. Engine data collected in [2, 3] was used in Chapter 3. The convolutional neural network developed by Yajie Bao was used for heat release rate classification in Section 3.2 and k-means developed by Aditya Basina was used in Section 3.4. Dr. Mahdi Shahbakhti provided guidance on the aspects of the thesis includign engine data analysis, heat release rate classification model based on machine learning approach, identification of scheduling parameter and building control architecture with scheduling variable. Dr. Jeffrey Naber provided guidance for proper analysis of the engine heat release data. Dr. Hoseinali Borhan and Dr. Javad Mohammadpour Velni provided technical advise on optimization tools for building data driven modelling for engine data and machine learning approach for classification of heat release rate traces. The LS-SVM code from the reference [6] was used in Chapter 4 to perform data driven modelling. RCCI engine plant developed in references [1, 2, 3, 3] is used to assess the performance of controller.

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I would also like to recognise the invaluable support provided by Yajie Bao, Aditya Basina, Sadaf Batool and Behrouz Khoshbakht Irdmousa during this study. They helped me out at a peer level on various research queries. I wish to express my deepest gratitude to my friend Shruti Amre for always being there as a moral support throughout this study.

## List of Abbreviations

| ANN | Artificial Neural Network |
| :--- | :--- |
| aTDC | after Top Dead Center |
| bTDC | before Top Dead Center |
| CAD | Crank Angle Degree |
| CFD | Computational Fluid Dynamics |
| CFR | Cooperative Fuel Research |
| CI | Compression Ignition |
| CNG | Compressed Natural Gas |
| CNN | Convolutional Neural Network |
| COV | Data Driven Modelling |
| DDM | Direct Injection |
| DI | Deep Learning Neural Network |
| DKL | Electronic Control Unit |
| ECU | Exhariation |
| EGR | Extreme Learning Machine Combustion |
| ELM | EPA |


| FPGA | Field Programmable Gate Array |
| :---: | :---: |
| GA | Genetic Algorithm |
| GDI | Gasoline Direct Injection |
| HCCI | Homogeneous Charge Compression Ignition |
| HDMR | High Dimensional Model Representation |
| IC | Internal Combustion |
| IMEP | Indicated Mean Effective Pressure |
| LPV | Linear Parameter Varying |
| LS-SVM | Least Square Support Vector Machine |
| LTC | Low Temperature Combustion |
| MABX | Micro Auto Box |
| MPC | Model Predictive Control |
| MPRR | Maximum Pressure Rise Rate |
| MSE | Mean Square Error |
| $\mathrm{NO}_{x}$ | Oxides of Nitrogen |
| NTEOFC | Not To Exceed Oxygen Fuel Control |
| PCA | Principal Component Analysis |
| PCCI | Premixed Charge Compression Ignition |
| PFI | Port Fuel Injection |
| PM | Particulate matter |
| PN | Particulate Number |


| PR | Premixed Ratio |
| :--- | :--- |
| PSO | Particle Swam Optimisation |
| RCCI | Reactivity Controlled Compression Ignition |
| RGS | Random Gaussian Signal |
| RMSE | Root Mean Square Error |
| RVM | Relevance Vector Machine |
| SA | Simulated Annealing |
| SI | Spark Ignition |
| SOC | Start of Combustion |
| SOI | Start of Injection |
| SVM | Support Verctor Machine |
| SVSF | Smooth Variable Structure Filter |
| VGT | Variable Geometry Turbocharger |

## Nomenclature

| Symbol | Variable | Units |
| :---: | :---: | :---: |
| $c_{v}$ | Specific heat at constant volume | kJ/kg.K |
| LHV | Lower Heating Value | $\mathrm{MJ} / \mathrm{kg}$ |
| $m^{\prime}{ }_{\text {air }}$ | Mass flow of air | $\mathrm{g} / \mathrm{s}$ |
| $m^{\prime}{ }_{\text {fuel }}$ | Mass flow of fuel | mg/cycle |
| $m f_{\text {iso }}$ | Mass flow of iso- octane fuel | mg/cycle |
| $m f_{\text {nhep }}$ | Mass flow of n-heptane fuel | mg/cycle |
| $N$ | Engine speed | RPM |
| $n_{c}$ | Polytropic coefficient for compression | - |
| $n_{e}$ | Polytropic coefficient for expansion | - |
| $P_{i n}$ | Intake Pressure | kPa |
| $P_{i v c}$ | Pressure at IVC | kPa |
| $r_{c}$ | Compression Ratio | - |
| Sig | Spontaneous ignition front speed | $\mathrm{m} / \mathrm{s}$ |
| $T_{e x h}$ | Exhaust gas Temperature | K |
| $T_{\text {in }}$ | Intake Temperature | K |
| $T_{i v c}$ | Temperature at IVC | K |
| $T_{r g}$ | Temperature of residual gas | K |


| $T_{w}$ | Temperature of cylinder wall | K |
| :--- | :--- | :--- |
| $\gamma$ | Ratio of specific heat | - |
| $\Delta T$ | Temperature rise | K |
| $\phi$ | Equivalence ratio | - |
| $\theta$ | Crank Angle | CAD |


#### Abstract

Low Temperature Combustion (LTC) regimes have gained attention in internal combustion engines since they deliver low nitrogen oxides $\left(\mathrm{NO}_{x}\right)$ and soot emissions with higher thermal efficiency and better combustion efficiency, compared to conventional combustion regimes. However, the operating region of these high-efficiency combustion regimes is limited as it is prone to knocking and high in-cylinder pressure rise rate outside the engine safe zone. By allowing multi-regime operation, high-efficiency region of the engine is extended. To control these complex engines, understanding and identification of heat release rate shapes is essential. Experimental data collected from a 2 liter 4 cylinder LTC engine with in-cylinder pressure measurements, is used in this study to calculate Heat Release Rate (HRR). Fractions of early and late heat release are calculated from HRR as a ratio of cumulative heat release in the early or late window to the total energy of the fuel injected into the cylinder. Three specific HRR patterns and two transition zones are identified. A rule based algorithm is developed to classify these patterns as a function of fraction of early and late heat release percentages. Combustion parameters evaluated also showed evidence on characteristics of classification. Supervised and unsupervised machine learning approaches are also evaluated to classify the HRR shapes. Supervised learning method ( Decision Tree)is studied to develop an automatic classifier based on the control inputs to the engine. In addition, supervised learning method (Convolutional


Neural Network (CNN)) and unsupervised learning method (k-means clustering) are studied to develop an automatic classifier based on HRR trace obtained from the engine. The unsupervised learning approach wasn't successful in classification as the arrived k-means centroids didn't clearly represent a particular combustion regime. Supervised learning techniques, CNN method is found with a classifier accuracy of $70 \%$ for identifying heat release shapes and Decision Tree with the accuracy of $74.5 \%$ as a function of control inputs.

On rule based classified traces with the use of principle component analysis (PCA) and linear regression, heat release rate classifiers are built as a function of engine input parameters including, Engine speed, Start of injection (SOI), Fuel quantity (FQ) and Premixed ratio (PR). The results are then used to build a linear parameter varying (LPV) model as a function of the modelled combustion classifiers by using the least square support vector machine (LS-SVM) approach. LPV model could predict $\mathrm{CA}_{50}$ (Combustion phasing), IMEP (indicated mean effective pressure) and MPRR (maximum pressure rise rate) with a RMSE of $0.4 \mathrm{CAD}, 16.6 \mathrm{kPa}$ and $0.4 \mathrm{bar} / \mathrm{CAD}$ respectively. The designed LPV model is then incorporated in a model predictive control (MPC) platform to adjust $\mathrm{CA}_{50}$, IMEP and MPRR. The results show the designed LTC engine controller could track $\mathrm{CA}_{50}$ and IMEP with average error of 1.2 CAD and 6.2 kPa while limiting MPRR to 6 bar/CAD. The controller uses three engine inputs including, SOI, PR and FQ as manipulated variables, that are optimally changed to control the LTC engine.

## Chapter 1

## Introduction

Greenhouse gas emissions in atmosphere have increased world wide. In the latest report by the United States Environmental Protection Agency (EPA), it is evident that transportation sector is one of the major contributors of greenhouse gas emissions in the United States [7]. EPA and other emission regulating agencies across the world have taken measures to curb the pollutants. They have imposed stringent emission norms and higher fuel economy targets. Automotive manufacturers and researchers have continuously worked to innovate new techniques in order to achieve emission and fuel economy targets. Many concepts have been developed to eliminate the drawback observed on a conventional injection technique. In the conceptual model of conventional direct injection (DI) combustion in [8] the process involved in creation of $\mathrm{NO}_{x}$ and soot is described. $\mathrm{NO}_{x}$ gets created at the contact of diffusion flame front
with premixed charge. Soot gets generated at the fuel rich zones of the fuel plume. Based on this understanding a recent technique of low temperature combustion(LTC) was developed. It results in ultra low $\mathrm{NO}_{x}$ and soot as significant amount of fuel is pre-mixed with air before the actual combustion begins. Soot is eliminated by having a premixed mixture of fuel and air. $\mathrm{NO}_{x}$ is reduced by having a premixed volumetric combustion [9].Multiple concepts of LTC demonstrated by researchers [2, 9, 10, 11], either used single fuel or combination of two fuels.

Some of the prominent techniques of LTC are shown in the Figure 1.1, in local equivalence ratio and temperature space.


Figure 1.1: Soot and $\mathrm{NO}_{x}$ in equivalence ratio to Temperature space reference [12] Adapted from reference [13]

Interestingly, conventional diesel operates in a zone which is prone for higher $\mathrm{NO}_{x}$ and soot. Advanced combustion techniques depicted, predominantly operate on a lower $\mathrm{NO}_{x}$ and soot zone. Various Combustion regimes of interest and research work is described below.
$\dagger$ Homogeneous charge compression ignition (HCCI) is a concept in which fuel is injected into intake manifold to achieve a homogeneous premixed charge. Charge is compressed in the compression stroke. It results in controlled auto ignition (CAI). So, a volumetric combustion with a small burn duration is achieved [14, 15]. It results in high in cylinder pressure rise rate.
$\dagger$ Premixed charge compression ignition (PCCI) was developed from HCCI concept to reduce its drawbacks of higher pressure rise rate. In PCCI, fuel is injected partially in the manifold and in-cylinder in order to reduce homogeneity of fuel and air, [16, 17, 18]. Secondary fuel injection timing adds more control on combustion phasing.
$\dagger$ Reactivity controlled compression ignition (RCCI) works on the principle of difference in reactivity rates of two different fuels being used for combustion. The low reactivity fuel is injected into the intake ports. In the homogeneous mixture of low reactivity fuel and air, the high reactivity fuel is injected inside the cylinder. Studies in references, [19, 20, 21] discuss additional control levers for governing combustion phasing such as difference in reactivity of both fuels,
start of injection timing of the higher reactivity fuel and the ratio of both low reactivity and high reactivity fuel on the engine.

Understanding of these low temperature combustion techniques play critical role in order to study the heat release traces of the engine and incorporate the dynamics involved while developing engine models.

### 1.1 Engine modelling for controls

Internal combustion (IC) engine modelling techniques have gained attention as it could improve engine performance. It could predict engine performance parameter without physically running the engine and also estimate parameters which are difficult to be measured [22]. Automotive manufacturers are keen to improve accuracy of engine model as it saves money and product development time. Control oriented models are advanced mathematical models suitable for control system design. It is built based on two fundamental methods
$\dagger$ First principle based approach
$\dagger$ Data driven approach

In first principle based approach, model is primarily based on physical principles.

Additionally engine experimental data is used to parameterize engine models. This helps to closely represent the engine. Input-output models and first principle based models are inter dependent on each other to ensure accuracy of the engine model. In [23] reviewed advancement in engine modelling. Improved engine model has resulted in better control of engine. The model was developed for performance optimisation of steady state calibration and dynamic corrections to calibration.

First principle based approach is time consuming to build. As an alternative, data driven approach has gained significance. In [24] data driven approach, the relationship between inputs and outputs of the system is modelled, without complex physics based modelling of the system. Data driven modelling represent the significant contribution made by the fields, artificial intelligence (AI), Computational intelligence (CI), soft computing (SC), machine learning (ML), data mining (DM) and intelligent data analysis (IDA). Data driven modelling approach focused in this research work is based on machine learning based techniques. Machine learning theory is about building a model capable of learning to improve its own performance based on its previous experience. It uses pattern recognition and statistical inference to come up with a conclusion. The study in 25 discussed approaches using machine learning to make engine modelling process faster. The results showed that data driven models demonstrated better performance than physical models by its ability to capture nonlinear trends and pattern in the data. It is recommended in a scenarios where data is incomplete to build a physical model. Machine learning approach has been widely
used in the literature for modelling engine by utilizing engine experimental data.

Next sections discuss on the current research work on identification of combustion events, system identification of the engine through machine learning approach and control of the engine.

### 1.2 Machine learning based approach for combustion classification

Combustion identification in ICEs can be studied by analyzing in-cylinder pressure data. In-cylinder pressure measurement with a piezoelectric sensor mounted on the engines, is a conventional approach for off-line analysis of combustion process.

Various combustion metrics listed in Figure 1.2 can be analysed with machine learning techniques. With machine learning algorithm, misfire event identification was done by analysing the vibration pattern associated with particular cylinder in [26]. Identification of misfire events is closely tied to identification of patterns in combustion trace, which corresponds to misfire. Linear model tree algorithm was suggested to have better classification accuracy compared to other algorithms considered in [26]. Similarly, with the vibration measurement data from the engine, classifier accuracy was compared in [27], between convention feature extraction approach with support


Figure 1.2: Combustion metrics
vector machine (SVM) and deep learning convolutional neural network (CNN) without feature extraction. Deep learning approach was observed to perform better better compared to CNN with feature extraction and SVM for multi-class misfire detection.

In [28] have listed deep learning techniques with 2-D convolutional neural network, which could extract features to identify combustion instability. This could help in identifying and preventing the occurrence of poor combustion. Discussed in [29] is a novel method of building adopted artificial neural network(ANN) model from the empirical model. The developed model showed an accuracy of $85 \%$ as mean prediction accuracy. In [30], developed a misfire detection technique for an HCCI engine. Misfire was created by cutting the fuel supply, varying air to fuel ratio (AFR) and low air intake temperature. Engine powered with ethanol by using experimental data to
model ANN for misfire detection. ANN is modelled using the in-cylinder pressure value modeled using regression equation using maximum heat release rate (MHRR) at crank angles, $0,5,10,15$ and 20 aTDC. The ANN model developed with four hidden layers using in-cylinder pressure was able to detect the misfire with $100 \%$ accuracy.

In [31, a misfire identification technique for HCCI engine fueled with ethanol was carried out. Skewness and kurtosis of in cylinder pressure and crankshaft rotational speed were analysed. Result showed that on all misfire cycles, engine speed showed negative skew values. In [32], to improve the operating range of the HCCI engine, the authors studied cyclic variation of CA50 near misfire region to extend the range of operation. Return map and symbol sequence approach was used to statistically model the system and a joint prediction of CA50 one cycle ahead was conducted. The residual between predicted and actual data was in the $95 \%$ confidence interval and hence model prediction is acceptable.

In [33], the authors discussed about limited operating range of HCCI due to higher pressure rise rate and ringing. Ringing intensity (RI) increased with lower burn duration and advanced CA50. ANN model was built with in-cylinder pressure values at 5,10 and 15 CAD aTDC and Pmax to predict RI with prediction error of $4.2 \%$. In [34, intense ringing in an HCCI engine, which limits the range of operation was studied. To this end a ANN based approach was designed to predict the combustion
noise level to identify ringing regions. The model was able to predict with an error of less than $0.5 \%$ from the actual combustion noise level.

Extreme learning machine (ELM) are feed forward neural networks for classification [35] with extremely fast learning speed. So, was named as "Extreme learning machine". ELM is single hidden layer feedforward neural networks which randomly chooses hidden nodes and analytically determines the output weight. In theory [35], algorithm provides good generalization performance at extremely fast learning speed. ELM was used to model a bio-diesel engine performance. In [36], optimisation of engine was carried out using logarithmic transformation to reduce the impact of data scarcity in real time. The result was concluded based on the comparison of engine model between two optimization techniques, simulated annealing (SA) and particle swam optimisation (PSO).

Engine ignition pattern analysis is one of the diagnostic method for gasoline engines. In [37], wavelet packet transform was used to extract features from the ignition pattern. Based on identified features, then a multi-class least square support vector machine (MCLS-SVM) was used to identify fault related to malfunctioning parts of engine. Diagnosis accuracy of MCLS-SVM was higher than the typical MLP (multi layer perceptron) approach in the experimental results.

In [38], studied about fault diagnosis for process monitoring in industrial environment. In process monitoring, unsupervised learning approach on multi dimensional
data for clustering result was slow due to the curse of dimensionality and result in unrelated features existence. Dimensionality reduction was carried out using Principal Component Analysis (PCA). PCA is an approach for feature extraction by creation of new independent variable which is a combination of the old variables. Engine output parameters are dependent on many input variables. PCA can help reduce dimensionality of the data by generating new independent variables,also known as principal axes. Multi-linear extensions of PCA was observed to be effective in reducing the dimensionality to result in better separation of clusters. Also, the study in the reference article [39] show that vibration measurement from the engine was used to identify fault on engine related to defective lash adjuster and chain tensioner. Based on the severity of measured vibration, it could identify and classify fault into specific fault domain. The smooth variable structure filter (SVSF) algorithm outperformed in comparison with other approaches and showed a success rate of $97 \%$ in the detecting the faults.

With the study on reference articles, its evident that a lot of research has been done in order to identify misfire and fault diagnostics on engine, but significant study hasn't happened in terms of characterizing the combustion traces to identify heat release patterns. This in turn opens up a large scope of work in terms of classification of combustion traces on a multi-mode engine. Once classification of combustion traces is done, an effective method of integration of this information into real-time system identification is done and the combustion control for the engine will be required.

Thus, in the subsequent section prior studies in terms of system identification and control of engine combustion are reviewed.

### 1.3 Machine learning approaches for ICE combustion modeling and control

Multiple machine learning techniques have been explored to build engine models that are compatible for ICE controls. In [40], HCCI engine powered with butanol and ethanol was studied. Engine powered with butanol, n-heptane and ethanol was modelled with feed forward neural network (FFNN) and radial basis function neural network (RBFNN). Multiple-input and multiple-output (MIMO) neural network developed showed that both approaches were able to predict the engine performance metrics including indicated mean effective pressure (IMEP), thermal efficiency, incylinder pressure, net total heat released, nitrogen oxides $\left(\mathrm{NO}_{x}\right)$, carbon monoxide (CO), and total hydrocarbon (THC) concentrations with error less than $4 \%$. With the fact that FFNN involved less complex equation in comparison to RBFNN, which involved complex equations but needed less training time.

In 41, a high accuracy models with low computational effort for HCCI engine was built. The authors in reference [41] developed a gray box modelling technique that
used a combination of physical model with artificial neural network (ANN) feed forward model for the prediction of CA50, IMEP and exhaust gas temperature (Texh). Developed model predicted CA50, IMEP and Texh with an accuracy of less than 1 crank angle degree, 0.2 bar and $6^{\circ} \mathrm{C}$, respectively. In [42], prediction of engine rotational dynamics was done using a gray box model that consisted of a physical mode and a black box ANN. The authors studied 2 gray box architectures: series and parallel. Gray box model with series structure was identified and found to perform better than the parallel approach. In [43], discussed that HCCI engines could be brought to practical use if the drawbacks on high THC and CO is reduced by controlling $\mathrm{CA}_{50}$ for lower emissions and higher thermal efficiency. Gray box modeling as a combination of both physical and feed forward artificial neural network (FFANN). Model was build for two different HCCI engines. The model could predict combustion phasing, load, exhaust gas temperature and emissions (THC, $\mathrm{CO}, \mathrm{NO}_{x}$ ) with the validation on steady state and transient test prediction error resulted in less than $10 \%$.

In 44], optimisation of bio diesel engine engine model was built using kernel based ELM technique. By use of cuckoo search (CS), optimal bio-diesel ratio with minimization cost function for both fuel cost and emissions. The results were compared with LS-SVM. It was concluded that K-ELM achieves comparable result and optimisation with CS results in reliable prediction and optimisation. In [36], optimisation of bio-diesel engine with less emissions was evaluated with ELM, least-squares support
vector machine (LS-SVM) and RBFNN approach to model the engine. It was evaluated with two optimization methods, namely simulated annealing (SA) and particle swarm optimization (PSO) as optimisation function to result in optimal bio-diesel ratio. ELM with logarithmic transformation model was observed to perform faster and better. PSO as an optimisation algorithm performed better with cost function on fuel cost and lower emissions.

In [45], evaluated the prediction capability of the ANN model built for an engine operated with exhaust gas re-circulation (EGR) strategies. It was built with $70 \%$ experimental data, $15 \%$ for cross validation to avoid overfitting and other $15 \%$ for testing the model accuracy in prediction. With the inputs- load, rail pressure, EGR\% and fuel, model could predict the performance and emission parameters with high correlation, it was also able to map the trade off between PM-NO $x_{x}$-brake specific fuel consumption (BSFC) under operation with EGR. In [46, authors studied that engine operating on transient condition based on steady state tuned tables may not result in optimal performance. To mitigate this issue, authors built a real time system capable of perceiving driver, driving pattern and optimize performance by using Markov decision process. It resulted resulted in overall $9.3 \%$ improvement in fuel economy compared to baseline calibration by the use of decentralised learning to optimize fuel economy and emission by varying variable geometry turbocharger (VGT) position and injection timing, .

In [47], a control oriented model was built to control combustion timing, engine load and combustion efficiency for an HCCI engine. Detailed physics based model was developed including effect of residual gases and rate of fueling on model out put parameters (combustion timing, engine load and combustion efficiency). Model could perform with acceptable accuracy in both steady state and transient validation. [48] is based on combustion timing and load control of HCCI engine. Nonlinear control oriented model (NCOM) developed was linearized and integral discrete time sliding mode controller (IDSMC) was built to control load and combustion timing. Its performance was compared to manually tuned proportional- integral (PI) controller. IDSMC showed better tracking efficiency and also responded well to the introduction of disturbance in equivalence ratio and intake temperature. In 49], combustion analysis comparison of performance between DI engine and bio-diesel with waste vegetable oil was compared on similar operating conditions. ANN model was built to model the engine characteristics operated with waste vegetable oil from the experimental results and IDSMC performed better in tracking efficiency.

RCCI promising for its high thermal efficiency but comes with a need of high accuracy control oriented model and control technique. Approach of data driven linear parameter varying model, built based on support vector machine was developed in [50]. The model could be built fast and model could track $\mathrm{CA}_{50}$ for change in load with less than 1 CAD when built with a model predictive controller (MPC). The linear parameter varying (LPV) model is built as a function of fuel quantity. In 51],
model based control was developed and trajectory optimised for lower emissions was fed as reference. The computational requirement of the gray box model was 1 ms in a 2.67 GHz processor. Controller ability to track optimum trajectory for IMEP and CA50 was tested and verified. In [52], automated the proportional-integral-derivative (PID) system tuning by using simulator CARLA, an open source simulator . Model was evaluated for performance on the governing the engine idle speed. The method performed better than typical tuning process of the PID parameters and better results both in simulation and in practice.

LPV modelling approximates the non linear system with a state space structure suitable to build linear controller on it. In [6, 50], method of developing LPV model based on support vector machine is proposed. The study in [50] demonstrated system identification capability using the above technique for control of combustion phasing of the RCCI engine. In addition to [50, capability of this technique for modelling maximum pressure rise rate (MPRR) is discussed in [5]. The limitation of this approach is only 2 manipulated variables start of injection (SOI) and fuel quantity were available to achieve control on combustion phasing and IMEP.

### 1.4 Shortcomings of literature

The review in Section 1.2 and 1.3, showed prior studies into extracting features of combustion parameters from the in-cylinder pressure traces, vibration measurements or identifying engine combustion related fault, but the area of identifying the heat release rate patterns from engine data for the control of a multi-mode LTC engine remains under explored. Identifying pattern of heat release rate in combustion events will be critical to optimally control operation of multi-mode LTC engines.

The review in Section 1.3, discussed various machine learning and deep learning approaches in practice for ICE modelling and control. However there is no integrated machine learning and control method based on engine heat release shapes for LTC engines. In particular one promising area is the application of machine learning based LPV models for MPC control of LTC engines based in identifying varying heat release shapes.

### 1.5 Scope of Research

Based on the shortcomings listed in Section 1.4, the scope of the thesis is defined as: Machine learning approach is suggested for building accurate model of IC engine.

Numerical simulation capability of the technique will help to improve modelling capability. A real time predictive control on a cycle to cycle basis, to optimize combustion mixture formation and improve stability of combustion.

Scope of the research is listed as :-
$\dagger$ Study machine learning algorithm and develop an algorithm to classify the heat release rate patterns in an LTC engine. This would form the basis in identification of heat release rate patterns which can be used for engine combustion control. Model classification with machine learning technique would also help assess if the classification problem could be solved with higher prediction accuracy.
$\dagger$ Analyze experimental data from an LTC engine to determine between heat release pattern and engine control variables. The results from this study will be used to determine optimum scheduling parameters for engine controls.
$\dagger$ Create a machine learning based control oriented model to predict $\mathrm{CA}_{50}$, IMEP and MPRR for an LTC engine
$\dagger$ Design and verify optimal predictive combustion controller for a LTC engine to adjust engine load and combustion phasing, while meeting MPRR and actuators constraints.

### 1.6 Organization of Thesis

Experimental setup of engine is discussed in Chapter 2. Machine learning approach used for classification, results and its accuracy are discussed in Chapter 3. Identification of combustion classifier, discussed in Chapter 4 and building of LPV- SVM model as a function of it as scheduling parameter is discussed in Chapter 5. Building a MPC control structure to control combustion phasing, IMEP with MPRR limitation is covered in Chapter 6. Conclusion and future work are listed in Chapter 7, followed by sections of appendix including data files and other relevant details of the thesis.


Figure 1.3: Thesis Organization

## Chapter 2

## Experimental Setup

Engine experimental data is required in order to study and classify LTC heat release shapes and identify appropriate schedulign parameters for LTC engine control. Specifications of the engine, test cell layout and data acquisition are explained in this chapter.

### 2.1 Engine Specification

This thesis uses a 2 Liter GM Ecotec engine with the specification listed in Table 2.1. The engine is located at Michigan tech's Advanced Propulsion Systems Research Center (APSRC).

Table 2.1
Engine Specifications

| Make | General Motors |
| :--- | :--- |
| Model | Ecotec 2.0L Turbocharged |
| Engine Type | 4 stroke,Gasoline |
| Fuel System | Direct Injection |
| Number of Cylinders | 4 Cylinders |
| Displaced Volume | $1998[\mathrm{cc}]$ |
| Bore | $86[\mathrm{~mm}]$ |
| Stroke | $86[\mathrm{~mm}]$ |
| Compression Ratio | $9.2: 1$ |
| Max Engine Power | 164 @ $5300[\mathrm{~kW}$ @rpm] |
| Max Engine Torque | $353 @ 2400[\mathrm{Nm}$ @rpm] |
| Firing Order | $1-3-4-2$ |
| IVO | $25.5 /-24.5\left[{ }^{\circ} \mathrm{CAD} \mathrm{bTDC}\right]$ |
| IVC | $2 /-48\left[{ }^{\circ} \mathrm{CAD}\right.$ bBDC] |
| EVO | $36 /-14\left[{ }^{\circ} \mathrm{CAD} \mathrm{bBDC}\right]$ |
| EVC | $22 /-28\left[{ }^{\circ} \mathrm{CAD} \mathrm{bTDC}\right]$ |
| Valve lift | $10.3[\mathrm{~mm}]$ |

### 2.1.1 Engine Modifications

The engine is modified to demonstrate low temperature combustion concepts Figure 2.1. To this end, a dual fuel injection system is added to the engine as part of the modifications. Engine is modified to have both iso-octane port fuel injection (PFI) system and a n-heptane direct injection (DI) system. In the data used for this research work, both fuels are used to vary the reactivity of the charge inside the cylinder. Injection system calibration was carried out and documented in [2, 3].

The engine setup also has a heater upstream of air intake, in order to vary intake air temperature.


Figure 2.1: LTC engine setup in this work [4]

Iso-octane is the low reactivity fuel and n-heptane is the high reactivity fuel. Properties of these two fuels are summarized in Table 2.2.

Table 2.2
Fuel Specifications

| Property | Iso-Octane | N-Heptane |
| :--- | :--- | :--- |
| Higher Heating Value $[\mathrm{MJ} / \mathrm{kg}]$ | 47.77 | 48.07 |
| Lower Heating Value $[\mathrm{MJ} / \mathrm{kg}]$ | 44.30 | 44.56 |
| Density $\left[\mathrm{kg} / \mathrm{m}^{3}\right]$ | 693.8 | 686.6 |
| Octane Number [-] | 100 | 0 |

### 2.2 Data Acquisition

Data from the engine is captured using 3 subsystems including, National Instruments Labview, dSPACE and ACAP combustion analyser. The NI Labview gathered temperature data from the engine. It also sends control commands to dynamometer and the air intake temperature. dSPACE helped in sending control signals to various actuators on the engine. Injectors, spark plug and EGR valve control signals are also provided by dSPACE. Calculations are preformed in Field Programmable Gate Array(FPGA) as shown in [3] and communicated to RapidPro through a CAN. dSpace also has a slave controller named micro auto box (MABX). Both RapidPro and MABX together assist to control the engine.


Figure 2.2: LTC Engine Data Acquisition from reference [5]

ACAP is used to collect in-cylinder pressure traces from the piezo electric transducers115A04 transducers. The crank angle reference is gathered by encoder mounted on the crankshaft of the engine.

### 2.3 Test data and Analysis

Engine data analysed in this research work was collected by varying independent parameters like engine speed, fuel quantity, pre-mixed ratio, start of injection of nheptane, intake manifold temperature and intake manifold pressure. Pre-mixed ratio $(\mathrm{PR})$ is defined as the ratio of the energy of the low reactivity fuel to the energy of the total fuel. The low reactivity fuel in current experiment is iso-octane and the high reactivity fuel is n-heptane.

Table 2.3 summarizes independent parameters varied in the test. Parameter of interest is in-cylinder pressure trace as a function of engine crank angle. At every steady state operating point 100 cycles of data is collected.

Table 2.3
Test conditions of engine data

| Engine Speed (rpm) | Fuel Quantity (mg/st) | Pre- mixed ratio (\%) | $\begin{gathered} \text { SOI } \\ (\mathrm{bTDC}) \end{gathered}$ | Intake manifold temperature $\left({ }^{\circ} \mathrm{C}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| 800 | 10-30 | $\begin{aligned} & 20 \\ & 40 \\ & 60 \\ & \hline \end{aligned}$ | 15-40 | 40-110 |
| 1000 | 10-40 | $\begin{aligned} & 20 \\ & 40 \\ & 60 \end{aligned}$ | 20-100 | 40-110 |
| 1100 | 30 | 60 | 60-80 | 70-80 |
| 1200 | 10-40 | $\begin{aligned} & 20 \\ & 40 \\ & 60 \end{aligned}$ | 28-80 | 40-110 |
| 1400 | 10-40 | $\begin{aligned} & 20 \\ & 40 \\ & 60 \\ & \hline \end{aligned}$ | 33-60 | 40-110 |
| 1600 | 20-40 | $\begin{aligned} & 20 \\ & 40 \\ & 60 \\ & \hline \end{aligned}$ | 40-60 | 40-110 |
| 1800 | 20-40 | $\begin{aligned} & 20 \\ & 40 \\ & 60 \\ & \hline \end{aligned}$ | 47-70 | 60-110 |
| 1900 | 20 | $\begin{aligned} & 20 \\ & 40 \end{aligned}$ | 53-60 | 80-90 |
| 2000 | 20-30 | $\begin{aligned} & 20 \\ & 40 \\ & 60 \end{aligned}$ | 53-80 | 80-100 |
| 2100 | 20-30 | $\begin{aligned} & 20 \\ & 40 \end{aligned}$ | 53-70 | 80-100 |
| 2300 | 20 | 20 | 65 | 80 |

### 2.3.1 Uncertainty Analysis

Level of confidence in the results comes based on the amount of uncertainty associated with the measurement of data. Uncertainty arises in measured data due to numerous
factors like instrumentation and operating conditions. Uncertainty associated with various engine parameters are documented in Table 2.4 from [2]. The uncertainties

Table 2.4
Table of measured parameters and associated uncertainties

| Parameter[Units] | Value | Uncertainty $(+/-)$ |
| :--- | :--- | :--- |
| Bore $[\mathrm{m}]$ | 0.086 | 0.001 |
| Stroke $[\mathrm{m}]$ | 0.086 | 0.001 |
| Cylinder Pressure $[\mathrm{kPa}]$ | $95-4000$ | $1 \%$ |
| Crank Angle $[\mathrm{CAD}]$ | $0-720$ | 1 |
| $\mathrm{~T}_{\text {in }}\left[{ }^{\circ} \mathrm{C}\right]$ | $4-100$ | $2 \%$ |
| $\mathrm{P}_{\text {in }}[\mathrm{kPa}]$ | $95-105$ | $0.5 \%$ |
| $\mathrm{~m}_{\text {fuel }}[\mathrm{mg} / \mathrm{st}]$ | $11.0-40.0$ | $0.1 \%$ |
| $\mathrm{~N}[\mathrm{rpm}]$ | $800-2300$ | 10 |

of the derived parameters are tabulated in Table 2.5 from [2]
Table 2.5
Derived parameters and associated uncertainties

| Parameter[Units] | Value $+/$ - Uncertainty |
| :--- | :--- |
| CA_5_0 [CAD aTDC] | $-1+/-1$ |
| IMEP [kPa] | $540.7+/-28.1$ |
| MPRR [bar/CAD] | $12+/-0.6$ |

### 2.4 Heat release rate calculation

In-cylinder pressure trace is collected on engine. The pressure transducers are capable of measuring in range of $0-35000 \mathrm{psi}$ and have sensitivity of $1.442 \mathrm{pC} / \mathrm{psi}$. The pressure
transducers measure relative pressure and process of referencing it to intake manifold pressure is called pegging. Pressure signal is obtained as a function of crank angle at an interval of 1 crank angle degree (CAD). In pressure trace, the noise associated with it, has to be cleared off [53] before analysis for heat release rate. Based on the work carried out by [3], a Butterworth low pass filter with a cut off frequency of 0.5 and order 1 was identified to filter pressure trace.

Further calculation of heat release rate is carried out by using first law of thermodynamics and is given by Eq. (2.1).

$$
\begin{equation*}
\frac{d Q}{d \theta}=\frac{\gamma}{\gamma-1} \cdot P \frac{d V}{d \theta}+\frac{1}{\gamma-1} V \frac{d P}{d \theta}+\frac{d Q_{h t}}{d \theta}+\frac{d Q_{\text {crevice }}}{d \theta} \tag{2.1}
\end{equation*}
$$

Where $\gamma$ is a polytropic compression coefficient calculated from the compression region. Instantaneous volume ( $V$ ) at each crank angle is calculated by Eq. 2.2). $\mathrm{dQ}_{h t}$ refers to heat loss to the walls. $d Q_{\text {crevice }}$ refers to crevice loss and is neglected.

$$
\begin{equation*}
V(\theta)=V_{c}+\frac{\pi \cdot B^{2}}{4} \cdot P\left(l+a-a \cos \theta-\sqrt{l^{2}-\left(a \sin \theta^{2}\right)}\right. \tag{2.2}
\end{equation*}
$$

Where $B$ is the diameter of the bore, $l$ is length of the connecting rod, $V_{c}$ is the clearance volume and $a$ is the crank radius.

The phenomenon for the heat loss to the surrounding is attributed to the convective
heat transfer, represented by Eq. 2.3.).

$$
\begin{equation*}
\frac{d Q_{h t}}{d \theta}=h_{c}\left(T(\theta)-T_{w}\right) \tag{2.3}
\end{equation*}
$$

Where $T$ is the instantaneous temperature of charge inside the cylinder and $T_{w}$ is the temperature of the cylinder wall. $T$ is calculated by using the the ideal gas equation. $h_{c}$, heat transfer coefficient is calculated by using the Woshini model which was later modified by Chang [54] has been used in LTC combustion regimes.

With heat release rate calculated for each combustion trace, in Chapter 3, classification of heat release type is carried out. Classification of heat release rate traces, helps interpret and optimise combustion efficiency. Rule based and machine learning based approaches are evaluated to identify the best approach to effectively classify heat release trace.

## Chapter 3

## Classification of heat release rate

## traces

Machine learning provides a wide range of algorithms for classification. With reference to classification, a multi-class classification problem is being addressed here as the heat release rate traces are intended to be grouped in three predominant combustion phases and the fourth and fifth bins are accounted for the transition. On a classification problem the main goal addressed is that the model should be capable of predicting appropriate class for the given heat release trace. Classification model, is trained to identify heat release rate traces by using either supervised or unsupervised learning techniques of machine learning. Clusters of heat release types of a multi-dimensional engine data is reduced to two dimensional space to identify critical
parameter for classification. To start with classification algorithm problem, below are the terminologies used in machine learning for defining the classification model:
$\dagger$ Feature, refer to measurable/ identifiable parameter of input.
$\dagger$ Classifier is the learning algorithm that assigns the class to the data based on its learning of the model from the training data. Classifier and Classification model are used interchangeably in most of the cases.

Below is the procedure followed, for building a classification model:
$\dagger$ Algorithm for classification is identified
$\dagger$ Training of the classifier for the given input (X) against the label (Y)
$\dagger$ Predict label $(\mathrm{Y})$ for the input ( X ), from test data using trained model
$\dagger$ Evaluate prediction accuracy

The data has to be labelled for classification using supervised learning approach, where X refers to the heat release rate trace and Y refers to the labels of classification. To avoid the impact of bias introduced by the use of threshold, unsupervised learning approach is also evaluated by using k-means approach, in the later sections of this chapter.

### 3.1 Rule based Classification

Rule based classification of heat release rate trace is carried out based on the subject knowledge. The classified data form basis for developing a supervised machine learning model subsequently. In order to classify the data, the crank angle at the start and end of main heat release are identified for each of the HRR traces manually and then logged into the data files.


Figure 3.1: Heat release rate trace with Start and End of Main HR depicted

From the crank angle associated with start and end of main heat release by using below relation, the percentage of heat release which happens before main is calculated
using Eq. (3.1)) termed as Fraction of Early Heat Release.

Fraction of Early Heat Release $=\frac{\text { Cumulative HR from the SOI to Start of main }}{\text { Energy in the fuel quantity injected }}$

The percentage of heat release that happens after the main heat release until $\mathrm{CA}_{90}$ is termed as Fraction of Late Heat Release and, is calculated by :

Fraction of Late Heat release $=\frac{\text { Cumulative HR from the end of main } \mathrm{HR} \text { to } \mathrm{CA}_{90}}{\text { Energy in the fuel quantity injected }}$

The HRR traces are classified based on the fraction of early and late heat release value. Based on the decision tree in Figure 3.2, the complete classification is arrived. The threshold value for classification to denote different types of heat release rate is obtained by analysis of the engine experimental data.


Figure 3.2: Flowchart of Classification Algorithm

Summarized are few traces from each of the classification type in Figure 3.3, depicting 3 classification bins. Between Type 1, Type 2 and Type 3, separate classification Type- 4 and Type- 5 are identified, to represent the combustion phase transition between the types. Filtered and normalised traces grouped in specific bins are depicted in Figure 3.3 .


Figure 3.3: Sample heat release rate traces for three main HRR patterns
Each classified type of $H R R$, group traces which show a unique pattern of combustion.
$\dagger$ Type 1: Refers to a type of combustion observed in the HRR where it neither has a significant premixed combustion nor a diffusion combustion. It is similar to the combustion pattern observed in HCCI.
$\dagger$ Type 2 : Refers to a type of combustion with HRR where it has a significant premixed combustion. It is similar to PCCI type of combustion pattern.
$\dagger$ Type 3: Refers to a type of combustion with HRR where it has a significant diffusion combustion. It is similar to combustion HRR pattern observed in RCCI.

Summary of the count of HRR traces identified into each type is listed in Table 3.1
Table 3.1
Summary of the classified HRR traces

| Type of HRR traces | Count of traces |
| :---: | :---: |
| Type 1 | 131 |
| Type 2 | 71 |
| Type 3 | 373 |

Distribution of $\operatorname{COV}_{\text {IMEP }}$ across the data points in Figure 3.4 is analyzed before evaluating other combustion characteristics.


Figure 3.4: Distribution of $\mathrm{COV}_{I M E P}$

Majority of the traces are below the limit of $5 \%$ as shown in Table 3.2 and Figure 3.4.

Table 3.2
Table of $\mathrm{COV}_{\text {IMEP }}$ distribution

|  | Median <br> $\mathbf{\%}$ | Mean <br> $\mathbf{\%}$ | Standard deviation <br> $\mathbf{\%}$ | Skewness <br> $(-)$ | Kurtosis <br> $(-)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Type 1 | 2.24 | 2.71 | 1.74 | 1.75 | 6.10 |
| Type 2 | 4.19 | 5.36 | 3.09 | 1.8 | 7.13 |
| Type 3 | 3.94 | 4.63 | 2.50 | 1.42 | 6.48 |

### 3.1.1 Characteristics of combustion type

Characteristics of classified combustion HRR traces are evaluated by looking into multiple combustion parameters and its statistical distribution across the traces grouped into each type.

### 3.1.1.1 Peak Cylinder Pressure

In Figure 3.5, the spread of peak cylinder pressure across 3 types of heat release is plotted and in Table 3.3 statistical parameters of the each of the distribution are summarized.

Table 3.3
Table of peak cylinder pressure distribution

|  | Median <br> $\mathbf{k P a}$ | Mean <br> $\mathbf{k P a}$ | Standard deviation <br> $\mathbf{k P a}$ | Skewness <br> $(-)$ | Kurtosis <br> $(-)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Type 1 | 4329 | 4204 | 714.2 | -0.72 | 2.73 |
| Type 2 | 3924 | 3998 | 618.2 | 0.22 | 2.12 |
| Type 3 | 3530 | 3561 | 417.7 | 0.31 | 2.73 |

Peak cylinder pressure is observed the highest in Type 1, followed by Type 2 and least


Figure 3.5: Peak cylinder pressure distribution
in Type 3. It is the highest in Type 1, as the most of the fuel heat release happens in the main heat release and least in Type 3 as significant amount of fuel burns after the end of main heat release. Higher peak cylinder pressure is predominantly caused by early combustion which can result in excessive noise and damage to the engine. Type 1 depicts traces with rapid heat release rate which is due to the rapid pressure rise of the combustion mixture. A HRR trace of Type 1 at higher loads can potentially lead to higher peak cylinder pressure. Since, Type2 and Type 3 depict controlled heat release spread over a wider crank angle window, it results in lower peak cylinder pressures.

### 3.1.1.2 Maximum pressure rise rate

In Figure 3.6, the spread of maximum pressure rise rate across 3 types of heat release is plotted and in Table 3.4 statistical parameters of the each of the distribution are summarized.

Table 3.4
Table of maximum pressure rise rate distribution

|  | Median <br> bar/CAD | Mean <br> bar/CAD | Standard deviation <br> bar/CAD | Skewness <br> $(-)$ | Kurtosis <br> $(-)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Type 1 | 5.77 | 5.65 | 2.47 | 27 | 2.44 |
| Type 2 | 4.34 | 5.23 | 2.70 | 0.72 | 2.42 |
| Type 3 | 3.93 | 4.05 | 1.14 | 0.53 | 3.11 |





Figure 3.6: Maximum pressure rise rate distribution

Maximum pressure rise rate is observed the highest in Type 1 , followed by Type 2 and least in Type 3. Pressure rise rate is significantly governed by mixture reactivity at the start of combustion. It is the highest in Type 1 as it depicts combustion kinetics on a homogeneous mixture resulting in rapid heat release rate and pressure rise rate.

In Type 2 and Type 3, as the flame front propagates, due to in-homogeneity of the mixture a combustion pattern resulting in significant early and late heat release is observed.

### 3.1.1.3 $\mathrm{CA}_{10}$

In Figure 3.7, the spread of crank angle at 10 percentage of total heat released in an engine cycle across 3 types of heat release is plotted and in Table 3.5 statistical parameters of the each of the distribution are summarized.

Table 3.5
Table of $\mathrm{CA}_{10}$ distribution

|  | Median <br> CAD | Mean <br> CAD | Standard deviation <br> CAD | Skewness <br> $(-)$ | Kurtosis <br> $(-)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Type 1 | 5 | 4.58 | 5.58 | -0.07 | 2.60 |
| Type 2 | -1 | -1.88 | 5.66 | -0.50 | 2.68 |
| Type 3 | 4 | 4.03 | 2.00 | -1.27 | 8.39 |



Figure 3.7: $\mathrm{CA}_{10}$ distribution
$\mathrm{CA}_{10}$ is observed earliest in Type 2, followed by Type 1 and Type 3. It can be justified from the HRR trace of Type 2 from Figure 3.3 due to the significant heat release before the main heat release, it has the earliest $\mathrm{CA}_{10} . \mathrm{CA}_{10}$ is significantly affected by the ignition delay of the in-cylinder fuel and charge. All these three types of HRR data points had iso-octane injected in the intake port and n- heptane direct injected in cylinder. Based on the homogeneity of the mixture, the ignition delay varied. HRR with least ignition delay resulted in Type 2, followed by Type 1 and Type 3.

### 3.1.1.4 $\mathrm{CA}_{90}$

In Figure 3.8, the spread of crank angle at 90 percentage of total heat released in an engine cycle across 3 types of heat release is plotted and Table 3.6 statistical parameters of the each of the distribution are summarized.

Table 3.6
Table of $\mathrm{CA}_{90}$ distribution

|  | Median <br> CAD | Mean <br> CAD | Standard deviation <br> CAD | Skewness <br> $(-)$ | Kurtosis <br> $(-)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Type 1 | 34 | 32.41 | 11.53 | -0.76 | 3.28 |
| Type 2 | 29 | 22.4 | 17.86 | -0.18 | 1.38 |
| Type 3 | 48 | 46.59 | 6.07 | -0.42 | 3.11 |

$\mathrm{CA}_{90}$ is the earliest with Type 2, followed by Type 1 and the last with Type 3. It is directly connected to the the pattern of heat release type and since type 3 has


Figure 3.8: $\mathrm{CA}_{90}$ distribution
significant late heat release, hence the value of $\mathrm{CA}_{90}$ is significantly higher than other types. Homogeneity and ignition delay of the in-cylinder mixture plays a critical role in $\mathrm{CA}_{90}$. Combination of these two parameters result in Type 2 having the least $\mathrm{CA}_{90}$ and with Type 3 which predominantly showed diffusion heat release pattern having the highest $\mathrm{CA}_{90}$.

### 3.1.1.5 Maximum in-cylinder temperature

In Figure 3.9, the spread of maximum in-cylinder temperature across 3 types of heat release is plotted and Table 3.7 statistical parameters of the each of the distribution are summarized.

Higher in-cylinder temperature is observed in Type 1 as the rate of fuel burnt through the main heat release is highest. It is followed by Type 2 and Type 3. Rapid pressure

Table 3.7
Table of Maximum in-cylinder temperature distribution

|  | Median <br> $\mathbf{K}$ | Mean <br> $\mathbf{K}$ | Standard deviation <br> $\mathbf{K}$ | Skewness <br> $(-)$ | Kurtosis <br> $(-)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Type 1 | 1812 | 1780 | 334 | -0.35 | 2.60 |
| Type 2 | 1494 | 1508 | 225 | 0.09 | 2.78 |
| Type 3 | 1508 | 1536 | 241 | 0.36 | 2.95 |



Figure 3.9: Maximum in-cylinder temperature distribution
rise observed in the Type 1 HRR pattern resulted in higher in-cylinder temperature observed. In case of Type 2 and Type 3, they depict similar range of in-cylinder temperature as both of these HRR patterns have comparatively slower heat release rates and wider burn duration.

### 3.1.1.6 In-cylinder temperature at Start of main heat release

In Figure 3.10, the spread of in-cylinder temperature at the start of main heat release across 3 types of heat release is plotted and Table 3.8 statistical parameters of the of
the distribution are summarized.
Table 3.8
Table of in-cylinder temperature distribution at start of main heat release

|  | Median <br> $\mathbf{K}$ | Mean <br> $\mathbf{K}$ | Standard deviation <br> $\mathbf{K}$ | Skewness <br> $(-)$ | Kurtosis <br> $(-)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Type 1 | 703 | 702 | 62.8 | -0.07 | 2.74 |
| Type 2 | 741 | 725 | 59.7 | -0.06 | 2.39 |
| Type 3 | 698 | 712 | 91.5 | 2.67 | 21.99 |



Figure 3.10: In-cylinder temperature at Start of Main distribution

With Type 2 having early heat release, it is the highest while comparing in-cylinder temperatures across start of main, followed by Type 1 and Type 3 together, as both of them don't depict any significant early heat release. In case of Type 1 , the in-cylinder temperature arrived at start of main is due to the impact of compression process on the mixture. Similar, is the case with Type 3 pattern as well. Hence both of them show lower in-cylinder temperature at start of main. But, in case of Type 2, some of portion of the combustible mixture is already burnt, resulting in higher in-cylinder temperature at the start of main heat release.

### 3.1.1.7 In-cylinder temperature at End of main heat release

In Figure 3.11, the spread of in-cylinder temperature at the end of main heat release across 3 types of heat release is plotted and Table 3.9 statistical parameters of the of the distribution are summarized.

Table 3.9
Table of in-cylinder temperature distribution at end of main heat release

|  | Median <br> $\mathbf{K}$ | Mean <br> $\mathbf{K}$ | Standard deviation <br> $\mathbf{K}$ | Skewness <br> $(-)$ | Kurtosis <br> $(-)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Type 1 | 1781 | 1758 | 323 | -0.32 | 2.62 |
| Type 2 | 1478 | 1495 | 220 | 0.04 | 2.55 |
| Type 3 | 1447 | 1448 | 189 | 0.33 | 3.30 |



Figure 3.11: In-cylinder temperature at end of Main distribution

With Type 1, most of the fuel is burnt in the main heat release, which results in it being the highest of all 3 types while comparing in-cylinder temperatures across end of main. It is followed by Type 2 and Type 3 in close range.At the end of main heat
release, the complete mixture has undergone a constant volume heat release over a smaller burn duration in Type 1. It has resulted in higher in-cylinder temperature at the end of main heat release. Even in case of Type 2, most of the fuel is burnt by end of main heat release, but since the burn duration is wide the heat losses associated resulted in lower in-cylinder temperature. In Type $3, \mathrm{CA}_{90}$ values also indicate that comparatively less percentage of fuel is burnt by end of main heat release. Hence, it also resulted in lower in-cylinder temperature.

### 3.1.1.8 Exhaust gas temperature

As Type 3 traces have significant late heat release and lower heat loss to coolant, the exhaust gas temperature of these traces will be the highest in comparison with the other two types. It is followed by Type 1 and Type 2 as neither of them have higher late heat release percentage.

### 3.1.1.9 Engine out emissions

Engine exhaust emission data was not available to compare the three combustion types in this thesis. Here, the expected emission trend is explained by looking at the data available from the literature. In [55] it is clearly documented that change in heat release shapes critically impact the engine out emissions. Inferences from the
articles are discussed below, where comparison is being made between HCCI, PCCI and RCCI combustion type.


Figure 3.12: Heat release types comparison [55]

The fuel type used for comparison is diesel and gasoline. The classified heat release rates in the article, $\mathrm{HCCI}, \mathrm{PCCI}$ and RCCI are similar in nature to the heat release types being targeted in the major classification HRR types 1, 2 and 3 .


Figure 3.13: HC emission 555


Figure 3.14: CO emission [55]

The data in Figure 3.13 and 3.14 , shows that unburned HC and CO emissions are
significantly higher in RCCI owing to crevice flow of low reactive gasoline fuel and lower combustion temperatures resulting in lower rate of oxidation of HC and CO .


Figure 3.15: $\mathrm{NO}_{x}$ emission 55]


Figure 3.16: Smoke (FSN) 55

The data in Figure 3.15, $\mathrm{NO}_{x}$ emissions depend strongly upon in-cylinder gas temperatures, oxygen availability and residence time available for high temperature gases. Lower $\mathrm{NO}_{x}$ is achieved due to low combustion temperature. In Figure 3.16, HCCI combustion results in near zero smoke due to higher degree of homogeneity of fuel-air mixture. The smoke emissions are higher in PCCI. This could be due to fuel wall wetting because of early direct injection.

Based on the analysis of various combustion parameters in Section 3.1.1, it was evident that the classification of heat release traces is helpful since it allows for identifying combustion types that have distinct $\mathrm{P}_{\max }, \mathrm{MPRR}, \mathrm{CA}_{10}, \mathrm{CA}_{90}$, maximum in-cylinder temperature, in-cylinder temperature at start and end of main heat release $\mathrm{T}_{\text {exh }}$ and emission characteristics. This information can be used for properly controlling engine combustion. Next, it is desired if the classification can be done automatically. To this
end, different machine learning methods were applied and investigated by evaluating their accuracy in classifications. On the classified traces, machine learning technique of supervised learning approach (Convolutional neural network and decision tree) was evaluated and the classifier prediction accuracy was compared. Unsupervised learning was also evaluated on the raw data to evaluate the classification.

### 3.2 Supervised learning - Convolutional Neural Network

In Supervised learning approach, convolutional neural network is a subset of artificial neural networks. Convolutional neural network has been proved effective for image recognition. In [56] the authors designed CNN, for identifying hand written numbers and it revolutionised application of CNN for image recognition. 1D CNN is used for identifying heat release rate traces is also built as a combination of series of layers to extract the prominent feature of the input and assign it to corresponding output label.

### 3.2.1 CNN Theory

The CNN takes the 1D vector of HRR trace and passes it across a multiple layers of convolutional, pooling and a fully connected layer to obtain output. Output here is the probability of five different classification bins which could best represent the HRR trace. First layer of 1D CNN is a convolutional layer with an activation function, in which elements from the data, as per kernel dimension is taken and multiplied with the filter weights. Its summed up as a single element in the feature vector. The kernel slides all through the input data and elements of the the feature vector are arrived. Number of filters depicts multiple combinations of weights of the filter, to extract features from input data. Each of theses combination results in a feature vector. All the feature vectors together constitute the convolutional layer. An activation function introduces non linearity in the output and helps in making decisions as depicted in the Figure 3.17. The change in dimension of input data is depicted in Figure 3.18.

Pooling is used to reduce the spatial dimension of the feature vector, in order to reduce the computation involved. Since, pooling operates individually on each of the feature vectors, though maps dimension reduce, the number of maps still remain same. In the final layer global average pooling is used, where it reduces the complete dimension of the feature vector in to a single value. A dense layer is a fully connected neural network layer where in each node on the input is connected to a node on the


Figure 3.17: Representation of CNN structure
output. A dropout layer is very similar to dense layer except that when the layer is used, the activation is set to zero for some random nodes, by using this approach over fitting is being avoided.

Training of neural network is achieved by adjusting the filter values through back propagation process. During the training process, initially the weights of the filter are randomly assigned and so the output probabilities also end up as random values in the forward pass. The error of the output layer is calculated based on Eq. (3.3), referred to as loss or total error (L). In order to have the predicted and actual label to be same, the loss has to minimum.

$$
\begin{equation*}
\text { Total error }(\mathrm{L})=\sum \frac{1}{2}(T-O)^{2} \tag{3.3}
\end{equation*}
$$

Where $T$ refers to target probability and $O$ refers to output probability. By using
back propagation method, the gradients of the error to weights in the network are adjusted to minimize error. By using gradient descent, the filter weights are adjusted in order to minimize. Weight update is carried out based on Eq. (3.4).

$$
\begin{equation*}
\mathrm{W}=W_{i}-\eta \frac{d L}{d W} \tag{3.4}
\end{equation*}
$$

Where, $W$ is the weight, $W_{i}$ is the initial weight and $\eta$ is the learning rate of the network. If the learning rate is set too high it results in large jumps and makes it difficult to reach the optimised point. The process of forward pass, followed by loss calculation and backward pass is carried out for 500 iterations predefined in the coding to get a trained model.

When the same image is fed as input into the trained model, the probability results of the predicted label would more align with the actual label. Thus, the model has learnt to process the particular heat release trace to the corresponding label. Through the process of training only the weights of the filter and connection weights get updated. The structure of the network in terms of number of filters and filter size, remains the same. The heat release rate traces are classified into bins with the rule based algorithm. For supervised learning approach part of the data is fed for training the model and rest is used to evaluate. Thus, $65 \%$ of the data is used for training and the rest $35 \%$ of the data is used for testing the model.

### 3.2.2 Application of CNN in HRR shaping

1D CNN model was built and tested using keras.It is a python package. In CNN approach for classifying the heat release rate traces, filter of length 9 with 32 features is used and the activation function used is exponential linear unit (ELU). Max pooling is used in the CNN structure built for heat release trace identification. It helps to reduce dimension of feature map in patches. The layer at end is connected completely to its earlier activation layers. Depiction of CNN with convolution and pooling layers, followed by vectored fully interconnected layer resulting in final classification is shown in Figure 3.17. The dimensions of data as it is processed through multiple layers of CNN is detailed in Figure 3.18

Layers on convolution and max pooling extract information from the image with the final dense and dropout layer leading to the classification bins by avoiding overfitting of model to training data.

### 3.2.2.1 Prediction Accuracy of CNN model

By evaluating with the testing data, model prediction accuracy is observed to be $70 \%$. The prediction accuracy of the model is documented by using a confusion matrix, which compares between the actual and prediction. Diagonal elements of the

| Layer (type) | Output Shape | Param \# |
| :---: | :---: | :---: |
| conv1d_1 (Conv1D) | (None, 292, 32) | 320 |
| max_pooling1d_1 (MaxPooling1 | (None, 97, 32) | 0 |
| conv1d_2 (Conv1D) | (None, 91, 64) | 14400 |
| max_pooling1d_2 (MaxPooling1 | (None, 30, 64) | 0 |
| conv1d_3 (Conv1D) | (None, 26, 128) | 41088 |
| global_average_pooling1d_1 ( | (None, 128) | 0 |
| dropout_1 (Dropout) | (None, 128) | 0 |
| dense_1 (Dense) | (None, 5) | 645 |
| lambda_1 (Lambda) | (None, 5) | 0 |
| Total params: 56,453 Trainable params: 56,453 Non-trainable params: 0 |  |  |

Figure 3.18: Data dimensions through layers of CNN
matrix depict The traces, in which true label from data and predicted label by model are the same. The higher the diagonal elements, the better is the prediction accuracy of the model.

### 3.3 Supervised learning - Decision tree

Decision tree is used as a powerful supervised learning model for classification problem. It is capable of achieving higher accuracy and is highly interpretable. Decision tree involves sequential hierarchical decisions which lead to final classification. The model is created by 2 steps including, induction and pruning. Induction is a process

| CNN |  | Predicted Label |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 |
|  | 1 | 36 | 0 | 0 | 2 | 1 |
|  | 2 | 1 | 16 | 0 | 0 | 18 |
|  | 3 | 3 | 0 | 97 | 29 | 5 |
|  | 4 | 9 | 1 | 6 | 38 | 1 |
|  | 5 | 5 | 2 | 0 | 1 | 9 |

Figure 3.19: Prediction summary of CNN
in which a decision tree is built, but the nature of training process results in overfitting issue. Through the process of pruning, unnecessary structures from the decision tree are removed to prevent overfitting.

### 3.3.1 Decision tree theory

Decision tree consists of node, an evaluation condition of a certain feature. Edges/Branch, refers to the outcome of a node, which connects with another node.

And, finally leaf nodes, refer to the final outcome resulting in the class labels. Moving into details of the decision tree used for classification of heat release rate traces, recursive binary splitting is used at every node. It splits into two at decision making node. To calculate accuracy of the split at each node, cost of split is evaluated. For a
classification problem, cost function (Gini Index Function) gives a perspective of the the goodness of split by the Eq. (3.7).

$$
\begin{equation*}
\mathrm{G}=1-\Sigma_{k}\left(p_{k}^{2}\right) \tag{3.5}
\end{equation*}
$$

Where $p_{k}$ is the proportion of class inputs belonging to a particular group. High level of purity i.e higher value of $p_{k}$ is achieved when the the value of $G$ is lower. The concept of having a single class segregated out is measured by another parameter, information gain. So at every split decision tree algorithm evaluates all the features for the highest value of information gain. Then, it is chosen as a condition for node. It is depicted by the equation (3.8) below.

$$
\begin{equation*}
\operatorname{Gain}(S, A)=\operatorname{Entropy}(S)-\Sigma_{v e V a l u e s}(A) \frac{\left|S_{v}\right|}{|S|} \cdot \operatorname{Entropy}\left(S_{v}\right) \tag{3.6}
\end{equation*}
$$

Where $S$ refers to set of occurrence, $A$ refers to the feature, $S_{v}$ is the subset of S when A equals to a particular classification value and $\operatorname{Values}(A)$ refer to all the possible values of A in the training data. Entropy refers to measure of uncertainty in the random variable, it also depicts the impurity of the collection. At each node the same step step is evaluated till all the classes are achieved as leaf node. But, the issue associated would be overfitting of the model on the training data.

### 3.3.2 Application of decision tree in HRR shaping

To apply the decision tree method on HRR data, MATLAB predefined function fitctree with binary recursive approach is used. The function takes 2 major inputs, with one being the features and other being labels of classification. So in HRR classification, the features considered are the engine control input parameters (engine speed,start of injection of DI fuel, total fuel quantity, pre-mixed ratio and intake manifold temperature. The output is the true labels for traces identified initially for training the model. The Figure 3.20 shows the binary recursive classification arrived at by the decision tree algorithm based on the features of the data. The decision tree approach is prone to overfitting issue, hence the number of leaf nodes were restricted to a maximum of 12 , to avoid overfitting issue.

### 3.3.2.1 Prediction Accuracy of decision tree model

Once the decision tree model is determined, testing data is evaluated. The summary of the true label and predicted is shown in Figure 3.21. The prediction accuracy of the model is $74.5 \%$, with diagonal elements signifying the predictions tallying with the true label.


Figure 3.20: Decision tree for the engine HRR classification


Figure 3.21: Prediction summary of Decision tree

### 3.4 Unsupervised learning - k-means clustering

In unsupervised learning approach, k-means clustering is used to solve a classification problem. The parent algorithm used for classification of HRR traces is discussed in Section 3.2. It is based on multiple thresholds. In order to eliminate bias introduced by thresholds in training data, an unsupervised approach is being evaluated.

### 3.4.1 k-means theory

k -means clustering is a popular technique for clustering problem, where centroid would represent data point in a 2-dimensional data frame. In order to classify the
centroid would represent a complete HRR trace. k -means clustering starts with random initialisation of centroids, $\mathrm{c}_{1}, \mathrm{c}_{2}, \ldots \mathrm{c}_{k}$, of heat release rate data. Since, traces are intended to be segregated into five bins, k is initialised to 5 . Iteration of following two steps is done, till the centroids converge.

1. In this step each data point based on them minimum euclidean distance is assigned to the nearest center.

$$
\begin{equation*}
\operatorname{argmin}_{c_{i} \epsilon C} \operatorname{dist}\left(x-c_{i}\right)^{2} \tag{3.7}
\end{equation*}
$$

$\mathrm{c}_{i}$ is the centroid belonging to the the collection of Centroids C and each data point x is being assigned to the cluster based on euclidean distance calculated by $\operatorname{dist}()$.
2. In the second step of the sequence, centroid is recalculated as the mean of data points assigned to its cluster. The set of data points assigned to $\mathrm{i}^{\text {th }}$ cluster is $\mathrm{S}_{i}$.

$$
\begin{equation*}
c_{i}=\frac{1}{\left|S_{i}\right|} * \Sigma_{x_{i} \epsilon S_{i}} x_{i} \tag{3.8}
\end{equation*}
$$

Algorithm is iterated until the sum of euclidean distance has become minimum and no data points switch between clusters. A similar approach is carried out through the complete length of the heat release rate vector to identify the centroid for the cluster
of traces.

### 3.4.2 Application of k -means in HRR shaping

k-means clustering approach was used to classify data into 5 bins. Since, each trace is observed to have different magnitude peak heat release rate it affected the clustering pattern. The traces were normalised individually to range from 0 to 1 , so that traces could be clustered on its pattern of heat release rate rather than magnitude of peak.

Centroids are chosen randomly at the beginning of the classification and the euclidean distance of each trace from the centroid is calculated. Traces with the least distance from the centroid are clustered in a bin. From the clustered traces, centroid is recalculated. The process is repeated until the centroid and clustered traces remain same after consecutive iterations.

Figure 3.22 depicts the clustered traces, arrived by K-means in 4 different bins.

### 3.4.2.1 Drawbacks of k-means classification

With k-means clustering approach, two major drawbacks were observed. With multiple iterations of the clustering, alignment of clustered traces and the centroid of


Figure 3.22: k-means classification of traces
the bins changed. Due to this, it became difficult to assign a bin to a specific pattern of heat release rate. Second drawback was that, between the clustered traces in bins, it was difficult to identify distinct differences in heat release rate pattern. This apparently made the classification difficult to justify unique characteristics of each bin.

Due to these drawbacks of k-means, supervised learning approach is preferred. First preference is Decision tree approach leads to a prediction accuracy of $74.5 \%$. Decision tree is built as a function of key operating conditions of engine and its control inputs.

The CNN model leads to an prediction accuracy of $70 \%$. CNN model is built as a function of heat release rate traces from the engine. Use of Machine learning based approach also facilitates in means to learn from the engine in actual operation scenario as well. It is discussed further in the future work section on an idea for implementation of control structure of the above discussed machine learning based models.

Rule based technique, was used to classify HRR traces and classified traces were used in supervised learning approach to train and evaluate the model. With rule based classification, distinct characteristics of grouped traces are also observed in Section 3.1.1. Rule based classified traces are used for identification of scheduling parameters Chapter 4.

## Chapter 4

## Identification of combustion

## classifiers

LTC engines heat release rate pattern changes with change in the operating conditions i.e engine speed, intake manifold pressure and temperature) and manipulated variables (fuel quantity, SOI and PR). Hence, it is evident that heat release pattern variation is in a multi dimensional data frame. To control complex combustion heat release in LTC engines, one can use linear parameter varying (LPV) representation to capture non-linear LTC engine behavior in LPV state space model that can be used for combustion control. Building up the result in Chapter 3, an LPV model is developed for LTC engine control. Thus, we need to identify a scheduling parameters of LPV matrices that can represent the non-linearity of the LTC engine as a function
of engine conditions and manipulated variables. With proper selection of a scheduling variables details of change in HRR pattern of the engine can be decoded.

### 4.1 Scheduling parameter identification

The multi dimensional heat release data frame has to be reduced to a one or two dimensional space so that identified parameter can be used as a scheduling variable in the LS-SVM code for building LPV matrices. To this end, principal component analysis (PCA) and multi variable linear regression approach are evaluated to reduce higher dimensions of the data and parameterize the equation with identified dimensions .

### 4.1.1 Principal Component Analysis (PCA)

Principal component analysis is the procedure of dimension reduction of the large data set into a small one which still holds most of the information from the original data. It is achieved by translating the information from correlated input variables to principal components.

The first principle component is identified such that it accounts for the maximum variability contained in the data; thus the subsequent principle components are chosen
such that it could account for rest of the variability in the data set. The principal components are arrived as a linear combination of observed variables weighted by the corresponding eigen values. Values are represented in rotational matrix, which can be interpreted as the rotation of data in order to achieve projection with greatest variance along the axis of first principal component. Subsequent principal axes are chosen such that its geometrically orthogonal.Principal axis identification could be confused with linear regression. The difference is, PCA works to minimize the perpendicular distance between the principal component axis and the data point. But, in linear regression the distance between the predicted and actual value of the data point is minimized.

Looking into the mathematics behind PCA, data is centered by calculating the mean. The covariance matrix of the data is calculated as the sum of the product of the coordinate based on the Equation 4.1, with n as the number of observations and X and $Y$ are set of 2 data columns.

$$
\begin{equation*}
\operatorname{cov}(X, Y)=\frac{1}{n-1} x \Sigma_{i=1}^{n}\left(X_{i}-\bar{x}\right)\left(Y_{i}-\bar{y}\right) \tag{4.1}
\end{equation*}
$$

Where X refers to data representing operating conditions i.e engine speed, intake manifold pressure and temperature) and manipulated variables (fuel quantity, SOI and PR ) and Y refers to the classified HRR traces. PCA is evaluated in R Studio, a statistical software using prcomp function and the rotational matrix with eigen values
and the variability associated with each of the principle axes is shown in Table 4.1
Table 4.1
Output of PCA on HRR classifier identification

| Principal axis | Parameter name | Proportion of <br> variance (\%) |
| :---: | :---: | :---: |
| PC1 | Start of Injection | 26.4 |
| PC2 | Premixed ratio | 23.5 |
| PC3 | Fuel quantity | 20.3 |
| PC4 | Engine speed | 16.5 |
| PC5 | Intake manifold temperature | 9.4 |
| PC6 | Intake manifold pressure | 3.9 |

Even though PCA is a powerful tool, it comes with the limitation of missing on nonlinear data patterns. Since, engine data is widely known for its non linear behaviour, the tool is applied on an evaluation basis to look at the outcome and understand the variability explained by the technique across different principal axis.

Based on the results of PCA, its evident that start of injection, premixed ratio, fuel quantity and engine speed have a significant impact in the change of heat release pattern in data. The variability is potentially spread across, more than 2 axis parameters. Hence, a method of multivariable linear regression is also looked into as a potential option for grouping the significant engine inputs arrived through PCA into regression equation.

### 4.1.2 Multivariable linear regression

Multivariable linear regression is a technique to build a model as a function of two or more explanatory variables and a response variable, by fitting a linear equation on test data. For a model with p explanatory variables, $\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}, \ldots, \mathrm{x}_{p}$ and y as response variable, the model equation could be represented as

$$
\begin{array}{r}
y_{i}=\beta_{0}+\beta_{1} \cdot x_{i 1}+\beta_{2} \cdot x_{i 2}+\ldots+\beta_{p} \cdot x_{i p}+\epsilon_{i}  \tag{4.2}\\
\text { for } \mathrm{i}=1,2,3, . . \mathrm{n}
\end{array}
$$

Where n is the number of observations in data. The fit of the model is governed by the coefficients $\left(\beta_{0}, \beta_{1}, \beta_{2}, . ., \beta_{p}\right)$ of the explanatory variables and $\epsilon$ depicts the residual term. The residual term accounts for the deviation of the fitted value to the actual observed value of the response variable.

Most of the occasions the coefficients are computed by statistical software. In theory, the best line fitting data is evaluated by using a cost function. Cost function is a sum of squares of vertical distance from each data point to the predicted value by the fitted line divided by number of observations. These deviations are squared, so that the positive and negative differences don't cancel out each other. The cost function
is described in Equation 4.3.

$$
\begin{equation*}
\text { Mean Square Error }(\mathrm{MSE})=\frac{1}{n} \Sigma_{i=1}^{n}\left(y-y_{i}\right)^{2} \tag{4.3}
\end{equation*}
$$

Where $y$ is observed value and $y_{i}$ is the predicted value. With the minimisation of cost function, the coefficients of the best fit line are arrived. With this approach, significant engine input parameters could be formulated into a single equation.

### 4.1.2.1 Application of multi variable linear regression

The classification of heat release traces is based on fraction of early HR and fraction of late HR. With PCA, the parameters with greater influence on the heat release classification is identified as start of injection, premixed ratio,fuel quantity and engine speed. As a combination of these parameters, by using regression approach the fraction of early HR and fraction of late HR are modelled using the identified engine parameters.

Multiple combinations were evaluated to model fraction of early HR and fraction of late HR. By using the R- square value the quality of the model is evaluated. In the Table 4.2, different combinations evaluated are listed.
Table 4.2
Table of iteration of engine parameters to model fraction of early HR and

| Serial Number | Engine Parameters | Number of parameters in Equation | R-square <br> Fraction of Early HR | R- square <br> Fraction of Late HR |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Start of Injection Premixed ratio | 6 (Quadratic terms) | 61.9 | 36.7 |
| 2 | Start of Injection Premixed ratio Engine Speed | 10 (Quadratic terms) | 64.5 | 65.2 |
| 3 | Start of Injection Premixed ratio Engine Speed Fuel quantity | 5 (Linear terms) | 59.0 | 67.4 |
| 4 | Start of Injection Premixed ratio Engine Speed Fuel quantity | 15 (Quadratic terms) | 69.1 | 78.3 |
| 5 | Start of Injection Premixed ratio Engine Speed Fuel quantity | 19 (Cubic terms) | 69.6 | 80.4 |
| 6 | Start of Injection Premixed ratio Engine Speed Fuel quantity <br> Intake manifold pressure and temperature | 19 (Cubic terms) | 71.6 | 79.8 |

For all the combinations after modelling, the modelled fraction of early HR and fraction of late HR are compared with the experimental data and classification. The accuracy of classification is also evaluated by calculating the prediction accuracy. Upon evaluating all the above mentioned combinations, it was observed that the fifth combination with start of injection, premixed ratio, engine speed and fuel quantity was observed to have significant $R^{2}$ value and also resulted in better prediction accuracy in the LPV - Support Vector Machine based system identification discussed in Chapter 5.

Fraction of early HR is formulated as
$-13.2+0.012 \times$ SOI $-0.47 \times \mathrm{PR}+0.03 \times$ Speed $+0.2 \times \mathrm{FQ}+0.0026 \times \mathrm{SOI}^{2}+$ $0.013 \times \mathrm{PR}^{2}-2.2 \times 10^{-5} \times$ Speed $^{2}-7.2 \times 10^{-3} \times \mathrm{FQ}^{2}-2.4 \times 10^{-3} \times \mathrm{SOI} \times \mathrm{PR}+$ $1.8 \times 10^{-4} \times$ SOI x Speed $-3.8 \times 10^{-3} \times$ SOI x FQ $-1.2 \times 10^{-4} \times$ Speed $\times$ FQ $-1.1 \times 10^{-5} \times$ Speed $\times \mathrm{PR}+4.5 \times 10^{-3} \times \mathrm{FQ} \times \mathrm{PR}-1.9 \times 10^{-5} \times \mathrm{SOI}^{3}$ $-1.2 \times 10^{-4} \times \mathrm{PR}^{3}+3.6 \times 10^{-9} \times \mathrm{Speed}^{3}+1.0 \times 10^{-4} \mathrm{x} \mathrm{FQ}^{3}$

Fraction of late HR is formulated as
$-16.5+0.04 \times$ SOI $+0.08 \times$ PR $-0.04 \times$ Speed $+4.5 \times$ FQ $-0.025 \times \mathrm{SOI}^{2}$
$-3.2 \times 10^{-03} \times \mathrm{PR}^{2}+4.9 \times 10^{-05} \times$ Speed $^{2}-1.6 \times 10^{-01} \times \mathrm{FQ}^{2}+$
$1.0 \times 10^{-05} \times$ SOI x PR $+5.0 \times 10^{-04} \times$ SOI x Speed $-1.5 \times 10^{-02} \times$ SOI x FQ + $2.7 \times 10^{-04} \times$ Speed $\times$ FQ $-3.6 \times 10^{-04} \times$ Speed $\times$ PR $-7.3 \times 10^{-03} \times \mathrm{FQ} \times \mathrm{PR}+$
$1.6 \times 10^{-04} \times \mathrm{SOI}^{3}+4.5 \times 10^{-05} \times \mathrm{PR}^{3}-1.6 \times 10^{-08} \times \mathrm{Speed}^{3}+1.7 \times 10^{-03} \times \mathrm{FQ}^{3}$
The classification of heat release types with experimental values of fraction of early HR and fraction of late HR is shown in Figure 4.1.


Figure 4.1: Plot of experimental data

With modelled fraction of early HR and fraction of late HR as the scheduling parameter, the identification of LPV matrices for LTC engine is covered in Chapter 5

## Chapter 5

## LPV model Identification with combustion classifiers

Combustion classifiers identified in Chapter 4 is used as scheduling parameter to build a LPV model of the LTC engine. By using combustion classifiers as scheduling variable of LPV model, the information of combustion type is inbuilt into LTC engine model. Support Vector Machine is used for identification of LPV matrices and is discussed in Section 5.1

### 5.1 Support Vector Machine (SVM)

Support vector machine(SVM) is a supervised machine learning approach. It is used both as a classification and regression algorithm. SVM for classification, identify parameters of a hyper plane (line on a 2-dimensional frame) that result in classification of data. In case of regression, it retains all the features in the data and comes up with a system equation from training data with maximum margin and minimum error.

Approach of support vector machine is used to build LPV state space matrix as a function of combustion classifier as scheduling parameter to model the RCCI engine.

### 5.1.1 LS-SVM system identification

SVM regression approach is used to identify the state space matrices of the engine model. LS SVM state space matrix at discrete instant of time $k$, can be represented as 50

$$
\begin{array}{r}
X_{k+1}=A\left(p_{k}\right) X_{k}+B\left(p_{k}\right) U_{k}+K\left(p_{k}\right) e_{k}  \tag{5.1}\\
Y_{k}=C\left(p_{k}\right) X_{k}+D\left(p_{k}\right) U_{k}+e_{k}
\end{array}
$$

where $X$ represents states of the system, $Y$ is measurable output of the system and $U$ refers to the manipulated variable for controlling the system. $p$ represents the scheduling parameter and $e$ represents stochastic white noise associated. $A\left(p_{k}\right), B\left(p_{k}\right), C\left(p_{k}\right), D\left(p_{k}\right)$ and $K\left(p_{k}\right)$ represent the the state space matrices of the system and vary as a function of the parameter $p_{k}$. Equation 5.1 is restructured as

$$
\begin{equation*}
e_{k}=Y_{k}-C\left(p_{k}\right) X_{k}-D\left(p_{k}\right) U_{k} \tag{5.2}
\end{equation*}
$$

Substituting back into Equation 5.1

$$
\begin{gather*}
X_{k+1}=A\left(p_{k}\right) X_{k}+B\left(p_{k}\right) U_{k}+K\left(p_{k}\right) Y_{k}-K\left(p_{k}\right) C\left(p_{k}\right) X_{k}-K\left(p_{k}\right) D\left(p_{k}\right) U_{k}  \tag{5.3}\\
X_{k+1}=\left(A\left(p_{k}\right)-K\left(p_{k}\right) C\left(p_{k}\right)\right) X_{k}+\left(B\left(p_{k}\right)-K\left(p_{k}\right) D\left(p_{k}\right)\right) U_{k}+K\left(p_{k}\right) Y_{k} \\
\bar{A}=A\left(p_{k}\right)-K\left(p_{k}\right) C\left(p_{k}\right)  \tag{5.4}\\
\bar{B}=B\left(p_{k}\right)-K\left(p_{k}\right) D\left(p_{k}\right)
\end{gather*}
$$

So, Equation 5.1 can be rewritten as

$$
\begin{array}{r}
X_{k+1}=\bar{A}\left(p_{k}\right) X_{k}+\bar{B}\left(p_{k}\right) U_{k}+K\left(p_{k}\right) Y_{k}  \tag{5.5}\\
Y_{k}=C\left(p_{k}\right) X_{k}+D\left(p_{k}\right) U_{k}+e_{k}
\end{array}
$$

The plant matrices $\bar{A}\left(p_{k}\right), \bar{B}\left(p_{k}\right), C\left(p_{k}\right), D\left(p_{k}\right)$ and $K\left(p_{k}\right)$ are computed using support vector machine approach. By taking the training data into SVM framework, the plant matrices are transformed using weighing matrices $(W)$, regression vectors or features
of the data $(\phi)$ as shown in Equation 5.6

$$
\begin{array}{r}
X_{k+1}=W_{1} \phi_{1}\left(p_{k}\right)+W_{2} \phi_{2}\left(p_{k}\right)+W_{3} \phi_{3}\left(p_{k}\right)+\epsilon_{k}  \tag{5.6}\\
Y_{k}=W_{4} \phi_{4}\left(p_{k}\right)+W_{5} \phi_{5}\left(p_{k}\right)+\zeta_{k}
\end{array}
$$

where $\epsilon$ and $\zeta$ represent the residual error at the instant $k$. Equation 5.6 is deduced further by representing the regression vector $(\phi)$ as a function of basis function ( $\Phi$ )

$$
\begin{array}{r}
X_{k+1}=W_{1} \Phi_{1}\left(p_{k}\right) X_{k}+W_{2} \Phi_{2}\left(p_{k}\right) U_{k}+W_{3} \Phi_{3}\left(p_{k}\right) Y_{k}+\epsilon_{k}  \tag{5.7}\\
Y_{k}=W_{4} \Phi_{4}\left(p_{k}\right) X_{k}+W_{5} \Phi_{5}\left(p_{k}\right) U_{k}+\zeta_{k}
\end{array}
$$

In order to identify the state space matrices the weighting matrices have to be determined. To optimise the estimation,least square optimisation method is chosen and the cost function $(\mathrm{J})$ in shown in Equation (5.8)

$$
\begin{equation*}
J=\frac{1}{2} \Sigma_{i=1}^{5}\left\|W_{i}\right\|_{F}^{2}+\frac{1}{2} \Sigma_{k=1}^{N}\left(\epsilon_{k}^{T} \Gamma \epsilon_{k}+\zeta_{k}^{T} \psi \zeta_{k}\right) \tag{5.8}
\end{equation*}
$$

where $\Gamma$ and $\zeta$ represent the diagonal regularisation parameters used on the the residual errors to avoid overfitting of the training data. $\|x\|_{F}$ is the Forbenius norm. Cost function is optimised by using Lagrange optima identification. The equation
with Lagrangian multipliers are shown

$$
\begin{array}{r}
L\left(W_{1}, W_{2}, W_{3}, W_{4}, W_{5}, \epsilon, \zeta, \alpha, \beta\right)=J-\left(\Sigma _ { j = 1 } ^ { N } \alpha _ { j } ^ { T } \left(W_{1} \Phi_{1}\left(p_{j}\right) X_{j}+W_{2} \Phi_{2}\left(p_{j}\right) U_{j}+\right.\right. \\
\left.\left.W_{3} \Phi_{3}\left(p_{j}\right) Y_{j}\right)+\epsilon_{j}-X_{j+1}\right)-\Sigma_{j=1}^{N} \beta_{j}^{T}\left(W_{4} \Phi_{4}\left(p_{j}\right) X_{j}+\right.  \tag{5.9}\\
\left.W_{5} \Phi_{5}\left(p_{j}\right) U_{j}+\zeta_{j}-Y_{j}\right)
\end{array}
$$

$\alpha_{j}$ and $\beta_{j}$ are Lagrange multipliers at the instant $j$. Optimum solution is arrived by taking partial derivative of the Equation 5.9

$$
\begin{align*}
& \frac{\partial L}{\partial W_{1}}=0, \Longrightarrow W_{1}=\Sigma_{j=1}^{N} \alpha_{j} \Phi_{1}^{T}\left(p_{j}\right) X_{j}^{T} \\
& \frac{\partial L}{\partial W_{2}}=0, \Longrightarrow W_{2}=\Sigma_{j=1}^{N} \alpha_{j} \Phi_{2}^{T}\left(p_{j}\right) U_{j}^{T} \\
& \frac{\partial L}{\partial W_{3}}=0, \Longrightarrow W_{3}=\Sigma_{j=1}^{N} \alpha_{j} \Phi_{3}^{T}\left(p_{j}\right) Y_{j}^{T} \\
& \frac{\partial L}{\partial W_{4}}=0, \Longrightarrow W_{4}=\Sigma_{j=1}^{N} \beta_{j} \Phi_{4}^{T}\left(p_{j}\right) X_{j}^{T} \\
& \frac{\partial L}{\partial W_{5}}=0, \Longrightarrow W_{5}=\Sigma_{j=1}^{N} \beta_{j} \Phi_{5}^{T}\left(p_{j}\right) U_{j}^{T}  \tag{5.10}\\
& \frac{\partial L}{\partial \alpha_{j}}=0, \Longrightarrow \epsilon_{j}=X_{j+1}-W_{1} \Phi_{1}^{T}\left(p_{j}\right) X_{j}^{T}-W_{2} \Phi_{2}^{T}\left(p_{j}\right) U_{j}^{T}-W_{3} \Phi_{3}^{T}\left(p_{j}\right) Y_{j}^{T} \\
& \frac{\partial L}{\partial \beta_{j}}=0, \Longrightarrow \zeta_{j}=Y_{j}-W_{4} \Phi_{4}^{T}\left(p_{j}\right) X_{j}^{T}-W_{5} \Phi_{5}^{T}\left(p_{j}\right) U_{j}^{T} \\
& \frac{\partial L}{\partial \epsilon_{j}}=0, \Longrightarrow \alpha_{j}=\Gamma \epsilon_{j} \\
& \frac{\partial L}{\partial \zeta_{j}}=0, \Longrightarrow \beta_{j}=\psi \zeta_{j}
\end{align*}
$$

Substituting back in Equation 5.7

$$
\begin{array}{r}
X_{k+1}=\sum_{j=1}^{N} \alpha_{j} X_{j}^{T}\left(\Phi_{1}\left(p_{j}\right)^{T}\right)\left(\Phi_{1}\left(p_{k}\right)\right) X_{k}+\sum_{j=1}^{N} \alpha_{j} X_{j}^{T}\left(\Phi_{2}\left(p_{j}\right)^{T}\right)\left(\Phi_{2}\left(p_{k}\right)\right) U_{k}+ \\
\sum_{j=1}^{N} \alpha_{j} X_{j}^{T}\left(\Phi_{3}\left(p_{j}\right)^{T}\right) Y_{k}\left(\Phi_{3}\left(p_{k}\right)\right)+\Gamma^{-1} \alpha_{k} \\
Y_{k}=\sum_{j=1}^{N} \beta_{j} X_{j}^{T}\left(\Phi_{4}\left(p_{j}\right)^{T}\right) X_{k}\left(\Phi_{4}\left(p_{k}\right)\right)+\sum_{j=1}^{N} \beta_{j} X_{j}^{T}\left(\Phi_{5}\left(p_{j}\right)^{T}\right) U_{k}\left(\Phi_{5}\left(p_{k}\right)\right)+\psi^{-1} \beta_{k} \tag{5.11}
\end{array}
$$

By applying the kernel trick to reduce $\left(\Phi_{1}\left(p_{j}\right)^{T}\right) \cdot\left(\Phi_{1}\left(p_{k}\right)\right)$ with $K^{-1}\left(p_{j}, p_{k}\right)$. By substituting results from Equation 5.10 in Equation 5.11, it can be rewritten as

$$
\begin{gather*}
X_{k+1}=\alpha \Omega+\Gamma^{-1} \alpha  \tag{5.12}\\
Y_{k}=\beta \Xi++\psi^{-1} \beta
\end{gather*}
$$

$\Omega$ and $\Xi$ represent an array of kernel or grammian matrices. Deriving from the Equation 5.12

$$
\begin{array}{r}
\operatorname{vec}(\alpha)=\left(I_{N} \otimes \Gamma_{-1}+\Omega^{T} I_{n x}\right)^{-1} \operatorname{vec}\left(X_{k+1}\right)  \tag{5.13}\\
\operatorname{vec}(\beta)=\left(I_{N} \otimes \Psi_{-1}+\Xi^{T} I_{n y}\right)^{-1} \operatorname{vec}\left(Y_{k}\right)
\end{array}
$$

where $\otimes$ represent the Kronecker product, $I_{n x}, I_{n y}, I_{N}$ all represent the identity matrices and vec refers to vectorization function.

By applying kernel trick and $\alpha$ and $\beta$ identified, Equation 5.11 is restructured as

$$
\begin{array}{r}
X_{k+1}=\sum_{j=1}^{N} \alpha_{j} X_{j}^{T} k^{-1}\left(p_{j}, p_{k}\right) X_{k}+\sum_{j=1}^{N} \alpha_{j} U_{j}^{T} k^{-2}\left(p_{j}, p_{k}\right) U_{k}+ \\
\sum_{j=1}^{N} \alpha_{j} Y_{j}^{T}() k^{-3}\left(p_{j}, p_{k}\right) Y_{k}+\Gamma^{-1} \alpha_{k}  \tag{5.14}\\
Y_{k}=\sum_{j=1}^{N} \beta_{j} X_{j}^{T}\left(k^{-4}\left(p_{j}, p_{k}\right)\right) X_{k}+\sum_{j=1}^{N} \beta_{j} U_{j}^{T} k^{-5}\left(p_{j}, p_{k}\right) U_{k}+\psi^{-1} \beta_{k}
\end{array}
$$

From the Equation 5.15, the state space matrices could be deduced

$$
\begin{align*}
& \bar{A}\left(p_{k}\right)=\sum_{k=1}^{N} \alpha_{k} X_{k}^{T} k^{-1}\left(p_{k}, .\right) \\
& \bar{B}\left(p_{k}\right)=\sum_{k=1}^{N} \alpha_{k} U_{k}^{T} k^{-2}\left(p_{k}, .\right) \\
& K\left(p_{k}\right)=\sum_{k=1}^{N} \alpha_{k} Y_{k}^{T} k^{-3}\left(p_{k}, .\right)  \tag{5.15}\\
& C\left(p_{k}\right)=\sum_{k=1}^{N} \beta_{k} X_{k}^{T} k^{-3}\left(p_{k}, .\right) \\
& D\left(p_{k}\right)=\sum_{k=1}^{N} \beta_{k} U_{k}^{T} k^{-3}\left(p_{k}, .\right)
\end{align*}
$$

### 5.1.2 Test data

To identify LPV state space model for the lTC engine, transient engine data is required. Transient engine data was collected from the experimentally validated LTC engine model [4, 5] by varying operating conditions and the control inputs to the engine. Start of injection (SOI) of the DI fuel, fuel quantity (FQ) and premixed fuel ratio ( PR ) are the engine manipulated variables changed during the test. Engine
speed was kept to constant 1000 rpm .

### 5.1.3 LTC engine modelling

Using the LS-SVM approach mentioned in Section 5.1.1, Combustion parameters prediction by coming up with linear parametric varying system matrices is discussed in this subsection.

States of the system $(\mathrm{X})$ are $\left[\begin{array}{lllll}\mathrm{CA}_{50} & \mathrm{MPRR} & \mathrm{T}_{\text {soc }} & \mathrm{P}_{\text {soc }} & \text { IMEP }\end{array}\right]^{T}$

Manipulated Variables of the system (U) are $\left[\begin{array}{lll}\mathrm{SOI} & \mathrm{FQ} & \mathrm{PR}\end{array}\right]^{T}$

Scheduling parameter of the system $(\mathrm{p})$ is $\left[\begin{array}{ll}\mathrm{p}_{1} & \mathrm{p}_{2}\end{array}\right]^{T}$, where $p_{1}$ is fraction of early HR and $\mathrm{p}_{2}$ is fraction of late HR

Output of the system $(\mathrm{Y})$ is $\left[\begin{array}{lll}\mathrm{CA}_{50} & \mathrm{MPRR} & \mathrm{IMEP}\end{array}\right]^{T}$

Hyper parameters to be optimized by the LS-SVM algorithm are
$\dagger$ Kernel functions associated with each of the system matrix A, B and C
$\dagger$ Sigma functions associated with each of the system matrix A, B and C
$\dagger$ Multiplier associated with each of the system matrix A, B and C
$\dagger$ Regularisation parameters associated with each of the 5 states of the system
$\dagger$ Regularisation parameter associated with each of the 3 outputs of the system.

### 5.1.3.1 Model identification results

Identification of hyper parameters associated with LTC engine model with LPV-SVM approach was accomplished by using the Mode Frontier Optimisation Tool. Details on the tool are discussed on Appendix C.


Figure 5.1: Manipulated variables of the LTC engine

In Figure 5.1 the manipulated variables of the LTC engine are shown. The range of manipulated variables also define the training range of manipulated variables of the LTC engine model. Other operating parameters like engine speed at 1000 rpm , intake temperature at $60^{\circ} \mathrm{C}$ and intake pressure at 96.5 kPa are maintained at a constant value.


Figure 5.2: States of the LTC engine

In Figure 5.2 the states of the LTC engine are shown. The states are estimated by the experimentally validated LTC engine model.


Figure 5.3: Scheduling parameters of the LTC engine

In Figure 5.3 the scheduling parameters of the LTC engine are shown. The range of both the scheduling parameters cover all three combustion types of interest.


Figure 5.4: Comparison of measured and modelled output of LTC engine
In Figure 5.4 the comparison of prediction and measured values of the LTC engine are shown. $35 \%$ of the data used for testing is shown in the plot. The LPV model is able to predict $\mathrm{CA}_{50}$, MPRR and IMEP with a RMSE of $0.4 \mathrm{CAD}, 0.5 \mathrm{bar} / \mathrm{CAD}$ and 9.6 kPa . Error observed could be associated to the measurement uncertainty associated with experimental data used to build the model and prediction errors of the experimentally validated LTC engine. Additionally, the states $\mathrm{P}_{s o c}$ and $\mathrm{T}_{s o c}$ are internally calculated since these parameters are very difficult to be measured in the engine, which can also introduce error int he output.

### 5.1.3.2 System matrices

With Mode Frontier, the hyper parameters of the state space model are identified. The identified hyper parameters summary is listed in Appendix D. Variation in the coefficients of the the system matrices for the change in the scheduling parameter are depicted in the figures below 5.5, 5.6 and 5.7. The variation in the elements of the matrices depict the non-linearity of the LTC engine captured into the state space model.


Figure 5.5: $\bar{A}\left(p_{1 k}, p_{2 k}\right)$ matrix elements as a function of scheduling parameters


Figure 5.6: $\bar{B}\left(p_{1 k}, p_{2 k}\right)$ matrix elements as a function of scheduling parameters


Figure 5.7: $\mathrm{C}\left(p_{1 k}, p_{2 k}\right)$ matrix elements as a function of scheduling parameters

## Chapter 6

## Control of combustion phasing and

## IMEP with MPRR limitation

This chapter centers on system, identification of a multi- input multi- output (MIMO) state space model for the LTC engine and design of an adaptive MPC for control of $\mathrm{CA}_{50}$ and IMEP while limiting maximum pressure rise rate.

### 6.1 LPV identification

System identification by using LPV- SVM approach was discussed in Chapter 5.

### 6.1.1 Evaluation of model accuracy

To evaluate the validity of model prediction across all combinations of manipulated variables, a comparison is carried out with the parent LTC engine physics based model from the research work [4]. This helped to identify specific zones where the predicted model accuracy is acceptable for the LTC engine control.

All three manipulated variables, SOI is varied from 0 to 80 bTDC, injected fuel quantity is varied from 5 to $55 \mathrm{mg} /$ cycle and PR is varied from 0 to 60 to evaluate prediction accuracy of the LPV-SVM model of LTC engine. The predicted values of LPV-SVM model is compared with the physics based plant model. Since, LPV-SVM model is a data-driven model it is observed to be valid only across the trained region and it is listed in Table 6.2

## Table 6.1

Valid operating region of LPV-SVM model of LTC engine

| Manipulated Variable | Range |
| :---: | :---: |
| Start of Injection | $(32-45) \mathrm{CAD}$ bTDC |
| Fuel quantity | $(18-27) \mathrm{mg} / \mathrm{cycle}$ |
| Premixed ratio | $(0-40) \%$ |

The Figures 6.1 to 6.3 show the comparison between LPV -SVM model of the LTC engine and the physics based plant of the engine as a function of scheduling parameters (modelled values of fraction of early HR and fraction of late HR).


Figure 6.1: Predicted $\mathrm{CA}_{50}$ from (a) LPV-SVM model and (b) physics based plant model as function of scheduling parameter p1 and p2

Comparison between figures 6.1(a) and 6.1(b) shows that the same trend is followed though prediction variability is observed in $\mathrm{CA}_{50}$ prediction.


Figure 6.2: Predicted MPRR from (a) LPV-SVM model and (b) physics based plant model as function of scheduling parameter p1 and p2

Comparison between figures 6.2 (a) and 6.2 (b) shows that the MPRR prediction is in
the similar range as that of the RCCI physical model.


Figure 6.3: Predicted IMEP from (a) LPV-SVM model and (b) physics based plant model as function of scheduling parameter p1 and p2

Comparison between Figures 6.3(a) and 6.3(b) shows that the IMEP prediction is very close between the LPV-SVM model and RCCI physical model as the prediction accuracy of LPV-SVM model was observed high for IMEP.

### 6.2 Model Predictive Control

An MPC controller is designed for combustion control of the LTC engine. The MPC uses the LPV model from Section 6.2 to predict future outputs of the LTC engine and optimise the manipulated variables based on the optimisation of cost function. MPC Toolbox of Matlab is used as part of the design. In LPV-SVM model of the the LTC
engine, at any instant of operation the system matrices are derived as a function of $\mathrm{p}_{1}$ (fraction of early HR) and $\mathrm{p}_{2}$ (fraction of late HR).

### 6.2.1 Design

Prediction of states and solution to optimisation problem is only arrived for certain future time steps. The number of future steps in which the output of the system is predicted is called prediction horizon and the manipulated variables of the system are optimised for a certain number of steps called control horizon. It is a quadratic optimisation at each of the control step. Hence, control horizon and prediction horizon are selected as 20 and 10 engine cycles, respectively.

The solution of quadratic problem (QP) optimisation results in the identification of manipulated variables of the system. It includes a cost function, whose value is minimised by the controller. Optimisation is constrained by constraints, which are the bounds on the manipulated variables, their rate of change, states and outputs of the system. This results in a realistic and optimal solution. A solution for manipulated variables minimises the cost function and also fulfil the requirements of constraints.

Cost function is built as a sum of three terms in the current design.

$$
\begin{equation*}
J\left(z_{k}\right)=J_{y}\left(z_{k}\right)+J_{\Delta u}\left(z_{k}\right)+J_{\epsilon}\left(z_{k}\right) \tag{6.1}
\end{equation*}
$$

where $\mathrm{z}_{k}$ is the QP decision over the control interval
k is current control interval
$\mathrm{J}_{y}$ refers to output reference tracking
$\mathrm{J}_{\Delta u}$ refers to manipulated variable tracking
$\mathrm{J}_{\epsilon}$ refers to constraint violation
Output reference tracking is achieved by the controller cost function.

$$
\begin{equation*}
J_{y}\left(z_{k}\right)=\sum_{j=1}^{n_{y}} \sum_{i=1}^{p}\left\{\frac{w_{i, j}^{y}}{s_{j}^{y}}\left[r_{j}(k+i \mid k)-y_{j}(k+i \mid k)\right]\right\}^{2} \tag{6.2}
\end{equation*}
$$

In the equation, p represents the prediction horizon, $\mathrm{n}_{y}$ refers to number of plant outputs, $\mathrm{z}_{k}$ is the decision of the QP.

$$
z_{k}^{T}=\left[\begin{array}{llll}
u(k \mid k)^{T} & u(k+1 \mid k)^{T} & u(k+p-1 \mid k)^{T} & \epsilon_{k} \tag{6.3}
\end{array}\right]
$$

$\mathrm{r}_{j}(k+i \mid k)$ and $\mathrm{y}_{j}(k+i \mid k)$ refers to the reference and predicted value of the $\mathrm{j}^{t h}$ plant output at the $\mathrm{i}^{\text {th }}$ step of the prediction horizon. $\mathrm{s}_{j}^{y}$ refers to the scale factor for the $\mathrm{j}^{\text {th }}$ plant output and $\mathrm{w}_{i, j}^{y}$ is the tuning weight for the $\mathrm{j}^{\text {th }}$ plant output at the $\mathrm{i}^{\text {th }}$ step of the prediction horizon.

The second scalar parameter used by the controller in the cost function to keep the
rate of change of manipulated variables of the system is

$$
\begin{equation*}
\left.J_{\Delta u}\left(z_{k}\right)=\sum_{j=1}^{n_{u}} \sum_{i=0}^{p-1}\left\{\frac{w_{i, j}^{\Delta u}}{s_{j}^{u}}\left[u_{j}(k+i \mid k)-u_{j \text { target }}(k+i \mid k)\right)\right]\right\}^{2} \tag{6.4}
\end{equation*}
$$

Where, $\mathrm{n}_{u}$ refers to the number of manipulated variables. $\mathrm{s}_{j}^{u}$ refers to the scale factor for the $\mathrm{j}^{\text {th }}$ plant output and $\mathrm{w}^{\Delta u}{ }_{i, j}$ is the tuning weight for the $\mathrm{j}^{\text {th }}$ plant manipulated variable rate of change at the $\mathrm{i}^{\text {th }}$ step of the prediction horizon.

The designed controller employs the parameter $\mathrm{J}_{\epsilon}$ to measure the violation of constraints.

$$
\begin{equation*}
J_{\epsilon}\left(z_{k}\right)=\rho_{\epsilon} \epsilon_{k}^{2} \tag{6.5}
\end{equation*}
$$

Where, $\epsilon_{k}$ is the slack variable at control interval k and $\rho$ represents the penalty weight associated to it. The maximum and minimum limit set on the plant outputs, manipulated variables and the rate of change of manipulated variables, predominantly constitute the explicit constraints associated with the MPC,

$$
\begin{array}{r}
\frac{y_{j, \min }(i)}{s_{j}^{y}}-\epsilon_{k} V_{j, \min }^{y}(i) \leq \frac{y_{j}(k+i \mid k)}{s_{j}^{y} \leq} \frac{\left.y_{j, \max }(i)\right)}{s_{j}^{y}}+\epsilon_{k} V_{j, \max }^{y}(i)  \tag{6.6}\\
\\
i=1: p, \quad j=1: n_{y} z
\end{array}
$$

$$
\begin{gather*}
\frac{u_{j, \text { min }}(i)}{s_{j}^{u}}-\epsilon_{k} V_{j, \text { min }}^{u}(i) \leq \frac{u_{j}(k+i-I \mid k)}{s_{j}^{u}} \leq \frac{\left.u_{j, \text { max }}(i)\right)}{s_{j}^{u}}+\epsilon_{k} V_{j, \text { max }}^{u}(i),  \tag{6.7}\\
i=1: p, \quad j=1: n_{u} \\
\frac{\Delta u_{j, \min }(i)}{s_{j}^{u}}-\epsilon_{k} V_{j, \text { min }}^{\Delta u}(i) \leq \frac{\Delta u_{j}(k+i-I \mid k)}{s_{j}^{u}} \leq \frac{\left.\Delta u_{j, \max }(i)\right)}{s_{j}^{u}}+\epsilon_{k} V_{j, \text { max }}^{\Delta u}(i), \\
i=1: p, \quad j=1: n_{u} \tag{6.8}
\end{gather*}
$$

Where, $\mathrm{y}_{j, \min }(i)$ and $\mathrm{y}_{j, \max }(i)$ refer to the min and max bounds set on the $\mathrm{j}^{i h}$ outputs of the system at the $\mathrm{i}^{\text {th }}$ step of the prediction horizon. Similarly, $\mathrm{u}_{j, \min }(i)$ and $\mathrm{u}_{j, \max }(i)$ refer to themin and max bounds set on the manipulated variables and $\Delta u_{j, \min }(i)$ and $\Delta u_{j, \max }(i)$ refer to the min and max bounds set on the rate of change of the manipulated variable.

### 6.2.2 Application

Adaptive MPC is used to track the output, $\mathrm{CA}_{50}$ and IMEP of the system and limit MPRR by using SOI, fuel quantity and PR as manipulated variables. The control time step is set to 1 engine cycle. The prediction horizon and control horizon are set to 20 and 10 engine cycles.


Figure 6.4: Schematic of the designed LPV-MPC controller for the LTC engine

### 6.2.2.1 Control structure

Control structure of the desired adaptive MPC controller is shown in Figure-6.4. Scheduling parameters (p1, p2) are calculated from engine speed, start of injection, fuel quantity injected and premixed ratio. Based on the scheduling parameters, LPV matrices of the LTC engine can be identified. These matrices are used by MPC to predict performance of the LTC engine. $\mathrm{CA}_{50}$, IMEP and MPRR constraint are fed to the MPC controller. The LTC physics based plant is fed with manipulated variables (start of injection, fuel quantity injected and premixed ratio) at each engine cycle. Kalman filter is used in the schematic to predict the unmeasured states of the physics based plant. The $\mathrm{CA}_{5} 0$ and IMEP reference on implementation in an engine, is derived from the engine speed and torque request to the electronic control module based on driver operation. The connection of engine speed and torque request are depicted in dotted line as its not set up in the current model, but are depicted in the control structure to show model's relevance to real life operation of engine.

The weights of the allowed rate of change of manipulated variables and output are tuned to achieve required tracking performance. The weights of the rate of change of SOI is 0.3 , fueling quantity is 0.5 and PR is 0.05 . With the setting, PR is the quickest lever to be changed followed by SOI and fueling quantity.

Table 6.2
Summary of constraints applied on manipulated variables and outputs of the adaptive MPC

| Variable | Minimum constraint | Maximum constraint |
| :---: | :---: | :---: |
| Start of Injection | 32 CAD bTDC | 45 CAD bTDC |
| Fuel quantity | $18 \mathrm{mg} / \mathrm{cycle}$ | $27 \mathrm{mg} / \mathrm{cycle}$ |
| Premixed ratio | $0 \%$ | $40 \%$ |
| $\mathrm{CA}_{50}$ | $-10 \mathrm{CAD} \mathrm{aTDC} \%$ | $30 \mathrm{CAD} \mathrm{aTDC} \%$ |
| IMEP | $500 \mathrm{kPa} \%$ | $1000 \mathrm{kPa} \%$ |
| MPRR | $0 \%$ | $6 \%$ |

### 6.2.2.2 Tracking Performance

The tracking performance of the designed controller to follow the desired change of $\mathrm{CA}_{50}$ from 5 to 12 CAD aTDC and IMEP from 525 kPa to 650 kPa . As the system tracks the change in output by holding MPRR less than 6bar/CAD. The change in manipulated variables and scheduling parameter of the LPV system is also evaluated in the various cases depicted in Figures from 6.5 to 6.9 .

In Figure 6.5, the tracking ability of designed controller to follow the desired change in both $\mathrm{CA}_{50}$ and IMEP is evaluated. Tracking with RMSE of 1.2 CAD for $\mathrm{CA}_{50}$, IMEP with a RMSE of 6.2 kPa and MPRR is limited to $6.1 \mathrm{bar} / \mathrm{CAD}$.

In Figure 6.6, the tracking ability of designed controller of a LTC engine for a change in both IMEP and $\mathrm{CA}_{50}$ while the restrictions on MPRR being relaxed to 8bar/CAD. Tracking with RMSE of 1 CAD for $\mathrm{CA}_{50}$, IMEP with RMSE of 10.3 kPa and the
maximum pressure rise rate is limited to 6.3 bar/CAD. Also, with relaxed MPRR, $\mathrm{CA}_{50}$ tracking performance improved significantly but the error associated with IMEP tracking increased.

In Figure 6.7, the tracking ability of the designed controller to follow a change in outputs of LTC engine with measurement uncertainty is evaluated. The measurement uncertainty from Table 2.5 are added to the outputs of the LTC engine physics based plant, to simulate measurement uncertainty. Tracking with RMSE of 2.2 CAD for $\mathrm{CA}_{50}$, RMSE of 17.3 kPa for IMEP and the maximum pressure rise rate is observed to be $6.5 \mathrm{bar} / \mathrm{CAD}$. Error in tracking had gone up due to uncertainty in the outputs. In $83^{r d}$ engine cycle, as all the manipulated variables saturate a violation in the MPRR is observed. The controller comes into action to bring the MPRR within limit in subsequent cycles.

To compare the effect of selecting proper scheduling variables, the results from this thesis are compared with those in 5. To this end, Figure 6.8 is added in which LTC engine tracking capability achieved is achieved by using only PR as scheduling parameter. Tracking was achieved only by using SOI and fueling quantity as the manipulated variables of the LTC engine. It is evident that the maximum tracking capability for IMEP was limited due to $\mathrm{CA}_{50}$ tracking errors when IMEP $\geq 650 \mathrm{kPa}$. In Figure 6.9, the tracking ability of LTC engine to follow the change in IMEP set to 690 kPa with constraints on MPRR set at 6 bar/CAD using new scheduling variables
and also, using PR as the additional manipulated variable. Tracking with RMSE of 1.1 deg for $\mathrm{CA}_{50}$, IMEP with RMSE of 8.6 kPa and MPRR limited to $6 \mathrm{bar} / \mathrm{CAD}$ was achieved. SOI and PR have almost saturated to its maximum in order to achieve the target. Reduction in RMSE of $\mathrm{CA}_{50}$ and IMEP is seen on comparison of Figure 6.8 and Figure 6.9.

In Figure 6.10, the tracking ability of the designed controller of LTC engine with $\mathrm{CA}_{50}$ target raised to 14 CAD aTDC while constraints on MPRR set to 6bar/CAD is shown. Tracking is achieved with RMSE of 1.7 CAD for $\mathrm{CA}_{50}$, IMEP with RMSE of 5.8 kPa and the maximum pressure rise rate is limited to $6.2 \mathrm{bar} / \mathrm{CAD}$. PR has saturated to 40 in order to achieve the target. The motivation for evaluating controller ability in tracking delayed CA50, comes from the result of work carried out in [57]. It shows that retarded combustion phasing shows benefit of smooth heat release rate and reduced MPRR.


Figure 6.5: Tracking capability of designed controller to follow desired $\mathrm{CA}_{50}$ and IMEP with MPRR limit is $6 \mathrm{bar} / \mathrm{CAD}$


Figure 6.6: Tracking capability of designed controller to follow desired $\mathrm{CA}_{50}$ and IMEP. The MPRR limit is $8 \mathrm{bar} / \mathrm{CAD}$


Figure 6.7: Tracking capability of designed controller to follow desired $\mathrm{CA}_{50}$ and IMEP along with measurement uncertainty added in measured outputs of LTC engine. The MPRR limit is 6 bar/CAD


Figure 6.8: Tracking capability achieved for $\mathrm{CA}_{50}$ and IMEP with PR as scheduling parameter [49]. MPRR limit is 5.8 bar/CAD


Figure 6.9: Maximum tracking capability achieved for IMEP, when increased to 690 kPa and MPRR limit is 6 bar/CAD


Figure 6.10: Maximum tracking capability achieved for $\mathrm{CA}_{50}$, when increased to 14 CAD aTDC and MPRR limit is 6 bar/CAD

## Chapter 7

## Conclusions and Future Work

### 7.1 Summary and Conclusions

In this research work, classification of heat release rate traces of LTC engine was developed. Significant engine inputs leading to different HR shapes were identified. The parameters fraction of early HR and fraction of late HR used for classification were modelled using significant engine inputs. The modelled fraction of early HR and fraction of late HR were used as scheduling variables into the LPV-SVM matrices of the LTC engine model. This model was used to build MPC to control LTC engine. Major contributions/ findings from this research work are presented below.
$\dagger$ Heat release rate data from the experimental study conducted on the LTC engine were analysed. A rule based classification was developed to classify HRR traces into three significant combustion pattern similar to HCCI, PCCI and RCCI. Two transition bins were also identified to create accommodate traces transitioning between the significant combustion pattern.
$\dagger$ Characteristics of the distribution of classified traces were studied. Distribution of combustion parameters like, peak cylinder pressure, maximum pressure rise rate, $\mathrm{CA}_{10}, \mathrm{CA}_{90}$, maximum in-cylinder temperature at start and end of main heat release were analysed. It was observed that combustion parameters had a distinct characteristics across three significant classification bins and the information from these parameters could be further used for controlling the engine.
$\dagger$ As a next step to classify the HRR traces automatically, supervised and unsupervised techniques of machine techniques were applied. With unsupervised approach, it was evident that the classified clusters didn't clearly represent different combustion patterns. On comparison between CNN and decision tree, it was observed that decision tree prediction with higher accuracy of $74.5 \%$.
$\dagger$ In order to model a LPV matrices of the LTC engine, scheduling parameter of LPV matrices were identified. PCA was used to identify the significant LTC engine inputs. SOI, PR ,fuel quantity and engine speed are the significant inputs of engine combustion. Linear regression was used to model, fraction of early

HR and fraction of late HR as a function of these significant engine inputs. The combination of modelled fraction of early HR and fraction of late HR which resulted in highest $\mathrm{R}^{2}$ value was selected as scheduling parameters.
$\dagger$ Using Support Vector Machine(SVM) approach, a data driven LPV control model of the LTC engine was developed. The LPV model used modelled fraction of early HR and fraction of late HR as the scheduling parameters. The model was validated with the data generated by the detailed LTC engine dynamic model. It was able to predict $\mathrm{CA}_{50}$, IMEP and MPRR with RMSE of 0.4 CAD , 16.6 kPa and $0.4 \mathrm{bar} / \mathrm{CAD}$.
$\dagger$ MPC was built to control the LPV model of the LTC engine. It was developed with the prediction horizon of 20 engine cycles and control horizon of 10 engine cycles. The controller was able to track $\mathrm{CA}_{50}$ and IMEP with MPRR constraint of $6 \mathrm{bar} / \mathrm{CAD}$ with SOI, PR and Fuel quantity as manipulated variables. It was able to track $\mathrm{CA}_{50}$ and IMEP with RMSE of 1.2 CAD and 6.2 kPa . MPC performance on $\mathrm{CA}_{50}$ tracking improved with MPRR constraint of 8 bar/CAD. But, the tracking error of IMEP increased.It was able to track $\mathrm{CA}_{50}$ and IMEP with RMSE of 1 CAD and 10.3 kPa .
$\dagger$ Disturbance rejection capability of the MPC was also evaluated by addition of measurement uncertainty into the outputs of the detailed LTC physics based dynamic plant. The MPC controller was able to track $\mathrm{CA}_{50}$ and IMEP of 690 kPa with RMSE of 1.1 CAD and 8.6 kPa on MPRR constraint of $6 \mathrm{bar} / \mathrm{CAD}$.

The controller was also able to track IMEP and $\mathrm{CA}_{50}$ of 14 CAD with RMSE of 5.6 kPa and 1.7CAD on MPRR constraint of $6 \mathrm{bar} / \mathrm{CAD}$.

### 7.2 Future work

Based on the findings of this work, a few areas can be explored further. They are listed below.

### 7.2.1 Control architecture for a multi-mode engine using HRR classification

In order to control the heat release type of the engine real time, an idea of the control architecture depicted in Figure (7.1) can be pursued. The proposed architecture may consist of multiple blocks:

Architecture consists of multiple blocks.
$\dagger$ Prediction models including

1. model to predict as a function of control inputs of LTC engine
2. model to predict as a function of HRR trace


Figure 7.1: Proposed control architecture for a multi-mode engine using HRR classification
$\dagger$ Algorithm for desired HRR type input
$\dagger$ Learning algorithm
$\dagger$ MPC controller

In the following the main blocks in Figure 7.1 are briefly explained

### 7.2.1.1 Predictive models

Two predictive models are used in this control structure. One of the predictive model works as a function of manipulated variables of the engine, like LPV-SVM model built in Chapter 5. It is represented as LPV-SVM as a function of inputs in Figure 7.1. The model based on inputs, calculates the scheduling parameters. Based on scheduling
parameters, can predict the HRR type. It can also calculate the output of the LTC engine, as a function of LPV matrices identified with the scheduling parameters. The second model, works as the function of HRR trace, like CNN model built in Section 3.2. It is represented as Prediction model 2 in Figure 7.1.

### 7.2.1.2 Algorithm for desired HRR type input

A map based logic is set to identify desired heat release rate type as a function of engine speed and fuel quantity injected. Also, based on the HRR type is chosen corresponding cost function and constraints also are fed to the controller. Cost function associated with heat release type 1 is to maximise main heat release, with type 2 is to maximise fraction of early heat release and with type 3 is to maximise fraction of late heat release. Constraints are rate of change of control inputs to engine and limiting constraints combustion parameters. Limiting constraints are on MPRR, $\mathrm{CA}_{50}$, co-efficient of variation of IMEP and emissions. Desired heat release rate type is fed to the Adaptive model predictive controller(MPC).

### 7.2.1.3 MPC controller

Controller block interacts with the LPV-SVM model in order to optimise future control inputs to the engine plant. Its depicted in the control architecture with the
nomenclature of $(k+1)$. The finalised control input is fed to the engine plant. With the help of in cylinder pressure transducer on the engine, the feedback cylinder pressure trace is collected and converted to heat release rate as a function of engine crank angle. By using Prediction model 2, the heat release rate type is identified.

### 7.2.1.4 Learning Algorithm

Learning algorithm is the final block in the architecture which will ensure that LPVSVM model is updated based on real time observations and prediction based on engine in-cylinder pressure data. This block could consist of three elements.
$\dagger$ Operating conditions to learn
$\dagger$ Error calculation
$\dagger$ Learning summary table and update of LPV-SVM model

Engine operating with $\operatorname{COV}_{I M E P} \leq 3 \%$ to ensure stability of operation and with no occurrence of engine combustion related error are some of the conditions to be considered for the learning algorithm to learn. An update summary table is setup inside the learning algorithm, it has the count of region of fueling and engine speed updated in real life operation. The prediction error $\left(\mathrm{e}_{k}\right)$ shown in Figure 7.1 is calculated as
a weighted sum of current prediction by LPV-SVM model and the difference in prediction between LPV-SVM model and Model 2. Once $\mathrm{e}_{k}$ is calculated, the learning algorithm updates the value for future reference in both the summary table and prediction LPV-SVM model. The learning process will help the model to update the prediction as the function of control inputs to reflect real time operating condition of the engine.Complete operational model with the architecture shown in 7.1 is still in the concept phase, it is yet to be built and verified.

### 7.2.2 Other future works

Here is the list of other ideas to advance the outcomes from this thesis
$\dagger$ Experimental implementation and validation of the designed controllers from Chapter 6.
$\dagger$ Design of LPV data driven models from Chapter 5 using the engine experimental data, including $\mathrm{COV}_{\text {IMEP }}$, emissions and combustion noise constraints and on board learning based on real time engine data

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## Appendix A

## LTC engine data used for

## identification of scheduling

## parameter

Data tabulated are collected from the LTC engine in APSRC lab for the research work by references [3],LTC-04

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| SOI <br> $(\mathrm{bTDC})$ | PR <br> $(\%)$ | Total Fuel <br> mass <br> $(\mathrm{mg} /$ cycle $)$ | Engine <br> Speed <br> $(\mathrm{rpm})$ | Intake air <br> temperature <br> (Deg c) | Intake air <br> Pressure <br> $(\mathrm{kPa})$ | CA_Start of <br> Main HR <br> $($ aTDC $)$ | CA_End of <br> Main HR <br> (aTDC) | Heat <br> release <br> type | Fraction <br> of early <br> $(\%)$ | Fraction <br> of Late <br> $(\%)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 40 | 26 | 1200 | 40 | 108 | 2 | 17 | 1 | 4.6 | 15.2 |
| 50 | 40 | 31 | 1200 | 40 | 107 | 6 | 22 | 1 | 3.7 | 10.6 |
| 60 | 40 | 16.3 | 1400 | 40 | 113 | 3 | 26 | 2 | 9.3 | 14.9 |
| 60 | 40 | 19 | 1400 | 40 | 114 | 3 | 18 | 2 | 7.9 | 18.7 |
| 60 | 40 | 22 | 1400 | 40 | 115 | 2 | 13 | 5 | 6.7 | 18.0 |
| 60 | 40 | 19 | 1600 | 40 | 113 | 7 | 26 | 2 | 8.6 | 19.4 |
| 60 | 40 | 22 | 1600 | 40 | 113 | 7 | 28 | 2 | 7.1 | 16.6 |
| 60 | 40 | 25 | 1600 | 40 | 113 | 6 | 14 | 5 | 5.5 | 52.2 |
| 40 | 60 | 19.5 | 800 | 40 | 113 | 3 | 14 | 3 | 3.5 | 32.6 |
| 40 | 60 | 22 | 800 | 40 | 114 | 2 | 11 | 3 | 3.0 | 33.7 |
| 40 | 60 | 29 | 800 | 40 | 112 | 6 | 19 | 1 | 2.4 | 10.7 |
| 45 | 60 | 19 | 1000 | 39 | 109 | 2 | 12 | 5 | 5.4 | 30.8 |
| 45 | 60 | 22 | 1000 | 40 | 108 | 3 | 18 | 1 | 4.7 | 15.8 |
| 45 | 60 | 25 | 1000 | 40 | 108 | 3 | 17 | 1 | 4.3 | 13.2 |
| 45 | 60 | 28 | 1000 | 40 | 108 | 4 | 17 | 1 | 3.8 | 11.2 |
| 45 | 60 | 33 | 1000 | 40 | 109 | 10 | 30 | 1 | 3.0 | 6.5 |
| 20 | 20 | 9 | 800 | 59 | 112 | -2 | 15 | 4 | 2.8 | 19.0 |
| 20 | 20 | 10.1 | 800 | 60 | 112 | -1 | 14 | 4 | 2.8 | 19.7 |
| 20 | 20 | 13 | 800 | 60 | 112 | -2 | 14 | 3 | 1.3 | 27.9 |
| 20 | 20 | 18.5 | 800 | 60 | 112 | 2 | 14 | 3 | 1.5 | 26.2 |
| 20 | 20 | 22 | 800 | 60 | 112 | -3 | 14 | 3 | 0.0 | 24.9 |
| 20 | 20 | 27 | 800 | 60 | 112 | -2 | 17 | 4 | -0.4 | 19.3 |
| 25 | 20 | 9 | 1000 | 60 | 110 | 1 | 13 | 2 | 7.1 | 22.9 |
| 25 | 20 | 10 | 1000 | 59 | 110 | 1 | 14 | 5 | 6.1 | 21.8 |


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| $\begin{aligned} & \text { SOI } \\ & (\mathrm{bTDC}) \end{aligned}$ | $\begin{aligned} & \text { PR } \\ & (\%) \end{aligned}$ | Total Fuel mass (mg/cycle) | Engine Speed (rpm) | Intake air temperature (Deg c) | Intake air <br> Pressure <br> (kPa) | CA_Start of Main HR (aTDC) | CA_End of Main HR (aTDC) | Heat release type | Fraction of early (\%) | Fraction of Late (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 25 | 40 | 14 | 800 | 59 | 113 | -2 | 14 | 3 | 0.5 | 25.8 |
| 25 | 40 | 18 | 800 | 60 | 113 | -1 | 12 | 3 | 0.7 | 31.6 |
| 25 | 40 | 23 | 800 | 60 | 114 | 0 | 15 | 3 | 0.0 | 27.8 |
| 25 | 40 | 28 | 800 | 60 | 113 | 2 | 15 | 3 | 0.2 | 23.0 |
| 30 | 40 | 13 | 1000 | 59 | 110 | 1 | 15 | 3 | 4.4 | 25.7 |
| 30 | 40 | 15 | 1000 | 60 | 110 | 0 | 16 | 3 | 3.1 | 25.5 |
| 30 | 40 | 18.5 | 1000 | 60 | 110 | 0 | 14 | 3 | 2.5 | 29.5 |
| 30 | 40 | 23 | 1000 | 60 | 110 | -1 | 12 | 3 | 1.2 | 29.6 |
| 30 | 40 | 28 | 1000 | 60 | 110 | 1 | 13 | 3 | 1.2 | 24.7 |
| 40 | 40 | 16 | 1200 | 60 | 108 | 1 | 13 | 5 | 5.6 | 32.7 |
| 40 | 40 | 19 | 1200 | 60 | 109 | 0 | 13 | 3 | 3.9 | 32.4 |
| 40 | 40 | 23.5 | 1200 | 60 | 108 | 1 | 14 | 3 | 3.0 | 28.2 |
| 40 | 40 | 27.5 | 1200 | 60 | 108 | 3 | 19 | 4 | 2.7 | 18.7 |
| 47 | 40 | 16.5 | 1400 | 59 | 115 | 1 | 12 | 5 | 5.2 | 36.7 |
| 47 | 40 | 19.5 | 1400 | 60 | 114 | 1 | 11 | 3 | 4.9 | 36.3 |
| 47 | 40 | 24 | 1400 | 61 | 114 |  | 17 | 3 | 3.2 | 25.2 |
| 47 | 40 | 29 | 1400 | 60 | 115 | 3 | 18 | 4 | 2.3 | 21.5 |
| 60 | 40 | 16 | 1600 | 59 | 115 | 2 | 14 | 2 | 7.7 | 29.7 |
| 60 | 40 | 19 | 1600 | 60 | 114 | 1 | 13 | 5 | 5.9 | 26.9 |
| 60 | 40 | 21 | 1600 | 60 | 112 | 2 | 11 | 5 | 6.5 | 29.7 |
| 65 | 40 | 17 | 1800 | 59 | 115 | 2 | 13 | 2 | 8.7 | 29.3 |
| 65 | 40 | 20 | 1800 | 59 | 114 | 1 | 13 | 5 | 6.9 | 24.9 |
| 30 | 60 | 19.5 | 800 | 59 | 114 | 0 | 14 | 3 | 1.1 | 37.0 |
| 30 | 60 | 21 | 800 | 60 | 114 | 0 | 13 | 3 | 1.3 | 36.5 |
| 30 | 60 | 24 | 800 | 60 | 115 | 1 | 13 |  | 0.5 | 33.3 |


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| $\begin{aligned} & \text { SOI } \\ & (\mathrm{bTDC}) \end{aligned}$ | PR <br> (\%) | Total Fuel mass (mg/cycle) | Engine Speed (rpm) | Intake air temperature (Deg c) | Intake air <br> Pressure <br> (kPa) | CA_Start of Main HR (aTDC) | CA_End of Main HR (aTDC) | Heat release type | Fraction of early (\%) | Fraction of Late (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 20 | 22 | 1200 | 80 | 110 | 0 | 15 | 3 | 0.1 | 26.9 |
| 30 | 20 | 26 | 1200 | 80 | 109 | 2 | 18 | 4 | 0.3 | 22.8 |
| 37 | 20 | 10 | 1400 | 79 | 116 | -2 | 10 | 3 | 3.9 | 29.2 |
| 37 | 20 | 13 | 1400 | 80 | 116 | -2 | 10 | 3 | 1.5 | 36.7 |
| 37 | 20 | 18 | 1400 | 80 | 115 | -1 | 12 | 3 | 0.8 | 33.2 |
| 37 | 20 | 22 | 1400 | 80 | 115 | -2 | 15 | 3 | 0.0 | 28.0 |
| 37 | 20 | 25.5 | 1400 | 80 | 115 | -1 | 17 | 3 | 0.0 | 24.4 |
| 42 | 20 | 11 | 1600 | 80 | 114 | -1 | 12 | 3 | 4.1 | 30.1 |
| 42 | 20 | 13 | 1600 | 80 | 114 | 0 | 13 | 3 | 2.7 | 34.4 |
| 42 | 20 | 18 | 1600 | 80 | 113 | 0 | 16 | 3 | 1.3 | 29.7 |
| 42 | 20 | 22 | 1600 | 80 | 113 | 1 | 16 | 3 | 0.9 | 28.0 |
| 42 | 20 | 25.5 | 1600 | 80 | 111 | 2 | 19 | 3 | 0.9 | 24.1 |
| 53 | 20 | 12 | 1800 | 80 | 118 | -1 | 13 | 3 | 4.0 | 34.1 |
| 53 | 20 | 13 | 1800 | 80 | 117 | 0 | 13 | 3 | 3.7 | 34.7 |
| 53 | 20 | 18 | 1800 | 80 | 117 | -1 | 13 | 3 | 1.8 | 32.6 |
| 53 | 20 | 22 | 1800 | 80 | 118 | 0 | 16 | 3 | 1.1 | 27.6 |
| 53 | 20 | 26 | 1800 | 80 | 118 | 0 | 17 | 3 | 0.5 | 23.9 |
| 57 | 20 | 12 | 2000 | 80 | 108 | 0 | 11 | 2 | 8.9 | 33.3 |
| 57 | 20 | 13 | 2000 | 80 | 108 | 0 | 15 | 2 | 8.0 | 30.2 |
| 57 | 20 | 18 | 2000 | 80 | 109 | 0 | 13 | 3 | 4.9 | 31.3 |
| 57 | 20 | 22 | 2000 | 80 | 108 | -1 | 15 | 3 | 3.1 | 27.7 |
| 57 | 20 | 26 | 2000 | 80 | 109 | 3 | 18 | 4 | 3.1 | 22.7 |
| 65 | 20 | 12 | 2200 | 79 | 100 | 2 | 16 | 2 | 12.6 | 26.9 |
| 65 | 20 | 13 | 2200 | 80 | 100 | 1 | 14 | 2 | 10.8 | 31.2 |
| 65 | 20 | 17 | 2200 | 79 | 102 | 1 | 11 | 2 | 8.0 | 34.3 |


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| $\begin{aligned} & \text { SOI } \\ & (\mathrm{bTDC}) \end{aligned}$ | PR <br> (\%) | Total Fuel mass (mg/cycle) | Engine Speed (rpm) | Intake air temperature (Deg c) | Intake air <br> Pressure <br> (kPa) | CA_Start of Main HR (aTDC) | CA_End of Main HR (aTDC) | Heat release type | Fraction of early (\%) | Fraction of Late (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 53 | 20 | 13.5 | 2000 | 98 | 109 | -1 | 14 | 2 | 8.2 | 26.1 |
| 53 | 20 | 18 | 2000 | 99 | 109 | 0 | 12 | 5 | 6.0 | 31.6 |
| 53 | 20 | 22 | 2000 | 98 | 109 | 0 | 14 | 3 | 4.2 | 27.9 |
| 53 | 20 | 26 | 2000 | 99 | 109 | -1 | 16 | 3 | 2.7 | 24.4 |
| 17 | 40 | 11 | 800 | 100 | 110 | -2 | 12 | 3 | 0.5 | 28.7 |
| 17 | 40 | 13.5 | 800 | 100 | 111 | -1 | 11 | 3 | 0.0 | 29.7 |
| 17 | 40 | 18 | 800 | 100 | 112 | -1 | 11 | 3 | -0.4 | 34.8 |
| 17 | 40 | 22 | 800 | 100 | 110 | -2 | 11 | 3 | -0.6 | 28.3 |
| 17 | 40 | 26 | 800 | 100 | 110 | 1 | 12 | 3 | -0.4 | 26.9 |
| 24 | 40 | 11.2 | 1000 | 99 | 111 | 0 | 14 | 3 | 2.7 | 29.7 |
| 24 | 40 | 13.6 | 1000 | 99 | 112 | 1 | 14 | 3 | 1.7 | 30.6 |
| 24 | 40 | 18 | 1000 | 100 | 112 | 0 | 14 | 3 | 0.2 | 33.3 |
| 24 | 40 | 26 | 1000 | 100 | 112 | 2 | 18 | 3 | 0.2 | 24.6 |
| 32 | 40 | 11.7 | 1200 | 99 | 107 | 0 | 14 | 5 | 5.9 | 29.5 |
| 32 | 40 | 13.8 | 1200 | 100 | 107 | 0 | 14 | 3 | 4.8 | 29.3 |
| 32 | 40 | 18 | 1200 | 100 | 107 | -1 | 13 | 3 | 2.7 | 34.1 |
| 32 | 40 | 22 | 1200 | 100 | 107 | 0 | 14 | 3 | 2.0 | 32.0 |
| 32 | 40 | 26 | 1200 | 100 | 108 | 0 | 15 | 3 | 1.4 | 27.9 |
| 39 | 40 | 12 | 1400 | 99 | 114 | 0 | 14 | 5 | 5.6 | 30.0 |
| 39 | 40 | 14 | 1400 | 100 | 115 | 0 | 12 | 3 | 4.7 | 31.9 |
| 39 | 40 | 18 | 1400 | 100 | 114 | -1 | 13 | 3 | 2.4 | 33.7 |
| 39 | 40 | 22 | 1400 | 100 | 115 | -1 | 14 | 3 | 1.7 | 31.9 |
| 39 | 40 | 26 | 1400 | 100 | 115 | 0 | 13 | 3 | 1.1 | 30.7 |
| 49 | 40 | 12.7 | 1600 | 99 | 112 | 0 | 12 | 5 | 6.5 | 33.1 |
| 49 | 40 | 14 | 1600 | 100 | 111 | 0 | 15 | 5 | 5.7 | 29.5 |


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| $\begin{aligned} & \text { SOI } \\ & (\mathrm{bTDC}) \end{aligned}$ | $\begin{aligned} & \mathrm{PR} \\ & (\%) \end{aligned}$ | Total Fuel mass (mg/cycle) | Engine Speed (rpm) | Intake air temperature (Deg c) | Intake air <br> Pressure <br> (kPa) | CA_Start of Main HR (aTDC) | CA_End of Main HR (aTDC) | Heat release type | Fraction of early (\%) | Fraction of Late (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 70 | 60 | 21 | 1800 | 100 | 114 | 5 | 21 | 3 | 3.8 | 28.4 |
| 70 | 60 | 24 | 1800 | 100 | 116 | 6 | 27 | 1 | 3.0 | 15.5 |
| 70 | 60 | 28 | 1800 | 100 | 114 | 7 | 24 | 1 | 3.2 | 15.0 |
| 80 | 60 | 23 | 2000 | 99 | 109 | 6 | 30 | 5 | 5.3 | 13.5 |
| 80 | 60 | 27 | 2000 | 99 | 109 | 6 | 26 | 1 | 5.0 | 11.1 |
| 35 | 40 | 11.7 | 1200 | 79 | 109 | 0 | 14 | 5 | 6.1 | 28.7 |
| 35 | 40 | 13.5 | 1200 | 80 | 109 | 0 | 14 | 5 | 5.0 | 28.5 |
| 35 | 40 | 18 | 1200 | 80 | 109 | -1 | 14 | 3 | 2.6 | 32.0 |
| 35 | 40 | 22 | 1200 | 80 | 109 | -1 | 15 | 3 | 1.8 | 29.0 |
| 35 | 40 | 26.5 | 1200 | 80 | 109 | 1 | 16 | 3 | 1.5 | 24.0 |
| 40 | 40 | 12 | 1400 | 79 | 114 | 1 | 15 | 5 | 6.1 | 29.3 |
| 40 | 40 | 14.3 | 1400 | 80 | 116 | 1 | 14 | 3 | 4.2 | 30.1 |
| 40 | 40 | 18 | 1400 | 80 | 116 | 0 | 13 | 3 | 2.7 | 34.6 |
| 40 | 40 | 22 | 1400 | 80 | 117 | 0 | 14 | 3 | 1.6 | 32.2 |
| 40 | 40 | 26 | 1400 | 80 | 116 | 1 | 15 | 3 | 1.5 | 28.5 |
| 52 | 40 | 13 | 1600 | 80 | 113 | 0 | 15 | 5 | 6.2 | 30.4 |
| 52 | 40 | 14.8 | 1600 | 80 | 114 | 1 | 14 | 5 | 5.4 | 33.0 |
| 52 | 40 | 18 | 1600 | 80 | 112 | 0 | 11 | 3 | 4.9 | 37.4 |
| 52 | 40 | 22 | 1600 | 80 | 111 | 2 | 14 | 3 | 4.2 | 30.8 |
| 52 | 40 | 26 | 1600 | 80 | 111 | 4 | 15 | 3 | 3.5 | 30.2 |
| 60 | 40 | 13.5 | 1800 | 80 | 115 | 0 | 15 | 2 | 7.4 | 29.4 |
| 60 | 40 | 15 | 1800 | 79 | 116 | 1 | 14 | 5 | 6.7 | 32.6 |
| 60 | 40 | 20 | 1800 | 80 | 116 | 0 | 12 | 3 | 4.2 | 31.1 |
| 60 | 40 | 22 | 1800 | 80 | 116 | 0 | 11 | 3 | 3.9 | 30.3 |
| 70 | 40 | 16 | 2000 | 80 | 107 | 2 | 17 | 2 | 9.6 | 24.2 |


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| SOI <br> $(\mathrm{bTDC})$ | PR <br> $(\%)$ | Total Fuel <br> mass <br> $(\mathrm{mg} /$ cycle $)$ | Engine <br> Speed <br> $(\mathrm{rpm})$ | Intake air <br> temperature <br> $($ Deg c) | Intake air <br> Pressure <br> $(\mathrm{kPa})$ | CA_Start of <br> Main HR <br> $($ aTDC | CA_End of <br> Main HR <br> (aTDC) | Heat <br> release <br> type | Fraction <br> of early <br> $(\%)$ | Fraction <br> of Late <br> $(\%)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | 20 | 26 | 800 | 101 | 112 | -2 | 15 | 4 | -1.1 | 20.5 |
| 30 | 20 | 10 | 800 | 40 | 95 | -1 | 11 | 1 | -0.1 | 16.1 |
| 30 | 20 | 14 | 800 | 40 | 95 | -2 | 9 | 3 | -0.8 | 24.7 |
| 30 | 20 | 17 | 800 | 40 | 95 | -4 | 10 | 4 | -1.0 | 22.1 |
| 30 | 20 | 21 | 800 | 40 | 96 | -2 | 8 | 4 | -0.1 | 20.4 |
| 30 | 20 | 28 | 800 | 40 | 96 | -2 | 8 | 1 | -1.1 | 16.2 |
| 40 | 20 | 12 | 1000 | 40 | 94 | -2 | 11 | 3 | 0.6 | 23.7 |
| 25 | 20 | 9 | 800 | 40 | 94 | 1 | 15 | 1 | -1.7 | 16.5 |
| 25 | 20 | 11 | 800 | 42 | 95 | 1 | 13 | 4 | -1.0 | 19.4 |
| 25 | 20 | 19 | 800 | 40 | 95 | 1 | 12 | 4 | -0.3 | 20.8 |
| 25 | 20 | 27 | 800 | 40 | 95 | 2 | 12 | 1 | -0.5 | 16.9 |
| 35 | 20 | 10 | 1000 | 39 | 94 | 3 | 20 | 1 | 0.6 | 15.3 |
| 35 | 20 | 14 | 1000 | 39 | 95 | 1 | 14 | 4 | 1.0 | 22.5 |
| 35 | 20 | 19 | 1000 | 40 | 95 | 0 | 14 | 4 | -0.1 | 21.3 |
| 35 | 20 | 28 | 1000 | 40 | 95 | 1 | 15 | 1 | -0.6 | 15.1 |
| 50 | 20 | 12 | 1200 | 40 | 94 | 3 | 14 | 5 | 5.2 | 25.3 |
| 50 | 20 | 15 | 1200 | 40 | 93 | 2 | 10 | 3 | 3.8 | 34.5 |
| 50 | 20 | 19 | 1200 | 40 | 94 | 0 | 12 | 4 | 1.9 | 21.4 |
| 50 | 20 | 28 | 1200 | 40 | 94 | 1 | 14 | 1 | 0.8 | 14.0 |
| 60 | 20 | 12.5 | 1400 | 39 | 93 | 4 | 17 | 2 | 8.3 | 21.7 |
| 60 | 20 | 14.8 | 1400 | 40 | 93 | 2 | 15 | 5 | 6.1 | 19.2 |
| 60 | 20 | 16.5 | 1400 | 40 | 93 | 1 | 12 | 5 | 5.3 | 18.9 |
| 60 | 20 | 18.5 | 1400 | 40 | 94 | 0 | 11 | 4 | 4.3 | 17.1 |
| 35 | 40 | 14 | 800 | 41 | 95 | 2 | 14 | 4 | 1.1 | 22.9 |
| 35 | 40 | 17 | 800 | 40 | 95 | 1 | 12 | 3 | 0.6 | 26.2 |


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| SOI <br> $(\mathrm{bTDC})$ | PR <br> $(\%)$ | Total Fuel <br> mass <br> $(\mathrm{mg} /$ cycle $)$ | Engine <br> Speed <br> $(\mathrm{rpm})$ | Intake air <br> temperature <br> $($ Deg c) | Intake air <br> Pressure <br> $(\mathrm{kPa})$ | CA_Start of <br> Main HR <br> $($ aTDC | CA_End of <br> Main HR <br> (aTDC) | Heat <br> release <br> type | Fraction <br> of early <br> $(\%)$ | Fraction <br> of Late <br> $(\%)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 20 | 10.1 | 800 | 60 | 94 | -1 | 14 | 4 | -2.4 | 19.2 |
| 20 | 20 | 13 | 800 | 60 | 95 | -2 | 14 | 3 | -2.4 | 26.2 |
| 20 | 20 | 18.5 | 800 | 60 | 95 | 0 | 14 | 3 | -1.1 | 23.8 |
| 20 | 20 | 22 | 800 | 60 | 95 | 3 | 14 | 4 | 0.1 | 22.1 |
| 20 | 20 | 27 | 800 | 60 | 95 | 2 | 17 | 4 | -1.3 | 17.4 |
| 25 | 20 | 9 | 1000 | 60 | 94 | 1 | 14 | 4 | -2.0 | 22.3 |
| 25 | 20 | 10 | 1000 | 59 | 94 | 1 | 14 | 4 | -1.7 | 21.8 |
| 25 | 20 | 13 | 1000 | 60 | 94 | 0 | 16 | 3 | -1.0 | 25.4 |
| 25 | 20 | 18 | 1000 | 60 | 94 | 1 | 15 | 3 | -1.0 | 24.8 |
| 25 | 20 | 22 | 1000 | 60 | 94 | 2 | 15 | 4 | -0.2 | 22.6 |
| 25 | 20 | 27 | 1000 | 60 | 94 | 2 | 17 | 4 | -1.1 | 19.3 |
| 35 | 20 | 10 | 1200 | 59 | 93 | 1 | 14 | 4 | 0.7 | 21.4 |
| 35 | 20 | 13 | 1200 | 60 | 93 | 1 | 15 | 3 | 1.1 | 26.1 |
| 35 | 20 | 17 | 1200 | 60 | 94 | 0 | 13 | 3 | -0.2 | 27.3 |
| 35 | 20 | 22 | 1200 | 60 | 93 | 0 | 13 | 3 | 0.0 | 24.1 |
| 35 | 20 | 27 | 1200 | 60 | 93 | 2 | 16 | 4 | -0.2 | 19.4 |
| 45 | 20 | 11 | 1400 | 59 | 93 | 1 | 14 | 4 | 2.6 | 21.9 |
| 45 | 20 | 12 | 1400 | 60 | 93 | 0 | 13 | 3 | 2.2 | 27.2 |
| 45 | 20 | 14 | 1400 | 60 | 93 | 0 | 12 | 3 | 1.7 | 26.2 |
| 45 | 20 | 18 | 1400 | 60 | 93 | -1 | 11 | 3 | 1.2 | 27.5 |
| 45 | 20 | 22 | 1400 | 60 | 93 | 0 | 13 | 3 | 0.7 | 24.0 |
| 45 | 20 | 27 | 1400 | 60 | 94 | -1 | 13 | 4 | -0.2 | 20.8 |
| 50 | 20 | 12 | 1600 | 60 | 93 | 3 | 17 | 3 | 3.8 | 27.5 |
| 50 | 20 | 14 | 1600 | 60 | 93 | 3 | 14 | 3 | 3.5 | 27.1 |
| 50 | 20 | 18 | 1600 | 60 | 93 | 2 | 16 | 3 | 2.0 | 25.0 |


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| $\begin{aligned} & \text { SOI } \\ & (\mathrm{bTDC}) \end{aligned}$ | PR <br> (\%) | Total Fuel mass (mg/cycle) | Engine Speed (rpm) | Intake air temperature (Deg c) | Intake air <br> Pressure <br> (kPa) | CA_Start of Main HR (aTDC) | CA_End of Main HR (aTDC) | Heat release type | Fraction of early (\%) | Fraction of Late (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 57 | 20 | 18 | 2000 | 80 | 95 | 0 | 11 | 3 | 1.4 | 30.7 |
| 57 | 20 | 22 | 2000 | 80 | 95 | 1 | 15 | 3 | 0.4 | 25.2 |
| 57 | 20 | 26 | 2000 | 80 | 95 | 1 | 17 | 4 | 0.0 | 21.6 |
| 65 | 20 | 12 | 2200 | 79 | 95 | 2 | 16 | 3 | 4.0 | 25.1 |
| 65 | 20 | 13 | 2200 | 80 | 95 | 1 | 14 | 3 | 3.6 | 28.1 |
| 65 | 20 | 17 | 2200 | 79 | 95 | 1 | 11 | 3 | 2.4 | 32.7 |
| 16 | 40 | 9.5 | 800 | 79 | 59 | -1 | 13 | 3 | -4.0 | 35.6 |
| 16 | 40 | 10.2 | 800 | 80 | 96 | -2 | 13 | 3 | -3.4 | 25.0 |
| 16 | 40 | 14 | 800 | 80 | 95 | -1 | 12 | 3 | -2.0 | 24.3 |
| 16 | 40 | 18 | 800 | 80 | 96 | 1 | 12 | 3 | -1.2 | 27.4 |
| 16 | 40 | 22 | 800 | 80 | 82 | 0 | 12 | 3 | -1.6 | 28.3 |
| 16 | 40 | 27 | 800 | 80 | 96 | 2 | 14 | 4 | -0.9 | 19.5 |
| 25 | 40 | 11.5 | 1000 | 80 | 96 | 0 | 13 | 3 | -1.1 | 26.6 |
| 25 | 40 | 13.5 | 1000 | 80 | 96 | 0 | 16 | 3 | -1.3 | 24.2 |
| 25 | 40 | 18 | 1000 | 80 | 95 | 0 | 15 | 3 | -0.9 | 27.6 |
| 25 | 40 | 22 | 1000 | 80 | 95 | 0 | 15 | 3 | -0.9 | 26.3 |
| 25 | 40 | 26.5 | 1000 | 80 | 90 | 2 | 16 | 4 | -0.6 | 22.5 |
| 35 | 40 | 11.7 | 1200 | 79 | 94 | 0 | 14 | 3 | 0.2 | 26.1 |
| 35 | 40 | 13.5 | 1200 | 80 | 95 | 0 | 14 | 3 | 0.7 | 25.3 |
| 35 | 40 | 18 | 1200 | 80 | 98 | 0 | 13 | 3 | 0.7 | 28.7 |
| 35 | 40 | 22 | 1200 | 80 | 95 | -1 | 15 | 3 | 0.2 | 24.6 |
| 35 | 40 | 26.5 | 1200 | 80 | 95 | 1 | 16 | 4 | 0.1 | 19.9 |
| 40 | 40 | 12 | 1400 | 79 | 94 | 1 | 15 | 3 | 1.5 | 26.3 |
| 40 | 40 | 14.3 | 1400 | 80 | 94 | 1 | 13 | 3 | 1.4 | 27.8 |
| 40 | 40 | 18 | 1400 | 80 | 95 | 0 | 13 | 3 | 0.6 | 31.0 |


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| SOI <br> $(\mathrm{bTDC})$ | PR <br> $(\%)$ | Total Fuel <br> mass <br> $(\mathrm{mg} /$ cycle $)$ | Engine <br> Speed <br> $(\mathrm{rpm})$ | Intake air <br> temperature <br> (Deg c) | Intake air <br> Pressure <br> $(\mathrm{kPa})$ | CA_Start of <br> Main HR <br> $($ aTDC $)$ | CA_End of <br> Main HR <br> (aTDC) | Heat <br> release <br> type | Fraction <br> of early <br> $(\%)$ | Fraction <br> of Late <br> $(\%)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 52 | 60 | 28.5 | 1400 | 80 | 93 | 2 | 14 | 1 | 2.2 | 13.9 |
| 60 | 60 | 20.5 | 1600 | 80 | 94 | 1 | 15 | 4 | 2.5 | 22.9 |
| 60 | 60 | 23 | 1600 | 80 | 94 | 2 | 16 | 1 | 2.9 | 16.6 |
| 60 | 60 | 26 | 1600 | 80 | 94 | 2 | 17 | 1 | 2.7 | 12.9 |
| 60 | 60 | 31 | 1600 | 80 | 94 | 5 | 17 | 1 | 2.8 | 9.0 |
| 70 | 60 | 22 | 1800 | 79 | 94 | 5 | 21 | 4 | 3.5 | 19.4 |
| 70 | 60 | 24 | 1800 | 80 | 93 | 4 | 19 | 4 | 3.1 | 17.3 |
| 70 | 60 | 28 | 1800 | 80 | 93 | 5 | 21 | 1 | 3.0 | 11.2 |
| 70 | 60 | 31 | 1800 | 80 | 94 | 7 | 21 | 1 | 3.6 | 8.1 |
| 15 | 20 | 10 | 800 | 100 | 96 | -2 | 12 | 4 | -3.9 | 20.4 |
| 15 | 20 | 13 | 800 | 100 | 95 | -2 | 12 | 3 | -2.6 | 24.2 |
| 15 | 20 | 18 | 800 | 100 | 99 | 0 | 11 | 3 | -2.0 | 23.2 |
| 15 | 20 | 22 | 800 | 101 | 95 | 0 | 14 | 4 | -1.6 | 18.8 |
| 15 | 20 | 26 | 800 | 101 | 95 | 1 | 15 | 1 | -1.8 | 16.9 |
| 20 | 20 | 10.3 | 1000 | 100 | 96 | -2 | 13 | 4 | -2.4 | 22.2 |
| 20 | 20 | 13 | 1000 | 100 | 95 | 1 | 16 | 3 | -1.6 | 25.5 |
| 20 | 20 | 18 | 1000 | 100 | 95 | 2 | 17 | 3 | -1.6 | 23.7 |
| 20 | 20 | 22 | 1000 | 100 | 95 | 4 | 19 | 4 | -1.3 | 20.6 |
| 20 | 20 | 26 | 1000 | 100 | 96 | 5 | 21 | 4 | -1.2 | 17.6 |
| 28 | 20 | 10.7 | 1200 | 99 | 94 | -3 | 12 | 3 | -2.1 | 23.5 |
| 28 | 20 | 12.7 | 1200 | 100 | 94 | -1 | 14 | 3 | -1.3 | 27.3 |
| 28 | 20 | 18 | 1200 | 100 | 95 | 0 | 15 | 3 | -1.4 | 24.8 |
| 28 | 20 | 22 | 1200 | 100 | 95 | 1 | 16 | 4 | -0.6 | 22.6 |
| 28 | 20 | 26 | 1200 | 99 | 95 | 2 | 19 | 4 | -0.8 | 19.0 |
| 33 | 20 | 11.2 | 1400 | 100 | 81 | -2 | 10 | 3 | -0.9 | 29.9 |


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| SOI <br> $(\mathrm{bTDC})$ | PR <br> $(\%)$ | Total Fuel <br> mass <br> $(\mathrm{mg} /$ cycle $)$ | Engine <br> Speed <br> $(\mathrm{rpm})$ | Intake air <br> temperature <br> $($ Deg c) | Intake air <br> Pressure <br> $(\mathrm{kPa})$ | CA_Start of <br> Main HR <br> $($ aTDC $)$ | CA_End of <br> Main HR <br> $($ aTDC $)$ | Heat <br> release <br> type | Fraction <br> of early <br> $(\%)$ | Fraction <br> of Late <br> $(\%)$ |
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| 40 | 20 | 15 | 1000 | 40 | 101 | -2 | 8 | 4 | 1.3 | 21.8 |
| 40 | 20 | 18 | 1000 | 40 | 101 | -3 | 8 | 4 | 0.7 | 21.1 |
| 40 | 20 | 22 | 1000 | 40 | 102 | -3 | 8 | 4 | 0.8 | 17.8 |
| 40 | 20 | 29 | 1000 | 40 | 102 | -1 | 10 | 1 | 0.5 | 11.6 |
| 30 | 20 | 12.5 | 1000 | 40 | 96 | 0 | 13 | 3 | -9.5 | 31.8 |
| 30 | 20 | 15 | 1000 | 40 | 96 | 0 | 13 | 3 | -0.4 | 24.1 |
| 30 | 20 | 17 | 1000 | 40 | 97 | 0 | 14 | 4 | -0.4 | 22.6 |
| 30 | 20 | 19 | 1000 | 40 | 96 | -1 | 13 | 4 | -0.9 | 22.8 |
| 30 | 20 | 22 | 1000 | 40 | 96 | 1 | 14 | 4 | -0.5 | 20.7 |
| 30 | 20 | 29 | 1000 | 40 | 96 | 2 | 15 | 1 | -0.6 | 15.9 |
| 20 | 20 | 13 | 1000 | 40 | 96 | 4 | 23 | 4 | -1.3 | 21.7 |
| 20 | 20 | 15 | 1000 | 40 | 96 | 5 | 26 | 4 | -1.2 | 20.4 |
| 20 | 20 | 17 | 1000 | 40 | 96 | 6 | 25 | 4 | -1.1 | 20.8 |
| 20 | 20 | 22 | 1000 | 40 | 96 | 5 | 27 | 4 | -0.8 | 17.2 |
| 20 | 20 | 28 | 1000 | 40 | 96 | 5 | 31 | 1 | -1.0 | 12.6 |
| 100 | 30 | 16 | 1000 | 40 | 96 | 0 | 15 | 2 | 9.7 | 7.6 |
| 100 | 30 | 18 | 1000 | 40 | 95 | 0 | 14 | 2 | 8.7 | -0.9 |
| 80 | 30 | 14 | 1000 | 40 | 95 | 1 | 30 | 2 | 9.7 | 5.9 |
| 80 | 30 | 17 | 1000 | 40 | 95 | 0 | 12 | 2 | 9.1 | 2.8 |
| 80 | 30 | 19 | 1000 | 40 | 96 | 0 | 10 | 2 | 9.1 | -3.6 |
| 60 | 30 | 13.5 | 1000 | 40 | 96 | -1 | 17 | 5 | 6.0 | 11.7 |
| 60 | 30 | 15 | 1000 | 40 | 95 | -1 | 13 | 2 | 7.5 | 9.0 |
| 60 | 30 | 17 | 1000 | 40 | 96 | -1 | 9 | 5 | 5.9 | 6.3 |
| 60 | 30 | 19 | 1000 | 40 | 95 | -1 | 8 | 5 | 5.5 | 3.8 |
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| SOI <br> $(\mathrm{bTDC})$ | PR <br> $(\%)$ | Total Fuel <br> mass <br> $(\mathrm{mg} /$ cycle $)$ | Engine <br> Speed <br> $(\mathrm{rpm})$ | Intake air <br> temperature <br> $($ Deg c) | Intake air <br> Pressure <br> $(\mathrm{kPa})$ | CA_Start of <br> Main HR <br> $($ aTDC $)$ | CA_End of <br> Main HR <br> $($ aTDC $)$ | Heat <br> release <br> type | Fraction <br> of early <br> $(\%)$ | Fraction <br> of Late <br> $(\%)$ |
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| 40 | 40 | 40 | 1000 | 40 | 97 | 8 | 27 | 1 | 0.6 | 4.6 |
| 20 | 40 | 13 | 1000 | 40 | 96 | 9 | 29 | 4 | 0.6 | 19.6 |
| 20 | 40 | 20 | 1000 | 40 | 96 | 7 | 28 | 4 | 0.1 | 20.9 |
| 20 | 40 | 30 | 1000 | 40 | 96 | 8 | 27 | 4 | 0.4 | 19.4 |
| 20 | 40 | 33 | 1000 | 40 | 96 | 8 | 29 | 1 | 0.3 | 15.2 |
| 30 | 40 | 12.5 | 1000 | 40 | 96 | 3 | 18 | 4 | 1.4 | 21.7 |
| 30 | 40 | 18.5 | 1000 | 40 | 96 | 1 | 14 | 3 | 1.1 | 27.9 |
| 30 | 40 | 24.5 | 1000 | 40 | 96 | 2 | 12 | 3 | 0.6 | 27.7 |
| 30 | 40 | 35.5 | 1000 | 40 | 96 | 6 | 22 | 1 | 0.5 | 7.4 |
| 30 | 40 | 37.5 | 1000 | 40 | 96 | 9 | 32 | 1 | 0.6 | 5.9 |
| 40 | 60 | 20 | 1000 | 40 | 96 | 1 | 12 | 3 | 1.1 | 31.8 |
| 40 | 60 | 22 | 1000 | 40 | 96 | 1 | 12 | 3 | 1.3 | 30.7 |
| 40 | 60 | 24 | 1000 | 40 | 96 | 2 | 13 | 3 | 1.2 | 23.7 |
| 40 | 60 | 26 | 1000 | 40 | 97 | 2 | 13 | 4 | 1.1 | 21.7 |
| 40 | 60 | 28 | 1000 | 40 | 96 | 3 | 14 | 4 | 0.9 | 18.0 |
| 60 | 60 | 19 | 1000 | 40 | 95 | 1 | 19 | 1 | 3.0 | 11.7 |
| 60 | 60 | 20 | 1000 | 40 | 96 | 2 | 19 | 1 | 3.4 | 8.6 |
| 60 | 60 | 22 | 1000 | 40 | 96 | 3 | 21 | 1 | 3.6 | 6.5 |
| 60 | 60 | 25 | 1000 | 40 | 96 | 3 | 18 | 1 | 2.7 | 7.4 |
| 80 | 60 | 20 | 1000 | 40 | 96 | 2 | 21 | 1 | 4.6 | 9.7 |
| 80 | 60 | 22 | 1000 | 40 | 96 | 2 | 12 | 3 | 4.1 | 48.2 |
| 40 | 20 | 11 | 1000 | 60 | 97 | 2 | 17 | 1 | -0.5 | 12.7 |
| 40 | 20 | 12 | 1000 | 60 | 96 | -1 | 12 | 1 | -0.1 | 13.8 |
| 40 | 20 | 14 | 1000 | 60 | 98 | -2 | 8 | 1 | 0.3 | 16.6 |


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| $\begin{aligned} & \text { SOI } \\ & \text { (bTDC) } \end{aligned}$ | $\begin{aligned} & \text { PR } \\ & (\%) \end{aligned}$ | Total Fuel mass <br> (mg/cycle) | Engine Speed (rpm) | Intake air temperature (Deg c) | Intake air Pressure (kPa) | CA_Start of Main HR (aTDC) | CA_End of Main HR (aTDC) | Heat release type | Fraction of early (\%) | Fraction of Late (\%) |
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| 80 | 60 | 22.5 | 1000 | 80 | 97 | -2 | 12 | 1 | 2.8 | 0.8 |
| 80 | 60 | 25.5 | 1000 | 80 | 96 | 0 | 10 | 1 | 2.9 | 0.8 |
| 20 | 60 | 20.4 | 1000 | 80 | 97 | 3 | 15 | 3 | -1.3 | 33.7 |
| 20 | 60 | 21.5 | 1000 | 80 | 97 | 2 | 15 | 3 | -1.7 | 34.9 |
| 20 | 60 | 24 | 1000 | 80 | 97 | 2 | 15 | 3 | -1.5 | 34.2 |
| 20 | 60 | 28 | 1000 | 80 | 97 | 5 | 18 | 3 | -1.1 | 27.4 |

## Appendix B

## LTC engine model data used for

## LPV-SVM system identification

In the below set of data engine speed was set constant to 1000 rpm , intake manifold temperature was set to $60^{\circ} \mathrm{C}$ and Intake manifold pressure was set to 96.5 kPa . The data was generated by using a physics based LTC engine plant [5].

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| Cycle <br> number | SOI <br> $(\mathrm{bTDC})$ | FQ <br> $(\mathrm{mg} / \mathrm{cycle})$ | PR <br> $(\%)$ | Fraction of <br> early HR <br> modelled (\%) | Fraction of <br> late HR <br> modelled (\%) | CA50 <br> $($ aTDC $)$ | MPRR <br> $(\mathrm{bar} / \mathrm{CAD})$ | Tsoc <br> $(\mathrm{K})$ | Psoc <br> $(\mathrm{kPa})$ | IMEP <br> $(\mathrm{kPa})$ |
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| 293 | 40.1 | 18 | 39.4 | 2.3 | 24 | 13.5 | 5.1 | 736 | 1846 | 533 |
| 294 | 40.1 | 18 | 39.5 | 2.3 | 24 | 13.8 | 5.1 | 737 | 1851 | 533 |
| 295 | 39.5 | 18 | 39.6 | 2.2 | 24.4 | 13.8 | 5 | 737 | 1851 | 533 |
| 296 | 39 | 18 | 39.8 | 2.1 | 24.7 | 14.1 | 4.9 | 737 | 1855 | 534 |
| 297 | 39 | 18 | 39.8 | 2.1 | 24.7 | 14.4 | 4.9 | 738 | 1860 | 534 |
| 298 | 38.5 | 18 | 39.9 | 2.1 | 25 | 14.4 | 4.9 | 738 | 1860 | 534 |
| 299 | 38.5 | 18 | 40 | 2.1 | 25 | 14.7 | 4.9 | 738 | 1864 | 534 |
| 300 | 37.6 | 18 | 40 | 1.9 | 25.6 | 14.7 | 4.7 | 738 | 1864 | 534 |
| 301 | 37.6 | 18 | 40 | 1.9 | 25.6 | 15 | 4.7 | 739 | 1868 | 534 |
| 302 | 37.3 | 18 | 40 | 1.9 | 25.7 | 15 | 4.6 | 739 | 1868 | 534 |
| 303 | 37.3 | 18 | 40 | 1.9 | 25.7 | 15.2 | 4.6 | 739 | 1870 | 534 |
| 304 | 37 | 19.3 | 39.9 | 1.8 | 25.2 | 15.2 | 4.9 | 739 | 1870 | 534 |
| 305 | 37 | 19.3 | 39.8 | 1.8 | 25.2 | 15.2 | 4.9 | 739 | 1872 | 569 |
| 306 | 36.8 | 20.5 | 39.8 | 1.7 | 24.4 | 15 | 5.2 | 740 | 1870 | 563 |
| 307 | 36.8 | 20.5 | 39.6 | 1.7 | 24.4 | 15.2 | 5.2 | 741 | 1873 | 595 |
| 308 | 36.6 | 21.8 | 39.5 | 1.6 | 23.4 | 15 | 5.6 | 741 | 1871 | 590 |
| 309 | 36.6 | 23 | 39.4 | 1.6 | 22.2 | 14.9 | 5.9 | 742 | 1871 | 623 |
| 310 | 36.6 | 23 | 39.2 | 1.6 | 22.2 | 14.9 | 5.9 | 743 | 1871 | 650 |
| 311 | 36.6 | 24 | 39 | 1.5 | 21.1 | 14.7 | 6.2 | 744 | 1869 | 643 |
| 312 | 36.6 | 24 | 38.8 | 1.5 | 21 | 14.4 | 6.2 | 744 | 1867 | 669 |
| 313 | 36.6 | 25 | 38.6 | 1.4 | 19.8 | 14.4 | 6.5 | 745 | 1867 | 664 |
| 314 | 36.6 | 25 | 38.4 | 1.4 | 19.8 | 14.3 | 6.5 | 745 | 1865 | 690 |
| 315 | 36.7 | 26 | 38.1 | 1.4 | 18.4 | 14.1 | 6.8 | 745 | 1865 | 685 |
| 316 | 36.7 | 26 | 37.8 | 1.3 | 18.4 | 14 | 6.8 | 745 | 1863 | 710 |
| 317 | 36.9 | 27 | 37.5 | 1.3 | 16.9 | 13.8 | 7.1 | 746 | 1861 | 705 |


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## Appendix C

## Mode Frontier

## C.0.0.1 Optimization of hyper parameters of LS-SVM

Optimization of hyper parameters used to build the LPV-SVM model in Section 5.1.3.1 and Section 6.2 are carried out by using an optimization tool named Mode Frontier. Mode Frontier is a multi objective optimization tool. It is a multidisciplinary optimization software developed by an Italian software house ESTECO SpA.

In simpler terms, design of experiments is generated by the tool based on the chosen optimization algorithm. Each combination of design input parameters i.e. the hyper parameters are fed to the design software and the outputs,i.e. the RMSE associated
with prediction of $\mathrm{CA}_{50}$, IMEP and MPRR are received back by the tool. Based on the optimization condition and objective set on the outputs, subsequent experiments are redesigned. Optimization of hyper parameters for LPV-SVM model, is carried out with Mode Frontier tool tied up with MATLAB LS-SVM code. Every combination of hyper parameters are evaluated for minimization of RMSE of $\mathrm{CA}_{50}$, IMEP and MPRR prediction. The process is iterated till the maximum number of iterations are reached. Non-dominant sorting genetic algorithm (NSGA) is an extension of genetic


Figure C.1: Work flow of Mode Frontier tool
algorithm for optimization of multiple objective problem. Its is an adaptive algorithm, keeps redefining the inputs based on current population of data to optimise for the objectives. 4000 number of iterations are run for the model to optimise. If the result needs further improvement, the best design from current iterations are chosen and fed as initial combination for the next 4000 iterations.


Figure C.2: Hyper parameters tuned in Mode Frontier for LPV- SVM model from Section 6.2

Figure C.2 is an example of the hyper parameters tuned for 6.2. Seven different kernel functions are used and they are linear function, radial basis function, polynomial function, sigmoid function, multi quadratic function, inverse multi quadratic function and rational multi quadratic function. Mode Frontier could choose one of it. The kernel functions are defined "unordered" for arrangement with a step size of 1 . This helps the Mode Frontier tool to understand that each kernel function is independent of another even though they are numbered in a sequence. Other parameters sigma, multiplier, regularization parameter defined for the states and output are defined as "ordered" for arrangement. Range of these parameters were arrived by trial and error in order to provide a wide operating range for the Mode Frontier tool for optimization. The range of parameters are defined in the Mode Frontier, to optimize are defined in

Table C. 1
Range of hyper parameters defined in Mode Frontier

|  | Name | Minimum | Maximum |
| :--- | :--- | :--- | :--- |
| 1 | Kernel Function | 1 | 7 |
| 2 | Sigma | 0 | 1000 |
| 3 | Multiplier | 0 | 1000 |
| 4 | Regularization parameter on states | 0 | 1000000 |
| 5 | Regularization parameter on output | 0 | 1000000 |

Table C.1. For optimization, objective function is defined on the output parameters.

For the LPV- SVM model minimization objective was set on the RMSE of $\mathrm{CA}_{50}$, IMEP and MPRR prediction, shown in Figure C.3. The downward arrow attached to RMSE of $\mathrm{CA}_{50}$, IMEP and MPRR represents minimization.


Figure C.3: Hyper parameters tuned in Mode Frontier for LPV- SVM model from Section 6.2

## Appendix D

## Hyper Parameters Used for

## System Identification

The combination of hyper parameters used for system identification of $\mathrm{A}, \mathrm{B}, \mathrm{C}$ from Chapter5, Section 5.1.3.2 is listed in Table D. 1

Table D. 1
Table of hyper parameters for System Identification with A,B and C matrices

| Parameters | Value |
| :---: | :---: |
| Kernel Function A | Inverse multiquadratic function |
| Kernel function B | Radial basis function |
| Kernel Function C | Inverse multiquadratic function |
| Sigma A | 915.2 |
| Sigma B | 445.2 |
| Sigma C | 151.9 |
| Multiplier A | 74.47 |
| Multiplier B | 445.9 |
| Multiplier C | 443.5 |
| Regularisation parameter CA50 | 422210 |
| Regularisation parameter MPRR | 401080 |
| Regularization parameter Tsoc | 387890 |
| Regularization parameter Psoc | 424120 |
| Regularization parameter IMEP | 137420 |
| Regularization Parameter_output CA50 | 3.8 |
| Regularization parameter_output_MPRR | 5.5 |
| Regularization parameter_output_IMEP | 8.0 |

## Appendix E

## Program and data files summary

## E. 1 Chapter 1

Table E. 1
Figure Files

| File | Description |
| :--- | :--- |
| Equivalence ratio to temp.png | File of Figure 1.1 |

Table E. 2
Visio Files

| File | Description |
| :--- | :--- |
| Chapter1_intro_flowchart.vsdx | Visio file of Figure 1.2 |
| Content_thesis.vsdx | Visio file of Figure |
| 1.3 |  |

## E. 2 Chapter 2

Table E. 3
Figure Files

| File | Description |
| :--- | :--- |
| New_LTC_Engine_Setup.png | File of Figure $\overline{2.1}$ |
| Data_Setup.png | File of Figure $\overline{\overline{2.2}}$ |

## E. 3 Chapter 3

Table E. 4
Matlab Data File

| Data File | Description |
| :--- | :--- |
| Combined_data_RCCI_Nitin |  |
| _Kaushik_data.mat | Data used for classification |

Table E. 5
Matlab code Files

| File Name | Description |
| :--- | :--- |
| find_peaks_rev3.m | Matlab code used to analyse and <br> perform rule- based classification <br> Matlab code used to plot classified traces |
| Classification_plot.m | Matlab code used to analyse combustion <br> Plot_normal_dist_rev1.m <br> parameters <br> characteristics of classified traces |
| Decision_tree_5_bin.m | Matlab code used to create Decision <br> tree model |
| Shifting_HRR_trace_rev1.m | Matlab code for shifting and normalising <br> heat release rate |
| HRR_K_Means_5_bin.m | to evaluate traces for k-means <br> Matlab code to do k-means classification |

Table E. 6
Python code

| File | Description |
| :--- | :--- |
| regimeClass.py | Python code used to build CNN model |

Table E. 7
Visio Files

| File | Description |
| :--- | :--- |
| Classification_flow_chart.vsdx | Visio file of the Figure 3.2 |

Table E. 8
Figure Files

| File | Description |
| :--- | :--- |
| flow_chart.png | Figure 3.3 |
| emission_01.png | Figure 3.12 |
| emission_02.png | Figure $\overline{3.13}$ |
| emission_03.png | Figure 3.14 |
| emission_04.png | Figure |
| emission_05.png | Figure |
| Presentation_CNN.png | Figure |
| CNN_data_size.png | Figure |
| CNN_Prediction_summary.png | Figure |
| Decision_tree.png | Figure |
| decision_tree_Prediction_summary.png | Figure |
|  |  |

Table E. 9
Matlab Figure Files

| File | Description |
| :--- | :--- |
| heat release_C3.fig | Figure 3.1 |
| Combustion regime_plot_rev1.fig | Figure 3.3 |
| cov_imep.fig | Figure 3.3 |
| P_max_kPa.fig | Figure 3.5 |
| MPRR.fig | Figure 3.6 |
| CA_10_HR.fig | Figure $\overline{3.7}$ |
| CA_90_HR.fig | Figure $\overline{3.8}$ |
| IN_cy_Temp.fig | Figure 3.3 |
| T_SOM_K.fig | Figure $\overline{3.10}$ |
| T_EOM_K.fig | Figure 3.11 |
| kmeans_5bin.fig | Figure 3.2 |

## E. 4 Chapter 4

Table E. 10
Matlab code

| Data File | Description |
| :--- | :--- |
| Plot_scatter.m | Matlab code for plotting Figure 4.1 |

Table E. 11
Figures

| Data File | Description |
| :--- | :--- |
| 3clusters_exp_0.fig | Figure 4.1 |

Table E. 12
Rstudio data and Code

| Data File | Description |
| :--- | :--- |
| R_data_rev5_2804_type1_2_3.csv | Data with 3 clusters for PCA <br> and Linear regression |
| project.R | RStudio code for PCA and |
|  | Linear regression Table 4.1, 4.2 |
| Plot_scatter.m | Matlab code for Figure 4.1 |

## E. 5 Chapter 5

Table E. 13
Matlab code

| Data File | Description |
| :--- | :--- |
| sch_par_model_mF_script_ver5_ABC.m | Matlab code for SVM- modelling of the |
| and its sub functions | system with ABC matrices and to <br> generate Figure 5.1 to 5.4 |
| contourplot_matrix_v2_2sch_var.m | Matlab code for generating contour plot <br> of figure 5.5 to 5.7 |

Table E. 14
Data file

| Data File | Description |
| :--- | :--- |
| LPV_data_Aditya.mat | Dataset used to train SVM- LPV model and test it. |

Table E. 15
Figure files

| Data File | Description |
| :--- | :--- |
| Input_1.fig | Figure 5.1 |
| States.fig | Figure |
| scheduling_parameter.fig | Figure |
| normalised_Output_ABC.fig | Figure |
| n.4. |  |
| A_matrix_ABC.fig | Figure |
| B_matrix_ABC.fig | Figure |
| C_matrix_ABC.fig | Figure |
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## E. 6 Chapter 6

Table E. 16
Figure files

| Filename | Description |
| :--- | :--- |
| Comparison_P1_P2_set2range_CA50.fig | Figure 6.1 |
| Comparison_P1_P2_set2range_IMEP.fig | Figure 6.2 |
| Comparison_P1_P2_set2range_MPRR.fig | Figure 6.6 |
| MPC Control Model Schematic_0108_rev1.png | Figure 6.6 |
| Case1.fig | Figure 6.5 |
| Case2.fig | Figure 6.6 |
| Case1_dist.fig | Figure 6.7 |
| Case4_comp.fig | Figure 6.8 |
| Case4.fig | Figure 6.9 |
| Case3.fig | Figure 6.10 |

Table E. 17
Visio files

| Filename | Description |
| :--- | :--- |
| MPC Control Model Schematic_0108_rev1.vsdx | File for the Figure 6.4 |

Table E. 18
Matlab code

| File name | Description |
| :--- | :--- |
| Simulate_LPV_model.m | Simulink model to evaluate model accuracy |
| Surface_plot_prediction.m | Matlab code to create surface plots <br> from Figure 6.1 to Figure 6.3 |
|  |  |

Table E. 19
Simulink files

| File name | Description |
| :--- | :--- |
| LPV_SVM_prediction.slx | Simulink for evaluating model accuracy |
| LPV_MPC_rev6.slx | Simulink with the designed MPC controller |

Table E. 20
Matlab Data

File name
model_verification_set_to_Range.mat Steady state data of model
Description and RCCI engine
MPC_opt_workspace_rev9_thesis.mat Matlab parameters for running MPC

## E. 7 Chapter 7

Table E. 21
Figure file

| File name | Description |
| :--- | :--- |
| Future_work.png | Figure 7.1 |

## E. 8 Appendix A

Table E. 22
Data file

| File name | Description |
| :--- | :--- |
| Combined_data_RCCI_Nitin |  |
| _Kaushik_data.mat | Data used for classification of HRR |

## E. 9 Appendix B

Table E. 23
Data file

| File name | Description |
| :--- | :--- |
| LPV_data_Aditya.mat | Data used for LPV-SVM <br> identification of LTC engine |

## E. 10 Appendix C

Table E. 24
Figure file

| File name | Description |
| :--- | :--- |
| Mode frontier.png | Figure C.1 |
| mode_frontier_2.png | Figure $\overline{\text { C.2 }}$ |
| output_constraints.png | FigureC.3 |

