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Stresses induced by a demolition agent in non-explosive rock fracturing

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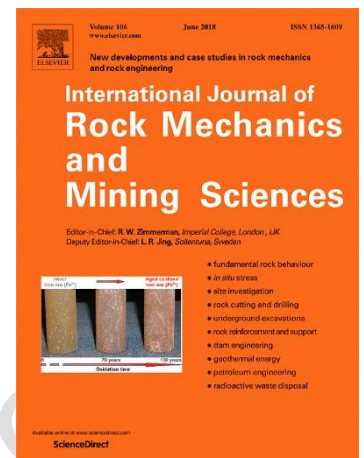
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Abstract

Stresses induced by a demolition agent in non-explosive rock fracturing was analysed using the theory of elasticity and the thick-walled cylinder principle. Circumferential and radial stresses in rock induced by an internally pressurized hole was first analysed under plane strain condition. Stresses perpendicular to the line connecting two adjacent holes were calculated based on coordinate transformation. A parametric study was carried out to investigate the influence of spacing and size of hole on the stress distribution. The analytical model provides a method to determine the optimum hole spacing and size as well as the time needed for fracturing rocks with properties similar to those employed to determine the pressure-time function of the demolition agent. It is found that tensile stress decreased dramatically with the increasing of hole spacing, while it increased with increment of hole size but the influence of spacing on stress changes was more significant than that of hole size. It is also concluded from the study that tensile stress in the middle of two holes decreased dramatically with a logarithmic distribution when solely increasing hole spacing. As can be anticipated more time is required for rock fracturing and breaking when hole spacing is increased for both soft and hard rocks.

Key works: Stress; Non-explosive rock fracturing; Rock engineering; Demolition agent; Analytical solution



37 1. Introduction

38 Non-explosive rock fracturing has been widely used in rock engineering projects
39 such as quarry, mining, underground infrastructure construction and rock slope
40 engineering. Fig. 1a shows a rock slope formed by a demolition agent (DA) at the
41 Castle Peak Road in Hong Kong where blasting may pose a significant threat to
42 human safety and was not allowed. An underground tunnel was excavated by a
43 PRS-95 hydraulic splitter in the construction of the Mass Transit Railway (Admiralty
44 section, Hong Kong) (see Fig. 1b). The major advantage of this “silent” rock
45 fracturing method is no fly rock, no vibration and controllability.

46 Despite the significant growth in the use of the controlled rock fracturing method,
47 more guidance for design of hole patterns in practical rock engineering would be
48 helpful. Spacing and diameter of holes are often empirically determined for a certain
49 lithology and requirement. Diameter of holes are generally recommended between
50 30 and 65 mm depending on rock property, with a spacing of holes generally ranging
51 from 200 to 1000 mm¹.

52 An empirical model was developed based on dimensional and polynomial
53 regression analysis to determine hole spacing². Gómez and Mura³ investigated the
54 relationship between hole diameter (l) and hole spacing (d) and concluded that
55 spacing is proportional to diameter which can be written as $d=kl$. In that study, the
56 value of k was experimentally determined as: $k<8$ for hard rock, $8<k<12$ for medium
57 hard rock and $12<k<18$ for soft rock.

58 Dowding and Labuz⁴ reported that temperature and thermal sensitivity of rock
59 material could influence hole spacing, and an optimum spacing of 8 times hole
60 diameter was proposed. Natanzi et al.⁵ experimentally investigated demolition of
61 masonry walls using DA. An optimum hole pattern with a d/l of 57 and a spacing of
62 225 mm was reported. Actually, these studies ignored the influence of time on
63 fracturing when investigating the relationship between spacing and diameter.

64 Knowledge of pressure from DA has a great importance for an improved
65 understanding of rock fracturing. An experimental methodology to determine the
66 internal pressure of a single hole under an expansive load has been reported by
67 measuring the tangential strain on the external boundary of a pipe wall that was
68 internally pressurized⁶. In that study, the pressure was suggested to be calculated
69 taking into account three independent parameters including hole diameter, loading
70 time and Young's modulus. The research however failed to consider the interactions

71 of neighbouring holes under expansive loads, which is very common in practical rock
72 engineering.

73 There have been some publications regarding the stresses around holes in an
74 infinite plate. Ling⁷ investigated the stresses in a plate containing two equal circular
75 holes. The aim of that study was to introduce a theoretical solution of stresses along
76 the edges of holes under external tension load. Haddon⁸ studied the stresses around
77 two unequal holes in an infinite plate using the conformal mapping and complex
78 variable methods. Based upon the Love's stress function, Ling et al.⁹ presented an
79 analytical solution for the stresses in a thick plate containing a cavity with a zero
80 surface stress. The aforementioned investigations succeeded in formulating
81 analytical solutions for stresses around holes but none of these researches can be
82 directly used to understand the stress distribution by DA when fracturing rock
83 because of the time dependent nature of the expansive pressure. On the other hand,
84 in the application of DA, stress concentration often occur around a hole^{10; 11; 12} under
85 incremental static loading in rock, which will lead to the initiation and coalescence of
86 fracture between adjacent holes¹³.

87 The aim of this paper is to investigate stresses between two neighbouring holes
88 under incremental expansive pressure from DA. A mathematical model comprising
89 two internally pressurized holes was developed and influential factors including hole
90 layout, loading time and rock property were taken into account. The relationships
91 between optimum hole spacing and size which can used as a guidance for design of
92 hole patterns in practical rock engineering were respectively derived for hard and
93 soft rocks.

94 **2. Non-explosive demolition agent**

95 The non-explosive DA in this paper refers to a commercially available chemical
96 powder which can expand considerably on mixing with water. In rock engineering,
97 circular holes are drilled and terminated within rock masses and these pre-drilled
98 holes are then filled with a mixture of DA and water at the recommended ratio (3.3
99 Kg/L). The DA hardens gradually and expands to fracture rock, typically over 24
100 hours¹⁵. The interaction mechanism of two adjacent holes with DA is illustrated in
101 Fig. 2. Tensile stress perpendicular to the line connecting the two holes is generated
102 by compression (due to the expansion of the DA within the holes); and the rock
103 material in between will be fractured when the tensile stress exceeds the tensile
104 strength of the rock.

105 3. Mathematical model and analysis

106 3.1 Stresses around a single internally pressurized hole

107 In this paper, the stresses arising from the interaction of two neighbouring holes
108 is focused. Fig. 3 shows two symmetrical holes internally pressurised and the
109 stresses acting on an element arising from Hole 2 in a polar coordinate. Assuming
110 the two symmetrical holes with an equal radius of r_i are drilled in an elastic-plastic
111 rock media. The DA is injected into the pre-drilled holes. The pressure (p) generated
112 from the DA acts on the inside wall of the holes. The problem could be simplified as
113 the interaction of two thick-walled rock cylinders internally pressurised. For the
114 assumed cylinder, the inner radius is r_i and the outer radius r_o equals to the hole
115 spacing (d , from centre).

116 The pre-drilled Hole 2 and the surrounding rock material can be treated like a
117 pressurised cylinder (Fig.3), and this problem can be simplified to plane strain state
118 assuming the hole depth is infinite. In polar coordinates, the general stress equations
119 of equilibrium without body force based on theory of elasticity can be given as¹⁶:

$$\begin{aligned} \frac{\partial \sigma_r}{\partial r} + \frac{1}{r} \frac{\partial \tau_{r\theta}}{\partial \theta} + \frac{\partial \tau_{r0}}{\partial 0} + \frac{\sigma_r - \sigma_\theta}{r} &= 0 \\ \frac{\partial \tau_{\theta r}}{\partial r} + \frac{1}{r} \frac{\partial \tau_\theta}{\partial \theta} + \frac{\partial \tau_{\theta 0}}{\partial 0} + 2 \frac{\tau_{\theta r}}{r} &= 0 \\ \frac{\partial \tau_{0r}}{\partial r} + \frac{1}{r} \frac{\partial \tau_{0\theta}}{\partial \theta} + \frac{\partial \sigma_0}{\partial 0} + \frac{\tau_{0r}}{r} &= 0 \end{aligned} \quad (1)$$

121 where r is the radius and θ is the azimuth in polar coordinates; the direction of σ_0 is
122 perpendicular to the yz plane.

123 In the plane strain situation, the expand of hole surface is free, thus:

$$124 \quad \sigma_0 = 0 \quad (2)$$

125 The general equations can be rewritten as:

$$\begin{aligned} \frac{\partial \sigma_r}{\partial r} + \frac{1}{r} \frac{\partial \tau_{r\theta}}{\partial \theta} + \frac{\partial \tau_{r0}}{\partial 0} + \frac{\sigma_r - \sigma_\theta}{r} &= 0 \\ \frac{\partial \tau_{\theta r}}{\partial r} + \frac{1}{r} \frac{\partial \tau_\theta}{\partial \theta} + \frac{\partial \tau_{\theta 0}}{\partial 0} + 2 \frac{\tau_{\theta r}}{r} &= 0 \\ \frac{\partial \tau_{0r}}{\partial r} + \frac{1}{r} \frac{\partial \tau_{0\theta}}{\partial \theta} + \frac{\tau_{0r}}{r} &= 0 \end{aligned} \quad (3)$$

127 This problem is symmetrical about y-axis as well as the line in the middle which
 128 is perpendicular to the line connecting the two holes, thus $\frac{\partial}{\partial \theta} = 0$. Also, the radial
 129 deformation is uniform ($\tau_{r\theta} = \tau_{\theta\theta} = \tau_{r0} = 0$). Thus, Eq. (3) reduces to:

$$130 \quad \frac{\partial \sigma_r}{\partial r} + \frac{\sigma_r - \sigma_\theta}{r} = 0 \quad (4)$$

131 A standard solution for Eq. (4) is:

$$132 \quad \sigma_r = c r^n \quad (5)$$

133 where c and n are constants.

134 The boundary conditions for a thick-walled cylinder with only internal pressure is:

$$135 \quad \begin{cases} \sigma_r = -p & (r = r_i) \\ \sigma_r = 0 & (r = r_0 = d) \end{cases} \quad (6)$$

136 Substituting Eq. (6) into Eq. (5), The radial and circumferential stresses can be
 137 expressed as:

$$138 \quad \begin{aligned} \sigma_r &= \frac{r_i^2 p (1 - \frac{d^2}{r^2})}{d^2 - r_i^2} \\ \sigma_\theta &= \frac{r_i^2 p (1 + \frac{d^2}{r^2})}{d^2 - r_i^2} \end{aligned} \quad (7)$$

139 3.2 Principal stresses perpendicular to the line connecting the two adjacent 140 holes

141 To obtain the principal stresses on each element, the stresses in polar
 142 coordinates were transformed to Cartesian coordinates. Assuming the y-axis
 143 direction along the line connecting the two adjacent holes, and z-axis direction
 144 normal to the line, as shown in Fig. 3. The equations transforming from polar to
 145 Cartesian coordinates can be written as:

$$146 \quad \begin{aligned} \sigma_{yy} &= \sigma_r \cos^2 \theta + \sigma_\theta \sin^2 \theta \\ \sigma_{zz} &= \sigma_r \sin^2 \theta + \sigma_\theta \cos^2 \theta \end{aligned} \quad (8)$$

147 where σ_{yy} is the principal stress along the line connecting the two pre-drilled holes in
 148 Cartesian coordinate system, and σ_{zz} is the principal stress perpendicular to the line.
 149 Note that if σ_{yy} and σ_{zz} work out to be positive, it is tension and if it is negative, it is
 150 compression.

151 From Eqs. (7) and (8), the principal stresses at any positions perpendicular to the
 152 line connecting the two adjacent holes can be written as:

$$\begin{aligned}
 \sigma_{zz} &= \frac{r_i^2 \rho}{d^2 - r_i^2} \left(\sin^2 \theta_1 - \frac{d^2}{r_1^2} \sin^2 \theta_1 \cos^2 \theta_1 + \frac{d^2}{r_1^2} \cos^2 \theta_1 \sin^2 \theta_2 - \frac{d^2}{r_2^2} \sin^2 \theta_2 \cos^2 \theta_2 + \frac{d^2}{r_2^2} \cos^2 \theta_2 \right) \\
 &= \frac{r_i^2 \rho}{d^2 - r_i^2} \left[2 + \frac{d^2}{r_1^2} (\cos^2 \theta_1 \sin^2 \theta_1 + \cos^2 \theta_2 \sin^2 \theta_2) \right] \\
 &= \frac{r_i^2 \rho}{d^2 - r_i^2} \left[2 + d^2 \left(\frac{1 - 2 \sin^2 \theta_1}{r_1^2} + \frac{1 - 2 \sin^2 \theta_2}{r_2^2} \right) \right]
 \end{aligned} \tag{9}$$

154 where r_1 and r_2 are the distance from any positions to the centres of Hole 1 and
 155 Hole 2, respectively. θ_1 and θ_2 are illustrated in Fig 3.

157 It is known that the pressure arising from DA is nonlinearly related with hole
 158 radius, time and mode-I fracture toughness of rock^{2; 6}, which can be defined as:

$$p = f(r_i, t, K_{IC}) = 12 \frac{r_i^{0.407} t^{0.993} K_{IC} (1.6)}{0} \leq t \tag{10}$$

160 where r_i is the radius of the hole (m), t is the loading time (h) and K_{IC} denotes mode-I
 161 fracture toughness (MPa·m^{1/2}).

162 It is worthwhile emphasizing that, in Eq. (10), only three parameters (i.e., loading
 163 time, hole size and rock strength property) are considered, due to the fact that these
 164 three parameters dominantly affect the pressure from DA^{6; 14; 17}. For example, rock
 165 strength affects the expansive pressure from DA. Because the increase of Young'
 166 modulus or fracture toughness of rock will lead to an increase of confinement to the
 167 expansion/hydration of DA, for which the DA can generate a high pressure^{2; 17}.

168 It has been reported that temperature contributes the hydration process of DA,
 169 thereby higher expansive pressure can be generated at higher temperatures^{4; 17; 18}.
 170 However, a quantitative relation/equation between temperature and the performance
 171 of DA (in terms of expansive pressure) is still not available, as such further work
 172 needs to be performed in this regard to further improve the prediction performance of
 173 Eq. (10).

174 Substituting Eq. (10) into Eq. (9), the principal stresses along z-axis can be
 175 rewritten as:

176

$$\sigma_{zz} = \frac{r_i^2 * f(r_i, t, K_{IC})}{d^2 - r_i^2} \left[2 + d^2 \left(\frac{1 - 2 \sin^2 \theta_1}{r_1^2} + \frac{1 - 2 \sin^2 \theta_2}{r_2^2} \right) \right] \quad (11)$$

$$= \frac{0.12 r_i^{2.407} * t^{0.933} (37 K_{IC} 41.6)^{0.493}}{d^2 - r_i^2} \left[2 + d^2 \left(\frac{1 - 2 \sin^2 \theta_1}{r_1^2} + \frac{1 - 2 \sin^2 \theta_2}{r_2^2} \right) \right]$$

177 4 Parametric study and discussion

178 For a certain rock and working environment, spacing and size of holes are key
 179 parameters to be considered by a practitioner to maintain an optimum use of DA. To
 180 understand the influence of these two parameters on principal tensile stresses, a
 181 parametric study was carried out. Midgley Grit sandstone (MGS) and Horton
 182 Formation siltstone (HFS), which respectively represent soft and hard rocks were
 183 employed in the parametric study. The uniaxial tensile strengths of MGS and HFS
 184 are 2.1 and 12.1, respectively; and the mode-I fracture toughness of these two rocks
 185 are 0.49 and 1.56, respectively¹⁹.

186 4.1 Influence of hole spacing

187 Fig. 4 shows the principal tensile stress against the hole spacing for fracturing
 188 MGS (soft rock). Spacing of holes was analysed at various values from 20 to 2000
 189 mm with an equal interval of 50 mm. For each situation, the loading time (t) was
 190 considered at 1, 2, 3, 5, 10, 15, 20, and 25 h, respectively, assuming that the DA can
 191 work up to 25 hours¹⁴.

192 Note that for the sake of simplification, the principal tensile stress shown in Fig. 4
 193 represents the stress at the middle of the two holes, thus:

$$194 \quad r_1 = r_2 = d / 2 \quad (12)$$

$$195 \quad \theta_1 = \theta_2 = 0 \quad (13)$$

196 Eq. (11) is simplified as:

$$197 \quad \sigma_{zz} = \frac{10 r_i^2 p}{d^2 - r_i^2} = 1.2 \frac{t^{0.933} \cdot r_i^{2.407} (37 K_{IC} 41.6)^{0.493}}{d^2 - r_i^2} \quad (14)$$

198 As shown in Fig. 4, the principal tensile stress decreased significantly when the hole
 199 spacing was increased. The rock will be fractured when the principal tensile stress
 200 equals to the tensile strength of MGS (indicated by the horizontal dashed lines in Fig.
 201 4). The time needed for fracturing MGS depends on hole spacing for a certain hole
 202 size. For example, for the hole with a radius of 27 mm (Fig. 4a), it took 20 hours for
 203 fracturing MGS when the hole spacing was 0.23 m, while it rose to 25 hours when
 204 the spacing was increased up to 0.26 m. The influence of the hole spacing on

205 fracturing time became much larger at a specific hole radius of 100 mm. As can be
206 seen in Fig. 4e, it required just 1 hour for fracturing MGS with a hole spacing of 0.29
207 m but 25 hours when the hole spacing reached up to 1.21 m.

208 Fig. 5 shows the relationship between the stress and spacing of hole for
209 fracturing HFS (brittle hard rock). As can be seen, it allowed a slightly higher value of
210 hole spacing for HFS compared with MGS at the same hole radius. For example, the
211 spacing was 1.21 m for fracturing MGS at a certain hole radius of 100 mm (Fig. 4e);
212 while it can be increased to 1.32 m for fracturing HFS under the same hole radius
213 (Fig. 5e). The increase in spacing is due to the increment of expansive pressure from
214 DA as a result of the increase of rock strength. In other words, hard brittle rock like
215 HFS can provide more confinement during the hydration of DA, leading to the
216 increment of expansive pressure from DA. Whereas the interaction between DA and
217 MGS became weaker due to the comparatively lower confinement that can be
218 provided by the soft rock, thus resulting in a lower expansive pressure from DA.

219 As shown in Figs. 4 and 5, the optimum hole spacing can be determined for a
220 given hole size and an expected loading time (which can be determined based on
221 project schedule). For example, the optimum hole spacing for fracturing HFS is
222 around 1.0 m when the hole radius is 80 mm and the loading time is 25 hours (Fig.
223 5d). For this case, selection of a smaller hole spacing (e.g., <1.0 m) will lead to an
224 excessive use of DA (because more holes need to be drilled), which will evidently
225 increase project budget. The optimum hole spacing against the time needed for
226 fracturing both soft and hard rocks (at some certain hole sizes) was plotted in Fig. 6
227 and polynomial curves are fitted. It can be seen that the optimum hole spacing is
228 increased when the loading time is increased for both soft and hard rocks as well as
229 different hole sizes. Also as mentioned earlier, for a certain hole size and a specific
230 loading time, the optimum hole spacing can be slightly larger for fracturing hard rock
231 than that for fracturing soft rock.

232 **4.2 Influence of hole size**

233 In this section, the influence of hole size on stress was investigated, while hole
234 spacing remained constant. Figs. 7 and 8 show the principal tensile stress against
235 hole radius for fracturing MGS and HFS, respectively. As observed, the stress
236 increased significantly when the hole radius increases for both soft and hard rocks,
237 which means that more DA will be used for fracturing the rocks. It was also observed
238 that the influence of spacing increment on stress (leading to a stress decrement) is

239 more significant than that from hole size increment (leading to stress increment). For
240 example, it took 1 hour for fracturing HFS when the hole radius was 70 mm and
241 spacing was 200 mm (Fig. 8a), while the time needed soared to at least 20 hours
242 when both hole radius and spacing were increased (up to 86 and 1000 mm
243 repressively, see Fig. 8e).

244 Fig. 9 shows the relationship between the optimum hole radius and the time
245 needed for fracturing soft and hard rocks. It can be seen that the time required for
246 fracturing both soft and hard rocks decreased with the increment of the hole radius
247 (for a specific hole spacing). For example, as shown in Fig. 9a, it took 1 hour for
248 fracturing MGS when holes with a radius of 74 mm and a spacing of 200 mm were
249 used. While the loading time rose up to 25 hours when the hole radius dropped to 22
250 mm with a same spacing. Similar situation occurred for the hard rock.

251 Based on the above analysis, the optimum hole spacing was plotted against hole
252 radius considering rock strength, as shown in Fig. 10. For a certain rock engineering
253 project, it is suggested that hole size can be confirmed first based on the available
254 drilling apparatus, and then the optimum hole spacing can be evaluated based on
255 the results of this study.

256 **5 Conclusion**

257 In this paper, an analytical model was presented to investigate the stresses
258 arising from a non-explosive demolition agent when fracturing rock based on the
259 elastic theory and thick-walled cylinder principle. The analytical model provides a
260 method to determine the optimum hole spacing and size as well as the time needed
261 for fracturing rocks with properties similar to those employed to determine the
262 pressure-time function of the demolition agent. The influences of hole size and
263 spacing on principal stress were examined taking into account loading time and
264 lithology. Several conclusions can be drawn from this study: (1) Tensile stress
265 decreased dramatically with the increasing of hole spacing, while it increased with
266 increment of hole size but the influence of spacing on stress changes was more
267 significant than that of hole size; (2) For a certain rock engineering project, the
268 optimum spacing can be determined when hole size is constrained by drilling rigs;
269 and the time needed for fracturing rock can be estimated based on the results of this
270 study; and (3) the potential influence of temperature on the performance of
271 demolition agent was not considered in the study, which needs to be addressed in
272 future research.

273 Results from this study can provide a scientific guidance in terms of layout
274 design and time management when using demolition agent for fracturing rock.
275 Additionally, the implementation of numerical analysis for investigating non-explosive
276 rock fracturing can probably be achieved based on the stress analysis results
277 presented in the study.

278 **Reference**

- 279 1. Huynh MP, Laefer, DF. Expansive cements and soundless chemical
280 demolition agents: state of technology review. In: 11th Conference on Science and
281 Technology, Ho Chi Minh City Vietnam, 21-23 October 2009: 209-214.
- 282 2. Arshadnejad S, Goshtasbi K, Aghazadeh J. A model to determine hole
283 spacing in the rock fracture process by non-explosive expansion material. *Int J Min*
284 *Met Mater.* 2011; 18(5):509-514.
- 285 3. Gómez C, Mura T. Stresses caused by expansive cement in borehole. *J Eng*
286 *Mech.* 1984; 110(6):1001-1005.
- 287 4. Dowding CH, Labuz JF. Fracturing of rock with expansive cement. *J Geotech*
288 *Eng.* 1982; 108(10):1288-1299.
- 289 5. Natanzi AS, Laefer DF, Mullane S. Chemical demolition of unit masonry: a
290 preparatory study. In: 10th International Conference on Structural Analysis of
291 Historical Constructions: Anamneris, Diagnosis, Therapy, Controls (SAHC2016),
292 Leuven, Belgium, 13-15 September: 1-13.
- 293 6. Gholinejad M, Arshadnejad S. An experimental approach to determine the
294 hole-pressure under expansion load. *J South Afr Inst Min Metall.* 2012; 112:631-635.
- 295 7. Ling CB. On the stresses in a plate containing two circular holes. *J Appl Phys.*
296 1948; 19(77):77-81.
- 297 8. Haddon AW. Stresses in an infinite plate with two unequal circular holes. *Q J*
298 *Mech Appl Math.* 1967; 20: 277-291.
- 299 9. Ling CB, Va B, Tsai CP. Stress in a thick plate containing an eccentric
300 spherical inclusion or cavity. *Acta Mech.* 1969; 7:169-186.
- 301 10. Coates DF, Yu YS. A note on the stress concentrations at the end of a
302 cylindrical hole. *Int J Rock Mech Min Sci.* 1970; 7:583-588.
- 303 11. Zimmerman RW. Stress concentration around a pair of circular holes in a
304 hydrostatically stressed elastic sheet. *J Appl Mech.* 1988; 55(2):487-488.

- 305 12. Li Y, Peng J, Zhang F, Qiu Z. Cracking behavior and mechanism of
306 sandstone containing a pre-cut hole under combined static and dynamic loading.
307 Eng Geol. 2016; 213:64-73.
- 308 13. Arshadnejad S, Niu J. Birth of the first crack and its growth under incremental
309 static loading between two holes in brittle rocks. J Earth Eng. 2014; 1(1):1-15.
- 310 14. Shang J, West LJ, Hencher SR, Zhao Z. Tensile strength of large-scale
311 incipient rock joints: A laboratory investigation. Acta Geotech. 2017;
312 <https://doi.org/10.1007/s11440-017-0620-7>
- 313 15. Shang J, Hencher SR, West LJ, Handley K. Forensic excavation of rock
314 masses: A technique to investigate discontinuity persistence. Rock Mech Rock Eng.
315 2017; 50(11):2911-2928.
- 316 16. Murakami Y. Theory of elasticity and stress concentration, Wiley, West
317 Sussex. 2016: pp. 445.
- 318 17. Jin ZZ, Liao H, Zhu W. Splitting mechanism of rock and concrete under
319 expansive pressure. In: Proceedings of Demolition and Reuse of Concrete and
320 Masonry, Japan. 1988: pp 141.
- 321 18. Hinze H, Brown J. Properties of soundless chemical demolition agents. J.
322 Constr. Eng. Manage. 1994; 120(4):816-827.
- 323 19. Shang J. Persistence and tensile strength of incipient rock discontinuities.
324 PhD thesis, the University of Leeds, United Kingdom. 2016: pp 248.

325 **Figure captions**

326 **Fig 1 a** A demolition agent used to form slopes at the Castle Peak Road in Hong
327 Kong where blasting was not allowed. Hammer for scale; **b** A hydraulic splitter
328 (model PRS-95) was employed for the non-explosive fracturing of rock in
329 construction of the Mass Transit Railway (Admiralty section) in Hong Kong.

330 **Fig 2** Interaction mechanism of two neighbouring holes subjected to the
331 expansive pressure from a non-explosive demolition agent. Redrawn from Natanzi et
332 al.⁵

333 **Fig 3** Model of two symmetrical holes internally pressurized. Stresses acting on
334 an element solely arising from Hole 2 is presented in polar coordinate. r is the radius
335 and θ is the azimuth in polar coordinate.

336 **Fig 4** Principal tensile stress against hole spacing for Midgley Grit sandstone
337 (soft rock).

338 **Fig 5** Principal tensile stress against hole spacing for Horton Formation siltstone
339 (hard rock).

340 **Fig 6** Relationships between the optimum hole spacing and the time required for
341 fracturing soft rock (a) and hard rock (b).

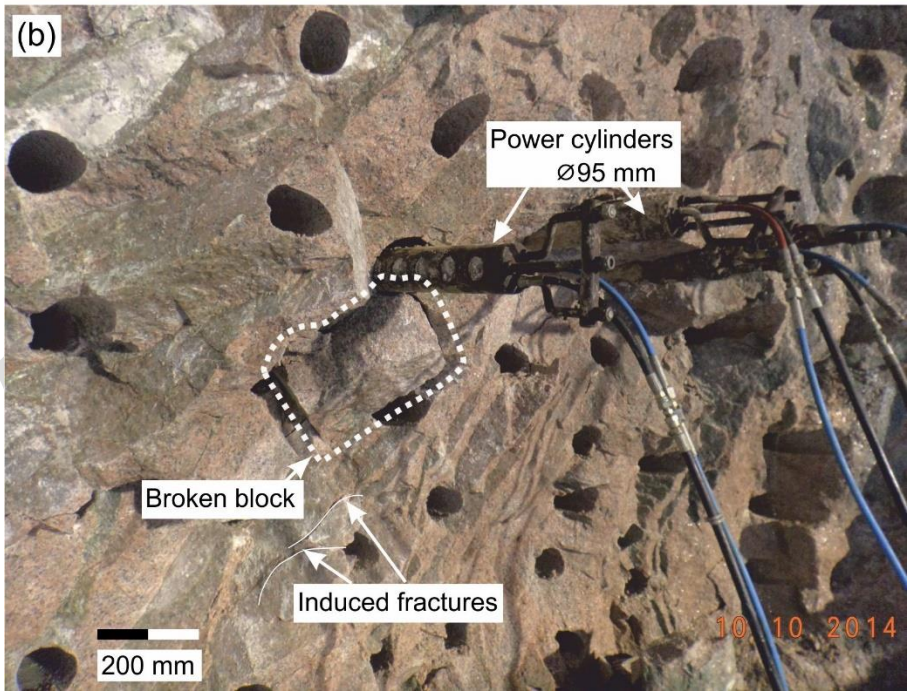
342 **Fig 7** Principal tensile stress against hole size for Midgley Grit sandstone (soft
343 rock).

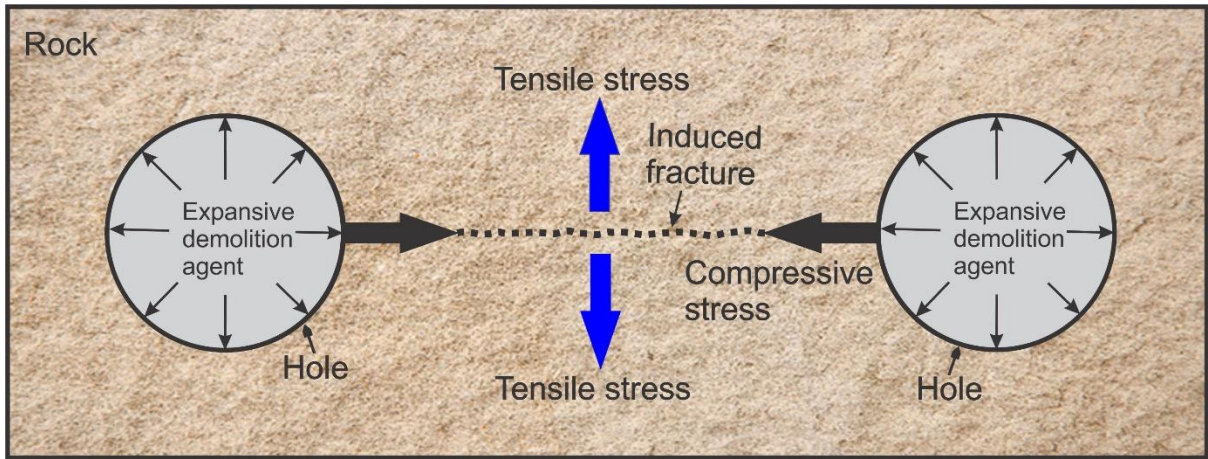
344 **Fig 8** Principal tensile stress against hole size for Horton Formation siltstone
345 (hard rock).

346 **Fig 9** Relationships between the optimum hole size and the time required for
347 fracturing soft rock (a) and hard rock (b).

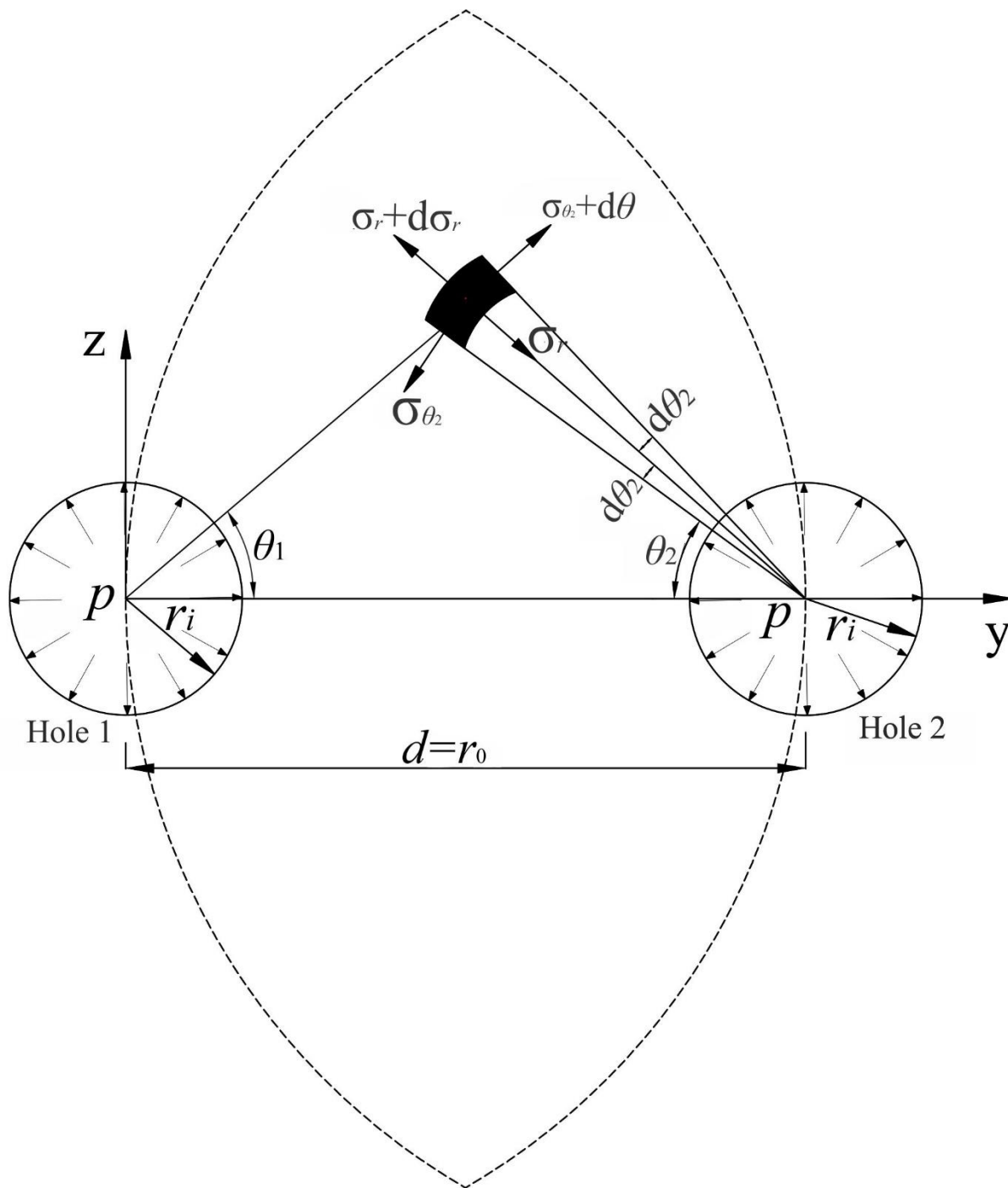
348 **Fig 10** Relationships between optimum hole size and hole spacing for fracturing
349 both soft and hard rocks.

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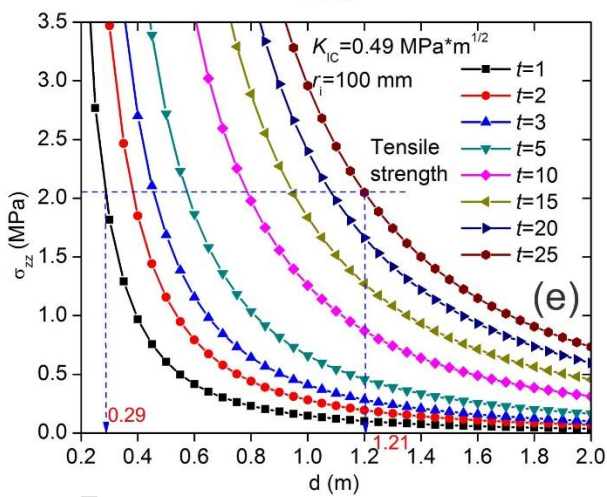
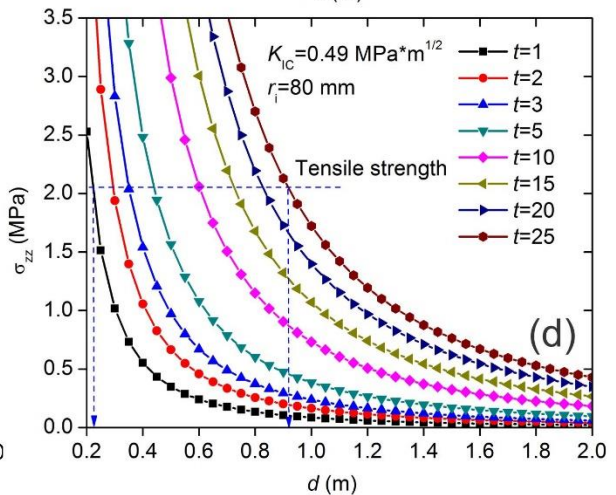
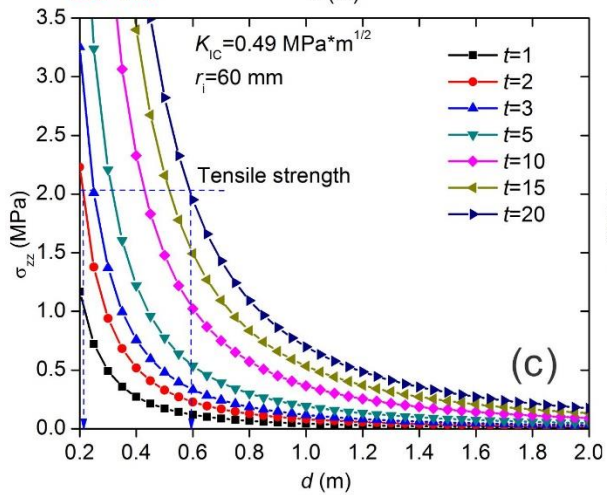
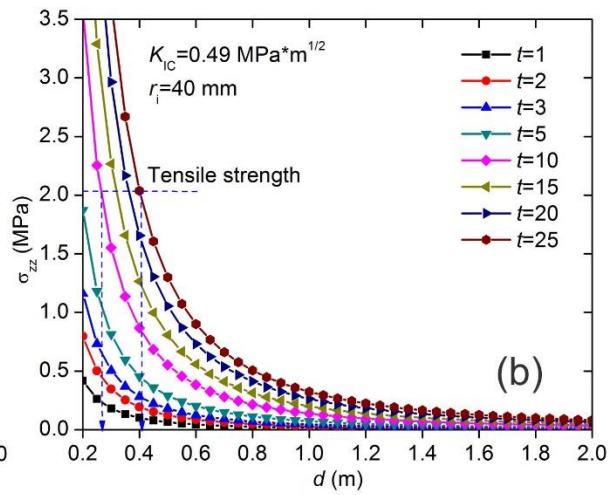
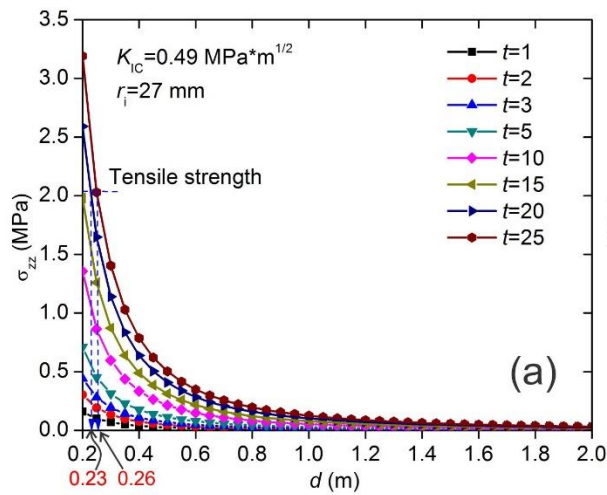


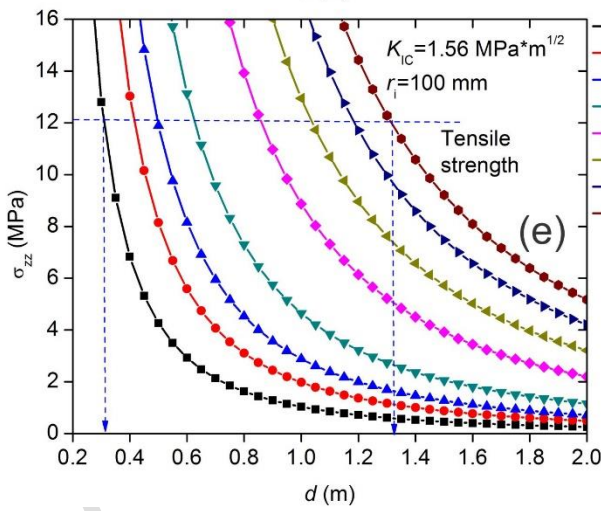
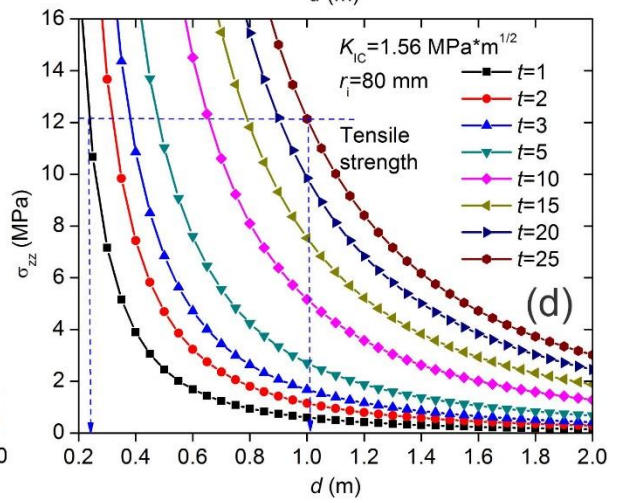
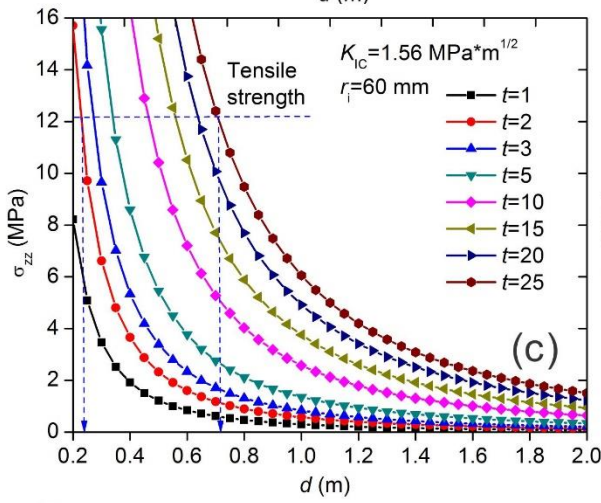
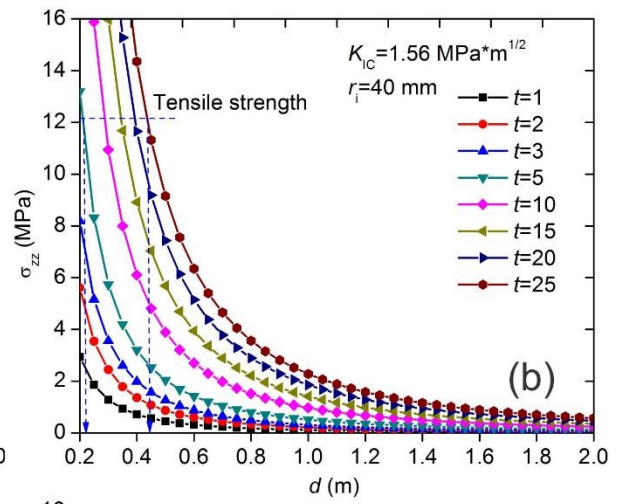
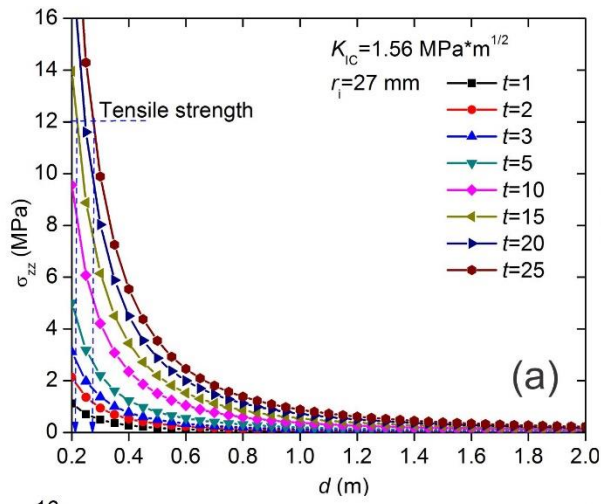


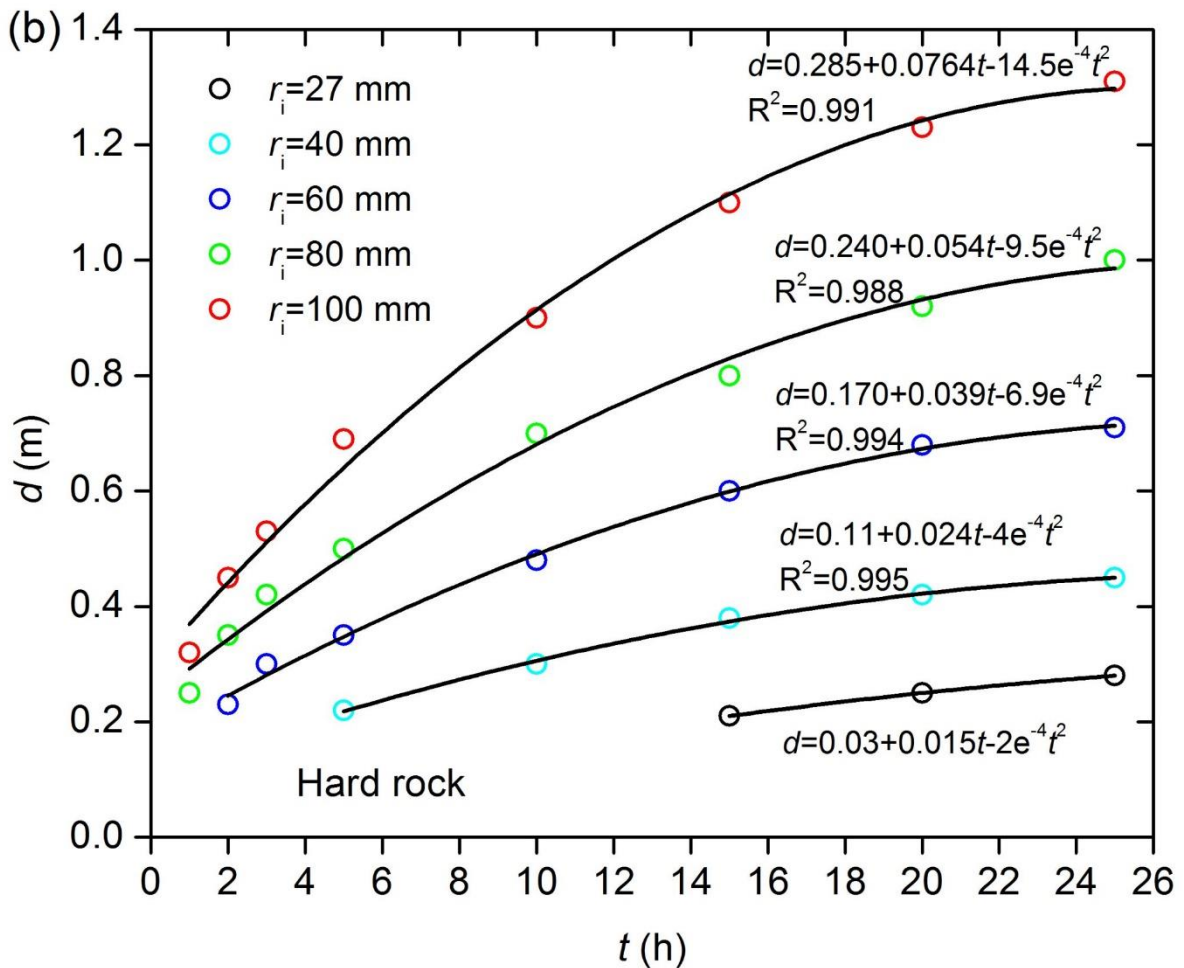
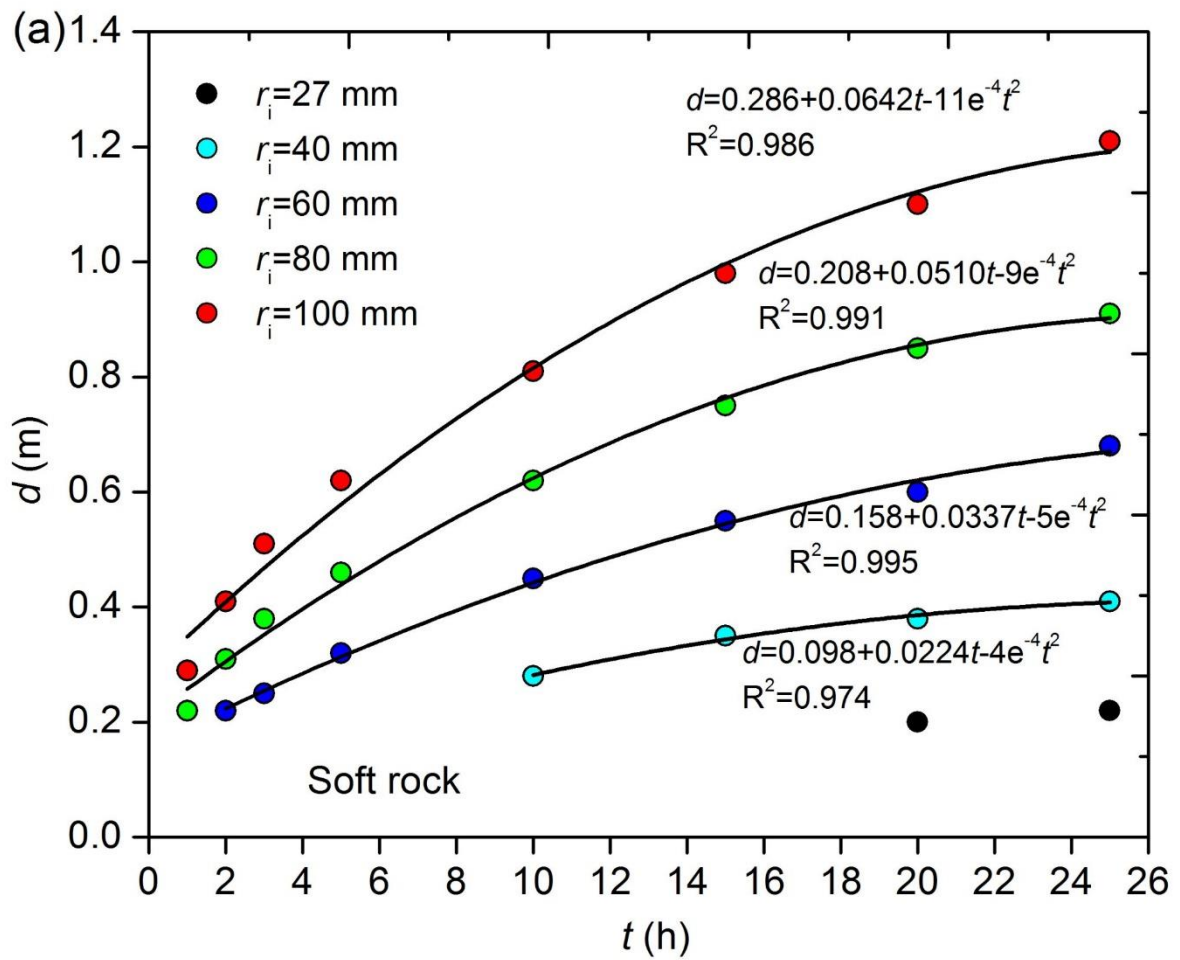
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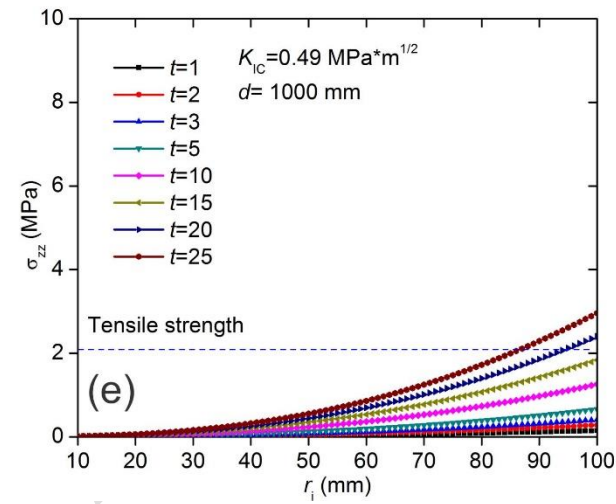
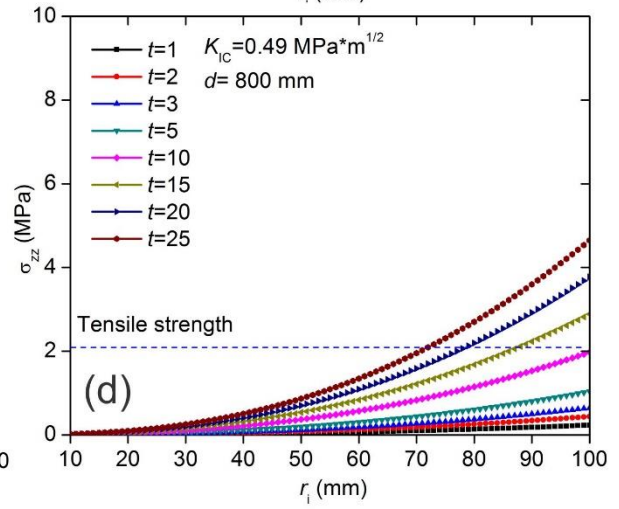
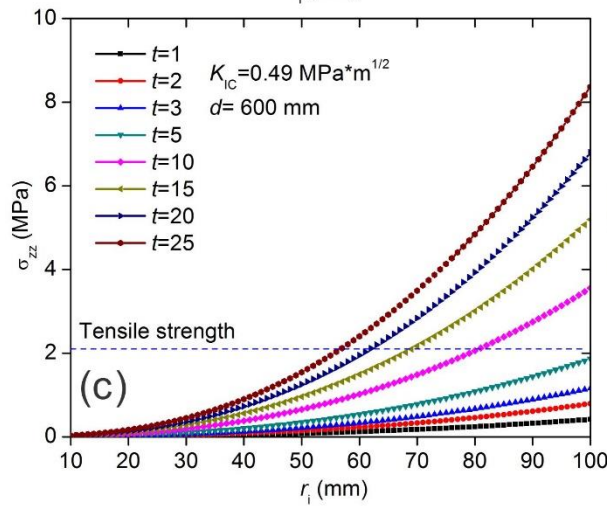
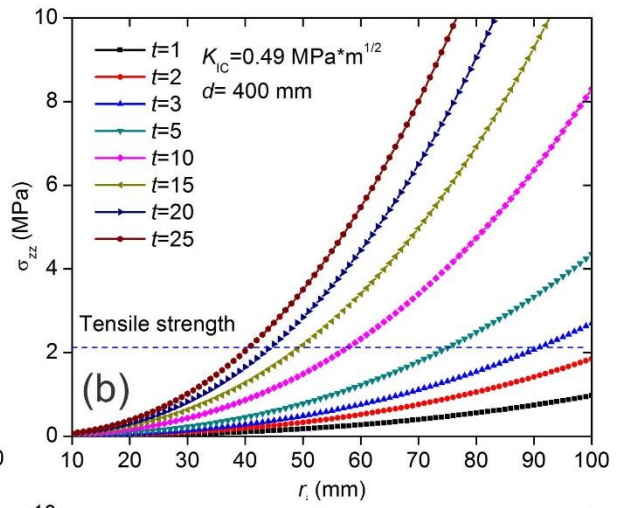
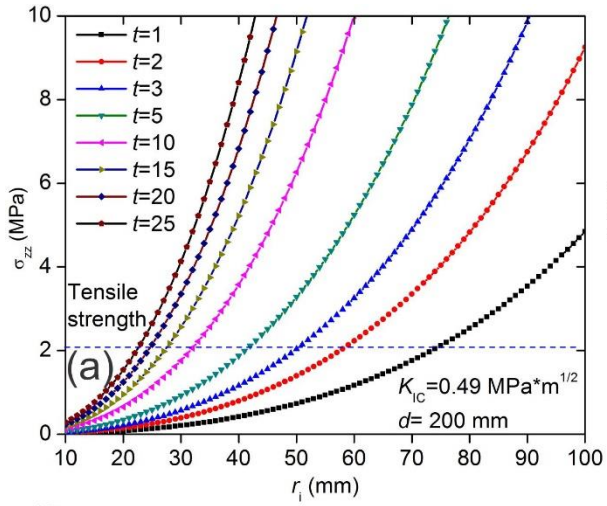


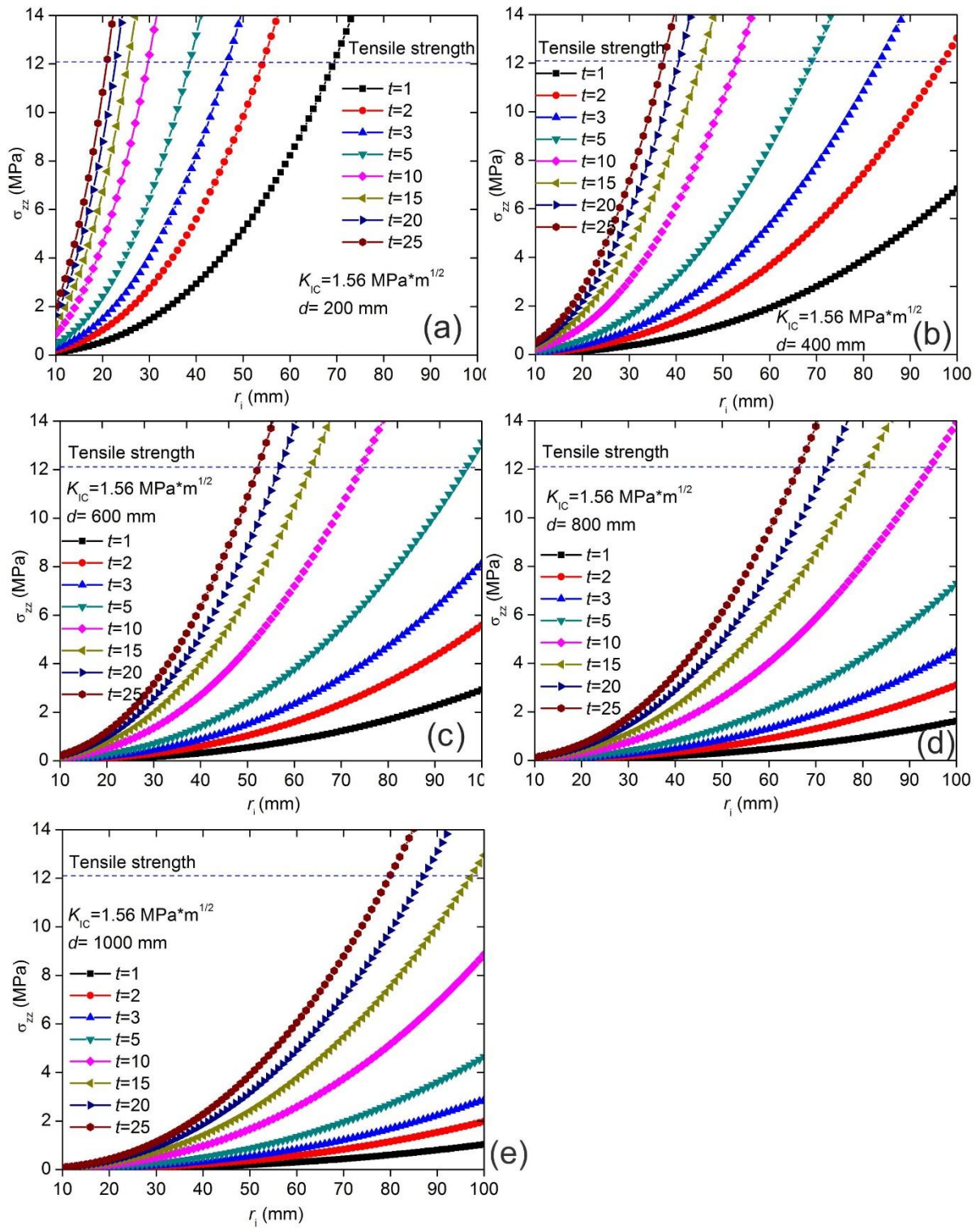
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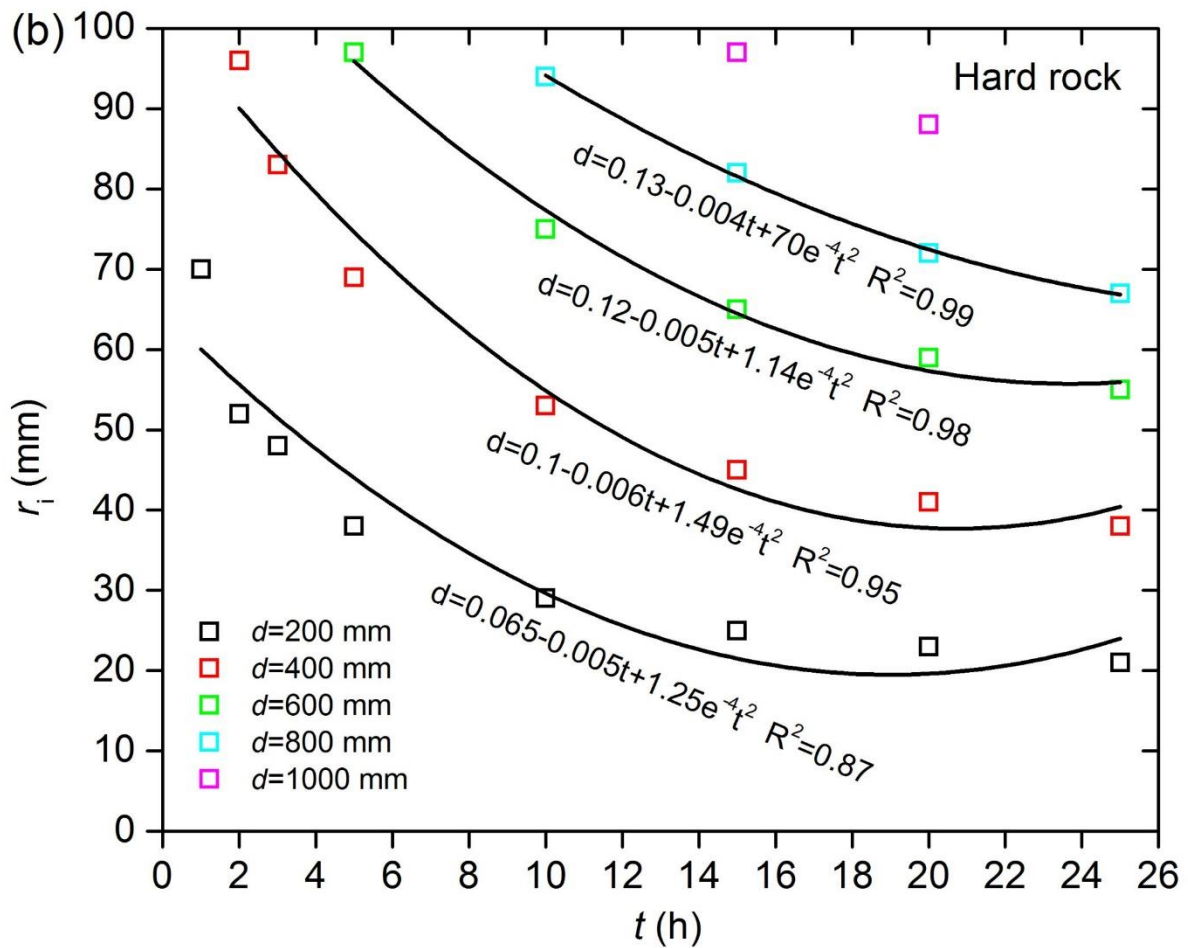
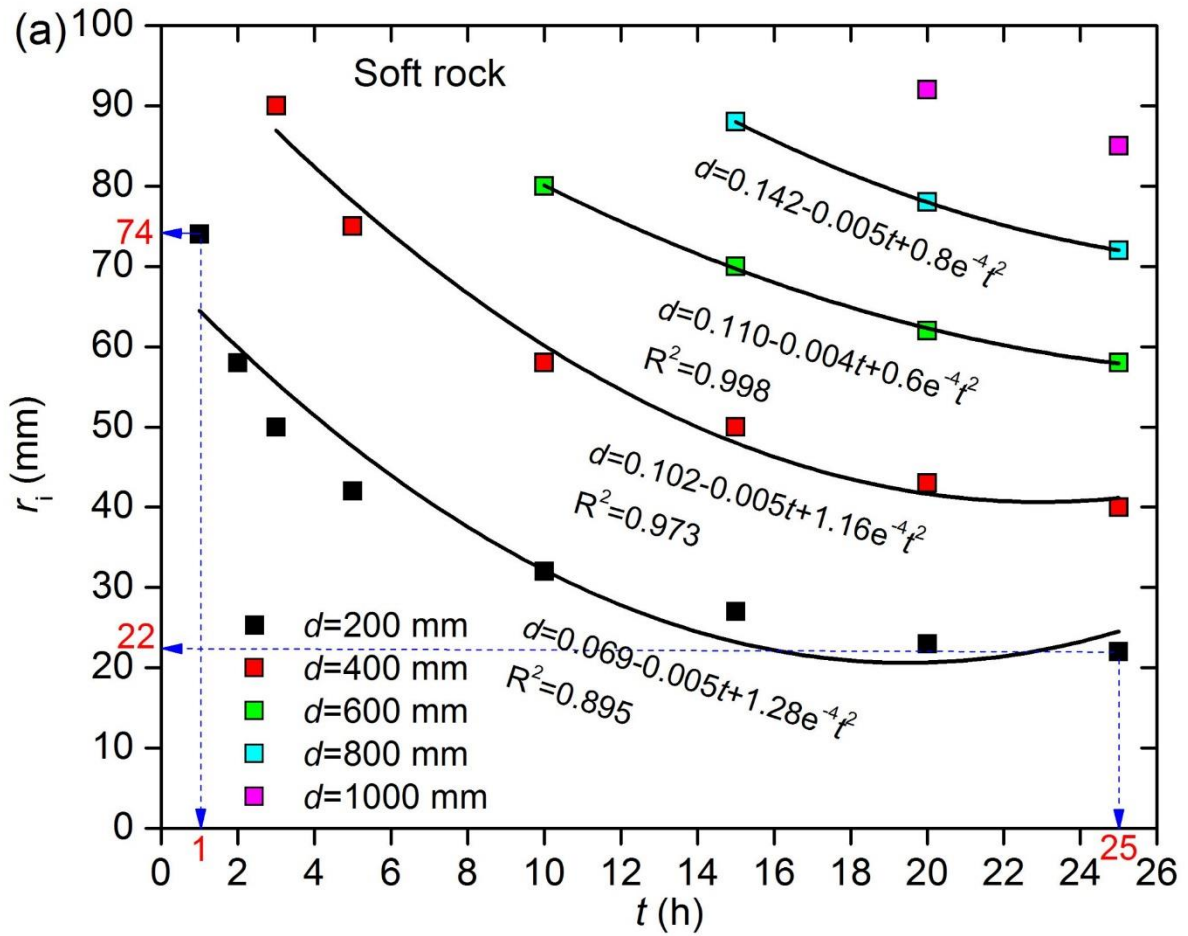


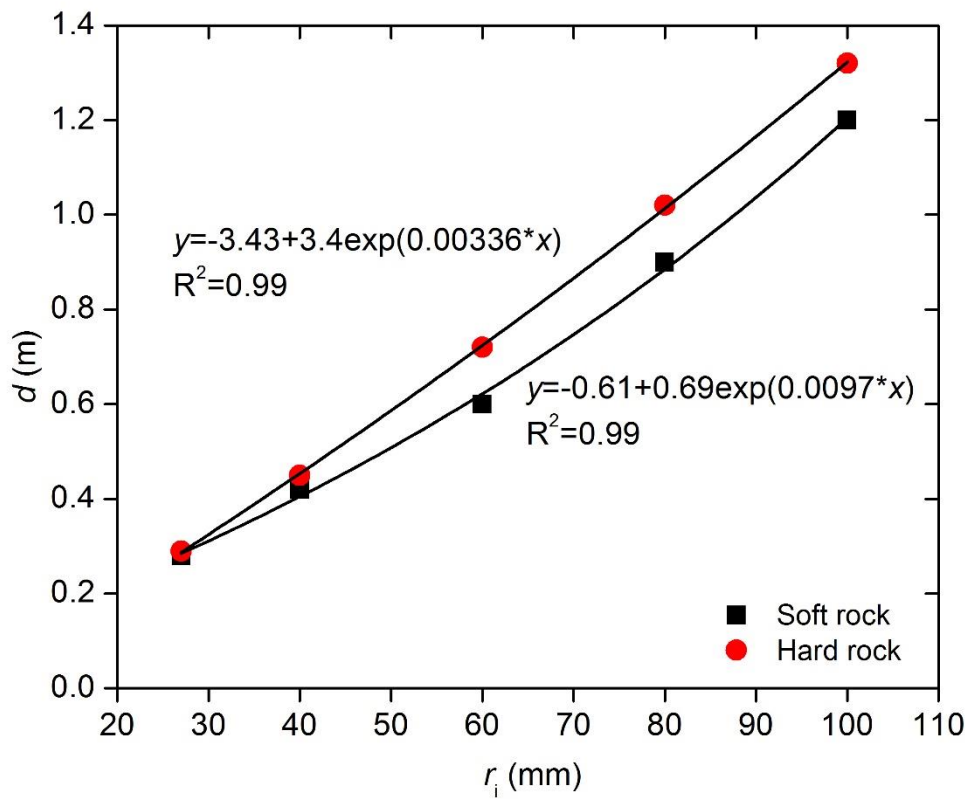












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