



## 13 **Abstract**

14 Clouds cover on average nearly 70% of Earth's surface and are important for the global  
15 albedo. The magnitude of the shortwave reflection by clouds depends on their location,  
16 optical properties, and 3D structure. Earth system models are unable to perform 3D ra-  
17 diative transfer calculations and thus partially neglect the effect of cloud morphology on  
18 albedo. We show how the resulting radiative flux bias depends on cloud morphology and  
19 solar zenith angle. Using large-eddy simulations to produce 3D cloud fields, a Monte Carlo  
20 code for 3D radiative transfer, and observations of cloud climatology, we estimate the  
21 effect of this flux bias on global climate. The flux bias is largest at small zenith angles  
22 and for deeper clouds, while the albedo bias is largest (and negative) for large zenith an-  
23 gles. Globally, the radiative flux bias is estimated to be  $1.6 \text{ W m}^{-2}$  and locally can be  
24 on the order of  $5 \text{ W m}^{-2}$ .

## 25 **Plain Language Summary**

26 Clouds cover on average about 70% of Earth's surface and are important for reg-  
27 ulating the surface temperature by reflecting nearly 15% of the incoming energy from  
28 the sun back to space. How individual clouds reflect this incoming radiation depends on  
29 where they are and what they look like. Earth system models cannot resolve the radi-  
30 ative effect of the detailed morphology of clouds due to computational constraints. In-  
31 stead, models approximate the way that clouds reflect light, which leads to a bias in the  
32 amount of energy reflected back to space. In this study, the reflection bias from neglect-  
33 ing the detailed 3D structure of clouds in radiative transfer calculations is studied to es-  
34 timate its net effect on climate. It is found that deep thunderstorm clouds near the equa-  
35 tor lead to significant biases, due to both their location and size. Globally, the implied  
36 energy bias is of a similar magnitude as the energy imbalance created by anthropogenic  
37 greenhouse gases. It is important to correct this bias in climate models.

## 38 **1 Introduction**

39 Earth's average albedo is roughly 29%, with clouds accounting for about half of the  
40 reflection of solar radiative energy fluxes back to space (Stephens et al., 2015). Accu-  
41 rately simulating clouds is crucial for modeling Earth's albedo. However, Earth system  
42 models (ESMs) struggle to accurately represent the mean albedo, its spatial patterns,  
43 and its seasonal variability (Bender et al., 2006; Voigt et al., 2013). Simulating clouds

44 is difficult for several reasons, but one major factor is their wide range of spatial scales.  
45 Clouds have complex three-dimensional morphologies created by turbulent motions at  
46 length scales down to tens of meters or smaller. However, the typical resolution of an  
47 ESM is around only 10 – 100 km in the horizontal and 100 – 200 m in the vertical in the  
48 lower troposphere (Schneider et al., 2017). This discrepancy means that clouds are not  
49 explicitly resolved in ESMs. Instead, they are represented by parameterizations and, for  
50 purposes of radiative transfer (RT) calculations, are approximated as plane-parallel struc-  
51 tures within grid cells (Marshak & Davis, 2005). Semi-empirical parameterizations ac-  
52 count for heterogeneity of optical properties on subgrid-scales (e.g., Macke et al., 1999;  
53 Wood et al., 2005; Gimeno García et al., 2012).

54 ESMs resort to two main simplifications when performing RT calculations: (1) the  
55 plane-parallel approximation (PPA) made on the cloud morphology, which assumes clouds  
56 are smeared out across the entire grid box, and (2) the independent-pixel approxima-  
57 tion (IPA), which assumes no horizontal radiative fluxes between neighboring grid cells.  
58 These different approximations amount to either ignoring the horizontal heterogeneity  
59 of cloud optical properties or considering the heterogeneity in optical properties, but as-  
60 suming a net zero transfer of photons, respectively (R. Cahalan & Wiscombe, 1992; R. F. Ca-  
61 halan et al., 1994). The PPA is a consequence of the limited spatial resolution of climate  
62 models, while the IPA is necessary to make radiative transfer calculations tractable.

63 Yet, the importance of the structure of clouds on radiative transfer has been rec-  
64 ognized for nearly 50 years (e.g., McKee & Cox, 1974; Barker, 1994) and has recently  
65 received renewed attention since advances in computation allow more direct simulation  
66 of 3D RT (e.g., Emde et al., 2016; Schäfer et al., 2016; Villefranque et al., 2019). For ex-  
67 ample, one topic that has garnered particular interest in the literature is the effect of bro-  
68 ken cloud fields (Barker, 1994; Hinkelman et al., 2007; Gristey et al., 2019), which con-  
69 sider the subgrid-scale heterogeneity in liquid water path; however, it does not consider  
70 the effects of 3D optics. Veerman et al. (2020) show the importance of including the 3D  
71 optical effects (or the bias resulting from the IPA) on the dynamics of shallow cumulus  
72 clouds and the coupling between the boundary layer and land surface.

73 The PPA may be avoided in ESMs using embedded 2D cloud-resolving models (Kooperman  
74 et al., 2016), an approach known as cloud superparameterization (Khairoutdinov & Ran-  
75 dall, 2001). However, 3D radiation computations will remain too expensive to run in ESMs

76 in the near future, making simplifications such as the IPA necessary. The structural dif-  
 77 ferences between IPA and a full three-dimensional RT calculation have been documented  
 78 before (Barker et al., 2003; Marshak, Davis, Wiscombe, & Titov, 1995; Barker et al., 2012),  
 79 and many alternatives to IPA have been proposed to minimize their mismatch (Marshak,  
 80 Davis, Wiscombe, & Cahalan, 1995; Várnai & Davies, 1999; Frame et al., 2009; Hogan  
 81 & Shonk, 2013; Wissmeier et al., 2013; Okata et al., 2017). Nevertheless, most studies  
 82 have been focused on theoretical cases, small spatial and temporal domains, or improv-  
 83 ing satellite retrieval algorithms. Some notable exceptions are Cole et al. (2005) and Barker  
 84 et al. (2015), who compared 3D and IPA RT calculations to estimate the bias present  
 85 in ESMs using a superparameterized cloud resolving model and coarse-resolution, two-  
 86 dimensional cloud fields retrieved from CloudSAT and CALIPSO, respectively.

87 Here we discuss the magnitude of the bias that results from making the IPA dur-  
 88 ing radiative transfer calculations in global climate simulations. We use large-eddy sim-  
 89 ulations (LES) to generate three-dimensional cloud fields representing three canonical  
 90 cloud regimes: shallow convection, stratocumulus, and deep convection. Then we cal-  
 91 culate the bias between the true reflected flux and the flux approximated by IPA using  
 92 a Monte Carlo RT code. The radiative flux bias is shown to vary with zenith angle and  
 93 cloud type. Because the zenith angle varies with the diurnal and seasonal cycle, we quan-  
 94 tify the effect of the 3D bias on these timescales. Finally, the 3D flux bias is mapped onto  
 95 observations of cloud climatology to estimate the global and spatial effect on climate sim-  
 96 ulations where three-dimensional radiative fluxes are neglected. As stated earlier, most  
 97 ESMs make both the IPA and some variant of the PPA for radiative transfer calcula-  
 98 tions, so the bias associated with the IPA is an underestimate of the total bias. How-  
 99 ever, because of the diversity of assumptions made by global models to account for phe-  
 100 nomena such as cloud overlap, and the fundamental resolution dependence of the PPA,  
 101 in this study we focus on the bias resulting from RT using only the IPA on fully resolved  
 102 3D cloud structures from LES.

## 103 **2 Methods**

### 104 **2.1 Large-eddy simulations of clouds**

105 Three-dimensional cloud fields are generated from high-resolution LES using the  
 106 anelastic solver PyCLES (Pressel et al., 2015, 2017). The LES are run in three dynam-



107 ical regimes to simulate shallow cumulus (ShCu), stratocumulus (Sc), and deep-convective  
108 clouds (Cb); details can be found in the Supporting Information. ShCu clouds are con-  
109 vective clouds with typical cloud cover of 10–20% and cloud top height (CTH) around  
110 2 km. They occur frequently over low- and mid-latitude oceans. In this study, ShCu are  
111 represented by two LES case studies, BOMEX and RICO, which represent non-precipitating  
112 and precipitating convection over tropical oceans, respectively (Siebesma et al., 2003;  
113 vanZanten et al., 2011). Sc clouds are shallow, with CTH only around 1 km, but opti-  
114 cally thick for longwave radiation. They have cloud cover near 100% and typically blan-  
115 ket subtropical oceans off the west coasts of continents. Sc are represented by the DYCOMS-  
116 II RF01 LES case of a Sc deck off the coast of California (Stevens et al., 2005). Cb clouds  
117 are deep convective thunderstorm clouds that occur frequently over midlatitude conti-  
118 nents in summer and at low latitudes, e.g., in the intertropical convergence zone (ITCZ).  
119 Their CTH can reach up to 15 km or higher, they often contain ice, and anvils at the  
120 top contribute to a cloud cover around 30%. Cb clouds are represented in this paper by  
121 the TRMM-LBA LES case based on measurements of convection over land in the Ama-  
122 zon (Grabowski et al., 2006).

123 An ensemble of snapshots is used to estimate the mean and variance of the bias  
124 for each cloud type. The ensemble sizes were chosen to capture the natural variability  
125 of morphology in each LES case: 10 for ShCu (BOMEX and RICO), 5 for Sc (DYCOMS-  
126 II RF01, and 15 for Cb (TRMM-LBA). For ShCu and Sc we take snapshots evenly spaced  
127 in time starting once the simulation has reached a statistically steady-state, after an ini-  
128 tial spin-up period. The snapshots are chosen to be at least one convective turnover time  
129 apart (1 hour for BOMEX and RICO and 30 minutes for DYCOMS-II RF01. For the  
130 Cb case we take snapshots from an initial-condition ensemble at a time point represen-  
131 tative of deep convection, characterized by stable liquid and ice water paths, occurring  
132 at 13:00 local time in the TRMM-LBA simulation. All subsequent results are calculated  
133 as the mean over the ensemble of cloud field snapshots.

## 134 **2.2 Radiative transfer computations**

135 The RT calculations were done using the libRadtran software package with the MYS-  
136 TIC Monte Carlo solver (Mayer & Kylling, 2005; Mayer, 2009; Emde et al., 2016). The  
137 MYSTIC solver requires, as input, three-dimensional fields of liquid/ice water content  
138 and particle effective radius. The LES uses bulk microphysics schemes (2-moment for

139 liquid, 1-moment for ice) and does not explicitly compute the effective radius. To com-  
 140 pute the effective radius, we follow the parameterization from Ackerman et al. (2009)  
 141 and Blossey et al. (2013) for liquid and Wyser (1998) for ice (Supporting Information).  
 142 For the RT, MYSTIC computes the scattering phase function. In the case of liquid droplets,  
 143 which can be assumed spherical, the full Mie phase function is used. For the case of ice  
 144 clouds, a parameterization of the habit-dependent scattering must be used. We find that  
 145 the results are insensitive to the choice of ice parameterization (Supporting Information),  
 146 mostly because the reflected flux signal is dominated by the liquid phase for the cloud  
 147 types simulated.

### 148 **3 Results and Discussions**

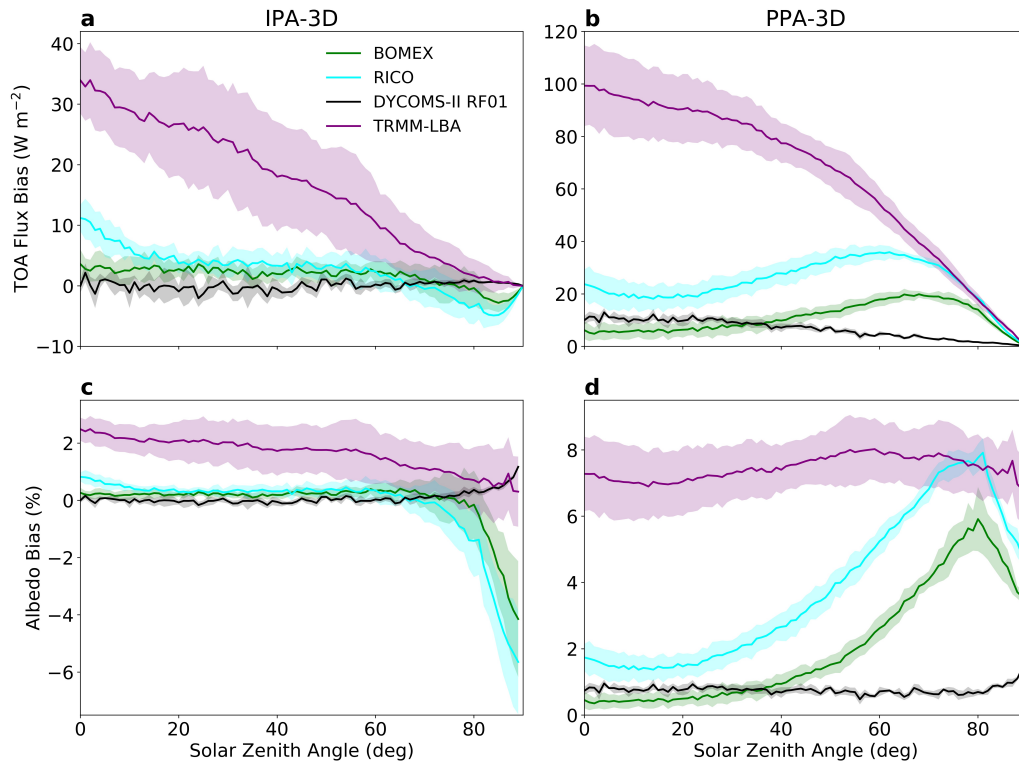
#### 149 **3.1 Radiative flux bias dependence on zenith angle**

150 The radiative flux bias is measured (in  $\text{W m}^{-2}$ ) as the difference in reflected irra-  
 151 diance between the 1D and 3D RT calculations. A positive bias means that the 1D is  
 152 reflecting more energy than the 3D truth, and the Earth system is artificially dimmed.  
 153 The albedo bias ( $\Delta\alpha$ ) is computed as the flux bias ( $\Delta F$ ) divided by the total incoming  
 154 solar flux ( $F_{in}$ ),

$$\Delta\alpha = \frac{\Delta F}{F_{in}} \times 100\%. \quad (1)$$

155 Figure 1 shows the flux and albedo biases (1D–3D) for the four cases of ShCu, Sc, and  
 156 Cb clouds. Shown are both the flux and albedo biases resulting from RT computations  
 157 using the IPA and also RT using the horizontally averaged cloud fields (PPA). We do  
 158 not try to account for cloud overlap (e.g. Tompkins & Di Giuseppe, 2007, 2015) or res-  
 159 olution dependence (e.g. Oreopoulos & Davies, 1998) in the PPA computations, so this  
 160 bias may be regarded as an upper bound for biases present in ESMs.

161 For all cloud types, the bias from the PPA is larger than from the IPA (note the  
 162 different y-axes between the left and right columns in Figure 1). Sc show negligible de-  
 163 viation between 1D and 3D reflected fluxes, especially for the IPA. For the PPA the bias  
 164 from all cloud types is always positive, meaning the PPA always overestimates the amount  
 165 of reflected radiation. For convective clouds (ShCu and Cb), the bias from the IPA is  
 166 positive, except for ShCu at very large solar zenith angles. ShCu scatter far fewer pho-  
 167 tons than Cb due to the low cloud cover and their small vertical extent (2 – 3 km). Cb  
 168 exhibit both the largest reflected irradiance and also the largest bias between the 1D (IPA



**Figure 1.** Bias (1D-3D) in TOA reflected flux (a, b) and albedo (c, d) as a function of zenith angle for ShCu (BOMEX and RICO), Sc (DYCOMS-II RF01), and Cb (TRMM-LBA). The left column (a, c) shows the bias resulting from the IPA, and the right column (b, d) the bias resulting from the PPA. For each cloud type, average fluxes (with shaded  $1\sigma$  error bars) are computed over the individual snapshots. Positive bias means the 1D approximation is reflecting more incoming flux than in the 3D RT calculation.

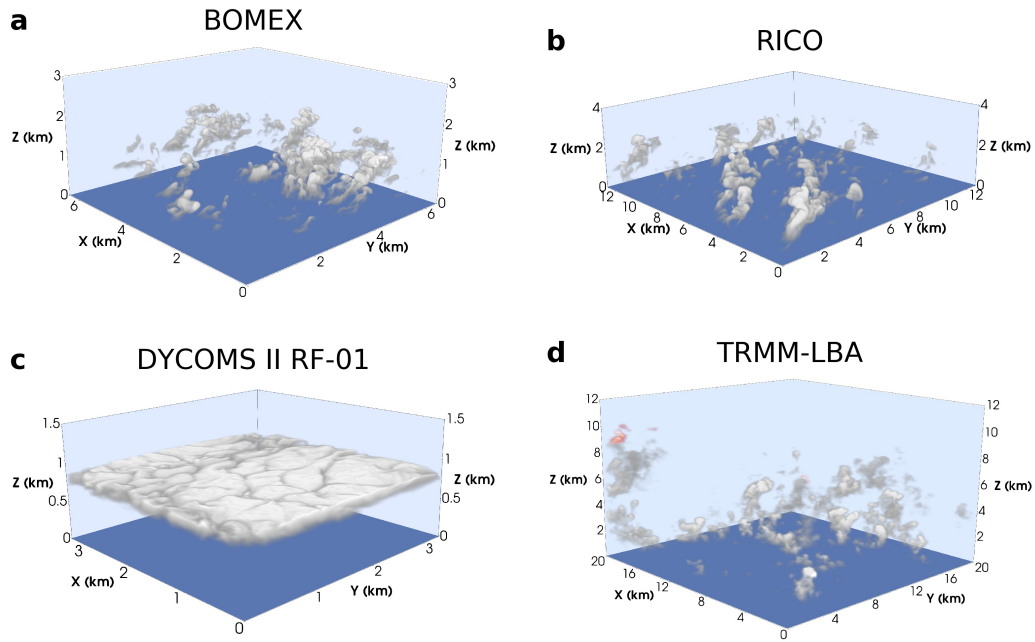
169 and PPA) and 3D RT calculations. The convective clouds show much more variation than  
170 the stratiform clouds between snapshots due to the variability in cloud cover even in a  
171 statistically steady state. Cb show nearly uniform albedo bias across zenith angles for  
172 the PPA. At large zenith angles, ShCu show a negative flux and albedo bias for IPA, but  
173 a large, positive flux and albedo bias for PPA.

174 In the IPA, the horizontal photon fluxes are ignored. For the Sc clouds that uni-  
175 formly cover the whole domain (Figure 2), this assumption has little effect: the flux bias  
176 is near zero for all zenith angles. For very small zenith angles, when the sun is overhead,  
177 the convective clouds (ShCu and Cb) produce a positive flux and albedo bias, meaning  
178 that the IPA overestimates the scattering. This is due to the fact that the IPA overes-  
179 timates the path length of a photon through the cloud; in reality (3D) the photons have  
180 a higher chance to exit the cloud through the sides (Schäfer et al., 2016). For large zenith  
181 angles ( $> 70^\circ$ ), the flux and albedo bias from ShCu is negative. This is because, at these  
182 large zenith angles, the ShCu begin to shadow each other, and scattering from the sides  
183 of the clouds becomes dominant. This “shadowing effect” has been discussed extensively  
184 in the literature (e.g. Marshak & Davis, 2005; Frame et al., 2009; Gristey et al., 2019);  
185 for example, Veerman et al. (2020) show the importance of coupling between the shad-  
186 owing and surface fluxes for cloud dynamics. In the IPA, when the horizontal fluxes are  
187 ignored, the cloud sides are not exposed, and the scattering is underestimated. These  
188 effects can be understood from Figure 2, which shows illustrations of the clouds from the  
189 four LES cases.

190 For the rest of the discussion, 1D RT refers only to the IPA on the fully resolved  
191 3D clouds; it does not include the horizontal homogenization (PPA).

### 192 **3.2 Seasonal cycle of radiative flux bias**

193 To assess the climate impact of the radiation bias resulting from the IPA, we con-  
194 sider the flux and albedo bias for each cloud type as a function of day of year and lat-  
195 itude. This calculation is done by assuming that the LES-generated cloud field is present  
196 at any given latitude circle on any given day of the year. This exercise is done not to be  
197 realistic, but to demonstrate the impact each cloud type might have on Earth. For any  
198 location and time, including a diurnal cycle, the solar zenith angle is calculated and the  
199 flux bias is estimated based on the results presented in Figure 1. The flux bias is com-



**Figure 2.** Snapshots of LES clouds, showing liquid water specific humidity (gray to white, low to high) and ice water specific humidity (red to white, low to high). (a) and (b) Shallow convective clouds. (c) Stratocumulus clouds. (d) Deep convective clouds. Note that the domain sizes vary between the cases. At high zenith angles, cloud shadowing becomes important for ShCu because the individual clouds can shadow a large portion of the domain and scattering from the cloud sides becomes dominant due to the low angle of the incoming photons.

200 puted hourly and averaged to show the diurnal-mean bias. The albedo bias is computed  
 201 analogously.

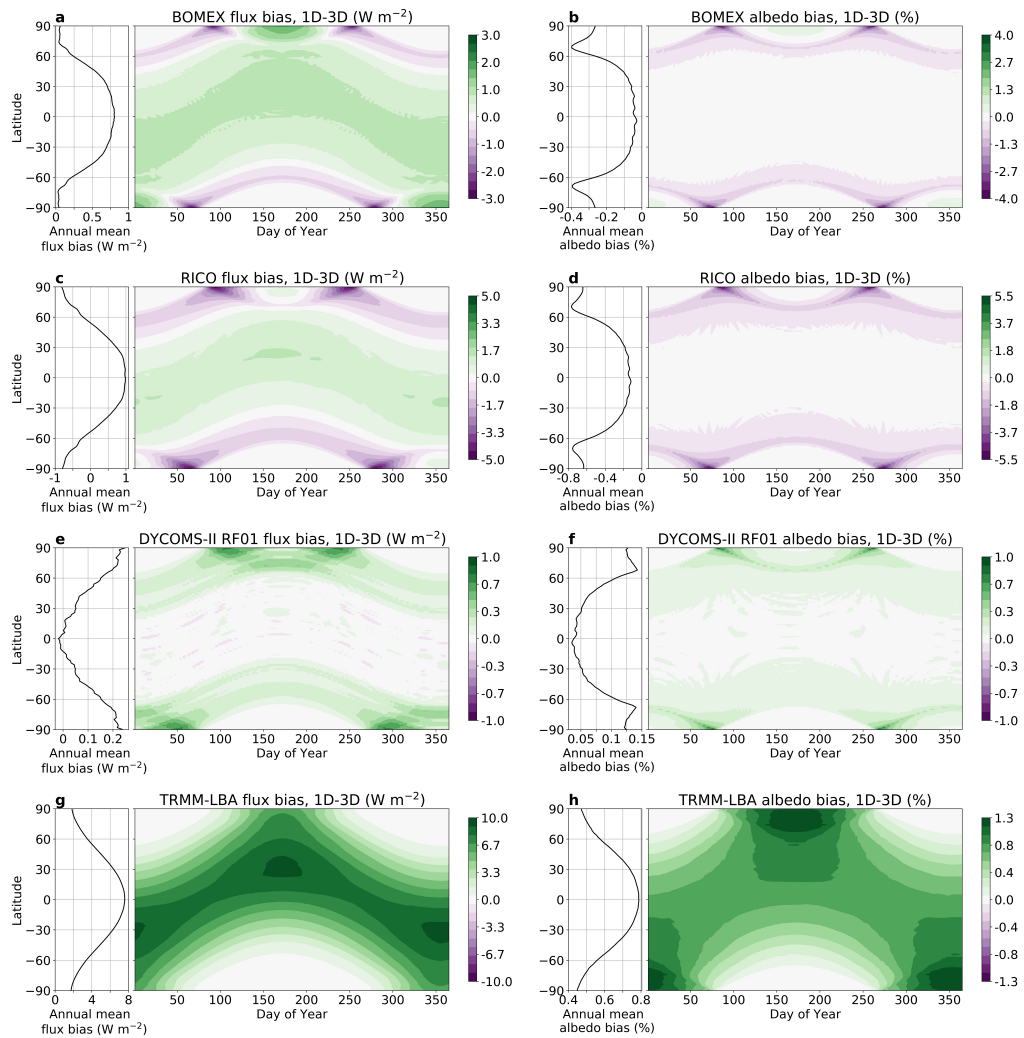
202 Figure 3 shows the TOA flux and albedo biases for each cloud type as a function  
 203 of day of year and latitude. The annual mean bias is shown in the insets to the left of  
 204 each panel. All cloud types show zero flux bias in regions of polar night where there is  
 205 no incoming solar flux. Both ShCu cases show similar patterns of flux bias with latitude  
 206 and time. As seen in Figure 1, these cases both have a negative bias for high solar zenith  
 207 angles ( $> 70^\circ$ ), and therefore the net flux (and albedo) bias during the shoulder sea-  
 208 sons at very high latitudes is negative. At lower latitudes, where the diurnally averaged  
 209 zenith angle is never larger than  $70^\circ$ , the net flux bias is always positive. Sc show a very  
 210 small flux (and albedo) bias for all zenith angles due to their high cloud cover and op-  
 211 tical depth, but they do exhibit a small positive flux bias ( $\sim 0.5 \text{ W m}^{-2}$ ) during sum-  
 212 mer in high latitudes. For Cb, the flux bias is very large, always positive, and varies roughly  
 213 linearly with zenith angle (Figure 1). This gives rise to a bias pattern that roughly mim-  
 214 ics the insolation pattern with latitude and day of year. The albedo bias for Cb is largest  
 215 and positive in the high-latitudes during summer because the mean zenith angle is small,  
 216 since the sun never sets.

217 In addition to the diurnal bias that arises from changes in zenith angle from sun-  
 218 rise to sunset over the course of the day, there is a seasonal cycle in the radiation bias  
 219 resulting from Earth’s orbital obliquity. For instance, equatorial deep convective clouds  
 220 create a TOA albedo bias that peaks during northern hemisphere summer and has a min-  
 221 imum in winter.

### 222 **3.3 Implications for Climate Models**

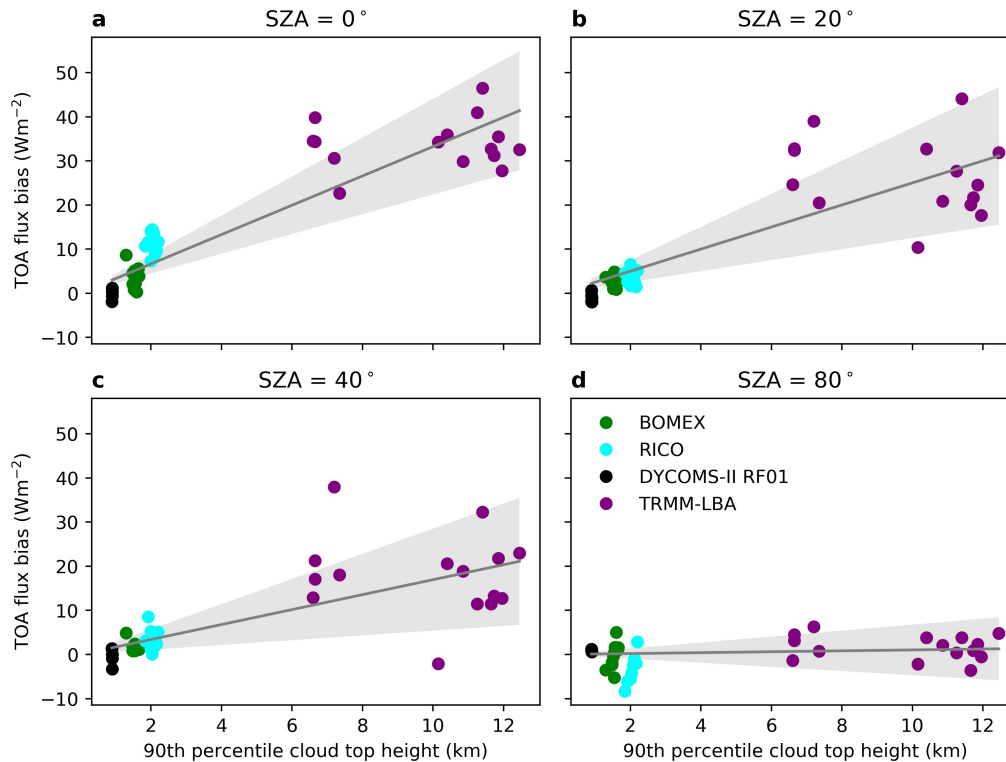
223 To make an assessment of the effect that the 3D radiative transfer through cloud  
 224 fields has on climate simulated with ESMs, we must account for the climatological oc-  
 225 currence of different cloud types in space and time. We observe a strong positive cor-  
 226 relation between CTH and flux bias (Figure 4). Sc have the lowest cloud top and small-  
 227 est flux bias, and Cb have the highest.

228 We regress the flux bias against CTH for 91 evenly spaced solar zenith angles be-  
 229 tween  $0$  and  $90^\circ$ , constraining the regression lines to pass through the origin because there  
 230 is no flux bias in clear-sky conditions ( $\text{CTH} = 0$ ). We define the CTH to be the 90th



**Figure 3.** Daily bias (1D-3D) as a function of latitude and day of year assuming the globe is covered by (a-d) ShCu (BOMEX and RICO), (e-f) Sc (DYCOMS-II RF01), and (g-h) Cb (TRMM-LBA). Left column shows flux bias, and right columns shows albedo bias. Inset panels on the left show annual average biases.

231 percentile height observed in the LES domain. We choose this metric to exclude small,  
 232 ephemeral clouds high in the domain. Note that the deviations from the fit of the Cb  
 233 clouds suggests that this simple linear model is insufficient. The radiative flux bias de-  
 234 pends on more than just CTH, but we use it here as a first approximation to model the  
 235 flux bias.



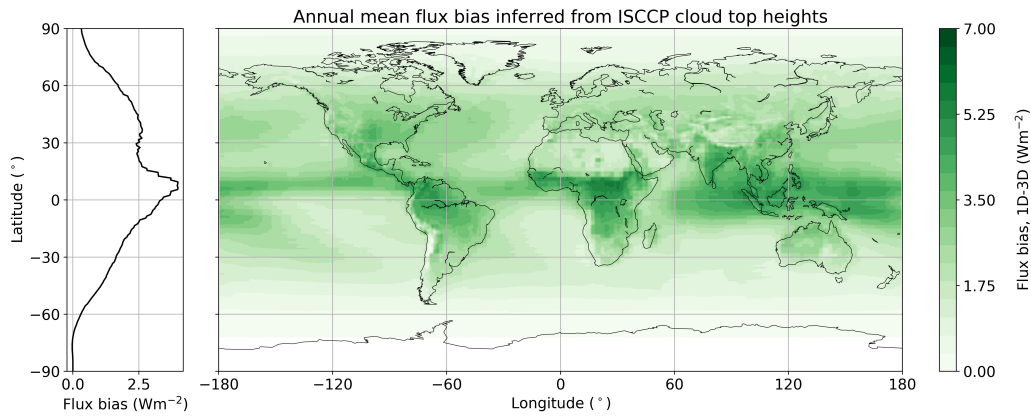
**Figure 4.** Scatter plot of 90th percentile cloud top height (CTH) from LES domain against flux bias at zenith angles (a)  $0^\circ$ , (b)  $20^\circ$ , (c)  $40^\circ$ , and (d)  $80^\circ$ . LES ensemble members are plotted by color (green, cyan, black, and purple for BOMEX, RICO, DYCOMS-II RF01, and TRMM-LBA, respectively). The grey lines and shaded error bars show the linear fits passing through the origin.

236 Using this relationship between CTH and flux bias for a series of zenith angles, we  
 237 can take the observed climatological CTHs from satellite data and infer the resulting flux  
 238 bias that would be associated with using the IPA for RT calculations in place of 3D RT.  
 239 We use the International Satellite Cloud Climatology Project (ISCCP) D2 dataset of CTH  
 240 (W. B. Rossow et al., 1999; W. Rossow & Duenas, 2004; Marchand et al., 2010; C. Stuben-  
 241 rauch et al., 2012; C. J. Stubenrauch et al., 2013). The ISCCP D2 cloud product is a



242 monthly climatological mean with spatial resolution of  $1^\circ \times 1^\circ$  constructed from mea-  
 243 surements during the period 1984 – 2007. These data are collected by a suite of weather  
 244 satellites that are combined into a 3-hourly global gridded product at the D1 level and  
 245 averaged, including a mean diurnal cycle, into the D2 product we use. The monthly tem-  
 246 poral resolution is not inherently an issue for this analysis given that the relationship  
 247 we use between CTH and flux bias is linear.

248 To construct the annual-mean flux bias map shown in Figure 5, we first calculate  
 249 the solar zenith angle for each location on Earth and each hour of the year. Then, we  
 250 obtain the flux bias given the observed CTH from the linear regression of flux bias against  
 251 CTH obtained from the LES data at the given zenith angle (Figure 4).



**Figure 5.** Map of annual mean flux bias inferred from ISCCP CTH. Left panel shows the zonally-averaged flux bias.

252 The largest bias occurs over the tropics in the ITCZ and over the mid-latitude storm  
 253 tracks (Figure 5). The large bias occurs where the tallest clouds on Earth exist and where  
 254 the mean zenith angle is smallest (deep tropics), and also where annual cloud cover is  
 255 high (storm track regions). Polar regions exhibit a negligible annual-mean flux bias due  
 256 to the weak incoming solar flux. The maximum flux bias, occurring in the tropics, is around  
 257  $6 \text{ W m}^{-2}$ , and the zonal-averaged tropical flux bias is estimated to be  $2.7 \pm 0.7 \text{ W m}^{-2}$ .  
 258 Our results agree well with those reported in Cole et al. (2005), who employ 2D radia-  
 259 tive transfer calculations in a superparameterized ESM with 4 km horizontal resolution,  
 260 sufficient to partially resolve deep convective clouds. They found the largest flux bias  
 261 occurring over the ITCZ region and at small zenith angles where cloud-side illumination

262 is important, with a maximum bias of  $5 \text{ W m}^{-2}$  and tropical zonal-average bias of  $1.5$   
 263  $\text{W m}^{-2}$ .

#### 264 **4 Conclusions**

265 We have quantified the radiative flux bias that results from making the IPA, us-  
 266 ing a 3D Monte Carlo radiative transfer scheme applied to LES-generated clouds. The  
 267 flux bias is assessed across different cloud regimes and solar zenith angles. The bias is  
 268 largest and positive for deep convective clouds at small zenith angles; however, the albedo  
 269 bias is largest and negative for shallow cumulus clouds at high zenith angles. The large  
 270 positive flux bias at small zenith angle for Cb clouds translates into a seasonal bias that  
 271 peaks just off the equator in the summer hemisphere, tracking the position of the ITCZ.  
 272 These results are used alongside observations of the climatological occurrence of clouds  
 273 to infer the resulting climate impact. The annual-mean global-mean flux bias is  $1.6 \pm$   
 274  $1.1 \text{ W m}^{-2}$ . The exact magnitude of the flux bias computed here is minimally sensitive  
 275 to the spatial resolution of the LES clouds (Supporting Information). We note, however,  
 276 that even a coarse-resolution LES will resolve cloud morphology with greater detail than  
 277 an ESM. As shown in Figure 1, the flux and albedo bias across zenith angles is signif-  
 278 icantly smaller when making the IPA versus the PPA. So the bias from neglect of 3D RT  
 279 effects in current ESMs is likely larger than the IPA bias which we focused on here.

280 The flux bias computed here is small compared to the TOA shortwave flux root  
 281 mean squared error typically in CMIP5 and CMIP6 models, which is on the order of  $10$   
 282  $\text{W m}^{-2}$  (Zhao et al., 2018; Hourdin et al., 2020). Radiative flux biases attributable to  
 283 clouds in current ESMs are predominantly due to deficiencies of subgrid-scale dynam-  
 284 ical parameterizations that generate cloud cover biases. These biases are distinct from  
 285 what we documented here, which is the bias that exists purely from neglecting the 3D  
 286 cloud morphology during the RT computations (i.e., neglecting horizontal photon fluxes  
 287 when making the IPA). However, as convection parameterizations improve and model  
 288 resolution increases, the relative contribution of 3D RT effects to the total model error  
 289 will increase. Additionally, the 3D bias is still large compared to the signal of anthro-  
 290 pogenic greenhouse gas emissions, which is on the order of  $2.5 - 3.1 \text{ W m}^{-2}$  (Myhre et  
 291 al., 2013).

292 This work is not without caveats. The inferred zenith angle dependence of the flux  
293 bias is based on only four LES cases, and therefore does not represent the full diversity  
294 of cloud morphologies. There is room for future work considering a larger ensemble of  
295 cloud morphologies, which could be generated again by LES or alternatively could be  
296 retrieved from satellite observations. Furthermore, the correlation between CTH and flux  
297 bias seen in these simulations is very high, but not perfect. There is potential for a more  
298 robust mapping from cloud properties to radiative flux bias that could serve as the ba-  
299 sis of a new parameterization of 3D RT effects, for inclusion in current ESMs. However,  
300 the results highlight the importance of considering the 3D radiative fluxes through clouds  
301 for Earth's radiation budget.

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309 Space Administration.

310 All code or data used in this paper are freely available online. The LES were run  
311 using the PyCLES code (<https://climate-dynamics.org/software/#pycles>). The  
312 radiative transfer computations were done using the libRadtran code ([http://www.libradtran](http://www.libradtran.org)  
313 [.org](http://www.libradtran.org)). Post-processed LES 3D fields used as input files for libRadtran computations are  
314 available in Singer et al. (2020). The ISCCP data were downloaded from the GEWEX  
315 database (<https://climserv.ipsl.polytechnique.fr/gewexca/>).

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