## Fatigue Life Analysis of Steel Riveted Rail Bridges Affected by Corrosion

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### Abstract

Decades-old steel bridges have to endure an unfavourable environment that causes the ageing and deterioration of material properties. Moreover, railway bridges in particular are exposed to a large number of stress ranges that may lead to fatigue damage. The combination of both phenomena has a significant impact on the condition of bridges and their remaining service life. In such cases, appropriate maintenance or even removal of the deteriorated structure is necessary; however, a lack of funds often makes this difficult. The subject of this paper is the development of methodology for the assessment of remaining service life of existing steel bridges considering the fatigue and corrosion effects. Using MATLAB<sup>®</sup> software, a program for the prediction of the remaining fatigue life has been developed. The results of earlier experiments and numerical simulations were integrated into this tool. Various scenarios regarding the future maintenance of bridges were included in the program, thus making it possible to calculate the remaining service life of bridges, including corresponding costs. The second half of the paper presents a case study demonstrating the application of the methodology and the calculation program.

Keywords: fatigue life; corrosion; steel bridges; stress spectrum; bridge maintenance

#### Introduction

#### Fatigue Load Effects

The service life of many steel bridges in the Czech Republic, and in many other countries, is close to their expected lifetime and therefore assessment of the current state of such bridges needs to be carried out. In particular, railway bridges, which are known for their permanent resistance to heavy movable loads, are exposed to large stress ranges that may lead to fatigue damage. However, diagnostic methods for existing riveted bridges are limited. Several documents containing background to the assessment of fatigue life of riveted bridges are available. Assessment procedures and detail categories for riveted connections of steel bridges are stated in the International Union of Railways publication UIC 778-2-R.<sup>1</sup> This document considers three groups of significant fatigue-sensitive details of riveted connections. Fatigue strengths of the most common riveted construction details are also available in Ref. [2].

#### **Corrosion Effects**

The corrosion process of steel is affected by many factors, such as the kind of steel and surface protection; environmental impact; and the presence of pollutants, cracks and stresses. The loss of material may result in a reduction in the cross-sectional area and thereby increase the stress level for a given load or increase the stress range for cycling loads. In addition, it can lead to a reduction in the buckling resistance of elements or the initiation of fractures. In general, the loss of cross-sectional area results in a decrease in geometric parameters such as the moment of inertia and radius of inertia.

For the assessment of existing steel members, the loss of material may be taken into account using corrosion models. Corrosion models depict the dependence of corrosion loss on time. Many types of models have been developed.<sup>3</sup> Individual types of corrosion models differ according to the various mathematical functions that describe the development of corrosion loss over time, the various corrosive environments that are considered (rural, urban, etc.) and the various types of steel material.

# Combination of Fatigue and Corrosion Damage

The influence of fatigue and corrosion on the behaviour of riveted connections has been the subject of much experimental and numerical research.4-6 Laboratory tests<sup>7</sup> show that corrosion has a negative impact on the fatigue behaviour of steel riveted connections. As a result of the corrosion process, the surface of steel members becomes rough and the stress distribution changes. The fatigue life of test specimens affected by corrosion is shorter and fatigue cracks occur earlier in comparison to uncorroded elements. The change in length of the fatigue life of corroded members may be expressed as a change in detail category. The detail category becomes worse with increasing corrosion loss.

At present, there are not enough methods available for assessing steel bridge structures affected by degradation and corrosion. The methods used for the assessment of bearing capacity are based on the methods used to assess new constructions. Consideration of corrosion is not sufficiently defined in structural analysis, for either static or fatigue capacity. To solve this problem, only a small amount of background is available to structural engineers. For example, the approach set out in UIC 778-2- $R^1$  is based on the application of a partial safety factor, the value of which depends on the state of the components in terms of corrosion. The consideration of degradation for assessing bridges is also stated in Standards Council of Canada code CAN/CSA-S6-06.8 Chapter 14 of this bridge design code, together with Ref. [9], recommends how to take into account the effects of corrosion on fatigue resistance, using a pitting factor  $K_{\rm p}$ .

For this reason, based on previous research,<sup>7</sup> the aim of the present paper is to develop a methodology that takes into account both fatigue and corrosion. The methodology will be usable for the fatigue assessment of existing steel riveted bridge structures affected by corrosion. Moreover, various scenarios related to maintenance will be taken into account for the remaining service life calculation.

# Remaining Fatigue Life Analysis

#### Fatigue Life Assessment Approaches

Many damage accumulation models have been developed.<sup>10</sup> These models may be classified into two categories: linear damage cumulative theories and nonlinear damage cumulative theories.

The linear damage accumulation theory, also known as the Palmgren– Miner rule,<sup>11</sup> is the most commonly used approach for cumulative fatigue damage analysis. The advantage of this method is its relative simplicity.

The coefficient of fatigue damage according to the Palmgren–Miner rule can be calculated according to Eq. (1):

$$D = \sum_{i=1}^{n} \frac{n_i}{N_i} \tag{1}$$

The end of fatigue life is given by reaching  $D \ge 1$ .

However, there are some disadvantages of the Palmgren–Miner method in comparison to nonlinear damage cumulative theories: the Palmgren– Miner rule does not consider load history, load interaction effects are not considered and cumulative damage has no relationship with load sequence effects. For these reasons, models of nonlinear damage accumulation were developed. These models take into account load interaction effects:

1. Corten–Dolan model<sup>12</sup>

The criterion of failure for the Corten– Dolan model is given as Eq. (2):

$$1 = \sum_{i=1}^{n} \frac{n_i}{N_1 (\sigma_{max}/\sigma_i)^d} \qquad (2)$$

2. Morrow's plastic work interaction rule<sup>13</sup>

The coefficient of fatigue damage under a variable-amplitude loading spectrum can be expressed as Eq. (3):

$$D = \sum_{i}^{n} \frac{n_i}{N_i} \left(\frac{\sigma_i}{\sigma_{\max}}\right)^f$$
(3)

3. V. Dattoma's model<sup>14</sup>

The coefficient of fatigue damage can be calculated according to Eq. (4):

$$D = 1 - \left[1 - \left(\frac{n_i}{N_f}\right)^{1/(1-\alpha)}\right]^{1/(1-\beta)}$$
(4)

Besides these models, there are many other models in the category of nonlinear damage cumulative theories,<sup>10</sup> e.g. the Freudenthal–Heller model and Carpinteri's model.

## Stress Spectrum Calculation

If the effects of traffic are known, then it is possible to make a more accurate calculation of the remaining fatigue life by determining the equivalent stress range using a cycle counting method and an approach of cumulative fatigue damage. Then, the stress spectrum, which is the stress range and the associated number of cycles in descending order, needs to be determined. The input data for calculation of the stress spectrum may be obtained in the following ways:

- 1. Real data obtained from taking measurements on the existing structure. Permanent or temporary monitoring of bridge structures is a very important method used during the bridge diagnostics. In this case, measurement devices and sensors, e.g. strain gauges, are installed in selected locations on the structure. Relative strain dependent on time is the most common form of data obtained by this method. Bridge monitoring is applied during load tests or to obtain information about the effects of day-to-day transport. According to the length of monitoring time, the obtained data may contain effects of one or more trains that crossed over the bridge. For evaluation of the data, a sorting method can be used. The result of this method is the stress spectrum, obtained in the place where the strain gauge was located on the structure.
- 2. Data obtained from numerical models of the evaluated bridge. Suitable software that enables time history analysis can be used to obtain data for the stress spectrum calculation. A numerical

model of the bridge is loaded by load model LM71 or models of real trains, and the effects on the behaviour of the bridge structure are observed. The result of this method is the stress range (or stress amplitude) on individual components obtained from one crossing of the load model.

## Stress Spectrum Generator

A computer program called Stress Spectrum Generator was created in MATLAB<sup>®</sup> software. This is a tool for stress spectrum calculation developed by the authors. The computation algorithm is based on the rainflow counting method. The input data have a form of stress (or strain) over time. If the input data have a form of relative strain, the values are multiplied by the modulus of elasticity and converted into stress values. The outputs from the program are stress ranges divided into a selected number of intervals and a number of cycles of stress ranges falling into the individual intervals. The mean value of each interval is the representative value of the stress range. If the input data were obtained from a static load test, the values of the stress range may be multiplied by a dynamic factor, which is computed according to the selected method.

## Calculation Model for Fatigue Behaviour Prediction of Corroded Steel Bridge Members

Insufficient background and tools are available for the assessment of remaining fatigue life of corroded structures. However, the need for more precise reassessment of existing bridges is becoming more important. For this reason, the calculation model for the fatigue behaviour prediction of corroded steel structures was developed by the authors.

The calculation model, called FALCom (Fatigue Assessment on Level of Component), is a program created in MATLAB software. The model includes the Stress Spectrum Generator program, which enables stress spectra to be calculated. In addition, the results of laboratory fatigue tests on deteriorated riveted members<sup>7</sup> are integrated into the model. The model provides the

calculation relationships considering the change in detail category due to corrosion loss.

# Methodology of the Calculation Model

The model was created to calculate the fatigue damage of structural members that are or are not deteriorated by corrosion and to estimate the remaining service life of such elements. The program is composed of several modules that are connected together: (a) corrosion effects, (b) stress spectrum calculation, (c) calculation of fatigue damage, (d) calculation of remaining fatigue life, and (e) financial costs estimation.

### Corrosion Effects

The rate of corrosion loss is taken into account by corrosion models. Several corrosion models<sup>3</sup> are included in FALCom: (a) the power model, (b) the corrosion model in Ref. [15], and (c) the corrosion model in Ref. [16]

#### Stress Spectrum Calculation

The program Stress Spectrum Generator is included in the calculation model (see "Stress Spectrum Calculation" in the previous section). On the basis of known traffic intensity of individual train units crossing over the bridge, the number of cycles per year is calculated. Stress spectra determined for each train unit are the results of the calculation. If necessary, the obtained values of stress range may be multiplied by dynamic factor.

### Calculation of Fatigue Damage

The fatigue assessment of critical bridge components is based on the approach of cumulative fatigue damage. The following linear and non-linear theories mentioned in "Fatigue Life Assessment Approaches" in the previous section are considered in the methodology: (a) linear cumulative damage theory—the Palmgren–Miner rule, and (b) nonlinear cumulative damage theories—Corten–Dolan's model,<sup>12</sup> Morrow's plastic work interaction model<sup>13</sup> and V. Dattoma's model.<sup>14</sup>

The calculation program takes into account possible weakening of the evaluated members due to corrosion, which is considered by changes in detail category over time. The relationship for the reduction of detail category was taken from the results of laboratory tests focusing on the fatigue behaviour of corroded elements.<sup>7</sup>

# Calculation of Remaining Fatigue Life

The calculation of remaining service life is based on the computational relationships of linear and nonlinear theories mentioned above. In addition, various scenarios considering the different maintenance methods are taken into account. Scenarios for the maintenance of structural members or the whole structure are stated in *Table 1*.

The following values are calculated for each scenario: coefficient of fatigue damage in the future, remaining service life and total service life of the assessed member.

#### Financial costs estimation

The financial costs necessary to maintain the structure during the required remaining service life are estimated on the basis of various scenarios. The scenarios stated in *Table 1* are considered for the calculation. Activities and subactivities related to these scenarios are introduced in *Table 2*. The total financial costs associated with maintenance are subsequently calculated for each scenario as the sum of costs for individual activities.

An approach taking into account the net present value (NPV) was used to compare past and future cash flows with the current ones. Costs are discounted to a common time to be time equivalent. The discount rate of money reflects the cost of the investor's missed opportunities over time. The NPV for costs, taking into account inflation, is determined according to Eq. (5):

$$NPV = \sum_{t=t_M}^{n} \frac{IM \cdot (1+i)^t}{(1+d)^t} \qquad (5)$$

	Scenario	Scenario description
1	No maintenance	There is no maintenance of the structure and structural elements from the corrosion point of view. The coating is not applied $\rightarrow$ the corrosion process continues $\rightarrow$ the detail category gets worse $\rightarrow$ the remaining life of structural elements is the shortest
2	Coating application	The coating is applied on the whole structure or on the critical members $\rightarrow$ the corrosion process does not continue during the coating lifetime. The detail category does not get worse if: (a) the coating lifetime is longer than or equal to the required remaining life of the structure, and (b) the coating is reapplied before the end of its lifetime. If the effectiveness of the coating is lost and there is no reapplication, then the corrosion process continues and the detail category gets worse with time. Finally, the remaining life of structural elements is longer than in scenario 1
3	Strengthening of the critical members + coating application	Strengthening of the critical members is applied. For example, a steel sheet is welded to the bottom flange of the cross-beam $\rightarrow$ the strain of the members increases $\rightarrow$ the stress range increases. At the same time, any increase in the corrosion loss is prevented due to the coating application and the impacts are the same as in scenario 2. The remaining life of structural elements is longer than in scenarios 1 and 2
4	Replacement of the critical members	The critical structural member is replaced by a new element $\rightarrow$ the detail category is equal to (or higher than) the detail category of the original uncorroded member. The remaining life of the structural element is longer than in scenarios 1, 2 and 3

Table 1: Scenarios considered for remaining service life calculation

Scenario	Scenario title	Activities related to financial costs in terms of maintenance		
1	No maintenance	None		
2	Coating application	1. Sandblasting of corroded surface		
		2. Grease removal		
		3. Coating application		
3	Strengthening of the critical	1. Sandblasting of corroded surface		
	members + coating application	2. Grease removal		
		3. Strengthening application		
		4. Coating application		
4	Replacement of the critical members	1. Removal of the original member		
		2. Mounting new steel members including coating application		
		3. Coating application		

Table 2: Activities related to financial costs in terms of maintenance

where *IM* is the financial costs for maintenance  $(\in)$ , *i* is the inflation rate (%), *d* is the discount rate (%), *t<sub>M</sub>* is the year of maintenance, and *n* is the required remaining service life of a bridge (years).

The outputs from the FALCom program are as follows:

- 1. Stress spectrum calculated for all train units crossing over the bridge: number of cycles per crossing and per year.
- 2. Coefficient of fatigue damage in history: includes the time period from bridge construction to the assessment.
- 3. Coefficient of fatigue damage in the future: includes the time period fro the assessment (or since the completion of bridge reconstruction) to the expiration of required remaining life.
- 4. Remaining service life (years).
- 5. Total service life (years).
- 6. Financial costs for the owner necessary to maintain the structure during the required remaining service life.

Points 3–6 are calculated for various scenarios, which depend on the maintenance method or on the type of reconstruction.

#### Comparison of Results of the Calculation Model and Laboratory Fatigue Tests

As mentioned in the subsection "Combination of Fatigue and Corrosion Damage" in the Introduction, experimental fatigue tests on real steel bridge components were conducted and a relationship considering the change in detail category of riveted connections over time was developed.<sup>7</sup> To determine the accuracy of the relationship, the results obtained from the calculation model FALCom and laboratory fatigue tests were compared. The number of cycles until failure was calculated for all tested samples using FALCom. The reduced detail category was calculated on the basis of the original detail category, level of corrosion weakening and cross-sectional dimensions of tested samples.

The mean value of the reduced detail category can be calculated according to Eqs. (6) and (7):

$$\Delta \sigma_{c,R,50} = \Delta \sigma_c \cdot c_{R,50} \quad [\text{MPa}] \quad (6)$$

$$c_{R,50} = (1 - 0.4874 \cdot d_A) \quad [-] \quad (7)$$

The 95% quintile value of the reduced detail category can be according to Eqs. (8) and (9):

$$\Delta \sigma_{c,R,95} = \Delta \sigma_c \cdot c_{R,95} \quad [MPa] \quad (8)$$

$$c_{R,95} = (1 - 0.9954 \cdot d_A) \qquad (9)$$

where  $\Delta \sigma_c$  is the original detail category of an uncorroded sample,  $c_{R,50}$ and  $c_{R,95}$  are reduction coefficients, and  $d_A$  is the level of corrosion determined as the change in cross-sectional area.

The original detail category of the tested riveted connection was 71. Considering the values of stress ranges obtained from fatigue tests, the number of cycles until failure was calculated (*Table 3* and *Fig. 1*). The calculated number of cycles for the 95%

		Number of cycles						
		Experiment	Calculated (mean)	N <sub>exp</sub> /N <sub>calc,</sub> mean	Calculated (95% quintile)	N <sub>exp</sub> /N <sub>calc,</sub> 95% q		
Sample		N <sub>exp</sub>	N <sub>calc, mean</sub>	ΔN (%)	$N_{ m calc, \ 95\% \ q}$	ΔΝ (%)		
1	<b>S</b> 1.1	184 452	194 455	-5	95 228	94		
2	S1.2	251 053	227 343	10	111 333	125		
3	S1.3	186 320	213 522	-13	104 565	78		
4	S1.4	300 140	314 553	-5	154 042	95		
5	S2.1	179 633	202 261	-11	99 051	81		
6	S2.2	161 769	131 912	23	64 600	150		
7	S2.3	222 551	218 639	2	107 071	108		
8	<b>S</b> 3.1	139 313	201 414	-31	98 636	41		
9	S3.2	62 003	57 016	9	27 922	122		
10	S3.3	182 980	139 719	31	68 422	167		
11	<b>S</b> 4.1	104 000	209 654	-50	102 671	1		
12	S4.2	171 843	198 642	-13	97 278	77		
13	S4.3	313 553	259 664	21	127 162	147		

Table 3: Comparison of the results of the calculation model and laboratory fatigue tests



*Fig. 1: Comparison of the results of the calculation model and laboratory fatigue tests. Nexp* = *experimental; Ncalc* = *calculated; 95% q* = 95% *quintile* 

quantile was lower in all cases in comparison with the measured numbers, which means that the calculation is on the safe side.

#### **Case Study**

The application of the method described in the previous section for the assessment of the remaining fatigue life of components is shown in a practical example. The most critical components with respect to fatigue of an old railway steel bridge were assessed and the possibilities for extending the service life of the bridge were analysed.

#### Description of the Bridge

An existing steel railway bridge is used to present the methodology in practice (Fig. 2). The bridge is situated in the Hlubočepské valley in Prague, Czech Republic, and takes a single-track railway over Dalejský brook. The angle of crossing is 70 degrees. The track on the bridge is located in a right-hand arc with a diameter of 334.0 m. The span is 10.0 m, the width is 5.65 m and the total length of the bridge is 26.70 m. From the static point of view, the bridge acts as a simply supported beam. The design velocity of track is 70 km/h. The bridge was built in 1872.

The load-bearing structure consists of two main riveted steel girders of length 10.60 m and the axial distance between them is 2.16 m. The height of the girders is not constant, but changes along the length; this is caused by the varying thickness of the upper and bottom flanges: the outside parts are 890 mm, the intervening parts are 900 mm and the middle parts are 918 mm thick. The upper flange is composed of two to four steel sheets of thickness 8–12 mm that are connected with rivets. The bottom flange is composed of one or two steel sheets of thickness 10–30 mm. The number of sheets changes along the span of the girders. The width of both flanges is the same, at 350 mm. The web consists of steel sheets with dimensions  $830 \times$  $8 \times 1441$ –2630 mm. The interaction between flanges and webs is ensured by isosceles angles  $L78 \times 78 \times 11$  that are joined to the webs and flanges by rivets.

The transverse bracing of the bridge is composed of a total of seven steel riveted cross-beams. Each of them consists of four isosceles angles  $L80 \times 80 \times$ 10 and diagonals  $L70 \times 70 \times 8$ . The axial distance of the bracing is from 1.99 to 2.15 m. The length of crossbeams is 2.16 m, which is the same value as the axial distance of the main girders. The longitudinal bracing of the bridge is composed of bars with cross-section of angles  $L70 \times 70 \times 8$ . These bars, with length 3.0 m, create a truss structure and each pair of cross-ing members is joined with one rivet. This bracing is connected to the upper bars of the lateral bracing and to the upper flanges of the main girders.

#### Current State of the Bridge

A detailed inspection of the bridge has been carried out and the following damage has been discovered. The upper flanges of the main girders have been weakened by corrosion pits and the measured difference between the original and current thickness is 5-6 mm in some parts. The average value of corrosion loss is about 3 mm. Some of the rivets have also been affected by corrosion and the material loss of rivet heads is 30-40% in some cases. The corrosion weakening of the bottom flanges is located close to the support owing to the presence of soil, dust and vegetation. The flange angle is the member most affected by corrosion. The average corrosion loss on



Fig. 2: Railway bridge: (a) longitudinal view; (b) view of the superstructure



Fig. 3: Bridge load: history and future prediction

the flange angle is about 4 mm, especially on the upper surface of the horizontal flange. This fact may have a big influence on the load-bearing capacity and fatigue behaviour of damaged elements and also of the whole structure.

The members of the transverse and longitudinal bracing have not been affected by corrosion or mechanical damage.

The steel structure is made of mild steel with material properties according to Ref. [1]:

- modulus of elasticity:  $E = 200\ 000\ \text{MPa}$
- yield strength:  $f_v = 210$  MPa
- ultimate strength:  $f_{\mu} = 340$  MPa.

#### Fatigue Load and Corrosion Exposure

For the fatigue assessment, only the effects of traffic load, which belongs to the group of variable loads, were considered. Other effects of variable loads, such as wind load, snow load and temperature effects, were neglected.

The load development over time on the track, where the bridge is situated, was taken according to Refs. [17,18]. *Figure 3* shows how passenger and heavy transport changed during the service life of the bridge. It can be seen that there have been big load fluctuations in the bridge's history. At the beginning of the bridge's operation, in 1872, the value of the total load was 0.1 million tonnes per year. This was followed by a gradual increase in passenger and heavy traffic. The most significant changes occurred in the period after the Second World War and the maximum value of track load (2 million tonnes per year) was reached in 1988. Since then, the value of heavy transport started to decrease rapidly (until 2004), although passenger transport continued to increase.

The year 2018 is considered as the year of the assessment, when the value of total track load was 0.98 million tonnes per year. In contrast to the historical loads, at present the passenger transport represents a greater portion of the total load than the heavy transport.

In the future, a slight increase in traffic load may be expected. For this reason, the development of traffic load on the



Table 4: Train units crossing over the bridge at present



Fig. 4: Numerical model of the bridge

bridge in the future is predicted as follows: the load caused by passenger and heavy transport will increase by 0.5% per year (*Fig. 3*). These data are used for the remaining service life calculation.

The number of trains crossing the bridge during one day in 2018 was found out according to the train timetable:

- slow passenger trains: 13
- passenger trains: 58
- goods trains: 2.

Five train units were chosen to represent the movable load on the bridge. Two of them belong to "slow passenger trains", where any axle force is not higher than 120 kN. Another two train units with axle forces higher than 120 kN for each driving vehicle fall into "passenger trains". The last one of the train units is a goods train, which consists of one locomotive and 17 railway cars with a total weight of 5060 t. An overview of train units crossing over the bridge at present is presented in *Table 4*.

As described in "Description of the Bridge" (above), the main beams are affected by corrosion, especially due to the negative impacts of weather. The average value of corrosion loss on the upper and the bottom flanges is 3 and 4 mm, respectively. This fact is taken into account in the assessment of the remaining fatigue life of bridge components. Corrosion models are used for the calculation of corrosion rates in the past and for the prediction of corrosion rates in the future. The assumption is that the coating was applied only during the bridge construction and not reapplied later, up to the present. The coating was estimated to be effective for 20 years.

#### Numerical Model

A three-dimensional numerical model of the bridge was created in CSI Bridge software t determination of the stress ranges that were used for fatigue assessment. All bridge components were modelled as bar elements (one dimension) with the real cross-section characteristics (Fig. 4). Three different cross-sections of main girders due to various thickness of flanges (see "Description of the Bridge", above) were taken into account in the model. Transverse bracing was composed of two isosceles angles  $L80 \times 80 \times 10$  in the upper plane and two isosceles angles  $L80 \times 80 \times 10$ in the bottom plane. Four crossed diagonals with cross-section  $L70 \times 70 \times 8$ filled in the space between the upper and bottom angles. Connections of  $2L80 \times 80 \times 10$  to the main girders were modelled by articulated joints in the horizontal and vertical directions as well as the connection of bars  $L70 \times 70 \times 8$  with  $2L80 \times 80 \times 10$ . Connections of crossed diagonals were



Fig. 5: (a) Beam cross-section; (b) evaluated detail category



Fig. 6: Maintenance scenarios

modelled by articulated crossing to ensure the interaction between them. Horizontal bracing was modelled using bar elements with cross-section of angles  $L70 \times 70 \times 8$ . Bars were connected to the main girders by solid bonds; however, joints, which allow rotation in both vertical and horizontal directions, were placed on both ends of the bracing. Fixed bearings of the bridge, which are located closer to Prague–Smíchov station, were modelled as flexible in the longitudinal and transversal directions of the

bridge. One-direction movable bearings, which are situated closer to Rudná station, were modelled as flexible in the transversal direction of the bridge.

Train units that are currently crossing over the bridge were modelled as a movable load. Axle forces and distances between them fully corresponded to diagrams stated in *Table 4*. The crossing time of each train unit was set up on the basis of the total train length and the speed of 70 km/h, which is the maximum allowed speed of trains on the bridge. The value of modal damping was set to 0.01.

The movable load was located on a track whose position was the same as the position of railway track axis. The track was modelled as a curved bar with radius R = 334 m and was situated 47 mm above the sleepers. The track was joined with the sleepers using solid bonds. Cross-sectional characteristics of the bar were the same as the characteristics of two rails S49.

		Activities and financial costs related to maintenance			
Scenario	Scenario title	Activity	Costs		Unit
1	No maintenance	None	_	0	(€)
2	Coating application	1. Sandblasting of corroded surface	Costs	4	(€/m <sup>2</sup> )
			Area	65	(m <sup>2</sup> )
		2. Grease removal	Costs	1	$(\epsilon/m^2)$
			Area	65	(m <sup>2</sup> )
		3. Coating application	Costs	40	(€/m²/layer)
			Area	65	(m <sup>2</sup> )
			Number of coatings	3	(coatings)
		4. Additional costs	1	0	(€)
3	Strengthening of the critical members + coating application	1. Sandblasting of corroded surface	Costs	4	(€/m <sup>2</sup> )
			Area	65	(m <sup>2</sup> )
		2. Grease removal	Costs	1	(€/m <sup>2</sup> )
			Area	65	(m <sup>2</sup> )
		3. Strengthening application	Costs	8	(€/kg)
			Weight	161	(kg)
		4. Coating application	Costs	40	(€/m²/layer)
			Area	65	(m <sup>2</sup> )
			Number of coatings	3	(coatings)
		5. Additional costs	1	0	(€)
4	Replacement of the critical members	1. Removal of the original member	Costs	0.5	(€/kg)
			Weight	8968	(kg)
		2. New steel members including	Costs	6	(€/kg)
		coating application	Weight	8968	(kg)
		3. Traffic closure	Costs	200	(€/h)
			Time	72	(h)
		4. Coating application	Costs	40	(€/m²/layer)
			Area	65	(m <sup>2</sup> )
			Number of coatings	3	(coatings)
		5. Additional costs		0	(€)

Table 5: Inputs for calculation of financial costs



Fig. 7: Change of corrosion loss over time on the bottom flange



Fig. 8: Change of detail category over time

Time history analysis was applied to calculate the dependence of stress on time in the evaluated elements and cross-sections. Then, the stress spectrum caused by one crossing of a train unit was calculated using the Stress Spectrum Generator. The same procedure was applied to all models of train units. In the next step, the stress spectra for years in history were calculated on basis of the ratio of track load in 2018 to individual years in history.

#### Members Under Assessment

The main beams of the bridge were selected for fatigue assessment and evaluation of remaining fatigue life, for several reasons: (a) low detail category of connections according to Ref. [1], (b) high value of stress range caused by the effects of real trains, and (c) high level of corrosion weakening, especially on the upper and bottom flanges (*Fig. 5*).

Detail categories occurred on the main beam:

- Detail category 71: in the place where the number of sheets, which create the bottom flange, changes. In the present case, the bottom flange in part P3 consists of two sheets (thickness: 30 + 10 mm) and part P2 consists of one sheet (thickness: 30 mm); the cross-section including the last row of rivets in part P2 before the change in the number of sheets was assessed.
- 2. Detail category 85: continuous connection of flange angle and flange; the detail was assessed in the place of maximum bending moment caused by models of real trains.

The value for the partial factor for fatigue strength is taken as:  $\gamma_{Mf} = 1.15$ .

#### **Scenarios**

For the assessment of future service life, four scenarios related to maintenance were considered (*Fig. 6*):

• Scenario 1: "No maintenance". There is no maintenance of the beams → the corrosion process continues and the category detail is getting worse over time. There are no costs for the owner.

- Scenario 2: "Coating application". The coating of the beams is renovated several times in a row (scenario 2a) or once (scenario 2b) according to the required remaining service life of the bridge. The corrosion process does not continue and the category detail is not getting worse.
- Scenario 3: "Strengthening of the critical members and coating application". Additional steel plates are put on the bottom flange of riveted beam for the purpose of increasing the cross-sectional area. The coating is applied several times in a row (scenario 3a) or once (scenario 3b). The corrosion process does not continue, the category detail is not getting worse and the values of stress ranges are lower because of the strengthening.
- Scenario 4: "Replacement of the critical members". The original corroded beams are replaced by new elements. The coating of new beams is applied several times in a row (scenario 4a) or once (scenario 4b).

It is assumed that all of these scenarios are applied in the same year as the bridge assessment is carried out, i.e. in 2018.

Table 5 contains the inputs for the calculation of the financial costs for each scenario. Corresponding activities and costs are entered in the table according to the type of maintenance. There are zero costs for the bridge owner in terms of maintenance in case of scenario 1, which simulates no maintenance during the future service life of the bridge. Scenarios 2 and 3 include activities related to coating application and strengthening of the critical members. Financial costs are dependent on the surface area of both main beams, the number of coatings and the weight of additional steel plates in scenario 3. Among other things, the costs of scenario 4, which is focused on replacement of the critical members, take into account the costs related to traffic closure, which is necessary during the time of reconstruction.

# Results and Evaluation of the Assessment

Applying the methodology developed in the MATLAB software, the assessment of the remaining fatigue life of

				Scenario							
Palmgren-M	1	2a	2b	<b>3</b> a	3b	<b>4</b> a	4b	No corrosion	Year		
CFD	At time of bridge construction	(-)	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1872
	At time of assessment	(-)	0.49	0.49	0.49	0.49	0.49	0.49	0.49	0.32	2018
	At end of required service life	(-)	0.69	0.66	0.68	0.58	0.60	0.03	0.03	0.39	2068
Service life	Required remaining service life (years)		50							_	
	Calculated remaining service life	(years)	102	151	112	182	135	>300	>300	>300	_
	Total service life	(years)	249	298	259	329	282	>500	>500	>500	_
						Scenari	0				
Corten-Dola	n		1	2a	2b	3a	3b	<b>4</b> a	4b	No corrosion	Year
CFD	At time of bridge construction	(-)	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1872
	At time of assessment	(-)	0.44	0.44	0.44	0.44	0.44	0.44	0.44	0.29	2017
	At end of required service life	(-)	0.64	0.61	0.62	0.53	0.55	0.02	0.02	0.36	2067
Service life	Required remaining service life	(years)	50								
	Calculated remaining service life	(years)	109	162	120	197	146	>300	>300	>300	
	Total service life	(years)	256	309	267	344	293	>500	>500	>500	_
	Scenario										
Morrow			1	2a	2b	3a	3b	4a	4b	No corrosion	Year
CFD	At time of bridge construction	(-)	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1872
	At time of assessment	(-)	0.43	0.43	0.43	0.43	0.43	0.43	0.43	0.29	2017
	At end of required service life	(-)	0.64	0.60	0.61	0.53	0.55	0.01	0.02	0.36	2067
Service life	Required remaining service life	(years)	50				_				
	Calculated remaining service life	(years)	110	163	121	199	147	>300	>300	>300	
	Total service life	(years)	257	310	268	346	294	>500	>500	>500	
			Scenario								
V. Dattoma			1	2a	2b	<b>3</b> a	3b	4a	4b	No corrosion	Year
CFD	At time of bridge construction	(-)	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1872
	At time of assessment	(-)	0.42	0.42	0.42	0.42	0.42	0.42	0.42	0.28	2017
	At end of required service life	(-)	0.62	0.59	0.60	0.51	0.53	0.01	0.01	0.35	2067
Service life	Required remaining service life	(years)	50						_		
	Calculated remaining service life	(years)	112	167	124	204	151	>300	>300	>300	_
	Total service life	(years)	259	314	271	351	298	>500	>500	>500	_

CFD = coefficient of fatigue damage.

Table 6: Coefficients of fatigue damage for all scenarios

the steel riveted bridge was conducted. The most critical components with respect to fatigue and corrosion loss were assessed and the possibilities for extending the service life of the bridge were analysed. On the basis of the calculations, the detail category 71 was the decisive detail from the point of view of length of remaining fatigue life. For this reason, the results are shown for the assessment of this detail. Corrosion loss is one of the parameters that affect the length of fatigue life. Corrosion models were used to calculate corrosion rates on the bridge in history and in the future. *Figure 7* shows the dependence of corrosion loss of the bottom flange on bridge age. The dependence was determined by Klinesmith's linear corrosion model.<sup>3</sup> The effectiveness of the original protective coating was estimated at 20 years. After the effectiveness of the coating was lost, the corrosion weakening began. At the time of bridge assessment, the average corrosion loss value was equal to 4 mm, which corresponds to the measured value. Regarding the corrosion loss in the future, scenario 1 leads to the highest value. Each of scenarios 2, 3 and 4 is divided into two cases: the full lines correspond to the situation when the coating is applied repeatedly, which means that the corrosion loss is no longer increasing. On the other hand, the dashed lines symbolize only one application of coating with an effectiveness of 20 years. The red and green lines in scenarios 2 and 3 overlap because of the similar maintenance procedure. The bridge age at the time of evaluation was 147 years.

The presence of corrosion loss has a negative impact on the fatigue behaviour of the corroded elements. The main reason for the is the changing of detail category with various corrosion levels.<sup>7</sup> The change in detail category over time is shown in Fig. 8. The original detail category of the evaluated member was assumed to be 71. In scenario 1, which corresponds to no bridge maintenance, the detail category is getting worse during the whole future service life of the bridge, because the process of corrosion loss is not stopped or interrupted. Scenarios 2 and 3 have a similar effect: the detail category is not getting worse during the time of coating effectiveness. Finally, the

assumption of scenario 4 is that the detail category of the new construction member is higher than that of the original one, in this case 85 instead of 71.

Table 6 summarizes the results of the assessment. The calculations are divided for each scenario according to the approach of fatigue assessment (linear and nonlinear theories). In the first step, coefficients of fatigue damage values were calculated at the time of bridge assessment (2018) and at the end of the required service life The required remaining (2068).service life was set to 50 years. Then, the remaining service life of the detail was calculated for all scenarios. The total service life is given as a sum of the current structure age and calculated remaining service life.

The calculated remaining service life for all scenarios is longer than required (coefficients of fatigue damage are lower than 1). However, comparing the results, scenario 1 results in the shortest service life of the bridge. The remaining service life for scenario 1 is



Fig. 9: Dependence of fatigue damage coefficients on time (Palmgren–Miner linear theory)



Fig. 10: Financial costs in the future: (a) total financial costs; (b) financial costs over time

102 years, according to the calculations. Scenario 4 gives the longest service life of the bridge. The calculated remaining service life is longer than 300 years. The dependence of coefficients of fatigue damage on time for all scenarios and the approach of linear theory is shown in *Fig. 9*.

Nonlinear approaches of calculation provide more favourable results than linear approaches (*Table 6*). The main reason for this is that nonlinear approaches take into account the load interaction effects.

From the bridge owner's point of view, financial costs play an important role in decision making. Costs related to all considered scenarios are shown in Fig. 10. On the basis of Table 5, there are zero costs in the case of scenario 1 owing to the absence of maintenance works. On the other hand, scenario 4 ensures the longest service life; however, the costs are the highest for the owner. An approach taking into account the NPV was used to compare past and future cash flows with the current ones. The value of the discount rate was set to 0.5%. The inflation rate was taken into account using a value of 2.0%. Figure 10 shows maintenance costs over time.

#### Conclusion

This paper presented the methodology developed for the assessment of remaining fatigue life of steel riveted bridge components. FALCom software was developed for automatic calculation of the remaining fatigue life, including the consideration of the current corrosion weakening and corrosion conditions.

The application of the developed methodology was shown in a practical example. The most critical components with respect to fatigue of an old railway steel bridge were assessed and the possibilities for extending the service life of the bridge were analysed.

The following conclusions may be drawn from the case study:

- 1. The calculated remaining fatigue life of the detail for all scenarios is longer than required. The longest remaining service life is ensured by scenario 4, where the critical components are replaced.
- 2. On the basis of the calculations, the bridge may be in service for another 100 years without any maintenance.

However, there are several uncertainties, such as the development of traffic intensity and the composition of traffic in the future.

- 3. In the case where the required service life would be longer than the current 50 years, scenarios 2 and 3 would provide suitable solutions to ensure the efficient fatigue capacity of the bridge. Scenarios 2a and 3b provide a similar remaining service life for approximately the same financial costs.
- 4. The approach of nonlinear accumulation of fatigue damage provides favourable results from the point of view of length of service life. The values of coefficients of fatigue damage are lower in the case of nonlinear approaches.
- 5. The developed methodology including FALCom software may be a suitable tool for more accurate evaluation of the current state of historical steel riveted bridges. Finally, the methodology can lead to cost savings, as historic bridges can be in operation for a long time without the need for extensive reconstruction.

#### Suggestions for Subsequent Research

The next phase of this research will focus on the optimization of scenarios. The most suitable maintenance procedure for the bridge, with respect to required service life and financial costs, will be evaluated.

## Nomenclature

$c_{R,50}$	reduction coefficient
CR 95	reduction coefficient
D	coefficient of fatigue damage
d	material parameter (Eq. $(2)$ )
d d	discount rate (Eq. (5))
$d_{\Lambda}$	level of corrosion determined
A	as the change in cross-section
	area
Ε	Modulus of elasticity
f	Morrow's plastic work inter-
	action exponent
$f_{\mu}$	Ultimate strength
$f_{v}$	Yield strength
i	inflation rate
IM	financial costs for the
	maintenance

-	n	required remaining service life
t		of a bridge
)-	n:	number of cycles at a given
		stress amplitude
A	$N_i$	number of cycles to failure at a
u	- 1	given stress amplitude
n	NPV	net present value
2	N	calculated number of cycles
-	r vcalc, mean	(mean value)
t	N 1 050	calculated number of cycles
_	r calc, 95% q	(95% quintile)
*	N	measured number of cycles
1	t exp	voor of maintenance
l-	$\iota_M$	for the former of the demonstrated
	α	function in the damage model
	β	coefficients of the damage
-		model
S	$\Delta \sigma_{c}$	original detail category of an
t	c	uncorroded sample
e.	$\Delta \sigma_{c R 50}$	mean value of reduced detail
f	0,10,00	category
	$\Delta \sigma_{c R 95}$	95% quintile value of reduced
C	0,10,00	detail category
	σ	the i <sup>th</sup> load stress level
	71	

σ<sub>max</sub> maximum stress of multilevel alternating load stress

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