

# Numerical simulation of bitumen emulsion-stabilised base course mixtures with C&D waste aggregates considering nonlinear elastic behaviour

Ignacio Pérez<sup>a,\*</sup>, Luis Medina<sup>a</sup>, Breixo Gómez-Meijide<sup>b</sup>, Pedro Alves Costa<sup>c</sup>, Antonio Silva Cardoso<sup>c</sup>

<sup>a</sup>Universidad da Coruña. Department of Civil Engineering. E.T.S.I. Caminos, Canales y Puertos, Campus de Elviña s/n, 15071. A Coruña, Spain

\*Corresponding author. Tel.: +34-981167000. Fax: +34-981167170

<sup>b</sup>European Asphalt Pavement Association. R. du Commerce 77, 1040 Brussels, Belgium

<sup>c</sup>Faculty of Engineering of the Universidade do Porto, R. Roberto Frias. Porto, Portugal

E-mail addresses: [iperez@udc.es](mailto:iperez@udc.es) (I. Pérez); [lmedina@udc.es](mailto:lmedina@udc.es) (L. Medina); [breixo@eapa.org](mailto:breixo@eapa.org) (B. Gómez Meijide); [pacosta@fe.up.pt](mailto:pacosta@fe.up.pt) (P.A. Costa); [scardoso@fe.up.pt](mailto:scardoso@fe.up.pt) (A. S. Cardoso)

## Abstract

This study presents the numerical modelling of a load-volume road pavement section with bitumen emulsion-stabilised base courses. The base courses used natural and construction and demolition aggregates. A 3D finite difference model was used to determine the peak responses of the pavement sections when subjected to loads. Three nonlinear models were adopted in the two base courses. The response predictions of the three models were similar. Both the resilient and permanent behaviours of these materials were modelled. An analysis was conducted on the rutting resistance of the base course materials. Both base courses were suitable for use in low-volume roads. The base course made with construction and demolition aggregates was more resistant to rutting.

**Keywords:** FLAC3D, bitumen emulsion, stabilised base course, C&D waste aggregates, rutting.

## 1. Introduction

Bitumen-stabilised materials with emulsion (BSM) are not only more environmentally friendly but also more economical than other types of asphalt mixtures such as hot-mix asphalt (HMA). Thus, these mixtures of aggregates, asphalt emulsion, and water, which can be mixed, stored, and transported at room temperature, are gaining importance in the field of road engineering as a tool to fight against climate change. Furthermore, the latest developments in cold asphalt technology have contributed to minimise classical problems such as their higher air-void content after compaction and weak early-life strength [1, 2]. Both the environmental and economic aspects can be enhanced by replacing natural aggregates (NAs) with recycled aggregates from construction and demolition waste (CDAs), in a similar way other publications have demonstrated for different road construction materials such as concrete [3, 4] and HMA [5, 6].

36 BSM materials exhibit a behaviour similar to both granular materials (stress dependency) and HMA  
37 (temperature and frequency of loading dependency) [7, 8]. According to Jenkins et al. [9] and Ebels  
38 [10], the nonlinear elastic behaviour tends to be highlighted at early curing stages after pavement  
39 construction, while the viscoelastic behaviour becomes more significant when the material is cured  
40 after a period of time that sometimes lasts several months or years.

41 According to some authors [9, 10, 11], the nonlinear behaviour of BSM materials makes the shear  
42 strength the most critical mechanical property. Consequently, the failure of BSM materials is  
43 principally the result of significant permanent deformation (rutting) with an irreversible effect on the  
44 structural and functional state of pavement. In this sense, Ebels [10] and Hornych et al. [12] studied  
45 the nonlinear behaviour of a BSM-type grade emulsion using triaxial tests. This behaviour was  
46 checked by Santagata et al. [13] with a short-term evaluation of the mechanical properties of BSMs. It  
47 was also studied in a laboratory by Gómez-Meijide and Pérez [14] for BSMs with NAs and CDAs by  
48 means of dynamic-load triaxial tests such as resilient modulus ( $M_r$ ) and permanent deformation  
49 constant confining pressure (CCP) tests.

50 In this context, in most cases, the structural analysis of pavement with BSM layers is performed under  
51 the similar principles employed in pavement with HMA layers [15]. In this way, BSM materials are  
52 studied as elastic or viscoelastic materials [15]. For instance, Shanbara et al. [16] investigated the  
53 linear elastic behaviour of cold-mix asphalt using the finite element method to obtain deflections on  
54 the pavement. The authors also obtained the stress and strain distributions in a cold asphalt mix with a  
55 glass fibre and predicted the rutting behaviour of natural fibre-reinforced cold-mix asphalt using the  
56 finite element method taking into account the viscoelastic behaviour [17]. Nevertheless, a different  
57 way to proceed is to consider the nonlinear nature of BSM materials. In this regard, Pérez et al. [18]  
58 used the nonlinear parameters obtained by Ebels [10] to investigate the nonlinear performance of  
59 BSMs and determine that rutting is the main mechanism of failure in these materials and that they are  
60 suitable for use in light-traffic roads.

61

62

## 63 **2. Aim and scope**

64 In this study, the laboratory results of the nonlinear behaviour investigations performed by triaxial  
65 tests were translated into numerical simulations with a fast Lagrangian analysis of continua in three  
66 dimensions (FLAC3D) model. The model predict the real behaviour of a base course pavement section  
67 made with BSM materials in low-volume roads. In this regard, the responses at critical positions of the  
68 pavement layers and the cumulative permanent deformation (rutting) of the BSM layers were  
69 analysed.

70 The simulations were performed for BSM made with cured and uncured CDAs, and the results were  
71 compared with those obtained with a controlled mixture made purely with NA. The simulations were  
72 performed to demonstrate that BSMs made with NA and CDA have enough structural capacity to  
73 resist rutting in low-volume road pavement. A complementary objective was to determine if it was  
74 possible to use a CDA as a substitute for an NA and, if so, if any of the properties of the BSM  
75 materials were improved. This would contribute to sustainable construction, as CDAs would be  
76 valued.

## 77 **3. Materials properties**

### 78 *3.1. BSM base-course properties*

#### 79 *3.1.1. Gradation*

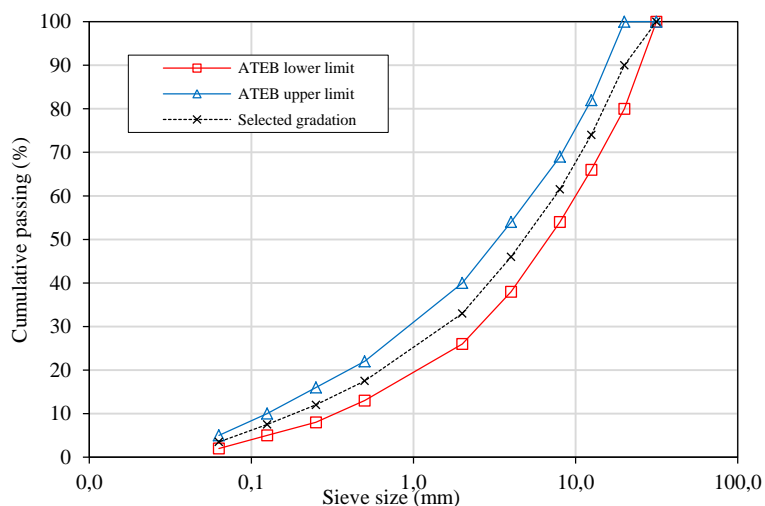
80 A continuous gradation-type grave-emulsion aggregate (Fig. 1) was selected for the BSM base-course  
81 material as specified by the Spanish Technical Association of Bituminous Emulsions (ATEB) [19].  
82 This gradation was suitable for medium- and low-traffic levels. In Spain, grave emulsion has been  
83 employed as a base-course layer with very good resistance to permanent deformation. In addition, it  
84 has been used as an anti-reflecting cracking layer, obtaining excellent results that place it above  
85 cement-treated layers.

#### 86 *3.1.2. Aggregates and bitumen emulsion properties*

87 BSM materials with CDA were studied. The main part of the recycled aggregate was composed of  
88 concrete, mortar, and stone with a certain proportion of impurities such as ceramic, metal pieces,  
89 gypsum, plastic, and glass. All the tests were repeated with control mixes for comparison purposes.  
90 The aggregate of these mixes was a natural common metamorphic siliceous aggregate (NA) extracted

91 from a local quarry in Ourense, Spain. The main characteristics of the NA and CDA are listed in Table  
 92 1.

93 The selected binder was C60B5GE, a cationic slow-setting bitumen emulsion (60% bitumen content)  
 94 with a 100-pen-grade base bitumen that fulfilled the specifications of the UNE EN 13808 standard.



95  
 96  
 97

**Fig. 1.** BSM aggregate gradation with ATEB recommendation.

**Table 1.** Characterisation of CDA and NA aggregates [14]

Property	CDA	NA
Flakiness index (UNE EN 933-3)	4.5%	19.8%
Crushed particles (UNE EN 933-5)	89%	94%
Sand equivalent (UNE EN 933-8)	77%	78%
Los Angeles coefficient (UNE EN 1097-2)	38%	14%
Bulk specific gravity (UNE EN 1097-6)	2.64 t/m <sup>3</sup>	2.78 t/m <sup>3</sup>
Dry specific gravity (UNE EN 1097-6)	2.23 t/m <sup>3</sup>	2.74 t/m <sup>3</sup>
SSD specific gravity (UNE EN 1097-6)	2.39 t/m <sup>3</sup>	2.75 t/m <sup>3</sup>
Absorption coefficient (UNE EN 1097-6)	7.0%	0.5%

98

### 99 3.1.3. Preparation of samples

#### 100 *Optimum bitumen content and water content*

101 The indirect tensile strength ratio (ITSR) test according to the Standard EN 12697-12 was used to  
 102 determine the optimum bitumen and water contents. For the BSM made with NA, four series of 10  
 103 cylindrical samples each were manufactured with 3 % of water content and four different bitumen  
 104 contents (2, 3, 4, and 5%). For the BSM made with CDA, four series of 10 cylindrical samples each  
 105 were manufactured with 9 % of water content and four different bitumen contents (5, 6, 7, and 8%).  
 106 The samples with CDAs needed a higher amount of water and bitumen because these aggregates have

107 a very high absorption coefficient (Table 1). Five samples of each series were conditioned (wet group)  
108 and the other five samples remained at room temperature (dry group) according to EN 12697-12.  
109 Then, both groups of samples were subjected to the indirect tensile strength (ITS) tests according to  
110 the Standard EN 12697-23. Once the ITS<sub>R</sub> test results for the NA samples were analysed it was found  
111 that the optimum contents were 4% of bitumen and 3% of water (ITS<sub>R</sub>=79%; ITS<sub>dry</sub>=851 kPa and  
112 ITS<sub>wet</sub>=675 kPa). For the CDA the samples the optimum contents were 6% of bitumen and 9% of  
113 water (ITS<sub>R</sub>=70%; ITS<sub>dry</sub>=862 kPa and ITS<sub>wet</sub>=602 kPa). It was considered that ITS<sub>R</sub>≥70% are  
114 suitable for BSM base courses for medium- and low-traffic levels.

#### 115 *Final samples for resilient modulus test and permanent deformation test*

116 Finally, for the resilient modulus and permanent deformation tests (Figure 2) the BSM samples were  
117 prepared with a diameter of 100 mm and a height of 200 mm with the two types of aggregates as  
118 published by Gómez-Meijide and Pérez [14]. All the samples with NA were manufactured with 3%  
119 water and 4% bitumen, and all the samples with CDA were manufactured with 9% water and 6%  
120 bitumen. After compaction some samples were testing immediately, and others were left to cure three  
121 days in an oven at 50 °C before testing. According to the ATEB, the curing of the samples for three  
122 days is equivalent to a real highway in-situ curing period of six months [19].

#### 123 *3.1.4. Mechanical properties*

##### 124 *Resilient modulus nonlinear models*

125 A nonlinear elastic behaviour was adopted for the base layers of the BSM material. The specific  
126 weight,  $\gamma_{sat}$ , was 22.0 kN/m<sup>3</sup>, and the coefficient of earth pressure at rest,  $K_0$ , was 0.6. The Poisson  
127 coefficient,  $\nu$ , was 0.35. The nonlinear elastic behaviour was determined by dynamic load triaxial tests  
128 with CCP in accordance with the Standard EN 13286-7 recommendations as published by Gómez-  
129 Meijide and Pérez [14]. The test apparatus used consisted of a removable chamber and an axial-load  
130 system generator (Fig. 2). An independent air compressor was used to provide the confining pressure  
131 (maximum 10 bar), while a hydraulic system was used to control the axial load generator.

132 Three different resilient modulus ( $M_r$ ) models were fitted to the experimental data. The models were  
 133 the Hicks model ( $M_r$ - $\theta$  model) [20], Uzan model [21], and NCHRP model (proposed by the National  
 134 Cooperative Highway Research Program) [22] described respectively as

$$135 \quad M_r = k_1 \cdot \theta^{k_2}, \quad (1)$$

$$136 \quad M_r = k_1 \cdot \theta^{k_2} \cdot \sigma_d^{k_3}, \quad (2)$$

$$137 \quad \frac{M_r}{P_a} = k_1 \left( \frac{\theta}{P_a} \right)^{k_2} \left( \frac{\tau_{oct}}{P_a} + 1 \right)^{k_3}, \quad (3)$$

138 where  $\theta$  is the sum of the principal stresses or bulk stress ( $\theta = \sigma_1 + 2\sigma_3$ ),  $\sigma_d$  is the deviator stress,  $\tau_{oct}$  is  
 139 the octahedral stress,  $P_a$  is a reference pressure ( $P_a = 101.35$  kPa), and  $k_1$ ,  $k_2$ , and  $k_3$  are the material  
 140 constants used for the FLAC3D numerical simulations.



141  
 142 **Fig. 2.** Sample and sensor arrangement for resilient modulus triaxial test according to Standard EN 13286-7.  
 143

144 The model parameters of Gómez-Mejjide and Pérez [14] were obtained by minimising the squared  
 145 error between the models and the experimental moduli obtained in the laboratory. The coefficient  
 146 values of the three models for CDAs and NAs are listed in Table 2.

147 **Table 2.** BSM nonlinear model coefficients [14]

Aggregate	Cured	Model							
		Hicks		Uzan			NCHRP		
		$k_1$	$k_2$	$k_1$	$k_2$	$k_3$	$k_1$	$k_2$	$k_3$
NA	yes	157.678	0.341	119.112	0.651	-0.302	7.765	0.550	-0.477
	no	16.132	0.596	11.583	1.033	-0.438	2.563	0.925	-0.721
CDA	yes	9.489	0.720	6.998	1.113	-0.393	2.664	1.087	-0.796
	no	9.755	0.636	7.469	0.990	-0.355	1.856	0.925	-0.633

148

149 As shown in Table 2, the cured and uncured BSM materials with NA had higher coefficient values.  
 150 Therefore, BSM materials with NA are stiffer than BSM materials with CDA. In addition, BSM  
 151 materials with NAs and CDAs are stiffer after curing.

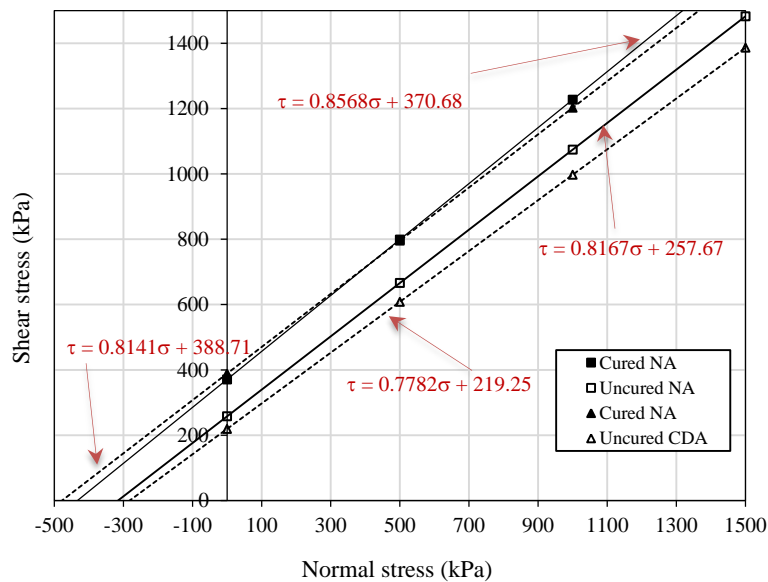
152 *Shear strength parameters*

153 The shear strength parameters cohesion ( $c$ ) and angle of friction ( $\varphi$ ) were obtained by Gómez-Meijide  
 154 and Pérez [14] by means of static triaxial tests (Table 3). Some authors [9, 10, 18] consider that  $c$  and  
 155  $\varphi$  determine the shear strength and therefore the resistance to permanent deformation of BSM  
 156 materials. The results in Table 3 show that in both aggregates after curing,  $c$  and  $\varphi$  increased and  
 157 improved the resistance to permanent deformation.

158 **Table 3.** Shear strength parameters [14]

Aggregate	Cured	$c$ (kPa)	$\varphi$ (°)
NA	yes	370.68	45.1
	no	257.67	43.6
CDA	yes	388.71	43.5
	no	219.25	42.1

159



160  
 161  
 162

**Fig. 3.** Mohr–Coulomb envelopes obtained for BSM mixtures.

163 In Fig. 3, the Mohr–Coulomb envelopes are plotted using the values of the shear parameters of Table  
 164 3. As seen for the uncured samples,  $c$  was lower for the BSM with CDA than with NA. However, after  
 165 curing, the  $c$  value of BSM with CDA increased and reached and even surpassed that of the BSM with

166 NA. The angle  $\varphi$  was greater for BSM with NA both before and after curing. However, all of the  
 167 recorded values were similar and between  $42^\circ$  and  $45^\circ$ . In Fig. 3, the curves of both materials were  
 168 very similar after curing. Therefore, after curing, BSM with an NA or a CDA will have very similar  
 169 shear strength.

170 *Cumulative axial permanent-strain model*

171 The permanent deformation behaviour was determined by dynamic-load triaxial tests with CCP in  
 172 accordance with Standard EN 13286-7 recommendations as published in Gómez-Meijide and Pérez  
 173 [14]. The permanent deformation of the BSM base course was studied using a double exponential  
 174 model that predicted the three phases of the cumulative axial permanent strain ( $\varepsilon_p$ ) versus the number  
 175 of load cycles (N) [10, 14] as

$$176 \quad \varepsilon_p = A \left( \frac{N}{1000} \right)^B + C \left( e^{D \frac{N}{1000}} - 1 \right), \quad (4)$$

$$177 \quad A = a_1 (SR)^{a_2}; B = b_1 (SR)^{b_2}; C = c_1 (SR)^{c_2}; D = d_1 (SR)^{d_2},$$

178 where  $a_1, a_2, b_1, b_2, c_1, c_2, d_1,$  and  $d_2$  are fitted experimental coefficients. The values of the eight fitted  
 179 coefficients for BSM materials with CDA and NA are listed in Table 4.

180 **Table 4.**  $\varepsilon_p$  model coefficients [14]

Aggregate	Cured	$a_1$	$a_2$	$b_1$	$b_2$	$c_1$	$c_2$	$d_1$	$d_2$
NA	yes	1.2902	0.692	0.00007	2.0299	$7 \cdot 10^{-13}$	5.7974	$1 \cdot 10^{-27}$	15.854
	no	0.4606	0.9308	0.00001	2.4538	$1 \cdot 10^{-35}$	19.303	$1 \cdot 10^{-36}$	20.649
CDA	yes	0.8552	0.7533	0.00005	2.0674	$5 \cdot 10^{-19}$	9.4728	$2 \cdot 10^{-19}$	10.784
	no	0.4261	0.8936	0.000001	2.7873	$1 \cdot 10^{-21}$	9.7506	$9 \cdot 10^{-46}$	24.703

181  
 182 The shear parameters were used to calculate the stress ratio (SR) expressed as the ratio between the  
 183 acting deviator stress ( $\sigma_d$ ) and the deviator stress at failure ( $\sigma_{d,f}$ ) for the Mohr–Coulomb criterion [9]:

$$184 \quad SR = \frac{\sigma_d}{\sigma_{d,f}} = \frac{\sigma_1 - \sigma_3}{\sigma_3 \left[ \tan^2 \left( 45^\circ + \frac{\varphi}{2} \right) - 1 \right] + 2c \tan \left( 45^\circ + \frac{\varphi}{2} \right)}, \quad (5)$$

185 where  $\sigma_1$  and  $\sigma_3$  are the major and minor principal stresses, and  $c$  and  $\varphi$  are the shear parameters listed  
 186 in Table 3. Jenkins et al. [9] reported that SR is a critical parameter that expresses the mechanical  
 187 response of BSM materials to permanent deformation. As the value of the SR increases, the  $\varepsilon_p$  value  
 188 increases as well. According to Jenkins et al. [9], when the SR value is over 0.40, rutting may occur. It  
 189 is important to find the critical position of the SR in the base course. To do this,  $\sigma_1$  and  $\sigma_3$  must be



190 obtained using FLAC3D at different locations in the BSM base course which permit the computation  
191 of the SR by means of Equation 5. The critical position is the point with the maximum SR.

### 192 3.2. HMA wearing course

193 A linear elastic behaviour was assumed for the HMA wearing course: elastic modulus  $E = 5.0 \times 10^6$   
194 kPa and  $\nu = 0.35$ . A specific weight  $\gamma_{sat} = 24.0 \text{ kN/m}^3$  and a coefficient of earth pressure at rest of  $K_0 =$   
195 0.6 were assumed.

### 196 3.3. Cement-stabilised soil material

197 A linear elastic behaviour was considered for the ‘in place’ cement-stabilised fine-grained soil (CSS)  
198 subgrade with an elastic modulus  $E = 1.0 \times 10^6$  kPa and Poisson coefficient  $\nu = 0.25$ . A specific  
199 weight  $\gamma_{sat} = 22.0 \text{ kN/m}^3$  and a coefficient of earth pressure at rest of  $K_0 = 0.6$  were assumed.

### 200 3.4. Fine-grained soil

201 A nonlinear elastic model was adopted for the fine-grained soil subgrade [15, 23]:

$$202 \quad M_r = k_1 + k_3(k_2 - \sigma_d) \quad \sigma_d \leq k_2,$$

$$203 \quad M_r = k_1 + k_4(\sigma_d - k_2) \quad \sigma_d \geq k_2, \quad (6)$$

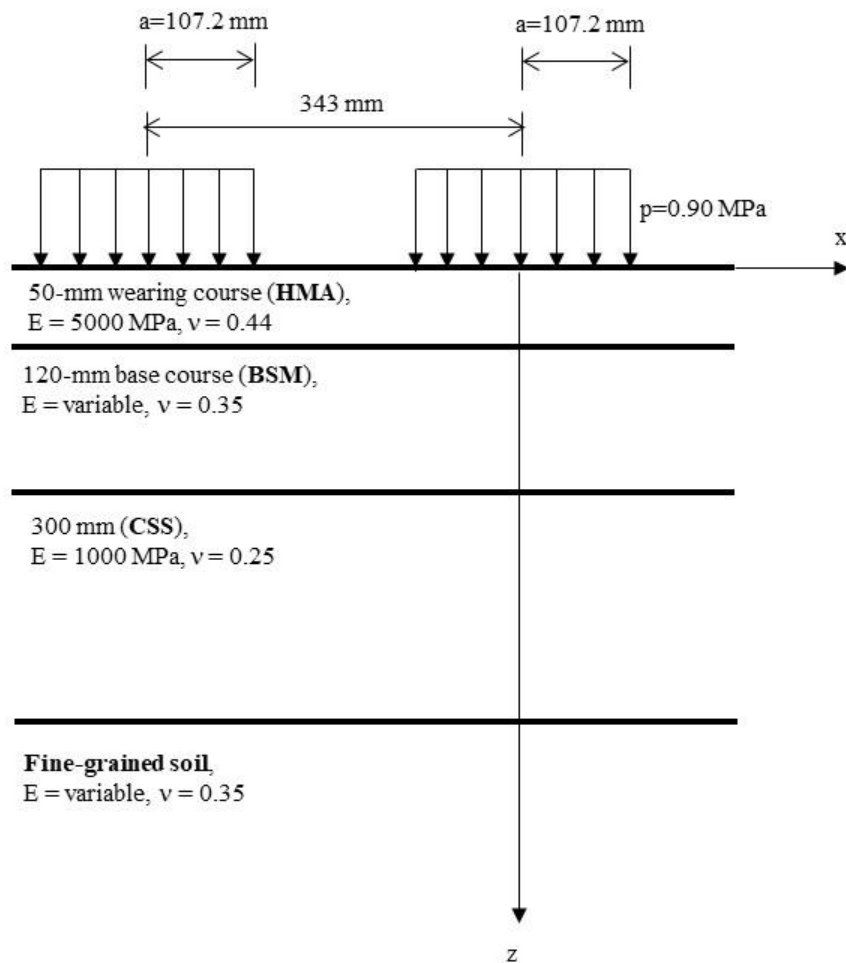
204 where  $k_1 = 8.5 \cdot 10^4$  kPa,  $k_2 = 42.8$  kPa,  $k_3 = 1,110$  kPa, and  $k_4 = 178$  kPa are coefficients obtained from  
205 dynamic triaxial tests [15, 23]. A specific weight  $\gamma_{sat} = 20.0 \text{ kN/m}^3$ , a coefficient of earth pressure at  
206 rest of  $K_0 = 0.6$ , and a Poisson coefficient of  $\nu = 0.35$  were assumed.

## 207 4. Pavement section and numerical model

208 The section selected for the analysis was defined by the ATEB [19] for low-volume roads with BSM  
209 base courses, specifically for the traffic category T4: annual average daily heavy traffic ( $AADT_{HT}$ )  
210  $\leq 49$  heavy vehicles/day. The section consisted of a 50-mm-thick HMA wearing course overlying a  
211 BSM-type material 120-mm-thick base course placed over a subgrade composed of two layers: an ‘in  
212 place’ 300-mm-thick CSS and a fine-grained soil (Fig. 4).

213 The Spanish standard 130-kN single axle with two dual tyres (65 kN carried by each set of dual tyres)  
214 was adopted as the load configuration for the analysis. Two homogeneous circular loads  $p$  of 0.90  
215 MPa were applied with a radius  $a$  of 107.2 mm, and the distance between the radial centres was 343  
216 mm (Fig. 4).

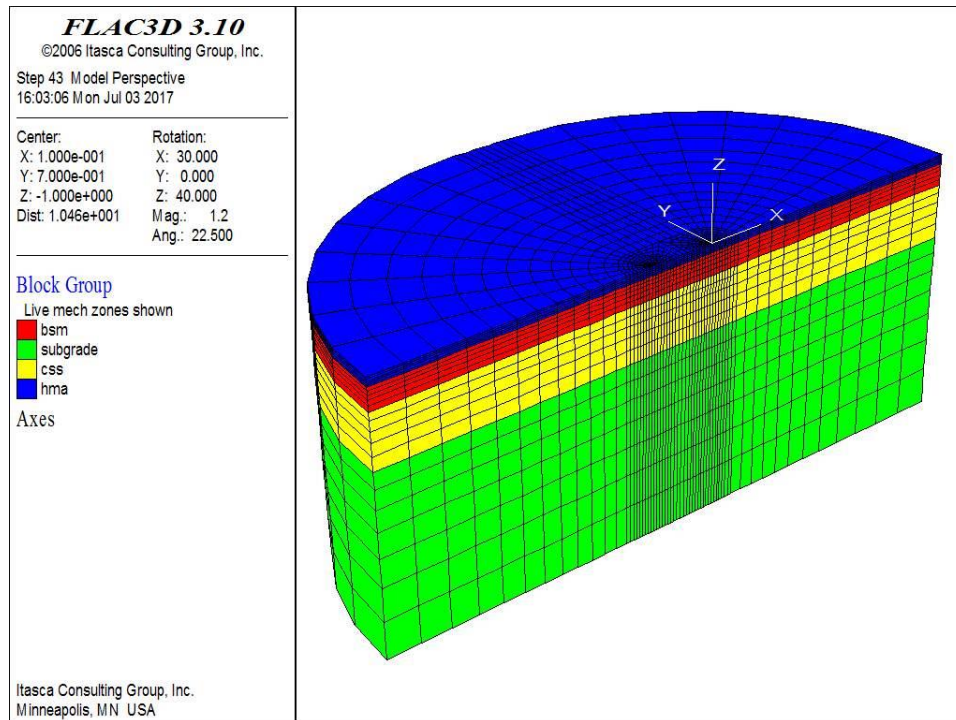
217 A numerical model to obtain the stresses and deformations produced in the pavement by the  
 218 application of a load configuration on its surface was developed with FLAC3D 3.10 [24].  
 219 FLAC3D is a 3D program that uses a specific scheme of finite differences which permits the  
 220 simulation of the elastic–plastic behaviour of the materials used in the pavement layers. By means of  
 221 FLAC3D, the materials are represented by polyhedral elements forming a 3D grid that fits the shape of  
 222 the modelled object. Each element behaves according to an established law of stress—strain (linear or  
 223 nonlinear) in response to the applied loads and the boundary conditions. The material may yield and  
 224 be plastically deformed. Figure 5 shows the grid of finite difference elements and the coordinate  
 225 system used in the pavement section for the dual tyres. The model contained 2,500 elements and 2,900  
 226 nodes. Given the conditions of symmetry entailed in the problem (in terms of geometry and loads),  
 227 only half of the real problem was studied taking care to impose the appropriate boundary conditions in  
 228 the symmetry plane.



229

230

Fig. 4. Pavement section used for modelling.



**Fig. 5.** Mesh and coordinate system.

231  
232  
233  
234  
235  
236  
237  
238  
239  
240  
241  
242  
243  
244  
245  
246  
247  
248

The following boundary conditions were applied:

- Movement was banned in y-direction on plane  $y = 0$  (symmetry plane).
- Movement was banned in the x- and y-directions on the lateral (circular) edge of the grid. The lateral edge of the grid was located 1.4 m from the dual tyres; therefore, it would have a minimal effect on the results.
- All movement was banned on the lower plane  $z = -1.24$  m.
- The ground-water level was assumed to be very deep and therefore did not interfere with the numerical simulations as the materials were not submerged. Hence, the total stresses coincided with the effective stresses. The contact between the layers was one of total adherence (equality of horizontal deformations). The process reproduced with the numerical model consisted of two phases. The first phase provided the state of in-situ stresses existing in the pavement before applying the tyre loads. Once a state of mechanical equilibrium was reached for the specific weights and boundary conditions were applied, all model movements were reset to zero. In the second phase of the modelling, the tyre loads were applied.

## 249 **5. Results and discussion**

### 250 *5.1. Predicted responses in BSM base course with three nonlinear models*

251 The values of the three nonlinear models coefficients obtained experimentally (Table 2) were used in  
252 the FLAC3D model to obtain the variation of the  $M_r$  through the BSM base-course depth below the  
253 tyre loads (Fig. 6). In addition, three BSM base-course responses were monitored at the following  
254 critical points:

- 255 • Deflection in the BSM higher fibre ( $d_B$ ) vs. distance to centre of dual tyres axle (Fig. 7).
- 256 • Tensile strain in BSM lower fibre ( $\epsilon_{rB}$ ) vs. distance to centre of dual tyres axle (Fig. 8).
- 257 • SR in the BSM higher fibre vs. distance to centre of dual tyres axle (Fig. 9).

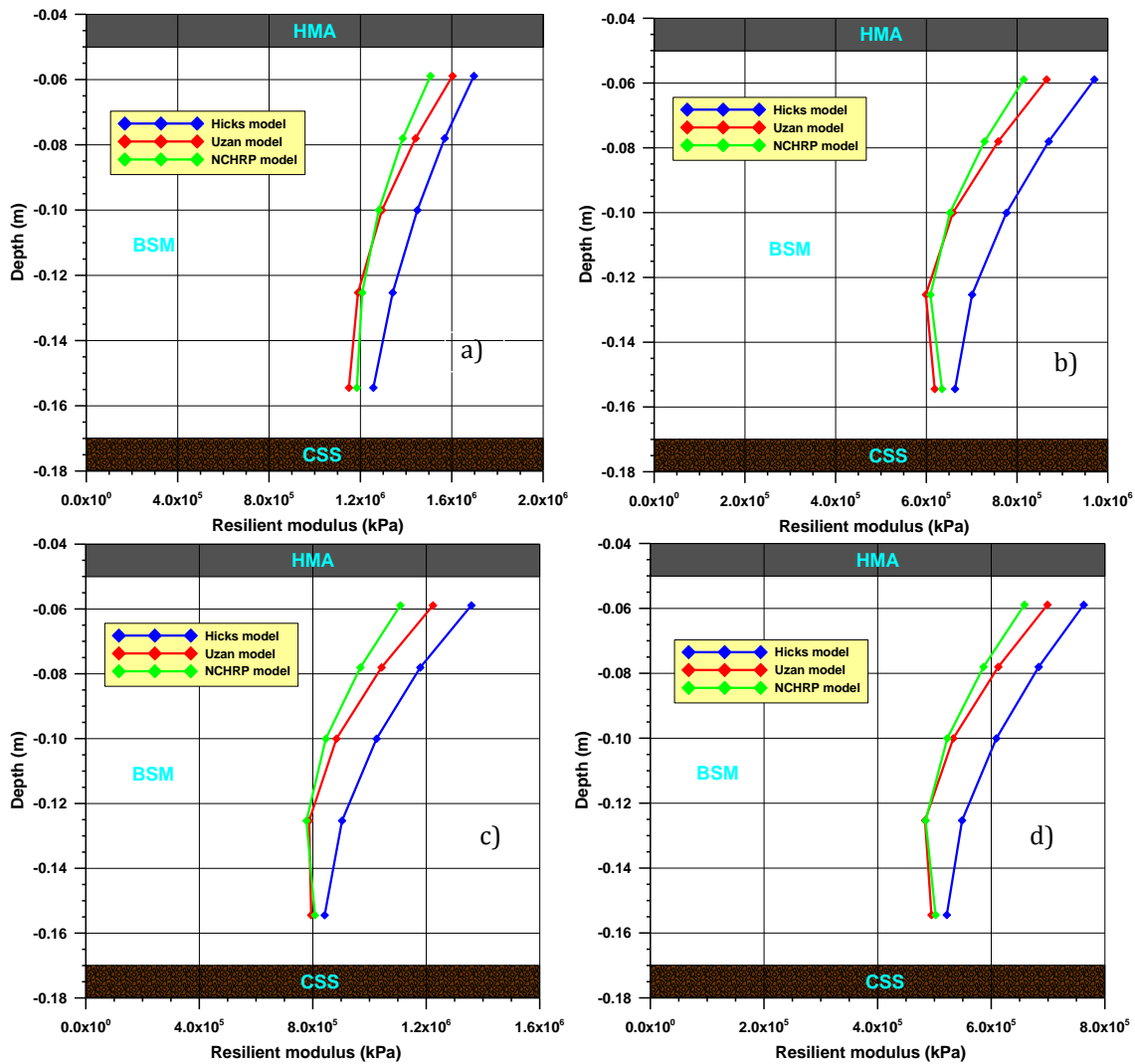
#### 258 *5.1.1. Resilient modulus*

259 The  $M_r$  variation through the BSM course depth predicted by the three models is shown in Fig. 6. The  
260  $M_r$  was predicted for the BSM materials cured and uncured with NAs and CDAs. As can be seen in the  
261 four cases, as the depth of the BSM base course increased, the  $M_r$  diminished because the stresses  
262 diminished with the depth. Therefore, the BSM showed a clear nonlinear behaviour with stress  
263 dependency. The slopes of the curves predicted by the three models were similar. Equations 2 (Uzan  
264 model) and 3 (NCHRP model) predicted a similar  $M_r$ , and after 0.125-m depth, both equations  
265 practically predicted the same values. Furthermore, Equation 1 (Hicks model) predicted a higher  $M_r$   
266 than Equations 2 and 3.

267 In the NA-BSM base course of the NCHRP model, after curing, the  $M_r$  varied between approximately  
268  $1.2 \times 10^6$  kPa and  $1.5 \times 10^6$  kPa (Fig. 6a), and before curing, it fluctuated between  $6.5 \times 10^5$  kPa and  
269  $8.0 \times 10^5$  kPa (Fig. 6b). The  $M_r$  of the CDA-BSM base course after curing varied between  
270 approximately  $8.0 \times 10^5$  kPa and  $1.1 \times 10^6$  kPa (Fig. 6c), and before curing it fluctuated between  
271 approximately  $5.0 \times 10^5$  kPa and  $6.5 \times 10^5$  kPa (Fig. 6d).

272 Therefore, as expected, the NA-BSM base course displayed a higher stiffness before and after curing  
273 than that of the CDA-BSM base course. Nevertheless, when the base courses were uncured, the  
274 stiffness difference between the BSM materials with NA and with CDA was less significant.  
275 Moreover, both the NA-BSM and CDA-BSM base courses displayed a higher stiffness after curing.

276



277

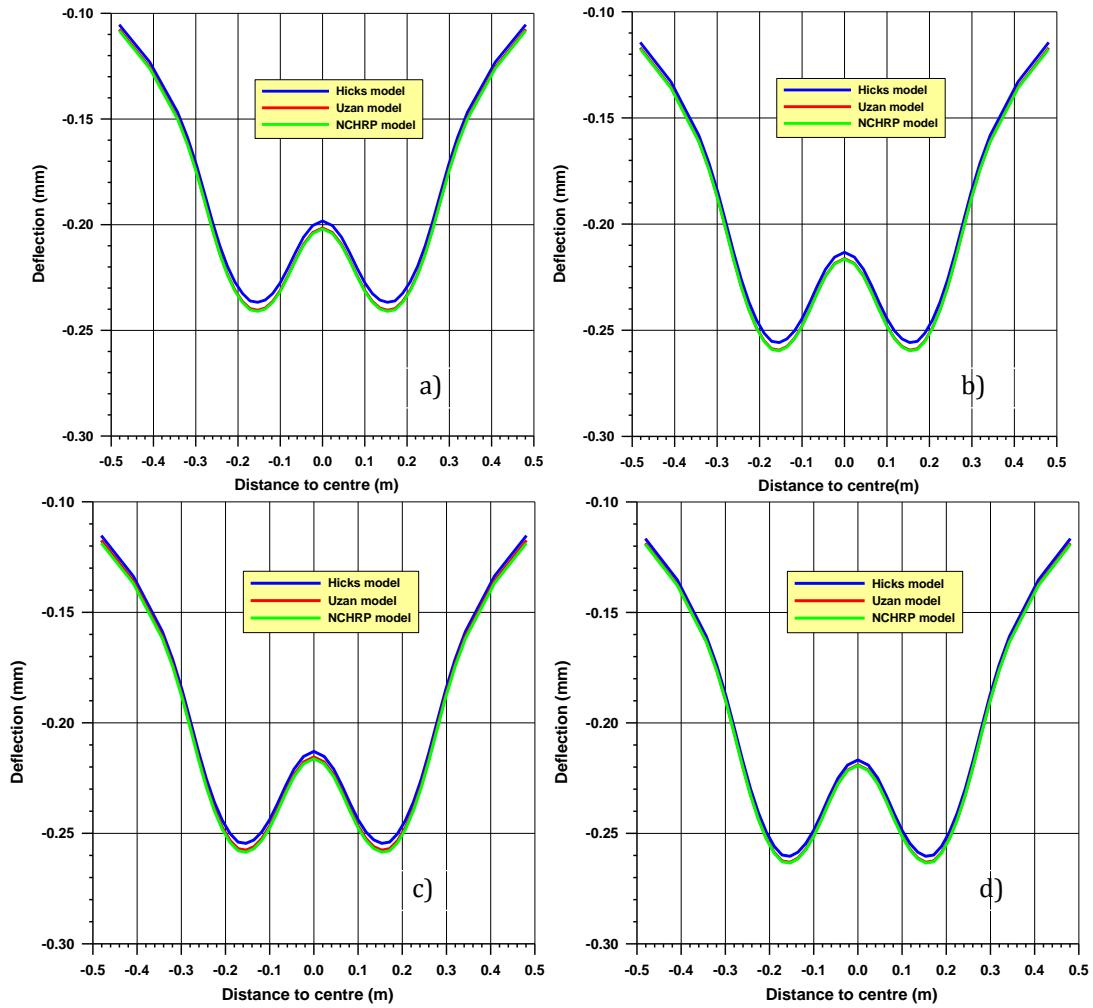
278  
279  
280

Fig. 6. Resilient modulus variation in BSM course: a) cured NA, b) uncured NA, c) cured CDA, and d) uncured CDA.

281 *5.1.2. Deflections*

282 The deflection variation in the BSM base-course higher fibre ( $d_B$ ) for the three nonlinear models in the  
 283 previous four conditions are shown in Fig. 7. The peak deflections were produced just below the two  
 284 tyres, and the Uzan and NCHRP models predicted the same deflection values, while the Hicks model  
 285 predicted slightly lower values (Table 5). This is expected because the Hicks model predicts a higher  
 286  $M_r$  (Fig. 6). Clearly, the cured BSM base courses had lower peak-deflection values, and the lowest  
 287 deflections were produced in the NA-BSM.

288

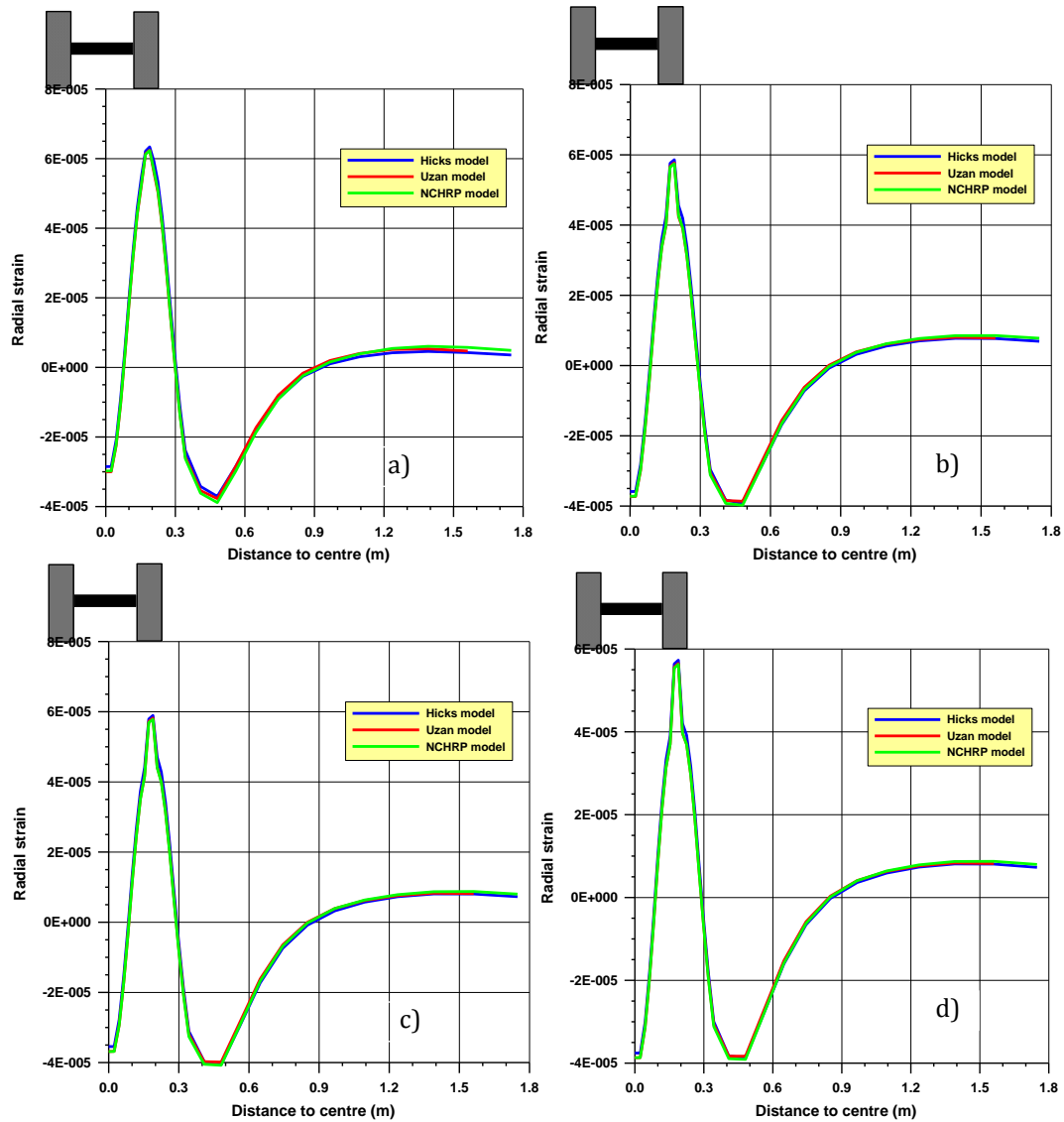


289  
290  
291  
292

**Fig. 7.** Deflection variation of BSM base course of three models: a) cured NA, b) uncured NA, c) cured CDA, and uncured CDA.

### 293 5.1.3. Tensile strains

294 The tensile strains in the BSM base-course lower fibre ( $\epsilon_{rB}$ ) predicted by the three nonlinear models  
295 versus the distance to the axle-dual tyres centre are shown in Fig. 8. The peak tensile strains were  
296 produced just below the tyres. Moreover, the values of the tensile strains were at compression (minus  
297 sign) between approximately 0 m and 0.1 m and between 0.3 m and 0.9 m from the axle-dual tyres  
298 centre. The tensile strains were at traction (plus sign) below the tyres between 0.1 m and 0.3 m and  
299 beyond 0.9 m from the axle-dual tyres centre. The Uzan and NCHRP models predicted similar peak  
300 tensile strain values, while the Hicks model predicted slightly higher values (Table 5) as shown in Fig.  
301 8. This was expected because the Hicks model predicts higher  $M_r$  values. The peak tensile strains were  
302 higher with cured NA-BSM base courses.



303

304  
305  
306  
307

**Fig. 8.** Tensile strain variation of BSM base course of three models: a) cured NA, b) uncured NA, c) cured CDA, and d) uncured CDA.

**Table 5.** Peak predicted responses in BSM layer using three nonlinear models

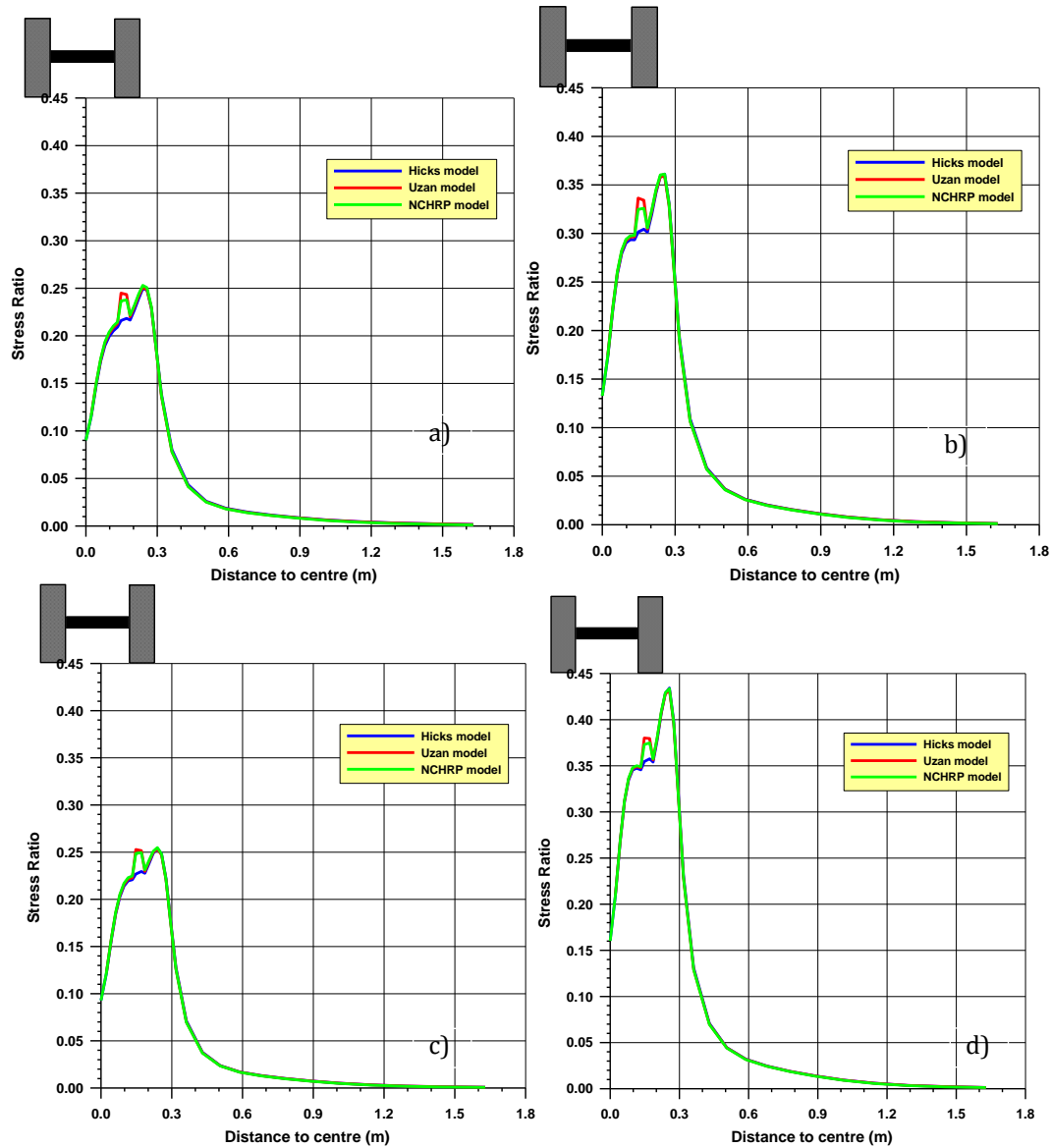
Aggregate	Cured	Model								
		Hicks			Uzan			NCHRP		
		$d_B$ (mm)	$\epsilon_{rB}$ ( $\mu\epsilon$ )	SR	$d_B$ (mm)	$\epsilon_{rB}$ ( $\mu\epsilon$ )	SR	$d_B$ (mm)	$\epsilon_{rB}$ ( $\mu\epsilon$ )	SR
NA	yes	0.237	64.2	0.250	0.241	62.2	0.252	0.241	62.3	0.253
	no	0.256	58.9	0.362	0.260	58.1	0.360	0.260	57.4	0.362
CDA	yes	0.256	58.6	0.255	0.259	57.6	0.255	0.259	57.8	0.256
	no	0.261	57.5	0.435	0.264	56.3	0.432	0.264	56.3	0.434

308

#### 309 5.1.4. Strain ratios

310 Figure 9 represents the SR calculated in the higher fibre of the BSM base course where the highest  
 311 values were obtained versus the distance to the axle-dual tyres centre. The highest peak SR prediction  
 312 values were produced at 0.25 m from the axle-dual tyres centre. Moreover, the three nonlinear models  
 313 practically predicted the same highest peak SR (Fig. 9, Table 5).

314 Before curing, the peak SRs of the CDA-BSM were higher than those of the NA-BSM (Table 5).  
 315 However, when the BSM was fully cured, the values of the peak SRs were similar in both types of  
 316 aggregate. The curing of BSM materials produced a sharp decrease in the peak SR values, and this  
 317 drop was even greater in the CDA-BSM base course.



318

319  
 320  
 321  
 322

**Fig. 9.** SR variation on BSM base course of three models: a) cured NA, b) uncured NA, c) cured CDA, and d) uncured CDA.

323 The peak SR predictions of the CDA-BSM base course before curing varied between 0.432 and 0.435  
 324 (Table 5). These values were higher than the 0.40 considered by Jenkins et al. [9] as the limit to  
 325 prevent rutting in a base course. Therefore, if this limit is correct, rutting will occur in an uncured  
 326 CDA-BSM base course. Finally, the three nonlinear models predicted similar deflections, tensile  
 327 strains and SRs. The Hicks model was very easy to use and had a lower computational cost than the



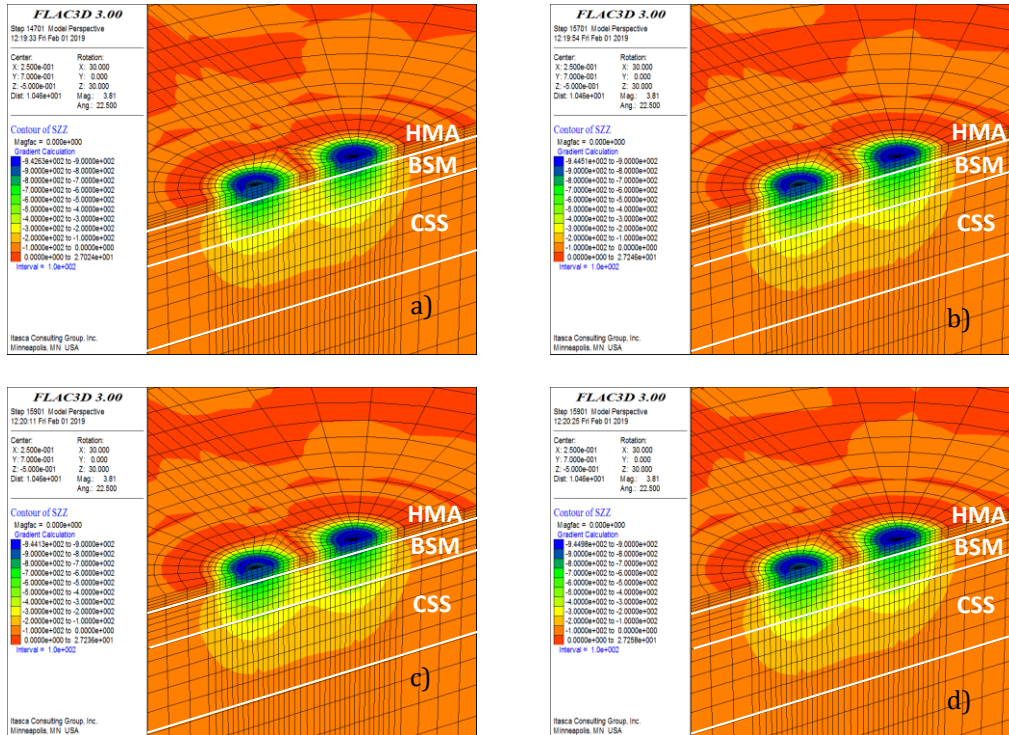
328 other models. Nevertheless, it predicted values slightly on the unsafe side because it predicted lower  
329 deflections. The Uzan and NCHRP model predictions were more similar. Nevertheless, the NCHRP  
330 model was the most modern and developed model and was selected for this study because of these  
331 considerations.

### 332 *5.2. Stresses in pavement section*

333 Having selected the NCHRP model, the vertical and horizontal stresses in the pavement were  
334 calculated. As shown in Fig. 10, the vertical stresses in the pavement were always in compression  
335 (negative sign) except in some HMA surface zones between the dual tyres and a distance from the  
336 tyres centre that were working at traction (positive sign). These compression stresses decreased with  
337 an increase in the pavement depth and with an increase in the radial distance to the centre of the tyres.  
338 In Fig. 10, the difference between the vertical stress values in the NA-BSM bases course and those in  
339 the CDA-BSM bases course were insignificant. Below the tyre load of the HMA lower fibre, the  
340 compression vertical stresses were between 700 kPa and 800 kPa, in the BSM lower fibre between 300  
341 kPa and 400 kPa, and in the CSS lower fibre between 0 kPa and 100 kPa. At some points far from the  
342 load centre, the vertical stresses were working at a maximum value of 27.25 kPa.

343 The pavement horizontal stresses are shown in Fig. 11. In the HMA and CSS lower-fibre cases, the  
344 horizontal stresses were at traction, and the CSS-layer higher slice was at compression. Nevertheless,  
345 in the BSM base courses, the horizontal stresses were at compression, while as shown in Fig. 8, the  
346 tensile strains were at traction in the lower fibre. This occurred because the tensile strains shown in  
347 Fig. 8 were the result of only the tyre loads, while in the Fig. 11 the horizontal stresses (at the same  
348 lower fibres) were the result of not only the tyre loads but also the in-situ compressive stresses owing  
349 to the pavement's own weight.

350



351

352

**Fig. 10.** Vertical stresses in pavement (negative sign indicates compression): a) cured NA, b) uncured NA, c) cured CDA, and d) uncured CDA.

353

354

355

Below the tyre loads, in the HMA and CSS-layer lower fibres, the traction horizontal stress values

356

ranged between 0 kPa and 99.57 kPa (cured NA-BSM), 0 kPa and 124.16 kPa (uncured NA-BSM), 0

357

kPa and 94.43 kPa (cured CDA-BSM), and 0 kPa and 164.59 kPa (uncured CDA-BSM). Therefore, as

358

in the HMA and CSS layers, the horizontal stresses at traction were similar when the CDA-BSM and

359

NA-BSM base courses were cured. When the base courses were uncured, the horizontal stresses were

360

higher in the CDA-BSM base course. In addition, the horizontal stresses at traction were higher before

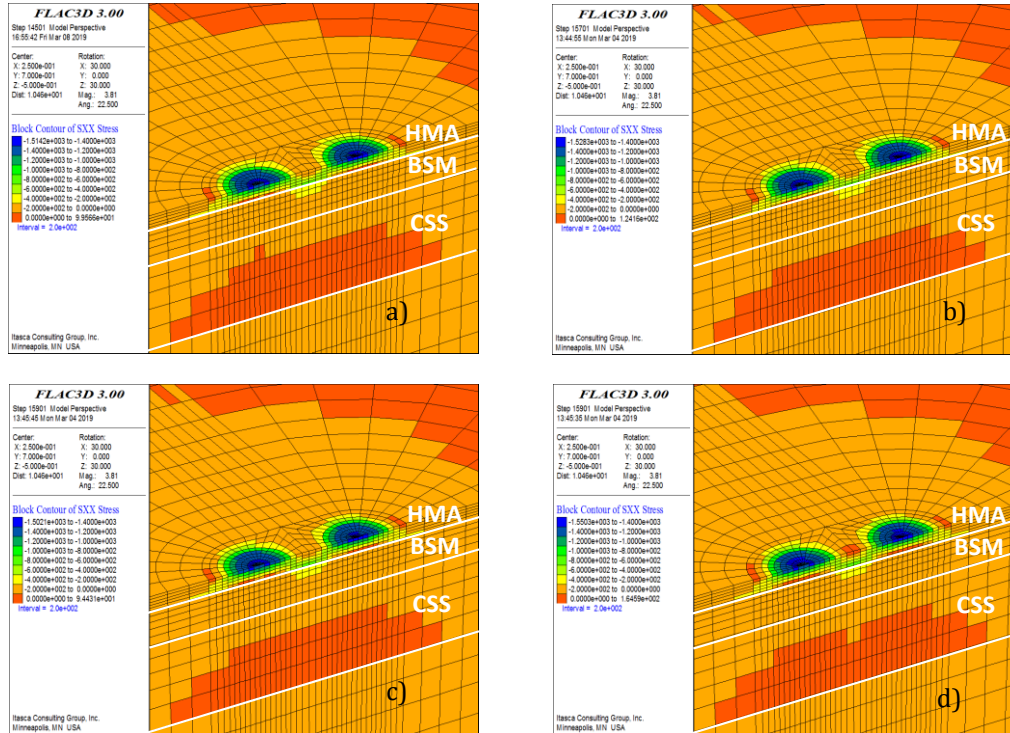
361

curing. The horizontal stresses of the BSM base courses were always at compression and between 0

362

kPa and 400 kPa for the two aggregates before and after curing.

363



364

365  
366  
367

**Fig. 11.** Horizontal stresses in pavement (negative sign indicates compression): a) cured NA, b) uncured NA, c) cured CDA, and d) uncured CDA.

368

### 5.3. Peak responses in pavement layers of different thicknesses

369

The pavement critical peak responses were calculated by FLAC3D for several thicknesses of HMA

370

wearing course and BSM base course. The thickness of the CSS layer was maintained at 300 mm. An

371

analysis was performed to determine the effect of variations in the thickness of BSM base course and

372

HMA wearing course on the performance of structural pavement layers. Seven pavement peak

373

responses were analysed at the following critical points:

374

- HMA wearing course: peak vertical deflection on the surface ( $d_H$ ) and peak tensile strain in the lower fibre ( $\epsilon_{rH}$ ) (Fig. 12),

375

376

- BSM base course: peak vertical deflection in the higher fibre ( $d_B$ ), peak tensile strain in the lower fibre ( $\epsilon_{rB}$ ), and peak SR in the higher fibre (Fig. 13),

377

378

- CSS subgrade layer: peak tensile stress in the lower fibre ( $\sigma_r$ ) (Fig. 14), and

379

- fine-grained soil subgrade: peak axial strain on the upper fibre ( $\epsilon_v$ ) (Fig. 15).

380

Each of the above-mentioned figures contain a legend. Using Fig. 12 as an example, the first term of

381 the legend denotes the type of aggregate used in the BSM base course (NA or CDA), and the second  
382 term denotes the type of layer thickness variation (HMA wearing course or BSM base course). Thus,  
383 CDA-HMA means that the BMS base course is constructed with CDAs and the HMA peak responses  
384 are a function of the HMA thickness variation. NA-BSM means that the BMS base course was  
385 constructed with NAs and the HMA peak responses are a function of the BSM thickness variation.  
386 The x-axis represents the critical peak responses, the left y-axis (HMA thickness) varies between 3 cm  
387 and 10 cm, and the right y-axis (BSM thickness) fluctuates between 8 cm and 22 cm. Moreover, the  
388 peak response curves versus the HMA wearing-course thickness were made with a constant 12-cm  
389 BSM base course; while the peak response curves versus the BSM base course thickness were made  
390 with a constant 5-cm HMA wearing course. Therefore, the curves for the 5-cm wearing-course and the  
391 12-cm BSM base-course thicknesses intercepted.

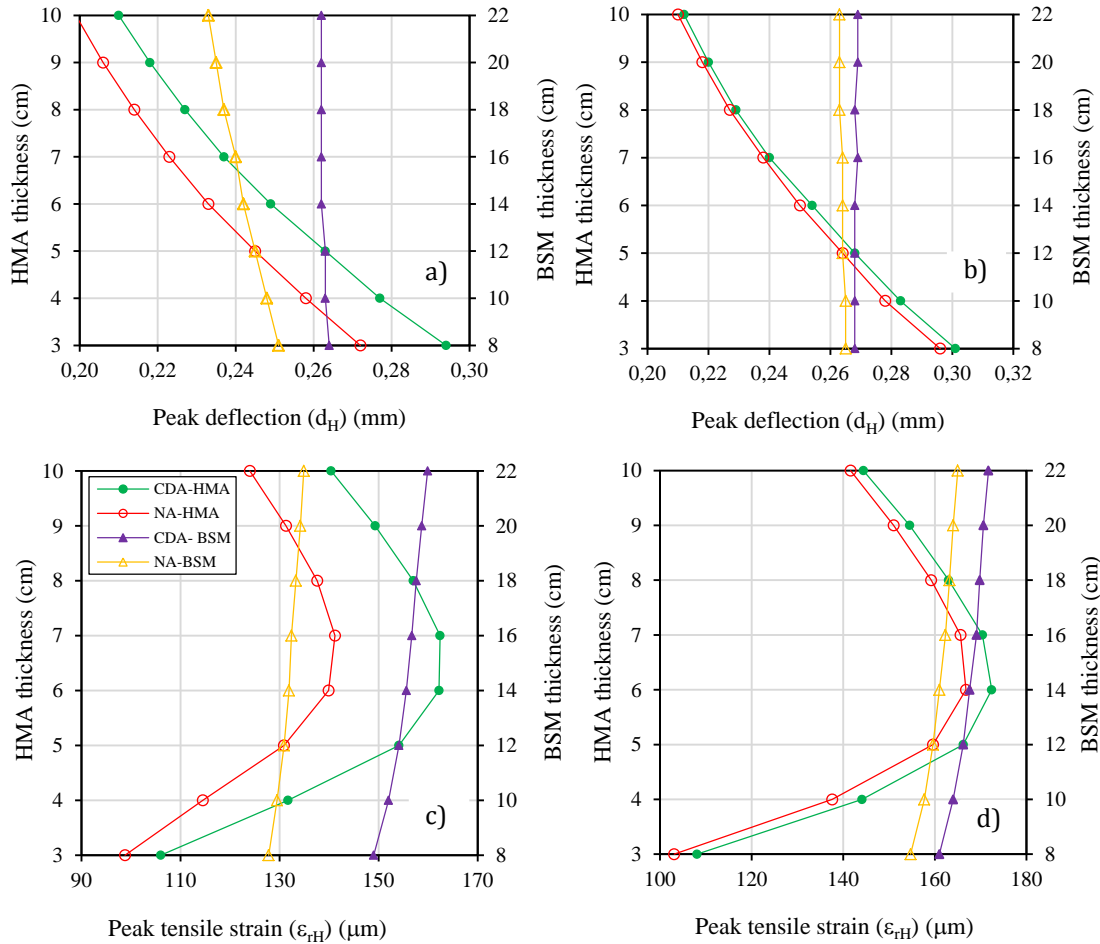
#### 392 5.3.1. HMA wearing course peak responses

##### 393 Peak deflections ( $d_H$ )

394 The variation of the HMA wearing-course peak responses when the BSM was cured is shown in Figs.  
395 12a and 12c and when uncured in Figs. 12b and 12d. As shown in Figs. 12a and 12b, the HMA  
396 wearing-course peak deflections increased with a constant 12-cm BSM base-course thickness and a  
397 decrease in the HMA wearing-course thickness from 10 cm to 3 cm. The peak deflections were higher  
398 when the BSM base course was made with CDA because of its lesser stiffness. Moreover, when the  
399 two BSM base courses were cured, the difference between the two peak deflection curves was higher  
400 (Fig. 12a). Thus, after curing, the difference between the two curves was approximately  $2 \times 10^{-2}$  mm  
401 and before curing was only approximately  $5 \times 10^{-3}$  mm. These occurrences resulted because the two  
402 uncured BSM materials had a similar  $M_r$ , while the cured BSM base courses with NA and CDA had  
403 very different values of  $M_r$  (Fig. 6).

404 However, with a constant 5-cm HMA wearing-course thickness and a decrease of the BSM base-  
405 course thickness from 22 to 8 cm, the HMA wearing-course peak deflections only increased slightly  
406 when the cured BSM base course was made with NA (Fig. 12a). When the cured BSM was made with  
407 CDA, the deflections were constant (Fig. 12a), and the peak deflections practically had constant values  
408 for different BSM base-course thicknesses when the two uncured BSM base courses were made with

409 NA and CDA (Fig. 12b). The variation of the BSM base-course thickness had practically no effect on  
 410 the HMA wearing-course peak deflections because the CCS subbase stiffness was similar or even  
 411 higher than that of the BSM base-course (Fig. 6).



412

413

414 **Fig. 12.** Peak responses in HMA wearing course: a) peak deflection, cured BSM, b) peak deflection, uncured BSM, c) peak  
 415 tensile strain, cured BSM, and d) peak tensile strain, uncured BSM.

416

417 Once more, when the BSM base courses were uncured, the peak deflections were higher with CDA. In  
 418 addition, the differences between the peak deflections were approximately  $15\text{--}29 \times 10^{-3}$  mm higher  
 419 after the BSM curing with CDA. Before the curing, the differences were only  $3\text{--}6 \times 10^{-3}$  mm.

420 Peak tensile strain ( $\epsilon_{rH}$ )

421 As shown in Figs. 12c and 12d, the HMA peak tensile strains were higher when the BSM base courses  
 422 were uncured. Moreover, before and after curing, the peak tensile strains in the HMA lower fibre were  
 423 higher when CDAs were used because the BSM base course with CDAs was less stiff and therefore  
 424 absorbed less tensile strains. Consequently, the peak tensile strains in the HMA were higher. However,

425 the curing of the two types of BSM base courses made with NAs and CDAs decreased the peak tensile  
426 strain values. This decrease occurred because a cured BSM base course is stiffer and therefore absorbs  
427 more tensile strains; consequently, the peak tensile strains in the HMA were lower. Also, the  
428 difference between the values of the peak tensile strain curves of the two BSM materials were higher  
429 after curing.

430 As shown in Figs. 12c and 12d, the peak tensile strain curves had a maximum value with a constant  
431 12-cm BSM base-course thickness and a variation of the HMA wearing-course thickness from 3 cm to  
432 10 cm. In other words, there was a critical thickness. Below the critical thickness, the tensile strain  
433 increased with a decrease in the HMA thickness, whereas above the critical thickness, the tensile strain  
434 decreased with a decrease in the HMA thickness. This performance was observed previously in  
435 flexible pavements constructed with bituminous wearing courses upon unbound granular materials  
436 [15]. The explanation is that, above the critical thickness, the wearing course provides an '*elastic*  
437 *structural layer action*', whereas below a thinner layer exhibits a '*membrane type behaviour*' [23]. In  
438 addition, after curing, the two maximum peak tensile strains were achieved for a 7-cm HMA wearing  
439 course and a 12-cm BSM base course with peak values of 141  $\mu\epsilon$  in the NA-HMA curve and 162  $\mu\epsilon$  in  
440 the CDA-HMA curve, respectively. Before curing, two maximum peak tensile strains were achieved  
441 for a 6-cm HMA wearing course and 12-cm BSM base course at 163  $\mu\epsilon$  in the NA-HMA curve and  
442 173  $\mu\epsilon$  in the CDA-HMA curve, respectively.

443 As shown in Figs. 12c and 12d, the peak tensile strains in the HMA lower fibre decreased slightly with  
444 a constant 5-cm HMA wearing course thickness and a variation of the BSM base course thickness  
445 from 22 cm to 8 cm. Again, the peak tensile strain curve differences were higher after curing. Note  
446 that the variation of the BSM base-course thickness did not have a significant effect on the HMA  
447 wearing-course peak tensile strains. Even so, there was a small decrease in the peak tensile strains  
448 with a decrease in the BSM base-course thickness.

#### 449 5.3.2. BSM base-course peak responses

450 Peak deflections ( $d_B$ )

451 Figs. 13a and 13b show the variation of the BSM base-course peak vertical deflections when the BSM

452 is cured and uncured. The effect of a decrease in the HMA wearing-course thickness is more  
453 significant than that of a decrease in the BSM base-course thickness. The curves in Figs. 13a and 13b  
454 corresponding to the BSM base-course peak deflection values were very similar to those of the HMA  
455 wearing-course peak deflection (Figs. 12a and 12b). Therefore, the former explanations of section  
456 5.31.1 are valid for Figs. 13a and 13b. The peak deflections of the BSM base courses were lower than  
457 those of the HMA wearing courses despite an approximate difference of  $4 \times 10^{-3}$  mm. Figs. 13a and  
458 13b show that the intercept values were the same as the predicted values in Table 5 (HMA thickness  
459 of 5 cm and BSM thickness of 12 cm).

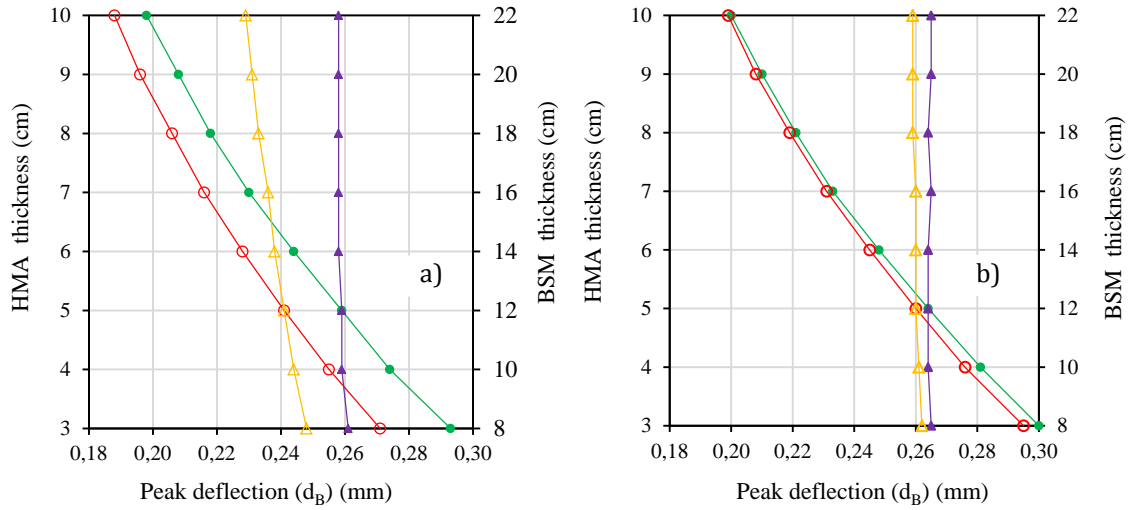
#### 460 Peak tensile strain ( $\epsilon_{rB}$ )

461 Figs. 13c and 13d represent the variation of the BSM base-course peak tensile strains. The peak tensile  
462 strains increased with a decrease in the HMA wearing course and the BSM base-course thicknesses. In  
463 this case, the peak tensile strains were higher when the BSM base courses were made with NAs and  
464 after curing. After curing, the difference between the HMA wearing-course curves was approximately  
465  $4 \mu\epsilon$ , and the BSM base-course curve differences were between 8.5 and  $4.4 \mu\epsilon$ . Before curing, the  
466 difference between the HMA wearing-course curves was approximately  $1 \mu\epsilon$ , and the BSM base-  
467 course curve differences were between 2.6 and  $1 \mu\epsilon$ .

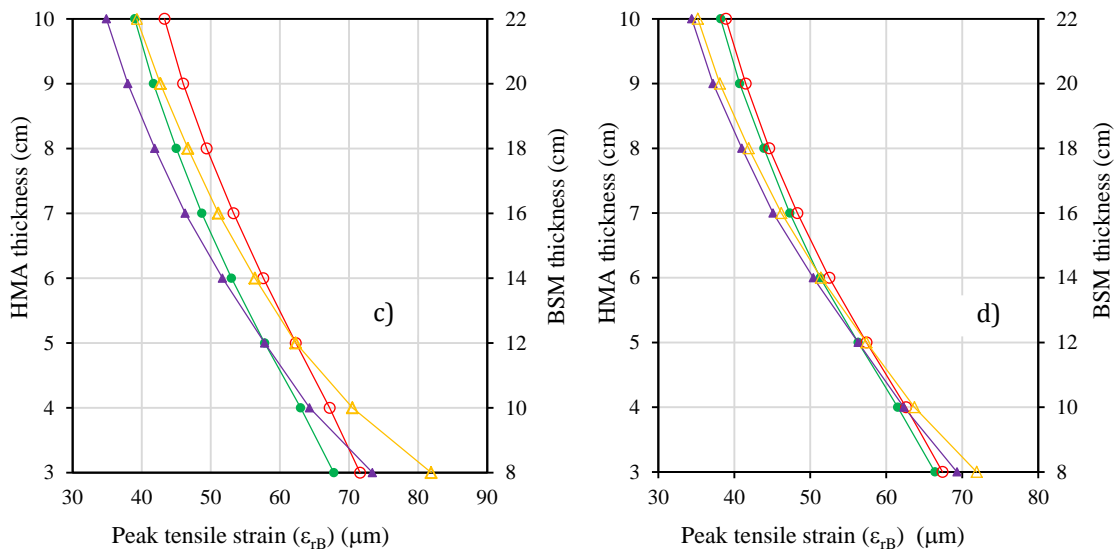
468 As previously mentioned, when the BSM base courses were cured, the stiffness was higher and the  
469 tensile strains increased. However, the peak tensile strains were lower in the BSM base courses made  
470 with CDA because their stiffnesses were lower. Comparing Figs. 13c and 13d to Figs. 12c and 12d,  
471 the HMA wearing-course peak tensile strain values were in the order of two to three times higher.  
472 Therefore, fatigue problems are not expected in the BSM base courses.

#### 473 Peak strain ratios

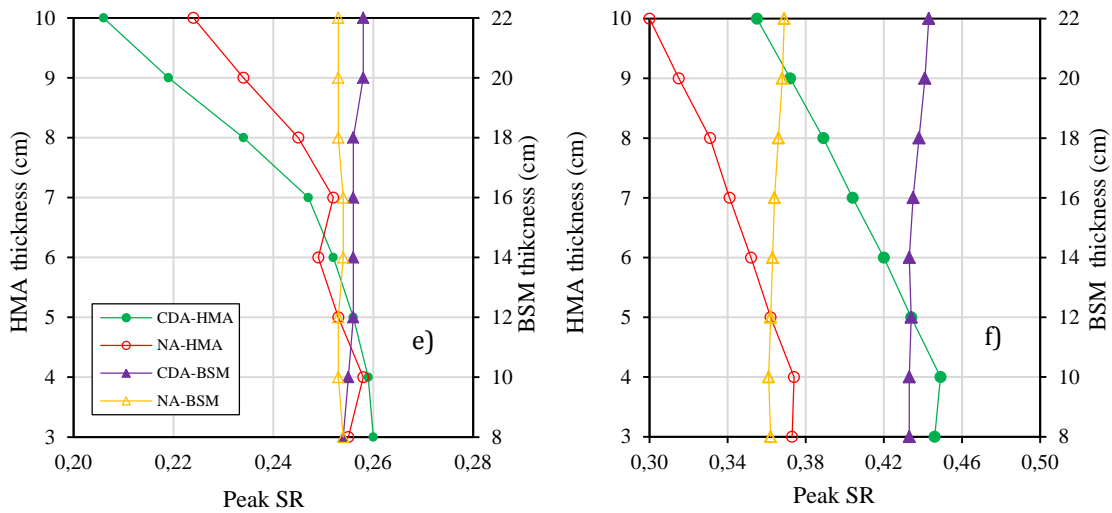
474 Figs. 13e and 13f show the variations of the peak SR values in the BSM base course. The decrease in  
475 the BSM base-course thickness had practically no influence on the peak SR values because the CSS-  
476 layer stiffness was similar or even higher than that of the BSM base-course stiffness. Nevertheless, a  
477 decrease in the HMA wearing-course thickness had an influence on the peak SR values because it  
478 increased the peak SR values.



479



480



481

482

483

484

**Fig. 13.** Peak responses of BSM base course: a) peak deflection, cured BSM, b) peak deflection, uncured BSM, c) peak tensile strain, cured BSM, d) peak tensile strain, uncured BSM, e) peak SR, cured BSM, and f) peak SR, uncured BSM.

485

As expected, before curing, the peak SR values were higher and generally higher when CDA was

486

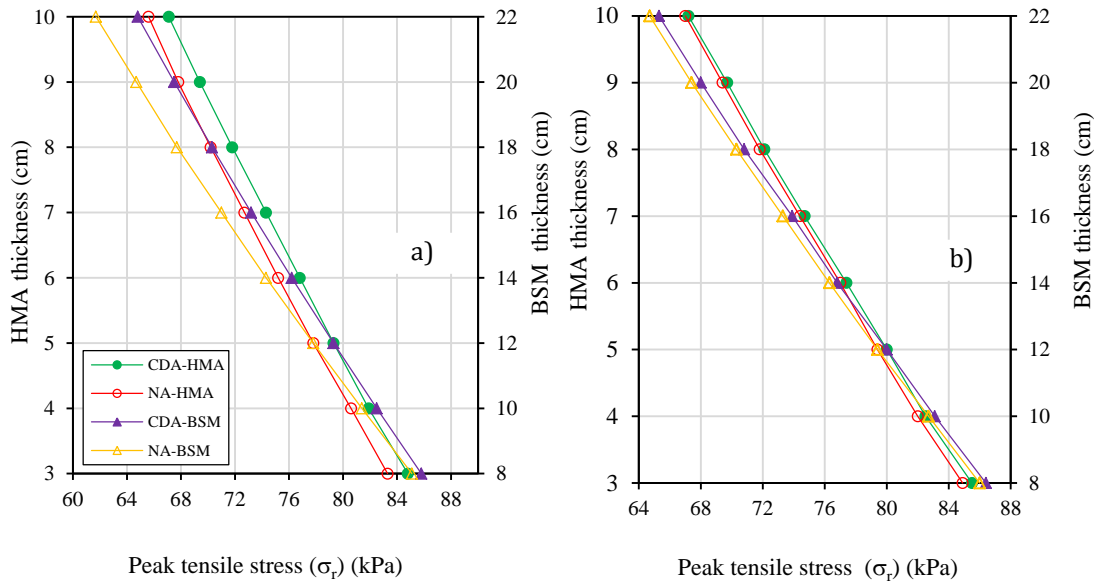
used. After curing, the difference between the BSM base-course curves was approximately  $3 \times 10^{-3}$ .



487 Before curing, the difference between the BSM base courses was approximately  $7 \times 10^{-2}$ .

### 488 5.3.3. CCS-layer peak tensile stress

489 Figs. 14a and 14b reflect the curves of the variation of the peak CSS tensile stress ( $\sigma_T$ ) values. A  
490 decrease in the HMA wearing-course thickness increased the peak CSS tensile stress values. Also, a  
491 decrease in the BSM base-course thickness increased the peak CSS tensile stress values. The peak  
492 CSS tensile stress values were slightly higher before the BSM base course was cured. When NA  
493 aggregates were used in the BSM base course, the peak CSS tensile stress values were lower than  
494 those when CDA aggregates were used. The difference in the peak CSS tensile stresses when the BSM  
495 base course was made with NA and when the BSM base course was made with CDA was  
496 approximately 2 kPa after curing (Figure 14a) and 1 kPa before curing (Figure 14b).



497

498 **Fig. 14.** Peak tensile stress in CCS layer: a) cured BSM and b) uncured BSM.

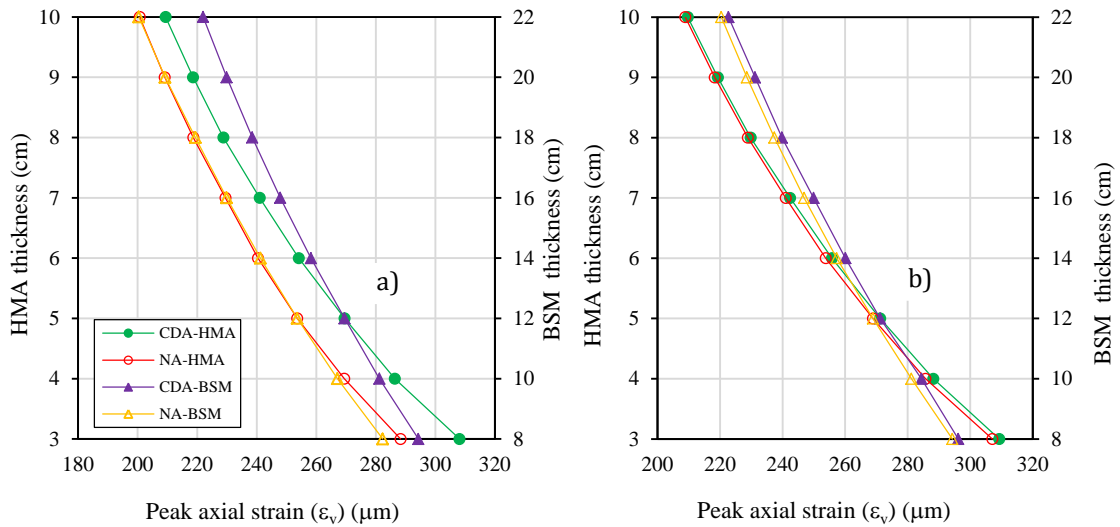
499

### 500 5.3.4. Fine-grained soil subgrade peak axial strain

501 Figs. 15a and 15b show the fine-grained soil peak axial strain ( $\epsilon_v$ ) variation curves. The peak ax  
502 ial strains always increased with a decrease in the HMA wearing-course and BSM base-course  
503 thicknesses. With CDAs, the peak axial strains were always higher, and the peak axial strains were  
504 lower after curing.

505 Finally, as presumed and explained in Section 5.3, a decrease in the BSM base-course thickness had

506 no significant effect on either the peak deflection or the SR values of the HMA and BSM layers.  
 507 Therefore, it is feasible to reduce the BSM base-course thickness. Nevertheless, a decrease could be  
 508 counterproductive as it increases the HMA and BSM peak tensile strains. In addition, it increases the  
 509 CCS-layer peak tensile stress and the fine-grained soil subgrade peak axial strain.

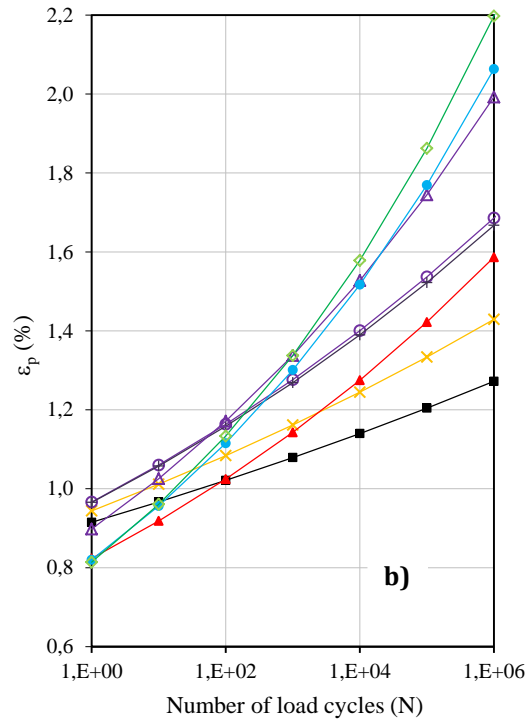
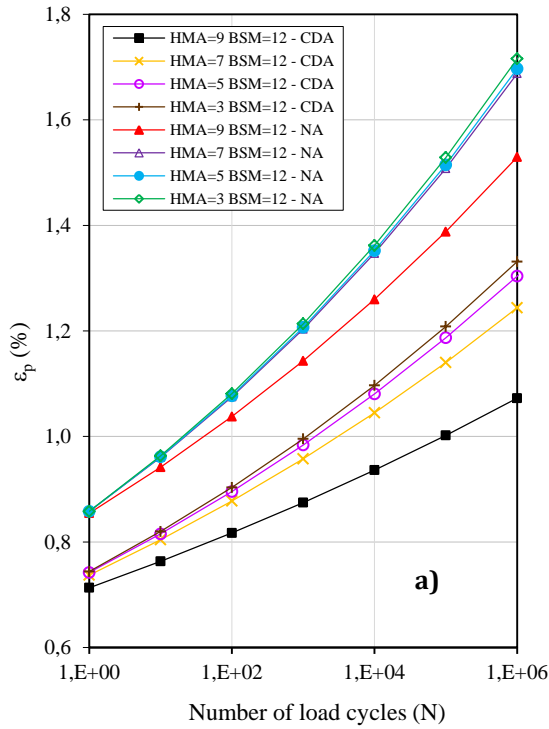


510  
 511 **Fig. 15.** Peak axial strain in fine-grained soil (S): a) cured BSM and b) uncured BSM.  
 512

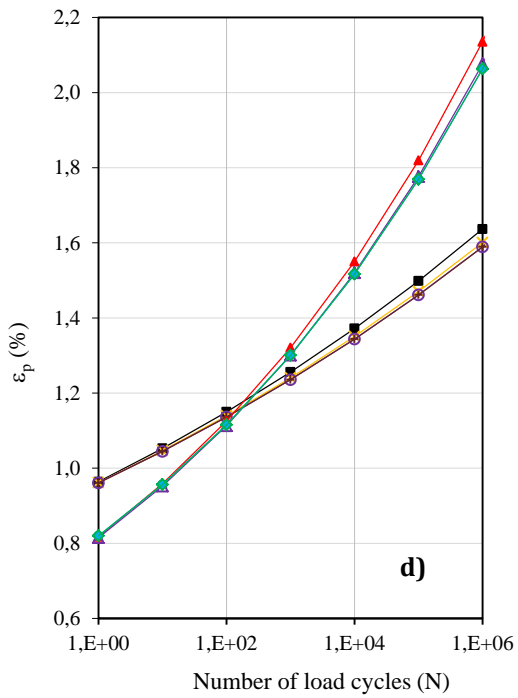
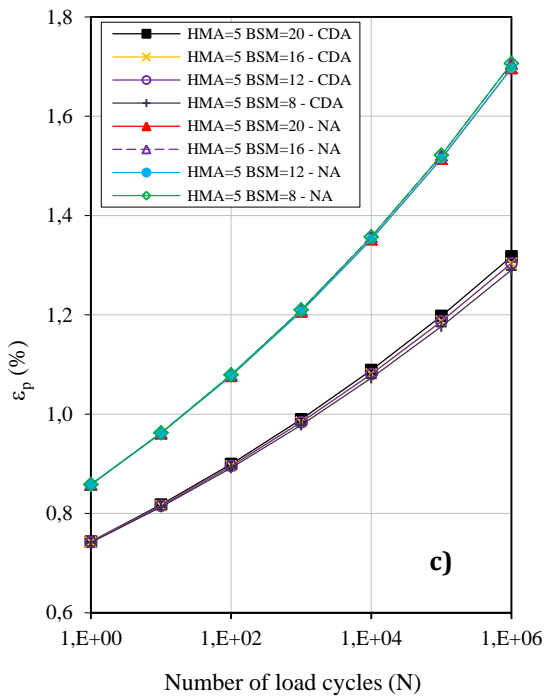
#### 513 5.4. BSM base-course axial cumulative permanent strain

514 The shear parameters of Table 3 ( $c$  and  $\phi$ ) were introduced into Equation 5 to calculate the maximum  
 515 SR. Then, the parameters of Table 4 were used in Equation 4 to estimate the axial cumulative  
 516 permanent strain ( $\epsilon_p$ ) in the BSM base courses. Fig. 16 shows the  $\epsilon_p(\%)$  versus the number of load  
 517 cycles (N), where logically  $\epsilon_p(\%)$  increases with an increase in N. Figs. 16a and 16b show eight curves  
 518 representing  $\epsilon_p(\%)$  versus N after and before curing, respectively. In each figure, four curves are BSM  
 519 base courses made with NA, and four curves are made with CDA. In both figures, the curves with NA  
 520 and CDA had a constant 12-cm BSM base-course thickness and four different HMA wearing-courses  
 521 thickness of 3, 5, 7, and 9 cm.

522 As can be seen in Fig. 16a, when the BSM bases courses were cured,  $\epsilon_p(\%)$  increased with a decrease  
 523 in the HMA wearing-course thickness. In this sense,  $\epsilon_p(\%)$  increased because the maximum SR  
 524 increased as a result of a decrease in the HMA wearing-course thickness. Moreover, in the cured BSM  
 525 base courses, the CDA  $\epsilon_p(\%)$  values were lower than those of the NA.



526



527

528 **Fig. 16.** BSM base courses  $\epsilon_p$  versus number of load cycles: a) HMA variation, cured BSM, b) HMA variation, uncured  
 529 BSM, c) BSM variation, cured BSM, and d) BSM variation, uncured BSM.  
 530

531 Therefore, when the material is cured, the BSM base courses made with CDA have higher resistance  
 532 to permanent deformation. However, as shown in Fig. 16b, in the uncured BSM base courses, after  
 533 approximately 1,000 N, the CDA  $\epsilon_p(\%)$  values were lower than those of the NA (except HMA = 9 and

534 BSM = 12 - NA). Before 1,000 N, it is unclear if the BSM base courses made with CDAs had a lower  
535  $\epsilon_p(\%)$ . In this case, the comparison between the two BSM materials must be made with a relatively  
536 low N because in a real case, the number of load cycles until the BSM base-course curing is not very  
537 high. Therefore, when the two materials (CDA or NA) are uncured, it is ill-defined which BSM base  
538 course has the higher resistance to permanent deformation.

539 Fig. 16c shows the eight curves of  $\epsilon_p(\%)$  versus N after curing, and Fig. 16d shows the eight curves of  
540  $\epsilon_p(\%)$  versus N before curing at a constant 5-cm HMA wearing-course thickness and four BSM base  
541 courses with thicknesses of 8, 12, 16, and 20 cm. Fig. 16a shows the eight curves of  $\epsilon_p(\%)$  versus N  
542 after curing, and Fig. 16b shows the eight curves of  $\epsilon_p(\%)$  versus N before curing.

543 In Fig. 16a, clearly, when the base courses were cured, the CDA curves had a lower  $\epsilon_p(\%)$  than that of  
544 the NA curves. Nevertheless, in Fig. 16b, when the BSM base courses were uncured, the CDA curves  
545 had a lower  $\epsilon_p(\%)$  than that of the NA curves only after 100 load cycles. In this case, when the  
546 material was cured, the  $\epsilon_p(\%)$  curves were similar. Therefore, the BSM base-course thickness variation  
547 had an insignificant influence on the  $\epsilon_p(\%)$  values. Moreover, before the BSM material was cured as  
548 shown in Fig. 16b, the curves were very similar. Thus, the BSM base-course thickness influence was  
549 also insignificant.

550 As a final point of this section, it is necessary to clarify why in Figure 16 the BSM base courses made  
551 with CDA had less  $\epsilon_p(\%)$  than the BSM base courses made with NA. It is believed that when the  
552 BSM with CDA was subjected to a high number of triaxial load cycles a stiffening of the mortar rich  
553 in bitumen matrix produced the increase of the resistance to the permanent strain in the BSM with  
554 CDA. Therefore, when equation 4 was fitted to the cumulative axial permanent strain curves, the  
555 prediction of  $\epsilon_p(\%)$  in the BSM with CDAs was lower (Figure 16) and therefore there will also be  
556 lower rutting.

##### 557 *5.5. BSM base-course rutting during design period*

558 As described in Section 4, the load configuration adopted was the standard 130-kN single axle with  
559 two dual tyres. Therefore, rutting was formed by single-axle loads of 130 kN with dual tyres upon the  
560 pavement section. Then, the rut depth (mm) formed in the BSM base course was estimated as the

561 product of  $\epsilon_p$  and the BSM base-course thickness in mm.

562 The pavement section was designed for a low-volume road with an  $AADT_{HT}$  of 49 heavy vehicles/day  
563 that was supported in the service lane during the project period. This heavy traffic flow was used to  
564 estimate the number of equivalent single-axle loads of 130 kN in the service lane during the design  
565 analysis period ( $N_T$ ). For this purpose, the following equation was used [25]:

$$566 \quad N_T = AADT_{HT} \cdot C \cdot A \cdot 365 \cdot \gamma_T, \quad (7)$$

567 where  $A$  is the heavy-vehicle equivalency factor of a single axle (0.70);  $\gamma_t$  is the safety coefficient  
568 related to the degree of uncertainty of measurement of heavy-load vehicles (1.15);  $C = [(1+r)^n - 1]/r$  is  
569 the traffic growth factor (24.30) with an annual growth rate,  $r$ , of 0.02; and  $n$  is the 20-year analysis  
570 period. Substituting these values into Equation 7,  $N_T = 3.4986 \times 10^5$  equivalent single-axle loads of  
571 130 kN.

572 However, it is hypothesised in Spain that the real length of time for the in-situ curing of BSM base-  
573 course mixes is six months [19]. Therefore, in Equation 7,  $C = 0.5$  years, and the number of equivalent  
574 single-axle loads of 130 kN during the curing period is  $N_{Tbc} = 7.1987 \times 10^3$ . Accordingly, the number  
575 of equivalent single-axle loads of 130 kN during the design life period after curing is  $N_{Tac} = N_T - N_{Tbc} =$   
576  $3.4986 \times 10^5 - 7.1987 \times 10^3 = 3.4266 \times 10^5$  equivalent single-axe loads of 130 kN.

577 Table 6 lists the  $\epsilon_p(\%)$  and the rutting originated in pavement sections with different HMA wearing-  
578 course and the BSM base-course thicknesses. Some of these pavement sections were the same as those  
579 analysed in Fig. 16. Each pavement section  $\epsilon_p(\%)$  was obtained using Equations 4 and 5. The  $\epsilon_p(\%)$   
580 and the rut depths produced during the design life period in the BSM base courses made with NAs and  
581 CDAs after curing were estimated using  $3.4266 \times 10^5$  loads (Table 6). Thus, for the reference 120-mm  
582 BSM base-course thickness (Fig. 4) in the cured BSM base course made with NA, the estimated rut  
583 depth was 1.93 mm, and in the BSM base course made with CDA, the estimated rut depth was 1.50  
584 mm. In addition, in Table 6 the  $\epsilon_p(\%)$  and the rut depths produced during the curing period in the BSM  
585 base courses made with NAs and CDAs were estimated using  $7.1987 \times 10^3$  loads. Thus, for the  
586 reference 120-mm BSM base course thickness, during the curing period in the BSM made with NA,

587 the estimated rut depth was 1.78 mm, and in the BSM made with CDA, the estimated rut depth was  
 588 1.60 mm. Obviously, the  $\epsilon_p(\%)$  predicted by equation 4 and the rut depth are lower during the design  
 589 life after curing due to the increase in both the resilient modulus and shear strength parameters after  
 590 the curing of the BSM base courses.

591 **Table 6.** Rutting in BSM base course

Thickness (mm)		Design life after curing ( $3.4266 \times 10^5$ load cycles)				Curing period ( $7.1987 \times 10^3$ load cycles)			
		NA		CDA		NA		CDA	
HMA	BSM	$\epsilon_p$ (%)	Rutting (mm)	$\epsilon_p$ (%)	Rutting (mm)	$\epsilon_p$ (%)	Rutting (mm)	$\epsilon_p$ (%)	Rutting (mm)
90		1.46	1.75	1.04	1.25	1.26	1.51	1.13	1.36
70	120	1.60	1.92	1.19	1.43	1.50	1.80	1.23	1.48
50		1.61	1.93	1.25	1.50	1.48	1.78	1.33	1.60
30		1.63	1.95	1.27	1.53	1.54	1.85	1.37	1.65
		200	1.61	3.22	1.26	2.52	1.51	3.03	1.35
	160	1.62	2.59	1.25	2.00	1.49	2.38	1.33	2.14
50	120	1.61	1.93	1.25	1.50	1.48	1.78	1.33	1.60
	80	1.62	1.29	1.24	0.99	1.48	1.19	1.33	1.06

592

593 **Table 7.** Total rutting during pavement design and pavement total rutting allocated to BSM base course

Thickness (mm)		Total rut depth in BSM during design life (mm)		% of 20-mm failure rut on surface assigned to BSM	BSM failure rut depth (mm)
HMA	BSM	NA	CDA		
90		3.27	2.61	53	10.60
70	120	3.72	2.91	55	11.00
50		3.71	3.10	57	11.40
30		3.80	3.18	59	11.80
		200	6.25	5.23	65
	160	4.97	4.14	61	12.20
50	120	3.71	3.10	57	11.40
	80	2.49	2.06	53	10.60

594

595 Moreover, in Table 6, in the constant 120-mm BSM base-course thickness, an increase in the HMA  
 596 wearing-course thickness produced an  $\epsilon_p(\%)$  and decreased rutting. Nevertheless, with a constant 50-  
 597 mm HMA thickness, an increase in the BMA base-course thickness produced similar  $\epsilon_p(\%)$  values, but  
 598 the rutting values increase considerably.

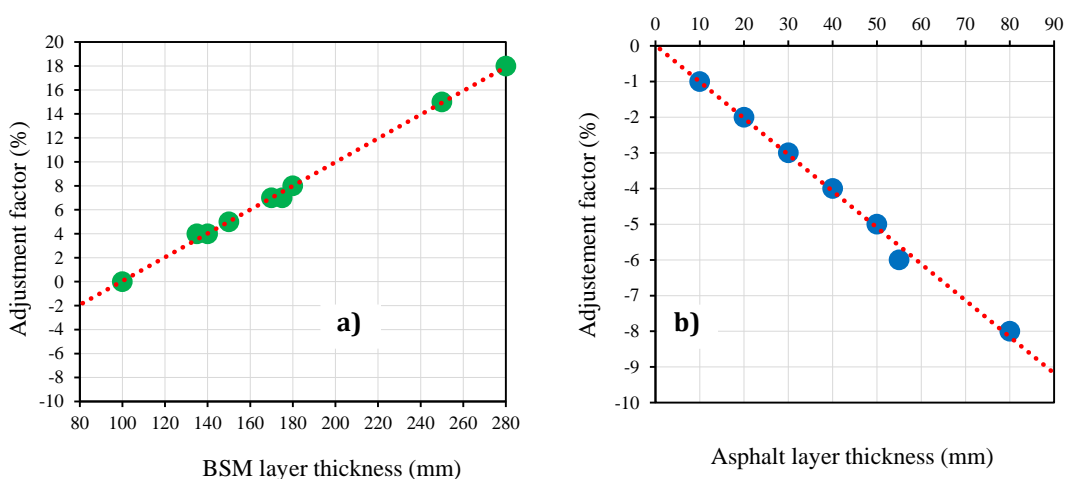
599 In Table 6, the BSM base courses made with CDAs had less rutting than the BSM base courses made  
 600 with NAs. In particular, in Table 6 when NAs were used, the rutting formed in the BSM base course  
 601 during the curing period was lower than the rutting produced after curing. On the contrary, when  
 602 CDAs were used, the rutting formed in the BSM base course during the curing period was higher than

603 that after curing. Then, the rutting of both periods was summed to obtain the total rutting during the  
604 design life period in the reference base course was 3.71 mm when NA was used and 3.10 mm when  
605 CDA was used (Table 7). Note that 48% and 52% of the total rutting was reached only during the  
606 curing periods in the BSM base courses with NA and CDA, respectively (Table 7).

607 According to Liebenberg and Visser [26], in South Africa an appropriate rutting failure criterion for  
608 low-volume roads made with BSM base courses is a 20-mm rut depth on the pavement surface. Roos  
609 [27] performed a pavement analysis in South Africa to calibrate a new transfer function. In this  
610 analysis, the rut depth was measured in full pavement section structures at different times after  
611 construction, and the percentage of rutting attributed to BSM layers was estimated based on:

- 612 1. BSM thickness: the rutting percentage assigned to a BSM increase when the BSM thickness  
613 increased (Fig. 17a),
- 614 2. Asphalt layer thickness: the rutting percentage assigned to a BSM decrease when the HMA  
615 thickness increased (Fig. 17b), and
- 616 3. Type of supporting layer under the BSM: Weak support layers result in smaller percentages of  
617 rutting attributed to the BSM, while strong support layers result in higher percentages of rutting  
618 attributed to the BSM.

619 The adjustment factors used by Roos for the asphalt and BSM layers are shown in Fig. 17.



620

621

622

**Fig. 17.** Rutting adjustments: a) BSM layer thickness and b) asphalt layer thickness [27].

623 In the case of a strong support made with cement, the adjustment factor was 10%. Roos assigned an  
624 initial 50% of rutting to a 100-mm-thick BSM base course and adjusted this percentage according to  
625 the three former criterions. The adjustment factors shown in Fig. 17 were used to calculate the  
626 percentage of the failed 20-mm rut on the surface assigned to the BSM base course and to estimate the  
627 rut-depth failure (Table 7). For example, for a pavement section with a 50-mm HMA wearing course  
628 and a 120-mm BSM base course, the percentage of the 20-mm rut assigned to the BSM base course  
629 was  $50 + 2 - 5 + 10 = 57\%$ . Then, the 20-mm failed rut depth in the BSM was  $20 \text{ mm} \times 0.57 = 11.40$   
630 mm.

631 The results in Table 7 show that the design life adopted by the ATEB [19] for the 120-mm-thick BSM  
632 base course pavement section was satisfactory because the rut depths (3.71 mm for NA and 3.10 mm  
633 for CDA) formed during the design life in the BSM base course pavement section were lower than the  
634 11.40-mm rut-depth failure. Moreover, all the pavement section combinations of HMA thickness and  
635 BSM thickness generated rut depths smaller than those of the rut depth failures. Therefore, all the  
636 studied sections were suitable from a rutting point of view.

## 637 **6. Conclusions**

638 This study investigated the mechanical behaviour of BSM base-course pavement sections of low-  
639 volume roads made with natural aggregates and construction and demolition aggregates. In this regard,  
640 the responses at critical positions of pavement layer sections and the cumulative permanent  
641 deformation (rutting) of the BSM layers were analysed. Based on the results of this research, the  
642 following conclusions can be drawn.

- 643 • BSM base courses with NAs and with CDAs present a typical nonlinear behaviour with a resilient  
644 modulus dependency on the stresses.
- 645 • The resilient modulus is higher in cured and uncured BSM base courses with NAs. Nevertheless,  
646 the shear strength before curing is higher in the BSM base courses with CDAs and after curing it  
647 is comparable with both types of aggregates. The BSM base courses made with CDAs had less  
648 cumulative axial permanent strain  $\epsilon_p$  (%) than the BSM base courses with NAs.
- 649 • The rutting produced during the curing period is approximately 50% of the total rutting produced



650 during the design life period. The total rutting produced in a BSM base course made with CDAs is  
651 lower than the total rutting produced in a BSM base course made with NAs. All the BSM base-  
652 course pavement sections were able to resist rutting during the design life period. Therefore, it is  
653 possible to use CDAs in BSM materials.

654 Finally, it must be noted that the present research is a first step in the numerical simulation  
655 performance prediction of BSM base courses made with CDAs and NA aggregates. The results were  
656 encouraging and showed that the BSM made with CDAs might have high potential use in road  
657 pavements. However, further investigation is necessary to assess aspects such as the BSM with CDAs  
658 cumulative permanent strain (rutting) resistance, the effect of different curing times on the mechanical  
659 performance and the cracking performance.

#### 660 **Acknowledgements**

661 The authors acknowledge the funding of project BIA2016-80317-R from the Spanish Ministry of  
662 Economy and Competitiveness.

#### 663 **References**

- 664 [1] Transportation Research Board, Asphalt Emulsion Technology, Transportation Research Circular  
665 Number E-C102, Washington DC (USA), 2006.
- 666 [2] I.N.A. Thanaya, S.E. Zoorob, J.P. Forth, A laboratory study on cold-mix, cold lay emulsion  
667 mixtures, Proc. Inst. Civ. Eng. Trans. 162 (2009) 47–55.  
668 <https://doi.org/10.1680/tran.2009.162.1.47>
- 669 [3] M. Limbachiya, M.S. Meddah, Y. Ouchagour, Use of recycled concrete aggregate in fly-ash  
670 concrete, Constr. Build. Mater. 27 (2012) 439–449.  
671 <https://doi.org/10.1016/j.conbuildmat.2011.07.023>
- 672 [4] M. Pepe, R.D. Toledo Filho, E.A.B. Koenders, E. Martinelli, Alternative processing procedures  
673 for recycled aggregates in structural concrete, Constr. Build. Mater. 69 (2014) 124–132.  
674 <https://doi.org/10.1016/j.conbuildmat.2014.06.084>
- 675 [5] Y.D. Wong, D.D. Sun, D. Lai, Value-added utilization of recycled concrete in hot- mix asphalt,  
676 Waste Manag. 27 (2007) 294–301. <https://doi.org/10.1016/j.wasman.2006.02.001>
- 677 [6] A.R. Pasandín, I. Pérez, Overview of bituminous mixtures made with recycled concrete  
678 aggregates, Constr. Build. Mater. 74 (2015) 151–161.  
679 <https://doi.org/10.1016/j.conbuildmat.2014.10.035>
- 680 [7] F. Lekarp, U. Isacsson, A. Dawson, State of the art. I: resilient response of unbound aggregates, J.  
681 Trans. Eng. 126 (2000) 66–75. [https://doi.org/10.1061/\(ASCE\)0733-947X\(2000\)126:1\(66\)](https://doi.org/10.1061/(ASCE)0733-947X(2000)126:1(66))
- 682 [8] K.J. Jenkins, M. Yum, Cold-recycling techniques using bitumen stabilization: Where is the  
683 technology going? In: W.Steyn, J. Kim Jenkins, M. Solaimanian (eds.), ASCE Geotechnical  
684 Special Publication 191, Road Pavement Material Characterization and Rehabilitation: Selected  
685 Papers from the 2009 GeoHunan International Conference, Hunan, China, 2009, pp. 191-200.  
686 <https://doi.org/10.1061/9780784410431>
- 687 [9] K.J. Jenkins, F. M. Long, L.J. Ebels, Foamed bitumen mixes= shear performance? Int. J. Pavement  
688 Eng. 8 (2007) 85-98. <https://doi.org/10.1080/10298430601149718>
- 689 [10] L.J. Ebels, Characterisation of Material Properties and Behaviour of Cold Bituminous Mixtures  
690 for Road Pavements. PhD thesis. Stellenbosch University, South Africa, 2008.
- 691 [11] K.J. Jenkins, D.S. Collings, Mix design of bitumen-stabilised materials–South Africa and abroad.

- 692 Road Mater. Pavement. 18 (2017) 331-349. <https://doi.org/10.1080/14680629.2016.1213511>
- 693 [12] P. Hornych, V. Gaudefroy, J.L Geffard, S. Goyer, Study of the mechanical behaviour of gravel-  
694 emulsion using triaxial tests. In: A. Loizos, M.N Partl, T. Scarpas, I.L. Al-Qadi, (eds.),  
695 Proceedings of the 7th International RILEM Symposium on Advanced Testing and  
696 Characterization of Bituminous Materials (ATCBM09), CRC Press/Balkema, Rhodes, Greece,  
697 2009, pp. 639-649.
- 698 [13] E. Santagata, G. Chiapinelli, P.P. Riviera, O. Baglieri, Triaxial testing for the short term  
699 evaluation of cold-recycled bituminous mixtures. Road Mater. Pavement. 11 (2010) 123-147.  
700 <https://doi.org/10.1080/14680629.2010.9690263>
- 701 [14] B. Gómez-Meijide, I. Pérez, Nonlinear elastic behavior of bitumen emulsion-stabilized materials  
702 with C&D waste aggregates, Constr. Build. Mater. 98 (2015) 853–863.  
703 <https://doi.org/10.1016/j.conbuildmat.2015.07.004>
- 704 [15] Y.H. Huang, Pavement Analysis and Design. Pearson Prentice Hall, second edition, Upper Saddle  
705 River, NJ USA, 2004.
- 706 [16] H. K. Shambara, A. Dulaimi, F. Ruddock, W. Atherton, The linear elastic analysis of cold mix  
707 asphalt by using finite element modeling, Conference Proceedings, The 2<sup>nd</sup> BUiD Doctoral  
708 Research Conference BDRC 2016, The British University in Dubai, 14<sup>th</sup> May, 2016.
- 709 [17] H. K. Shambara, F. Ruddock, W. Atherton, Predicting the rutting behaviour of natural fibre-  
710 reinforced cold mix asphalt using the finite element method. Constr. Build. Mater. 167 (2018)  
711 907-917. <https://doi.org/10.1016/j.conbuildmat.2018.02.072>
- 712 [18] I. Pérez, L. Medina, L., M.A. del Val, Nonlinear elasto-plastic performance prediction of materials  
713 stabilized with bitumen emulsion in rural road pavements, Adv. Eng. Softw. 91 (2016) 69-79.  
714 <https://doi.org/10.1016/j.advengsoft.2015.10.009>
- 715 [19] ATEB, Technical Association of Bituminous Emulsions, Gravel-emulsion specifications.  
716 [https://www.ateb.es/images/pdf/PLI\\_GRAVA.pdf](https://www.ateb.es/images/pdf/PLI_GRAVA.pdf). (Accessed 24 April 2018) (in Spanish).
- 717 [20] R.G. Hicks, Factors influencing the resilient response of granular materials. Doctoral Dissertation,  
718 University of California, Berkeley, USA, 1970.
- 719 [21] J. Uzan, M.W. Witczak, T. Scullion, R.L. Lytton, Development and validation of realistic  
720 pavement response models. Proceedings of the 7th International Conference on Asphalt  
721 Pavements. Nottingham, UK, 1992, pp. 334-350.
- 722 [22] NCHRP (National Cooperative Highway Research Program), Guide for Mechanistic-Empirical  
723 Design of New and Rehabilitated Pavement Structures, Part 2 Design Inputs, Final Report  
724 NCHRP 1-37A, 2004.
- 725 [23] M.R. Thompson, R.P. Elliot, Illi-Pave-Based Response Algorithms for Design of Conventional  
726 Flexible Pavements. Transp. Res. Record 1043 (1985) 50-57.
- 727 [24] Itasca Consulting Group, Inc. FLAC3D (Fast Lagrangian Analysis of Continua in 3 Dimensions),  
728 Version 3.10, User's manual, Minneapolis, MN, 2006.
- 729 [25] L. Medina, I. Pérez, R. Crespo, Structural verification of roadbed sections according to the  
730 Spanish road design manual 6.1 and 6.2 I.C. Revista de Obras Públicas 149 (3417) (2002) 35-52  
731 (in Spanish).
- 732 [26] J.J.E. Liebenberg, A.T. Visser, Towards a mechanistic structural design procedure for emulsion-  
733 treated base layers. J. S. Afr. Inst. Civ. Eng. 46 (2004) 2-8.
- 734 [27] B.C. Roos, A design function for Bitumen Stabilised Material performance based on laboratory  
735 and field evaluation. PhD thesis. Stellenbosch University, South Africa, 2018.