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Effect of attenuation mismatches in time of flight PET reconstruction

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Abstract

© 2020 Institute of Physics and Engineering in Medicine. While the pursuit of better time resolution in positron emission tomography (PET) is rapidly evolving, little work has been performed on time of flight (TOF) image quality at high time resolution in the presence of modelling inconsistencies. This works focuses on the effect of using the wrong attenuation map in the system model, causing perturbations in the reconstructed radioactivity image. Previous work has usually considered the effects to be local to the area where there is attenuation mismatch, and has shown that the quantification errors in this area tend to reduce with improved time resolution. This publication shows however that errors in the PET image at a distance from the mismatch increase with time resolution. The errors depend on the reconstruction algorithm used. We quantify the errors in the hypothetical case of perfect time resolution for maximum likelihood reconstructions. In addition, we perform reconstructions on simulated and patient data. In particular, for respiratory-gated reconstructions from a wrong attenuation map, increased errors are observed with improved time resolutions in areas close to the lungs (e.g. from 13.3% in non-TOF to up to 20.9% at 200 ps in the left ventricle).

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Effect of attenuation mismatches in time of flight PET reconstruction

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Abstract

While the pursuit of better time resolution in positron emission tomography (PET) is rapidly evolving, little work has been performed on time of flight (TOF) image quality at high time resolution in the presence of modelling inconsistencies. This works focuses on the effect of using the wrong attenuation map in the system model, causing perturbations in the reconstructed radioactivity image. Previous work has usually considered the effects to be local to the area where there is attenuation mismatch, and has shown that the quantification errors in this area tend to reduce with improved time resolution. This publication shows however that errors in the PET image at a distance from the mismatch increase with time resolution. The errors depend on the reconstruction algorithm used. We quantify the errors in the hypothetical case of perfect time resolution for maximum likelihood reconstructions. In addition, we perform reconstructions on simulated and patient data. In particular, for respiratory-gated reconstructions from a wrong attenuation map, increased errors are observed with improved time resolutions in areas close to the lungs (e.g. from 13.3% in non-TOF to up to 20.9% at 200 ps in the left ventricle).

1. Introduction

The emergence of the first time of flight (TOF) positron emission tomography (PET) scanners brought a whole new dimension to nuclear imaging, by incorporating within the PET image reconstruction the time information from a coincidence pair to estimate more accurately the localisation of the originating annihilation event. The reconstruction problem is better determined and therefore less ill-posed, accomplishing an overall better image quality and better quantification (Conti [2011](#page-14-0)). Vendors and research teams are now improving the physical characteristics of their scanners in order to get better time resolution (Lecoq [2017](#page-14-0), Cates and Levin [2018\)](#page-14-0). Current PET scanners with TOF capabilities used in clinical settings have TOF resolution between 210 ps (van Sluis *et al* [2019,](#page-15-0) Pan *et al* [2019\)](#page-14-0) and *≈* 550 ps (Bettinardi *et al* [2011](#page-14-0), Rausch *et al* [2015](#page-14-0)), but sub-100 ps time resolutions are expected in the future. A current initiative is hoping to achieve 10 ps resolution (Lecoq [2017,](#page-14-0) The 10 ps Challenge committee [2019\)](#page-15-0), which would possibly allow 'reconstruction-less' PET images, as the detected events could be placed directly in the images. However, effects such as photon attenuation and scatter will still have to be taken into account.

Attenuation is defined as the loss of coincidences resulting from the photon interactions occurring within the body of the patient. Whereas photon attenuation is the foundation of x-ray imaging, it represents a major issue in PET where the fraction of photons attenuated in a tissue is proportional to the tissue density and the distance travelled through medium. For large patients, the fraction can be up to 95% and needs to be accounted for (Mettler Jr and Guiberteau [2018\)](#page-14-0). In practice, this requires an attenuation map (also referred as μ map). All current scanners are in fact dual modality: they are either combined with a CT gantry (PET/CT) or with a MRI gantry (PET/MR). In this case, the PET attenuation maps are in most cases derived from the coupled modality. A CT acquisition can usually provide quite accurate information to derive the attenuation

factors used in the PET image reconstruction, usually via rescaling the CT attenuation values to PET 511 keV photon energy (Kinahan *et al* [1998,](#page-14-0) Alessio *et al* [2004\)](#page-14-0) (although problems exist, e.g. metal artefacts, see Blodgett *et al* [\(2011\)\)](#page-14-0). MR-derived attenuation maps are usually less robust (Lillington *et al* [2019](#page-14-0)).

Another common cause of mismatch between the estimated and actual attenuation map is motion (Bousse *et al* [2016\)](#page-14-0). Mismatched data are common, especially in case of respiratory motion: errors can be large when no motion correction/gating is used, although intra-gate motion is unavoidable.

The use of 'mismatched' attenuation maps in the PET reconstruction can induce large quantification errors in the reconstructed images, as discussed theoretically in Bai *et al* [\(2003\)](#page-14-0), Thielemans *et al* [\(2008\),](#page-15-0) Ahn *et al* [\(2014\)](#page-14-0) and clinically in Geramifar *et al* [\(2013\)](#page-14-0), Nyflot *et al* [\(2015\)](#page-14-0) and Mehranian and Zaidi [\(2015\).](#page-14-0)

In the lungs, the attenuation mismatch is not solely due to the 'displacement' caused by the compression and dilation, but also to the change of density while doing so. Cuplov *et al* [\(2018\)](#page-14-0) has shown that up to 17.1% of mass density changes can be observed during respiration. The effect of motion mismatch in the lungs was assessed in Holman *et al* [\(2016\)](#page-14-0) specifically for non-TOF reconstructions and demonstrated the importance of the density changes for quantification, additionally to the effect of mis-alignment due to motion displacement. Strategies to mitigate this exist (outside of correcting for motion), such as the use of average CT images for attenuation correction (Pan *et al* [2005\)](#page-14-0).

In non-TOF reconstruction (i.e. when the time information is not used), when far away from the edges, for an 'emission object' that is large enough (for example, in the chest), the effect is mostly local and depends on the size of the perturbation area, as well as the amount of activity in the surrounding areas. This was used to derive approximations to quantify the error in the reconstructed PET image in the area where the mismatch occurs (Thielemans *et al* [2008](#page-15-0), Bousse *et al* [2017\)](#page-14-0). In Ahn *et al* [\(2014\)](#page-14-0), the effect of mismatched attenuation maps in TOF reconstruction was also considered as local, which allowed the authors to obtain an approximation of the quantification errors. Under that assumption, if the object size is considered negligible compared to the time resolution, an estimation close to the one found in Thielemans *et al* [\(2008\)](#page-15-0) can be found, now depending on the time resolution instead of the size of the emission object. In both cases, only the local effect of a perturbation in the attenuation map on the emission image was considered in the analysis.

This work aims to demonstrate the non-local effect of attenuation mismatches in the reconstructed PET images for high time resolution scanners, with a focus on Maximum Likelihood Expectation Maximisation (MLEM) and Ordered Subset Expectation Maximisation (OSEM) reconstructions. Particular attention will be given to non-local errors in quantification, i.e. in regions where there is no attenuation mismatch.

The paper will first briefly introduce mathematically the reconstruction problem in PET, including a demonstration of the non-local effect and its quantification error for perfect time resolution. Then, it will show the spatial extent of a localised attenuation mismatch in the reconstructed images for different time resolutions. Finally simulations and the reconstruction of patient data will demonstrate the quantification error that can arise from the use of mismatched data. The convergence rates will also be assessed in both cases.

2. Theory

2.1. PET imaging system

The measured data take the form of a random vector $g\in\mathbb{N}^{n_{\rm b}},$ where $[g]_i$ is the number of counts at bin $i \in [1, n_b]$ and n_b is the number of detection bins. n_b depends on the PET system, i.e. $n_b = n_d$ for non-TOF PET and $n_b = n_d n_t$ for TOF PET, n_d and n_t denoting the number of detection bins for non-TOF reconstruction and the number of temporal bins, respectively. The imaging system is usually modelled as

$$
p = M\lambda + n \tag{1}
$$

where $\pmb{p}=\mathbb{E}[\pmb{g}],\pmb{\lambda}\in\mathbb{R}^{n_\text{v}}_+$ is the unknown emission image, $\pmb{M}\in\mathbb{R}^{n_\text{b}\times n_\text{b}}$ is the imaging system matrix, \pmb{n} is the background term (comprising randoms and scatter), and n_v is the number of voxels.

Each entry $[M]_{i,j} = M_{i,j}$ represents the probability that a pair of unscattered photons emitted in a voxel *j* is detected at the detection bin *i*, and incorporates the attenuation. In principle, detector blurring should be modelled after attenuation; however, for simplicity, we will consider the factorisation of *M* as Leahy and Qi [\(2000\)](#page-14-0)

$$
M = a(\mu)H, \tag{2}
$$

where $a(\mu)$ is a $n_b \times n_b$ diagonal matrix containing the attenuation factors corresponding to μ and *H* is a system matrix that incorporates a geometrical mapping between the source and the data—each entry $[H]_{i,j} = H_{i,j}$ represents the probability that an emission from voxel *j* is detected by the detection bin *i* in the absence of attenuation.

The background term *n* includes scatter, which in practice can be estimated from the attenuation map (Watson *et al* [1996,](#page-15-0) Ollinger [1996\)](#page-14-0). In the remainder of this section, we will assume that $n = 0$, so that ([1\)](#page-4-0) becomes

$$
p = a(\mu) H\lambda. \tag{3}
$$

This can be achieved, for example, by subtracting *n* from *p* and zeroing the negative values.

2.2. Spatial extent of activity errors due to local attenuation mismatch

We assume the true activity and attenuation images are respectively $\bm{\lambda}^\star\in\mathbb{R}^{n_\text{v}}_+$ and $\bm{\mu}^\star\in\mathbb{R}^{n_\text{v}}_+$. Furthermore, we assume that *H* is full rank with $n_b \ge n_v$ such that the mapping $H: x \mapsto Hx$ is injective. The transmission system matrix—used to generate the attenuation coefficients—is the discretised line integral operator $R \in \mathbb{R}^{n_{\text{d}} \times n_{\text{v}}}.$

The attenuation coefficient diagonal matrix $a(\mu)$ is of size $n_d n_t \times n_d n_t$ (in non-TOF PET, $n_t = 1$) and for each bin detector pair $d \in [1, n_d]$ and time bin $t \in [1, n_t]$, the diagonal element at the detection bin $[id = AB]$ $i = (d-1) \times n_t + ti = (t-1)n_t + d$ is

$$
[\boldsymbol{a}(\boldsymbol{\mu})]_{i,i} = \exp(-[\boldsymbol{R}\boldsymbol{\mu}]_d),
$$

that is to say, in TOF PET, the attenuation coefficients are independent of the time bin.

Let p^\star be an idealised noiseless measurement of the true activity λ^\star with attenuation $\mu^\star\in\R^{\eta_v},$ i.e.

$$
p^* = a(\mu^*) H \lambda^* \,. \tag{4}
$$

In absence of noise, the PET image reconstruction problem becomes

find
$$
\lambda
$$
 such that $p^* = a(\mu^*) H \lambda$ (5)

and has a unique solution $\lambda = \lambda^*$.

Now assume that the attenuation map $\tilde{\mu}$ used for reconstruction is a perturbed version of μ^* , i.e. $\widetilde{\mu} = \mu^* + \eta$ where η

is a small perturbation supported on a small region far from the edges. The reconstruction problem (5) is equivalent to solving

$$
a(\widetilde{\mu})H\lambda = a(\mu^*)H\lambda^*
$$

$$
\Leftrightarrow H\lambda = a(-\eta)H\lambda^*
$$

Non-TOF PET:

Along the lines of Thielemans *et al* [\(2008\)](#page-15-0) and Bousse *et al* [\(2017\),](#page-14-0) using a Taylor expansion around $R\mu^*$, the problem is approximated in non-TOF PET as:

$$
H(\lambda - \lambda^*) \approx \text{diag}[R\eta] H \lambda^* \tag{6}
$$

where diag[*·*] is the operator that generates a diagonal matrix from a vector. In non-TOF, the PET system matrix *H* and transmission matrix *R* are equal. Furthermore, *Rη* is sparse and its non-zero entries correspond to the lines of responses *i* intersecting the support of η . Assuming that $H\lambda^*$ is approximately constant where $R\eta$ is non-zero (this is the case, for example, when the perturbation is located far from the body contour), we can further approximate (6) as

$$
R(\lambda - \lambda^*) \approx \rho R \eta \tag{7}
$$

where ρ is the mean projected activity along the lines of response intersecting the support of η . Approximation (7) shows that when μ and μ^* differ from a local perturbation η , then, by injectivity of **R**, the solution to the approximated reconstruction problem is $\hat{\lambda} = \lambda^{\star} + \rho \eta$, which suggests that the error in the reconstructed activity remains localised on the mismatch.

TOF PET:

Equation([6\)](#page-5-0) can be extended to TOF PET, i.e. for all line of response *i* intersecting the support of *η* and for all time bin *t*,

$$
[\mathbf{H}(\boldsymbol{\lambda} - \boldsymbol{\lambda}^*)]_i \approx [\mathbf{R}\boldsymbol{\eta}]_d [\mathbf{H}\boldsymbol{\lambda}^*]_i. \tag{8}
$$

Approximation (8) implies that for all lines of response *i* intersecting the mismatch area, the error between the reconstructed activity $\hat{\lambda}$ and λ^* propagates to each time bin *t* by a factor proportional to $[R\eta]_d$, which means the error can no longer be considered local.

The previous equation (8) implies that in most cases the system to solve is made of inconsistent equations. For this reason, the solution depends on the cost function used for solving such reconstruction problem.

2.3. Maximum-likelihood expectation maximisation in perfect time resolution

In this section we deepen the analysis from section [2.2](#page-5-0) by investigating the effect of the attenuation mismatch from the perspective of MLEM reconstruction. We will consider the highly idealised case of perfect spatial resolution here.

We denote for $(i, j) \in [1, n_b] \times [1, n_v]$ (here *i* is a TOF bin and $n_b = n_d n_t$):

• $\widehat{\lambda} = \left[\widehat{\lambda}_j \right]$ the activity image reconstructed with the true attenuation map μ^* , i.e. using $M^* = \left[M^*_{i,j} \right] =$ $a(\mu^{\star})H$. *⋆*

 \bullet $\widetilde{\bm{\lambda}} = \left[\widetilde{\lambda}_{j}\right]$ the activity image reconstructed with a wrong attenuation map $\widetilde{\bm{\mu}}$, where $\widetilde{\bm{M}} = \left[\widetilde{M}_{i,j}\right] = \bm{a}(\widetilde{\bm{\mu}})\bm{H}$.

We also define the sets

$$
\mathcal{S}_j = \{i \in \llbracket 1, n_{\rm b} \rrbracket \, | \, H_{i,j} \neq 0 \, \} \, .
$$

In a hypothetical case of an activity image reconstructed with perfect time resolution as well as perfect spatial resolution, the S_i are disjoint, so that

$$
\forall i \in [\![1, n_b]\!], \exists ! j \in [\![1, n_v]\!], i \in \mathcal{S}_j. \tag{9}
$$

In other words, $[M]_{i,j}$ is non-zero if and only if $i \in S_j$. Given a system matrix M , which can either be M^{\star} or \widetilde{M} , and the measurement data $\boldsymbol{p} = \{p_i\}_{i \in [\![1,n_b]\!]}$, the MLEM algorithm $(k+1)$ -th iteration at a voxel *j* is

$$
\lambda_j^{(k+1)} = \frac{\lambda_j^{(k)}}{M_j} \sum_{i=1}^{n_b} M_{i,j} \frac{p_i}{\sum_{l=1}^{n_v} M_{i,l} \lambda_l^{(k)}}
$$
(10)

where $M_j = \sum_{i=1}^{n_{\rm b}} M_{i,j}$ and $\lambda_j^{(k)}$ *j* is the value of the activity image at a voxel *j* and iteration *k* (Dempster *et al* [1977](#page-14-0), Shepp and Vardi [1982](#page-15-0), Lange and Carson [1984\)](#page-14-0).

In TOF PET, assuming the temporal resolution is perfect, condition (9) holds and therefore $\sum_{l=1}^{n_\mathrm{v}} M_{i,l} \lambda_l^{(k)} = M_{i,j} \lambda_j^{(k)}$ $j^{(k)}$. Equation (10) simplifies to

$$
\lambda_j^{(k+1)} = \frac{\lambda_j^{(k)}}{M_j} \sum_{i \in S_j} M_{i,j} \frac{p_i}{M_{i,j} \lambda_j^{(k)}} = \frac{\sum_{i \in S_j} p_i}{\sum_{i \in S_j} M_{i,j}}
$$
(11)

and convergence is achieved after one iteration. Substituting M with M^{\star} and \widetilde{M} successively in (11) leads to

$$
\frac{\widetilde{\lambda}_j}{\widehat{\lambda}_j} = \frac{\sum_{i \in S_j} M_{i,j}^*}{\sum_{i \in S_j} \widetilde{M}_{i,j}} = \frac{\sum_i M_{i,j}^*}{\sum_i \widetilde{M}_{i,j}}
$$
\n(12)

where the second equation follows from the fact that the S_i are disjoint. Therefore, *the ratio between the 'wrong' and 'true' reconstructed images is equal to the ratio of the 'true' and 'wrong' sensitivity images*. The quantification of the non-local effect due to a local error in the attenuation map, from equation (8) can therefore be quantified easily for MLEM/OSEM in the case of perfect time resolution by the relative error

$$
\frac{\widetilde{\lambda}_j - \widehat{\lambda}_j}{\widehat{\lambda}_j} = \frac{\sum_i M^*_{i,j}}{\sum_i \widetilde{M}_{i,j}} - 1
$$
\n(13)

The maximum-likelihood (ML) solution being unique in this case, equations [\(12\)](#page-6-0) and [\(13\)](#page-6-0) are valid for other ML algorithms. It is worth noticing that for small attenuation mismatches and using the same first-orderTaylor expansion around μ^* , ([13](#page-6-0)) resembles an image space version of [\(8](#page-6-0)). Similar results for other reconstruction algorithms are shown in the appendix.

3. Experiments and results

In this section we will study the quantification errors in TOF reconstruction due to attenuation mismatch for MLEM/OSEM.

3.1. Summary of simulated and patient data

We use four different datasets, either simulated for or acquired on a GE Discovery 690 PET/CT scanner (Bettinardi *et al* [2011\)](#page-14-0). The PET reconstructions use two different attenuation maps: the true attenuation map μ^{\star} and a wrong attenuation map $\widetilde{\mu}$.

3.1.1. Simulations

The simulated datasets are the following:

Simulation 1:

A 28.8-cm diameter uniform cylinder (linear attenuation: 0.091 6 cm*−*¹) is placed at the centre of the FOV. The wrong attenuation map $\tilde{\mu}$ is known accurately in the reconstruction except for one small cylinder $(diameter = 6 mm)$ at the centre of the FOV, where the attenuation is overestimated by 15%. This simulation is aimed at studying the impact of a very small attenuation mismatch on the reconstructed activity image. The phantom volumes are shown in figure 1.

Simulation 2:

An XCAT PET/CT simulation of an FDG oncological pulmonary acquisition at end-inspiration (tumour of 1 cm³ situated in the lower right lung). Two incorrect input $\widetilde{\mu}$ maps are assessed:

- *Lung density changes only*: The incorrect $\tilde{\mu}$ map (denoted $\tilde{\mu}_1$) is aligned with the structures in the PET data, however the density in the lung is not known accurately (overestimation of 15%). Note that the lung tumour density does not change, as the structure is considered rigid. Such simulation is relevant in motioncompensated image reconstruction (MCIR) or gated reconstruction, when a static μ map is warped to another respiratory gate (for which intra-motion is negligible), but the changes in density are not considered.
- *Lung density changes* + *misalignment*: The incorrect $\tilde{\mu}$ map (denoted $\tilde{\mu}_2$) corresponds to the end-expiration state, therefore both structure alignment and lung density are wrong. The input simulation images are given in figure [2](#page-8-0).

Data generation:

The simulations were performed using STIR with TOF (Efthimiou *et al* [2018\)](#page-14-0) in the following order:

(a) Forward projection of the true activity image λ^* to obtain the non-attenuated projection data.

Table 1. Time resolution FWHM simulated and the corresponding number of MLEM iterations used.

- (b) Calculation of the attenuation coefficient sinogram $a(\mu^*)$ from the true attenuation map μ^* and multiplication by the projection data.
- (c) Reconstruction of the attenuated projection data using either the true attenuation map μ^* or the incorrect attenuation map $\tilde{\mu}$.

To assess the effect of varying time resolution in the TOF reconstruction, the overall scanner geometry of the GE PET/CT Discovery 690 was used, but the TOF characteristics were altered:

- The maximal number of TOF bins extended to 175 (of width equal 28 ps) instead of the original 55 bins (of width *≈* 89 ps).
- The time resolution was modified to test a range of time resolutions, from 70 ps to 550 ps.

Image reconstruction:

For the simulations, the projection data were reconstructed with MLEM (image size: 256 *×* 256 *×* 47, voxel size: 2.130 6 \times 2.130 6 \times 3.27 mm³, no post-filter applied), using a sufficient number of iterations so that the mean difference between the last two iterations was less than 0.1% overall, when the correct attenuation map was used in the reconstruction. The numbers of iterations for the TOF reconstructions, depending therefore on the time resolution, are given in table 1. 1600 iterations were used in non-TOF reconstructions. For computational reasons, TOF 'mashing' was used in this work, therefore combining TOF bins together with only small loss reported for quantification (Efthimiou *et al* [2018](#page-14-0)).

3.1.2. Patient data

A 76-year-old male patient (clinical trial ID: NCT02 885 961) underwent a static FDG acquisition (injected activity: 170.8 MBq), on a GE Discovery 690 at the Institute of Nuclear Medicine, University College London Hospital (London, UK). Two different CT acquisitions were available: one at end-expiration (CTAC acquisition, multislice helical acquisition at shallow breathing, slice thickness: 3.75 mm, pitch: 1.375, voltage: 120 kVp, current: 40 mA, revolution time: 0.8 s) and one at end-inspiration (HRCT, multislice helical acquisition at breathhold, slice thickness: 1.25 mm, pitch: 0.516, voltage: 120 kVp, current: 149 mA, revolution time: 0.6 s). In addition, the listmode data were also (amplitude-) gated into 4 respiratory bins (no cardiac gating) based on the respiratory trace from a Varian RPM system. The end-expiration gated PET data were reconstructed using two μ maps μ^* and $\tilde{\mu}$, computed from the end-expiration and the end-inspiration CT images, respectively. The alignment between the end-expiration PET data and CT image was visually assessed using non-attenuation-corrected (AC) TOF gated images. The patient data were reconstructed using GE proprietary software in MATLAB (Matlab 2016b), with OSEM using 8 subsets with 200 iterations for non-TOF data and 100 iterations for TOF data. A 2D Gaussian postfilter of FWHM 6 mm and a 1-4-1 weighted z-axis postfilter were applied to the final images (image size: 256 *×* 256 *×* 83, voxel size: $2.7344 \times 2.7344 \times 3.27$ mm³).

3.1.3. Measures

At a given time resolution, we denote $\hat{\lambda}$ and $\hat{\lambda}$ the reconstructed images at the final reconstruction iteration, using the true attenuation map μ^* and the incorrect attenuation map $\tilde{\mu}$, respectively. In the following, we will use the relative errors in absolute value defined in a region of interest (ROI) *R* as

$$
|RE|_{\mathcal{R}} = \frac{\left| \underset{\mathcal{R}}{\operatorname{mean}(\tilde{\lambda})} - \underset{\mathcal{R}}{\operatorname{mean}(\hat{\lambda})} \right|}{\operatorname{mean}(\hat{\lambda})}
$$

where mean (\cdot) designates the mean value in \mathcal{R} .

We also define the relative difference image RD_{λ} (in absolute values) such that

$$
\left[\mathbf{R}\mathbf{D}_{\lambda}\right]_{j\in\left[\!\left[1,n_{\mathrm{v}}\right]\!\right]}=\frac{\left|\widetilde{\lambda}_{j}-\widehat{\lambda}_{j}\right|}{\widehat{\lambda}_{j}}
$$

3.2. Results

3.2.1. Simulation 1

We consider five rectangular ROIs $(4 \times 4 \times 45)$ voxels, the first and last slices are excluded). The first one is placed at the centre of the field of view (FOV), therefore at the centre of the perturbation area. The four other ROIs are off-centre (distance between the centre of the FOV and the ROIs: 12.8 mm, 21.3 mm, 29.8 mm and 55.4 mm respectively). In order to minimise problems related to discretisation, off-centre ROIs measures average values in reconstructed images rotated about the centre of the cylinder (60 rotation angles considered).

We computed the relative error within the perturbation area and in the four off-centre ROIs. The plots showing the relative errors with respect to the time resolution are shown in figure [4,](#page-9-0) where the relative error at perfect time resolution was predicted by equation([13](#page-6-0)).

The first subplot is consistent with previous results on TOF, where improved time resolution decreases errors locally in the activity images. The second subplot confirms that the errors propagate globally in the image, in agreement with equation [\(8\)](#page-6-0).

non-TOF.

Table 2. Simulation 2 (*Lung density changes* ⁺ *misalignment*) – Relative errors *[|]*RE*|^R* for different time resolutions and for non-TOF in different ROIs $\mathcal R$: ascending aorta (AA), descending aorta (DA), left ventricle (LV), right ventricle (RV) and liver.

ROI	AA	DA	ΙV	RV	
Perfect TOF	12.8%	3.3%	22.9%	25.5%	
70 ps	12%	1.0%	23.0%	26.6%	
200 ps	8.8%	1.7%	20.9%	27.9%	
550 ps	6.5%	4.5%	14.2%	21.8%	
non-TOF	8.3%	5.4%	13.3%	16.6%	

Figure 8. Patient data—Relative errors for TOF reconstruction (550 ps) in (a) coronal and (b) sagittal views and for non-TOF reconstruction in (c) coronal and (d) sagittal views.

3.3. Simulation 2: lung XCAT simulation

3.3.1. Lung density changes only

In figure [5](#page-10-0), the relative errors are plotted in different $3 \times 3 \times 3$ voxel ROIs (left and right lungs, descending aorta and lung tumour), relative to time resolution. Similarly as for Simulation 1, the relative errors within the lungs (where the attenuation mismatch is located) decrease with improved time resolution. However, the errors increase in the lung tumour and the descending aorta. The same behaviour was observed for the right and left ventricles, as well as ascending aorta (results not shown). The results show the propagation of the errors outside of the lungs (where the attenuation mismatches lie), in neighbouring regions, as predicted by Formula [\(13\)](#page-6-0).

The relative difference images corresponding to different time resolutions are shown in figure [6](#page-10-0).

3.3.2. Lung density changes + *misalignment*

In figure 7, the relative difference images in absolute values are shown.

Additionally, the relative errors RE_R were quantified in different ROIs R : ascending aorta (AA), descending aorta (DA), left ventricle (LV), right ventricle (RV) and liver. The relative differences *|*RD*|* between $\hat{\lambda}$ and $\hat{\lambda}$ are given in table 2.

3.4. Patient data

The two input CT images and the relative errors images are shown in figures [3](#page-9-0) and 8, respectively. Additionally, spherical ROIs were drawn on the end-expiration CT for measurements using ITK-SNAP (Yushkevich et al [2006](#page-15-0)): Ascending Aorta (AA, 1.76 cm³), upper Descending Aorta (U-DA,

Table 3. Patient data—Relative errors $|RE|_{\mathcal{R}}$ in TOF and non-TOF in different ROIs \mathcal{R} : ascending aorta (AA), upper descending aorta (U-DA), upper descending aorta (L-DA), left ventricle (LV), right ventricle (RV) and liver.

ROI	AA	U-DA	L-DA	LV	RV	Liver
TOF	5.1%	2.1%	14.0%	8.2%	5.7%	8.6%
non-TOF	2.7%	0.5%	13.5%	2.8%	3.6%	5.1%

1.76 cm³), lower Descending Aorta (L-DA, 1.76 cm³), Left Ventricle (LV, 1.76 cm³), Right Ventricle (RV, 1.54 cm^3) and Liver (7.33 cm³).

The relative differences $|RE|_{\mathcal{R}}$ in different ROIs $\mathcal R$ between $\hat \lambda$ and $\hat \lambda$ are shown in table 3.

4. Discussion

System model inconsistencies in PET reconstruction are a cause of quantification errors. When improving the TOF resolution, local errors in the attenuation map will lead to non-local quantitative errors in the reconstructed activity image. Moreover, the errors in areas away from the attenuation mismatch increase with improved timing resolution. The errors depend on the optimisation chosen to reconstruct the data. Here we focused on MLEM/OSEM reconstructions, which are the most widely used algorithms in the clinics. We first derived a simple formula for the relative error for perfect time resolution. This formula was confirmed with simulations, by observing the trend for improved time resolution.

Results were first shown for a simple cylindrical simulation, to demonstrate the non-local effect with highly symmetrical structures. They were in agreement with Ahn *et al* [\(2014\)](#page-14-0) at the centre of the mismatch, however we observed errors in areas outside of the mismatch, as predicted by the theory presented in this paper. The region in closest proximity to the mismatch (12.8 mm off-centre) presented a mixed effect: the corresponding relative error curve (figure [4\)](#page-9-0) is not monotonic and resembles the curve for the ROI in the region of the mismatch at low time resolution. The study was then extended to XCAT simulations with activity at end-inspiration, first using an aligned μ map with incorrect values in the lung, and then a mismatched end-expiration *µ* map. As expected, the quantitative errors decreased in the lungs but increased in the neighbouring regions, such as the ventricles and the aorta. Finally patient PET data were gated (end-expiration) and reconstructed using two different μ maps: one close to the PET gate and the second one corresponding to end-inhalation. Both TOF (FWHM: 550 ps) and non-TOF were employed. The differences between the two sets of images were similar to those observed with the second XCAT simulation. While differences in the lung reduced with increased TOF timing resolution, they increased in most neighbouring ROIs, such as the ascending aorta (from 2.7% to 5.1%) or the left ventricles (from 2.8% to 8.2%), similarly to the 12.8 mm off-centre ROI of the cylindrical simulation.

The findings have clinical implications for PET in the thorax. The observed effects are likely to be most important for TOF PET/MR, where existing methods to compute the attenuation map from MR acquisitions are not quantitatively accurate in the thorax, although progress has been made to overcome this issue (Lillington *et al* [2019](#page-14-0)). It is likely that the problem would be largest in the case where the bones are not inserted in the MR-derived attenuation map used for the reconstruction. Effects due to errors in the attenuation map are also important for PET/CT as perfect alignment between PET and CT is usually impossible (especially in the thorax).

These results also show a possible impact on kinetic modelling. As previously stated, larger errors will be expected in regions commonly used to estimate image-derived input functions, such as the aorta or the left ventricle. From the values in tables [2](#page-11-0) and 3, we suggest to use an input function derived from either the ascending aorta or an upper region of the descending aorta. A further complication is that errors due to attenuation mismatch depend on the surrounding activity distribution. This was reported in non-TOF PET (Thielemans *et al* [2008,](#page-15-0) Holman *et al* [2016,](#page-14-0) Merida *et al* [2017\)](#page-14-0) but is also the case with TOF, although this dependency disappears at perfect TOF resolution (see equation (12)). As the activity distribution is globally changing over the duration of the dynamic PET acquisitions, we expect time-dependent errors in presence of an attenuation mismatch on both image-derived input function and reconstructed activity, which would affect estimated kinetic parameters. Kotasidis *et al* [\(2016\)](#page-14-0) already discussed such errors and found that although the biases were reduced with improved time resolution, they could not completely be resolved.

Furthermore, as shown in figure [5](#page-10-0) the observed effect has consequences for MCIR, where it would therefore be necessary to model the density changes in the lung Cuplov *et al* [\(2018\),](#page-14-0) Emond *et al* [\(2019\)](#page-14-0) in order to avoid intra-gate inconsistencies.

A possible way to correct the attenuation maps is by using an algorithm such as Maximum-Likelihood reconstruction of Activity and Attenuation (MLAA) Nuyts *et al* [\(1999\).](#page-14-0) When TOF information is available, it is possible to determine, from the prompts only, the corrected attenuation sinogram up to a

constant Defrise *et al* [\(2012\).](#page-14-0) It becomes therefore possible to compute the entire attenuation sinogram when at least a part of it is known precisely (e.g. when a suitable region of the *µ* map is known). Rezaei *et al* [\(2019\)](#page-15-0) has recently demonstrated clinical feasibility of MLAA, when robust calibration and corrections are used. The results in this paper imply that MLAA will become essential at higher TOF timing resolution. The effect observed in this paper also provides an alternative explanation for the fact that MLAA becomes more stable with improved TOF resolution: the non-locality of the error can be a reflection of the inconsistencies between the data and the system model if the wrong attenuation map is used (equation([8\)](#page-6-0)).

This publication only focused on system model inconsistency linked to the attenuation map. The study could be extended to inconsistencies due to incorrect background term within the reconstruction (i.e. including estimation of randoms and scatters). An accurate estimation of the scatter sinogram was indeed shown to be of great importance to obtain quantitative measures in TOF-MLAA Rezaei *et al* [\(2019\)](#page-15-0).

5. Conclusion

We have shown that the effect of using an incorrect attenuation map in the reconstruction on the activity image cannot be considered local in TOF reconstructions. The relative errors can be easily quantified for perfect time resolution, which should be very similar to high resolution reconstruction such as 100 ps or better.

In conclusion, even at high time resolution, using an accurate attenuation map within the PET reconstruction is essential to obtain robust quantitative measures. When the attenuation map is not known precisely enough (as is usually the case for lung imaging), the attenuation images would need to be systematically re-estimated, for example via MLAA. This is especially important in future scanners with sub-100 ps time resolution.

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Appendix A. Extension to other reconstruction algorithms

The notations in this appendix follows the one used in section [2.3.](#page-6-0) In this appendix, we derive formulas similarto equation (12) (12) for unweighted least-squares reconstructions. When using pre-corrected data, this derivation is equivalent to that of filtered back-projection. The unweighted least-squares solution is obtained by solving

$$
\min_{\lambda \ge 0} \|\mathbf{p} - \mathbf{M}\lambda\|_2^2 \tag{A1}
$$

The solutions of (A1) with $M = M^*$ and $M = \widetilde{M}$ are respectively

$$
\widehat{\lambda} = (M^{\star T} M^{\star})^{-1} M^{\star T} p
$$
 and $\widetilde{\lambda} = (\widetilde{M}^T \widetilde{M})^{-1} \widetilde{M}^T p$

where $[\cdot]^{T}$ is the transpose matrix operator. For a voxel pair (j, j') and using ([9\)](#page-6-0), we have the following element of M^TM :

$$
[\boldsymbol{M}^{\mathrm{T}}\boldsymbol{M}]_{j,j'}=\sum_{i\in\mathcal{D}}M_{i,j}M_{i,j'}=\delta_{j,j'}\sum_{i\in\mathcal{S}_j}M_{i,j}^2\,,
$$

where $\delta_{j,j'}$ is the Kronecker delta. Thus, M^TM is a diagonal matrix and the solution $\widehat\lambda$ corresponding to a given system matrix M is therefore straightforward (provided that $\sum_{i \in \mathcal{S}_j} M_{i,j}^2 > 0$):

$$
\widehat{\lambda}_j = \frac{\sum_{i \in S_j} M_{i,j} p_i}{\sum_{i \in S_j} M_{i,j}^2}.
$$

In the noiseless situation $p = M^* \lambda^*$, then

$$
\widehat{\lambda}_{j} = \lambda_{j}^{\star} \cdot \frac{\sum_{i \in S_{j}} M_{i,j} M_{i,j}^{\star}}{\sum_{i \in S_{j}} M_{i,j}^{2}}
$$
\n(A2)

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References

- Ahn S, Cheng L and Manjeshwar M 2014 Analysis of the effects of errors in attenuation maps on PET quantitation in TOF PET *2014 IEEE Nuclear Science Symp. and Medical Imaging Conf. (NSS/MIC) (Seattle, WA, 8–15 November 2014)* [\(https://doi.org/10.1109/](https://doi.org/10.1109/NSSMIC.2014.7430781) [NSSMIC.2014.7430781\)](https://doi.org/10.1109/NSSMIC.2014.7430781)
- Alessio A M, Kinahan P E, Cheng P M, Vesselle H and Karp J S 2004 PET/CT scanner instrumentation, challenges and solutions *Radiol. Clin. North Am.* **[42](https://doi.org/10.1016/j.rcl.2004.08.001)** [1017–32](https://doi.org/10.1016/j.rcl.2004.08.001)
- Bai C, Kinahan P E, Brasse D, Comtat C, Townsend D E, Meltzer C C, Villemagne V, Charron M and Defrise M 2003 An analytic study of the effects of attenuation on tumor detection in whole-body PET oncology imaging *Eur. J. Nucl. Med.* **44** 1855–61
- Bettinardi V, Presotto L, Rapisarda E, Picchio M, Gianolli L and Gilardi M C 2011 Physical performance of the new hybrid PET/CT discovery-690 *Med. Phys.* **[38](https://doi.org/10.1118/1.3635220)** [5394](https://doi.org/10.1118/1.3635220)
- Blodgett T M, Mehta A S, Mehta A S, Laymon C M, Carney J and Townsend D W 2011 PET/CT Artifacts *Clin. Imaging* **[35](https://doi.org/10.1016/j.clinimag.2010.03.001)** [49–63](https://doi.org/10.1016/j.clinimag.2010.03.001) Bousse A, Bertolli O, Atkinson D, Arridge S, Ourselin S, Hutton B F and Thielemans K 2016 Maximum-likelihood joint image
- reconstruction/motion estimation in attenuation-corrected respiratory gated PET/CT using a single attenuation map *IEEE Trans. Med. Imaging* **[35](https://doi.org/10.1109/TMI.2015.2464156)** [217–28](https://doi.org/10.1109/TMI.2015.2464156)
- Bousse A, Manber R, Holman B F, Atkinson D, Arridge S, Ourselin S, Hutton B F and Thielemans K 2017 Evaluation of a direct motion estimation/correction method in respiratory-gated PET/MRI with motion-adjusted attenuation *Med. Phys.* **[44](https://doi.org/10.1002/mp.12253)** [2379–90](https://doi.org/10.1002/mp.12253)
- Cates J W and Levin C S 2018 Evaluation of a TOF-PET detector design that achieves = 100 ps coincidence time resolution *Phys. Med. Biol.* **[63](https://doi.org/10.1088/1361-6560/aac504)** [115011](https://doi.org/10.1088/1361-6560/aac504)
- Conti M 2011 Why is TOF PET reconstruction a more robust method in the presence of inconsistent data? *Phys. Med. Biol.* **[56](https://doi.org/10.1088/0031-9155/56/1/010)** [155–68](https://doi.org/10.1088/0031-9155/56/1/010) Cuplov V, Holman B F, McClelland J, Modat M, Hutton B F and Thielemans K 2018 Issues in quantification of registered respiratory
- gated PET/CT in the lung *Phys. Med. Biol.* **[63](https://doi.org/10.1088/1361-6560/aa950b)** [015007](https://doi.org/10.1088/1361-6560/aa950b) Defrise M, Rezaei A and Nuyts J 2012 Time-of-flight PET data determine the attenuation sinogram up to a constant *Phys. Med. Biol.* **[57](https://doi.org/10.1088/0031-9155/57/4/885)** [885–99](https://doi.org/10.1088/0031-9155/57/4/885)
- Dempster A P, Laird N M and Rubin D B 1977 Maximum likelihood from incomplete data via the em algorithm *J. R. Stat. Soc. Ser.* B **39** 1–38
- Efthimiou N, Emond E, Wadhwa P, Cawthorne C, Tsoumpas C and Thielemans K 2018 Implementation and validation of time-of-flight PET image reconstruction module for listmode and sinogram projection data in the STIR library *Phys. Med. Biol.* **[64](https://doi.org/10.1088/1361-6560/aaf9b9)** [035004](https://doi.org/10.1088/1361-6560/aaf9b9)
- Emond E C, Bousse A, Brusaferri L, Groves A M, Hutton B F and Thielemans K 2019 Mass preservation for respiratory motion registration in both PET and CT *IEEE Symp. and Conf.* (accepted)
- Geramifar P, Zafarghandi M S, Ghafarian P, Rahmim A and Ay M R 2013 Respiratory-induced errors in tumor quantification and delineation in ct attenuation-corrected PET images: Effects of tumor size, tumor location and respiratory trace: A simulation study using the 4D XCAT phantom *Mol. Imaging Biol.* **[15](https://doi.org/10.1007/s11307-013-0656-5)** [655–65](https://doi.org/10.1007/s11307-013-0656-5)
- Holman B F, Cuplov V, Hutton B F, Groves A M and Thielemans K 2016 The effect of respiratory induced density variations on non-TOF PET quantitation in the lung *Phys. Med. Biol.* **[61](https://doi.org/10.1088/0031-9155/61/8/3148)** [3148–63](https://doi.org/10.1088/0031-9155/61/8/3148)
- Kinahan P E, Townsend D W, Beyer T and Sashin D 1998 Attenuation correction for a combined 3D PET/CT scanner *Med. Phys.* **[25](https://doi.org/10.1118/1.598392)** [2046–53](https://doi.org/10.1118/1.598392)
- Kotasidis F A, Mehranian A and Zaidi H 2016 Impact of time-of-flight on indirect 3D and direct 4D parametric image reconstruction in the presence of inconsistent dynamic PET data *Phys. Med. Biol.* **[61](https://doi.org/10.1088/0031-9155/61/9/3443)** [3443–71](https://doi.org/10.1088/0031-9155/61/9/3443)
- Lange K and Carson R 1984 Em reconstruction algorithms for emission and transmission tomography *J. Comput. Assist. Tomogr.* **8** 306–16
- Leahy R M and Qi J 2000 Statistical approaches in quantitative positron emission tomography *Stat. Comput.* **[10](https://doi.org/10.1023/A:1008946426658)** [147–65](https://doi.org/10.1023/A:1008946426658)
- Lecoq P 2017 Pushing the Limits in Time-of-Flight PET Imaging *IEEE Trans. Radiat. Plasma Med. Sci.* **[1](https://doi.org/10.1109/TRPMS.2017.2756674)** [473–85](https://doi.org/10.1109/TRPMS.2017.2756674)
- Lillington J *et al* 2019 PET/MRI attenuation estimation in the lung: A review of past, present and potential techniques *Med. Phys.* **[47](https://doi.org/10.1002/mp.13943)** [790–811](https://doi.org/10.1002/mp.13943)
- Merida I, Reilhac A, Redoute J, Heckemann R A, Costes N and Hammers A 2017 Multi-atlas attenuation correction supports full quantification of static and dynamic brain PET data in PET-MR *Phys. Med. Biol.* **[62](https://doi.org/10.1088/1361-6560/aa5f6c)** [2834–58](https://doi.org/10.1088/1361-6560/aa5f6c)
- Mehranian A and Zaidi H 2015 Impact of time-of-flight PET on quantification errors in MR imaging-based attenuation correction *Eur. J. Nucl. Med.* **[56](https://doi.org/10.2967/jnumed.114.148817)** [635–41](https://doi.org/10.2967/jnumed.114.148817)
- Mettler Jr F A and Guiberteau M J 2018 *Essentials of Nuclear Medicine and Nuclear Imaging* (Amsterdam: Elsevier)
- Nuyts J, Dupont P, Stroobants S, Benninck R, Mortelmans L and Suetens P 1999 Simultaneous maximum a posteriori reconstruction of attenuation and activity distributions from emission sinograms *IEEE Trans. Med. Imaging* **[18](https://doi.org/10.1109/42.774167)** [393–403](https://doi.org/10.1109/42.774167)
- Nyflot M J, Lee T C, Alessio A M, Wollenweber S D, Stearns C W, Bowen S R and Kinahan P E 2015 Impact of CT attenuation correction method on quantitative respiratory-correlated (4D) PET/CT imaging *Med. Phys.* **[42](https://doi.org/10.1118/1.4903282)** [110–20](https://doi.org/10.1118/1.4903282)
- Ollinger J M 1996 Model-based scatter correction for fully 3D PET *Phys. Med. Biol.* **[41](https://doi.org/10.1088/0031-9155/41/1/012)** [153–76](https://doi.org/10.1088/0031-9155/41/1/012)

Pan T *et al* 2005 Attenuation correction of PET images with respiration-averaged CT images in PET/CT *J. Nucl. Med.* **46** 1481–7

- Pan T et al 2019 Performance evaluation of the 5-Ring GE Discovery MI PET/CT system using the national electrical manufacturers association NU 2-2012 standard *Med. Phys.* **[46](https://doi.org/10.1002/mp.13576)** [3025–33](https://doi.org/10.1002/mp.13576)
- Rausch I, Cal-González J, Dapra D, Gallowitsch H J, Lind P, Beyer T and Minear G 2015 Performance evaluation of the biograph mCT Flow PET/CT system according to the NEMA NU2-2012 standard *EJNMMI Phys.* **[2](https://doi.org/10.1186/s40658-015-0132-1)** [1–17](https://doi.org/10.1186/s40658-015-0132-1)

Rezaei A, Schramm G, Willekens S M A, Delso G, Van Laere K and Nuyts J 2019 A quantitative evaluation of joint activity and attenuation reconstruction in TOF-PET/MR brain imaging *J. Nucl. Med.* **[60](https://doi.org/10.2967/jnumed.118.220871)** [1649–55](https://doi.org/10.2967/jnumed.118.220871)

Shepp L A and Vardi Y 1982 Maximum likelihood reconstruction in emission tomography *IEEE Trans. Med. Imaging* **[1](https://doi.org/10.1109/TMI.1982.4307558)** [113–22](https://doi.org/10.1109/TMI.1982.4307558) The 10 ps Challenge committee 2019 'The 10 ps Challenge website' <https://the10ps-challenge.org/> (Accessed: 9 November 2019) Thielemans K, Asma E, Manjeshwar R M, Ganin A and Spinks T J 2008 Image-based correction for mismatched attenuation in PET images *IEEE Symp. Conf.* [pp 5292–6](https://doi.org/10.1109/NSSMIC.2008.4774427)

van Sluis J, de Jong J, Schaar J, Noordzij W, van Snick P, Dierckx R, Borra R, Willemsen A and Boellaard R 2019 Performance characteristics of the digital biograph vision PET/CT system *J. Nucl. Med.* **[60](https://doi.org/10.2967/jnumed.118.215418)** [1031–6](https://doi.org/10.2967/jnumed.118.215418)

Watson C C, Newport D and Casey M E 1996 *Three-Dimensional Image Reconstruction in Radiology and Nuclear Medicine* (Berlin: Springer) pp 255–68

Yushkevich P A, Piven J, Hazlett H C, Smith R G, Ho S, Gee J C and Gerig G 2006 User-guided 3D active contour segmentation of anatomical structures: Significantly improved efficiency and reliability *NeuroImage* **[31](https://doi.org/10.1016/j.neuroimage.2006.01.015)** [1116–28](https://doi.org/10.1016/j.neuroimage.2006.01.015)