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### **Spatial self-structuring accelerates** adaptive speciation in sexual populations

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### Interim Report IR-12-040

## Spatial self-structuring accelerates adaptive speciation in sexual populations

Varvara Fazalova Ulf Dieckmann (dieckmann@iiasa.ac.at)

#### Approved by

Pavel Kabat Director General and Chief Executive Officer

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1	Spatial self-structuring accelerates adaptive speciation
2	in sexual populations
3	Varvara Fazalova <sup>1,2</sup> and Ulf Dieckmann <sup>1</sup>
4	<sup>1</sup> Evolution and Ecology Program, International Institute for Applied Systems Analysis,
5	Schlossplatz 1, A-2361 Laxenburg, Austria
6	<sup>2</sup> Limnological Institute of the Siberian Branch of the Russian Academy of Sciences,
7	Ulan-Batorskaya 3, 664033 Irkutsk, Russia
8	

#### 9 Abstract

10 **Questions:** How does spatial self-structuring influence the waiting time until adaptive 11 speciation in a population with sexual reproduction? Which mechanisms underlie this effect?

Model: Using a spatially explicit individual-based multi-locus model of adaptive speciation, we investigate the evolution of a sexually reproducing population, with different levels of spatial self-structuring induced by different distances of natal dispersal. We analyze how waiting times until speciation are affected by the mobility of individuals, the number of loci determining the phenotype under disruptive selection, and the mating costs for individuals preferring rare phenotypes.

Conclusions: Spatial self-structuring facilitates the evolution of assortative mating 18 and accelerates adaptive speciation. We identify three mechanisms that are responsible for 19 this effect: (i) spatial self-structuring promotes the evolution of assortativity by providing 20 assortative mating "for free," as individuals find phenotypically similar mates within their 21 spatial clusters; (ii) it helps assortatively mating individuals with rare phenotypes to find mat-22 ing partners even when the selected phenotype is determined by a large number of loci, so that 23 strict assortativity is difficult; and (iii) it renders speciation less sensitive to costs of 24 assortative mating, especially for individuals preferring rare phenotypes. 25

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#### 27 Introduction

Speciation without geographic isolation has long been surrounded by controversy in evolu-28 tionary-biology research. For speciation to occur in the presence of gene flow, two essential 29 elements are necessary: ecological diversification and reproductive isolation between extreme 30 phenotypes (e.g., Maynard Smith 1966). While a number of theoretical studies have shown 31 that these elements can be established as a result of competitive interactions between individ-32 uals, and this scenario has received much attention in theoretical research (Rosenzweig 1978; 33 Slatkin 1979; Felsenstein 1981; Seger 1985; Udovic 1980; Doebeli 1996; Dieckmann and 34 Doebeli 1999; Bürger et al. 2006; Pennings et al. 2008; Ripa 2008), the exact conditions al-35 lowing for speciation without geographic isolation remain debated. Some of these conditions 36 have been addressed in several recent studies, including the number of loci determining the 37 trait under disruptive selection (e.g., Gourbiere 2004; Bolnick 2004; Bürger et al. 2006; 38 Bürger and Schneider 2006; Rettelbach et al. 2011), the strength of assortative mating (e.g., 39 Kirkpatrick and Nuismer 2004; Doebeli et al. 2007; Otto et al. 2008), and the cost of choosi-40 ness (e.g., Matessi et al. 2002; Bürger and Schneider 2006; Schneider and Bürger 2006; Kopp 41 and Hermisson 2008; Otto et al. 2008). 42

The number of loci determining phenotypic traits directly affects the phenotypic reso-43 lution at which these traits can be expressed: a larger number of loci results in a larger number 44 of possible phenotypic classes. This interferes with the competition strength between individ-45 uals (Bürger et al. 2006) and affects the number of mates that fall within a given individual's 46 range of acceptable phenotypes (Bolnick 2004). It has been shown that the likelihood of spe-47 ciation decreases when a large number of loci determine the traits under disruptive selection, 48 with speciation then being possible only when the level of assortative mating is high 49 (Gourbiere 2004; Bürger and Schneider 2006). Likewise, a large number of loci have been 50 shown to increase the waiting time until sympatric speciation (Dieckmann and Doebeli 1999, 51 2004; Bolnick 2004). However, also the opposite effect on the likelihood of speciation has 52 been reported (Kondrashov and Kondrashov 1999; Bürger et al. 2006; Rettelbach et al. 2011). 53

Reproductive isolation in sympatry usually results from a form of assortative mating, which may be pre-established or may evolve simultaneously with divergence in the trait under disruptive selection. In the case of pre-established assortative mating, reproductive isolation is more likely to emerge under a moderate level of assortativity, while very strong assortative mating can in fact act against speciation, by reducing polymorphism and by generating stabilizing sexual selection (Kirkpatrick and Nuismer 2004; Bürger et al. 2006; Otto et al. 2008). On the other hand, assortative mating might evolve simultaneously with ecological diver-

gence under a complex interplay of natural and sexual selection. It has been established that 61 the evolution of mating preference (from random to assortative) is generally favored when 62 intermediate phenotypes are less fit (Dieckmann and Doebeli 1999; Otto et al. 2008; Pennings 63 et al. 2008; Ripa 2008). It has been reported that if selection against intermediate phenotypes 64 ceases once they are sufficiently rare, evolution of assortative mating might stop at an inter-65 mediate level, thus preventing speciation (Matessi et al. 2002; Pennings et al. 2008). On the 66 other hand, in a model of secondary contact, an intermediate level of assortative mating has 67 been found to promote maximal trait differentiation (Servedio 2011). And even though it is 68 widely understood that recombination in sexual populations tends to obstruct adaptive specia-69 tion (Maynard Smith 1966; Felsenstein 1981), it has also been highlighted that under condi-70 tions of frequency-dependent selection recombination kernels of intermediate width can pro-71 mote ecological diversification and the evolution of assortative mating (Noest 1997; Doebeli 72 et al. 2007). 73

Costs of choosiness restrict the number of mating trials per female and/or otherwise 74 decrease the reproductive success of individuals preferring rare phenotypes. Recent findings 75 confirm the intuitive expectation that when high costs are associated with assortative mating, 76 this can prohibit the latter's evolution, thus reducing the range of conditions under which spe-77 ciation is possible (Matessi et al. 2002; Bürger and Schneider 2006; Schneider and Bürger 78 2006; Kopp and Hermisson 2008; Otto et al. 2008). It has also been reported that when costs 79 of choosiness are incorporated into models of adaptive speciation, waiting times until specia-80 tion are prolonged (Bolnick 2004). 81

The aforementioned studies considering conditions for non-allopatric speciation do 82 not take into account spatial interactions among individuals, but instead assume that organ-83 isms compete and form reproductive pairs irrespective of the relative spatial location of other 84 individuals. However, local interactions are important and inherent to most biological systems, 85 and the spatial distribution of individuals within populations is therefore bound to influence 86 the level of gene flow and the degree of intraspecific competition among the resident pheno-87 types. Local interactions between individuals are defined by spatial population structure, 88 which broadly speaking can arise in two forms. First, spatial structuring can be induced by 89 environmental heterogeneity. The evolutionary dynamics of populations with environmentally 90 induced spatial structure have been investigated both in metapopulations comprising discrete 91 spatially segregated patches (Gavrilets et al. 1998, 2000; Day 2001; Gavrilets and Vose 2005) 92 and along continuous environmental gradients (Endler 1977; Day 2000; Doebeli and 93 Dieckmann 2003, 2005; Mizera and Meszéna 2003; Heinz et al. 2009; Payne et al. 2011). Se-94 cond, if a spatial environment is homogeneous and uniform, the creation and maintenance of 95

spatial structure occurs only through self-structuring. Self-structuring emerges spontaneously as a result of intrinsic ecological dynamics (Lion and Baalen 2008), including those giving rise to reproductive pair correlations (Young et al. 2001). For populations with asexual reproduction, it has recently been reported that the coexistence of species, as well as their emergence through evolutionary branching, occurs for more restrictive parameter combinations when modeled on a lattice than when modeled under well-mixed conditions (Mágori et al. 2005).

Here we incorporate sexual reproduction into a model of adaptive speciation and investigate the effect of spatial self-structuring on the waiting time until speciation. In this context, we also investigate the interactions of spatial self-structuring, first, with the effect of the number of loci determining the trait under disruptive selection, and second, with the consequences of mating costs for individuals preferring rare phenotypes.

#### 108 Methods

#### **Model description**

**Overview.** Our individual-based model describes the genotypic and phenotypic evolutionary dynamics of sexual populations. The phenotypic traits of individuals are determined by several loci, which allows for a gradual evolution of resource specialization and mating behavior. The model is defined in continuous time and continuous space, with periodic boundary conditions in a uniform environment on the unit square. Algorithmically, the model is implemented according to the minimal-process method (Gillespie 1976).

Individuals. Each individual possesses two phenotypic traits, each of these being de-116 termined by two sets of diallelic diploid loci with equal additive effect. The first trait is an 117 ecological character, which controls resource use and thus affects competition. The second 118 trait is a mating preference, which regulates the degree of assortativeness when mating. Each 119 trait is defined by the difference between the number of "+" and "-" alleles, divided by the 120 total number of alleles, so that both traits can vary from -1 to +1. The ecological trait u de-121 termines the type of resource or environment to which an individual is best adapted. Specifi-122 cally, the function  $K(u) = K_0 N_{\sigma_v}(u)$  describes how u determines an individual's carrying-123 capacity density, where  $N_{\sigma}(z) = \exp(-\frac{1}{2}z^2/\sigma^2)$  and  $K_0$  is the maximally attainable carrying-124 capacity density. The mating trait a determines the mating preference of individuals, based 125 on similarity in the ecological trait. Mating preference can vary from disassortative (a < 0) to 126 assortative (a > 0), with random mating occurring for a = 0. All individuals in the model are 127

characterized by the rates at which births, deaths, and dispersals occur, as well as by their spatial location (x, y), with  $0 \le x, y \le 1$ .

**Events.** All individuals *i* are assigned birth rates  $b_i$ , death rates  $d_i$ , and dispersal 130 rates  $m_i$ , for i = 1, ..., N, where N is the current population size. These rates are updated after 131 each event. The time that elapses until the next event is based on the total rates  $B = \sum_{i=1}^{N} b_i$ , 132  $D = \sum_{i=1}^{N} d_i$ ,  $M = \sum_{i=1}^{N} m_i$ , and E = B + D + M, being drawn from an exponential probability 133 density with mean 1/E. The affected individual *i* for the next event (birth, death, or dispersal) 134 of the process is then chosen with probability  $(b_i + d_i + m_i) / E = e_i / E$ . The type of event is cho-135 sen according to probabilities  $b_i/e_i$ ,  $d_i/e_i$ , and  $m_i/e_i$ , respectively. Accordingly, the affect-136 ed individual will reproduce by giving birth to one offspring, will die, or will perform a dis-137 persal step. Unless stated otherwise, the parameter values we use for model runs are shown in 138 Table 1. 139

**Reproduction.** The mating probability between individuals *i* and *j* is given by the 140 product of a phenotypic weight  $p_{ij}$  and a spatial weight  $q_{ij}$  (Doebeli and Dieckmann 2003). 141 For a < 0, the phenotypic weight is defined as  $p_{ij} = 1 - N_{\sigma_-}(\Delta u_{ij})$ , where  $\sigma_- = a^2$ , and  $\Delta u_{ij}$  is 142 the phenotypic difference between the potential mates *i* and *j*. For a > 0,  $p_{ij} = N_{\sigma_+}(\Delta u_{ij})$ , 143 where  $\sigma_{+} = 1/(20a^2)$ . For a = 0,  $p_{ij} = 1$ . The spatial weight  $q_{ij}$  decreases with the spatial 144 distance  $r_{ij} = \sqrt{\Delta x_{ij}^2 + \Delta y_{ij}^2}$  between potential mates *i* and *j* according 145 to  $q_{ij} = N_{\sigma_p}(r_{ij})/(2\pi\sigma_p^2)$ . The offspring inherits alleles from both of its parents at each locus in-146 dependently, implying free recombination. Random mutations that switch alleles from "+" to 147 "-", and vice versa, occur with a small probability  $\mu$ . A cost for individuals preferring to ma-148 te with locally rare phenotypes arises from a birth rate defined as  $b_i = bN_{p,i} / (c + N_{p,i})$ , where 149  $N_{p,i} = \sum_{j=1, j \neq i}^{N} p_{ij} q_{ij}$  is the number of suitable mating partners in the neighborhood of individu-150 al i, and c is the strength of the cost. 151

**Death.** An individual's death rate depends both on local logistic competition and its carrying-capacity density. Specifically, the death rate of individual *i* with ecological trait  $u_i$ at location  $(x_i, y_i)$  is defined as  $d_i = [2\pi\sigma_s^2 K(u_i)]^{-1} \sum_{j=1, j\neq i}^N N_{\sigma_s}(\Delta u_{ij}) N_{\sigma_s}(\Delta y_{ij})$ , where the competition function's standard deviations are denoted by  $\sigma_c$  for phenotypic differences and by  $\sigma_s$  for spatial distances.

Dispersal. There are two types of dispersal events. First, each newborn individual undergoes natal dispersal from the location of its mother, i.e., of the parent that has chosen its mate. Second, the subsequent dispersal of all individuals occurs at a constant rate  $m_i = m$ . In either case, individuals are changing their locations by random displacements in the directions x and y, each drawn from a normal distribution with mean 0 and standard deviation  $\sigma_m$ .

#### 162 Identification of speciation

To identify speciation, we apply the following criterion. We count the number of individuals 163 for each of the phenotypic classes of the ecological trait (the number of these classes equals 164 twice the number of loci determining the ecological trait plus 1). In the resulting histogram, 165 we identify the two most prevalent phenotypic classes, denoting the corresponding number of 166 individuals by  $h_1$  and  $h_2$ , while denoting the total number of individuals in all intermediate 167 phenotypic classes by  $h_{\min}$ . We recognize speciation, if three conditions are met simultaneous-168 ly: (i) the two peaks are sufficiently separated, i.e., the phenotypes  $u_1$  and  $u_2$  that correspond 169 to  $h_1$  and  $h_2$  differ by at least 0.5,  $|u_1 - u_2| \ge 0.5$ ; (ii) hybrids in between the two peaks are suf-170 ficiently rare, i.e., the total number  $h_{\min}$  of intermediate individuals is less than 5% of the av-171 erage of  $h_1$  and  $h_2$ ,  $h_{\min} < 0.05 (h_1 + h_2)/2$ ; and (iii) the heights of the two peaks are suffi-172 ciently similar, i.e.,  $h_1$  and  $h_2$  differ by a factor of less than 2,  $0.5 < h_1 / h_2 < 2$ . Extensive 173 numerical explorations confirm that this criterion ensures the stability of the phenotypic clus-174 ters resulting from speciation, across the full parameter range we investigate: if speciation is 175 recognized, we never observe the subsequent collapse of those phenotypic clusters. We refer 176 to the time at which this criterion is first met as the waiting time T until speciation. To ex-177 plore stochastic variation in this waiting time, we employ replicate model runs (using differ-178 ent random seeds). We perform these model runs across the parameter range that has previ-179 ously been identified as allowing for speciation (Dieckmann and Doebeli 1999, 2004). To en-180 sure that all model runs have enough time to result in speciation, we continued them until a 181 sufficiently long maximal duration (5000 generations). 182

#### 183 Identification of the average size of spatial clusters

In our model, spatial self-structuring implies the emergence of spatial clusters that are dynam-184 ic and have self-organized shapes and sizes. To measure the average size of these spatial clus-185 ters for different degrees of spatial self-structuring, we calculate the pairwise distances r be-186 tween all individuals of the population. For well-mixed populations in two-dimensional envi-187 ronments, the expected number C(r) of pairs of individuals with distances between r and 188 r + dr for small dr increases linearly with r, so we construct correlation histograms as 189 c(r) = C(r)/r. In well-mixed populations, there are no spatial aggregations of individuals, so 190 the corresponding function  $c_m(r)$  is flat. Conversely, self-structuring results in the emergence 191 of spatial clusters, so the function  $c_s(r)$  shows a peak at small values of r. With increasing r, 192  $c_{s}(r)$  decreases at a speed proportional to the level of self-structuring, first dropping below 193 and then eventually converging to  $c_m(r)$ . The drop below  $c_m(r)$  corresponds to the empty 194 areas around the spatial clusters. Thus, we identify the average cluster size as the distance at 195

which the function  $c_s(r)$  describing a self-structured population intersects with the function  $c_m(r)$  for the corresponding well-mixed population (for the latter, we set  $\sigma_m = 0.2$ ). Since the mating radius  $\sigma_p$  also influences the size of spatial clusters, we consider 15 different values of  $\sigma_p$  for each of the 15 analyzed values of  $\sigma_m$  (Figure 2;  $0.01 \le \sigma_m \le 0.08$  and  $0.01 \le \sigma_p \le 0.1775$ ). For each of these 225 combinations of  $\sigma_m$  and  $\sigma_p$ , we analyze 5,000 snapshots of spatial structure. The average cluster size for each  $\sigma_m$  is averaged over the considered 15 values of  $\sigma_p$ .

#### 203 **Results**

# Adaptive speciation is faster in self-structured than in well-mixed sexual populations

Figure 1 shows typical results for the joint evolution of resource utilization and mating prefer-206 ence in spatially well-mixed populations and spatially self-structured populations, accompa-207 nied by snapshots of the corresponding initial and resulting spatial patterns. Initially, individ-208 uals are either randomly distributed in space (Figure 1a) or aggregated in spatial clusters (Fig-209 ure 1d). The evolution of resource utilization starts from monomorphic populations located at 210 the resource optimum (Figures 1b and 1e, top panels). The mating preference first gradually 211 changes from random to slightly assortative (Figures 1b and 1e, bottom panels); this reduces 212 gene flow and allows for diversification of the ecological trait, with two phenotypic clusters 213 emerging (Figures 1b and 1e, top panels). The degree of assortative mating eventually be-214 comes stronger, and this allows reproductive isolation to be established between those two 215 phenotypic clusters. 216

In self-structured populations, assortatively mating individuals limit their partner search to spatial clusters, thus decreasing the probability of recombination between phenotypic morphs occupying different clusters. As some phenotypes that prevail transiently become extinct only after more extreme phenotypes get locally established, the reduced supply of recombinants means that the distribution of phenotypes across phenotypic clusters remains polymorphic for longer periods.

After adaptive speciation, more individuals mate assortatively in self-structured populations (Figure 1e, bottom panel) than in well-mixed populations (Figure 1b, bottom panel). Individuals of the two newly formed species are distributed across the whole habitat either randomly (Figure 1c) or in spatial clusters (Figure 1f). The resulting mosaic of spatial clusters is endogenously generated by intrinsic ecological dynamics, even though the considered habitat is continuous and completely homogeneous. Spatial clusters dynamically arise as selforganized entities with characteristic average diameters (see below). The number of individuals inside a cluster depends on the balance between the local birth and death processes
(source-sink dynamics). The distance between clusters is defined by the spatial competition
radius, and also arises endogenously.

It is noteworthy that inside the spatial clusters of self-structured populations, assortatively mating individuals are likely to encounter appropriate mating partners; this provides conditions for assortative mating "for free," which may in turn be responsible for the greater fraction of individuals mating assortatively, and thus for the earlier speciation in these populations. The next subsection confirms this interpretation.

#### 238 Optimal ratio of mating radius and dispersal radius promotes early speciation

To understand in greater detail how spatial self-structuring provides conditions for assortative 239 mating "for free," and thus accelerates speciation, we compare waiting times until speciation 240 for many different combinations of dispersal radius and mating radius. The degree of spatial 241 self-structuring in sexually reproducing populations is determined by both of these parameters. 242 While the dispersal radius directly affects the spatial population structure, the influence of the 243 mating radius is indirect, by defining the spatial area across which mate search occurs: if this 244 area is large, spatial population structure, even if present, has no impact on the availability of 245 phenotypes that can be chosen as mates. 246

Figure 2 shows the dependence of the average waiting time until speciation on the dispersal radius and the mating radius. Light and dark areas correspond to short and long waiting times until speciation, respectively. In populations with the highest considered level of selfstructuring ( $\sigma_m = 0.01$ ), an increase in mating radius delays speciation. For intermediate levels of self-structuring ( $0.02 \le \sigma_m \le 0.05$ ), a very small or very large mating radius delays speciation. A further increase in dispersal radius (beyond  $\sigma_m = 0.05$ ) makes the spatial clusters indistinguishable, so the waiting time until speciation is no longer affected.

The thick curve in Figure 2 shows the average size of spatial clusters for different dispersal radii. Comparing the mating radii enabling the earliest speciation with these sizes of spatial clusters reveals that speciation times are shortest when the mating radius corresponds to one-fourth to one-third of the cluster size, as indicated by the two dashed curves in Figure 2.

#### 258 Spatial self-structuring weakens the effect of a large number of loci

Figure 3 shows that increasing the number of loci determining the ecological trait delays speciation. As we explain below, this delay is caused by the diminished level of strict assortative mating when a large number of loci results in a higher resolution of the phenotypes that can
be expressed for the ecological trait.

For a small number of loci, assortative mate choice easily becomes virtually restricted 263 to partners with identical phenotypes (Figure 3b, panel for 5 loci), whereas for a large number 264 of loci, the same degree of assortativity (as measured by the mating trait a) leads to mating 265 individuals accepting mates from a larger number of phenotypic classes (Figure 3b, panels for 266 10 and 15 loci). This occurs because mating probabilities are a function of the absolute pheno-267 typic difference between potential partners. Therefore, if a large number of loci determine the 268 ecological trait, the relative proportion of strictly assortative mating is smaller. This decreases 269 the probability of alleles increasing assortativity spreading in the populations, and thereby de-270 lays speciation. 271

Importantly, we not only find that in self-structured populations the waiting time until 272 speciation is shorter (Figures 1 and 2), but also that this effect of spatial self-structuring be-273 comes more noticeable with an increase in the number of loci determining the ecological trait. 274 This suggests that in such populations the aforementioned effect of assortative mating "for 275 free" is increasingly important for promoting the establishment of assortative mate choice and 276 for accelerating speciation, by providing an alternative mechanism for enhancing the relative 277 proportion of strictly assortative mating. This explains why for a small number of loci the ef-278 fect of spatial self-structuring is negligible, because strictly assortative mating is facilitated by 279 the resultant low phenotypic resolution, so that speciation in this case occurs very fast. 280

#### 281 Spatial self-structuring renders mating costs less severe for rare phenotypes

The influence of the mating cost on the average waiting time until speciation is shown in Figure 4a. We find that in well-mixed populations ( $\sigma_m = 0.07$ ) an increase in the mating cost for individuals preferring rare phenotypes delays speciation. By contrast, in highly self-structured populations ( $\sigma_m = 0.01$ ), as well as in populations with an intermediate level of spatial selfstructuring ( $\sigma_m = 0.035$ ), even a strong mating cost does not cause a significant delay in the average waiting time until speciation.

To find a mechanistic explanation for this observation, we track the evolution of a population's average level of assortative mating. The mean values of mating traits among individuals of populations for different degrees of spatial self-structuring and for different strengths of mating costs, are shown in the small panels of Figure 4b. Both for highly structured populations ( $\sigma_m = 0.01$ ) and for intermediately structured populations ( $\sigma_m = 0.035$ ), the evolution of mate choice proceeds in a similar way, with the average mating trait gradually evolving toward assortative mating. By contrast, in well-mixed populations ( $\sigma_m = 0.07$ ), the average level of assortative mating keeps fluctuating around random mating when the mating cost is strong (c = 10). From these observations, we can thus conclude that the mating cost affects the waiting time until speciation by inhibiting the evolution of assortative mating and that this effect can be overcome by the spatial self-structuring of populations.

#### 299 **Discussion**

In this study, we have investigated how the waiting time until adaptive speciation in a popula-300 tion with sexual reproduction is influenced by spatial self-structuring. We find that self-301 structuring generally facilitates the evolution of assortative mating and thus promotes earlier 302 speciation. The main feature of a self-structured population is that individuals inside a spatial 303 cluster tend to possess very similar phenotypes. This feature influences the evolutionary dy-304 namics in several ways. First, it allows for assortative mating "for free," since individuals typ-305 ically find phenotypically similar mates inside their spatial clusters (Figure 2), jump-starting 306 the evolution of assortative mating required for speciation. Second, it allows individuals pre-307 ferring rare phenotypes to find mating partners from the same phenotypic class, implying 308 strict assortative mating, even when a large number of loci determine the ecological trait (Fig-309 ure 3). Third, spatial self-structuring enables fast speciation even when individuals preferring 310 rare phenotypes experience additional fitness costs (Figure 4). 311

#### 312 Why an optimal ratio of mating radius and dispersal radius accelerates speciation

We find that waiting times until speciation are shortest when there is a match between the mating radius and the (natal) dispersal radius of individuals (Figure 2). Our comparison of the mating radius with the average size of spatial clusters suggests that speciation is fastest when the spatial mating radius is 3-4 times smaller than the average size of spatial clusters. This ratio guarantees that even individuals preferring rare phenotypes find appropriate mates, and thus promotes the evolution of assortative mating. When the mating radius is very small (  $\sigma_p = 0.01$ ), early speciation is only possible in highly self-structured populations.

Our results extend previous findings by Kawata (2002), who studied a spatially explicit model of sympatric speciation and found that the probability of speciation decreases with an increase in both mating area and dispersal radius. That study conjectured that an increase in both of these factors increases the dispersal of genes, which promotes recombination and thus homogenizes a population's genetic structure. As a result, it can destroy any association between alleles for ecological adaptation and alleles for assortative mating that might be created by natural selection (Felsenstein 1981). Our results suggest a different interpretation. While Kawata (2002) investigated the influence of dispersal radius and of the size of the mating area independently from each other, here we have explored the joint effect of these factors on the evolutionary dynamics underlying speciation. We find that the interaction between these two factors is more complex, with our results suggesting that speciation is fastest for a certain ratio between the mating radius and dispersal radius.

#### 332 Why spatial self-structuring weakens the effect of a large number of loci

Our results show that when the ecological trait is controlled by a large number of loci, the 333 waiting time until speciation is longer (Figure 3). The mechanism underlying this effect can 334 be described as follows: a large number of loci results in more phenotypic classes, and as mat-335 ing individuals accept a higher proportion of partners from different phenotypic classes, this 336 hinders the establishment of assortative mating and delays speciation. Our results confirm and 337 extend findings from previous studies in which a delay in speciation was observed resulting 338 from of a large number of loci determining the ecological trait (Dieckmann and Doebeli 1999, 339 2004; Bolnick 2004). Earlier, it was shown that (not surprisingly) increasing the phenotypic 340 width of the mating function prolongs the waiting time until speciation (Bolnick 2004). We 341 find that the this effect is weaker in self-structured populations, because appropriate mates are 342 likely to be available in a mating individual's local neighborhood, which allows those mating 343 individuals to find a large proportion of mates with identical phenotypes. 344

It has been reported that the likelihood of speciation depends in a "non-straightforward 345 way" on the number of loci determining the ecological trait (Bürger et al. 2006). Specifically, 346 Bürger and coauthors found that if disruptive selection is weak, the likelihood of speciation 347 decreases with an increased number of loci. They suggest that, under these conditions, split-348 ting the phenotypic distribution of ecological traits requires the emerging phenotypic clusters 349 in that trait to be located near the boundary of the corresponding phenotypic range, which 350 could be easier to achieve for a smaller number of loci. This is because, under these condi-351 tions, the average phenotypic distance between all resident phenotypes is larger, so the aver-352 age mating probabilities across phenotypic classes are lower. For stronger disruptive selec-353 tion, speciation is possible only with strong assortative mating, and speciation occurs more 354 readily with more loci, since the self-organized fine-tuning of the evolutionary dynamics 355 helps to keep phenotypic clusters at the optimal distance for coexistence. In our model, in-356 creasing the number of loci invariably results in delayed speciation. This is because we mostly 357 consider relatively weak disruptive selection, which results in phenotypic clusters always be-358 ing located at the boundary of the phenotypic range. When disruptive selection is strong, we 359 also observe the emergence of more than two phenotypic clusters when ecological traits are 360

determined by more than 15 loci. In such cases, evolutionary dynamics are more complex than those underlying the emergence of two species, and will benefit from additional investigation.

#### 364 Why spatial self-structuring reduces mating costs for rare phenotypes

Our results confirm that high mating costs increase the waiting time until speciation in well-365 mixed populations (Figure 4a), as mating individuals preferring rare phenotypes are less likely 366 to find appropriate mates. In well-mixed populations, potential mates for individuals with rare 367 phenotypes will usually be located at a significant spatial distance from those individuals 368 seeking a partner, so the mating cost reduces their chance to reproduce. This delays the evolu-369 tion of assortative mating, which causes a longer waiting time until speciation (Figure 3b). 370 Conversely, in self-structured populations, individuals possessing similar phenotypes form 371 spatial clusters: as mating individuals are then more likely to find appropriate mates in their 372 local neighborhood, the effect of mating cost is largely cancelled out. 373

Here we have modeled mating costs phenomenologically for individuals preferring (locally) rare phenotypes, similar to Doebeli and Dieckmann (2003) and Gourbiere (2004). Other studies have examined models of sympatric speciation in which costs for choosy individuals are modeled more mechanistically, resulting from a restriction of their number of mating trials (Drossel and McKane 2000; Doebeli and Dieckmann 2005; Bürger and Schneider 2006; Bürger et al. 2006; Schneider and Bürger 2006; Kopp and Hermisson 2008). We expect the effect of spatial self-structuring on speciation readily to extend to those later models.

#### 381 Comparison with other speciation modes

Throughout this study, we have referred to the examined diversification dynamics as adaptive speciation. This is because, in our model, the speciation process can be understood as an adaptive response that allows a population trapped at a fitness minimum through the action of frequency-dependent disruptive selection to escape from this trap (Dieckmann et al. 2004).

To further contextualize our findings, it might be worthwhile highlighting that the speciation processes analyzed here also meet the specifications of competitive speciation (which occurs when "intermediate forms [are] fit if and only if some extreme forms are rare or absent"; Rosenzweig 1978) and of ecological speciation (defined as the "evolution of reproductive isolation between populations as a result of ecologically-based divergent natural selection"; Schluter 2000; Schluter & Conte 2009).

In contrast to the aforementioned three process-based speciation modes of adaptive, competitive, and ecological speciation, traditional discussions of alternative speciation routes have instead focused on geographical patterns at the onset of species formation (e.g., Mayr 1942, 1963; Dobzhansky 1951). While the well-mixed populations we have analyzed here, by considering large radii for dispersal and mating, are essentially sympatric, smaller such radii result in ecological settings traditionally explored in the context of parapatric speciation scenarios, with the role of isolation by distance (Wright 1943) increasing as those radii become smaller relative to the average distance between neighboring individuals and to the spatial scale of the considered habitat.

Last but not least, the speciation dynamics we have examined here are related to the 401 notions of micro-allopatric speciation (Smith 1955, 1965) and mosaic sympatry (Mallet 2008; 402 Mallet et al. 2009). Both terms are used to refer to spatial patterns in which species can be 403 viewed as coexisting sympatrically when assessed at larger spatial scales, yet are recognized 404 as being spatially segregated when assessed at smaller spatial scales. This description fully 405 matches the spatial patterns resulting from self-structuring in our model, which could be taken 406 to suggest that both terms apply to our study. It must be borne in mind, however, that micro-407 allopatry and mosaic sympatry are meant to arise from a heterogeneous external environment 408 to which the coexisting species differentially latch on through habitat choice or habitat-409 dependent reproductive success, whereas the small-scale spatial segregation between the co-410 existing species observed in our model arises in a homogeneous external environment through 411 limited dispersal and phenotype-dependent local competition. Consequently, the spatial pat-412 terns emerging in our model should not be misunderstood as examples of either micro-413 allopatry or mosaic sympatry. 414

#### 415 Comparison with related studies and extensions

While our results show that spatial self-structuring accelerates speciation in sexual popula-416 tions, in populations with asexual reproduction the opposite effect has been found. Specifical-417 ly, a study by Day (2001) reported that limited dispersal in deme-structured metapopulations 418 inhibits disruptive selection, because mutants rarely gain a fitness benefit when being sur-419 rounded by very similar phenotypes. Mágori et al. (2005) investigated the coexistence of spe-420 cies, and their emergence through evolutionary branching, on a lattice and found that both of 421 these occur only for more restrictive parameter combinations than in well-mixed populations. 422 Also this latter result was explained by the reduced fitness advantage of rare mutant pheno-423 424 types.

To analyze the effects of spatial self-structuring on evolutionary branching in asexual populations, we can readily eliminate sexual reproduction and assortative mate choice from our model. Our corresponding investigations confirm the aforementioned previous findings by Day (2001) and Mágori et al. (2005), as well as the mechanism conjectured by those studies to underlie the observed delay of adaptive speciation. Going beyond those previous studies, we find that an additional mechanism contributes to the observed delay: in self-structured
asexual populations, common phenotypes, being situated at the fitness minimum causing disruptive selection, escape extinction for longer durations than in well-mixed populations, due
to their local coexistence with different phenotypes in spatial clusters (Fazalova and
Dieckmann, submitted).

In sexual populations, by contrast, the two aforementioned delaying effects of spatial self-structuring arising from natural selection are being overshadowed by the consequences of sexual selection: assortatively mating rare phenotypes gain an extra fitness benefit from cooccurring with similar phenotypes, while assortatively mating common phenotypes incur an extra fitness cost from co-occurring with other phenotypes.

In our study, spatial self-structuring arises from limited offspring dispersal. The result-440 ant spatio-phenotypic correlations facilitate the evolution of assortative mating, in turn pro-441 moting faster adaptive speciation. Analogous conditions favoring assortative mating may in-442 stead be generated through, or further enhanced by, other mechanisms, such as dispersal with 443 philopatry, dispersal with natal homing, conditional dispersal triggered by phenotype-based 444 quorum sensing, and/or dispersal concluding with habitat choice. All of these alternative or 445 additional mechanisms - being widespread among animal species and occurring even for mi-446 croorganisms - result in the kind of spatio-phenotypic correlations emerging in our model an-447 alyzed here, and can thus be expected likewise to facilitate and accelerate adaptive speciation. 448

It also needs to be highlighted that spatial self-structuring, by increasing the mating frequency among relatives, can sometimes result in inbreeding depression. Hence, an interesting extension of our model would be to examine possible costs and benefits of inbreeding, and to ascertain their impacts on the waiting times until adaptive speciation.

While we have focused our analyses here on competition for a unimodal resource, we 453 expect spatial self-structuring to promote adaptive speciation also in scenarios with bimodal 454 or multimodal resource distributions (e.g., Doebeli 1996; Thibert-Plante and Hendry 2011). 455 For non-unimodal resource distributions, the inhibiting effect of stabilizing selection on adap-456 tive diversification might be even weaker, and the resource distribution's intrinsic minima 457 may further facilitate the evolution of assortative mating. In future studies, it would therefore 458 be interesting to analyze interactions between the effects of non-unimodal resource distribu-459 tions and spatial self-structuring in models of adaptive speciation. 460

#### 461 **Conclusions**

The role of spatial self-structuring for adaptive speciation is complex. On the one hand, it de-462 lays adaptive speciation in populations with asexual reproduction (Fazalova and Dieckmann, 463 submitted). On the other hand, as demonstrated in this study, self-structuring facilitates and 464 accelerates speciation in sexually reproducing populations: this occurs by allowing for 465 assortative mating "for free," by reducing the effect of a large number of loci on the probabil-466 ity of strict assortative mating, and by cancelling out costs for assortative mating. Our results 467 suggest that no very high level of spatial self-structuring is necessary for fast speciation; in-468 termediate levels can suffice, and are sometimes even optimal for accelerating speciation in 469 sexual populations. 470

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#### 480 **Figure captions**

Figure 1. Comparison of initial spatial structure, evolutionary dynamics of ecological trait and mating trait, and resulting spatial structure in spatially well-mixed ( $\sigma_m = 0.08$ ; a,b,c) and spatially self-structured ( $\sigma_m = 0.01$ ; d,e,f) populations. In the snapshots of spatial structures, taken at times t = 50 and t = 500, the horizontal and vertical axes measure the spatial position of individuals, while the color scale indicates the ecological trait u. In the panels showing evolutionary dynamics, the color scale indicates the number of individuals within the shown phenotypic classes.

Figure 2. Dependence of the average waiting time until speciation on the dispersal radius  $\sigma_m$ and on the mating radius  $\sigma_p$ . Each cell shows an average over 100 replicate model runs. The thin gray contour lines are inferred from a polynomial approximation of the data. The thick black curve describes how the average size of spatial clusters varies with the dispersal radius <sup>492</sup>  $\sigma_{\rm m}$ . Dashed black curves correspond to one-third and one-fourth of this average cluster size. <sup>493</sup> The bottom row shows snapshots of spatial structures, for  $\sigma_{\rm p} = 0.1$  and values of  $\sigma_{\rm m}$  shown <sup>494</sup> along the main panel's horizontal axis.

Figure 3. (a) Dependence of the waiting time until speciation on the level of spatial selfstructuring for different numbers of loci determining the ecological trait. The shaded areas extend between the 40% and 60% percentiles of the distribution of waiting times until speciation for 100 replicate model runs, while the continuous curves show the corresponding medians. (b) Corresponding frequencies of mates, according to the difference between the phenotypic classes of mating partners. Other parameters:  $\sigma_p = 0.2$  and  $K_0 = 800$ .

Figure 4. (a) Dependence of the waiting time until speciation on the mating cost c for wellmixed ( $\sigma_m = 0.07$ ), intermediately self-structured ( $\sigma_m = 0.035$ ), and highly self-structured ( $\sigma_m = 0.01$ ) populations. The shaded areas extend between the 40% and 60% percentiles of the distribution of waiting times until speciation for 100 replicate model runs, while the continuous curves show the corresponding medians. (b) Corresponding evolution of the average mating trait a; time series end when reaching the average waiting time until speciation. Other parameters:  $l_e = 5$ .

#### 508 **Table**

Parameter	Description	Default value
b	Birth rate	1.0
m	Dispersal rate after birth	0.0
$\sigma_{ m c}$	Phenotypic competition width (= phenotypic standard de-	1.0
	viation of competition function)	
$\sigma_{ m s}$	Spatial competition radius (= spatial standard deviation of	0.2
	competition function)	
$\sigma_{ m K}$	Phenotypic resource width (= phenotypic standard devia-	2.0
	tion of resource distribution)	
$\sigma_{ m m}$	Dispersal radius (= spatial standard deviation of probability	0.01
	density for dispersal distance)	
$\sigma_{ m p}$	Mating radius (= spatial standard deviation of probability	0.1
	density for mate choice)	
$K_0$	Maximal carrying-capacity density	500

509 **Table 1.** Overview of model parameters.

μ	Mutation probability	0.002
с	Mating cost	0
l <sub>e</sub>	Number of loci determining ecological trait	15
l <sub>m</sub>	Number of loci determining mating trait	5

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