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Research Paper

The stellar rotation–activity relation for a sample of SuperWASP and ASAS-SN field stars

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Abstract

It is well established that late-type main-sequence (MS) stars display a relationship between X-ray activity and the Rossby number, *Ro*, the ratio of rotation period to the convective turnover time. This manifests itself as a saturated regime (where X-ray activity is constant) and an unsaturated regime (where X-ray activity anti-correlates with Rossby number). However, this relationship breaks down for the fastest rotators. We cross-correlated SuperWASP visually classified photometric light curves and All-Sky Automated Survey for Supernovae automatically classified photometric light curves with XMM-Newton X-ray observations to identify 3 178 stars displaying a photometrically defined rotational modulation in their light curve and corresponding X-ray observations. We fitted a power-law to characterise the rotation– activity relation of 900 MS stars. We identified that automatically classified rotationally modulated light curves are not as reliable as visually classified light curves for this work. We found a power-law index in the unsaturated regime of G- to M-type stars of $\beta = -1.84 \pm 0.18$ for the SuperWASP catalogue, in line with the canonical value of $\beta = -2$. We find evidence of supersaturation in the fastest rotating K-type stars, with a power-law index of $\beta_s = 1.42 \pm 0.26$.

Keywords: Stars: activity – Stars: starspots – Stars: variable – Stellar rotation

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1. Introduction

Every star has a magnetic field, and an important product of such a field is X-ray emission. The majority of X-ray emissions originate from active regions—concentrated areas of magnetic fields on the stellar surface such as star spots, collisions between the wind and circumstellar material (Parkin et al. [2009\)](#page-10-0), and small-scale wind shocks (Lucy & White [1980\)](#page-10-1).

In solar and late-type stars, the stellar magnetic field is generated in a magnetically confined plasma (Vaiana et al. [1981\)](#page-11-0). This plasma is driven by the stellar magnetic dynamo, which is in turn driven by the internal stellar differential rotation (Parker [1955;](#page-10-2) Wilson [1966;](#page-11-1) Kraft [1967\)](#page-10-3). This process was confirmed in the Sun through helioseismology (Duvall et al. [1984\)](#page-10-4).

Over the lifetime of a star, the rotation rate changes significantly. As a star ages and moves from the pre-main sequence (PMS) to the main sequence (MS), it experiences spin-down, the internal dynamo weakens, and as a result, the coronal Xray emission decreases (Wright et al. [2011\)](#page-11-2). Magnetic braking is active in PMS phase, but opposed by collapse/contraction which would speed up the star, and continues on the MS. Spin-down is driven primarily by mass loss through the magnetised stellar winds steadily transferring angular momentum away from the star. For MS stars, this decline in rotation can be approximated by Skumanich's law, $\Omega_e \propto t^{-1/2}$ (Skumanich [1972\)](#page-11-3), where Ω_e is the angular velocity of the star's equator, and *t* is the age of the star.

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Following this work, a relationship between rotation and activity was quantified by Pallavicini et al. [\(1981\)](#page-10-5), who found that X-ray luminosity scaled as $L_X \propto (v \sin i)^{1.9}$, providing the first evidence for the dynamo-induced nature of stellar coronal activity. Subsequently, Noyes et al. [\(1984\)](#page-10-6) combined these parameters into the Rossby number, $Ro = P_{rot}/\tau$, as the ratio of stellar rotation period, P_{rot} , to the convective turnover time, τ , of plasma covering a certain distance in the convective envelope, and which acts as a parameter for the stellar dynamo (Landin, Mendes, & Vaz [2010\)](#page-10-7).

Numerous studies of late-type MS stars (e.g., Pizzolato et al. [2003;](#page-10-8) Wright et al. [2011\)](#page-11-2) have characterised the relationship between stellar activity and rotation period, dividing the rotation activity into two main regimes for rotation periods of ∼1–10 d: the unsaturated and saturated regimes, and a third possible regime, the supersaturated regime.

In the unsaturated regime, for $Ro > 0.13$, the fractional X-ray luminosity, *Lx*/*Lbol*, anticorrelates with *Ro*. Wright et al. [\(2011\)](#page-11-2) find a power-law slope of $\beta \sim -2.7$ for F- to M-type MS stars. This strong rotation–activity relation indicates that the dynamo is responsible for stellar activity levels.

For fast rotating solar and late-type MS stars, the relationship is found to break down (Micela et al. [1985\)](#page-10-9), and saturation of *Lx*/*Lbol* occurs at *Ro* ∼ 0.13, regardless of spectral type (Vilhu [1984\)](#page-11-4), with L_x/L_{bol} saturating at $L_x/L_{bol} \sim 10^{-3}$. At this point, X-ray emission becomes a function of bolometric luminosity alone (Pizzolato et al. [2003\)](#page-10-8), i.e. the colour, mass, or radius of the star. The saturation threshold, Ro_{sat} , scales with the convective turnover time, τ , such that *Ro* is constant. The cause of saturation is still debated. Theories include centrifugal stripping of the corona at high rotation rates (Jardine & Unruh [1999\)](#page-10-10), saturation of the filling factor of

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active regions on the stellar surface, or a saturation of the dynamo itself (Vilhu [1984\)](#page-11-4).

Studies have found that nearly all fully convective, fast-rotating solar and late-type stars exhibit saturation of coronal X-rays (Wright et al. [2011\)](#page-11-2). The rotation period at which saturation occurs is longer for later spectral type stars, due to larger convective turnover times (Landin et al. [2010;](#page-10-7) Wright et al. [2011\)](#page-11-2). Whilst surprising, it has also been found that fully convective slow rotators show a solar-type rotation–activity relation (Wright et al. [2018\)](#page-11-5). Despite this, a comprehensive and satisfactory dynamo theory that explains both the saturated and unsaturated regimes is yet to be found (Weiss [2005;](#page-11-6) Brandenburg et al. [2011\)](#page-10-11).

In addition to these two regimes, studies have indicated that a third regime, supersaturation, may exist for the very fastest rotating MS stars. Supersaturation has been detected in PMS stars, M-dwarfs, and W UMa contact binaries (e.g., Randich [1998;](#page-10-12) Argiroffi et al. [2016;](#page-10-13) Jeffries et al. [2011;](#page-10-14) Stępień, Schmitt, & Voges [2001\)](#page-11-7). In this regime, the X-ray to bolometric luminosity ratio has been observed to decrease slightly below the saturation level (Jardine & Unruh [1999;](#page-10-10) Jardine [2004;](#page-10-15) Jeffries et al. [2011\)](#page-10-14). Although very scarcely observed, supersaturation has been seen to occur in young (< 100 Myr) G- and K-type stars in young clusters (Randich et al. [1996\)](#page-10-16). Whilst Argiroffi et al. [\(2016\)](#page-10-13) have found evidence for supersaturation in pre-main-sequence (PMS) stars, studies such as Wright et al. [\(2011\)](#page-11-2) have found no statistically significant evidence for supersaturation in MS stars, or any decline in luminosity ratio for fast rotators.

In this paper, we update the research by Norton et al. [\(2007\)](#page-10-17) with a new cross-correlation of the SuperWASP and XMM-Newton 4XMM-DR9 catalogues, which has detected 16 827 X-ray visible unique objects displaying variability, including 1 257 rotationally modulated variables, and 2 131 binaries and pulsators. Additionally, the All-Sky Automated Survey for Supernovae (ASAS-SN) Catalogue of Variable Stars has been cross-correlated against the XMM-Newton 4XMM-DR9 catalogue. These catalogues have been cross-correlated with Gaia-DR2, which contains the parallaxes and proper motions, as well as light curves for >550 000 variable sources.

2. Data reduction

The catalogue was primarily compiled from the SuperWASP archive, ASAS-SN Catalogue of Variable Stars, 4XMM-DR9 catalogue, and Gaia-DR2 catalogue, selecting only unique objects displaying a rotational modulation with photometric, X-ray, and parallax data. Here we describe the catalogues used in crosscorrelation, the data reduction, and analysis.

2.1. SuperWASP photometric catalogue

The Wide Angle Search for Planets, SuperWASP, is the most successful ground-based search for transiting exoplanets (Pollacco et al. [2006\)](#page-10-18), having discovered ∼200 hot Jupiters since 2004. The entire sky has been surveyed, excluding the Galactic Plane where individual objects cannot be resolved due to the large pixel scale of the telescope. Not only has it discovered numerous exoplanets but it has also produced an archive of more than 30 million light curves.

SuperWASP is made up of two identical robotic observatories and a consortium of eight academic institutions. SuperWASP-North is located on the island of La Palma in the Canaries,

Figure 1. Example of a light curve of a rotator with a period of 16 019 s (∼0.19 d) in the SuperWASP archive.

and SuperWASP-South is situated with the South African Astronomical Observatory (SAAO), in South Africa. Each observatory consists of eight wide-angle cameras giving each camera a 7.8×7.8 square degrees field of view (FoV), giving a total of 500 square degrees of sky coverage. The large pixel size of 16.7 arcsec per pixel means that whilst all-sky coverage can be completed, SuperWASP avoided observing the Galactic Plane as it could not resolve individual stars within this dense area of sky (Pollacco et al. [2006\)](#page-10-18). SuperWASP data provide a high cadence, long baseline allsky archive, away from the Galactic Plane, for stars between about $V = 8 - 15$ to investigate stellar variability.

The *SuperWASP periodicity* catalogue is the result of a new search by Norton [\(2018\)](#page-10-19) for periodic variability in the SuperWASP archive of ∼ 31 million light curves. The period searching routine used CLEANed power spectrum analysis and a phase dispersion minimisation folding analysis. This routine detected ∼8 million potential periods in ∼3 million objects, with a sensitivity of between ∼1 h and ∼1 yr. However, many systematic effects occurred in the period search of SuperWASP light curves, resulting in the detection of periods of a lunar month, sidereal day, or integer multiples, and fractions of a day (i.e. 1/2, 1/3, 1/4, etc.). As a result of these systematic effects, any object 'flagged' as having a period close to these values was rejected from this work. All 'unflagged' objects are the subject of a citizen science Zooniverse project aiming to classify 1 569 061 periods in 767 199 objects, resulting in the construction of catalogues of types of stellar variable (Norton [2018\)](#page-10-19). The periods in this catalogue have an uncertainty of ∼±0.1%.

The *SuperWASP periodicity* catalogue also contains duplicated objects, arising from the detection of multiple periods for a single object. The most likely period for each object was found through identifying the most significant period and any duplicates were removed. Any remaining duplicated objects were removed by performing an internal positional cross-correlation, removing objects within a 2 arcmin radius of each other $(> 4$ times the photometric aperture radius, 34 arcsec).

The remaining 767 199 (∼2.5% of objects in SuperWASP archive) genuine objects with detectable periodic variability on timescales from hours to years are ready to be cross-correlated with X-ray data. [Figure 1](#page-2-0) gives an example of the light curve of a rotationally modulated star in the SuperWASP archive.

Figure 2. Example of a light curve of a rotator with a period of 191 731 s (∼2.22 d) in the ASAS-SN variable stars database.

2.2. ASAS-SN photometric catalogue

The ASAS-SN is an optical survey which has monitored the entire sky since 2014 (Jayasinghe et al. [2019\)](#page-10-20). ASAS-SN is currently composed of 24 telescopes based in Hawaii, Chile, Texas, South Africa, and China. Each camera has a FoV of 4.5 deg^2 and a pixel scale of 8 arcsec. Despite the relatively large pixel scale, the typical astrometric error is ∼1 arcsec. ASAS-SN uses APASS (Henden et al. [2015\)](#page-10-21) magnitudes which tend to deviate from the V-band ASAS-SN magnitudes for $V > 14$ due to blended sources where multiple APASS sources are detected by a single ASAS-SN pixel.

Like SuperWASP, this survey did not aim to study stellar variability, instead focusing on bright supernovae, but given the cadence of \sim 2–3 d, and a limiting magnitude of V ≤ 17 mag, ASAS-SN has been able to study > 50 million bright sources. Light curves of variable stars are classified using a random forest classifier and verified against other catalogues, as described in Jayasinghe et al. [\(2018\)](#page-10-22). Cross-correlated with other cataglogues, e.g. NOMAD, 99% of ASAS-SN variables detected are within 5.2 arcsec of a previously catalogued star. The ASAS-SN Catalogue of Variable Stars contains 666 502 light curves, of which 90 712 belong to rotational variables. Each object in the ASAS-SN Catalogue of Variable Stars contains information about the variability type, classification probability, period, and magnitude, amongst other values. For this work, we selected stars with a classification probability of >0.75 .

[Figure 2](#page-3-0) gives an example of the light curve of a rotationally modulated star in the ASAS-SN Catalogue of Variable Stars.

2.3. XMM-Newton X-ray catalogue

The 4XMM-DR9 catalogue contains detections of 550 124 unique X-ray sources from 11 204 observations made by the XMM-Newton EPIC cameras covering 1 089 square degrees. The detections cover the energy range 0.2–12 keV and span 19 yr between 2000 February 3 and 2019 February 26. This work uses the broad energy band (0.2–4.5 keV).

Low-mass stellar X-ray sources are known to show high levels of variability due to magnetic flares (Caramazza et al. [2007\)](#page-10-23) and rotational modulation. Bright flares can significantly increase the X-ray flux from a source over the course of a short observation. Short-lived increases in X-ray flux should be removed through multiple observations of the same source; however, the majority (∼80%) of objects in the 4XMM-DR9 catalogue contain only one detection of the source, with only ∼41% of these objects having an uncertainty in the soft X-ray band of \leq 20% in flux. Approximately 71% have an uncertainty of \leq 30% in flux. We expect this to be one of the most significant sources of uncertainty in our work.

As with the *SuperWASP periodicity* catalogue, possible duplicated objects were removed by performing an internal positional cross-correlation, removing objects within a 24 arcsec radius of each other (four times the uncertainty in the EPIC extent radius). The remaining objects are assumed to be unique.

The 4XMM-DR9 catalogue contains a summary flag for each source, from 0 to 11. For example, a flag of 0 indicates a 'good' source, a flag of 1 indicates that parameters may be affected, a flag of 2 indicates a possibly spurious source, and a flag of 3 indicates that the source is located in an area where there may be a spurious detection. In total, 95.7% of the sources in our catalogue have a flag \leq 1. All unique sources with a flag \geq 2 are removed from the catalogue.

2.4. Additional tables

For the calculation of bolometric luminosity, photometric colour and parallax are required. The majority of previous studies of the rotation–activity relation have used either the $B - V$ or $V - K_s$ colour as various proxies, i.e. for effective temperature. B, V, R, J, H, K photometric magnitudes were taken from the Two Micron All Sky Survey (2MASS) (Skrutskie et al. [2006\)](#page-11-8) and NOMAD (Zacharias et al. [2004\)](#page-11-9) catalogues, supplemented by USNOB1.0 (Monet et al. [2003\)](#page-10-24), APASS (Henden et al. [2015\)](#page-10-21), and GCS2.3 (Lasker et al. [2008\)](#page-10-25), and used to derive $V - K_s$ for all stars. $V - K_s$ was used as a proxy for effective temperature and used to derive bolometric corrections. For each star, estimated spectral types were based on Mamajek et al. [\(2015\)](#page-10-26).

The conversion of observed to absolute magnitude requires stellar distance. Due to well-known problems with the use of non-corrected Gaia-DR2 parallaxes for distance calculation, the Bailer-Jones et al. [\(2018\)](#page-10-27) catalogue was used, which provides corrected distances. A 10 arcsec cross-correlation was used between the Bailer-Jones et al. [\(2018\)](#page-10-27) catalogue and *SuperWASP periodicity* catalogue and ASAS-SN Catalogue of Variable Stars. Both the bolometric luminosity and the X-ray luminosity scale with d^2 , hence the distance value cancels in the bolometric flux ratio. In this work, distances are instead used to identify MS stars and correct for interstellar reddening.

Such a spatial cross-correlation is likely to pick up non-stellar and non-rotational stellar objects in the process; hence, the final cross-correlation is a 10 arcsec search of SIMBAD tables to identify such objects. Non-stellar and non-rotational stellar objects were removed based on the SIMBAD object type. The catalogue V magnitudes and the observed V magnitudes of the remaining objects were plotted, as shown in [Figure 3,](#page-4-0) and objects with a difference in V magnitude of > 0.85 (or 1 σ) were removed.

2.5. Cross-correlation

Through a 2 arcmin cross-correlation of unique objects in both *SuperWASP periodicity* and 4XMM-DR9 objects using TOPCAT,

Figure 3. V magnitude (observed) against V magnitude (catalogue). Stars with a V magnitude difference of greater than 1σ are removed from the catalogue.

39 367 possibly coincident objects with both periodic photometric variability and an X-ray flux were identified. The large crosscorrelation radius of 2 arcmin between the SuperWASP and 4XMM-DR9 catalogues is due to the large (34 arcsec) photometric aperture radius of SuperWASP and accounts for ∼4 times this radius.

Of these, 16 827 were flagged as not having a period close to 1 d. Phase-folded light curves were plotted for 16 827 objects and were visually classified by the authors. Totally, 12 509 were rejected as not convincingly variable, 1 232 displayed rotational modulation, and 2 131 were categorised as binaries and pulsators. Of the 1 257 objects, 990 had corresponding colours and positive, real Gaia-DR2 parallaxes in the Bailer-Jones et al. [\(2018\)](#page-10-27) catalogue. Of these 990 objects, 106 were found to be non-stellar or non-rotational stellar objects, and 303 were found to be giant or supergiant stars. Such stars do not follow a rotation–activity relation and are known to experience a sharp decrease in X-ray emission at spectral type K1. Giant and supergiant stars were identified using stellar luminosity by spectral class from Cox [\(2000\)](#page-10-28). Removing giant stars from the catalogue leaves 581 SuperWASP stars.

The ASAS-SN rotational variable stars were cross-correlated with 4XMM-DR9 with a 10 arcsec cross-correlation radius, giving 1 921 objects. Of these, 75 appeared in the SuperWASP catalogue and were removed as duplicates. For objects which occurred in both catalogues with a period detection, 72% of the objects had a period difference of <2%, and 80% agreed to within <10%. For objects with periods which differed by $>$ 2%, each was assessed by eye to determine which was the most likely true period. Of the 1 846 remaining objects, 882 contain information on both period and colour. Of these, 786 have an ASAS-SN classification probability of > 0.75 . The ASAS-SN Catalogue of Variable Stars has already been cross-correlated with catalogues of variable stars (e.g. VSX and GCVS), and as such, all 786 objects are MS stars. About 115 SuperWASP and ASAS-SN objects with observed to catalogue V magnitude difference of $> 1\sigma$ were removed. Finally, all ASAS-SN stars were visually inspected, and 173 stars not displaying a clear rotational modulation were discarded. Combined, this gives a full catalogue of 1 079 stars from the SuperWASP and ASAS-SN catalogues.

Figure 4. The *^V* [−] *Ks* , *^J* [−] *^H* colour–colour plot of 900 stars in the full catalogue. The black line indicates the locus of the zero age MS for zero reddening.

2.6. Positional coincidence

SuperWASP has a large pixel size of 13.7 arcsec pixel⁻¹. When combined with the 2.5 pixel extraction aperture for photometry, the error radius is 34 arcsec. Although XMM-Newton sources have low positional uncertainties, there is still the possibility of chance positional coincidences between the photometric data and X-ray sources.

The SuperWASP all-sky survey is composed of 2×8 cameras in the Northern and Southern hemisphere, covering 7712 square degrees. We have light curves of 3 091 808 unique objects with detectable photometric periods from the *SuperWASP periodicity* catalogue. Therefore, the mean linear separation between nearest neighbours is 180 arcsec for SuperWASP objects. The 4XMM-DR9 catalogue contains 550 124 unique X-ray sources covering 1089 square degrees, overlapping the SuperWASP sky area. The mean error radius of XMM-Newton positions is <2 arcsec. This corresponds to a 0.6% chance of an XMM-Newton source and a SuperWASP source coinciding at random. We find 39 367 positional matches (of which, we use 581 to characterise the rotation– activity relation), rather than ∼2316 matches expected as a result of chance, suggesting that (39 367 − 2 316)/39 367 = 94% of the positional coincidences are the result of genuine X-ray emissions from SuperWASP sources.

Using the same method, the mean linear separation between nearest neighbours for ASAS-SN sources is 103 arcsec, and a 2% chance that XMM-Newton and ASAS-SN sources coincide at random. We find that 80% of the positional coincidences are the result of genuine X-ray emissions from ASAS-SN sources.

2.7. Colours and reddening

[Figure 4](#page-4-1) shows the $V - K_s$ vs. $J - H$ colour–colour plot of the catalogue, and the solid black line shows the locus of the MS for zero reddening. Extinction will move the line upwards in *J* − *H* and right in $V - K_s$ according to Wegner [\(1994\)](#page-11-10). There is a very slight offset shifting $J - H$ upwards, which may be due to the nonstandard V magnitude calculated by SuperWASP (Norton et al. [2007\)](#page-10-17); however, since the majority of the objects are close to the zero-reddening MS, all objects are relatively close-by.

2.8. Bolometric flux ratio

To calculate bolometric luminosities, all targets were converted from observational magnitudes to absolute magnitudes and extinction corrected.

$$
M_{\nu} = m - 5 \log \left(\frac{d}{10} \right) + A,\tag{1}
$$

where $A = 3.2[E(B - V)]$ and distance is measured in parsecs.

The extinction for each star was synthesised using the Binary and Stellar Evolution and Population Synthesis (BiSEPS) implementation of extinction given by Drimmel et al. [\(2003\)](#page-10-29), using Bailer-Jones et al. [\(2018\)](#page-10-27) Gaia-DR2 distances.

Bolometric corrections were calculated from $V - K_s$ colour and Bailer-Jones et al. [\(2018\)](#page-10-27) Gaia-DR2 distances, allowing for the calculation of bolometric luminosities using $M_{bol} = BC_v - M_v$. The bolometric luminosity was calculated using

$$
L_{bol} = L_0 \times 10^{-0.4M_{bol}},\tag{2}
$$

where L_0 is the zero point luminosity 3.0128×10^{28} W. X-ray fluxes were converted to X-ray luminosities using soft X-rays and Gaia-DR2 Bailer-Jones et al. [\(2018\)](#page-10-27) distances using $L_x = 4\pi D^2 F_x$. Finally, the X-ray-to-bolometric luminosity ratios, $R_x = L_x/L_{bol}$, were determined.

2.9. Rossby number

We calculated the convective turnover time, τ , using the $V - K_s$ colour relation derived by Wright et al. [\(2018\)](#page-11-5). Previous empirically derived relationships have been found, e.g. Pizzolato et al. [\(2003\)](#page-10-8) and Wright et al. [\(2011\)](#page-11-2); however, these relationships have small $V - K_s$ ranges. Wright et al. [\(2018\)](#page-11-5) extended this relationship, and as such, it is well constrained for $1.1 < V - K_s < 7.0$. It is worth noting that to derive this empirical form of the relation, Wright et al. [\(2018\)](#page-11-5) assume a rotation–activity relation as the input; hence, it might be reasonable to assume that the output will be self-consistent and will show a rotation–activity relation in line with canonical values. This relationship has the form:

$$
\log \tau = 0.64(\pm_{0.12}^{0.10}) + 0.25(\pm_{0.07}^{0.08})[V - K_s], \tag{3}
$$

where τ is the convective turnover time. Rossby numbers, $Ro =$ P_{rot}/τ , were calculated for all targets.

2.10. The full catalogue

Having characterised *Ro* and *Lx*/*Lbol*, cuts were made to the catalogue of 1 079 stars to make it suitable for use for the rotation– activity relation. Any stars with a period of \geq 50 d were removed, since long period photometric variability is difficult to correctly define for long periods. Late-type stars with a bolometric luminosity of $L_{bol} \geq 10L_{\odot}$ were discarded as giants. The 4XMM-DR9 variability flag, *VAR*_*FLAG*, was used to remove the 34 GKM-type sources detected as variable.

The full catalogue contains 900X-ray visible unique objects displaying rotational modulation in their photometric variability. [Figures 5](#page-5-0) and [6](#page-5-1) show the distribution of period and $V - K_s$ colour in the full catalogue. The catalogue is concentrated around objects with a rotation period of 3–10 d. Like the ASAS-SN Catalogue of Variable Stars, the *SuperWASP periodicity catalogue* reports the rotation period derived for each target. The periods given in this catalogue are therefore the 'best guess' rotation period and may

Figure 5. The period distribution of 900 stars in the full catalogue coincident with 4XMM-Newton sources.

Figure 6. The *^V* [−] *Ks* colour distribution of 900 stars in the full catalogue coincident with 4XMM-Newton sources.

not be the actual rotation periods of the stars. However, given that both the ASAS-SN Catalogue of Variable Stars and the *SuperWASP periodicity catalogue* have independently derived almost identical rotation periods through different methods, we can be confident enough in their accuracy to use this new catalogue to probe the rotation–activity relation. [Tables 1](#page-5-2) and [2](#page-5-3) show a sample of the full catalogue. Splitting the catalogue into spectral types based on *V* − K_s colour and tables by Mamajek et al. [\(2015\)](#page-10-26) gives 431 O-A-type, 33 F-type, and 402 GKM-type stars.

The spatial distribution of the full catalogue is shown in [Figure 7,](#page-8-0) indicating SuperWASP stars lying away from the Galactic Plane and ASAS-SN stars lying mostly along the Galactic Plane.

The columns of the tables are as follows: 1. IAUNAME: The XMM-Newton identifier in the form $4XMM$ Ihhmmss.ss $+$ ddmmss.s; with the position encoded in this identifier. 2. WASP ID: The SuperWASP identifier in the form 1SWASP $J\$ h\mmss.ss + ddmmss.s; the position encoded in this identifier is identical to the position of the corresponding object in the USNO B1 catalogue, or ASAS-SN ID: The ASAS-SN identifying in the form ASASSN-V Jhhmmss.ss + ddmmss.s. 3. Spectral Type: Spectral type taken from Mamajek et al. [\(2015\)](#page-10-26) based on Table 1. Subset of the 180 G- to M-type SuperWASP objects from the full catalogue containing 900 X-ray visible unique objects displaying rotational modulation in their photometric variability.

V − *K*_c colour. 4. Period: The SuperWASP photometric period in days identified by the SuperWASP periodicity period search, or Period: The ASAS-SN photometric period in days. 5. V magnitude: V is the mean SuperWASP magnitude defined as $-2.5\log 10(\frac{F}{10^6})$ where F is the mean SuperWASP flux in microVegas—a pseudo-V magnitude which is comparable to the Tycho V magnitude, or V magnitude: ASAS-SN V magnitude. 6. $V - K$: $V - K$ calculated using 2MASS and USNOB1 catalogue magnitudes. 7. Distance: Distance in parsec taken from Bailer-Jones et al. [\(2018\)](#page-10-27). 8. log Ro: Rossby number calculated using relationship derived in Wright et al. [\(2018\)](#page-11-5). 9. log *Rx*: Logarithm of the ratio of X-ray to bolometric luminosity.

3. Characterising the rotation–activity relation

To characterise the rotation–activity relation for each spectral type, we fit a power-law function to a plot of $\log (L_x/L_{bol})$ to $\log R_o$ for the unsaturated and supersaturated regimes, where applicable, and found a mean for the saturated regime. The saturation point, Ro_{sat} is initially taken to be $Ro_{sat} = 0.13$ based on canonical values e.g. Wright et al. [\(2011\)](#page-11-2). Points for supersaturation fit are based on literature values. The fits for each regime and spectral type are based on [Equation](#page-7-0) [\(4\)](#page-7-0) and an initial fit using OLS was done to identify the saturation point as $Ro_{sat} = 0.14 \pm 0.03$. Each regime's fit is improved using the Python package *emcee*, a Markov Table 2. Subset of the 222 G- to M-type ASAS-SN objects from the full catalogue containing 900 X-ray visible unique objects displaying rotational modulation in their photometric variability.

chain Monte Carlo implementation of the affine-invariant ensemble sampler created by Foreman-Mackey et al. [\(2013\)](#page-10-30), which takes both uncertainties in *Ro* and (L_x/L_{bol}) into account.

The commonly used two-part power-law for the unsaturated and saturated regime (e.g. Pizzolato et al. [2003;](#page-10-8) Wright et al. [2011;](#page-11-2) Wright et al. [2018\)](#page-11-5) has the form:

$$
\frac{L_x}{L_{bol}} = \begin{cases} CRo^{\beta} & \text{if } Ro > Ro_{sat} \\ \left(\frac{L_x}{L_{bol}}\right)_{sat} & \text{if } Ro \le Ro_{sat} \end{cases} . \tag{4}
$$

It is assumed that the supersaturated regime will have a similar, but positive, power-law form, β*s*.

4. Results

Plots of the Rossby number, $Ro = P_{rot}/\tau$, against bolometric flux ratio, *Lx*/*Lbol*, for for the full SuperWASP and ASAS-SN catalogue are shown in [Figures 8,](#page-8-1) [9](#page-8-2) and [10.](#page-9-0) O-A-type stars are known to not display the rotation–activity relation, as shown in [Figure 8.](#page-8-1) A-type stars are typically X-ray dark, whereas O- and B-type stars generate X-rays via wind shocks or for binaries, shocks between colliding winds. Any X-ray emission from A-type stars is most likely the emission from an unresolved companion star (Schröder & Schmitt [2007\)](#page-10-31).

The full catalogue was separated into the component ASAS-SN and SuperWASP catalogues and fitted separately, shown in

Figure 7. The spatial distribution of the 900 objects in the full catalogue.

Figure 8. The 431 OBA-type stars in the catalogue do not display the rotation–activity relation.

[Figures 9](#page-8-2) and [10.](#page-9-0) This demonstrates the significant difference between each subset of stars in the full catalogue. A fit to the SuperWASP catalogue shows the classical two-part power-law fit of unsaturated and saturated regime and a third supersaturated regime, whereas the fitting to the ASAS-SN catalogue is extremely unconvincing and is shown purely to demonstrate this fact. The breakdown of fitting parameters for each regime and catalogue subset are shown in [Table 3.](#page-9-1)

The unsaturated regime typically lies between 0.10 < *Ro* < 2.00. We find the unsaturated regime for our catalogue to be in the range 0.14 < *Ro* < 2.00. In the unsaturated regime, there is an anticorrelation between the Rossby number, *Ro*, and X-ray luminosity ratio, *Lx*/*Lbol*. We used 89 SuperWASP G- to M-type stars to fit find a power-law fit of $\beta = -1.84 \pm 0.18$, matching the canonical value $\beta = -2$, within uncertainties.

The saturated regime exists for fast rotating solar and latetype stars with 0.03 < *Ro* < 0.14, independent of spectral type. The SuperWASP subset contains 31 saturated stars. Previous studies have found the value of the saturation point to be between *Rosat* ∼ 0.08 (Marsden, Carter, & Donati [2009\)](#page-10-32) and *Rosat* ∼ 0.16 ±

Figure 9. Fractional X-ray luminosity, *Lx*/*Lbol*, plotted against the Rossby number, *Ro*, for 192 G- to M-type SuperWASP stars. Regime thresholds are as follows: supersaturated regime (0.03 > *Ro*), saturated regime (0.03 < *Ro* < 0.14), and unsaturated regime (0.14 < *Ro* < 2.00). GKM-type SuperWASP (full black line) and ASAS-SN catalogues (dashed black line).

0.02 (Wright et al. [2011\)](#page-11-2). We find the value of $Ro_{sat} = 0.14 \pm 0.03$ and find a mean saturation of $log (L_x/L_{bol}) = -3.14$.

The supersaturated regime occurs for the very fastest rotating stars with $Ro < 0.03$. For the fastest rotating stars, L_x/L_{bol} has been observed to decrease below the saturation level. Our SuperWASP G- to M-type sample clearly displays evidence of a supersaturated regime, with a power-law slope fit of $\beta_s = 1.42 \pm 0.26$, with 60 stars in this subset.

The scatter in L_x/L_{bol} in the saturated regime is likely to arise from a number of factors: X-ray luminosity varying over a stellar cycle [sometimes up to an order of magnitude in our Sun (Peres et al. [2000\)](#page-10-33)], and with a significant portion of X-ray sources having only one detection, varying starspot coverage may change the measured activity of the star.

In $V - K_s$ space, the stars used to characterise the rotation– activity relation are distributed across the range $1.1 \leq V -$

Table 3. Parameters for the GKM-type regime, separated by catalogues and period ranges. nWasp and nASAS-SN indicate the number of stars in each regime.

Regime	nWASP	WASP	nASAS-SN	ASAS-SN
Supersaturated (β)	60	$1.42 + 0.22$	21	$0.43 + 0.24$
Saturated (Rx)	31	-3.14	76	-2.81
Unsaturated (β_s)	89	$-1.84 + 0.18$	125	-0.33 ± 0.11

Figure 10. Fractional X-ray luminosity, L_x/L_{bol} , plotted against the Rossby number, *Ro*, for 244 G- to M-type ASAS-SN stars. Regime thresholds are as follows: supersaturated regime (0.03 > *Ro*), saturated regime (0.03 < *Ro* < 0.14), and unsaturated regime (0.14 < *Ro* < 2.00).

 $K_s \leq 5.7$, with K-type stars dominating. Uncertainties in V magnitudes are generally small (∼3%) compared to the measured X-ray fluxes, which have a typical uncertainty of ∼20%. Distance uncertainties are also typically small (∼5%). As such, in *Lx*/*Lbol*, the X-ray uncertainty dominates. The rotation periods for the SuperWASP archive, *Prot*, are derived empirically, and the typical uncertainty is ∼0.1%. It is assumed that ASAS-SN periods have an equivalent uncertainty. Additionally, the SuperWASP subset has marginally smaller uncertainties, with a mean uncertainty of \pm 6.05 × 10⁻⁵ in *L_x*/*L*_{bol} compared to \pm 9.88 × 10⁻⁵ for the ASAS-SN subset. Similarly, in *Ro*, the SuperWASP catalogue has a mean uncertainty of ± 0.06 , whereas the ASAS-SN catalogue has a mean uncertainty of ± 0.15 .

5. Discussion

Somewhat unexpectedly, the ASAS-SN and SuperWASP catalogues show very different results. Notably, the SuperWASP catalogue shows convincing evidence for the unsaturated and supersaturated regimes, and with a higher saturation point, whereas the ASAS-SN catalogue shows no convincing evidence for the unsaturated or supersaturated regimes.

It is likely even after cleaning the data, both subsets still have some level of contamination. Jayasinghe et al. [\(2018\)](#page-10-22) state that rotational variables are 'usually the most difficult to precisely classify', and as such rotational variables in the ASAS-SN Catalogue of Variable Stars and the SuperWASP periodicity catalogue may be unclassified binaries or low amplitude Cepheids, especially for fast rotating objects with periods of ≤ 1 d, or for longer period objects.

Figure 11. The *^V* [−] *Ks* colour distribution of GKM-type stars.

Figure 12. The period distribution of GKM-type stars.

Jayasinghe et al. [\(2018\)](#page-10-22) note that the majority of rotational variables in the catalogue overlap with pulsators in colour and period space. Without spectroscopic measurements for this study, these light curves can still be open to interpretation. However, since both catalogues have been classified by eye using the same method (for initial selection of the SuperWASP objects, and for final verification of the ASAS-SN objects), contamination alone cannot account for the inter-catalogue variation.

Investigating the differences between the two catalogues shows that the data sets show similar distributions of X-ray flux; however, the ASAS-SN catalogue shows a distribution towards redder, fainter objects, shown in [Figure 11.](#page-9-2) This is unsurprising, since the limiting magnitude of ASAS-SN is $V = 17$ mag, whereas SuperWASP is $V = 15$ mag; however, we would still expect such objects to follow the relationship.

[Figure 12](#page-9-3) shows that the ASAS-SN catalogue contains no GKM-type objects with a period ≤ 0.3 d, whereas almost 25% of the SuperWASP catalogue contains objects within that period range. All flagged SuperWASP objects were removed from the catalogue to avoid the inclusion of spurious periods; hence, there is a lack of SuperWASP objects with a period of close to 1 d. The SuperWASP data set includes a larger proportion of short period objects, made very clear by [Figure 8](#page-8-1) which shows a significant difference between Ro, and hence period range, of the two catalogues. As a test, removing all ASAS-SN objects with a period of ≥ 10 d

does improve the power-law fit slightly, to $\beta = -0.87 \pm 0.18$. It is likely that the detection and automated classification methods used by ASAS-SN struggles with the period detection and classification of faint, long period rotational objects. We can find no other conclusive reason why the ASAS-SN sample appears to not follow the rotation–activity relation.

It is likely that misclassification of rotationally modulated objects is also the primary reason for the small but noticeable difference for the unsaturated regime power-law fit between the canonical value of $\beta = -2$ and for the SuperWASP value, which finds $\beta = -1.84 \pm 0.18$. Another, less likely possibility is that field stars may follow a marginally different rotation–activity relation than stars in clusters. Stars in clusters will have a similar age, metallicity, composition, and formation and would experience magnetic braking and activity decline at similar rates, whereas field stars may not, however, this is beyond the scope of this study.

6. Conclusion

The study of the rotation–activity relation has so far been limited by the availability of deep observations over long baselines and accuracy of stellar rotation periods. We sought to tackle this through the use of the SuperWASP archive, which contains ∼10 yr of high-cadence, long baseline observations, and a period search of the resulting > 30 million light curves, and the automatically classified light curves in the ASAS-SN Catalogue of Variable Stars.

Through cross-correlations of SuperWASP and ASAS-SN photometric data and XMM-Newton X-ray data, we have updated the work by Norton et al. [\(2007\)](#page-10-17), and we have characterised 900 rotationally modulated stars with photometric rotation periods from the *SuperWASP periodicity* period search and ASAS-SN Catalogue of Variable Stars, of which 402 late-type MS field stars are used to study the rotation–activity relation.

We find that while the ASAS-SN Catalogue of Variable stars provides a large catalogue of stars classified as rotationally modulated, using the catalogue without visually inspecting each light curve means that automatically classified data cannot be used to characterise the rotation–activity relation, and even after visual inspection, there may still be issues with the period detection for long period rotational objects in ASAS-SN. Having classified the SuperWASP light curves by eye, we find that late-type stars follow the rotation–activity relation, and the slope of the power-law fit of $\beta = -1.84 \pm 0.18$ is in line with the canonical value of $\beta = -2$. We also find a third supersaturation regime for the fastest rotating stars, and fit a power-law slope of $\beta_s = 1.42 \pm 0.26$. We suggest that the inclusion of indistinguishable non-rotational objects is the main reason for the lower β fit.

Since the rotation–activity relation is believed to be a proxy for the stellar magnetic dynamo, and most dynamo models cannot yet reliably predict a correlation between rotation and activity indicators such as X-ray activity, all-sky observational studies prove vital for understanding the stellar dynamo; however, we advise that automatically classified rotationally modulated light curves are first thoroughly vetted by eye prior to avoid contamination of the sample.

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