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Observable heavy Higgs dark matter

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ABSTRACT: Dark Matter (DM), arising from an Inert Higgs Doublet, may either be light, below the W mass, or heavy, above about 525 GeV. While the light region may soon be excluded, the heavy region is known to be very difficult to probe with either Direct Detection (DD) experiments or the Large Hadron Collider (LHC). We show that adding a second Inert Higgs Doublet helps to make the heavy DM region accessible to both DD and the LHC, by either increasing its couplings to the observed Higgs boson, or lowering its mass to $360 \,\mathrm{GeV} \lesssim m_{\mathrm{DM}}$, or both.

KEYWORDS: Higgs Physics, Beyond Standard Model, Cosmology of Theories beyond the SM, Discrete and Finite Symmetries

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1 Introduction

The long-awaited Higgs boson, with a mass of $m_h \approx 125\,\mathrm{GeV}$, was famously discovered in 2012 by the ATLAS and CMS experiments at the CERN Large Hadron Collider (LHC) [1, 2]. Although its properties are in accordance with the predictions of the Standard Model (SM), including Electro-Weak (EW) precision data, it remains an intruiging

possibility that the observed Higgs boson, denoted here as h, may just be one member of an extended Higgs sector. A good motivation for the latter is the idea that it might provide a candidate for Cold Dark Matter (CDM).

Although the nature of Dark Matter (DM) is not yet known, according to the Standard Cosmological Lambda-CDM Model [3] it should be a particle which is *stable* on cosmological time scales, *cold*, i.e., non-relativistic at the onset of galaxy formation, *non-baryonic*, *neutral* and *weakly interacting*. Various candidates for such a state exist in the literature, the most well-studied being the Weakly Interacting Massive Particles (WIMPs) [4–6], with masses between a few GeV and a few TeV. Any such WIMP candidate must be cosmologically stable, usually due to the conservation of a discrete symmetry, and must freeze-out (i.e., drop out of thermal equilibrium) to yield the observed relic density [3]:

$$\Omega_{\rm DM}h^2 = 0.1199 \pm 0.0027. \tag{1.1}$$

It is clear that the SM Higgs sector cannot provide a WIMP candidate, since its Higgs boson is unstable. However, it was suggested some time ago that the Higgs sector could be extended by the addition of an extra doublet, which may not develop a Vacuum Expectation Value (VEV), leaving a discrete Z_2 symmetry unbroken [7]. Independently, it was later shown that an extra scalar doublet with zero VEV, odd under a discrete Z_2 symmetry, could yield monojets at hadron colliders while being constrained by DM considerations (the first time to our knowledge that any connection with hadron colliders or DM was made) [8]. This possibility, which became known as the Inert Doublet Model (IDM), has been studied extensively for the last few years (see, e.g., [9–11]). Since the IDM involves 1 Inert Doublet plus 1 active Higgs Doublet, we shall also refer to it henceforth as the I(1+1)HDM.

In the IDM, aka the I(1+1)HDM, one extra spin-zero $SU(2)_L$ doublet with the same quantum numbers as the SM Higgs doublet is introduced. One of the possible vacuum states in this model involves the first doublet acquiring a VEV, henceforth called the *active doublet*, while the second doublet does not develop a VEV and is referred to as the *inert doublet* since it does not take part in EW Symmetry Breaking (EWSB). Since this doublet does not couple to fermions and it is by construction the only Z_2 -odd field in the model, it provides a stable DM candidate, namely the lightest state among scalar and pseudo-scalar Z_2 -odd particles.

The I(1+1)HDM remains a viable model for a scalar DM candidate, being in agreement with current experimental constraints. As of now, there are two regions of DM masses where one can expect viable solutions: a low DM mass region, $53 \text{ GeV} \lesssim m_{\rm DM} \lesssim m_W$ and a heavy DM mass region, $m_{\rm DM} \gtrsim 525 \text{ GeV}$. The most recent experimental data, both from direct detection experiments and from the LHC, has reduced the viable parameter space in the low mass region [12, 13]. In the heavy mass region, however, where the sensitivity of DM direct detection experiments decreases significantly with increasing DM mass, the DM candidate may escape possible detection in this model.

¹Since the Planck 2015 results quotes various results for $\Omega_{\rm DM}h^2$, depending on which spectra such as TT, TE and EE are used, we prefer to use here the Planck 2013 result whose error encompasses all of them.

In a recent paper [14] we studied DM in a model with 2 inert Higgs plus 1 active Higgs doublet, which we referred to as the I(2+1)HDM. In particular we focused on the region of parameter space of the I(2+1)HDM where the DM candidate, the lightest inert scalar, is in the light mass region ($m_{\rm DM} \lesssim m_W$). We found that the extended scalar sector can relax the exclusion limits from direct detection experiments, providing a viable DM candidate in a region of parameter space which would be excluded in the I(1+1)HDM. In this paper we study the heavy DM mass region of the I(2+1)HDM. We show that heavy Higgs DM in this model becomes more readily observable as a result of either lowering the DM mass to $360~{\rm GeV} \lesssim m_{\rm DM}$, or increasing the DM-Higgs coupling, or both, while always maintaining the DM relic density within the required region.

The layout of the remainder of this paper is as follows. In section 2 we review the I(2+1)HDM and focus on a simplified version of the model based on a smaller number of parameters. In section 3 we calculate the relic density in the I(2+1)HDM, discussing the relevant DM annihilation scenarios, including the extended co-annhilating (pseudo-)scalar sector. Section 4 will be focused on new features of the I(2+1)HDM with respect to the I(1+1)HDM in the context of DM phenomenology, including enhanced DM-Higgs couplings and the new mass region 360 GeV $\lesssim m_{\rm DM} \lesssim 525$ GeV as well as on discussing the resulting improved prospects for direct detection. In section 5 we present heavy DM signals via Higgs mediation at the LHC in the I(2+1)HDM which look more promising than in the I(1+1)HDM. Finally in section 6 we conclude the paper.

2 The I(2+1)HDM

2.1 The scalar potential

It has been shown in [15] that an N-Higgs-Doublet Model potential symmetric under a group G of phase rotations can be divided into two parts; a phase invariant part, V_0 , and a collection of extra terms ensuring the symmetry group G, V_G .

We construct our \mathbb{Z}_2 -symmetric 3-Higgs Doublet Model potential generated by the group

$$g = \operatorname{diag}(-1, -1, 1). \tag{2.1}$$

which is of the following form:²

$$V_{I(2+1)\text{HDM}} = V_0 + V_{Z_2}$$

$$V_0 = -\mu_1^2 (\phi_1^{\dagger} \phi_1) - \mu_2^2 (\phi_2^{\dagger} \phi_2) - \mu_3^2 (\phi_3^{\dagger} \phi_3)$$

$$+ \lambda_{11} (\phi_1^{\dagger} \phi_1)^2 + \lambda_{22} (\phi_2^{\dagger} \phi_2)^2 + \lambda_{33} (\phi_3^{\dagger} \phi_3)^2$$

$$+ \lambda_{12} (\phi_1^{\dagger} \phi_1) (\phi_2^{\dagger} \phi_2) + \lambda_{23} (\phi_2^{\dagger} \phi_2) (\phi_3^{\dagger} \phi_3) + \lambda_{31} (\phi_3^{\dagger} \phi_3) (\phi_1^{\dagger} \phi_1)$$

$$+ \lambda'_{12} (\phi_1^{\dagger} \phi_2) (\phi_2^{\dagger} \phi_1) + \lambda'_{23} (\phi_2^{\dagger} \phi_3) (\phi_3^{\dagger} \phi_2) + \lambda'_{31} (\phi_3^{\dagger} \phi_1) (\phi_1^{\dagger} \phi_3).$$

$$V_{Z_2} = -\mu_{12}^2 (\phi_1^{\dagger} \phi_2) + \lambda_1 (\phi_1^{\dagger} \phi_2)^2 + \lambda_2 (\phi_2^{\dagger} \phi_3)^2 + \lambda_3 (\phi_3^{\dagger} \phi_1)^2 + h.c.$$

$$(2.2)$$

²Note that adding extra Z_2 -respecting terms such as $(\phi_3^{\dagger}\phi_1)(\phi_2^{\dagger}\phi_3), (\phi_1^{\dagger}\phi_2)(\phi_3^{\dagger}\phi_3), (\phi_1^{\dagger}\phi_2)(\phi_1^{\dagger}\phi_1)$ and/or $(\phi_1^{\dagger}\phi_2)(\phi_2^{\dagger}\phi_2)$ does not change the phenomenology of the model. The coefficients of these terms, therefore, have been set to zero for simplicity.

We shall not consider CP-violation in this paper, therefore, we require all parameters of the potential to be real.

The doublets are defined as

$$\phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{H_1^0 + iA_1^0}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{H_2^0 + iA_2^0}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{v + h + iG^0}{\sqrt{2}} \end{pmatrix}, \quad (2.3)$$

where ϕ_1 and ϕ_2 are the two inert doublets and ϕ_3 is the one active doublet which plays the role of the SM Higgs doublet, with h being the SM-Higgs boson and G^{\pm} , G^0 are the would-be Goldstone bosons.

We assign Z_2 charges to each doublet according to the Z_2 generator in eq. (2.1): odd- Z_2 charge to the inert doublets, ϕ_1 and ϕ_2 , and even- Z_2 charge to the active doublet, ϕ_3 . It is clear that the symmetry of the potential is respected by the vacuum alignment $(0, 0, \frac{v}{\sqrt{2}})$. The neutral fields from the inert doublets could then in principle be DM candidates. These neutral fields are stabilised from decaying into SM particles as a result of the conserved Z_2 symmetry of the potential after EWSB.

To make sure that the entire Lagrangian and not only the scalar potential is Z_2 symmetric, we assign an even Z_2 parity to all SM particles, identical to the Z_2 parity of the only doublet that couples to them, i.e., the active doublet ϕ_3 . With this parity assignment Flavour Changing Neutral Currents (FCNCs) are avoided as the extra doublets are forbidden to couple to fermions by Z_2 conservation.

The Yukawa Lagrangian of the model is identical to the SM Yukawa Lagrangian, with ϕ_3 playing the role of the SM Higgs doublet:

$$\mathcal{L}_{\text{Yukawa}} = \Gamma_{mn}^{u} \bar{q}_{m,L} \tilde{\phi}_{3} u_{n,R} + \Gamma_{mn}^{d} \bar{q}_{m,L} \phi_{3} d_{n,R} + \Gamma_{mn}^{e} \bar{l}_{m,L} \phi_{3} e_{n,R} + \Gamma_{mn}^{\nu} \bar{l}_{m,L} \tilde{\phi}_{3} \nu_{n,R} + h.c.$$
(2.4)

2.2 Mass eigenstates

The minimum of the potential sits at the point $(0,0,\frac{v}{\sqrt{2}})$ with $v^2 = \frac{\mu_3^2}{\lambda_{33}}$.

The mass spectrum of the scalar particles are as follows.

• The fields from the active doublet

The fields from the third doublet, G^0, G^{\pm}, h , which play the role of the SM Higgs doublet fields have squared masses:

$$m_{G^0}^2 = m_{G^{\pm}}^2 = 0$$

 $m_h^2 = 2\mu_3^2$ (2.5)

• The CP-even neutral inert fields

The pair of inert neutral scalar gauge eigenstates, H_1^0, H_2^0 , which are rotated by

$$R_{\theta_h} = \begin{pmatrix} \cos \theta_h & \sin \theta_h \\ -\sin \theta_h & \cos \theta_h \end{pmatrix}, \quad \text{with} \quad \tan 2\theta_h = \frac{2\mu_{12}^2}{\mu_1^2 - \Lambda_{\phi_1} - \mu_2^2 + \Lambda_{\phi_2}}$$

into the mass eigenstates, H_1, H_2 , have squared masses:

$$m_{H_1}^2 = (-\mu_1^2 + \Lambda_{\phi_1})\cos^2\theta_h + (-\mu_2^2 + \Lambda_{\phi_2})\sin^2\theta_h - 2\mu_{12}^2\sin\theta_h\cos\theta_h$$

$$m_{H_2}^2 = (-\mu_1^2 + \Lambda_{\phi_1})\sin^2\theta_h + (-\mu_2^2 + \Lambda_{\phi_2})\cos^2\theta_h + 2\mu_{12}^2\sin\theta_h\cos\theta_h$$
where
$$\Lambda_{\phi_1} = \frac{1}{2}(\lambda_{31} + \lambda'_{31} + 2\lambda_3)v^2, \quad \Lambda_{\phi_2} = \frac{1}{2}(\lambda_{23} + \lambda'_{23} + 2\lambda_2)v^2$$
 (2.6)

• The charged inert fields

The pair of inert charged gauge eigenstates, $\phi_1^{\pm}, \phi_2^{\pm}$, which are rotated by

$$R_{\theta_c} = \begin{pmatrix} \cos \theta_c & \sin \theta_c \\ -\sin \theta_c & \cos \theta_c \end{pmatrix}, \quad \text{with} \quad \tan 2\theta_c = \frac{2\mu_{12}^2}{\mu_1^2 - \Lambda'_{\phi_1} - \mu_2^2 + \Lambda'_{\phi_2}}$$

into the mass eigenstates, H_1^{\pm}, H_2^{\pm} , have squared masses:

$$m_{H_1^{\pm}}^2 = (-\mu_1^2 + \Lambda'_{\phi_1})\cos^2\theta_c + (-\mu_2^2 + \Lambda'_{\phi_2})\sin^2\theta_c - 2\mu_{12}^2\sin\theta_c\cos\theta_c$$

$$m_{H_2^{\pm}}^2 = (-\mu_1^2 + \Lambda'_{\phi_1})\sin^2\theta_c + (-\mu_2^2 + \Lambda'_{\phi_2})\cos^2\theta_c + 2\mu_{12}^2\sin\theta_c\cos\theta_c$$
where
$$\Lambda'_{\phi_1} = \frac{1}{2}(\lambda_{31})v^2, \quad \Lambda'_{\phi_2} = \frac{1}{2}(\lambda_{23})v^2$$
(2.7)

• The CP-odd neutral inert fields

The pair of inert pseudo-scalar gauge eigenstates, A_1^0, A_2^0 , which are rotated by

$$R_{\theta_a} = \begin{pmatrix} \cos \theta_a & \sin \theta_a \\ -\sin \theta_a & \cos \theta_a \end{pmatrix}, \quad \text{with} \quad \tan 2\theta_a = \frac{2\mu_{12}^2}{\mu_1^2 - \Lambda''_{\phi_1} - \mu_2^2 + \Lambda''_{\phi_2}}$$

into the mass eigenstates, A_1, A_2 , have squared masses:

$$m_{A_1}^2 = (-\mu_1^2 + \Lambda_{\phi_1}'')\cos^2\theta_a + (-\mu_2^2 + \Lambda_{\phi_2}'')\sin^2\theta_a - 2\mu_{12}^2\sin\theta_a\cos\theta_a$$

$$m_{A_2}^2 = (-\mu_1^2 + \Lambda_{\phi_1}'')\sin^2\theta_a + (-\mu_2^2 + \Lambda_{\phi_2}'')\cos^2\theta_a + 2\mu_{12}^2\sin\theta_a\cos\theta_a$$
where
$$\Lambda_{\phi_1}'' = \frac{1}{2}(\lambda_{31} + \lambda_{31}' - 2\lambda_3)v^2, \quad \Lambda_{\phi_2}'' = \frac{1}{2}(\lambda_{23} + \lambda_{23}' - 2\lambda_2)v^2$$
(2.8)

We will refer to (H_1, A_1, H_1^{\pm}) as the fields from the first generation and to (H_2, A_2, H_2^{\pm}) as the fields from the second generation. Each of the four neutral particles could, in principle, be the DM candidate, provided it is lighter than the other neutral states. In what follows, without loss of generality, we assume the CP-even³ neutral particle H_1 from the first generation to be lighter than all other inert particles, that is:

$$m_{H_1} < m_{H_2}, m_{A_{1,2}}, m_{H_{1,2}^{\pm}}.$$
 (2.9)

(Note that this choice is arbitrary: if the CP-even particle from the second generation, H_2 , where to be assumed lighter than the other inert states, then H_2 will play the role of the DM candidate.)

³For the CP-even particle to be the DM candidate rather than the CP-odd particle, it is required that $m_{H_1} < m_{A_1}$, which leads to $\lambda_2, \lambda_3 < 0$. If instead A_1 is assumed to be the DM candidate, $\lambda_2, \lambda_3 > 0$. Hence, the results of our analysis are also applicable to the A_1 DM case by changing the sign of λ_2 and λ_3 .

Assuming the CP-even neutral inert particles are lighter than the CP-odd and charged inert particles puts the following constraints on the parameters:

$$2\lambda_2, 2\lambda_3 < \lambda'_{23}, \lambda'_{31} < 0. (2.10)$$

In our DM analysis, we consider cases where the mass alignment is changed, but where H_1 is always the lightest inert state and hence is the DM particle. In the remainder of the paper the notations H_1 and DM particle will be used interchangeably.

2.3 Constraints on parameters

In [14], we have studied in detail the theoretical constraints; positivity of the mass eigenstates, bounded-ness of the potential, positive-definite-ness of the Hessian, and the LEP limits on the parameters of the potential. These limits have been taken into account in the present paper.

Our parameter choice is also compliant with all experimental constraints studied in [16] for the I(1+1)HDM, namely the Electroweak Precision Test (EWPT) bounds. In the I(2+1)HDM studied here, we are considering heavy inert particles (with the lightest being $m_{H_1} > 425 \,\text{GeV}$) with large mass splittings (with $\delta_a = \delta_c = \Delta = 1 \,\text{GeV}$ in case G and $\delta_a = \delta_c = 1 \,\text{GeV}$, $\Delta = 100 \,\text{GeV}$ in case H), which clearly satisfy the EWPT bounds presented in figure 1 in [16].

2.4 Simplified couplings in the I(2+1)HDM

Due to the large number of free parameters in the I(2+1)HDM which makes it impractical to analyse the model in the general case, we focus on a simplified case where parameters related to the first inert doublet are k times the parameters related to the second doublet

$$\mu_1^2 = k\mu_2^2, \quad \lambda_3 = k\lambda_2, \quad \lambda_{31} = k\lambda_{23}, \quad \lambda'_{31} = k\lambda'_{23},$$
 (2.11)

resulting in

$$\Lambda_{\phi_1} = k\Lambda_{\phi_2}, \quad \Lambda'_{\phi_1} = k\Lambda'_{\phi_2}, \quad \Lambda''_{\phi_1} = k\Lambda''_{\phi_2},$$
(2.12)

without introducing any new symmetry to the potential. The motivation for this simplified scenario is that in the k=0 limit the model reduces to the well-known I(1+1)HDM. We assume no specific relation among the other parameters of the potential. It is important to note that the remaining quartic parameters do not influence the discussed DM and LHC phenomenology of the model and thus their values have been fixed in agreement with the constraints discussed in section 2.3 and compliant with the results on unitarity obtained in [17].

The k = 1 case. In this paper we focus on the k = 1 case in the heavy DM mass region.⁴ The mass spectrum in this case is simplified to:

$$m_{H_1}^2 = -\mu_2^2 + \Lambda_{\phi_2} - \mu_{12}^2, \qquad m_{H_2}^2 = m_{H_1}^2 + 2\mu_{12}^2, \qquad (2.13)$$

$$m_{H_1^{\pm}}^2 = -\mu_2^2 + \Lambda'_{\phi_2} - \mu_{12}^2, \qquad m_{H_2^{\pm}}^2 = m_{H_1^{\pm}}^2 + 2\mu_{12}^2,$$

$$m_{A_1}^2 = -\mu_2^2 + \Lambda''_{\phi_2} - \mu_{12}^2, \qquad m_{A_2}^2 = m_{A_1}^2 + 2\mu_{12}^2.$$

⁴Other scenarios with $k \neq 1$ are studied in [14].

The quartic couplings in the potential can be written in terms of the masses of the physical particles as:

$$\lambda'_{23} = \frac{1}{v^2} (m_{H_1}^2 + m_{A_1}^2 - 2m_{H_1^{\pm}}^2),
\lambda_2 = \frac{1}{2v^2} (m_{H_1}^2 - m_{A_1}^2),
\lambda_{23} = g_{H_1 H_1 h} - \frac{2}{v^2} (m_{H_1}^2 - m_{H_1^{\pm}}^2),$$
(2.14)

where $g_{H_1H_1h} = \lambda_{23} + \lambda'_{23} + 2\lambda_2$ is the Higgs-DM coupling. The Feynman rules for this model are presented in appendix A.

3 Calculating the relic density in the I(2+1)HDM

The relic density of the WIMP (identified in our model as the lightest inert scalar H_1) is calculated with the assumption that the WIMP was in thermal equilibrium with the SM particles after inflation. Once the rate of

$$DM DM \leftrightarrow SM SM$$

reactions becomes smaller than the Hubble expansion rate of the Universe, the WIMP freezes out, i.e., drops out of the thermal equilibrium. After freeze-out the co-moving WIMP density remains essentially constant with the current value estimated by the Planck experiment to be the one already given in eq. (1.1).

As mentioned, in the I(2+1)HDM one of the neutral inert (pseudo-)scalar particles play the role of the DM. The relic density of a (pseudo-) scalar DM candidate, S, after freeze-out is given by the solution to the Boltzmann equation:

$$\frac{dn_S}{dt} = -3Hn_S - \langle \sigma_{\text{eff}} v \rangle (n_S^2 - n_S^{eq \, 2}), \qquad S = H_1, H_2, A_1, A_2, \tag{3.1}$$

where the thermally averaged effective (co)annihilation cross-section contains all relevant scattering processes of any S_iS_j pair into SM particles:

$$\langle \sigma_{\text{eff}} v \rangle = \sum_{ij} \langle \sigma_{ij} v_{ij} \rangle \frac{n_i^{eq}}{n_S^{eq}} \frac{n_j^{eq}}{n_S^{eq}}, \tag{3.2}$$

where

$$\frac{n_i^{eq}}{n_S^{eq}} \sim \exp\left(-\frac{m_i - m_S}{T}\right). \tag{3.3}$$

Therefore, only processes in which the mass splitting between a state S_i and the lightest Z_2 -odd particle S (H_1 in our case) are comparable to the thermal bath temperature T provide a sizeable contribution to this sum.

In the I(2+1)HDM, the presence of additional inert particles has important consequences in the heavy mass regime. For lighter masses the most important channel for the annihilation of DM particles is the Higgs-mediated process

$$H_1H_1 \to f\bar{f}$$

(see figure 12a), as studied in [14]. However, coannhilation with H_2 , A_1 and A_2 may change the results significantly (see figure 12b).

For heavier masses the diagrams including one or two virtual gauge bosons, shown in figure 13 also contribute to the total annihilation cross-section. Finally, co-annihilation plays an important role in scenarios with multiple particles which are close in mass. This scenario is realised in the I(2+1)HDM for the heavy DM mass region. Particles up to 20% heavier than the DM candidate may influence the DM relic density. Therefore, the co-annihilation diagrams should be included in calculating the effective annihilation cross-section. These diagrams are presented in figures 14 and 15 — representing pure gauge channels and coannhilation channels involving the SM-like Higgs particle, respectively.

3.1 Relevant co-annihilation scenarios

In the I(2+1)HDM, the strength and importance of coannhilation processes depend on the mass splittings between the inert particles. We define δ_A and δ_C as the splitting between H_1 and the pseudoscalar and charged state from the first generation, respectively,

$$\delta_A = m_{A_1} - m_{H_1}, \quad \delta_C = m_{H_1^{\pm}} - m_{H_1}.$$
 (3.4)

 $\delta_{A,C}$ are related to the quartic couplings in the potential, which are constrained by the perturbativity (and unitarity) conditions, i.e., the λ_i 's cannot be too large. As a result of this, all particles within one generation will have a similar mass. These masses, however, could have high values because of the (almost) unconstrained quadratic parameters μ_2^2 and μ_{12}^2 :

$$m_{H_1}^2 = -\mu_2^2 - \mu_{12}^2 + \frac{v^2}{2} g_{H_1 H_1 h}. (3.5)$$

It is important to stress that, even if bounds on λ_i were relaxed leading to larger values of $\delta_{A,C}$, there exist very stringent limits from relic density analysis. Coannihilation must occur at least between H_1, A_1 and H^{\pm} to achieve DM relic density in agreement with the current experimental measurements. This is a pattern followed by all general heavy scalar DM models. In the absence of these co-annihilation channels, the maximum relic density that can be achieved through $H_1H_1 \to \text{SM SM}$ (even when $H_iH_j \to \text{SM SM}$ is allowed) is of order 10^{-3} which is well below the observed value.

The other important mass splitting, Δ , is defined as the mass difference between H_1 and the other CP-even state H_2 ("splitting between doublets"):

$$\Delta = m_{H_2} - m_{H_1} \tag{3.6}$$

 Δ is related to the quadratic parameter μ_{12}^2 through

$$\mu_{12}^2 = \frac{1}{2}(m_{H_2}^2 - m_{H_1}^2) = \frac{1}{2}(\Delta^2 + 2m_{H_1}\Delta). \tag{3.7}$$

Note that μ_{12}^2 is not limited by any theoretical constraints — similar to μ_2^2 — and therefore Δ can in principle be very large. So, unless Δ is forced to be small by limits put on μ_{12}^2 , one should also consider a case where the second doublet is decoupled from the first, leading to a scenario which was not listed in [14]. Therefore, in the very heavy mass region one can consider:

	Small δ_A, δ_C	Large δ_A, δ_C
Small Δ	Case G is realised	Coannhilation between H_1, H_2 is not efficient enough and DM density is below experimental bounds.
Large Δ	Case H is realised	There are no co-annihilatin channels open and gauge annihilation reduces DM relic density effectively below the experimental bounds.

Table 1. Valid regions of the parameter space schematically shown in terms of δ_A , δ_C and Δ in the heavy mass regime of I(2+1)HDM.

- Case G: with small $\delta_A, \delta_C, \Delta$, where all inert particles are close in mass and coannihilate with each other.
- Case H: with small δ_A, δ_C and large Δ , where the second generation is effectively decoupled from the first generation and does not influence relic density calculations. In this case, the relevant diagrams are the (co)annihilation channels between fields from the lighter generation only, H_1, A_1, H_1^{\pm} .

Table 1 summarises the two possible scenarios for relic density studies.

3.2 The gauge limit

To illustrate the difference between cases G and H, let us first consider the gauge limit in both scenarios, which is the limit where all quartic couplings λ_i are set to zero. Therefore, all scalar self-couplings, including the DM-Higgs coupling, are removed in this limit. As a result $\delta_{A,C} = 0$, leading to degenerate H_1, A_1, H_1^{\pm} states. Note that this limit is excluded by results of direct detection experiments, nevertheless, it is an interesting limit to study as it represents the main difference between cases G and H. In this limit H_1 annihilates solely through the gauge annihilation channels presented in figure 14.

Non-zero λ_i will lift this degeneracy and, at the same time, reduce the effective annihilation cross-section for a given mass. Therefore, the gauge limit corresponds to the minimum value of m_{H_1} , for which it is possible to obtain a proper relic density for any value of the Higgs-DM coupling.

These results are presented in figure 1 for the two scenarios: case G where all particles have degenerate mass (in the $\delta_{A,C}$, $\Delta \to 0 \Leftrightarrow \lambda_i \to 0$, $\mu_{12}^2 \to 0$ limit) and case H with large Δ where the second generation is decoupled from the first generation and all particles in the first generation are degenerate in mass (in the $\delta_{A,C} \to 0 \Leftrightarrow \lambda_i \to 0$ limit).

It is clear that, for a given mass of m_{H_1} the destructive interference between an increased number of coannhilation diagrams in case G leads to a reduced cross-section, i.e. larger DM relic density with respect to case H. The important consequence of this interference is that for case G it is possible to obtain proper relic density for smaller masses of DM candidate in comparison to case H. Note also that case H behaves like the I(1+1)HDM (the Inert Doublet Model) in this limit. This similarity in behaviour will be repeated as we will show in the following sections.

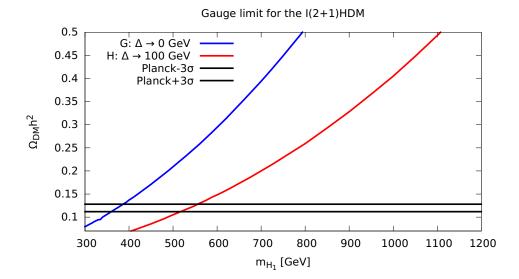


Figure 1. The gauge limit in case G (blue curve) where all particles have degenerate mass (in the $\delta_{A,C}$, $\Delta \to 0$) and case H (red curve) with large Δ where the second generation is decoupled from the first generation and all particles in the first generation are degenerate in mass (in the $\delta_{A,C} \to 0$ limit).

3.3 The benchmark points

With non-zero scalar couplings and mass splitting more diagrams contribute to the coannihilation of DM — all diagrams shown in figures 14 and 15 contribute to the total annihilation cross-section. Here we present two benchmarks points, two sets of parameters, for which we have studied the DM relic density:

• For case G with $\delta_A = \delta_C = 1 \, {\rm GeV}$ and $\Delta = 1 \, {\rm GeV}$

Here all inert particles have similar masses and therefore can co-annihilate with each other. The degeneracy between charged and "pseudo-scalar" particles is allowed and doesn't lead to any unacceptable results. The important degeneracy which must be avoided is H_1 - A_1 degeneracy leading to the scattering through the Z boson which is tightly constrained by direct detection experiments and puts a lower limit on δ_A .

• For case H with $\delta_A = \delta_C = 1 \, \text{GeV}$ and $\Delta = 100 \, \text{GeV}$

Here the second generation of inert scalars is significantly heavier than the first one. Within each generation, however, particles are almost degenerate.

Note that there are certain differences between cases G and H. In case H, the heavier generation of inert particles is decoupled from the first generation particles and does not influence the relic density calculations. The model in this case resembles the I(1+1)HDM. Furthermore, in case G the Higgs-DM couplings which result in a relic density in agreement with experiment are larger in comparison to case H for the same DM mass. This difference is explicit in figure 2.

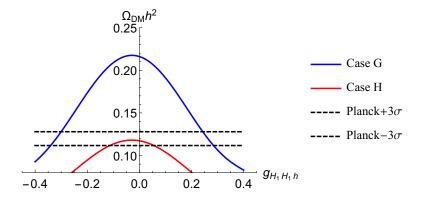


Figure 2. Relic density plots in case G ($\Delta = 1 \,\text{GeV}$, blue line) and H ($\Delta = 100 \,\text{GeV}$, red line) for $m_{H_1} = 550 \,\text{GeV}$. The dashed horizontal lines show the 3σ relic density limits from Planck in eq. (1.1).

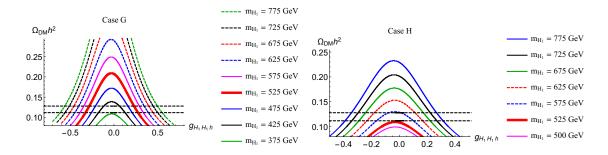


Figure 3. Relic density plots for case G (left) with $\Delta = 1 \,\text{GeV}$, $\delta = 1 \,\text{GeV}$ and case H (right) with $\Delta = 100 \,\text{GeV}$, $\delta = 1 \,\text{GeV}$. Note the solid red line in the case H which represents the minimum DM mass $m_{H_1} = 525 \,\text{GeV}$ which just touching the lower relic density limit. The relic density plot for the same DM mass has been highlighted in case G (red solid line) which is well within the acceptable relic density limits. The dashed horizontal lines show the 3σ relic density limits from Planck in eq. (1.1).

This leads to the fact that for case G we can obtain viable relic density values for $m_{\rm DM}$ much smaller than in case H (or the I(1+1)HDM) in which the minimal value of $m_{\rm DM}$ resulting in DM relic density in agreement with Planck limits is $m_{H_1} \approx 525 - 535 \, {\rm GeV}$. In case G (with $\Delta = 1 \, {\rm GeV}$), however, the DM mass can be as low as $\sim 375 \, {\rm GeV}$. This result is shown in figure 3 which represents relic density plots for cases G (left) and H (right). Note that in case G the minimum m_{H_1} which touches the lowest acceptable relic density limit (the green solid line) is $375 \, {\rm GeV}$ (for a given Δ of $1 \, {\rm GeV}$), whereas in case H this minimum value is $525 \, {\rm GeV}$ (the solid red line).

Figure 4 is meant to represent the same benchmark points as in figure 3, in the m_{H_1} - $g_{H_1H_1h}$ plane. The bands correspond to proper relic density in agreement with Planck measurements in case G (for an exemplary $\Delta = 1 \,\text{GeV}$, $\delta = 1 \,\text{GeV}$) in red and case H (for an exemplary $\Delta = 100 \,\text{GeV}$, $\delta = 1 \,\text{GeV}$) in red. Note that, for the a given DM mass (and same δ), the Higgs-DM coupling in case G is much larger than in case H.

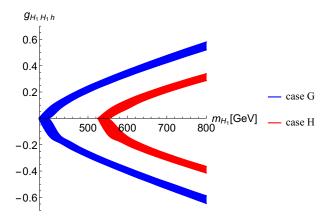


Figure 4. Relic density bands in agreement with Planck measurements in case G (for an exemplary $\Delta = 1 \, \text{GeV}$, $\delta = 1 \, \text{GeV}$) in red and case H (for an exemplary $\Delta = 100 \, \text{GeV}$, $\delta = 1 \, \text{GeV}$) in red. Note that for the a given DM mass, the Higgs-DM coupling in case G is much larger than in case H.

4 DM in the I(2+1)HDM: direct detection

4.1 Changes in Δ , δ_A , δ_C

For the two viable scenarios G and H we allow the physical parameters to vary in the following regions:

$$100 \text{ keV} \lesssim \delta_A, \delta_C \lesssim 15 \text{ GeV}.$$
 (4.1)

Since δ_A and δ_C are related to the quartic parameters λ_i 's, they are constrained from unitarity bounds and are required to be small. However, regardless of any limits on λ_i from unitarity, relic density studies show that both δ_A and δ_C must be relatively small to allow for co-annihilation between particles which is crucial in the heavy DM mass region. The upper limit follows the following rough rule: co-annihilation effects take place when the mass difference between co-annihilating particles is of the order of 20% of their mass.

The lower bound on δ_A comes from direct detection experiments where a degeneracy between H_1 and A_1 leads to the scattering through the Z boson which is tightly constrained. Further, the above limits in eq. (4.1) are in agreement with LEP searches for exotic particles. Finally, below $\delta_{A,C} \sim 0.1 \text{ GeV}$ there is no visible difference in the results.

As mentioned before, a large difference between δ_A and δ_C violates relic density limits. In the cases we study below, we have set $\delta_A = \delta_C = \delta$ for simplicity.⁵ The mass splitting between the two generations, Δ , is proportional to and therefore unconstrained by unitarity. The maximum value for Δ is proportional to the arbitrary maximum value chosen for μ_{12}^2 . In general, we allow for Δ to vary in the following region

$$100 \text{ keV} \lesssim \Delta \lesssim 200 \text{ GeV}.$$
 (4.2)

For large Δ values, $\Delta \gtrsim 20 - 50 \,\text{GeV}$ (depending on m_{H_1} , since the story-changing mass splitting is roughly $20\% m_{H_1}$), co-annihilation effects between the two generations

⁵Cases with $\delta_A \neq \delta_C$ do not lead to any new phenomenology and in fact the region of validity for $g_{H_1H_1h}$ decreases as we increase the difference between δ_A and δ_C .

are not strong enough to compete with the standard (co)annhilation between H_1 , A_1 , H_1^{\pm} , in which case the I(2+1)HDM acts just like the I(1+1)HDM. The second generation is effectively decoupled from the first generation and does not influence DM phenomenology. Therefore, scenario H is realised for:

$$\Delta \gtrsim 20 \; {\rm GeV} \quad \Rightarrow \quad {\rm scenario} \; {\rm H} \eqno(4.3)$$

The exact value of Δ , when above $\sim 20-50\,\mathrm{GeV}$ does not make any significant difference in the relic density calculations.

For small values of Δ , the co-annihilation effects between all particles are important. The smaller Δ is, the more relevant particles from the second generation are for DM studies: for $\Delta \approx 1.5$ GeV the relative contribution to relic density calculation coming from particles from the lighter generation to the heavier generation is 70%-30%. For $\Delta \approx 0.0001$ GeV this relation is 50%-50%. The case G, is therefore realised when Δ varies in the following window

$$0.0001 \text{ GeV} \lesssim \Delta \lesssim 20 \text{ GeV} \quad \Rightarrow \quad \text{scenario G}$$
 (4.4)

The closer Δ gets to this upper limit, the weaker the coannnihilation effects and the more scenario H is realised. Finally, notice that, for our studies, the Higgs-DM coupling, $g_{hH_1H_1}$, is kept within the $|g_{hH_1H_1}| < 1$ range.

Figure 5 illustrates the effect of changing Δ on the relic density. In all four plots $m_{\rm DM}$ has been set to 400 GeV as the value of Δ changes, 0.1 GeV in the top left plot, 1 GeV in the top right plot, 5 GeV in the bottom left plot and 10 GeV in the bottom right plot. In each plot different colours represent different δ s. For small values of Δ (0.1 GeV), the H_1 - H_2 co-annihilation leads to viable relic density values even for large δ (i.e. the H_1, A_1, H^{\pm} co-annihilation is absent). For large values of Δ (10 GeV) H_1 - H_2 co-annihilation does not exist and even small values of δ cannot compensate this lack, thus, the relic density is below the acceptable limit.

In figure 6 the value of δ is set to 0.5 GeV for $m_{\rm DM}=400$ GeV in the left plot and $m_{\rm DM}=550$ GeV in the right plot. In each plot, different colours correspond to changing Δ s. Note that in the left plot only small values of Δ lead to viable relic density values, which is where case G is realised. In the right plot, small values of Δ correspond to case G and large values of Δ correspond to case H, and they all lead to acceptable relic density values. Note that for $\Delta \gtrsim 50$ GeV all curves correspond to the same value.

4.2 Changes in $m_{\rm DM}$

Here we describe several sub-regimes where the DM mass can vary with important characteristics.

• In the region

$$m_{\rm DM} \lesssim 360 \text{ GeV}$$
 (4.5)

neither scenario H nor G results in viable relic density values.⁶ This lower limit can be reached in case G by very specific points in the parameter space: (a) when the

⁶In extensions of the I(2+1)HDM with more inert doublets, this $m_{\rm DM}$ limit could be lowered as more co-annihilation channels are present due to the extended number of inert particles.

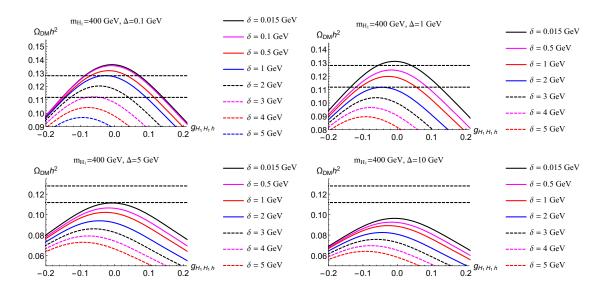


Figure 5. The effect of changing Δ on the relic density. In all four plots $m_{\rm DM}$ has been set to 400 GeV as the value of Δ changes, 0.1 GeV in the top left plot, 1 GeV in the top right plot, 5 GeV in the bottom left plot and 10 GeV in the bottom right plot. In each plot different colours represent different δ s. For small values of Δ (0.1 GeV), the H_1 - H_2 co-annihilation leads to viable relic density values even for large δ (i.e. the H_1 , A_1 , H^{\pm} co-annihilation is absent). For large values of Δ (10 GeV) H_1 - H_2 co-annihilation does not exist and even small values of δ cannot compensate this lack, thus, the relic density is below the acceptable limit.

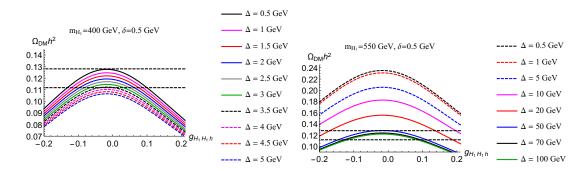


Figure 6. Relic density plot for $\delta = 0.5 \,\mathrm{GeV}$ for $m_{\mathrm{DM}} = 400 \,\mathrm{GeV}$ in the left plot and $m_{\mathrm{DM}} = 550 \,\mathrm{GeV}$ in the right plot. In each plot, different colours correspond to changing Δs . Note that in the left plot only small values of Δ lead to viable relic density values, which is where case G is realised. In the right plot, small values of Δ correspond to case G and large values of Δ correspond to case H, and they all lead to acceptable relic density values. Note that for $\Delta \gtrsim 50 \,\mathrm{GeV}$ all curves correspond to the same value.

mass splitting between all particles is tiny and all particles are almost degenerate in mass (up to $\mathcal{O}(100 \text{ keV})$ mass splitting to avoid direct detection limits), (b) when $g_{hH_1H_1}$ is close to 0.

• In the region

$$360 \text{ GeV} \lesssim m_{\text{DM}} \lesssim 525 \text{ GeV}$$
 (4.6)

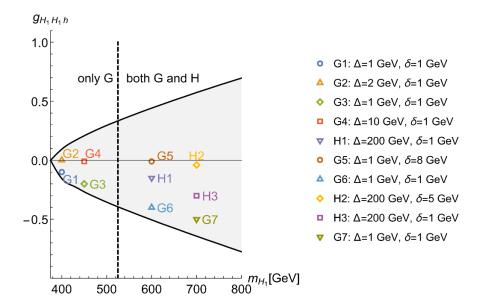


Figure 7. Here Gi and Hi represent certain points in the parameter space corresponding to cases G and H, respectively. The shaded region is where the I(2+1)HDM has acceptable relic density results. To the left of the vertical dashed line case G is realised and to the right of it both cases G and H are realised. Generally the outermost parts of the shaded region are populated by Gi since they correspond to larger Higgs-DM couplings, and the innermost parts of the region correspond to case H. However, depending on the values of δ the Higgs-DM coupling changes and Gi points can appear close to the $g_{hH_1H_1} = 0$ line as well, which is apparent in comparing the points G5, H1 and G6. Other points are shown on the plot for different values of Δ and δ for comparison.

only scenario G leads to acceptable values of DM relic density for specific values of Δ in the 0.0001 GeV $\lesssim \Delta \lesssim 20$ GeV and $|g_{H_1H_1h}| \lesssim 0.3$ window. As a rule of thumb, smaller Δ allows for a wider viable region in the parameter space and the larger m_{H_1} is the larger $|g_{hH_1H_1}|$ must be.

• In the region

$$535 \text{ GeV} \lesssim m_{\text{DM}} \lesssim 1.5 - 2 \text{ TeV}$$
 (4.7)

both scenarios, G and H, lead to viable values of DM relic density. The appropriate value of $g_{H_1H_1h}$ coupling depends on the DM mass in each case. In scenario G, couplings are generally larger compared to scenario H and a larger DM mass requires larger values of the $g_{H_1H_1h}$ coupling.

Figure 7 is meant to summarise all that was said above in one plot with Gi and Hi representing certain points in the parameter space corresponding to cases G and H, respectively. The shaded region is where the I(2+1)HDM has acceptable relic density results. To the left of the vertical dashed line case G is realised and to the right of it both cases G and H are realised. Generally the outermost parts of the shaded region are populated by Gi since they correspond to larger Higgs-DM couplings whereas the innermost parts of the region correspond to case H. However, depending on the values of δ the Higgs-DM coupling changes and Gi points can appear close to the $g_{hH_1H_1} = 0$ line as well, which

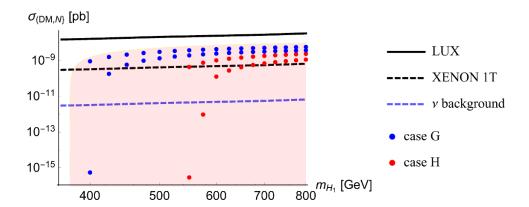


Figure 8. The DM-nucleon scattering cross-section for the I(2+1)HDM in comparison with the direct detection limits set by LUX (black line) and projected XENON 1T (black dashed line). Coherent neutrino scattering limit is also shown (dashed blue line). The shaded region corresponds to points with relic density in agreement with Planck measurements; results for benchmark points for case G ($\Delta = 1$ GeV, $\delta = 1$ GeV, blue) and case H ($\Delta = 100$ GeV, $\delta = 1$ GeV) are presented.

is apparent in comparing the points G5, H1 and G6. Other points are shown on the plot for different values of Δ and δ for comparison.

4.3 Direct detection

Direct detection experiments, which are mostly designed to hunt for the standard EW-scale WIMP, are the most sensitive to DM masses of the order of 100 GeV. For heavier DM masses the sensitivity of these experiments drops significantly. The most recent LUX results set the limit of the DM-nucleon scattering cross-section to be $\sigma_{\rm DM-N} \approx 10^{-8}$ pb for DM masses $\approx 500-1000\,{\rm GeV}$ [18].

In the I(2+1)HDM, similar to the other scalar DM models, DM candidate can be detected through elastic scattering on nuclei through the exchange of a Higgs particle. Therefore, $\sigma_{\text{DM}-N}$ will depend on the value of DM-Higgs coupling, and the DM mass.

These results are presented in figure 8 where the shaded region corresponds to the probed phase space of the I(2+1)HDM for various choices of Δ and δ (as shown in figure 7), all of which have relic density in agreement with Planck measurements. Also, results for the benchmark points studied in section 3 are presented explicitly. We found that the current experimental limits do not constrain the heavy DM mass region, neither for case H nor for case G, even though the Higgs-DM coupling is larger in the latter case.

Recall that for certain choices of Δ and δ one can obtain proper DM relic density for $g_{H_1H_1h} \approx 0$. This leads to a strongly suppressed scattering cross-section, which may not be detected as it lies within the coherent neutrino-nucleus scattering regime [19].

Figure 8 also shows a limit from the future XENON1T experiment [20], with a proposed sensitivity of the order of $10^{-9} - 10^{-10}$ pb (dashed black line). We expect the next generation of DM detectors, such as XENON1T, to be able to test a large portion of the parameter space of the heavy DM in the I(2+1)HDM for $m_{H_1} \lesssim 1 \text{ TeV}$.

As a final note to this subsection, we should like to mention that a viable intermediate DM mass region, $m_W \lesssim m_{\rm DM} \lesssim 160\,{\rm GeV}$, regarding relic density studies, has been found in the I(1+1)HDM. The correct relic density in this region is obtained due to cancellations between different diagrams contributing to DM annihilation into gauge bosons (W^+W^- and ZZ). In [21] it was shown that this scenario is realised if the inert particles, in particular the charged scalar, are heavy enough, $\sim 300-500\,{\rm GeV}$. A relatively large DM-Higgs coupling is also required for the DM in this mass region to stay within relic density limits, however, this large Higgs-DM coupling is excluded by LUX. Similarly, we did not find any solutions in the medium mass region with viable relic density and in agreement with direct detection experiments in the I(2+1)HDM.

5 Heavy Higgs DM at the LHC in the I(2+1)HDM

A scalar DM candidate is a stable particle with limited interactions with all SM particles and therefore it cannot be directly detected at the LHC. However, its presence can influence the detectable properties of SM particles. One way to ascertain the influence of DM candidate on the properties of a Higgs particle is to look at the Higgs invisible decays, $h \to SS$, where S is a scalar DM candidate with mass below $m_h/2$. Invisible decays of the SM-like Higgs particle in the I(2+1)HDM were studied in [14, 22], where limits for the mass of a light DM candidate combined with Planck limits for the relic density measurements provided constraints comparable or stronger than those from direct detection experiments.

Another strategy, useful for a heavy DM particle, is to look for a high p_T monojet or a two jet/two lepton signal, accompanied by a large missing transverse energy \mathcal{E}_T . The monojet signature in the I(2+1)HDM, $pp \to H_1H_1$ + jet, corresponds to h coupling to an invisible pair of DM particles (yielding the large \mathcal{E}_T) with produced in association with an energetic quark or gluon jet. The following processes are considered in our analysis.

- 1. $gg \to gH_1H_1$ (figure 16) via a triple gluon and a hgg effective vertex. Note, that the hgg effective vertex in the I(2+1)HDM is the same as in the SM, as the Higgs production here is not modified by presence of additional scalar states. This is the dominant contribution to the monojet process, as the gluon fusion is an enhanced production mechanism for the Higgs particle.
- 2. $q\bar{q} \to gH_1H_1$ (figure 17), where q = u, d, c, s, b. The dominant contribution comes from the s-channel via the $gq\bar{q}$ tree-level vertex and the hgg effective coupling (figure 17a).
- 3. $qg \to qH_1H_1$ (figure 18), where q = u, d, c, s, b. The dominant contributions here come from $gb \to H_1H_1b$ with the Higgs boson radiated off of the b quark legs (figure 18a) and $qg \to qH_1H_1$ t-channel via a $gq\bar{q}$ tree-level vertex and the hgg effective coupling (figure 18b).

Note, that all above processes contain the $h \to H_1H_1$ vertex, therefore a strong dependency on the $g_{H_1H_1h}$ coupling is expected, i.e., a significant difference between scenarios G and H, as discussed in the previous section.

For the studies of $pp \to H_1H_1 + 2$ jets we have considered the Vector Boson Fusion (VBF) process of the form $q_iq_j \to H_1H_1q_kq_l$, with q = u, d where a pair of DM particles (with large \mathbb{Z}_T) is produced by the neutral (figure 19) or charged (figure 20) VBF processes, either directly or mediated by the Higgs particle or another neutral scalar.

We have also considered the Higgs-Strahlung (HS) processes of the form $q_i \bar{q}_j \rightarrow V^* H_1 H_1$ where a pair of DM particles is radiated off the Z or W^{\pm} boson leg (figure 21 and figure 22, respectively), either directly or mediated by the Higgs particle or another neutral scalar.

Notice, that in the dijet searches only one diagram out of each set depends on the $g_{H_1H_1h}$, therefore we expect smaller differences between scenarios H and G than in the monojet searches. The strength of the other diagrams is set by the gauge interactions.

Also, it is important to stress that, given our initial choice of parameters, i.e. introducing the k=1 relation between the doublets (see eq. (2.11)), we have limited the number of possible diagrams, because vertices of the type ZH_iA_j and $W^{\pm}H_iH_j^{\mp}$ ($i \neq j$) are absent when k=1. Relaxing this initial assumption would in principle not only influence the evolution of DM relic density, but could also lead to a possibly stronger difference between scenarios G and H in the dijet analysis.

In the following subsections we present results for the monojet and dijet analysis, for the 14 TeV LHC. The following selections were used.

1. For the monojet searches, we require the following cuts on the transverse momentum of the jet, p_T^j , and the pseudo-rapidity of the jet, η^j ,

$$p_T^j > 20 \text{ GeV} \quad \text{and} \quad |\eta^j| > 2.5$$
 (5.1)

2. For the dijet searches, we require the following cuts on the invariant mass of the two jets, M(j,j), and the difference between the pseudo-rapidity of the forward and backward jet,

$$M(j,j) > 700 \text{ GeV} \quad \text{and} \quad |\eta_f^j - \eta_b^j| > 4$$
 (5.2)

Calculations were done with the aid of LanHEP [23] and CalcHEP [24] packages.

5.1 Monojet results

In figure 9 results for monojet signals of scenarios G ($\delta_A = \delta_C = 1 \text{ GeV}$, $\Delta = 1 \text{ GeV}$) and H ($\delta_A = \delta_C = 1 \text{ GeV}$, $\Delta = 100 \text{ GeV}$) are shown. For comparison, we also present results for the I(1+1)HDM, with $\delta_A = \delta_C = 1$ from [12]. The DM-Higgs coupling (defined as λ_{345} in [12]) is the same as $g_{H_1H_1h}$ in scenario H for equal DM masses, therefore the monojet diagrams in case H and in I(1+1)HDM are identical.

Scenario G, which corresponds to much larger Higgs-DM couplings compared to that of scenario H or the I(1+1)HDM, results in a significantly larger cross-section in the monojet process. Also the special features of the model are more visible in this process. For masses up to $m_{H_1} \approx 450 \text{ GeV}$ we observe a rise in the cross-section connected to an opening of the phase space combined with an increasing Higgs-DM coupling. After that peak, the cross-section decreases with increasing DM mass regardless of the rising of $g_{hH_1H_1}$.

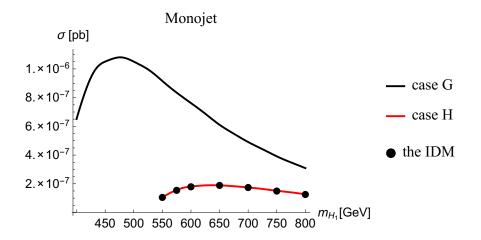


Figure 9. Monojet searches for cases G and H. For comparison we also provide monojet searches for the I(1+1)HDM which resemble case H in the I(2+1)HDM as expected.

Notice that for the lower masses, the difference between scenario G and H is significant, as every diagram involved in the monojet process contains the hH_1H_1 vertex, whose coupling differs significantly in cases G and H. Notice the low end of the allowed mass region in case G with a large cross-section for the mass region which is not even accessible by case H or the I(1+1)HDM. As the DM mass grows, results for both cases get closer together, stabilising for the very heavy mass region in the decoupling limit.

5.2 Dijet VBF results

Figure 10 presents values of the dijet cross-section for scenarios H and G in terms of the DM mass. The difference between cases H and G is less prominent compared to the monojet analysis, as only one of the involved diagrams in this process depends on the value of the Higgs-DM coupling (see figures 19 and 20 for diagrams involved in the neutral and charged VBF processes, respectively). We can still observe some differences in the lower mass range. The cross-section for case G is generally larger (as is the $g_{hH_1H_1}$ strength) than in case H. Also, charged channels have slightly larger cross-sections than the neutral ones, since the cross-section for producing the W^{\pm} boson is larger than the cross-section for producing the Z boson. For the heavier masses all results, for both scenarios G and H, as well as for charged and neutral channels, tend to converge.

5.3 HS results

HS signatures depend on the W and Z decay patterns. While at the LHC, leptonic signatures are preferred, hadronic ones are also possible. The latter potentially interfere with the VBF topologies, but the effect is small so that we can safely ignore it here.

The results of the (on-shell) HS process cross-sections in terms of the DM mass are presented in figure 11. It is clear that the general picture is different from the VBF studies. The largest cross-section again appears in the lower mass region where only case G can be realised. Similarly to the VBF case, the charged channels have larger cross-

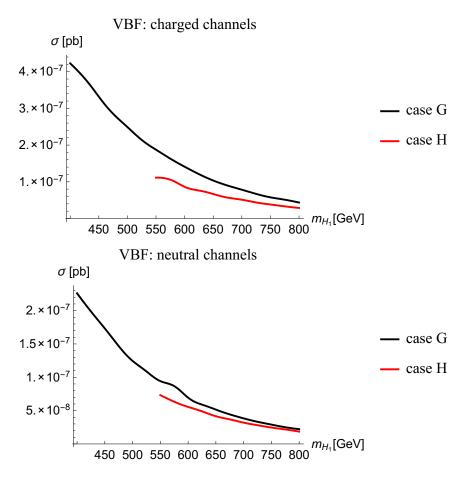


Figure 10. The cross-section in dijet VBF processes in terms of the DM mass in charged (top) and neutral (bottom) processes.

section compared to the neutral channels since the W^{\pm} production in theses processes has a larger cross-section than the Z boson production. All cross-sections in neutral and charged processes in both cases G and H converge to a similar value as $m_{\rm DM}$ approaches very large values.

Note that the cross-section in both G and H are similar in the region of DM mass above 525 GeV, i.e., where both cases can be realised (unlike in the VBF processes). This similarity is the result of the fact that the difference in the Higgs-DM coupling does not translate into a difference in the cross-section between cases G and H. To explain this similarity let us focus, e.g., on the neutral VBF and HS processes (figure 19 and figure 21).

In the neutral VBF process, out of all the involved diagrams (figure 19a,b,c) there is only one diagram, figure 19a, which depends on the Higgs-DM coupling. The cross-section of this diagram (σ_h) for a given $m_{\rm DM}$ relative to the cross-section of all three diagrams involved ($\sigma_{\rm tot}$) is $\sigma_h/\sigma_{\rm tot}=0.1445$ for case G and $\sigma_h/\sigma_{\rm tot}=0.2416$ for case H. Recall that the main difference between cases G and H is that for a chosen $m_{\rm DM}$ the Higgs-DM

⁷The same argument applies to comparing the charged VBF and HS processes.

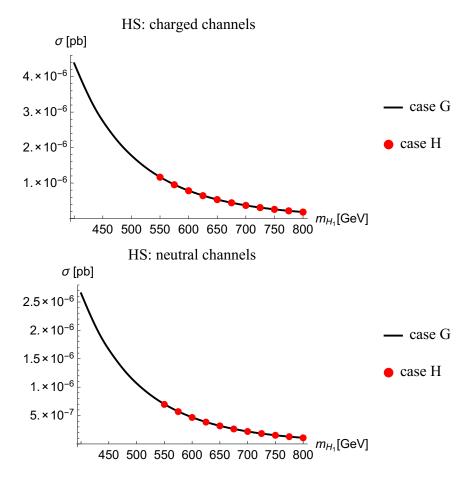


Figure 11. The cross-section in HS processes in terms of the DM mass in charged (top) and neutral (bottom) processes.

is larger in case G than in case H. We conclude that the Higgs-mediated diagram plays a much more important role in case H than it does in case G. As a result, even though the $g_{hH_1H_1}$ coupling is much smaller in case H, the total cross-section does not fall far below the total cross-section in case G, which is depicted in figure 10.

Now, let us consider the HS neutral processes (figure 21a,b,c). Again, only one diagram, figure 21a, depends on the Higgs-DM coupling. Repeating the procedure above, we calculate the relative cross-section of this one diagram (σ_h) relative to the cross-section of all diagrams involved (σ_{tot}). For a given m_{DM} , we obtain $\sigma_h/\sigma_{\text{tot}} = 0.9736$ in case G and $\sigma_h/\sigma_{\text{tot}} = 0.9708$ in case H. So, this diagram plays only a slight role in case H compared to case G. We therefore conclude that the difference in $g_{hH_1H_1}$ coupling does not play an important role in distinguishing case G and H in the HS processes. Thus, we do not expect to see a difference between cases G and H, which is depicted in figure 11, with the important exception that case G allows for the heavy Higgs DM mass to be below 525 GeV, making its cross-section significantly larger.

6 Conclusion

We have calculated the relic density for heavy Higgs DM in the I(2+1)HDM and shown that the prospects for its discovery at both DD experiments and the LHC are significantly enhanced as compared to the I(1+1)HDM, where the heavy Higgs DM particle must have a mass above about 525 GeV and is weakly coupled to the observed Higgs boson. Adding a second inert Higgs doublet helps to make the heavy Higgs DM region accessible to both DD and the LHC, by either increasing its couplings to the observed Higgs or lowering its mass to 360 GeV $\lesssim m_{\rm DM}$, or both. In particular we have presented LHC signatures of the I(2+1)HDM in the monojet, VBF (dijet) and HS processes and shown that the prospects for heavy Higgs DM discovery are significantly brighter for all channels.

In DD experiments, although the standard values of annihilation cross-section for the heavy Higgs DM masses in the I(2+1)HDM are well below current experimental exclusion limits for DM decaying into pairs of gauge bosons or fermions, the prospects for a future DD discovery remain open due to the complementary nature of collider vs cosmological limits and the fact that the DD cross-sections are higher than in the I(1+1)HDM.

Turning to indirect detection signatures of the I(2+1)HDM, there is the possibility of internal bremsstrahlung in the processes of $H_1H_1 \to W^+W^-\gamma$, generated through the exchange of any of the two charged scalars $H_{1,2}^{\pm}$. It was shown that one can expect such signatures in the I(1+1)HDM [25], mediated by a charged scalar in the t-channel, which would correspond to scenario H considered in the I(2+1)HDM. In principle, the signal could even be stronger for scenario G, as the scalar couplings are enhanced.

Finally we comment on the observed $h\to\gamma\gamma$ channel where, in the I(1+1)HDM, only in the heavy DM mass region are both proper DM relic density and (minimal) enhancement in the $h\to\gamma\gamma$ channel realised. By contrast, in the I(2+1)HDM there exist two charged scalars, H_1^\pm and H_2^\pm , which contribute to the $h\to\gamma\gamma$ loop which may enhance the rate for a wide range of parameters.

In conclusion, adding a second inert Higgs doublet significantly improves the prospects for observability of heavy Higgs dark matter in future experiments both underground and at the CERN LHC.

Acknowledgments

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A Feynman rules in the simplified I(2+1)HDM

Here we present the Feynman rules of the model.

$$\begin{array}{lll} H_2^+ H_2^- h, \ H_1^+ H_1^- h & \lambda_{23} v \\ H_1 H_1 h, \ H_2 H_2 h & (\lambda_{23} + \lambda'_{23} + 2\lambda_2) \frac{v}{2} \\ A_1 A_1 h, \ A_2 A_2 h & (\lambda_{23} + \lambda'_{23} - 2\lambda_2) \frac{v}{2} \\ H_2^+ H_2^- \gamma, \ H_1^+ H_1^- \gamma & \frac{i}{2} (g \sin \theta_W + g' \cos \theta_W) (K + K')^\mu \\ H_2^+ H_2^- Z, \ H_1^+ H_1^- Z & \frac{i}{2} (g \cos \theta_W - g' \sin \theta_W) (K + K')^\mu \\ H_1^\pm H_1 W^\pm, \ H_2^\pm H_2 W^\pm & \frac{ig}{2} \cos(\theta_h - \theta_c) (K + K')^\mu \\ H_2^\pm H_1 W^\pm, \ H_1^\pm H_2 W^\pm & \frac{ig}{2} \sin(\theta_h - \theta_c) (K + K')^\mu \\ H_1^\pm A_1 W^\pm, \ H_2^\pm A_2 W^\pm & \frac{g}{2} \cos(\theta_a - \theta_c) (K + K')^\mu \\ H_2^\pm A_1 W^\pm, \ H_1^\pm A_2 W^\pm & \frac{g}{2} \sin(\theta_a - \theta_c) (K + K')^\mu \\ H_2 A_1, \ H_2 A_2 Z & \frac{1}{2} (g \cos \theta_W + g' \sin \theta_W) \cos(\theta_h - \theta_a) (K + K')^\mu \\ H_2 A_1, \ H_1 A_2 Z & \frac{1}{2} (g \cos \theta_W + g' \sin \theta_W) \sin(\theta_h - \theta_a) (K + K')^\mu \end{array}$$

where K and K' are the momenta of the associated particles in the decay channel and θ_W is the Weak mixing angle. The Yukawa couplings in the model are identical to those of the SM.

B Feynman diagrams for relic density calculations

Here we present the DM (co)annihilation diagrams which play a role in our relic density studies.

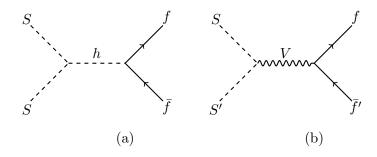


Figure 12. For light DM masses the most important channel for the annihilation of DM particles is the Higgs-mediated process (a). Coannhilation with other neutral scalars could have a significant effect on the relic density (b).

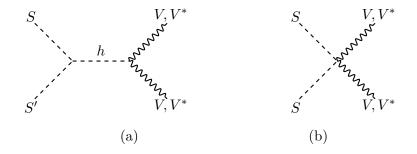


Figure 13. For heavy DM masses, the processes involving one or two virtual gauge bosons, also contribute to the total annihilation cross-section and affect the relic density.

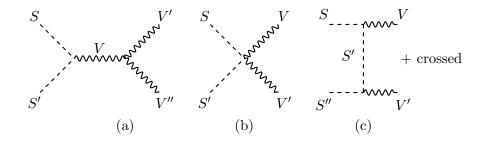


Figure 14. Heavy DM (co)annihilation diagrams with pure gauge boson final states.

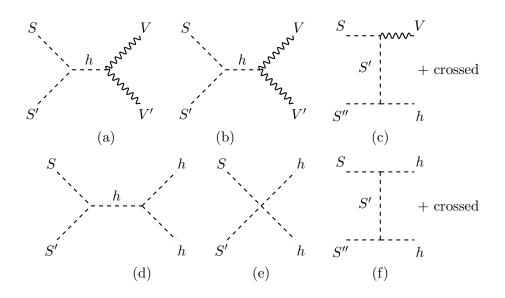


Figure 15. Heavy DM (co)annhilation channels involving the SM-like Higgs boson.

C Feynman diagrams for the LHC analysis

Here we present the DM (co)annihilation diagrams which play a role in our LHC studies.

C.1 Diagrams with monojet final states

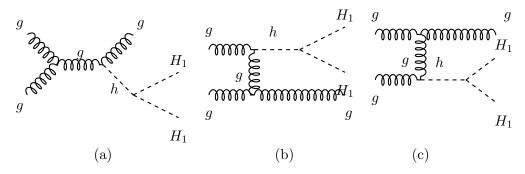


Figure 16. Relevant monojet diagrams with initial gluon states $(gg \to hg \to gH_1H_1)$ containing triple gluon vertex and an effective ggh vertex.

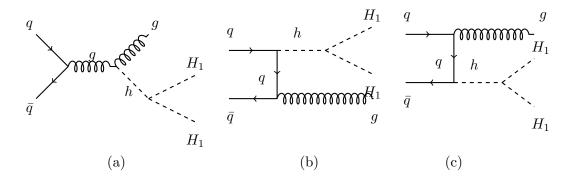


Figure 17. Relevant monojet diagrams with initial quark states $(q\bar{q} \to gH_1H_1 + \text{diagrams with initial particles reversed})$ containing ggh effective vertex, where q = u, d, c, s, b.

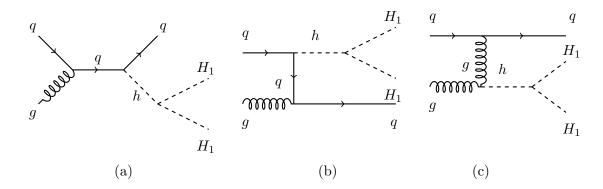


Figure 18. Relevant monojet diagrams with initial quark and gluon states $(qg \rightarrow qH_1H_1 + equivalent \bar{q}g \rightarrow \bar{q}H_1H_1 \text{ diagrams} + \text{diagrams} \text{ with initial particles reversed})$ containing ggh effective vertex, where q = u, d, c, s, b.

C.2 VBF diagrams with dijet final states

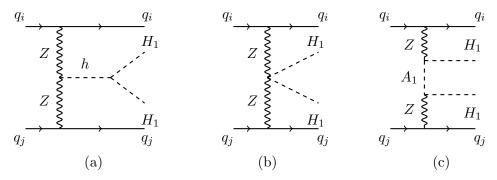


Figure 19. Relevant VBF diagrams with dijet final states $(q_iq_j \to H_1H_1q_iq_j)$ with only neutral intermediate gauge bosons, where q = u, d. Note that only one of the involved diagrams in this process depends on the value of the Higgs-DM coupling.

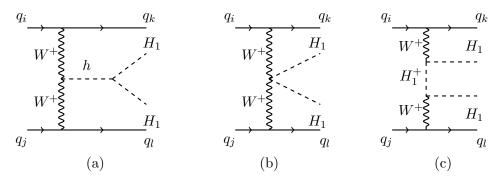


Figure 20. Relevant VBF diagrams with dijet final states $(q_iq_j \to H_1H_1q_kq_l)$ with only charged intermediate gauge bosons, where q = u, d. Note that only one of the involved diagrams in this process depends on the value of the Higgs-DM coupling.

C.3 HS diagrams with (on-shell) gauge boson final states

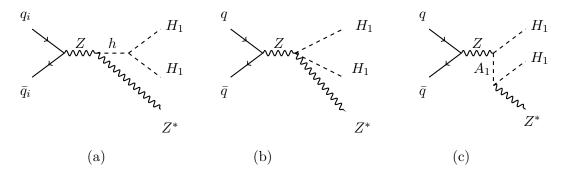


Figure 21. Relevant HS diagrams with (on-shell) neutral gauge boson final states $(q_i\bar{q}_i \to H_1H_1Z^*)$ and only neutral intermediate gauge bosons, where q = u, d. Note that only one of the involved diagrams in this process depends on the value of the Higgs-DM coupling.

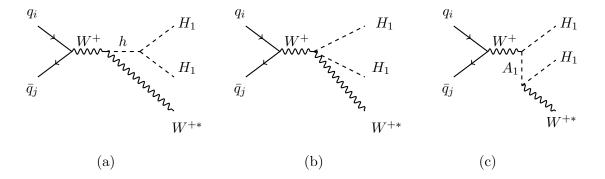


Figure 22. Relevant HS diagrams with (on-shell) charged gauge boson final states $(q_i\bar{q}_j \to H_1H_1W^{*+})$ and only charged intermediate gauge bosons, where q=u,d. Note that only one of the involved diagrams in this process depends on the value of the Higgs-DM coupling.

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