# Elliptic flow of muons from heavy-flavour hadron decays at forward rapidity in $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}$ 

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#### Abstract

The elliptic flow, $v_{2}$, of muons from heavy-flavour hadron decays at forward rapidity ( $2.5<y<4$ ) is measured in $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}$ with the ALICE detector at the LHC. The scalar product, two- and four-particle $Q$ cumulants and Lee-Yang zeros methods are used. The dependence of the $v_{2}$ of muons from heavy-flavour hadron decays on the collision centrality, in the range $0-40 \%$, and on transverse momentum, $p_{\mathrm{T}}$, is studied in the interval $3<p_{\mathrm{T}}<10 \mathrm{GeV} / c$. A positive $v_{2}$ is observed with the scalar product and two-particle $Q$ cumulants in semi-central collisions ( $10-20 \%$ and $20-40 \%$ centrality classes) for the $p_{\mathrm{T}}$ interval from 3 to about $5 \mathrm{GeV} / c$ with a significance larger than $3 \sigma$, based on the combination of statistical and systematic uncertainties. The $v_{2}$ magnitude tends to decrease towards more central collisions and with increasing $p_{\mathrm{T}}$. It becomes compatible with zero in the interval $6<p_{\mathrm{T}}<10 \mathrm{GeV} / c$. The results are compared to models describing the interaction of heavy quarks and open heavy-flavour hadrons with the high-density medium formed in high-energy heavy-ion collisions. © 2015 CERN for the benefit of the ALICE Collaboration. Published by Elsevier B.V. This is an open access article under the CC BY license (http://creativecommons.org/licenses/by/4.0/). Funded by SCOAP ${ }^{3}$.


## 1. Introduction

Experiments with ultra-relativistic heavy-ion collisions aim at investigating the properties of strongly-interacting matter at very high temperatures and energy densities. Quantum Chromodynamics (QCD) calculations on the lattice predict, under these conditions, the formation of a Quark-Gluon Plasma (QGP), where color confinement vanishes and chiral symmetry is partially restored [1-5]. Heavy quarks (charm and beauty) are created in initial hard-scattering processes on a time scale shorter than the QGP formation time. Subsequently, they interact with the medium constituents via inelastic [6,7] and elastic [8-10] processes. Therefore, heavy quarks are regarded as effective probes of the QGP properties.

Heavy-quark energy loss due to in-medium interactions can be studied by means of the nuclear modification factor $R_{\text {AA }}$, defined as the ratio of the yield of heavy-flavour particles measured in nucleus-nucleus (AA) collisions to that observed in protonproton ( pp ) collisions scaled by the number of binary nucleonnucleon collisions. The PHENIX and STAR Collaborations measured, in central $\mathrm{Au}-\mathrm{Au}$ collisions at $\sqrt{s_{\mathrm{NN}}}=200 \mathrm{GeV}$, a strong suppression corresponding to a $R_{\mathrm{AA}}$ of about 0.2-0.3 for heavy-flavour decay electrons at mid-rapidity $(y)$ and transverse momentum $p_{\mathrm{T}}>5 \mathrm{GeV} / c$ [11-17]. A similar suppression was also measured by

[^0]the STAR Collaboration for mid-rapidity $\mathrm{D}^{0}$ mesons [18]. A significant suppression was also observed by the PHENIX Collaboration at forward rapidity for muons from heavy-flavour hadron decays in central $\mathrm{Cu}-\mathrm{Cu}$ collisions at $\sqrt{s_{\mathrm{NN}}}=200 \mathrm{GeV}$ [19]. At the LHC, the ALICE Collaboration reported a similar effect in central $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}$ for D mesons at mid-rapidity [20] and muons from heavy-flavour hadron decays at forward rapidity [21] in the interval $2<p_{\mathrm{T}}<16 \mathrm{GeV} / \mathrm{c}$ and $4<p_{\mathrm{T}}<10 \mathrm{GeV} / \mathrm{c}$, respectively. The CMS Collaboration measured a significant suppression of non-prompt $\mathrm{J} / \psi$ from beauty-hadron decays in the interval $6.5<p_{\mathrm{T}}<30 \mathrm{GeV} / \mathrm{c}\left(3<p_{\mathrm{T}}<30 \mathrm{GeV} / \mathrm{c}\right)$ and $|y|<2.4$ $(1.6<|y|<2.4)[22,23]$. A first measurement of non-prompt J/ $\psi$ by the ALICE Collaboration at mid-rapidity $(|y|<0.8)$ and in the interval $4.5<p_{\mathrm{T}}<10 \mathrm{GeV} / \mathrm{c}$ has been recently published [24].

Further insights into the QGP evolution and the in-medium interactions can be gained from the study of the azimuthal anisotropy of particles carrying heavy quarks which, in contrast to light quarks, have experienced the full system evolution. The study of azimuthal anisotropy is a field of intense experimental and theoretical investigations (see [25] and references therein). In non-central collisions, the initial spatial anisotropy of the overlap region, elongated in the direction perpendicular to the reaction plane, defined by the beam axis and the impact parameter of the collision, is converted into an anisotropy in momentum space through rescatterings [26]. Experimentally, the study of the particle azimuthal anisotropy is based on a Fourier expansion of azimuthal distributions given by:

$$
\begin{equation*}
\frac{\mathrm{d}^{2} N}{\mathrm{~d} p_{\mathrm{T}} \mathrm{~d} \varphi}=\frac{1}{2 \pi} \frac{\mathrm{~d} N}{\mathrm{~d} p_{\mathrm{T}}}\left(1+2 \sum_{n=1}^{\infty} v_{n}\left(p_{\mathrm{T}}\right) \cos \left[n\left(\varphi-\Psi_{n}\right)\right]\right) \tag{1}
\end{equation*}
$$

where $\varphi$ and $p_{\mathrm{T}}$ are the particle azimuthal angle and transverse momentum, respectively. The Fourier coefficients, $v_{n}$, characterize the anisotropy of produced particles and $\Psi_{n}$ is the azimuthal angle of the initial-state symmetry plane for the $n$th harmonic, introduced to account for the event-by-event fluctuations of the initial nucleon density profile. The second Fourier coefficient, $v_{2}$, which can also be expressed as $v_{2}=\left\langle\cos \left[2\left(\varphi-\Psi_{2}\right)\right]\right\rangle$, is named elliptic flow.

The $v_{2}$ of heavy-flavour hadrons is expected to provide information on the collective expansion and degree of thermalization of heavy quarks in the medium at low $p_{\mathrm{T}}\left(p_{\mathrm{T}}<2-3 \mathrm{GeV} / \mathrm{c}\right)$. The participation of heavy quarks in the collective expansion is expected to give a positive $v_{2}$ [26]. Moving towards intermediate $p_{\mathrm{T}}\left(3<p_{\mathrm{T}}<6 \mathrm{GeV} / \mathrm{c}\right)$, the $v_{2}$ Fourier coefficient is also expected to be sensitive to the presence of recombination processes in the hadronization of heavy quarks $[27,28]$. At high $p_{\mathrm{T}}\left(p_{\mathrm{T}}>6 \mathrm{GeV} / \mathrm{c}\right)$, the $v_{2}$ measurement can constrain the path-length dependence of the in-medium parton energy loss, which becomes the dominant contribution to the azimuthal anisotropy and is also predicted to give a positive $v_{2}$ [29,30], thus complementing the $R_{\mathrm{AA}}$ measurement.

The PHENIX Collaboration reported a positive $v_{2}$ of heavyflavour decay electrons at mid-rapidity in $\mathrm{Au}-\mathrm{Au}$ collisions at $\sqrt{s_{\mathrm{NN}}}=200 \mathrm{GeV}$, reaching a maximum value of about 0.15 at $p_{\mathrm{T}}=1.5 \mathrm{GeV} / \mathrm{c}$ in semi-central collisions [14,15,31]. A similar behavior was also observed by the STAR Collaboration [32]. Recently, a $v_{2}$ value significantly larger than zero was measured for D mesons at mid-rapidity in $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}[33$, 34]. A complementary measurement at the same energy, provided by the heavy-flavour decay muon elliptic flow at forward rapidity $(2.5<y<4)$, is of great interest in order to provide new constraints for models that implement the heavy-quark interactions with the medium. Finally, the measurement is also important for the interpretation of the $\mathrm{J} / \psi$ elliptic flow results at forward rapidity [35] in terms of a regeneration production from deconfined charm quarks in the medium.

In this Letter, we present the measurement of the elliptic flow of muons from heavy-flavour hadron decays at forward rapidity $(2.5<y<4)$ in $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}$ recorded with the ALICE detector. The elliptic flow is measured using different methods: scalar product [36], two- and four-particle $Q$ cumulants [37,38] and Lee-Yang zeros [39-41]. These methods exhibit different sensitivities to flow fluctuations and correlations not related to the azimuthal asymmetry in the initial geometry (nonflow effects). The $v_{2}$ coefficient is measured as a function of $p_{\mathrm{T}}$ in the interval $3<p_{\mathrm{T}}<10 \mathrm{GeV} / \mathrm{c}$ and in three centrality classes in the range $0-40 \%$. The centrality dependence of $v_{2}$ is presented in the interval $3<p_{\mathrm{T}}<5 \mathrm{GeV} / c$.

The Letter is organized as follows. The ALICE detector, with an emphasis on the muon spectrometer, and the data sample are presented in Section 2. The analysis details, the methods for the $v_{2}$ measurement, the inclusive muon $v_{2}$ determination, the procedure for the subtraction of the background of muons from decays of light-flavour hadrons and the study of systematic uncertainties, are described in Section 3. The $v_{2}$ results for muons from heavyflavour decays are presented in Section 4. The $v_{2}$ measurement in semi-central collisions as well as the published $R_{\mathrm{AA}}$ in central collisions are compared to model calculations in Section 5. Finally, conclusions are given in Section 6.

## 2. ALICE experiment and data sample

The ALICE detector is described in detail in [42,43]. The apparatus is composed of a set of central barrel detectors (pseudorapidity coverage $|\eta|<0.9$ ) located inside a solenoid magnet that generates a field of 0.5 T parallel to the beam direction, a muon spectrometer ( $-4<\eta<-2.5^{1}$ ) and a set of detectors for event characterization and triggering located in the forward and backward $\eta$ regions. The muon spectrometer consists of a passive front absorber made of carbon, concrete and steel, a beam shield, a 3 Tm dipole magnet, tracking chambers, a muon filter (iron wall) and trigger chambers. The muon tracking system is composed of five stations, each including two planes of cathod pad chambers, with the third station inside the dipole magnet. The muon tracking system is completed by four trigger planes of resistive plate chambers downstream of the iron wall, which absorbs hadrons that punch through the front absorber, as well as secondary particles produced inside it and low momentum muons ( $p<4 \mathrm{GeV} / \mathrm{c}$ ).

Two scintillator arrays (V0) covering the pseudo-rapidity intervals $-3.7<\eta<-1.7$ and $2.8<\eta<5.1$ are used for triggering, for collision centrality determination and for beam-induced background rejection. The Zero Degree Calorimeters (ZDC), located at 114 m from the centre of the detector on both sides, can detect spectator protons and neutrons and are also used for the offline rejection of beam-induced background and electromagnetic interactions. The Silicon Pixel Detector (SPD), that composes the two innermost layers of the Inner Tracking System (ITS), is used for the interaction vertex reconstruction. The Time Projection Chamber (TPC), which measures charged-particle tracks with full azimuthal coverage in $|\eta|<0.9$, is used in this analysis for the measurement of the reference particles (Section 3.1).

The results presented in this Letter are obtained from the data sample recorded with ALICE during the $2011 \mathrm{~Pb}-\mathrm{Pb}$ run. The data were collected with a minimum-bias trigger requiring the coincidence of signals in the two V0 arrays in synchronization with the passage of two crossing bunches. In addition, the recorded event sample was enriched with central and semi-central $\mathrm{Pb}-\mathrm{Pb}$ collisions by applying thresholds, at the trigger level, on the V0 signal amplitude. The beam-induced background (beam-gas interactions) was reduced by using the timing information from the V0 and ZDC detectors. Furthermore, a minimal energy deposit in the ZDC was required to reject the contribution from electromagnetic $\mathrm{Pb}-$ Pb interactions. Only events with a reconstructed primary vertex within $\pm 10 \mathrm{~cm}$ from the nominal position of the interaction vertex along the beam direction are analyzed. The $\mathrm{Pb}-\mathrm{Pb}$ collisions are classified according to their degree of centrality by means of the sum of the amplitudes of the signals in the V0 detector and the centrality classes are defined as percentiles of the total hadronic $\mathrm{Pb}-\mathrm{Pb}$ cross section [44]. The analysis is carried out in three centrality classes: $0-10 \%$ (using the sample with trigger on central collisions), $10-20 \%$ and $20-40 \%$ (using the sample with trigger on semi-central collisions). The analyzed data sample corresponds to an integrated luminosity of $11.3 \mu \mathrm{~b}^{-1}$ in the $0-10 \%$ centrality class and of $3.5 \mu^{-1}$ in the other two centrality classes.

## 3. Data analysis

The elliptic flow of muons from heavy-flavour hadron decays, $v_{2}^{\mu \leftarrow \mathrm{HF}}$, is obtained from the measurement of the inclusive muon elliptic flow, $v_{2}^{\mu}$, by subtracting the elliptic flow of muons from pri-

[^1]mary charged pion and kaon decays $v_{2}^{\mu \leftarrow \pi, \mathrm{K}}$ (Sections 3.1 and 3.4), as:
$v_{2}^{\mu \leftarrow \mathrm{HF}}=\frac{v_{2}^{\mu}-f^{\mu \leftarrow \pi, \mathrm{K}} \cdot v_{2}^{\mu \leftarrow \pi, \mathrm{K}}}{1-f^{\mu \leftarrow \pi, \mathrm{K}}}$,
where $f^{\mu \leftarrow \pi, \mathrm{K}}$ is the muon background fraction, defined as the ratio of the yield of muons from primary charged pion and kaon decays to that of inclusive muons. The measurement of the $v_{2}^{\mu \leftarrow \mathrm{HF}}$ coefficient is carried out in the interval $3<p_{\mathrm{T}}<10 \mathrm{GeV} / \mathrm{c}$ in order to limit the systematic uncertainty on the subtraction of the muon background contribution.

### 3.1. Track selection

The selection criteria for particles of interest, muon tracks, are similar to those used in the previous analyses of pp collisions at $\sqrt{s}=2.76 \mathrm{TeV}$ and 7 TeV and $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}$ [21,45]. The tracks are required to be within the geometrical acceptance of the muon spectrometer, with $-4<\eta<-2.5$ and $170^{\circ}<\theta_{\text {abs }}<178^{\circ}$, where $\theta_{\text {abs }}$ is the polar angle measured at the end of the absorber. In order to improve the muon identification, a reconstructed track in the tracking chambers is required to match a track segment in the trigger chambers. This leads to a very efficient rejection of the background produced by charged hadrons, which are absorbed in the iron wall. Furthermore, a cut on the product $p \cdot D C A$ of the track momentum $p$ and distance of closest approach ( $D C A$ ) to the primary vertex is applied to remove the beam-induced background tracks and fake tracks coming from the superposition of several particles crossing the muon spectrometer. Due to multiple scattering in the front absorber, the DCA distribution of tracks coming form the interaction vertex is expected to be described by a Gaussian function, its width being dependent on the absorber material and proportional to $1 / p$. Background tracks have a very broad distribution in $p \cdot D C A$ and are effectively rejected by a cut at $6 \sigma$, where $\sigma$ is extracted from a Gaussian fit to the $p \cdot D C A$ distribution measured in two intervals of $\theta_{\mathrm{abs}}$, corresponding to different materials in the front absorber. The relative momentum resolution of reconstructed tracks varies from about $1 \%$ to $4 \%$ for tracks with momentum between $20 \mathrm{GeV} / \mathrm{c}$ and $100 \mathrm{GeV} / c$. After the cuts are applied, in the region $p_{\mathrm{T}}>3 \mathrm{GeV} / c$ the residual background to heavy-flavour decay muons consists of muons from decays of primary charged pions and kaons ${ }^{2}$ and it amounts to $5-15 \%$, depending on $p_{\mathrm{T}}$ and on collision centrality (Section 3.4).

The mid-rapidity charged-particle tracks used to determine the flow vector $\vec{Q}_{n}$ or the generating function (Section 3.2) are called in the following reference particles. They are defined as tracks measured in the TPC in $|\eta|<0.8$. These are required to have at least 70 associated space points out of the maximum of 159 , a $\chi^{2}$ per degree of freedom (ndf) for the momentum fit in the range $\chi^{2} / \mathrm{ndf}<2$ and a transverse momentum value in the interval $0.2<p_{\mathrm{T}}<5 \mathrm{GeV} / c$. Additionally, tracks are rejected if their distance of closest approach to the primary vertex is larger than 3 cm in the plane transverse to the beam direction or in the longitudinal direction.

### 3.2. Flow analysis methods

The elliptic flow measurement is carried out using various methods that have different sensitivities to flow fluctuations and

[^2]non-flow effects [46]. Flow fluctuations are mainly due to event-by-event fluctuations of the initial density profile, while non-flow effects correspond to correlations not related to the azimuthal anisotropy in the initial state, such as resonance decays, jets and Bose-Einstein correlations between identical particles. It is worth mentioning that, in the present analysis, most of these non-flow effects are strongly suppressed by introducing an $\eta$ gap between reference particles and particles of interest [47]. In this analysis, the scalar product [36], two- and four-particle $Q$ cumulants [37, 38] and Lee-Yang zeros [39-41] methods are employed. The description of these methods will be limited to the features specific to the present analysis. The following notations are introduced: $v_{2}^{\mu(\mu \leftarrow \mathrm{HF})}\{\mathrm{SP}\}$, refers to the measurement using the scalar product, $v_{2}^{\mu(\mu \leftarrow \mathrm{HF})}\{2\}$ and $v_{2}^{\mu(\mu \leftarrow \mathrm{HF})}\{4\}$ correspond to the ones using the two-particle $Q$ cumulants and four-particle $Q$ cumulants, while $v_{2}^{\mu(\mu \leftarrow \mathrm{HF})}\{$ LYZ-Prod $\}$ and $v_{2}^{\mu(\mu \leftarrow \mathrm{HF})}\{$ LYZ-Sum $\}$ are obtained using Lee-Yang zeros with product and sum generating functions. The superscripts $\mu$ and $\mu \leftarrow$ HF refer to inclusive muons and muons from heavy-flavour hadron decays, respectively. It is worth mentioning that these methods are more accurate than the standard event plane method, which yields a measurement lying between the event-averaged mean value and the root-mean-square value in the presence of flow fluctuations [48,49]. Moreover, the multiparticle correlation methods (four-particle $Q$ cumulants and LeeYang zeros) are less affected by non-flow correlations than twoparticle correlation methods, but they cannot be used reliably when the muon flow magnitude is small and when the number of muons is small in the selected phase-space region e.g. in central and peripheral collisions, respectively [37,39]. Under these conditions, the scalar product and two-particle cumulant methods provide a $v_{2}$ measurement in a wider centrality range.

The scalar product method $[36,48]$, derived from the standard event plane technique [48], is based on the measurement of the flow vector $\vec{Q}_{n}$ [36] computed from reference particles. In order to determine the elliptic flow, the $\vec{Q}_{2}$ vector in a given event is expressed as:
$\vec{Q}_{2}=\left(\sum_{j=1}^{N} \cos 2 \varphi_{j}, \sum_{j=1}^{N} \sin 2 \varphi_{j}\right)$,
where $\varphi_{j}$ is the particle azimuthal angle and $N$ is the multiplicity of reference particles.

With this method the 2nd harmonic coefficient is given by:
$v_{2}\{\mathrm{SP}\}=\frac{\left\langle\vec{Q}_{2} \cdot \vec{u}_{2, i}\left(\eta, p_{\mathrm{T}}\right)\right\rangle}{2 \sqrt{\left\langle\vec{Q}_{2}^{\mathrm{A}} \cdot \vec{Q}_{2}^{\mathrm{B}}\right\rangle}}$,
where the brackets in the numerator indicate the average over muons at forward rapidity, in all events. The vector $Q_{2}$ is calculated from Eq. (3) and the vector $\vec{u}_{2, i}=\left(\cos 2 \varphi_{i}, \sin 2 \varphi_{i}\right)$ is the unit vector of the $i$ th muon. In the denominator, each sample of reference particles used to compute $\vec{Q}_{2}$ is divided into two sub-samples of same multiplicity in symmetrical $\eta$ intervals, $-0.8<\eta<-0.5$ and $0.5<\eta<0.8$, separated by a $\eta$ gap of one unit of pseudorapidity, labeled with the superscripts A and B and the brackets correspond to the average over events.

The cumulant technique $[37,38]$ is based on a cumulant expansion of multi-particle azimuthal correlations. Different order cumulants have different sensitivities to flow fluctuations. In the present analysis, two- and four-particle cumulants are used to extract the muon elliptic flow. The results presented in the following are obtained from a direct calculation of multi-particle cumulants performed by using the $Q$-cumulant technique [38], which is based on the moments of the magnitude of the flow vector $\vec{Q}_{2}$. It is
worth mentioning that in this approach the cumulants are not biased by the interferences between various harmonics. The reference elliptic flow values $V_{2}$ evaluated from the 2nd order cumulant $c_{2}\{2\}$ and 4 th order cumulant $c_{2}\{4\}$ with reference particles are given by $V_{2}\{2\}=\sqrt{c_{2}\{2\}}$ and $V_{2}\{4\}=\sqrt[4]{-c_{2}\{4\}}$, respectively. Once the reference elliptic flow is estimated, the muon elliptic flow with respect to the reference elliptic flow is obtained from the 2nd and 4th order cumulants according to:
$v_{2}\{2\}=\frac{d_{2}\{2\}}{V_{2}\{2\}}$ and $v_{2}\{4\}=\frac{d_{2}\{4\}}{V_{2}\{4\}^{3}}$,
where $d_{2}\{2\}$ and $d_{2}\{4\}$ are the 2 nd and 4 th order cumulants of selected muons [38].

The Lee-Yang zeros method [39-41] relies on correlations involving all particles in the event. This is the limit of cumulants when the order of cumulants goes to infinity. The method is based on the location of the zeros in the complex plane, of a generating function of azimuthal correlations, which relates the position of the first minimum of the generating function to the magnitude of the reference elliptic flow $V_{2}$ defined as:
$V_{2} \equiv\left\langle\sum_{j=1}^{M} \cos \left[2\left(\varphi_{j}-\Psi_{2}\right)\right]\right\rangle_{\text {events }}$,
where $M$ is the multiplicity of reference particles and the average is taken over all events. For this purpose, the following complexvalued generating function is evaluated as a function of a positive real variable $r$ and few, typically five, equally spaced reference angles $\vartheta$ (LYZ-Prod method):
$G^{\vartheta}(i r) \equiv\left\langle\prod_{j=1}^{M}\left(1+\operatorname{ir} \cos \left[2\left(\varphi_{j}-\vartheta\right)\right]\right)\right\rangle_{\text {events }}$.
The first positive minimum of $\mid G^{\vartheta}($ ir $) \mid$, denoted as $r_{0}^{\vartheta}$, allows one to estimate $V_{2}^{\vartheta}$, which can be written as $V_{2}^{\vartheta}=j_{01} / r_{0}^{\vartheta}$, where $j_{01} \simeq 2.405$ is the first root of the Bessel function. Once the first minimum $r_{0}^{\vartheta}$ is determined, the differential muon elliptic flow is estimated with respect to the reference flow $V_{2}^{\vartheta}$ as detailed in [41]. Finally, the result is averaged over all $\vartheta$ angles. An alternative form of the generating function provided with the LYZ-Sum method is:
$G^{\vartheta}($ ir $) \equiv\left\langle\exp \left(\operatorname{ir} \sum_{j=1}^{M} \cos \left[2\left(\varphi_{j}-\vartheta\right)\right]\right)\right\rangle_{\text {events }}$.
The version of the method involving a product for the construction of the generation function (Eq. (7)) was designed to disentangle interferences between different harmonics, which is not the case with the generating function using a sum of the individual reference particle contributions. Both generating functions are used in this analysis.

Note that, for all methods, autocorrelation effects are avoided because the particles (muons) used in the determination of the flow are not included in the estimation of the reference flow.

### 3.3. Inclusive muon elliptic flow

The elliptic flow of inclusive muons, $v_{2}^{\mu}$, is studied with twoparticle correlation methods (scalar product and two-particle $Q$ cumulants) in the centrality intervals $0-10 \%, 10-20 \%$ and $20-40 \%$. In the $20-40 \%$ centrality interval, the multi-particle correlation methods (four-particle $Q$ cumulants and Lee-Yang zeros) are also used.

Several sources of systematic uncertainty affecting the muon elliptic flow measurement are considered. These take into account the changes due to the variations of the reference particle selection criteria as in $[33,34,50]$, to allow us to check the robustness of the $v_{2}^{\mu}$ measurement. Since the collision impact parameter distribution could slightly depend on the observable used for the centrality determination, a systematic uncertainty is estimated by repeating the analysis using the number of clusters in the outermost layer of the SPD and the number of tracks in the TPC as centrality estimators, instead of the V0 signal amplitude. The systematic uncertainty due to the effect of TPC tracks from different $\mathrm{Pb}-\mathrm{Pb}$ collisions piled-up in the same recorded event is estimated by applying a tighter cut to remove outliers in the multiplicity distribution of reference particles. This is done by requiring that the centrality values determined using the V0 signal amplitude and the number of TPC tracks do not differ by more than $5 \%$. An additional systematic uncertainty specific to the scalar product is evaluated by varying the $\eta$ gap between the two sub-events from 1 to 0.8 $\eta$-units (see Eq. (4) and [36]). The various systematic uncertainties are added in quadrature. They tend to increase with increasing $p_{\mathrm{T}}$ (see Fig. 1). A summary of the systematic uncertainties, in the interval $3<p_{\mathrm{T}}<4.5 \mathrm{GeV} / \mathrm{c}$, is presented in Table 1.

Fig. 1 shows the $p_{\mathrm{T}}$-differential muon elliptic flow $\left(v_{2}^{\mu}\right)$ in the $0-10 \%, 10-20 \%$ and $20-40 \%$ centrality classes as obtained using the various methods. The values of $v_{2}^{\mu}$ slightly increase from central to semi-central collisions and this effect is more pronounced in the $p_{\mathrm{T}}$ interval $3<p_{\mathrm{T}}<4.5 \mathrm{GeV} / c$. The two-particle correlation methods (scalar product and two-particle $Q$ cumulants) give consistent results over the whole $p_{\mathrm{T}}$ range, indicating that these methods have a similar sensitivity to non-flow effects ${ }^{3}$ and in particular to flow fluctuations. A similar agreement is found when comparing the multi-particle correlation methods (four-particle $Q$ cumulants and Lee-Yang zeros) to each other. No significant difference between the $v_{2}^{\mu}$ results extracted with Lee-Yang zeros using either the sum or product generating function is seen, hence indicating that interferences between harmonics are negligible [51]. Moreover, four-particle $Q$ cumulants give comparable results as Lee-Yang zeros. The four-particle $Q$ cumulants and Lee-Yang zeros are expected to be less affected by non-flow effects than scalar product or two-particle $Q$ cumulants [52]. However, as mentioned non-flow effects are expected to be negligible, even with twoparticle correlation techniques, due to the large $\eta$ between reference particles and inclusive muons. Finally, the central values of $v_{2}^{\mu}$ obtained with four-particle $Q$ cumulants or Lee-Yang zeros are systematically smaller than with two-particle correlation methods, although compatible within uncertainties. Such differences may indicate that initial fluctuations play a role in the development of the final momentum-space anisotropy.

### 3.4. Muon background subtraction

The subtraction of the muon background contribution to the measured $v_{2}^{\mu}$ requires an estimate of the elliptic flow of muons from charged pion and kaon decays, $v_{2}^{\mu \leftarrow \pi, K}$, and of the background fraction, $f^{\mu \leftarrow \pi, K}$ (see Eq. (2)). The determination of the $v_{2}^{\mu \leftarrow \pi, K}$ coefficient requires two steps. First, the $p_{T^{-}}$and $\eta$-differential $v_{2}$ of charged particles measured in $|\eta|<2.5$ by the ATLAS Collaboration in $\mathrm{Pb}-\mathrm{Pb}$ collisions [53] and the $p_{\mathrm{T}}$ distributions of charged pions and kaons measured in $|y|<0.8$ by

[^3]Table 1
Systematic uncertainty sources affecting the inclusive muon elliptic flow measurement in the $0-10 \%, 10-20 \%$ and $20-40 \%$ centrality classes for the interval $3<p_{\mathrm{T}}<4.5 \mathrm{GeV} / c$. They are given as a percentage of the $v_{2}$ value.

| $v_{2}^{\mu}$ analysis | Source | Systematic uncertainty (\%) |  |  |
| :--- | :--- | :---: | :---: | :---: |
|  |  | $0-10 \%$ | $10-20 \%$ | $20-40 \%$ |
| $v_{2}^{\mu}\{\mathrm{SP}\}$ | Reference particles | 3 | 1 | 3 |
|  | Centrality selection | 6 | 1 | 4 |
|  | TPC pile-up | 2 | 4 | 2 |
|  | $\eta$ gap | 13 | 1 | 1 |
|  | Reference particles | 13 | 3 | 2 |
| $v_{2}^{\mu}\{2\}$ | Centrality selection | 14 | 3 | 6 |
|  | TPC pile-up | 8 | 1 | 4 |
|  | Reference particles |  |  | 10 |
|  | Centrality selection |  |  | 1 |
|  | TPC pile-up |  |  | 4 |
|  | Reference particles |  |  | 7 |
|  | Centrality selection |  |  | 2 |
|  | TPC pile-up |  |  | 2 |
|  | Reference particles |  |  | 8 |
|  | Centrality selection |  |  | 2 |



Fig. 1. $p_{\mathrm{T}}$-differential inclusive muon $v_{2}$ in $2.5<y<4$ and various centrality intervals, in $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{S_{\mathrm{NN}}}=2.76 \mathrm{TeV}$. The symbols are placed at the centre of the $p_{\mathrm{T}}$ interval and, for visibility, the points from two-particle $Q$ cumulants and Lee-Yang zeros with product generating function are shifted horizontally. The vertical error bars represent the statistical uncertainty, the horizontal error bars correspond to the width of the bin (not shown for the shifted data points) and the open boxes are the systematic uncertainties. The $p_{\mathrm{T}}$ intervals used with the Lee-Yang zeros method are different with respect to the other methods. Upper panels: results from two-particle correlation flow methods (scalar product and two-particle Q cumulants) in the $0-10 \%$ (left) and $10-20 \%$ (right) centrality intervals. Lower panels: results in the $20-40 \%$ centrality interval from two-particle correlation flow methods (scalar product and two-particle $Q$ cumulants) and from four-particle $Q$ cumulants (left), and from four-particle $Q$ cumulants and Lee-Yang zeros (right).
the ALICE Collaboration in pp and $\mathrm{Pb}-\mathrm{Pb}$ collisions [54,55] are extrapolated to forward rapidity. Then, the $p_{\mathrm{T}}$ distributions of muons from charged pion and kaon decays, needed to estimate $f^{\mu \leftarrow \pi, \mathrm{K}}$ and $v_{2}^{\mu \leftarrow \pi, \mathrm{K}}$, are generated according to a simulation taking into account the decay kinematics and the effect of the front absorber.

The $p_{T^{-}}$and $\eta$-differential elliptic flow of charged particles in $|\eta|<2.5, v_{2}^{\mathrm{ch}}$, is extrapolated to forward rapidity using:
$v_{2}^{\text {ch }}\left(p_{\mathrm{T}}, \eta\right)=F(\eta) \cdot v_{2}^{\text {ch }}\left(p_{\mathrm{T}}, 2<|\eta|<2.5\right)$,
where $v_{2}^{\mathrm{ch}}\left(p_{\mathrm{T}}, 2<|\eta|<2.5\right)$ is the measured charged-particle elliptic flow in $2<|\eta|<2.5$ with the event plane method. Since
the $v_{2}^{\text {ch }}\left(p_{\mathrm{T}}\right)$ measured by the ATLAS Collaboration is affected by statistical fluctuations, it is assumed that in the interval $10<$ $p_{\mathrm{T}}<20 \mathrm{GeV} / c$, needed to simulate the decay muons up to $p_{\mathrm{T}}=$ $10 \mathrm{GeV} / \mathrm{c}, v_{2}^{\mathrm{ch}}$ remains constant with a value given by the one measured in the interval $10<p_{\mathrm{T}}<12 \mathrm{GeV} / \mathrm{c}$. The extrapolation factor $F(\eta)$ is calculated by parameterizing the $\eta$-differential $v_{2}^{\text {ch }}$ measured by the ATLAS Collaboration in various $p_{\mathrm{T}}$ intervals with a second order polynomial. In the interval $7<p_{\mathrm{T}}<20 \mathrm{GeV} / c$, the ATLAS $v_{2}^{\text {ch }}$ does not show a dependence on $\eta$ in $|\eta|<2.5$. Therefore, for $p_{\mathrm{T}}>7 \mathrm{GeV} / c, F(\eta)$ is computed as the average between a flat extrapolation function and the extrapolation factor obtained with the parabolic parameterization in $4<p_{\mathrm{T}}<7 \mathrm{GeV} / c$.

The mid-rapidity charged pion and kaon $p_{\text {T }}$ distributions measured in $\mathrm{Pb}-\mathrm{Pb}$ collisions are extrapolated to forward rapidity using the same strategy as in [21] and summarized in the following. Assuming that the nuclear modification factor $R_{\mathrm{AA}}^{\pi, \mathrm{K}}$ of charged pions and kaons in $\mathrm{Pb}-\mathrm{Pb}$ collisions does not depend on rapidity up to $y=4[21,56]$, the $p_{\text {T }}$ distributions of charged pions and kaons at forward rapidity can be expressed as:
$\frac{\mathrm{d} N_{\mathrm{Pb}}^{\pi, \mathrm{K}}}{\mathrm{d} p_{\mathrm{T}}^{\mathrm{d}} y}=\left\langle T_{\mathrm{AA}}\right\rangle \cdot \frac{\mathrm{d} \sigma_{\mathrm{pp}}^{\pi, \mathrm{K}}}{\mathrm{d} p_{\mathrm{T}} \mathrm{d} y} \cdot\left[R_{\mathrm{AA}}^{\pi, \mathrm{K}}\left(p_{\mathrm{T}}\right)\right]_{y=0}$,
where $\left\langle T_{\mathrm{AA}}\right\rangle$ is the average nuclear overlap function in centrality classes under study, estimated as described in [57]. The systematic uncertainty introduced by the assumption on $R_{\mathrm{AA}}^{\pi, \mathrm{K}}$ will be discussed later. The rapidity extrapolation of the mid-rapidity pion and kaon $p_{\mathrm{T}}$-differential cross sections measured in pp collisions $[21,58]$ is done according to:
$\frac{\mathrm{d}^{2} \sigma_{\mathrm{pp}}^{\pi, \mathrm{K}}}{\mathrm{d} p_{\mathrm{T}} \mathrm{d} y}=\left[\frac{\mathrm{d}^{2} \sigma_{\mathrm{pp}}^{\pi, \mathrm{K}}}{\mathrm{d} p_{\mathrm{T}} \mathrm{d} y}\right]_{y=0} \cdot \exp \left(\frac{-y^{2}}{2 \sigma_{y}^{2}}\right)$,
$\sigma_{y}$ being estimated from Monte-Carlo event generators (see [21] for details).

The elliptic flow of muons from charged pion and kaon decays, $v_{2}^{\mu \leftarrow \pi, \mathrm{K}}$, in $2.5<y<4$ and in various centrality classes, ${ }^{4}$ is obtained by means of fast simulations using $v_{2}^{\mathrm{ch}}\left(\eta, p_{\mathrm{T}}\right)$ given by Eq. (9) and charged pion and kaon $p_{\mathrm{T}}$ distributions as obtained from Eqs. (10)-(11). The absorber effect is accounted for by rejecting the pions and kaons that do not decay within a distance corresponding to one interaction length from the beginning of the absorber. The simulation was repeated twice, considering that charged particles are either all pions or all kaons.

The background fraction, $f^{\mu \leftarrow \pi, \mathrm{K}}$, is calculated as the ratio of the $p_{\mathrm{T}}$-differential yield of muons from charged pion and kaon decays in $2.5<y<4$ obtained in the simulation to the measured $p_{\mathrm{T}}$-differential yield of inclusive muons.

The systematic uncertainties affecting the estimated $v_{2}^{\mu \leftarrow \pi, K}$ are summarized in Table 2. They originate from i) the method used to measure the charged-particle $v_{2}^{\mathrm{ch}}$ in ATLAS, ii) the $\eta$ and $p_{\mathrm{T}}$ extrapolation of $v_{2}^{\mathrm{ch}}$ and iii) the treatment of the charged-particle $v_{2}^{\mathrm{ch}}$ in the fast simulation procedure. As the event plane method was used for the $v_{2}^{\mathrm{ch}}$ measurement in ATLAS, the results range between the mean $\left(\left\langle v_{2}^{\mathrm{ch}}\right\rangle\right)$ and R.M.S. $\left(\sqrt{\left\langle\left(v_{2}^{\mathrm{ch}}\right)^{2}\right\rangle}\right)$ of the true $v_{2}^{\mathrm{ch}}$ values due to fluctuations, depending on the event plane resolution which varies with the collision centrality [49]. According to a Monte-Carlo Glauber model [49], the ratio $\sqrt{\left\langle v_{2}^{2}\right\rangle} /\left\langle v_{2}\right\rangle$ is expected

[^4]Table 2
Systematic uncertainty sources affecting the estimated $v_{2}^{\mu \leftarrow \pi, \mathrm{K}}$ for the interval $3<$ $p_{\mathrm{T}}<10 \mathrm{GeV} / \mathrm{c}$. They are stated as a percentage of the $v_{2}$ value. The given range reflects the dependence on the collision centrality.

| Source | Systematic uncertainty $(\%)$ |
| :--- | :--- |
| Input $v_{2}^{\text {ch }}$ bias | 9 |
| $v_{2}^{\text {ch }} \eta$ extrapolation | $9-12$ |
| $v_{2}^{\text {ch }}$ high $p_{\mathrm{T}}$ extrapolation | $13-15$ |
| $\pi$ and K in fast simulations | $<1$ |

to vary from about 1.06 to 1.15 . Consequently, a conservative systematic uncertainty of $15 \%$ is applied to account for this bias and
 extrapolation of $v_{2}^{\mathrm{ch}}$ is evaluated using several fit functions (first and third order polynomials, and Gaussian function) in the region $p_{\mathrm{T}}<7 \mathrm{GeV} / c$, and for larger $p_{\mathrm{T}}$ values an additional systematic uncertainty due to the extrapolation procedure is considered. The latter is determined by comparing the results obtained with the two extrapolation functions used in the interval $p_{\mathrm{T}}>7 \mathrm{GeV} / c$. The systematic uncertainty due to the assumption on $v_{2}^{\mathrm{ch}}$ in the region $p_{\mathrm{T}}>10 \mathrm{GeV} / \mathrm{c}$ is estimated by varying $v_{2}^{\text {ch }}$ between 0 and the value in $10<p_{\mathrm{T}}<12 \mathrm{GeV} / c$ in the fast simulations. Such uncertainty affects mainly the high $p_{\mathrm{T}}$ region ( $p_{\mathrm{T}}>7 \mathrm{GeV} / c$ ). Finally, the systematic uncertainty obtained by treating charged particles separately as pions and kaons is found to be negligible. The various systematic uncertainty sources are propagated to the estimated $v_{2}^{\mu} \pi \pi, \mathrm{K}$ and added in quadrature.

The systematic uncertainty on $f^{\mu \leftarrow \pi, \mathrm{K}}$, detailed in [21], includes the uncertainty on the generated $p_{\mathrm{T}}$ distributions of muons from charged pion and kaon decays, and the uncertainty on the measured inclusive muon $p_{\mathrm{T}}$ distributions. The former originates from the input charged pion and kaon distributions, the rapidity extrapolation and the absorber effect. The systematic uncertainty on the measured inclusive muon yields contains the systematic uncertainty on detector response, residual mis-alignment and centrality dependence of the efficiency. This gives a total systematic uncertainty on $f^{\mu \leftarrow \pi, \mathrm{K}}$ of about $21 \%$ in the interval $3<p_{\mathrm{T}}<$ $4.5 \mathrm{GeV} / c$ with almost no dependence on the collision centrality. Finally, as done for the measurement of the heavy-flavour decay muon $R_{\mathrm{AA}}$ [21], the systematic uncertainty due to the unknown suppression of charged particles at forward rapidity is calculated by varying $f^{\mu \leftarrow \pi, \mathrm{K}}$ from 0 to two times the estimated value. This corresponds to a variation of $R_{A A}^{\pi, K}\left(p_{T}\right)$ at forward rapidity from 0 up to two times $\left[R_{A A}^{\pi, K}\left(p_{T}\right)\right]_{y=0}$. This systematic uncertainty amounts to $10-30 \%$ in the interval $3<p_{\mathrm{T}}<4.5 \mathrm{GeV} / c$, depending on the collision centrality and the flow analysis method.

Fig. 2 presents the estimated background elliptic flow ( $v_{2}^{\mu \leftarrow \pi, K}$, left) and background fraction ( $f^{\mu \leftarrow \pi, \mathrm{K}}$, right) as a function of $p_{\mathrm{T}}$ in the $0-10 \%, 10-20 \%$ and $20-40 \%$ centrality classes. The open boxes represent the systematic uncertainties previously discussed, except for the systematic uncertainty due to the unknown suppression of charged particles at forward rapidity which is treated separately. The estimated $v_{2}^{\mu \leftarrow \pi, \mathrm{K}}$ and $f^{\mu \leftarrow \pi, \mathrm{K}}$ decrease with increasing $p_{\mathrm{T}}$. A decreasing trend of the magnitude of $v_{2}^{\mu \leftarrow \pi, \mathrm{K}}$ from semi-central collisions towards central collisions is also observed.

Finally, the systematic uncertainty on the elliptic flow of muons from heavy-flavour decays, $v_{2}^{\mu \leftarrow \mathrm{HF}}$, contains two contributions: the systematic uncertainties on $v_{2}^{\mu}, v_{2}^{\mu \leftarrow \pi, \mathrm{K}}$ and $f^{\mu \leftarrow \pi, \mathrm{K}}$ propagated according to the definition of $v_{2}^{\mu \leftarrow \mathrm{HF}}$ given in Eq. (2), and the systematic uncertainty due to the unknown suppression of charged particles at forward rapidity. The final systematic uncertainty on $v_{2}^{\mu \leftarrow \mathrm{HF}}$ is obtained by adding in quadrature the two contributions.

 at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}$. The symbols are placed at the centre of the $p_{\mathrm{T}}$ interval and, for visibility, the points for the centrality classes $10-20 \%$ and $20-40 \%$ are shifted horizontally. The horizontal error bars correspond to the width of the bin (not shown for the shifted values) and the open boxes are the systematic uncertainties. See the text for details.


Fig. 3. $p_{\mathrm{T}}$-differential elliptic flow of muons from heavy-flavour decays, $v_{2}^{\mu \leftarrow \mathrm{HF}}$, in $2.5<y<4$ and various centrality intervals, in $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}$. The symbols are placed at the centre of the $p_{\mathrm{T}}$ interval and, for visibility, the points from two-particle $Q$ cumulants and Lee-Yang zeros with product generating function are shifted horizontally. The meaning of the symbols is the same as in Fig. 1. The horizontal error bars are not plotted for shifted data points. The $p_{\mathrm{T}}$ intervals used with the Lee-Yang zeros method are different with respect to the other methods. Upper panels: results from two-particle correlation flow methods (scalar product and two-particle $Q$ cumulants) in the $0-10 \%$ (left) and $10-20 \%$ (right) centrality intervals. Lower panels: results in the $20-40 \%$ centrality interval from two-particle correlation flow methods (scalar product and two-particle $Q$ cumulants) and from four-particle $Q$ cumulants (left), and from four-particle $Q$ cumulants and Lee-Yang zeros (right). See the text for details.

It amounts to about $12 \%-36 \%$ in the interval $3<p_{\mathrm{T}}<4.5 \mathrm{GeV} / c$, depending on the collision centrality and the flow analysis method.

## 4. Results

Fig. 3 presents the $p_{\mathrm{T}}$-differential elliptic flow of muons from heavy-flavour hadron decays, $v_{2}^{\mu \leftarrow \mathrm{HF}}$, calculated with Eq. (2). The results are shown for the $0-10 \%$ (upper, left), $10-20 \%$ (upper, right) and $20-40 \%$ (bottom) centrality classes using the same flow methods as for the measurement of the inclusive muon elliptic flow
(Fig. 1). When comparing the results to those obtained for inclusive muons (Fig. 1), one can notice that $v_{2}^{\mu \leftarrow \mathrm{HF}}$ and $v_{2}^{\mu}$ are similar due to the small background fraction (5\% to $15 \%$ ) in the $p_{T}$ interval $3-10 \mathrm{GeV} / c$. The differences between the various methods are similar to those discussed for the measurement of the inclusive muon $v_{2}^{\mu}$ i.e. i) scalar product and two-particle $Q$ cumulants give compatible results, ii) consistent results are also found with four-particle $Q$ cumulants and Lee-Yang zeros, and iii) the $v_{2}^{\mu} \leftarrow \mathrm{HF}$ values extracted from these multi-particle correlation methods are smaller, although still compatible within un-


Fig. 4. Elliptic flow of muons from heavy-flavour hadron decays as a function of the collision centrality in $2.5<y<4$ and $3<p_{\mathrm{T}}<5 \mathrm{GeV} / \mathrm{c}$, in $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{s_{\mathrm{NN}}}=2.76 \mathrm{TeV}$. The results are obtained with scalar product and two-particle $Q$ cumulants. Vertical bars (open boxes) represent the statistical (systematic) uncertainty, the horizontal error bars correspond to the width of the centrality bin. For visibility, the points from scalar product are shifted horizontally and the horizontal error bars are not plotted.
certainties, than the ones obtained with two-particle correlation methods. As mentioned in Section 3.3, such differences are expected if initial-state fluctuations play a role in the development of the final momentum-space anisotropy.

A positive $v_{2}^{\mu \leftarrow H F}$ is observed at intermediate $p_{\mathrm{T}}$ for the $20-40 \%$ and $10-20 \%$ centrality classes with a significance larger than $3 \sigma$ when combining statistical and systematic uncertainties. In the $20-40 \%$ centrality class, the values of the significance in the interval $3<p_{\mathrm{T}}<4 \mathrm{GeV} / \mathrm{c}\left(4<p_{\mathrm{T}}<5.5 \mathrm{GeV} / \mathrm{c}\right)$ are $4 \sigma(3.2 \sigma)$ and $4.3 \sigma(3.8 \sigma)$ with scalar product and two-particle $Q$ cumulants, respectively. In the $10-20 \%$ centrality class and in the interval $3<p_{\mathrm{T}}<4.5 \mathrm{GeV} / c$, the values of the significance correspond to $4.4 \sigma$ both with scalar product and two-particle $Q$ cumulants. This behavior results from the interplay between the significant interaction of heavy quarks with the expanding medium and the pathlength dependence of in-medium parton energy loss $[29,30]$. The $v_{2}^{\mu \leftarrow H F}$ of muons from heavy-flavour hadron decays decreases with increasing $p_{\mathrm{T}}$ and becomes compatible with zero in the high $p_{\mathrm{T}}$ region.

Fig. 4 shows the centrality dependence of the elliptic flow of muons from heavy-flavour hadron decays in the interval $3<p_{\mathrm{T}}<$ $5 \mathrm{GeV} / c$. It is investigated with scalar product and two-particle $Q$ cumulants, which can be applied in a wider event-multiplicity (i.e. centrality) interval compared to multi-particle correlation methods. A significant decrease of the $v_{2}$ magnitude towards central collisions is observed. This is expected from the decrease of the initial spatial anisotropy from semi-central to central collisions.

ALICE has measured the elliptic flow of prompt $D$ mesons in $|y|<0.8$ in three centrality classes in the interval $0-50 \%$ with various two-particle correlation methods [33,34]. Similar trends as those reported here for muons from heavy-flavour decays are observed, although in different $p_{\mathrm{T}}$ and rapidity intervals. In particular, a positive $v_{2}$ was observed for D mesons in semi-central collisions in $2<p_{\mathrm{T}}<6 \mathrm{GeV} / \mathrm{c}$ with a significance of $5.7 \sigma$.

The positive elliptic flow of muons from heavy-flavour hadron decays has been observed in a $p_{\mathrm{T}}$ interval from 3 to about $5 \mathrm{GeV} / c$ where the charm contribution is expected to be dominant with respect to the beauty component according to perturbative QCD calculations [21]. This measurement supports the interpretation of the $\mathrm{J} / \psi$ positive $v_{2}$ at forward rapidity [35] in terms of a significant contribution to $\mathrm{J} / \psi$ production from recombination of flowing charm quarks in the deconfined medium.

## 5. Comparison with models

The results presented in this publication may constrain models describing the interactions of heavy quarks with the medium via elastic (collisional) and inelastic (radiative) processes, and in particular the parton energy loss dependence on the path-length within the medium.

The elliptic flow coefficient and the nuclear modification factor of muons from heavy-flavour hadron decays [21] are compared to the following three models. The MC@sHQ + EPOS transport model [59] treats the propagation of heavy quarks in the medium including collisional and radiative energy loss, within a $3+1$ dimensional fluid dynamical expansion based on the EPOS model [60,61]. The hadronization of heavy quarks takes place at the transition temperature via recombination at low $p_{\text {T }}$ and fragmentation at intermediate and high $p_{T}$. The final-state hadronic interactions are not included in the model. TAMU [62] is a transport model including only collisional processes via the Langevin equation. The hydrodynamical expansion is constrained by $p_{\mathrm{T}}$ spectra and elliptic flow data of light-flavour hadrons. The hadronization is modeled including a component of recombination of heavy quarks with light-flavour hadrons in the QGP. The diffusion of heavy-flavour mesons in the hadronic phase is also included. BAMPS [63-65] is a partonic transport model based on the Boltzmann approach to multi-parton scatterings. It includes collisional processes with a running strong coupling constant. The lack of radiative contributions is accounted for by scaling the binary cross section with a correction factor, tuned to describe the nuclear modification factor and elliptic flow results at RHIC energies. Vacuum fragmentation functions are used for the hadronization.

Fig. 5 shows a comparison of the three models with the measurement of the $p_{\mathrm{T}}$-differential elliptic flow of muons from heavy-flavour hadron decays in the $20-40 \%$ centrality class (upper panel) and of the $p_{\mathrm{T}}$-differential nuclear modification factor of muons from heavy-flavour hadron decays in the $0-10 \%$ centrality class [21] (lower panel). In the interval $3<p_{\mathrm{T}}<5 \mathrm{GeV} / c$, the BAMPS model describes the $v_{2}^{\mu \leftarrow H F}$ data within uncertainties, while the TAMU and MC@sHQ+EPOS models give $v_{2}^{\mu \leftarrow H F}$ values lower than the data. The three models describe the $v_{2}^{\mu \leftarrow H F}$ data at higher $p_{\mathrm{T}}$, although the sizeable experimental uncertainties affect the significance of the comparison. The BAMPS model tends to slightly underestimate the $R_{\text {AA }}$ of muons from heavy-flavour decays in the $10 \%$ most central collisions, while the MC@sHQ+EPOS


Fig. 5. Upper panel: $p_{\mathrm{T}}$-differential elliptic flow of muons from heavy-flavour hadron decays in $2.5<y<4$, in $\mathrm{Pb}-\mathrm{Pb}$ collisions at $\sqrt{S_{\mathrm{NN}}}=2.76 \mathrm{TeV}$ for the centrality class $20-40 \%$ compared to various transport model predictions: MC@sHQ + EPOS [59-61], TAMU [62] and BAMPS [63-65]. The TAMU model is shown with a theoretical uncertainty band. Lower panel: $p_{\mathrm{T}}$-differential $R_{\mathrm{AA}}$ of muons from heavy-flavour hadron decays for the centrality class $0-10 \%$ from [21] compared to the same models as for $v_{2}^{\mu \leftarrow H F}$.
model tends to overestimate it. The TAMU model describes the $R_{\mathrm{AA}}$ measurement over the entire $p_{\mathrm{T}}$ interval within uncertainties. These comparisons indicate that it is challenging to simultaneously describe the strong suppression of high- $p_{\mathrm{T}}$ muons from heavy-flavour hadron decays in central collisions and the azimuthal anisotropy in semi-central collisions. Similar trends are also observed in the mid-rapidity region from the comparison of the $R_{\text {AA }}$ and $v_{2}$ of D mesons with model calculations [34].

## 6. Conclusions

In summary, we have reported on a measurement of the elliptic flow of muons from heavy-flavour hadron decays at forward rapidity in central and semi-central Pb-Pb collisions at $\sqrt{S_{\mathrm{NN}}}=2.76 \mathrm{TeV}$ with the ALICE detector at the LHC.

Measurements have been carried out using several methods which exhibit different sensitivity to initial-state fluctuations and non-flow correlations. The systematic comparison of scalar product, two- and four-particle $Q$ cumulants and Lee-Yang zeros helps in understanding the processes that build up the observed differences between two-particle correlation methods and multi-particle correlation methods and suggests that flow fluctuations are significant.

The magnitude of the elliptic flow of muons from heavy-flavour hadron decays increases from central to semi-central collisions and
decreases with increasing $p_{\mathrm{T}}$, becoming compatible with zero at high $p_{\mathrm{T}}$. The results indicate a positive elliptic flow with the scalar product and two-particle $Q$ cumulants in semi-central collisions ( $10-20 \%$ and $20-40 \%$ centrality classes) for the $p_{\mathrm{T}}$ interval from 3 to about $5 \mathrm{GeV} / c$ with a significance larger than $3 \sigma$. The elliptic flow in semi-central collisions and the previously published nuclear modification factor in the $10 \%$ most central collisions were compared with transport model calculations. These comparisons show that a simultaneous description of $R_{\mathrm{AA}}$ and $v_{2}$ over the whole $p_{\mathrm{T}}$ interval remains a challenge. The results reported in this Letter in various centrality classes may provide further important constraints to the models.

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[^1]:    ${ }^{1}$ In the ALICE reference frame, the muon spectrometer covers a negative $\eta$ range and consequently a negative $y$ range. In the following, given that the colliding system is symmetric, the results are presented with a positive $y$ notation.

[^2]:    ${ }^{2}$ Note that the contribution of muons from secondary light hadron decays produced inside the front absorber is negligible for $p_{\mathrm{T}}>3 \mathrm{GeV} / \mathrm{c}$ [45].

[^3]:    ${ }^{3}$ Note that, in this analysis, most non-flow correlations are suppressed, even with two-particle correlation methods since reference particles and inclusive muons are separated by at least $1.7 \eta$-units. However, it is worth mentioning that the main difference between the two methods is the $\eta$ gap between the two sub-samples used to compute $\vec{Q}_{2}$ (Eq. (4)) which also allows to partly remove non-flow effects.

[^4]:    ${ }^{4}$ The $v_{2}^{\mu} \leftarrow \pi, \mathrm{K}$ of muons from charged pion and kaon decays in the $20-40 \%$ centrality class is then obtained from the mean of the charged-particle $v_{2}$ in $20-30 \%$ and $30-40 \%$ centrality classes, with an additional systematic uncertainty provided by the difference with respect to the results in these two centrality classes.

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