2   Heterogeneity among species and

3   community dynamics – Norwegian bird

4   communities as a case study.

5

6   Erik B. Solbu[1], Ola H. Diserud[2*], John A. Kålås[2] and Steinar Engen[3]

7   * Corresponding author. OHD: orcid.org/0000-0002-7331-3230. ola.diserud@nina.no

8

9   [1] Dept. of Biology, Centre for Biodiversity Dynamics, Norwegian University of Science and

10   Technology, NO-7491 Trondheim, Norway.

11   [2] Norwegian Institute for Nature Research, P.O. Box 5685 Torgard, NO-7485 Trondheim,

12   Norway

13   [3] Dept. of Mathematical Sciences, Centre for Biodiversity Dynamics, Norwegian University of

14   Science and Technology, NO-7491 Trondheim, Norway.

15   EBS: orcid.org/0000-0002-6023-3100. erikbsolbu@protonmail.com

16   JAK: john.kalas@nina.no

17   SE: steinar.engen@math.ntnu.no

Abstract

We have in this study analysed bird communities across Norway with a heterogeneous species abundance model, where dynamical parameters can vary among species. Similarity in community composition over time, used as a measure of temporal β-diversity or the turnover rate, was then estimated. When we account for heterogeneity in dynamical parameters among species it will affect how we estimate environmental stochasticity, and, subsequently, how the temporal dynamics is modelled. In addition, spatial variation in species abundance within a sampling area can obscure the temporal dynamics of communities. By inadvertently including small-scale spatial variation within sampling areas in the sample noise term, it will be difficult to correctly detect changes in community structure, or species abundance similarity, in time. Using Norwegian bird communities as a case study, we have shown how to interpret the sample correlation of the bivariate Poisson lognormal distribution, fitted to pairs of transects, and why separation of the transects into spatially similar subgroups can be beneficial. This approach also makes us able to account for sampling error and over-dispersion relative to Poisson sampling. The partitioning of the variance of the species abundance distributions showed that heterogeneity among species in temporal dynamics accounted for roughly 75% of the variation, close to estimates for other taxa. High temporal similarity can be interpreted as a low baseline turnover rate, which is important when studying changes to ecosystems due to e.g. anthropogenic effects. Furthermore, the environmental stochasticity was more realistically estimated in this heterogeneous model. This is essential for predicting the dynamics of species abundances forward in time.

Keywords: β-diversity, environmental stochasticity, heterogeneous species abundance models, over-dispersion, temporal community dynamics.

1. Introduction

42

43 Understanding how human activities affect biodiversity is a key issue in community ecology.

44 However, even without human interference, fluctuations in species abundance, extinctions

45 and speciations change biodiversity naturally, and this baseline turnover rate needs to be

46 accounted for when analysing species communities and how they change (Magurran 2016).

47 One measure for the turnover rate in communities is the similarity in species' abundances

48 over time. Communities where species change considerably in relative abundance from one

49 year to the next will have a high turnover rate, while if the species have almost the same

50 relative abundance over time the turnover rate will be low. This difference in community

51 dynamics can be described by introducing the concept of community heterogeneity. If

52 species in a community have different temporal dynamics, this heterogeneity can be

53 modelled by letting population dynamical parameters vary among species (Engen and Lande

54 1996; Solbu et al. 2016). Conversely, in a homogeneous community, the parameters

55 describing the dynamics are assumed to be equal for all species. Here, community

56 heterogeneity is defined as the variation in carrying capacity among species (Engen et al.

57 2002), introduced in the model by assuming that the species' growth rates are a sample

58 from some distribution. The proportion of the total variation in the observed species

59 abundance distribution that can be attributed to heterogeneity will then be a measure of the

60 community's temporal turnover rate. If heterogeneity accounts for a large part of the

61 variation in species abundances, the turnover rate will be low, whereas a community with

62 low levels of heterogeneity will have a high turnover rate.

63

64   In addition to a baseline turnover rate, the plethora of different measures of biodiversity and

65   different spatial resolutions breed conflicting results in terms of consequences of human-

66   induced changes (McGill et al. 2015). Several considerations regarding sampling design

67   should be made before samples to analyse species diversity and abundance are collected

68   (Bonar et al. 2011). One important issue to consider, when conducting biodiversity analysis,

69   is the choice of sampling unit. A common sampling unit is counting individuals along line

70   transects. Ideally, these transects should be randomly distributed within the area where the

71   community of interest is analysed. However, it is often not physically possible to randomly

72   distribute transects due to the topography of the area, e.g. steep hills, thick vegetation or

73   rivers, and instead the transects follow trails already in the landscape. Or the sampling may

74   have been designed to study spatial structures in species diversity as well as temporal

75   dynamics, thereby distributing sampling units along gradients. The analysis presented here

76   illustrates how spatial variation between sampling units, intentional or not, can affect the

77   estimation of temporal heterogeneity in bird communities.

78

79   The proportion of variation in the species abundance distribution that can be attributed to

80   community heterogeneity is estimated by the correlation between sampling units over time.

81   If species abundances from sampling units within an area the same year are dissimilar, i.e. a

82   species having high abundance in one transect can have low abundance in the other

83   transect, this spatial dissimilarity will obscure analyses of temporal dynamics. It is then

84   crucial to know how to separate the effect of spatial variation from temporal heterogeneity

85   in spatiotemporal species abundance data sets. We show how within-year comparison of

86   correlation between transects can be used to estimate spatial variation that needs to be

87   under control when studying temporal dynamics and community heterogeneity.

88

89   The choice of species to include in the samples, i.e. our prior definition of the community,

90   will affect a similarity analysis, although some species may not have a large influence on the

91   estimated community dynamics. Individuals could, for instance, belong to species that are

92   not endemic to the area and can, therefore, introduce variation in the species abundance

93   distribution that is not necessarily true for the assessment of the local community dynamics,

94   thereby also affecting the estimated turnover rate. As an illustration, we will compare the

95   analysis of a community including all registered bird species with a community including only

96   passerine birds and discuss how the difference in community limitation may affect the

97   estimated spatial variation and temporal heterogeneity of the community.

98

99   Our approach is to fit a bivariate Poisson lognormal species abundance distribution to all

100   pairs of transects within an area and estimate the correlation among transects within the

101   same year, and then study how the correlation changes with increasing time difference

102   between transects. The use of the lognormal distribution has a long history in community

103   ecology (Preston 1948) and the Poisson sampling of this distribution is well known (Bulmer

104   1974). A species abundance distribution described by a Poisson lognormal distribution can

105   be modelled by a continuous time dynamic population model with a Gompertz type of

106   density regulation, which can also account for different temporal dynamics among species

107   (Engen and Lande 1996). The difference in temporal dynamics in this model, i.e. the degree

108   of community heterogeneity, can be attributed to variation in the carrying capacity among

109 species; some species fluctuate at high abundances while others remain at low abundances

110 over time. Species having different carrying capacities can be generated by niche segregation

111 (Hutchinson 1957; MacArthur 1960), but we do not attempt to test this theory formally

112 here. However, heterogeneity among species does deviate from the assumptions in the

113 neutral theory of community dynamics where species are assumed to have the same

114 dynamics, and population fluctuations are caused by demographic stochasticity only

115 (Hubbell 2001).

116

2. Material and Methods

2.1 Sampling design

119 The data we analyse have been collected since the early 1990s to document long-term

120 changes in Norwegian wildlife. Seven different areas were selected across Norway to cover a

121 wide range of climatic variation (Fig. 1A). Areas in the southern part of Norway have

122 historically been more exposed to pollution and while there is farming in some of the areas,

123 they are otherwise considered undisturbed habitats. Although data have been collected for a

124 wide range of plant and mammal species, we will here limit the community to consist of bird

125 species only. Within each area, several sampling points along transects have been used to

126 count the abundance of each species by listening for bird song. There are ten transects

127 within each area, except for Møsvatn which has eight. Each transect has usually 20

128 observation points with 200-300 m distance, but this number can vary in some areas due to

129 landscape constraints, for example in Solhomfjell (Fig. 1C). We use the transect as sampling

130 unit because the observer conducting the census along a transect corrected for observations

131 of the same individuals made at adjacent points, and we illustrate the applicability of the

Solbu, Erik Blystad; Diserud, Ola Håvard; Kålås, John Atle; Engen, Steinar.
Heterogeneity among species and community dynamics – Norwegian bird communities as a case study. Ecological Modelling 2018 ;Volum 388. s. 13-23
10.1016/j.ecolmodel.2018.09.008 CC-BY-NC-ND

132   method to data where the researcher only has information at the transect level. An

133   alternative design is to aggregate the points with respect to some covariate such as

134   elevation or vegetation, but we show that even with such potential underlying differences in

135   spatial composition, informative results can be obtained.
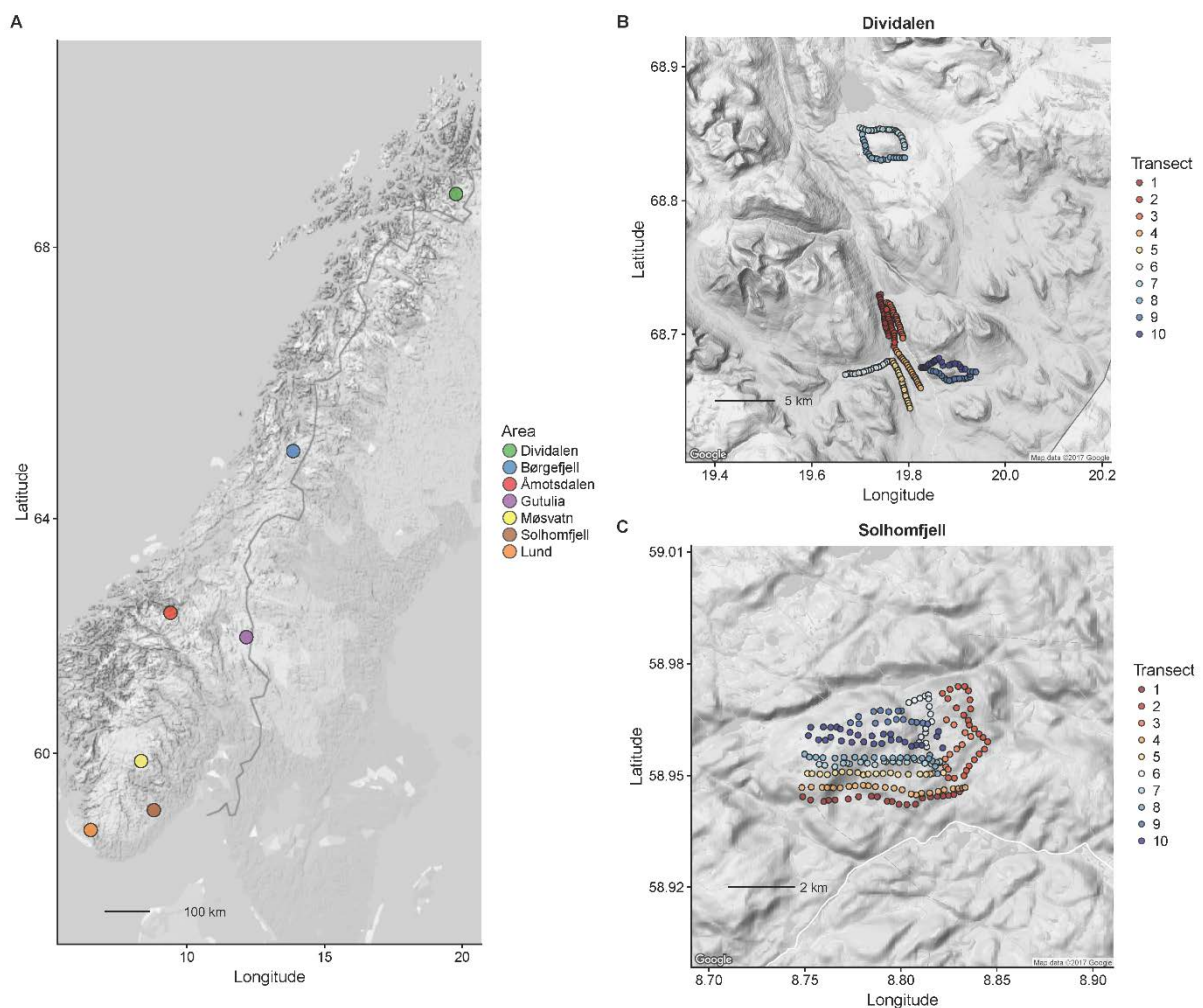
136

137   **Figure 1.** (A) Location of the seven areas where sampling has been conducted. (B) Location

138   of the sampling points for each transect in Dividalen. (C) Location of the sampling points for

139   each transect in Solhomfjell. The transects have been ordered according to mean elevation

140   from low (1) to high (10). Note that there is a considerable difference between the spatial

141   scales in the maps of Dividalen and Solhomfjell.

142

2.2 Spatial variation

144   As the locations of the areas cover the entire span of Norway, there is considerable spatial

145   variation both within and between areas in terms of sampling area size (Fig. 1B and 1C),

146   elevation (Fig. 2) and vegetation (Fig. 3). The transects in Dividalen cover an area of roughly

147   250 square kilometres (Fig. 1B), while the area covered in Solhomfjell is roughly 20 square

148   kilometres (Fig. 1C). The difference in the area covered by the transects in Dividalen and

149   Solhomfjell could indicate a greater variation in the species found among the transects in

150   Dividalen compared to those found in Solhomfjell. The elevation of each sampling point

151   varies both within and between areas (Fig. 2). While the overall mean elevation in Dividalen

152   and Solhomfjell is roughly the same, circa 500 meters, the difference between the lowest

153   and highest points (the range) within the areas is twice as large in Dividalen compared to

154   Solhomfjell. Lund has an overall mean elevation and range similar to Solhomfjell. Børgefjell

155   and Gutulia differ in their overall mean elevation, but have the same range, while

156   Åmotsdalen and Møsvatn have the same overall mean, but differ in range.

157
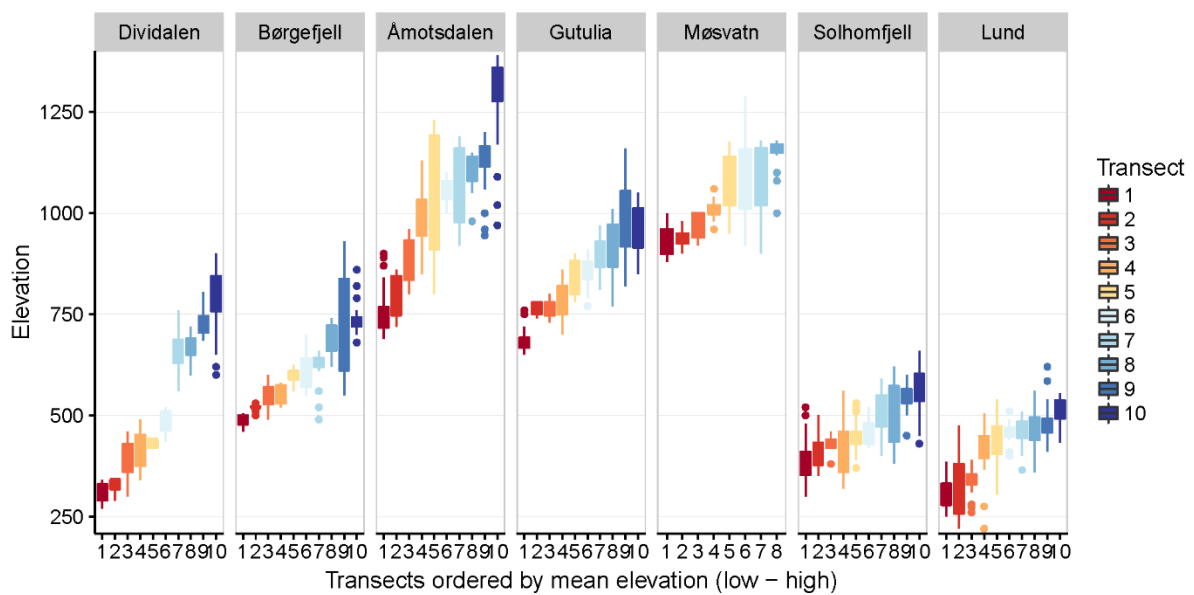
Figure 2. Elevation distribution of the sampling points within each area, where the transects

159   are ordered by their mean elevation from low (1) to high (10).

160

161 Each sampling point has been classified to a vegetation category, so aggregating the

162 proportion of each vegetation class within transects can illustrate the spatial variation within

163 a sampling area. Comparing the distribution of vegetation classes between Dividalen and

164 Solhomfjell reveals some interesting features of the sampling areas (Fig. 3). First, the

165 individual transects in Dividalen have little variation, they have roughly five classes each,

166 while the transects in Solhomfjell have around ten classes each. Part of the reason for the

167 greater variation within transects in Solhomfjell is the number of observation points, but the

168 number of classes is almost constant for each transect, even though the number of points

169 varies. Second, the difference between the measured characteristics is greater in Dividalen

170 than Solhomfjell. For instance, transects one to six in Dividalen have more forest vegetation

171 in common, such as conifers, lichens and birches, while the four other transects have more

172 open vegetation consisting of graminoid ridges, heather and grasses. In Solhomfjell on the

173 other hand, all transects consist of some type of coniferous or birch forest in addition to

174 some areas of bryophyte.

175

176 Knowing the spatial variation in each area is essential when we estimate the temporal

177 autocorrelation of the community, which in turn gives us an estimate of the heterogeneity

178 among species in dynamical parameters. When there is spatial variation among sampling

179 units, either due to suboptimal sampling designs or if sampling is designed with an intention

180 to study spatial diversity, it will obscure temporal autocorrelation among samples over time

181 if not handled appropriately. The available spatial information will be used as guidance when

182   determining how to analyse the transects to minimize the effect of spatial variation on

183   temporal estimates and predictions.
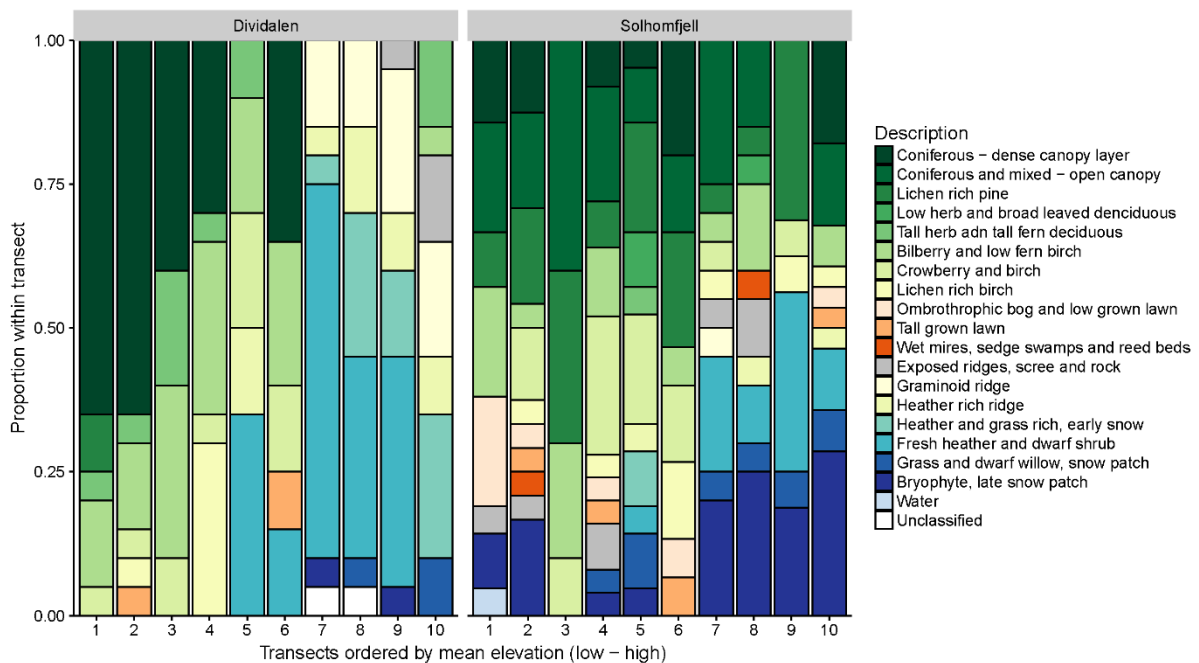
184

185   **Figure 3**. Vegetation description and distribution within transects in Dividalen and

186   Solhomfjell.

187

188   We first look at the spatial variation in species abundances for the censuses from the areas

189   Dividalen and Solhomfjell, before doing the temporal analyses in the next section. The

190   species abundance distribution in the first census year in Dividalen (Fig. 4A) is characterized

191   by a variation like that found in the elevation and vegetation descriptions. Starting from the

192   transect with the lowest mean elevation (300 m), there are five species that are most

193   abundant (*Carduelis flammea*, *Fringilla montifringilla*, *Phoenicurus phoenicurus*, *Phylloscopus*

194   *trochilus* and *Turdus illacus*), but as the mean elevation increases, their presence, in addition

195   to many of the less abundant species, decreases or ceases completely (from 650 m and up),

196   except one species (*Carduelis flammea*). Instead, two other species become more abundant

197 (*Anthus pratensis* and *Pluvialis apricaria*) in addition to several other less abundant species

198 not found at the lower altitudes. The species abundances in the first census year in

199 Solhomfjell (Fig. 4B) have a different development among transects. The abundances in each

200 transect are more similar, with three species (*Anthus trivalis*, *Fringilla coelebs* and

201 *Phylloscopus trochilus*) dominating across all transects, and the less abundant species do not

202 vary much in their presence between transects.

203

204 The community of study can be defined in many ways, both with respect to spatial and taxonomic

205 limitations, and this may affect the results of the analyses. For example, will a community limited to

206 bird species from one taxonomic order give different dynamic models than if all bird species are

207 studied simultaneously? When different community definitions severely change relative abundances

208 in the sample, model results will, of course, be affected, but limiting the community to closely related

209 species competing for the same resources may give a more focused analysis of the degree of

210 heterogeneity. The more abundant species in both study areas are all from the Passeriformes order,

211 so analysing a community where low abundance non-passerine species are removed (names

212 marked with a star (*), Fig. 4) can serve as an illustration of the sensitivity of this modelling

213 approach to community limitation and handling of species that are rare in the sample.
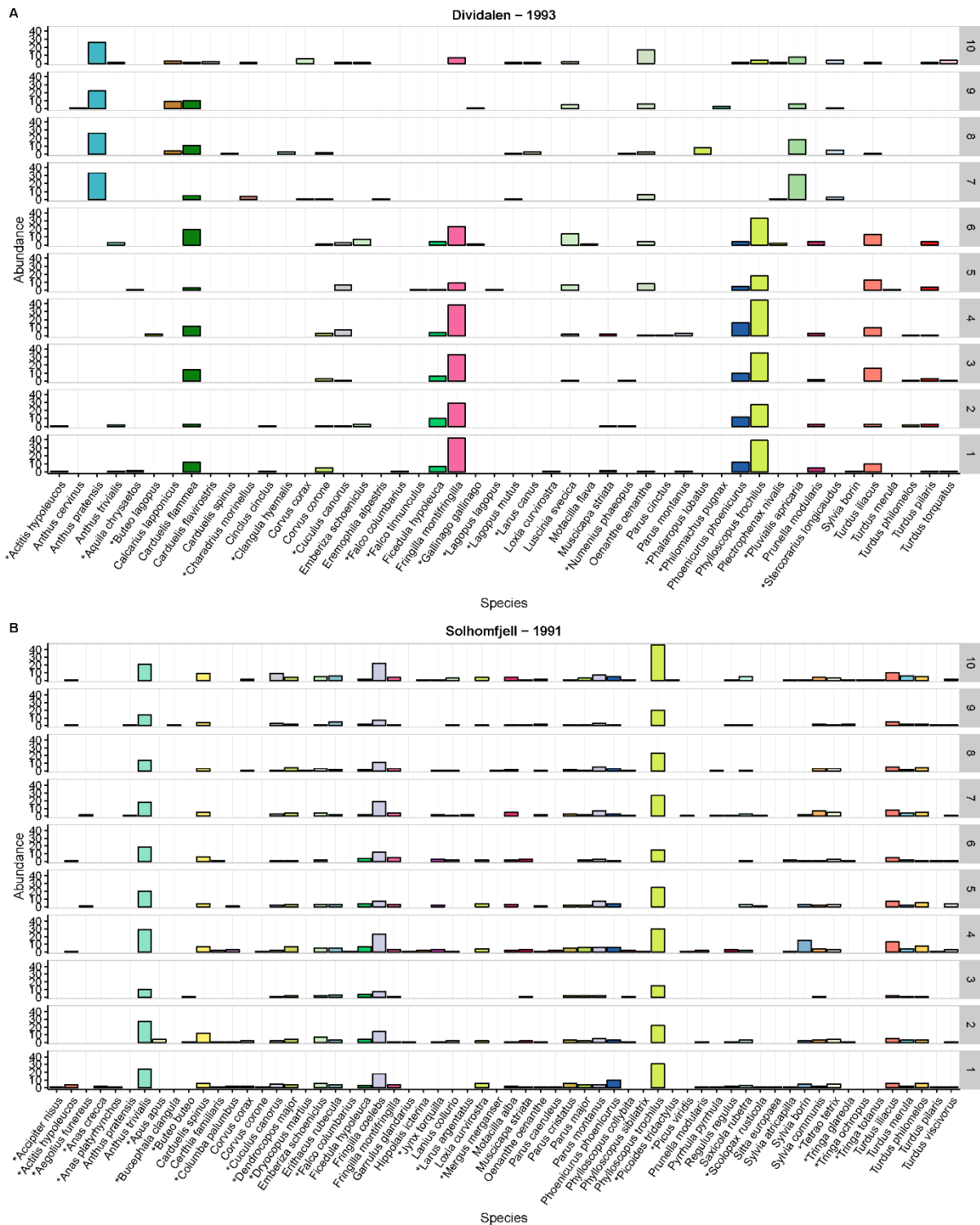
Figure 4. Species abundance observed in Dividalen in 1993 (A) and Solhomfjell in 1991 (B), i.e. at the first available census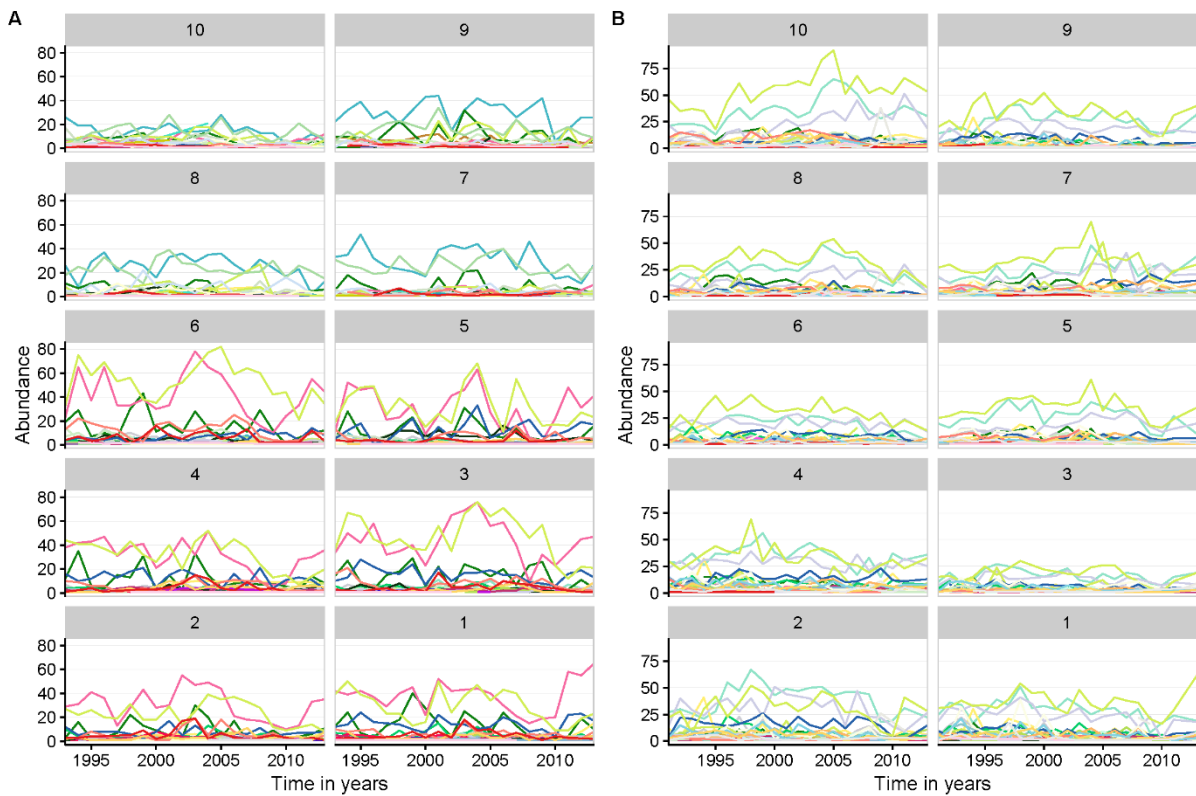 year, aggregated at transect level. The transects have been ordered by their mean elevation from low (1) to high (10). Species marked with a star (*) are the non-passerine species.

219

2.3 Temporal analyses

221 Since one goal is to identify the temporal covariation of species abundance, the spatial

222 variation in species abundance, like the one observed in Dividalen, will be an issue if the

223 pattern persists over time. If all the transects within an area are compared, a large habitat

224 variation among transects will decrease the estimated temporal correlation if species occupy

225 specific habitats. Time series of the species abundances within each transect over all census

226 years up to 2013 in Dividalen (Fig. 5A) and Solhomfjell (Fig. 5B), show that the species that

227 were the most abundant in the first years of the census continue their dominance over time.

228 The total abundance is higher among the transects at low altitudes in Dividalen (transects 1 -

229 6, Fig. 5A), compared to those at higher elevations. The temporal heterogeneity in species

230 abundance dynamics in Solhomfjell is slightly more obscured, but the most abundant species

231 persist over time and there is no variation among the transects in terms of which species are

232 most dominant, but there is considerable variation in total abundance. The difference in

233 total abundance among transects in Solhomfjell can be explained by the number of

234 observation points within each transect, for example, transect 3 has 10 points, compared to

235 transect 10 which has 28 points.

Figure 5. Species abundance for each species (coloured lines) observed in Dividalen (A) and

Solhomfjell (B) over the whole census period, aggregated at transect level. The transects

have been ordered by their mean elevation from low (1) to high (10). Note that the colours

represent the same species as in Figure 4.

2.4 Model

Here, we apply the dynamic model of Engen and Lande (1996), assuming that the log

abundance of species i follows an Ornstein-Uhlenbeck process (Karlin and Taylor 1981)

$$dX_i = (r_i - \delta X_i)dt + \sigma_s dB_i(t) + \sigma_c dB_c(t) \tag{1}$$

where $dB_i(t)$ and $dB_c(t)$ are independent increments of standard Brownian motions with

zero means and variances dt. The total environmental variance is accordingly $\sigma_e^2 = \sigma_s^2 + \sigma_c^2$,

248   where σ_s^2 and σ_c^2 express the species-specific and common environmental noise,

249   respectively. The intrinsic growth rates r_i are assumed to be a sample from a normal

250   distribution with mean r_0 and variance σ_r^2, and δ describes the strength of the density

251   regulation. The log of the carrying capacity of species i is then r_i / δ so that the log carrying

252   capacity among species has mean $\mathrm{E}[\ln K] = r_0 / \delta$ and variance σ_r^2 / δ^2. The log abundances

253   of species at time zero and $t > 0$ will then follow a bivariate normal distribution among

254   species. Under Poisson sampling, the corresponding counts of individuals will then follow a

255   bivariate Poisson-lognormal distribution (Engen et al. 2011a). A simple way of accounting for

256   possible over-dispersion relative to the Poisson is then to assume that the sampling is

257   described by a Poisson-lognormal distribution rather than a Poisson, with an over-dispersion

258   parameter θ^2 which is zero under Poisson sampling. Engen et al. (2011a) showed that the

259   counts still follow a bivariate Poisson-lognormal distribution with variance parameter

260
$$\sigma_{total}^2 = \sigma_s^2 / 2\delta + \sigma_r^2 / \delta^2 + \theta^2 \qquad (2)$$

261   This is then the variance parameter in the observed species abundance distribution, which

262   we write on the form $\sigma_{total}^2 = \sigma_{stoch}^2 + \sigma_{heter}^2 + \theta^2$, thus decomposing the variance into three

263   terms expressing the effect of species-specific environmental noise, the heterogeneity

264   among species and the over-dispersion in the sampling, respectively. The common

265   environmental noise σ_c^2 only affects the sample sizes with no effect on the parameters of

266   the distribution (Engen and Lande 1996). The bivariate Poisson-lognormal also has a

267   correlation parameter which is the correlation between two actual abundances (not the

268   observed ones) of the same species at time difference t, which can be expressed on the form

269
$$\rho_t = (\rho_0 - \rho_\infty) e^{-\delta t} + \rho_\infty \qquad (3)$$

270 where $\rho_0 = \left(\sigma_s^2/2\delta + \sigma_r^2/\delta^2\right)/\sigma_{total}^2$ and $\rho_\infty = \left(\sigma_r^2/\delta^2\right)/\sigma_{total}^2$. By fitting the bivariate

271 Poisson lognormal distribution to all pairs of samples at different time intervals using the

272 *poilog* package in R (Grøtan and Engen 2008, R Core Team), the common total variance as

273 well as the ρ_t for a large number of time differences can be estimated by maximising the

274 likelihood function. The estimates of the ρ_t can finally be smoothed to obtain estimates of

275 ρ_0, ρ_∞ and δ. Finally, these estimates yield estimates of the three additive components of

276 the total variance by the relations $\sigma_{heter}^2 = \rho_\infty\sigma_{total}^2$, $\theta^2 = (1-\rho_0)\sigma_{total}^2$ and

277 $\sigma_{stoch}^2 = (\rho_0 - \rho_\infty)\sigma_{total}^2$.

278

2.5 Estimation

280 Within each area, we estimated the temporal autocorrelation by fitting the bivariate Poisson

281 lognormal distribution to each possible combination of pairs of samples, for all time

282 differences. From all the estimated correlations from transects taken at the same time, we

283 estimated ρ_0 as the mean $\hat{\rho}_0 = \sum_{\forall t=0} \rho_t / n_{t=0}$ and the standard error as the sample standard

284 deviation $\mathrm{SE}(\hat{\rho}_0) = \sqrt{\sum_{\forall t=0} (\rho_t - \hat{\rho}_0)/(n_{t=0}-1)}$. The strength of density regulation δ can be

285 estimated by fitting the autocorrelation function (Eq. 3) to the estimated sample

286 correlations, by minimizing the sum of squares between each sample correlations and ρ_t,

287 assuming that $\hat{\rho}_0$ is known. We imposed the boundary condition that $\rho_0 \geq \rho_\infty \geq 0$. For a

288 density-regulated population, the return time to equilibrium is defined as the expected time

289 required for a deviation from equilibrium to reach a fraction 1/*e* of its original value in the

290 corresponding deterministic model (Solbu et al. 2013), and depends on life history

291   characteristics like survival rates, age at maturity and clutch sizes. From the estimated

292   strength of density-regulation $\hat{\delta}$ we can obtain an estimate of the mean return time to

293   equilibrium $\hat{T}_R = 1/\hat{\delta}$ that can be used to set the threshold for time differences used to

294   estimate ρ_∞. Specifically, we took the smallest integer strictly greater than twice the mean

295   return time to equilibrium. For all sample correlations with a time difference greater or

296   equal to this threshold, we estimated the correlation in the limit as the sample mean

297    $\hat{\rho}_\infty = \sum_{\forall t \geq 2\hat{T}_R} \rho_t / n_{t \geq 2\hat{T}_R}$ and the standard error $\mathrm{SE}\left(\hat{\rho}_\infty\right) = \sqrt{\sum_{\forall t \geq 2\hat{T}_R} \left(\rho_t - \hat{\rho}_\infty\right) / \left(n_{t \geq 2\hat{T}_R} - 1\right)}$. This

298   method of estimating ρ_∞ can give estimates of δ that are very small, which in turn yield

299   unrealistically long return times to equilibrium. Low estimates of δ can be due to the

300   observed correlations decreasing very slowly (if at all) with increasing time difference,

301   meaning that the species abundance distribution and the ranking of species abundances are

302   almost identical over long time differences. An alternative approach to estimating ρ_∞ is then

303   to determine a lower bound of δ or, conversely, an upper bound of T_R that is reasonable

304   based on other studies of the temporal dynamics of the species (see e.g. Table 2 in Sæther

305   and Engen (2002) for sample estimates of strength of density regulation in different bird

306   species, giving estimates of return time to equilibrium of 3 years or less). If the estimated δ is

307   less than 0.2, we will set the mean return time to equilibrium to five years and use sample

308   correlations with a time difference of ten or more years for calculating ρ_∞. If we set the

309   threshold for δ too high, we may end up with an unrealistically large proportion of variance

310   attributed to heterogeneity, and consequently a too low turnover rate. At the same time, we

311   need large enough samples to estimate ρ_∞, by not having the threshold too low.

312

313   There may be areas and sampling designs with large over-dispersion estimates that could

314   conceal species heterogeneity within a subset of samples in an area. To see if species

315   heterogeneity was concealed by over-dispersion, we estimated the over-dispersion for all

316   possible partitionings of an area into two subgroups where each group had two or more

317   transects and found the two groups that minimize the average over-dispersion, i.e.

318   $\min\left\{\rho_0 - \left(\rho_0^{Low} + \rho_0^{High}\right)/2\right\}$. We wanted to highlight how the subsequent analysis of the

319   temporal autocorrelation was affected by this division. The total variance σ_{total}^2 for each area

320   was estimated by fitting a univariate Poisson lognormal distribution to all samples in each

321   area and taking the sample mean of the estimated variances.

322

3. Results

324   We have in this study focused on the results from Dividalen and Solhomfjell, as these areas

325   represent the extremes of difference in habitat variation within an area and are best suited

326   for highlighting the important capabilities of our model. The other areas (Børgefjell,

327   Åmotsdalen, Gutulia, Møsvatn and Lund) fall within the range of these two and will,

328   therefore, not be commented on in detail, although a summary of results is provided in

329   Table 1 and at the end of the Results section. When we analysed all the transects in

330   Dividalen (Fig. 6A), a total of 21730 pairwise correlations, the estimated correlation between

331   transects within the same year was $\hat{\rho}_0 = 0.471$ with a standard error 0.016 ($n_{t=0} = 936$). The

332   estimated proportion of variance due to over-dispersion was then 0.529, generated by

333   spatial variation (habitat differences) and demographic stochasticity (variation in individual

334   reproduction or survival). Furthermore, the estimated strength of density dependence was

335   $\hat{\delta} = 0.11$, giving a mean return time to equilibrium of nine years, suggesting that we should

336   use estimated correlations with time differences equal to or greater than 18 years to be

337   confident that the autocorrelation function is close to ρ_{∞}. However, for the species we are

338   studying, such a mean return time to equilibrium seemed unrealistic. Therefore, assuming a

339   return time of five years, we used the sample correlations with time differences greater or

340   equal to ten to estimate the correlation in the limit, giving $\hat{\rho}_{\infty} = 0.468$

341    $\left(\text{SE} = 0.0058, n_{t \geq 10} = 6548\right)$, which equals the proportion of variance due to temporal

342   heterogeneity among species. Using time difference greater or equal to 18 gave $\hat{\rho}_{\infty} = 0.459$,

343   indicating that the assumed species' strength of density regulation does not seem to

344   influence our estimate of heterogeneity significantly.

345

346   A small proportion $\rho_0 - \rho_{\infty} = 0.0032$ of the total variance $\hat{\sigma}^2_{total} = 3.42$ was due to

347   environmental stochasticity ($\hat{\sigma}^2_{stoch} = 0.011$), compared to the variance due to heterogeneity

348    $\hat{\sigma}^2_{heter} = 1.6$. To investigate what was causing the large over-dispersion within the Dividalen

349   area, we looked at the two-sample correlations within the same year (Fig. 6B) and found

350   high correlations among transects from the same group, either [1 – 6] or [7 – 10], while

351   there was a low or negative correlation among transects from each of the groups [1 – 6] and

352   [7 – 10]. If we estimated ρ_0 for all possible ways of grouping the transects in Dividalen in two,

353   it transpired that by grouping [1 – 6] and [7 – 10], we obtained the largest mean estimates of

354   ρ_0 within the two subgroups, i.e. minimized the spatial variation component of the over-

355   dispersion the most, compared to the initial joint estimate of all transects. From our initial

356   inspection of the data, this subdivision seemed reasonable as there were considerable

differences in elevation (Fig. 2) and vegetation characteristics (Fig. 3) between the two

358   groups, so we called these subgroups Low and High (altitudes) respectively.

359
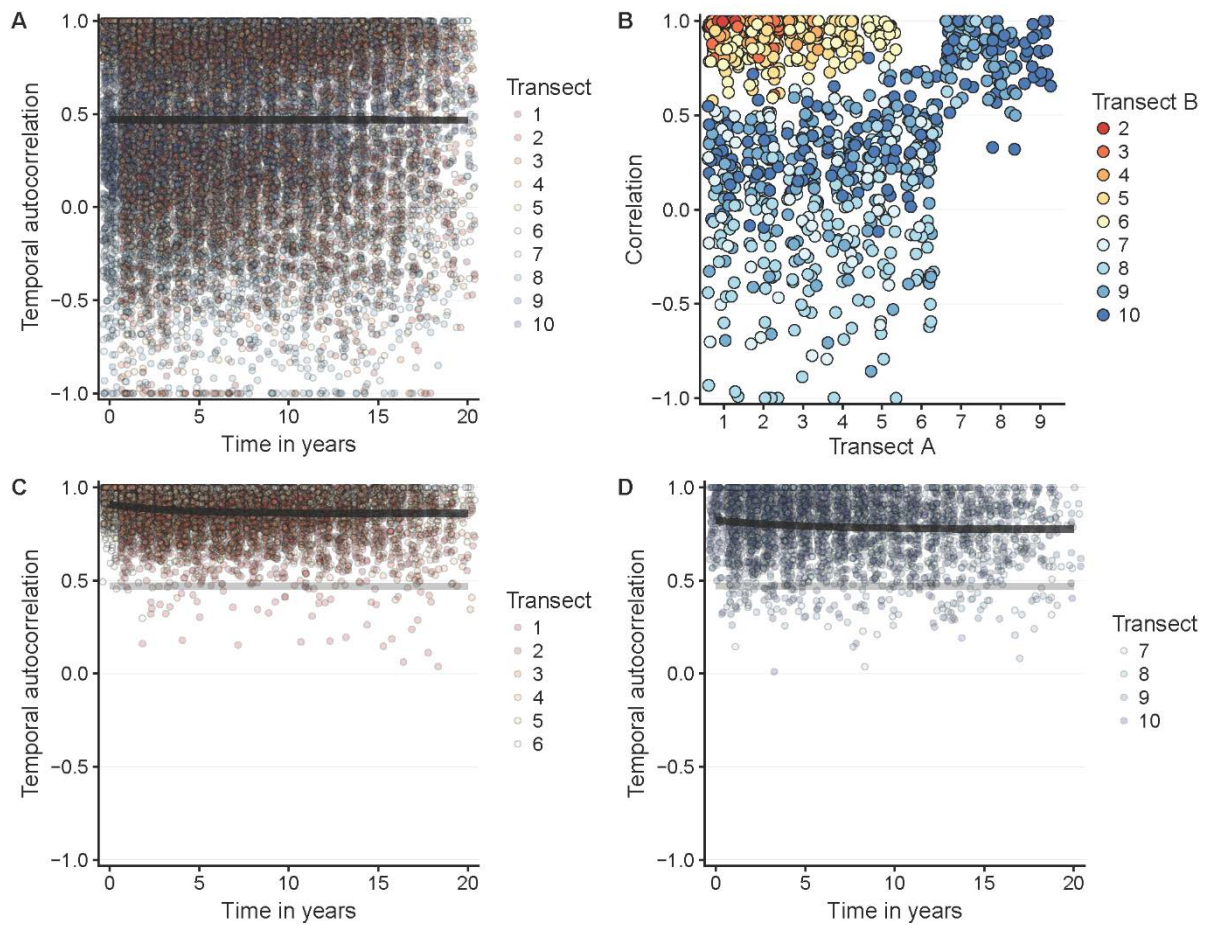
Figure 6: (**A**) Temporal autocorrelation function $\rho(t)$ (black line) estimated in Dividalen

when transects are considered as a single spatial group. The points are pairwise correlations

between a transect and the transect indicated by the colour, estimated from the bivariate

Poisson lognormal distribution. (**B**) Estimated correlations between transect A (x-axis) and

transect B (colour) in Dividalen within the same year ρ_0. (**C**) Temporal autocorrelation

function $\rho(t)$ (black line) estimated in Dividalen for transects grouped as Low mean

elevation [1 – 6]. The points are correlations between a transect and the transect indicated

by the colour within the Low spatial group, estimated from the bivariate Poisson lognormal

368   distribution. The grey line is the temporal autocorrelation function fitted in **A**. (**D**) Same as **C**,

369   but for transects grouped as High mean elevation [7 – 10].

370

371   Performing the variance partitioning within the two subgroups, we got rather different

372   results than our initial analysis indicated (Fig. 6C and 6D). First, the estimated proportion of

373   variance due to over-dispersion was much smaller, with $1 - \hat{\rho}_0 = 0.0916$ and 0.176 for the Low

374   and High groups respectively. Second, the Low group had a much shorter return time to

375   equilibrium $T_R = 3.5$, while the High group had a much longer return time compared to the

376   initial estimate $T_R = 14$. We, therefore, used sample correlations with a time difference

377   seven years or greater to estimate ρ_∞ within the Low transects, while we used ten or more

378   years for the High transects. The estimated proportion of variance due to heterogeneity

379   among species was $\hat{\rho}_\infty = 0.859$ for Low ($\hat{\sigma}^2_{heter} = 3.2$) and 0.774 for High ($\hat{\sigma}^2_{heter} = 2.3$) which

380   was a large increase compared to what the initial analysis indicated. Finally, the proportion

381   of variance attributed to environmental stochasticity was similar in the two subgroups, with

382    $\hat{\rho}_0 - \hat{\rho}_\infty = 0.0489$ and 0.0497, of their total variance $\hat{\sigma}^2_{total} = 3.72$ and 2.97, respectively. This

383   gave environmental variance component estimates of $\hat{\sigma}^2_{stoch} = 0.182$ within Low and

384    $\hat{\sigma}^2_{stoch} = 0.147$ within High transects.

385

386   Estimating the temporal autocorrelation for the community in Solhomfjell (Fig. 7A) we found

387   that spatial variation or demographic stochasticity only accounted for a small proportion

388    $1 - \hat{\rho}_0 = 0.0789$ of the total variation $\hat{\sigma}^2_{total} = 2.57$. The strength of density regulation was

389   0.12, so we used sample correlations with time difference ten years or greater when

390   estimating ρ_∞, as we did in Dividalen when we considered all the transects together, but in

391   Solhomfjell heterogeneity accounted for a large proportion $\hat{\rho}_\infty = 0.816$ of the total variance,

392   corresponding to $\hat{\sigma}^2_{heter} = 2.09$. The proportion of variance due to environmental

393   stochasticity was then $\hat{\rho}_0 - \hat{\rho}_\infty = 0.106$, i.e. $\hat{\sigma}^2_{stoch} = 0.271$. The over-dispersion estimate did

394   not indicate any large spatial differences among the transects, a result supported by the

395   sample correlations within the same year (Fig. 7B), where no apparent patterns of

396   correlation between the transects emerged. The small over-dispersion estimate was also as

397   expected from the preliminary inspection of the spatial data of elevation (Fig. 2) and

398   vegetation (Fig. 3), where no systematic difference between the transects was observed.

399   When we performed the subdivision of transects, the two subgroups that minimized the

400   mean estimated over-dispersion were transects [1 – 7, 9] (Low) and [8, 10] (High). The

401   correlation between transects 8 and 9 (Fig. 7B) was high but slightly lower between transect

402   9 and 10. Therefore, the 9th transect was excluded from the High group according to our

403   simple grouping rule. The variance decomposition for the two subgroups showed that while

404   the over-dispersion was reduced for the High group, it did not change our conclusions

405   regarding heterogeneity, environmental stochasticity or strength of density regulation (Fig.

406   7C and 7D, Table 1) compared to the joint analysis of all the transects.

407
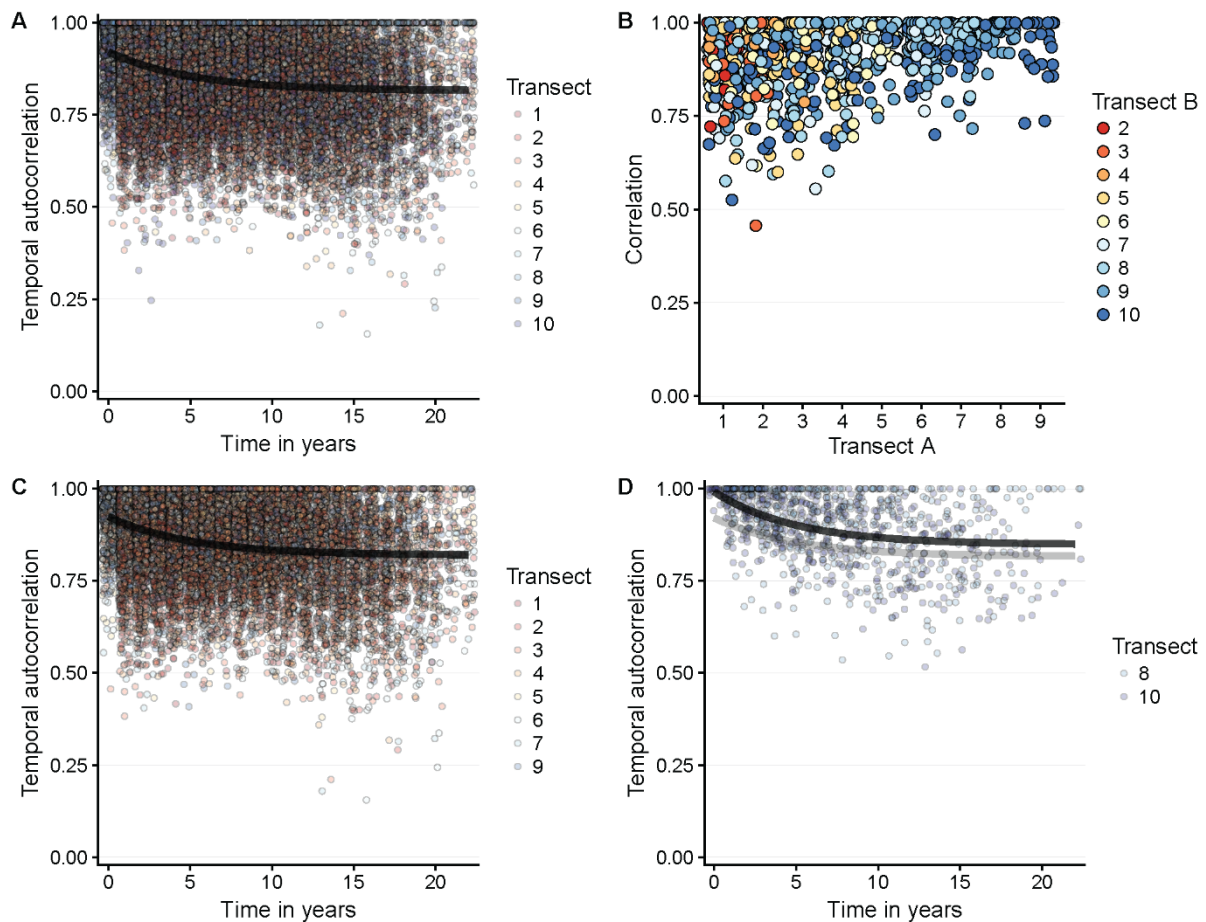
Figure 7: (**A**) Temporal autocorrelation function $\rho(t)$ (black line) estimated in Solhomfjell

when transects are considered as a single spatial group. The points are correlations between

a transect and the transect indicated by the colour, estimated from the bivariate Poisson

lognormal distribution. (**B**) Estimated correlations between transect A (x-axis) and transect B

(colour) in Solhomfjell within the same year ρ_0 . (**C**) Temporal autocorrelation function $\rho(t)$

(black line) estimated in Solhomfjell for transects grouped as Low mean elevation [1 – 7, 9].

The points are correlations between a transect and the transect indicated by the colour

within the Low spatial group, estimated from the bivariate Poisson lognormal distribution.

The grey line is the temporal autocorrelation function fitted in **A**. (**D**) Same as **C**, but for

transects grouped as High mean elevation [8, 10].

418

419 When we only used passerine species in the analysis of bird communities, the results

420 changed slightly in Dividalen, while they were practically the same in Solhomfjell (Table 1).

421 When analysing passerine species for all transects in Dividalen, we got a small decrease in

422 over-dispersion and a similar increase in heterogeneity. The over-dispersion, however, was

423 still of such a magnitude that dividing the transects into two subgroups was reasonable.

424 While the results in the Low group in Dividalen was the same for passerine species

425 compared to all species, there was a small decrease in heterogeneity for the High group. The

426 non-passerine species removed from the analysis (Fig. 4) were mainly species that were only

427 found in the High transects. The removal of species exclusive to High transects could explain

428 the decrease in over-dispersion when analysing all transects together, since restricting the

429 analysis to passerine species made High and Low transects more similar. When analysing

430 High transects separately, the reduction in heterogeneity among passerine species could be

431 due to there being fewer species at a low or intermediate abundance.

432

433 **Table 1**: Summary of the correlation and variance component estimates, when considering

434 all or passerine species only, and using all transects or dividing them into Low and High

435 subgroups. Values in parenthesis for ρ_0 and ρ_∞ gives the standard errors. Rows in bold

436 indicate our preference for subdivision of transects to Low and High groups or considering all

437 transects jointly.

438

439

440

	Area	Transects	ρ_0	ρ_∞	δ	σ^2_{total}	θ^2	σ^2_{heter}	σ^2_{stoch}
All species	Dividalen	All	0.471 (0.016)	0.468 (0.0058)	0.11	3.42	1.81	1.60	0.011
		Low	**0.908 (0.006)**	**0.859 (0.0012)**	**0.29**	**3.72**	**0.341**	**3.20**	**0.18**
		High (7-10)	**0.824 (0.013)**	**0.774 (0.0021)**	**0.073**	**2.97**	**0.524**	**2.30**	**0.15**
	Børgefjell	All	0.723 (0.007)	0.642 (0.0024)	0.021	2.67	0.741	1.71	0.22
		Low	**0.891 (0.005)**	**0.779 (0.0014)**	**0.060**	**3.02**	**0.331**	**2.35**	**0.34**
		High (8-10)	**0.852 (0.014)**	**0.753 (0.0017)**	**0.009**	**1.84**	**0.273**	**1.39**	**0.18**
	Åmotsdalen	All	0.629 (0.010)	0.602 (0.0035)	0.003	2.73	1.01	1.64	0.073
		Low	**0.825 (0.011)**	**0.786 (0.0015)**	**0.031**	**2.79**	**0.488**	**2.19**	**0.11**
		High (5-10)	**0.855 (0.008)**	**0.816 (0.0019)**	**0.072**	**2.68**	**0.388**	**2.19**	**0.11**
	Gutulia	All	0.728 (0.009)	0.648 (0.0036)	0.009	2.19	0.596	1.42	0.18
		Low	**0.862 (0.008)**	**0.718 (0.0026)**	**0.032**	**2.02**	**0.278**	**1.45**	**0.29**
		High (7-10)	**0.895 (0.010)**	**0.843 (0.0022)**	**0.073**	**2.46**	**0.258**	**2.07**	**0.13**
	Møsvatn	**All**	**0.794 (0.006)**	**0.757 (0.0026)**	**0.003**	**3.5**	**0.721**	**2.65**	**0.13**
		Low	0.968 (0.009)	0.903 (0.0008)	0.072	4.32	0.139	3.90	0.28
		High (3-8)	0.815 (0.008)	0.780 (0.0023)	0.002	3.23	0.597	2.52	0.11
	Solhomfjell	**All**	**0.921 (0.003)**	**0.816 (0.0014)**	**0.12**	**2.57**	**0.202**	**2.09**	**0.27**
		Low	0.924 (0.003)	0.820 (0.0014)	0.11	2.46	0.186	2.02	0.26
		High (8, 10)	0.992 (0.004)	0.848 (0.0013)	0.15	2.98	0.0242	2.53	0.43
	Lund	**All**	**0.912 (0.003)**	**0.808 (0.0015)**	**0.009**	**2.41**	**0.213**	**1.95**	**0.25**
		Low	0.900 (0.004)	0.807 (0.0016)	0.008	2.35	0.234	1.90	0.22
		High (5, 7)	0.986 (0.006)	0.834 (0.0012)	0.012	2.66	0.0363	2.21	0.41
Passerine species	Dividalen	All	0.524 (0.015)	0.511 (0.0055)	0.11	2.97	1.41	1.52	0.039
		Low	**0.915 (0.006)**	**0.854 (0.0018)**	**0.19**	**3.24**	**0.275**	**2.77**	**0.20**
		High (7-10)	**0.812 (0.017)**	**0.760 (0.0030)**	**0.005**	**2.56**	**0.48**	**1.95**	**0.13**
	Børgefjell	All	0.775 (0.007)	0.697 (0.0023)	0.015	2.48	0.557	1.73	0.20
		Low	**0.913 (0.005)**	**0.810 (0.0014)**	**0.070**	**2.77**	**0.242**	**2.24**	**0.28**
		High (8-10)	**0.880 (0.018)**	**0.771 (0.0019)**	**0.057**	**1.8**	**0.216**	**1.39**	**0.20**
	Åmotsdalen	All	0.621 (0.010)	0.588 (0.0037)	0.003	2.71	1.03	1.59	0.092
		Low	**0.810 (0.012)**	**0.758 (0.0017)**	**0.005**	**2.67**	**0.508**	**2.03**	**0.14**
		High (5-10)	**0.862 (0.009)**	**0.825 (0.0022)**	**0.004**	**2.74**	**0.377**	**2.26**	**0.10**
	Gutulia	All	0.746 (0.009)	0.667 (0.0038)	0.009	2.41	0.614	1.61	0.19
		Low	**0.870 (0.008)**	**0.714 (0.0027)**	**0.078**	**2.17**	**0.283**	**1.55**	**0.34**
		High (8-10)	**0.934 (0.009)**	**0.889 (0.0021)**	**0.110**	**2.78**	**0.183**	**2.47**	**0.13**
	Møsvatn	**All**	**0.792 (0.007)**	**0.751 (0.0027)**	**0.003**	**3.17**	**0.66**	**2.38**	**0.13**
		Low	0.973 (0.010)	0.899 (9e-04)	0.092	3.87	0.105	3.48	0.29
		High (3-8)	0.814 (0.008)	0.777 (0.0024)	0.032	2.94	0.547	2.29	0.11
	Solhomfjell	**All**	**0.923 (0.003)**	**0.825 (0.0015)**	**0.130**	**2.52**	**0.195**	**2.08**	**0.25**
		Low	0.926 (0.004)	0.831 (0.0015)	0.084	2.41	0.178	2.01	0.23
		High (8, 10)	0.992 (0.004)	0.856 (0.0012)	0.180	2.93	0.0226	2.51	0.40
	Lund	**All**	**0.912 (0.004)**	**0.807 (0.0017)**	**0.043**	**2.27**	**0.2**	**1.83**	**0.24**
		Low	0.901 (0.005)	0.806 (0.0017)	0.008	2.25	0.224	1.81	0.21
		High (5, 7)	0.987 (0.006)	0.831 (0.0012)	0.012	2.34	0.031	1.95	0.37

441

442 For the other areas, Børgefjell, Åmotsdalen, Gutulia, Møsvatn and Lund, the estimated

443 strength of density regulation was so small that the estimated mean return time to

444 equilibrium $\hat{T}_R$ was greater than our observed maximum time difference. We, therefore,

445 used the correlations with time differences of ten years or greater to estimate ρ_∞ and the

446 variance due to heterogeneity among species, as a simple approximation in the absence of a

447 reasonable estimate of δ. The estimated ρ_0 (Table 1) showed that there was more over-

448 dispersion when considering all transects together in Børgefjell, Åmotsdalen and Gutulia

449 compared to Møsvatn and Lund. Comparing the analysis for all the areas available (Fig. 8),

450 heterogeneity among species accounted for roughly three-quarters of the variation in

451 species abundance. For areas where over-dispersion was more than a quarter of the

452 variance when considering all transects together (Dividalen, Børgefjell, Åmotsdalen and

453 Gutulia), it was beneficial to partition the transects into two subgroups as this reduced the

454 over-dispersion in both subgroups, which was not the case for the other areas (Møsvatn,

455 Solhomfjell and Lund).
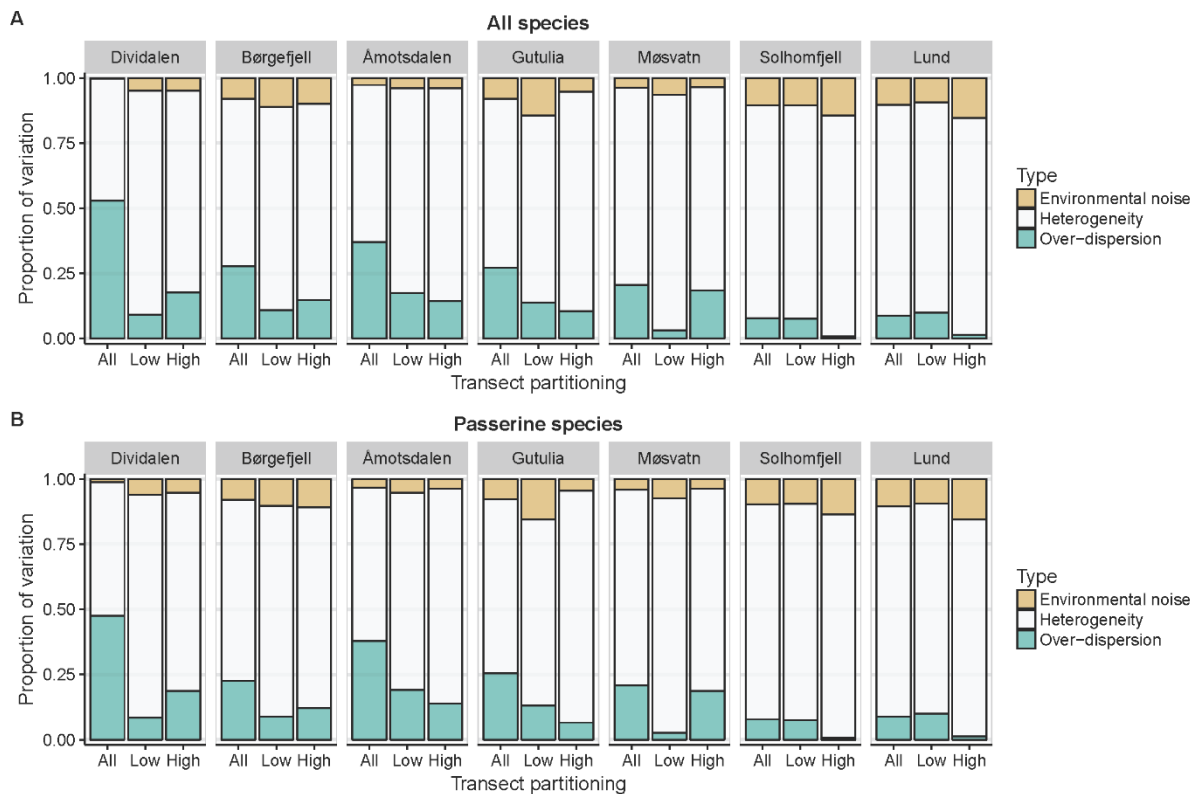
Figure 8: Partition of the total variance in species abundances into environmental noise, heterogeneity and over-dispersion components in all the areas considered.

The absolute values of the variance component estimates (Table 1) ranged from 0.11 to 0.34 for environmental noise σ^2_{stoch} if we considered High and Low subgroups in Dividalen, Børgefjell, Åmotsdalen and Gutulia, and all transects together in Møsvatn, Solhomfjell and Lund. There were no apparent trends in σ^2_{stoch} in terms of High or Low groups or the geographical location of the different areas. The optimal subdivision of the transects showed that for Dividalen, Børgefjell, Åmotsdalen, Gutulia and Møsvatn, the partitioning followed the mean elevation gradient. One of the subgroups in Møsvatn only included two transects, which seemed to reduce the over-dispersion very little in the remaining subgroup. The small reduction in over-dispersion for one of the subgroups was also the case for Solhomfjell and

469   Lund, where the division did not follow the mean elevation gradient, not surprising

470   considering that the elevation range was limited compared to the other areas (Fig. 2). Due to

471   the lack of overall reduction in over-dispersion, we would suggest keeping the analysis made

472   with all the transects considered jointly in areas with spatial variation similar to that in

473   Møsvatn, Solhomfjell and Lund.

474

4. Discussion

476   To monitor and understand community dynamics, typically wanting to distinguish natural

477   from human-induced changes in species assemblages, is a challenging task in community

478   ecology. The concept of β-diversity, introduced by Whittaker (1972), described the

479   difference in diversity between local communities and populations over larger geographical

480   areas. This approach has also been extended to the temporal scale, defined as the metric

481   describing changes in community composition over time, using some similarity measure to

482   find how fast similarity changes (species turnover) (McGill et al. 2015). Here, natural

483   temporal species turnover has been modelled by letting population model parameters vary

484   among species, so-called community heterogeneity (Engen et al. 2011b). Describing each

485   species' population dynamics put great demands on data sets and model parameterization,

486   but by modelling species-specific growth rates by a distribution, leading to variation in

487   carrying capacities among species, we do not need to specify the dynamics of each species in

488   detail. The community can thereby be described by a parsimonious model that still captures

489   the important properties of the dynamics. Without this assumption of heterogeneity, the

490   estimated environmental variance would have to be extremely large to generate the

491   variation seen in species abundance distributions and the model would still not describe the

492   species turnover correctly (Solbu et al. 2016). Trying to predict population dynamics with an

493   overestimated environmental variance would also result in an unrealistic short time to

494   extinction (Sæther et al. 2005).

495

496   With the modelling approach presented here, it is also possible to sort out potential spatial

497   variation in species abundances among sampling units that otherwise would obscure the

498   analysis of community dynamics. Long time series of community data are usually hard to

499   come by, they can be designed for other purposes (even studying spatial structures), or

500   some physical constraints may limit our freedom to design sampling optimally. The validity

501   of this approach has been illustrated by linking the spatial variation in species abundances to

502   elevation and vegetation, but habitat data like can often be unavailable and is not required

503   to fit the model. Even with suboptimal sampling designs of time series data, it is possible to

504   obtain reliable parameter estimates and predictions for the dynamics of a heterogeneous

505   community.

506

507   Our model development was started by revisiting the theory of dynamic species abundance

508   models (Engen and Lande 1996) to estimate the different sources of variation in species

509   abundance distributions, which in turn can be used to quantify the community similarity

510   over time. The method has several attractive features as it accounts for sampling error,

511   provides approximately unbiased estimates, and enables us to decompose the total variance

512   to variation due to species' temporal heterogeneity, species-specific environmental

513   stochasticity and over-dispersion, which in turn can uncover spatial variation in habitat.

514   Heterogeneity among species is the underlying assumption applied in the modelling, which

Solbu, Erik Blystad; Diserud, Ola Håvard; Kålås, John Atle; Engen, Steinar.
Heterogeneity among species and community dynamics – Norwegian bird communities as a case study. Ecological Modelling 2018 ;Volum 388. s. 13-23
10.1016/j.ecolmodel.2018.09.008 CC-BY-NC-ND

515 also gave us a measure of the temporal similarity. We applied this method to local

516 communities of birds throughout Norway, which have not undergone any dramatic changes

517 in habitat during the observation period. Other studies, such as on bird communities in

518 North America, have shown that diversity increased for some decades pre-2000s, before

519 starting to decline in recent years (Jarzyna and Jetz 2017). Across many taxa, communities

520 have generally been found to decrease in similarity over time, while maintaining a stable

521 species richness (Dornelas et al. 2014).

522

523 Our results show that a large proportion of the variation in species abundance was due to

524 heterogeneity among species, from which we can conclude the following: First, the

525 community composition was very similar over the whole 20-year period observed, with

526 abundant species remaining abundant while less abundant species maintaining a low

527 abundance. The high degree of similarity gives a small temporal β-diversity with a low

528 turnover rate (see Fig. 1 in McGill et al. 2015). As the areas studied are rather undisturbed,

529 the low turnover rate can be interpreted as a baseline. If the turnover rate increases, it could

530 be an indication of species invasions or climate change that would have to be addressed by

531 conservation managers (Magurran 2016). Second, the large proportion of variation due to

532 heterogeneity gave estimates of environmental variance that seems reasonable compared

533 to studies of both butterfly and aquatic insect communities (Engen et al. 2002, 2011b).

534

535 The low estimate for the strength of density regulation could be due to strong temporal

536 correlation between transects, as indicated by the data. A small δ makes it hard to estimate

537 the proportion of variance due to heterogeneity ρ_∞ (Eq. 3). The strategy of setting a lower

Solbu, Erik Blystad; Diserud, Ola Håvard; Kålås, John Atle; Engen, Steinar.
Heterogeneity among species and community dynamics – Norwegian bird communities as a case study. Ecological Modelling 2018 ;Volum 388. s. 13-23
10.1016/j.ecolmodel.2018.09.008 CC-BY-NC-ND

538 bound for the strength of density dependence, to determine the time difference used to

539 estimate the proportion of variance due to heterogeneity ρ_∞, was based on earlier studies of

540 temporal dynamics of bird species (Sæther and Engen 2002). An alternative, non-parametric

541 approach for estimating the correlation in the limit ρ_∞ is to use the quantiles of the sample

542 correlations to determine the threshold (Engen et al. 2011b). Using prior or expert

543 knowledge about the strength of density regulation is reasonable in cases where good

544 estimates are difficult to obtain (Solbu et al. 2015). The results from the different methods

545 used to determine the threshold for ρ_∞ were roughly the same, as the sample correlations

546 were high over the whole period (Fig. 6C and D, and Fig. 7A). Furthermore, the analysis is

547 robust with respect to the assumption of a normal distributed log abundance (Engen et al.

548 2011a).

549

550 With the plethora of indices ecologists have available for studying biodiversity, using the

551 bivariate Poisson lognormal distribution to estimate similarity between samples is a

552 favourable alternative as it accounts for many modelling challenges and allows for robust

553 analysis. Even though data may be collected within spatially varying areas, using this

554 knowledge to separate spatial from temporal variation reveals community dynamics that to

555 a large extent is governed by heterogeneity among species in dynamical parameters.

556

5. Acknowledgements

Solbu, Erik Blystad; Diserud, Ola Håvard; Kålås, John Atle; Engen, Steinar.
Heterogeneity among species and community dynamics – Norwegian bird communities as a case study. Ecological Modelling 2018 ;Volum 388. s. 13-23
10.1016/j.ecolmodel.2018.09.008 CC-BY-NC-ND

564

6. References

566   Bonar, S. A., Fehmi, J. S. and Mercado-Silva, N. 2011. An overview of sampling issues in

567   species diversity and abundance surveys. - In: Magurran, A. E. and McGill, B. J. (eds),

568   Biological Diversity: Frontiers in measurement and assessment. 1st ed. Oxford University

569   Press, pp. 11-24.

570   Bulmer, M. G. 1974. On fitting the Poisson Lognormal distribution to species-abundance

571   data. - Biometrics 30: 101-110.

572   Dornelas, M., Gotelli, N. J., McGill, B., Shimadzu, H., Moyes, F., Sievers, C. and Magurran, A.

573   E. 2014. Assemblage Time Series Reveal Biodiversity Change but Not Systematic Loss. -

574   Science 344: 296-299.

575   Engen, S. and Lande, R. 1996. Population dynamic models generating the lognormal species

576   abundance distribution. - Mathematical Biosciences 132: 169-83.

577   Engen, S., Lande, R., Walla, T. and DeVries, P. J. 2002. Analyzing Spatial Structure of

578   Communities Using the Two-Dimensional Poisson Lognormal Species Abundance Model. –

579   The American Naturalist 160: 60-73.

Solbu, Erik Blystad; Diserud, Ola Håvard; Kålås, John Atle; Engen, Steinar.
Heterogeneity among species and community dynamics – Norwegian bird communities as a case study. Ecological Modelling 2018 ;Volum 388. s. 13-23
10.1016/j.ecolmodel.2018.09.008 CC-BY-NC-ND

580   Engen, S., Grøtan, V. and Sæther, B.-E. 2011a. Estimating similarity of communities: A

581   parametric approach to spatio-temporal analysis of species diversity. - Ecography 34: 220-

582   231.

583   Engen, S., Aagaard, K. and Bongard, T. 2011b. Disentangling the effects of heterogeneity,

584   stochastic dynamics and sampling in a community of aquatic insects. - Ecological Modelling

585   222: 1387-1393.

586   Grøtan, V. and Engen, S. 2008. Poilog: Poisson lognormal and bivariate Poisson lognormal

587   distribution. P-package https://cran.r-project.org/web/packages/poilog/poilog.pdf

588   Hubbell, S. P. 2001. The unified neutral theory of biodiversity and biogeography. - Princeton

589   University Press.

590   Hutchinson, G. E. 1957. Concluding Remarks. - Cold Spring Harbor Symposia on Quantitative

591   Biology 22: 415-427.

592   Jarzyna, M. A. and Jetz, W. 2017. A near half-century of temporal change in different facets

593   of avian diversity. - Global Change Biology 23: 2999-3011.

594   Karlin, S. and Taylor, H. M. 1981. A second course in stochastic processes. - Academic Press.

595   MacArthur, R. 1960. On the relative abundance of species. – American Naturalist 94: 25-36.

596   Magurran, A. E. 2016. How ecosystems change. - Science 351: 448-449.

597   McGill, B. J., Dornelas, M., Gotelli, N. J. and Magurran, A. E. 2015. Fifteen forms of

598   biodiversity trend in the Anthropocene. - Trends in Ecology and Evolution 30: 104-113.

599   Preston, F. W. 1948. The commonness, and rarity, of species. – Ecology 29: 254-283.

Solbu, Erik Blystad; Diserud, Ola Håvard; Kålås, John Atle; Engen, Steinar.
Heterogeneity among species and community dynamics – Norwegian bird communities as a case study. Ecological Modelling 2018 ;Volum 388. s. 13-23
10.1016/j.ecolmodel.2018.09.008 CC-BY-NC-ND

600   R Core Team 2016. R: A language and environment for statistical computing. - R Foundation

601   for Statistical Computing.

602   Sæther, B.-E. and Engen, S. 2002. Pattern of variation in avian population growth rates. -

603   Philosophical Transactions of the Royal Society of London. Series B, Biological Sciences 357:

604   1185-1195.

605   Sæther, B.-E. et al. 2005. Time to extinction of bird populations. - Ecology 86: 693-700.

606   Solbu, E. B., Engen, S. and Diserud, O. H. 2013. Changing environments causing time delays in

607   population dynamics. - Mathematical Biosciences 244: 213-223.

608   Solbu, E. B., Engen, S. and Diserud, O. H. 2015. Guidelines when estimating temporal

609   changes in density dependent populations. - Ecological Modelling 313: 355-376.

610   Solbu, E. B., Engen, S. and Diserud, O. H. 2016. Characteristics of temporal changes in

611   communities where individual dynamics may vary among species. - Theoretical Population

612   Biology 111: 65-74.

613   Whittaker, R. H. 1972. Evolution and measurement of species diversity. - Taxon 21: 213-251.

614

Solbu, Erik Blystad; Diserud, Ola Håvard; Kålås, John Atle; Engen, Steinar.
Heterogeneity among species and community dynamics – Norwegian bird communities as a case study. Ecological Modelling 2018 ;Volum 388. s. 13-23
10.1016/j.ecolmodel.2018.09.008 CC-BY-NC-ND