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# High catalytic efficiency of palladium nanoparticles immobilized in a polymer membrane containing poly(ionic liquid) in Suzuki–Miyaura cross-coupling reaction

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## ABSTRACT

The elaboration of a polymeric catalytic membrane containing palladium nanoparticles is presented. The membrane was prepared using a photo-grafting process with imidazolium-based ionic liquid monomers as modifying agent and microPES<sup>®</sup> as support membrane. Ionic liquid serves as a stabilizer and immobilizer for the catalytic species, i.e. palladium nanoparticles. The Suzuki–Miyaura cross-coupling reaction was carried out on the catalytic membrane in flow-through configuration. Complete conversion was achieved in 10 s through one single filtration, without formation of byproducts. The apparent reaction rate constant was three orders of magnitude greater than in a batch reactor. No catalyst leaching was detected. This membrane offers the possibility of continuous production with no need for a separation step of the catalyst from the reaction medium.

### Keywords:

Catalytic membrane  
Palladium nanoparticles  
Flow-through membrane reactor  
Imidazolium-based ionic liquid  
Suzuki–Miyaura cross-coupling

## 1. Introduction

Catalytic membranes have found applications in the field of fine chemistry, petrochemical industry, water treatment, etc. [1–4]. Unlike a batch reactor whose conversion rate slows down with time, a catalytic membrane gives constant conversion over time as it can be considered as a plug-flow reactor. Another advantage of a catalytic membrane is that no separation of the catalyst from the reaction medium is necessary for reuse with the catalyst immobilized inside the membrane. The mass-transfer resistance towards the catalyst is also expected to be eliminated by forcing reactants to flow through membrane pores [5]. The intensive contact between the reactant mixture and the catalyst may lead to a higher apparent conversion rate [6].

Most catalytic membranes to the date are based on inorganic materials, with applications for steam reforming of methane, alkane dehydrogenation, oxidative coupling of methane, etc. [6–10]. Polymeric membranes used in membrane reactors, however, can have some advantages over the expensive inorganic membranes, namely

lower production costs, crack-free thin membranes, and large scale production [7]. However, polymeric membranes should be used under mild conditions (< 150 °C), and thus require a highly active catalyst to ensure good reactivity. Metallic nanoparticles (MNP) have shown very interesting catalytic activity thanks to their high surface/volume ratio [11]. In general, their activity increases when they get smaller because of higher surface/volume ratio and higher fraction of the low-coordinated corner and edge atoms. The high surface energy of MNPs makes them thermodynamically unstable. The presence of appropriate stabilizers is necessary to prevent their aggregation, which usually results in loss of activity. The stabilization of MNPs can be accomplished by a steric effect [12], an electrostatic effect [13], a combination of both (electrosteric effect) [14], or a ligand [15].

H. Hagiwara et al., reported the immobilization of palladium acetate in an ionic liquid in silica pores [16]. Since no chemical bonding exists between the ionic liquid and silica, reaction can be carried out only in a hydrocarbon solvent to prevent removal of the ionic liquid layer from the silica. Nevertheless, palladium leaching from the silica support was still observed [16]. In our case, poly(ionic liquid) (polyIL) was chemically grafted to microPES<sup>®</sup> support membrane to stabilize palladium nanoparticles by electrosteric effect so that leaching of both nanoparticles and ionic liquid could be effectively prevented. The well-defined palladium

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nanoparticles immobilized inside the membrane provided catalytically active sites for the organic transformations envisaged [17].

## 2. Materials and methods

For the general aspects related to the Experimental part, see the [Supplementary information](#).

### 2.1. Synthesis and characterization of ionic liquids **a** and **b**

Imidazolium-based ionic liquids (a non-cross-linking monomer **a** and a cross-linker **b**) used for MNP stabilization were synthesized according to [Scheme 1](#). Detailed syntheses of compound **i** and **ii** were previously reported [18]. The methodologies followed for the synthesis of the monomer **a** and the cross-linker **b** and their full characterization are described in the [Supplementary information](#).

### 2.2. Preparation of the catalytic membrane

#### 2.2.1. Grafting of poly(ionic liquid)s on the PES (polyethersulfone) support membrane

A round-shaped membrane was cut from a microPES<sup>®</sup> 2F flat sheet (purchased from Membrana GmbH, 0.2 μm nominal pore size). A 25 wt% IL monomer solution was prepared in methanol with a cross-linker/non-crosslinker molar ratio of 1/20. 2-Hydroxy-2-methylpropiophenone (1 wt% of total monomer weight) was added to the solution as photo-initiator. The membrane was dipped in the solution for a few seconds and taken out before being exposed to UV light (Heraeus TQ 150 lamp with quartz filter, cooled by a water circuit) for 1 h in air. The distance between the membrane and the quartz filter was 4 cm. After removal from the UV light, the membrane was rinsed thoroughly with ethanol to eliminate surplus IL monomers prior to the metal loading step.

#### 2.2.2. Metal loading

The membrane was first soaked in 10 mL solution of K<sub>2</sub>[PdCl<sub>4</sub>] (0.05 mol/L) in H<sub>2</sub>O/Methanol (1/1 volume ratio) for 90 min while shaking on a IKA KS 260 basic shaker at 100 rpm (1.67 s<sup>-1</sup>). The membrane was then rinsed with ionized water before installation in an Amicon filtration cell with IL-grafted side of the membrane facing up. 10 mL of 0.5 mol/L NaBH<sub>4</sub> solution in H<sub>2</sub>O/methanol (1:1 volume ratio, freshly prepared) was then filtered through the membrane (transmembrane pressure ≈ 0.2 bar). The membrane was then soaked in NaBH<sub>4</sub> for one hour before it was rinsed with

and kept in deionized water. The membrane was then directly used or cut into appropriate size before use.

### 2.3. Permeability test

Since ethanol is the solvent used for the catalytic reaction, ethanol permeability of the catalytic membrane was measured. The flux measurements were carried out in an Amicon cell at room temperature. The permeability was determined by the slope of the plot of flux density (L min<sup>-1</sup>cm<sup>-2</sup>) as a function of transmembrane pressure (bar) (Eq. (1)). The permeability was corrected to 25 °C by Eq. (2) [19] to take into account the variation of viscosity with temperature. Measurements were repeated twice on each membrane.

$$L_p = \frac{J_v}{\Delta P} \quad (1)$$

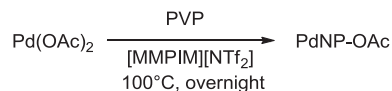
where  $J_v$  is the flux density and  $\Delta P$  is the transmembrane pressure.

$$L_p^{25} = L_p^T \frac{\mu_T}{\mu_{25}} = L_p^T \cdot e^{1708.1(1/T - 1/298.15)} \quad (2)$$

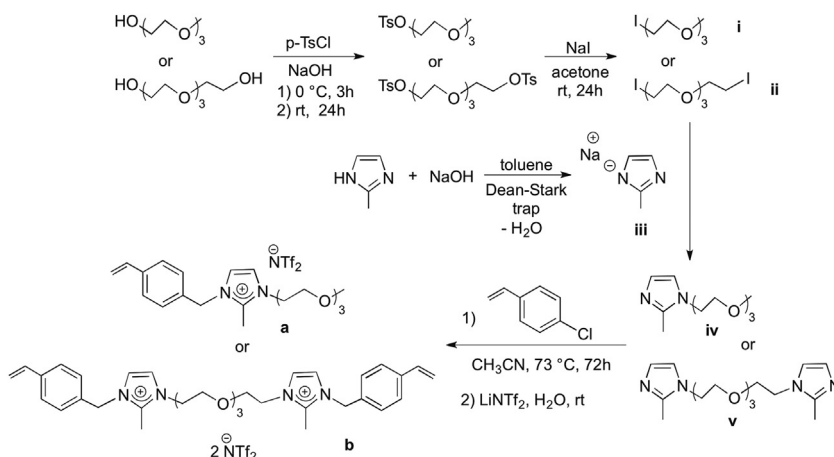
with  $L_p^{25}$  as permeability corrected to 25 °C,  $L_p^T$  as permeability measured at the temperature when the measurement was done,  $\mu_{25}$  as ethanol dynamic viscosity at 25 °C,  $\mu_T$  as ethanol dynamic viscosity at the temperature when the measurement was done.

### 2.4. Preparation of colloidal palladium nanoparticles

Palladium nanoparticles (PdNPs) were synthesized via thermal decomposition of palladium acetate [20], with the aim of obtaining a catalytic solution to perform the catalytic tests in batch conditions [21–24]. 11.5 mg (0.05 mmol) of Pd(OAc)<sub>2</sub> and 113 mg PVP (10,000 g/mol) were added in 5 mL of [MMPIM][NTf<sub>2</sub>] (1,2-dimethyl-3-propylimidazolium bis(trifluoromethylsulfonyl)imide) and stirred at room temperature under argon in a Schlenk tube until complete dissolution. The system was then heated and stirred at 100 °C overnight to give a colloidal system ([Scheme 2](#)). PVP acts as a co-stabilizer together with the ionic liquid (molar ratio Pd/PVP monomer = 1/20).



**Scheme 2.** Synthesis of colloidal palladium nanoparticles.



**Scheme 1.** Synthesis of imidazolium-based derivatives, the monomer **a**, and the crosslinker **b**.

### 2.5. Pd-catalyzed Suzuki–Miyaura C–C cross-coupling under batch conditions using a PdNPs-based colloidal catalytic solution

1-Iodo-4-nitrobenzene (254.1 mg, 1 mmol), phenylboronic acid (150.8 mg, 1.2 mmol), KtBuO (286.3 mg, 2.5 mmol, in 1 mL degassed H<sub>2</sub>O) and PdNP solution (1 mL, 0.01 mmol Pd) were mixed and stirred under argon at the chosen temperature. After the reaction, the reaction mixture was cooled down to room temperature. The organic products were extracted from the catalytic mixture with diethyl ether (10 mL × 2 mL). The organic phase was filtered over celite. The solvent was then removed by rotary evaporator and the product was analyzed and quantified by <sup>1</sup>H NMR and GC–MS analyses using mesitylene as an internal standard.

### 2.6. Pd-catalyzed Suzuki–Miyaura C–C cross-coupling under flow-through conditions using a PdNPs-based catalytic membrane

Catalytic tests were carried out in flow-through reactor configuration. The Amicon cell, equipped with a magnetic stir bar, was placed in a water bath at 60 °C. The reagents were dissolved in 96 vol% ethanol, stirred and heated in an oil bath at 60 °C for 20 min before it was poured into the Amicon cell 8050 and filtered through the membrane while stirring. The permeate flow was controlled by a peristaltic pump (Fig. 1). The membrane was then washed by filtering ethanol at the reaction temperature 5 times using the same volume of the reactive solution after each test. The permeate was collected and analyzed by GC–MS and <sup>1</sup>H NMR spectroscopy in order to identify the products obtained. Conversion (related with the consumption of the substrate, i.e., 1-iodo-4-nitrobenzene) and yield (related to the desired cross-coupling product, i.e., 4-nitrophenyl) at the outlet of the catalytic membrane were calculated by two analytical approaches (GC–FID and <sup>1</sup>H NMR), using decane and mesitylene, respectively, as internal standards; both methodologies gave similar results. Isolated yields were also determined.

In the case of yield determination, the permeate of the reactive solution together with the washing ethanol was collected. The yield was determined by <sup>1</sup>H NMR spectroscopy using mesitylene as an internal standard, which allows measurement of the moles of cross-coupling product produced, taking into account the losses occurring during the extraction steps.

#### 2.6.1. Catalytic protocol for Suzuki–Miyaura cross-coupling reaction

The molar ratio KtBuO/Ph-B(OH)<sub>2</sub>/1-iodo-4-nitrobenzene was 2.5/1.2/1. The stirring speed was 250 rpm (4.17 s<sup>-1</sup>). The pump permitted to vary the permeate flow rate. The transmembrane pressure was not measured but was in the range of 1–150 mbar as deduced from the solvent permeability. In order to isolate the products, the ethanol present in the permeate was removed via rotary evaporation. The product was then re-dissolved in dichloromethane and washed with water to remove the remaining KtBuO. The water phase was discarded and the organic phase was dried over anhydrous MgSO<sub>4</sub> and filtered. Dichloromethane

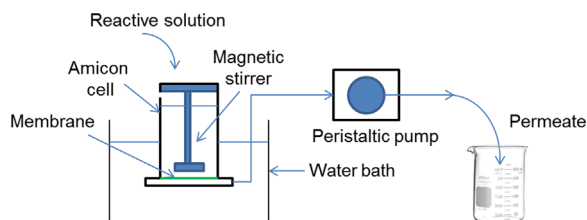


Fig. 1. Experimental set-up for C–C cross-coupling reactions performed on the catalytic membrane in a flow-through reactor.

was then removed under reduced pressure. The product thus obtained was analyzed by <sup>1</sup>H NMR spectroscopy and GC–MS using mesitylene as an internal standard.

## 3. Results and discussions

### 3.1. Choice and synthesis of imidazolium-based ionic liquids

The ionic liquids **a** and **b** serve as stabilizers for palladium nanoparticles. The cross-linker **b** is used to prevent the dissolution of the poly(ionic liquid) by the organic solvent during the reaction. The length and molecular weight of the cross-linking monomer were appropriately adapted to favor the formation of a homogeneous network [25–28]. The presence of the methyl group at C2 position on the imidazolium ring avoids the formation of molecular palladium *N*-heterocyclic carbene complexes under basic conditions [29], which could eventually promote palladium leaching from the membrane.

As shown in Scheme 1, we prepared first the iodo-ethers **i** and **ii** following a two-step classical methodology where the corresponding alcohols were protected by reaction with *p*-tosyl chloride, giving the corresponding tosylate derivatives; a further nucleophilic substitution using sodium iodide led to **i** and **ii**. These iodo-ethers reacted with the sodium imidazole salt (prepared by deprotonation of imidazole with NaOH) to give the neutral mono- and bis(imidazole)s **iv** and **v**, which were quaternized by treatment with 4-vinylbenzyl chloride. The anion exchange reaction using LiNTf<sub>2</sub> led to the desired imidazolium derivatives **a** and **b**.

### 3.2. Preparation of the catalytic membrane

In a first step, the IL was photochemically grafted to a PES support membrane. In the second step, the membrane was loaded with palladium via intermatrix synthesis [30]. The IL-grafted membrane was soaked in a solution of K<sub>2</sub>[PdCl<sub>4</sub>], where the IL anions (NTf<sub>2</sub><sup>-</sup>) were exchanged by [PdCl<sub>4</sub>]<sup>2-</sup>. The membrane turned from white color to brown after the ion exchange. Consecutively, a NaBH<sub>4</sub> solution was filtered through the membrane, which immediately turned from brown to black from reduction of Pd(II) to Pd(0) (Fig. 2).

### 3.3. Characterization of the catalytic membrane

#### 3.3.1. Degree of grafting

PES is a photosensitive material which generates radicals under UV irradiation [31]. Consequently, covalent bonds can be formed between the microPES<sup>®</sup> support membrane and the polyIL during the photografting. The membrane was thoroughly rinsed with ethanol after photo-grafting and ethanol was permitted to evaporate until no more weight change could be observed. This mass was taken as the membrane mass after grafting. The membranes were weighed before and after the photografting step (Section 2.2.1) to determine the amount of ionic liquid grafted onto the PES membrane. The grafting degree was calculated by Eq. (3).

$$\text{Grafting degree} = \frac{(m_g - m_i)}{m_i} \quad (3)$$

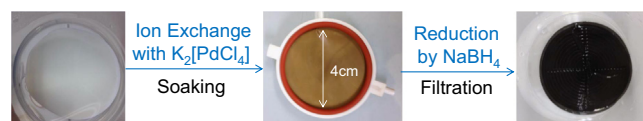


Fig. 2. Palladium loading via intermatrix synthesis.

where  $m_g$  is the membrane weight after photo-grafting (Section 2.2.1) and  $m_i$  is the membrane weight before photo-grafting.

The average degree of grafting was found to be 32.0% with standard deviation of 2.2%. The average mass of poly(ionic liquid) grafted onto the membrane was 1.2 mg/cm<sup>2</sup>.

### 3.3.2. Ethanol permeability of the catalytic membrane

The average ethanol (96 vol% ) permeability of the catalytic membrane at 25 °C was  $15 \pm 2$  mL/(min cm<sup>2</sup> bar), which is comparable to the PES virgin membrane permeability (17.9 mL/(min - cm<sup>2</sup> bar)). No significant drop in the permeability (or pore size reduction) of the membrane was triggered by the grafting.

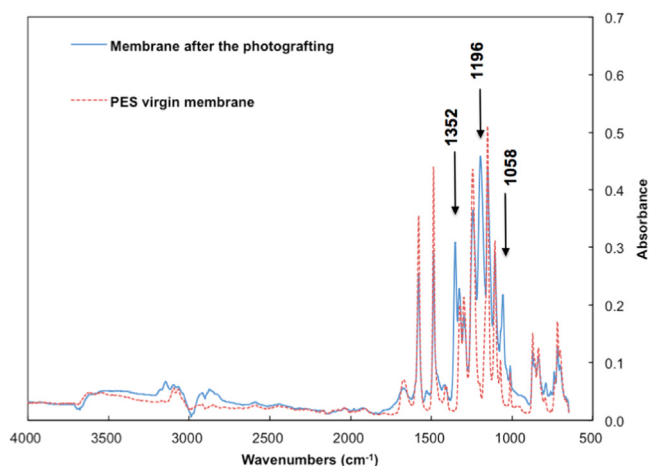


Fig. 3. ATR-IR spectra of pristine PES membrane (dotted red line) and the photo-grafted membrane (solid blue line). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

### 3.3.3. SEM and ATR-IR analyses

The IL-grafted membrane was analyzed by ATR-IR and SEM. Both analyses indicated that the membrane surface was modified by the ionic liquid.

Change of the chemical composition on the membrane surface was confirmed by ATR-IR analysis. Fig. 3 shows the appearance of new absorption bands for the grafted membrane. The absorption bands below 1500 cm<sup>-1</sup> are mainly assigned to the vibrations of bis(trifluoromethylsulfonyl)imide anion; 1352 cm<sup>-1</sup> associated with the SO<sub>2</sub> asymmetric stretching; 1196 cm<sup>-1</sup> is assigned to the CF<sub>3</sub> asymmetric stretching. The absorption band at 1058 cm<sup>-1</sup> can be attributed to the SNS asymmetric stretching, a ring in-plane asymmetric stretching and a C-C stretching [32]. These characteristic bands evidence the coverage of the membrane surface with the ionic liquids involved.

SEM images corroborated the chemical modification of the membrane after the photo-grafting treatment by an obvious morphology change. (Fig. S1 in the Supplementary information).

### 3.3.4. Palladium loading and distribution inside the membrane

The average palladium loading of the catalytic membrane (4 cm of diameter) was  $(7.5 \pm 0.4) \times 10^{-3}$  mmol, or  $(0.60 \pm 0.03) \times 10^{-3}$  mmol/cm<sup>2</sup> (normalized to the membrane surface area) and  $0.52 \times 10^{-3}$  mmol/mg, normalized to mass of polyIL. By comparing the quantity of the NTF<sub>2</sub> anion coming from the IL grafted onto the membrane and the final palladium loading, we can infer that ca. 60% of the NTF<sub>2</sub> anion was exchanged by [PdCl<sub>4</sub>]<sup>2-</sup>.

Ethanol was filtered through the catalytic membrane to study the possible palladium leaching from the membrane. By ICP-OES analyses, no leaching was observed (in the permeate, the palladium concentration was below the detection limit of the technique, i.e., 3 and 15 ppb respectively for the detecting wavelength of 340.3 nm and 361.0 nm (see the Supplementary information for details).

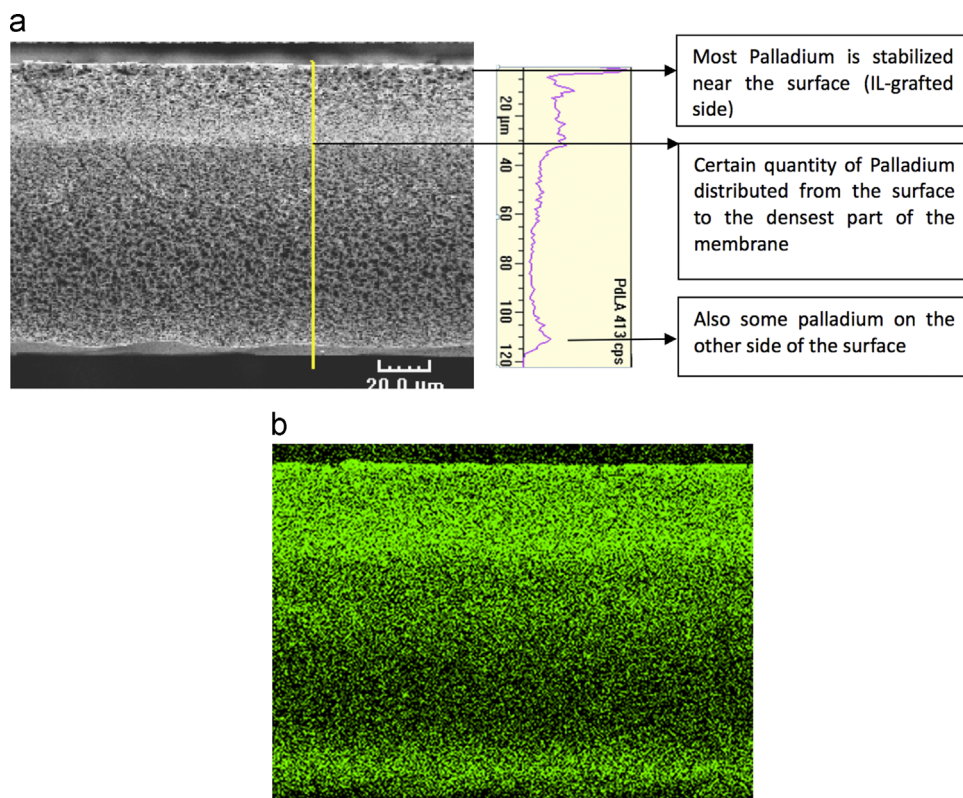


Fig. 4. SEM-EDX analysis: palladium distribution along the membrane thickness (a) and palladium cartography (b).

The PES flat sheet membrane is an asymmetric membrane, with the smallest pore sizes localized approximately 30–40  $\mu\text{m}$  from the IL-grafted membrane surface. The IL-grafted membrane surface was the side of the membrane facing the UV light during the photo-grafting. Consequently, most of the ionic liquid was grafted to the part of the membrane facing the light near the surface. EDX SEM analysis provided us information about the palladium concentration along the membrane thickness. As shown in Fig. 4, most palladium was essentially distributed from the IL-grafted surface to the densest part of the membrane.

TEM analyses of the catalytic membrane's cross-section with zooming on the IL-modified side showed that most palladium NPs were stabilized by the poly(ionic liquid) rather than by the PES support membrane (see Fig. S2 in the Supplementary information). PdNPs (mean diameter:  $2 \pm 1$  nm; see Fig. 7a inside the membrane) were very close to each other (inter-NP distance in the same order as the NP size). The large number of PdNPs per unit volume (ca.  $4 \times 10^{14} \text{ mm}^{-3}$ , this value is deduced from the palladium concentrated zone (i.e. reactive zone) of the membrane see Fig. S2 in Supplementary information) and the small inter-particle distance help to intensify the contact between reactants and catalyst by reducing the diffusion length but could induced concentration gradient inside the PIL containing PdNPs.

Our group previously published a work on catalytic hollow fiber membranes obtained using acrylic acid as modifying agent instead of ionic liquid [33]. The PdNP mean diameter was found to be  $5 \pm 2$  nm in the case of poly(acrylic acid) (polyAA). The difference in palladium size may result from the fact that the main chain of polyAA is negatively charged while that of polyIL is positively charged. The affinity of the palladium precursors towards the grafting layer was also different.

EDX TEM analysis provided information of elemental composition at different zones of the membrane (Fig. S3 in Supplementary information). Contents of S, N and Pd represent the PES support membrane, ionic liquid polymer and PdNPs, respectively (sulfur is also present in the anion of polyIL, but its quantity is estimated to be less than 10% of total sulfur). These analyses showed that palladium loading increases with the N/S ratio (Fig. S4 in Supplementary information), confirming the fact that palladium NPs are stabilized by polyIL rather than the PES support membrane, which is consistent with the TEM images (Fig. S2 in Supplementary information).

#### 3.4. Comparison to non-grafted PES membrane loaded with palladium

A PES virgin membrane was loaded with palladium in the same manner as described above (Section 2.2.2). The membrane color was slightly tinged with pale gray after the metal loading. The palladium loading of the PES virgin membrane was  $3.4 \cdot 10^{-5} \text{ mmol cm}^{-2}$ , 17 times less than that of IL modified membrane. Unlike the IL functionalized membrane, PdNPs present in the PES virgin membrane were mostly aggregated, as shown in Fig. 5. The presence of PdNPs inside the non-modified PES membrane was probably due to the adsorption of the palladium salt on the membrane surface or to the encapsulation of the  $\text{K}_2[\text{PdCl}_4]$  solution inside the membrane pores by capillary forces.

#### 3.5. Catalytic study

##### 3.5.1. Catalytic performance of the palladium colloidal system

For the preparation of colloidal PdNPs (see Section 2.4), [MMPIM][NTf<sub>2</sub>] was used as solvent instead of monomer **a** to avoid the polymerization of monomer **a** at relative high temperature [34]. PVP was used as the co-stabilizer for the corresponding PdNPs. This colloidal catalytic system was tested under batch conditions in order to compare its performance with that of the catalytic membrane.

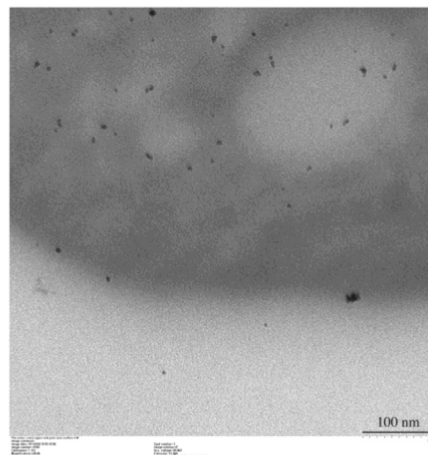


Fig. 5. Non-modified PES membrane loaded with palladium.

TEM analysis showed homogeneously dispersed PdNPs in ionic liquid with few agglomerates (Fig. 6a). The mean diameter of the PdNPs was  $4 \pm 2$  nm, about twice the size of those immobilized in the membrane (see above). For bigger particles, a lower reactivity is then expected, because the decrease of both the relative number of palladium atoms at the metallic surface and the atoms on edges and corners of the nanoclusters, showing low coordination numbers (related with their reactivity). In addition, despite the presence of the co-stabilizer (PVP), agglomerates could not be completely avoided (Fig. 6b). Light scattering measurements evidenced the presence of particles larger than 100 nm.

Stokes number is a dimensionless value defined as the ratio of the characteristic time of a particle to a characteristic time of the flow (Eq. (4)). When  $\text{Stk} \ll 1$ , particles follow streamlines closely.

$$\text{Stk} = \frac{\rho d^2 N}{18\mu} \quad (4)$$

with  $\rho$  and  $d$  as respectively the density ( $12.0 \times 10^3 \text{ kg m}^{-3}$ ) and diameter ( $4 \times 10^{-9} \text{ m}$ ) of PdNPs,  $N$  as agitator speed ( $8.3 \text{ s}^{-1}$ ) and  $\mu$  as dynamic viscosity of [MMPIM][NTf<sub>2</sub>] ( $\approx 20 \times 10^{-3} \text{ kg m}^{-1} \text{ s}^{-1}$  [35,36]). The Stokes number of the colloidal system was calculated to be  $5 \cdot 10^{-12}$ , indicating that the PdNPs follow the streamline so closely that the relative velocity between PdNPs and the liquid phase is nearly zero. The convection is inefficient and actually negligible. The mass transfer is therefore effectuated uniquely by diffusion. This boundary layer will increase with the consumption of the reactants near the catalyst surface to reach a constant value after few second corresponding to a Sherwood number equal to 2 [37,38]. For our particles, the boundary layer thickness is only 2 nm indicating that the mass transfer coefficient will be high.

Compared to the catalytic membrane, around 200 times fewer PdNPs per unit volume are present in the colloidal system. The mean inter-particle distance calculated from the Pd concentration and the particle diameter is in the range of 50–100 nm, larger than those observed in the catalytic membrane.

The Pd-based colloidal system was applied in the Suzuki–Miyaura cross-coupling between 1-iodo-4-nitrobenzene and phenylboronic acid, which was chosen as benchmark reaction (Scheme 3) at three different temperatures (60 °C, 80 °C and 120 °C). Results are summarized in Table 1. The PdNP colloidal system was active, giving mainly the expected cross-coupling product, up to 93% working at low temperature (entry 1). Whatever the temperature was, ca. 10% biphenyl (i.e., the homo-coupling byproduct coming from phenylboronic acid) was formed under batch conditions.

At 60 °C, we followed the kinetics of the reaction by taking samples at different reaction times. By plotting  $\ln(C/C_0)$  as a function of time, we got a linear correlation (with  $C$  as reactant concentration

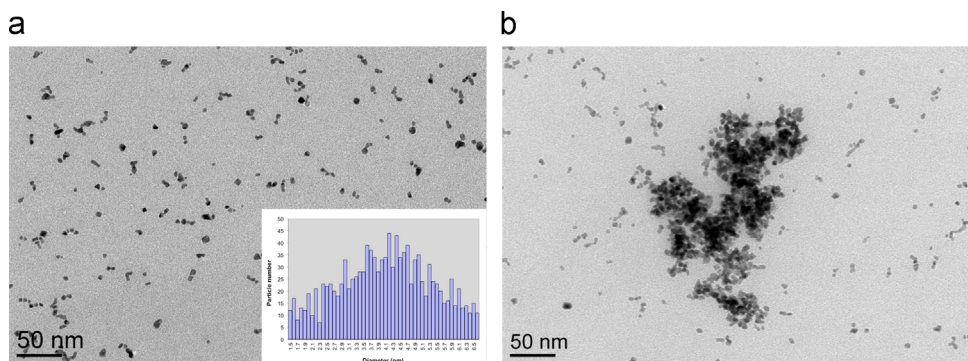
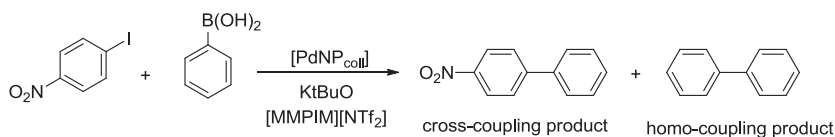


Fig. 6. TEM images of the PdNPs in the colloidal system and its size distribution (1389 particles measured).



Scheme 3. The Suzuki-Miyaura cross-coupling reaction under batch conditions catalyzed by colloidal PdNPs.

**Table 1**  
Pd-catalyzed Suzuki-Miyaura cross-coupling reaction at different temperatures using the preformed colloidal system (see Scheme 3).<sup>a</sup>

Entry	<i>T</i> (°C)	Reaction time (h)	Conversion (%) <sup>b</sup>	Selectivity towards the cross-coupling product (%) <sup>b</sup>
1	60	4	96	93
2	80	5.3	100	87
3	120	1	100	92

<sup>a</sup> Reaction conditions: molar ratio: 1-iodo-4-nitrobenzene/phenylboronic acid/KtBuO/Pd = 1/1.2/2.5/0.01; in IL [MMPIM][NTf<sub>2</sub>] (1 mL).

<sup>b</sup> Determined by GC and <sup>1</sup>H NMR using mesitylene as internal standard.

at time *t* and *C*<sub>0</sub> as its initial concentration). Therefore, the apparent kinetics for the colloidal system in the batch reactor turned out to be a first order reaction with the apparent reaction rate constant determined as  $k_{app, batch} = 2.3 \times 10^{-4} \text{ s}^{-1}$ , or  $0.22 \text{ s}^{-1} \text{ g}^{-1}$  when normalized to mass of palladium and  $6 \times 10^{-4} \text{ s}^{-1} \text{ m}^2$ , when normalized to total catalyst surface area (The PdNP were considered as cuboctahedron clusters for the surface calculation [39]).

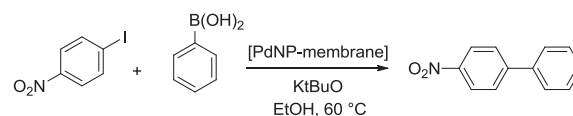
### 3.5.2. Catalytic performance of the membrane

For a catalytic membrane, the reaction time can be expressed as the residence time of the solution inside the membrane (Eq. (5)):

$$\tau = \frac{L}{F} \cdot \varepsilon \cdot S = \varepsilon \cdot \frac{L}{J} \quad (5)$$

where *L* is the membrane thickness (cm), *F* the permeate flow rate (mL/s), *S* the membrane surface area (cm<sup>2</sup>) and *J* the flux density (mL/(s cm<sup>2</sup>)). The membrane thickness *L* is shown on Fig. 4 and equal to 110 μm. The membrane surface area is 12.6 cm<sup>2</sup>. The porosity  $\varepsilon$  is unknown and therefore taken to 1 for the following residence time calculations. The resulting reaction times do not take into account of the membrane porosity which is probably in the range of 0.7–0.8 for this kind of membrane. The real reaction time is thus 0.7–0.8 times smaller than the reaction time reported here.

The benchmark Pd-catalyzed cross-coupling reaction was carried out in ethanol at 60 °C using the catalytic membrane under flow-through conditions (Scheme 4). Results are shown in Table 2. Full conversions were achieved by one single filtration with a residence time of ca. 9 s. No homo-coupling byproducts were observed. Given the selectivity observed in the batch reactor, the



Scheme 4. Pd-catalyzed Suzuki-Miyaura cross-coupling under flow-through conditions.

**Table 2**  
Suzuki-Miyaura cross-coupling reaction catalyzed by the catalytic membrane at different conditions (see Scheme 4).<sup>a</sup>

[C] (mol/L) <sup>b</sup>	Flow rate (mL/min)	Filtration volume (mL)	Pd/substrate molar ratio	$\tau^c$ (s)	Conversion (%) <sup>d</sup>	Selectivity (%) <sup>d</sup>
0.016	1.38	62	1/132	5.8	83.4	100
	0.88			9.1	100	100
0.032	0.88	31		9.1	100	100

<sup>a</sup> Reaction conditions: molar ratio 1-iodo-4-nitrobenzene/phenyl boronic acid/KtBuO/Pd = 1/1.2/2.5/0.007.

<sup>b</sup> Concentration of 1-iodo-4-nitrobenzene.

<sup>c</sup> Residence time.

<sup>d</sup> Determined by GC and <sup>1</sup>H NMR using mesitylene as internal standard.

formation of biphenyl should be much slower than that corresponding to the cross-coupling product formation. In the case of the catalytic membrane, the residence time of reagents in the membrane was so short that the formation of the homo-coupling byproduct was prevented. Actually, the high reactivity of the catalytic membrane favors the chemoselectivity of the process. Interests on catalytic membranes have recently aroused [40,41] but the reaction times of those membranes for Suzuki coupling reactions are in the order of hours and catalyst leaching is produced. Our catalytic membrane herein reported is so efficient that the reaction is complete within seconds.

The isolated yield obtained was 82% for a residence time of 9.1 s. The catalytic membrane was re-used 8 times without activity loss (no more runs were done), showing the robustness of the membrane. TEM analysis after catalytic membrane reusing did not evidence significant changes in the shape and size of the PdNPs (Fig. 7). Actually, a slight increase of the NP diameter occurs but, taking into account the standard deviation, the NP diameter remains practically constant. Neither palladium nor IL was detected in the

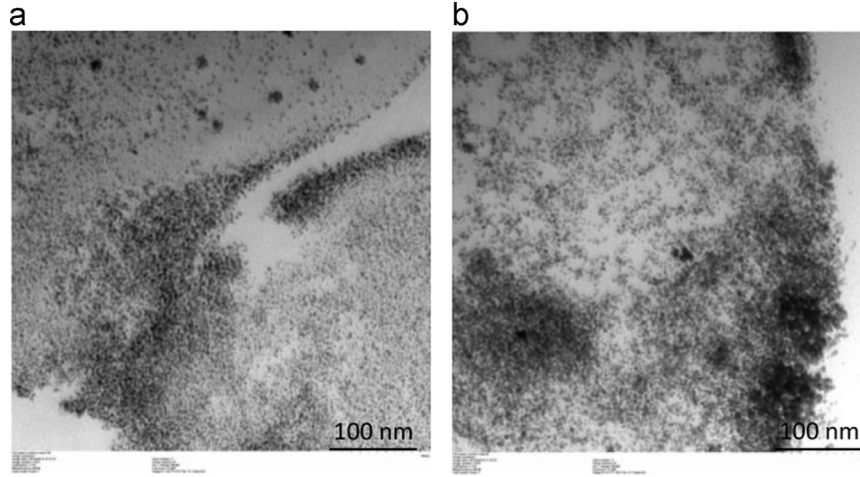


Fig. 7. TEM images of the catalytic membrane: (a) before and (b) after the 9th catalytic run, showing the corresponding PdNP mean diameter.

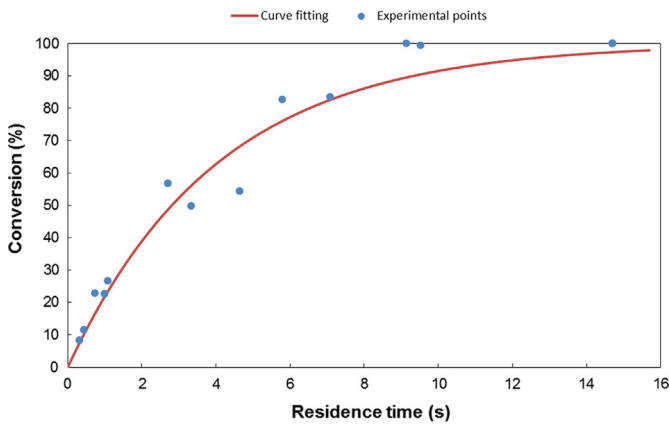


Fig. 8. Conversion as a function of residence time.

product, which proved membrane stability under catalytic conditions and filtration flows.

The reaction was then tested at different flow rates at 60 °C at 1-iodo-4-nitrobenzene concentration of 0.016 mol/L. Conversion increased with residence time as shown in Fig. 8.

$T=60\text{ }^{\circ}\text{C}$ ,  $[1\text{-iodo-4-nitrobenzene}]=0.016\text{ mol L}^{-1}$ , Permeate flux density:  $27\text{-}1300\text{ L h}^{-1}\text{ m}^{-2}$ ; data points at 100% conversion not taken into account for curve fitting.

Nagy established monodimensional complete models of pseudo-homogenous catalytic membrane reactors that allow the prediction of conversion from the physico-chemical parameters, the kinetic constant and the flux density [5]. These models take into account the diffusion and convection mass transfer in the boundary layers above the membrane and inside the membrane (in relation to the reaction) containing the catalytic NP. As the diffusion is a slow process compared to the convection, the Peclet parameter ( $Pe$ ) is used to describe which mechanism is dominant in each part of the catalytic membrane (Eq. (6)).

$$Pe = \frac{v \cdot \delta}{D} \quad (6)$$

where  $v$  is the fluid velocity,  $\delta$  the thickness of the boundary layer or membrane thickness, and  $D$  the diffusion constant. Nagy indicates the diffusion flux can be considered negligible compared to convective flux when  $Pe$  is larger than 3.

Under our experimental conditions, the  $Pe$  of the boundary layer increases from 3.4 to 166 and from 2 to 97 in the catalytic membrane when the flux density rises from 27 to  $1300\text{ L h}^{-1}\text{ m}^{-2}$ .

The diffusion can be neglected at high flux density and have a small influence at low flux density (i.e. high conversion or longer residence time). In contrast to the colloidal system, convective mass transfer becomes dominant in mass transfer for the catalytic membrane. The relative velocity between the fluid and the catalyst equals to the fluid velocity as the catalyst is immobilized inside the membrane.

Isothermal plug flow is achieved in the membrane pores under the experimental conditions [42–45]. Hence a first order pseudo-homogeneous reaction is assumed in a first approach to model the catalytic membrane. Taking into account only the convection and reaction inside the membrane, the differential mass balance can be written as Eq. (7) and solved as Eq. (8) [46]. Then the conversion can be simply expressed as Eq. (9):

$$v \frac{dc}{dz} + k_{app, memb} c = 0 \quad (7)$$

$$\ln \frac{c}{c_0} = -k_{app, memb} \frac{L}{v} \quad (8)$$

$$X = 1 - \frac{c}{c_0} = 1 - e^{-k_{app, memb} \tau} \quad (9)$$

where  $c_0$  is the initial reactant concentration;  $X$  is the conversion;  $k_{app, memb}$  the apparent reaction constant; and  $\tau$  the residence time inside the membrane. It should be noted that this apparent reaction constant is not the true kinetics constant of the reaction. In addition, it disregards the diffusion step towards the catalyst inside the polyIL containing the nanoparticles and the membrane structure which could induce a preferential pathway.

The apparent reaction constant for the membrane was deduced through fitting of Eq. (9) to experimental points (Fig. 8), found to be  $0.25\text{ s}^{-1}$  or  $309.62\text{ s}^{-1}\text{ g}^{-1}$  when normalized to palladium mass, and  $0.4\text{ s}^{-1}\text{ m}^{-2}$  when normalized to palladium surface area (PdNPs considered as cuboctahedron clusters for the surface calculation [39]).

The data points at 100% conversion (low flux density) were not taken into consideration for curve fitting because diffusion can have an influence on mass transfer. It is worth mentioning that, different from Nagy's model, our catalytic membrane is not homogeneous, exhibiting a concentration gradient of PdNPs (see above Fig. 4), which can lead to a reactivity gradient. The deviation between the experimental data and calculated fitting can partly be attributed to the heterogeneous distribution of PdNPs inside the membrane. Comparing with the results under batch conditions ( $k_{app, batch}=0.22\text{ s}^{-1}\text{ g}^{-1}$ ), the catalytic membrane triggered an acceleration of the reaction by three orders of magnitude.



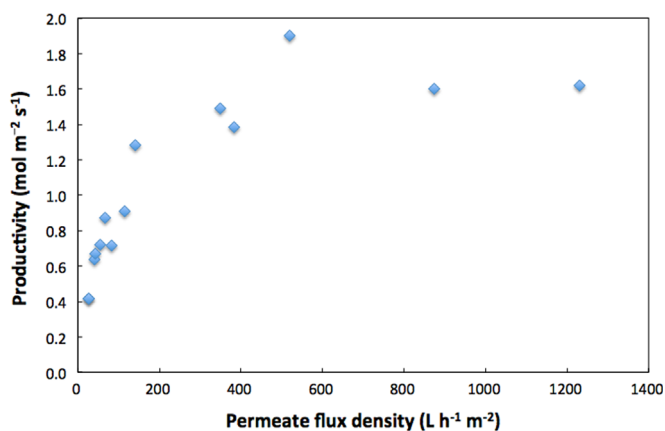


Fig. 9. Productivity per square meter of membrane as a function of permeate flux density. See Fig. 8 for experimental conditions.

In Fig. 9, the productivity per square meter of membrane is plotted versus the permeate flux density. The mass transfer is more effective at higher flow rates where the convection process dominates. Experimental results showed that the membrane offers a higher productivity at a higher flow rate before reaching a maximum plateau, because of the more effective mass transfer (Fig. 9). At low flow rates, the conversion was complete while the productivity was low. When the flow rate increased, the productivity increased and reached its maximum whereas the conversion decreased (Fig. 8). Once the maximum productivity was achieved, the reaction was no more limited by the mass transfer of reactants in the membrane pores, and accordingly the conversion decrease was limited by reactivity (due to the short residence time). Rubinstein show theoretically that when molecule diameter is smaller than the polymer correlation length (average distance from a monomer on one chain to the nearest monomer on another chain), the molecule diffusion coefficient (determined from the Stokes Einstein equation) is mainly determined by the solvent viscosity and not strongly affected by polymers [47]. Since swelling of polyIL in ethanol was observed, the reactant diffusion inside the polyIL should not be a limiting step at high flow rates.

The membrane can continuously be treated at 60 °C under a flow of ca. 1.3 mol h<sup>-1</sup> m<sup>-2</sup> of 1-iodo-4-nitrobenzene at 100% conversion. Besides the acceleration of the reaction, another advantage of the catalytic-based membrane reactors working under flow-through conditions is that they offer a more compact production unit compared to traditional batch reactors, especially in the configuration of hollow fibers. Assuming that the catalytic performance remains when the catalytic membrane is prepared as a hollow fiber and that hollow fiber specific surface (corresponding to a conventional hollow fiber module) is 1000 m<sup>2</sup>/m<sup>3</sup>, then a production capacity of ca. 1300 mol h<sup>-1</sup> m<sup>-3</sup> (ca. 260 kg h<sup>-1</sup> m<sup>-3</sup>) can be achieved for hollow fiber modules.

By immobilizing PdNPs inside the porous polymer matrix, the catalytic membrane succeeds in accelerating the Suzuki–Miyaura cross-coupling reaction. Exerting a higher flow rate helps to improve the reactant mass transfer toward the catalytic nanoparticles which are concentrated inside a polymeric gel. PdNPs inside the reactive zone of the catalytic membrane are smaller and much (200 times) more concentrated than in the colloidal system. The replacement of viscous ionic liquid by ethanol as solvent for the reaction also increases the diffusion coefficient to a large extent (ca. 34 times [35,36]). All these factors together lead to a better catalytic performance of the catalytic membrane in comparison to the colloidal system.

## 4. Conclusions

In summary, we prepared an efficient catalytic membrane using microPES<sup>®</sup> membrane as support and imidazolium-based ionic liquids as modifying agents. The average diameter of the PdNPs stabilized by the polyIL inside the catalytic membrane was ca. 2 nm. No leaching of palladium from the membrane was observed, neither during filtrations nor in the course of the catalytic reaction.

The catalytic membrane showed remarkable catalytic performance on C–C cross-coupling. The membrane was so active that with a residence time of some seconds, the conversion was complete, without formation of byproducts. The desired product was directly and continuously obtained in the permeate once the reaction started. No separation of the catalyst from the product was required. The high efficiency of the catalytic membrane favored a better chemoselectivity towards the kinetically favored product, achieving full conversion under mild conditions.

The catalytic membrane succeeded in greatly accelerating ( $\approx 2000$  times in terms of reaction time for total conversion) the Suzuki–Miyaura cross-coupling reaction compared to the colloidal PdNPs under batch conditions, due to the combination of several effects: smaller nanoparticles and higher catalyst concentration, use of low viscosity swelling solvent, and improved the mass transfer phenomenon. The catalytic membrane gave high productivity at high flow rates. Consequently, the membrane is probably more interesting for diffusion controlled reactions (i.e. fast intrinsic reaction). For kinetic-limited reactions, the acceleration of the process by the membrane may be less significant but significant due to the high PdNP concentration.

Studies concerning the catalytic membrane applications in the synthesis of compounds with added value in fine chemistry are underway.

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## Appendix A. Supporting information

Supplementary data associated with this article can be found in the online version at <http://dx.doi.org/10.1016/j.memsci.2015.05.051>.

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