# A Model of Competing Narratives<sup>†</sup>

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We formalize the argument that political disagreements can be traced to a "clash of narratives." Drawing on the "Bayesian Networks" literature, we represent a narrative by a causal model that maps actions into consequences, weaving a selection of other random variables into the story. Narratives generate beliefs by interpreting long-run correlations between these variables. An equilibrium is defined as a probability distribution over narrative-policy pairs that maximize a representative agent's anticipatory utility, capturing the idea that people are drawn to hopeful narratives. Our equilibrium analysis sheds light on the structure of prevailing narratives, the variables they involve, the policies they sustain, and their contribution to political polarization. (JEL D72, D83, D85, F52)

The idea that political disagreements can be traced to a "clash of narratives" has become commonplace. According to this view, divergent opinions involve more than heterogeneous preferences or information: they can arise from conflicting *stories* about political reality. Accordingly, public-opinion makers try to shape the popular narratives that surround policy debates, because a policy gains in popularity if it can be sustained by an effective narrative.

There are countless expressions of this idea in popular and academic discourse. A journalistic profile of a former aide of President Obama begins with the words "Barack Obama was a writer before he became a politician, and he saw his Presidency as a struggle over narrative."<sup>1</sup> Crow and Jones (2018) write: "There can be little doubt then that people think narratives are important and that crafting, manipulating, or influencing them likely shapes public policy." They add that narratives simplify complex policy issues "by telling a story that includes assertions about what causes what, who the victims are, who is causing the harm, and what should be done."<sup>2</sup>

In this paper we formalize the idea that public-opinion battles involve competing narratives. Of course, the term "narrative" is vague; any formalization inevitably

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<sup>1</sup>See https://www.newyorker.com/magazine/2018/06/18/witnessing-the-obama-presidency-from-start-to-finish.

<sup>2</sup>The quotes are taken from a blog post that discusses Crow and Jones (2018)—see https://blogs.lse.ac.uk/ impactofsocialsciences/2018/07/18/mastering-the-art-of-the-narrative-using-stories-to-shape-public-policy/.

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leaves certain aspects outside the scope of investigation. Echoing the Crow-Jones quote, our model is based on the idea that political narratives can be regarded as *causal models* that map actions to consequences. Following the "Bayesian networks" literature in Statistics, Artificial Intelligence, and Psychology (Cowell et al. 1999, Sloman 2005, Pearl 2009), we represent such causal models by directed acyclic graphs (DAGs).

In our model, what defines a narrative is the variables it incorporates and the way these are arranged in the causal mapping from actions to consequences. For instance, consider a debate over US trade policy and its possible implications for employment. Suppose the public has homogeneous preferences over actions and consequences; disagreements only arise from different beliefs. The DAG

(1) trade policy  $\rightarrow$  imports from China  $\rightarrow$  employment

represents a narrative that weaves a third variable (imports from China) into a causal story about the employment consequences of trade policy.

The nodes in the DAG represent variables (not the values they can take), and the links represent perceived direct causal effects (but not the sign or magnitude of these effects). The variables are coarse-grained, such that the narrative does not describe a single historical episode. Instead, it addresses numerous historical episodes, alerting the public's attention to long-run correlations between adjacent variables along the causal chain and offering a particular causal interpretation of these correlations. In general, our model assumes that when the public adopts a narrative, it constructs a belief by fitting the causal model to objective data. As in Spiegler (2016), this means factorizing the long-run distribution (over the DAG variables) according to the Bayesian-Network factorization formula. The public relies on this belief to evaluate the policy that the narrative promotes, where a policy is defined as a mixture over actions.

We refer to the causal model (1) as a "lever narrative" because it regards imports from China as a "lever" (or a mediator, to use statisticians' jargon), i.e., an endogenous variable that is influenced by actions and in turn influences the target variable. To the extent that imports from China are negatively correlated with both protectionism and employment, this narrative intuitively supports a protectionist policy. But while the support is intuitive, it is illusory if the narrative's causal structure is false, e.g., if the correlation between employment and imports from China is actually due to confounding by exogenous technological change. A false narrative will typically induce a distorted belief regarding the mapping from actions to consequences.

The following is another example of a lever narrative in the context of a foreign policy question, whether to impose economic sanctions on a rival country with a hostile regime. The public considers destabilizing the regime a desirable outcome. A lever narrative that intuitively gives support to a hawkish policy is

sanction policy  $\rightarrow$  economic situation in rival country  $\rightarrow$  regime strength.

The following is a lever narrative that involves a different "lever":

sanction policy  $\rightarrow$  nationalism in rival country  $\rightarrow$  regime strength.

This narrative intuitively supports a *dovish* policy, to the extent that nationalism in the rival country is positively correlated with the strength of its regime and ameliorated by a soft stance on sanctions. We can see that two narratives may have the same "lever" structure but differ in the "lever variables" and consequently in the policies to which they lend intuitive support.

Likewise, the same variable can be assigned different roles in the causal scheme. For instance, the following is a foreign-policy narrative that treats nationalism as an *exogenous* variable:

sanction policy  $\rightarrow$  regime strength  $\leftarrow$  nationalism in rival country.

We refer to a narrative with this structure as a "threat/opportunity narrative," because it regards the third variable as an external factor that the policy needs to cope with (rather than influencing it). In Section IIA we show how this narrative can lend intuitive support to a *hawkish* policy. Thus, narratives can differ in the variables they incorporate or in the role these variables play in the causal mapping from actions to consequences. Different narratives will typically generate different political beliefs because they manipulate correlations between different sets of variables.

But how does the public respond to competing narratives that support conflicting policies? In the context of policy debates, we find it natural to assume that people are drawn to *hopeful* narratives. By "hopeful," we do not mean that appealing narratives portray a rosy picture of the status quo (i.e., the distribution over consequences given historical action frequencies), but rather that they promise a "better future" (i.e., a preferred distribution over consequences) if a different action mixture is implemented. Because individual voters have little influence over public policy, they incur negligible decision costs when indulging in hopeful fantasies about the effects of counterfactual policies. Therefore, anticipatory feelings can be a powerful driving force behind political positions.<sup>3</sup>

Accordingly, we assume that the public selects a narrative-policy pair that maximizes *anticipatory utility*, subject to one empirical-consistency constraint: a narrative is credible if it correctly predicts the empirical distribution over consequences. If this condition is satisfied, the public is ready to believe the narrative's prediction regarding the consequences of a different policy. In other words, narratives can spin hopeful fantasies about the consequences of the policies they espouse, but not about the status quo.

Thus, our model is based on two related premises. First, political beliefs are shaped by narratives, which are simplified causal models that interpret long-run correlations. Second, in the presence of competing narratives, people are drawn to ones that promise a "happy ending." We define an *equilibrium* as a long-run distribution over narrative-policy pairs, such that every element in the support maximizes a representative agent's anticipatory utility, subject to the empirical-consistency constraint above. We refer to this concept as "equilibrium" because the empirical distribution

<sup>&</sup>lt;sup>3</sup> In their book on the use of narratives to win public support, De Graaf, Dimitriu, and Ringsmose (2015, p. 9) argue that one of the major features of an effective narrative is the prospect of success: "... the overarching story told by incumbent policy-makers must, to some extent, be a narrative of progress."

over policies can affect the anticipatory utility from competing narrative-policy. This feedback effect is a hallmark of behavior that is generated by misspecified causal models (see Spiegler 2016), and it is what creates the need for an equilibrium approach to competing narratives.

We employ our equilibrium concept to explore several questions: what is the structure of narratives that support a given policy, and what kind of variables do they involve? Can we account for divergent political beliefs or swings between prevalent political positions? What explains the popularity of certain real-life political narratives? Our results demonstrate the formalism's potential to shed light on such questions.

*Related Literature.*—The idea that people reason about empirical regularities in terms of "causal stories" (representable by DAGs) has been embraced by psychologists of causal reasoning (Sloman 2005, Sloman and Lagnado 2015). In Spiegler (2016), it underlies a model of decisions under causal misperceptions, in which the decision-maker forms a belief by fitting a subjective causal model to long-run data. This remains a building block of his paper, which goes beyond it in two major directions. First, the variables that appear in a causal model are selected endogenously. Second, we assume "hedonic" selection between competing causal models.

We are aware of at least three economics papers that draw attention to the role of narratives in economic contexts. Given that the term "narrative" has such a loose meaning, it should come as no surprise that it has received very different formalizations. Shiller (2017) regards certain terms that appear in popular discourse as indications of specific narratives and proposes to use epidemiological models to study their spread. Bénabou, Falk, and Tirole (2018) focus on moral decision-making and formalize narratives as messages or signals that can affect decision-makers' beliefs regarding the externality of their actions. Levy and Razin (2018) use the term to describe information structures in game-theoretic settings that people postulate to explain observed behavior. Schwartzstein and Sunderam (2019) propose an alternative approach to "persuasion by models," where models are formalized as likelihood functions and the criterion for selecting models is their success in accounting for historical observations.

The idea that people adopt distorted beliefs to enhance their anticipatory utility has precedents in the economics literature (Akerlof and Dickens 1982; Bénabou and Tirole 2002, 2016; Brunnermeier and Parker 2005; Spiegler 2008). Relative to this literature, the key innovation here is that the object of agents' choice is not beliefs but (causal) *models*: wrong beliefs emerge as a consequence of fitting a misspecified model to historical data. This feature constrains agents' ability to distort reality and leads to novel equilibrium effects. Recently, Montiel Olea et al. (2018) studied "competing models" in a different context of experts who compete for the right to make predictions. Each expert believes in a linear regression model that differs in the set of variables it admits. Winning models thus maximize the indirect expected utility they induce when estimated against a random sample.

Finally, our paper joins a handful of works in so-called "behavioral political economics" that study voters' belief formation according to misspecified subjective models or wrong causal attribution rules, e.g., Spiegler (2013), Esponda and Pouzo (2019).

#### I. An Example: "Easy-Fix" Narratives

Before formally presenting our framework, we illustrate its key ideas with a simple example, which also showcases the framework's ability to express ideas that are informally discussed in popular media.

Demagoguery is a common feature of public opinion. Demagogues often spin oversimplified descriptions of a complex social problem, attributing it to a single (often spurious) cause and suggesting it has an "easy fix." This seems to be a hallmark of so-called "populist narratives." By contrast, a "rational" narrative would more faithfully describe the factors behind the social problem and acknowledge that it lacks simple solutions. Our example captures the tension between rational and easy-fix narratives.

Consider a public debate about how an action a can affect an outcome y. In reality, y has a "root cause"  $\theta$  that cannot be influenced by a. Instead, a can only influence s, a "symptom" of  $\theta$ . The actual causal relations among these four variables are represented by the DAG  $G^* : a \to s \leftarrow \theta \to y$ . The long-run distribution p over  $a, \theta, s, y$  obeys the conditional-independence properties that are implied by this causal model. All variables take values in  $\{0, 1\}$ . The long-run frequency of a = 1 is  $p(a = 1) = \alpha$ , to be endogenized later;  $p(\theta = 1) = \delta \in (\varepsilon, 1 - \varepsilon)$ , independently of a, where  $\varepsilon > 0$  is arbitrarily small;  $p(y = \theta | \theta) = 1$  for all  $\theta$ ; and  $p(s = 1 | a, \theta) \equiv a + (1 - a)\theta$ .

We offer two economic stories for this process, in both of which y represents working-class well-being. In one story,  $\theta$  represents technological change, s represents foreign trade, and a represents tariff policy. In the other story,  $\theta$  represents independent trends in developing economies, s represents immigration, and a represents immigration policy.<sup>5</sup>

A representative agent (referred to as "the public") needs to choose a policy, which is a probability mixture over actions. We let d denote the weight the policy puts on a = 1, and force it to lie in  $[\varepsilon, 1 - \varepsilon]$ ; this restriction will later ensure that  $\alpha \in (0, 1)$ . The public's payoff is  $y - (1/2)(d - \varepsilon)^2$ . That is, y = 1 is the desirable outcome, and any departure from the lowest possible policy is costly.

The public faces a supply of policy recommendations. Each recommendation is coupled with a narrative, which is a DAG over some subset of the four relevant variables. For the sake of this example, imagine there are only two possible narratives: the "rational narrative" given by the correct DAG  $G^*$ , and the "easy-fix narrative" given by the DAG  $G^e : a \to s \to y$ . The latter is a lever narrative that neglects the root cause of y and misrepresents the symptom s as a lever for changing y.<sup>6</sup>

We think of narrative-policy pairs (G, d) as being proposed by implicit "narrators" (news outlets, politicians, pundits). We do not model narrators explicitly as distinct

<sup>&</sup>lt;sup>4</sup> In general, we need p to have full support, in order to avoid certain zero-probability events. In this example we only need to require that  $\alpha, \delta \in (0, 1)$ .

<sup>&</sup>lt;sup>5</sup>David Frum proposed that rising income and human capital in developing countries allows more individuals to migrate into developed economies: see "If Liberals Won't Enforce Borders, Fascists Will," *The Atlantic Magazine*, April 2019, https://www.theatlantic.com/magazine/archive/2019/04/ david-frum-how-much-immigration-is-too-much/583252/.

<sup>&</sup>lt;sup>6</sup>Our analysis is robust to expanding the set of feasible narratives to include all DAGs in which *a* is an ancestral node and there is a direct link  $a \rightarrow s$  (consistent with the interpretation that *a* is a policy instrument that manifestly impacts *s*).

agents, because this is not necessary for our model (in analogy to the shadow role of price makers in competitive equilibrium). To evaluate a narrative-policy pair, the public computes its induced expected anticipatory payoff, and adopts a pair (G,d) that offers the highest anticipatory payoff. This means that G is the "prevailing narrative" and the policy d gets implemented (such that a = 1 is taken with probability d).

We will now motivate a notion of a steady state in this scenario of competing narrative-policy pairs. As with other equilibrium concepts in economic theory (such as competitive equilibrium), we have in mind an underlying dynamic adjustment process. At every time period, narrative-policy pairs vie for public support. The public has a long but bounded memory. To calculate its anticipatory utility from each pair, in a way we describe below, it relies on the empirical frequencies of  $(a, \theta, s, y)$  in the *M* most recent periods, where *M* is arbitrarily large (such that *p* approximates these frequencies). The action taken at that period is a random draw from the selected policy. This action influences the realization of *s* (but not  $\theta$  and *y*). The same scenario is repeated in the next period.

We will later see that as the *M*-truncated history changes over time, so can the relative appeal of different narrative-policy pairs. This is what makes the dynamic process nontrivial. We look for a notion of a steady state of this process. Again, as with other equilibrium concepts in economics, ours is defined in purely static terms; the dynamic story that motivates it remains in the background.

Let us begin from a putative steady state in which the only prevailing narrative is  $G^*$ . Because this narrative correctly describes the causal structure underlying p, it correctly predicts that y = 1 with probability  $\delta$ , regardless of the action taken. Therefore, a narrative-policy pair  $(G^*, d)$  will induce the anticipatory payoff  $\delta - (1/2)(d - \varepsilon)^2$ . Only narrators who accompany  $G^*$  with the ideal policy  $\varepsilon$  will prevail, inducing an anticipatory utility of  $\delta$ . The steady-state action frequency  $\alpha$  would be  $\varepsilon$ .

Yet now suppose that a narrator enters this seemingly stable public-opinion scene with a narrative-policy pair  $(G^e, d)$ , where  $d > \varepsilon$ . To calculate the anticipatory payoff induced by this pair, we first define the conditional consequence distribution induced by the easy-fix narrative:

(2) 
$$p_{G^{e}}(y|a) = \sum_{s=0,1} p(s|a)p(y|s)$$

This definition captures the idea that the belief is formed by *fitting* the causal model  $G^e: a \to s \to y$  to the long-run distribution p. The interpretation is as follows. Since the easy-fix narrative postulates that a influences y via the lever s, it alerts the public to the conditional distributions (p(s|a)) and (p(y|s)) and combines them in accordance with the causal chain  $a \to s \to y$ . Thus,  $G^e$  invites the public to view long-run correlations through prism of a particular causal model.

Let us now calculate the terms in (2), given our specification of p:

$$p(s = 1 | a = 1) = 1,$$
  

$$p(s = 1 | a = 0) = \delta,$$
  

$$p(y = 1 | s = 1) = \frac{\delta}{\delta + (1 - \delta)\alpha}$$
  

$$p(y = 1 | s = 0) = 0.$$

Therefore, the anticipatory utility induced by  $(G^{e}, d)$  is

(3) 
$$U(G^{e}, d; \alpha) = d \cdot 1 \cdot \frac{\delta}{\delta + (1 - \delta)\alpha} + (1 - d) \cdot \delta \cdot \frac{\delta}{\delta + (1 - \delta)\alpha} - \frac{1}{2}(d - \varepsilon)^{2}$$
$$= \delta \cdot \frac{\delta + (1 - \delta)d}{\delta + (1 - \delta)\alpha} - \frac{1}{2}(d - \varepsilon)^{2}.$$

Since  $\alpha = \varepsilon \approx 0$  under the putative stable long-run distribution,  $U(G^e, d; \alpha) \approx \delta + (1 - \delta)d - (1/2)d^2$ . The policy that maximizes this expression is  $d = 1 - \delta$ , inducing an anticipatory utility of  $\delta + (1/2)(1 - \delta)^2$ . This is strictly higher than  $\delta$ , which, as we recall, is the anticipatory utility delivered by the narrative-policy pair  $(G^*, \varepsilon)$ . This means that when  $G^*$  is the only prevailing narrative, the resulting long-run distribution is unstable. A demagogic narrator can invade the public-opinion scene with the easy-fix narrative and a non-ideal policy, a combination that will become more popular than the existing narrative-policy pair. Although the proposed policy is costly, the easy-fix narrative (falsely) argues that the benefit outweighs the cost because the social problem has a simple solution.

Note that although  $G^e$  conveys a false promise conditional on deviating from the status quo policy  $\alpha$ , it does correctly predict the expected outcome if the policy adheres to the status quo: when we plug  $d = \alpha$ , we obtain

$$\alpha \cdot p_{G^{e}}(y = 1 | a = 1) + (1 - \alpha) \cdot p_{G^{e}}(y = 1 | a = 0) = \delta.$$

Note that this equation would hold for any  $\alpha$ . Thus, the narrative  $G^e$  is partly credible, in the sense that it makes an accurate prediction if the status quo policy is maintained. We will later refer to (a weaker version of) this property as No Status Quo Distortion (NSQD).

The rise to dominance of the pair  $(G^e, 1 - \delta)$  when  $\alpha = \varepsilon$  means that over time, the frequency of a = 1 will gradually shift upward, since  $1 - \delta > \varepsilon$ . However, as  $\alpha$  increases,  $U(G^e, 1 - \delta; \alpha)$  goes down. The intuition is that as the gap between the status quo and proposed policies shrink, the easy-fix narrative's power to convey false hope diminishes. As a result, the policy that maximizes (3) decreases with  $\alpha$ . By comparison, the anticipatory utility of the pair  $(G^*, \varepsilon)$  remains  $\delta$  even as  $\alpha$  increases.

A stable point of this process will be reached when the long-run action frequency hits a level  $\alpha^*$  for which  $U(G^e, d^e; \alpha^*) = \delta$ , where  $d^e = \operatorname{argmax}_d U(G^e, d; \alpha^*)$ . In this case, the two pairs  $(G^*, \varepsilon)$  and  $(G^e, d^e)$  both maximize anticipatory utility, such that either of them can prevail. Moreover, this equilibrium is locally stable. If  $\alpha$  is perturbed above (below)  $\alpha^*$ , the rational (easy-fix) narrative will become more popular and its accompanying policy will be implemented; this will cause  $\alpha$  to gradually shift back down (up) toward  $\alpha^*$ .

In general, we will define an equilibrium as a distribution  $\sigma$  over pairs (G, d) that maximize the public's anticipatory utility (subject to the NSQD constraint), calculated against the long-run action frequency induced by  $\sigma$  itself. The

complete characterization of equilibrium in our example is given by the following conditions:

$$d^{e} = \arg \max_{d} \left( \delta \cdot \frac{\delta + (1 - \delta)d}{\delta + (1 - \delta)\alpha^{*}} - \frac{1}{2}(d - \varepsilon)^{2} \right),$$
  

$$\delta = \delta \cdot \frac{\delta + (1 - \delta)d^{e}}{\delta + (1 - \delta)\alpha^{*}} - \frac{1}{2}(d^{e} - \varepsilon)^{2},$$
  

$$\alpha^{*} = \sigma(G^{e}, d^{e}) \cdot d^{e} + \sigma(G^{*}, \varepsilon) \cdot \varepsilon,$$

where  $\sigma$  describes the frequency with which each of the two narrative-policy pairs prevail. In the  $\varepsilon \to 0$  limit, the solution is

$$d^{e} = \sqrt{\left(\frac{\delta}{1-\delta}\right)^{2} + 2\delta} - \frac{\delta}{1-\delta},$$
$$\alpha^{*} = \frac{1}{2}d^{e},$$
$$\sigma(G^{e}, d^{e}) = \frac{1}{2}.$$

Thus, in equilibrium the rational and easy-fix narratives prevail with equal frequency.

This result uncovers a subtle interplay between rational and easy-fix narratives. The rational narrative acknowledges that *a* cannot influence the root cause of *y*. Therefore, it cannot offer the illusion of a "happy ending"; the only consolation it offers is a justification for taking the costless, ideal policy  $\varepsilon$ . In contrast, the easy-fix narrative misinterprets the correlation between *s* and *y* as a causal effect and therefore conveys an illusion that departing from the ideal policy can improve *y*. Yet the easy-fix narrative feeds off the rational narrative, and needs it as a foil. Without the rational narrative,  $\alpha^*$  would coincide with the easy-fix narrative's endorsed policy, thus robbing it of the ability to convey false hope. The narrative's appeal originates from the departure of its accompanying policy from the status quo  $\alpha^*$ . For this to happen, the rational narrative *must* belong to the support of the equilibrium distribution. In other words, *demagoguery needs the rational narrative as a rival; it can only thrive if public opinion gives some room to the rational narrative*.

Another insight concerns comparative statics with respect to  $\delta$ . One might think that demagogues would flourish when underlying objective prospects are dire. However, as we can see, the popularity of the easy-fix narrative is 1/2, independently of  $\delta$ . In addition, the departure of  $d^e$  from the ideal policy is not monotone with respect to  $\delta$ . Instead,  $d^e$  (and consequently  $\alpha^*$ ) is hump-shaped with respect to  $\delta$ (attaining a maximum at  $\delta \approx 0.32$ ). The reason is that the easy-fix narrative's belief distortion arises from misattributing the fluctuations in y. The narrative's ability to instill a false hope hinges on having enough historical variation in y. An increase in  $\delta$  in its low region increases the variability of y, and therefore leaves more room for the easy-fix narrative to stoke false hope by attributing this variation in y to the wrong cause. Thus, the effect of demagoguery can actually become *stronger* when the underlying situation is better.

#### II. The Model

Let  $X = X_1 \times \cdots \times X_m$ , where m > 2 and  $X_i = \{0,1\}$  for each  $i = 1, \ldots, m$ . For every  $N \subseteq \{1, \ldots, m\}$ , denote  $X_N = \prod_{i \in N} X_i$ . For any  $x \in X$ , the components  $x_1$  and  $x_m$ , also denoted a and y, are referred to as the *action* and the *consequence*. Let  $p \in \Delta(X)$  be an objective probability distribution with full support. Denote  $p(a = 1) = \alpha$  and  $p(y = 1) = \mu$ . We interpret  $\alpha$  as a historical, long-run action frequency and endogenize it later in this section. The exogenous components of p are given by the collection of conditional probabilities  $(p(x_2, \ldots, x_m \mid a))$ .

A directed acyclic graph (DAG) is a pair G = (N, R), where  $N \subseteq \{1, ..., m\}$  is a set of nodes and  $R \subseteq N \times N$  is a set of directed links. Acyclicity means that the graph contains no directed path from a node to itself. We use iRj or  $i \rightarrow j$  to denote a directed link from the node *i* into the node *j*. Abusing notation, let  $R(i) = \{j \in N | jRi \}$  be the set of "parents" of node *i*. Following Pearl (2009), we interpret a DAG as a *causal model*, where the link  $i \rightarrow j$  means that  $x_i$  is perceived as an immediate cause of  $x_j$ . Directedness and acyclicity of *G* are consistent with basic intuitions regarding causality. The causal model is agnostic about the sign or magnitude of causal effects.

Let  $\mathcal{G}$  be a collection of DAGs. We refer to an element in  $\mathcal{G}$  as a *narrative*. Every  $G \in \mathcal{G}$  satisfies the following restrictions. First,  $\{1,m\} \subseteq N$ —i.e., all feasible narratives involve actions and consequences. Second,  $|N| \leq n$ , where  $n \in \{2, \ldots, m\}$  is an exogenously given constant that represents an upper bound on narrative complexity. Third, 1 is an *ancestral* node. This restriction means that actions have no prior causes. We relax this restriction in Section IV. In applications, we will impose additional restrictions on  $\mathcal{G}$  because certain causal models are implausible in the relevant context (e.g., assuming that tariff policy has no causal effect on imports).

From Narratives to Beliefs.—Given an objective distribution p, a narrative G = (N, R) induces a subjective belief over  $X_N$ , defined as follows:

(4) 
$$p_G(x_N) = \prod_{i \in N} p(x_i | x_{R(i)}).$$

The full-support assumption ensures that all the terms in this factorization formula are well defined.<sup>7</sup>

The conditional distribution of  $x_m$  given  $x_1$  induced by  $p_G$  is computed in the usual way. It has a simple expression because 1 is an ancestral node:

(5) 
$$p_G(x_m | x_1) = \sum_{x_{N-\{1,m\}}} \left( \prod_{i \in N-\{1\}} p(x_i | x_{R(i)}) \right).$$

<sup>7</sup>When  $R(i) = \emptyset, p(x_i | x_{R(i)}) = p(x_i)$ , i.e., an ancestral node enters the formula with its marginal probability.

The fact that 1 is ancestral also ensures that this conditional distribution has a natural interpretation as a perceived causal effect of  $x_1$  on  $x_m$ .

For illustration, when n = m = 4 and the narrative is  $G: 1 \rightarrow 3 \rightarrow 4 \leftarrow 2$ ,

$$p_G(x_1, x_2, x_3, x_4) = p(x_1)p(x_2)p(x_3 | x_1)p(x_4 | x_2, x_3),$$

and

$$p_G(x_4 | x_1) = \sum_{x_2, x_3} p(x_2) p(x_3 | x_1) p(x_4 | x_2, x_3).$$

The induced marginal distribution over consequences is

(6) 
$$p_G(x_m) = \sum_{x_1, \dots, x_{m-1}} p_G(x_1, \dots, x_m)$$

Formula (4) is the standard Bayesian-network factorization formula (see Spiegler 2016 and the references therein). Its interpretation in the current context is as follows. A narrative selects up to n - 2 variables (other than the action and the consequence) and incorporates them into a causal story. This is akin to a novelist who conjures up a collection of events, and then organizes their unfolding according to a plot. The narrative generates a subjective belief regarding the mapping from actions to consequences, by drawing the audience's attention to particular correlations deemed relevant by the causal model and combining them in accordance with the model. Each term in the factorization (4) is correctly extracted from the objective distribution p. It is the way the terms are combined that may lead to distorted beliefs.

Policies and Anticipatory Utility.—A policy  $d \in [\varepsilon, 1 - \varepsilon]$  is a proposed frequency of playing the action a = 1, where  $\varepsilon > 0$  is arbitrarily small.<sup>8</sup> A representative agent has a utility function  $u(y,d) = y - C(d - d^*)$ , where  $d^*$  is the agent's ideal policy, and C is a symmetric, twice-differentiable and convex cost function that satisfies C(0) = 0. Thus, y = 1 is the agent's desirable outcome, and C represents the intrinsic disutility he experiences when deviating from his ideal policy.

Given p, a narrative-policy pair (G, d) induces gross anticipatory utility

(7) 
$$V(G,d;\alpha) = d \cdot p_G(y = 1 | a = 1) + (1-d) \cdot p_G(y = 1 | a = 0)$$

This is simply the subjective probability of the good outcome y = 1 under the policy *d*, according to  $p_G$ . The agent's net anticipatory utility from the narrative-policy pair (G, d) given *p* is

(8) 
$$U(G,d;\alpha) = V(G,d;\alpha) - C(d-d^*).$$

The notation  $V(G, d; \alpha)$  highlights a crucial feature, which was illustrated in Section I: a change in  $\alpha$  (namely the marginal of p over a) can alter  $p_G(y|a)$ . This would be impossible under rational expectations, as p(y|a) is invariant to  $\alpha$  by definition.

<sup>&</sup>lt;sup>8</sup>We define a policy as a mixture over actions rather than identifying it with a, in order to prevent certain interesting effects from being obscured.

Since the only payoff-relevant variables are *a* and *y*, variables that are perceived as consequences of *y* can be safely ignored: dropping them from *G* will not change  $p_G(y|a)$ . Therefore, from now on we will assume that *y* is a *terminal* node in any  $G \in \mathcal{G}$ . This entails no loss of generality.

*No Status Quo Distortion.*—Recall that we require *a* to be an ancestral node in *G*. It immediately follows from (4) that  $p_G(a = 1) = \alpha$ , and therefore

(9) 
$$V(G, \alpha; \alpha) = p_G(a = 1) \cdot p_G(y = 1 | a = 1)$$
  
  $+ p_G(a = 0) \cdot p_G(y = 1 | a = 0) = p_G(y = 1)$ 

In other words, the gross anticipatory utility from a "status quo policy" that mimics the objective long-run action frequencies is equal to the ex ante probability of a good outcome implied by  $p_G$ .

DEFINITION 1 (No Status Quo Distortion): A DAG G satisfies No Status Quo-Distortion (NSQD) with respect to  $\alpha$  if  $V(G, \alpha; \alpha) = \mu$ .

Viewed formally, NSQD is the familiar Bayes plausibility condition: the expected posterior distribution over *y* should coincide with its marginal distribution. In the present context, it can be interpreted as follows. When considering the narrative *G*, the public may contemplate its implications under the status quo policy  $\alpha$ . If  $V(G, \alpha; \alpha) \neq \mu$ , it is as if the narrative makes an absurd statement: "Let us keep doing what we have done so far, and the outcome will be different." NSQD rules out such narratives. It allows narratives to make false promises about *counterfactual* policies, but it does not allow them to distort the status quo.

By (9), NSQD is equivalent to requiring  $p_G(y = 1) = \mu$ . This enables a more direct interpretation of NSQD as an empirical-consistency criterion that constrains narratives' ability to delude the public: prevailing narratives must not induce beliefs that distort the steady-state distribution over consequences. The justification is that while testing correlations between variables is a difficult task for the lay public, monitoring the long-run behavior of the target variable y is relatively easy. Therefore, it would be relatively easy to discredit a narrative G that induces  $p_G(y = 1) \neq \mu$ .

*Equilibrium.*—The model's exogenous components are the conditional distribution  $(p(x_2, ..., x_m | x_1))$ , the set of feasible narratives  $\mathcal{G}$ , the ideal policy  $d^*$ , and the cost function C. That is, when a narrator constructs a narrative G, he can only choose among the DAGs in  $\mathcal{G}$ , and the belief  $(p_G(x_m | x_1))$  that his narrative induces (computed according to (5)) is constrained by the distribution  $(p(x_2, ..., x_m | x_1))$ .

For any probability distribution  $\sigma$  over narrative-policy pairs (G, d), let

$$lpha(\sigma) \;=\; \sum_{(G,d)} \sigma(G,d) \,\cdot\, d$$

be the overall probability of a = 1 implied by  $\sigma$ .

DEFINITION 2: A probability distribution  $\sigma$  over narrative-policy pairs (G, d) constitutes an equilibrium if any  $(G, d) \in \text{supp}(\sigma)$  maximizes  $U(G, d; \alpha(\sigma))$  subject to the constraint that G satisfies NSQD with respect to  $\alpha(\sigma)$ .

The solution concept captures a steady state in the battle over public opinion: prevailing narrative-policy pairs are those that maximize the representative agent's net anticipatory utility, subject to the NSQD constraint. This reflects the idea that voters do not adjudicate between narratives using "scientific" methods; rather, they are attracted to narratives with a "happy ending." Faced with contradictory causal models, the public behaves as if it believes, paraphrasing George Box's famous quote, that "all models are wrong, but some are hopeful."<sup>9</sup>

In Definition 2, the public's anticipatory utility is evaluated against  $\alpha(\sigma)$ , the action frequency that is induced by the marginal of  $\sigma$  over policies (the restriction that  $d \in (0, 1)$  ensures that  $\alpha(\sigma)$  is interior, too). This condition aims to capture a dynamic process behind our notion of equilibrium, as illustrated in Section I. At any point in time, a particular policy rises to dominance because its accompanying narrative appeals to the public. Over time, as the long-run action frequency gravitates toward the dominant policy, the anticipatory payoff from various narrative-policy pairs can change. As a result, a different narrative-policy pair can become dominant. While  $\sigma$  describes the long-run frequencies with which different narrative-policy pairs prevail,  $\alpha(\sigma)$  is the long-run average action that results from the periodic swings between dominant narrative-policy pairs. In Section III, we will provide a local-stability result that further substantiates this interpretation.

An alternative, purely static interpretation views the representative agent as a unit mass of identical voters, each of whom adopts one narrative-policy pair. According to this "cross-sectional" interpretation,  $\sigma(G,d)$  describes the popularity of (G,d), namely, the fraction of voters who adopt it. One of the voters is drawn at random from  $\sigma$  and implements his favored policy. The resulting average action is precisely  $\alpha(\sigma)$ .

The following is a simple rational-expectations benchmark. Suppose that  $\mathcal{G}$  consists of a single narrative  $G : a \to y$ . Then,  $p_G(y|a) \equiv p(y|a)$ . Any equilibrium  $\sigma$  will assign probability 1 to policies d that maximize  $d \cdot p(y = 1 | a = 1) + (1 - d) \cdot p(y = 1 | a = 0) - C(d - d^*)$ . When C is strictly convex, the equilibrium is unique. From now on, we depart from this benchmark and assume that the model's primitives are minimally rich in the following sense.

DEFINITION 3: The pair  $(p, \mathcal{G})$  is non-null if there exist  $G, G' \in \mathcal{G}$ , such that  $p_G(y|a)$  is nonconstant in a and  $p_{G'}(y|a) = \mu$  for all a.

Thus, the set of feasible narratives is rich enough to enable a belief that actions can affect consequences, as well as a belief that the distribution of consequences is independent of actions. For instance, if  $\mathcal{G}$  contains a DAG in which *a* and *y* are

<sup>&</sup>lt;sup>9</sup>Dahlstrom (2014, p. 13617) writes that "narratives can also perpetuate misinformation ... accepted narratives are trusted so much that individuals rarely allow evidence to contradict the narrative; evidence is altered to fit their narratives." McComas and Shanahan (1999) and Szostek (2018) also argue that people's attachment to a particular narratives is not necessarily based on scientific scrutiny.

both ancestral nodes, as well as a DAG  $a \to x_k \to y$  such that  $x_k$  is correlated with both a and y, then  $\mathcal{G}$  is non-null. All the results in the paper take it for granted that  $(p, \mathcal{G})$  is non-null.

## PROPOSITION 1: An equilibrium exists.

The proof of this result involves constructing an auxiliary game, such that existence of Nash equilibrium in this game is equivalent to existence of our notion of equilibrium.

Comment: Perfect DAGs and NSQD.—In certain cases, the DAG's structure alone ensures NSQD. A DAG (N,R) is perfect if whenever iRk and jRk for some  $i,j,k \in N$ , it is the case that iRj or jRi. Thus, in a perfect DAG, if two variables are perceived to be direct causes of a third variable, there must be a perceived direct causal link between them. For example,  $1 \rightarrow 2 \rightarrow 3$  is perfect (because the condition holds vacuously), whereas  $1 \rightarrow 3 \leftarrow 2$  is imperfect. Perfection is a familiar property in the Bayesian-networks literature. In our context, the crucial property of perfection is its relation to NSQD. If G is perfect, then  $V(G, \alpha; \alpha) = \mu$  for every objective distribution p with any given  $\alpha, \mu$ . Conversely, if G is imperfect, we can find objective distributions for which NSQD fails. This result is stated and proved in Spiegler (2020) in a different context. Thus, from now on, we only need to check NSQD for imperfect DAGs.

*Comment: Strengthening NSQD.*—The equilibrium concept requires that in  $\sigma$ , prevailing narratives satisfy NSQD with respect to  $\alpha(\sigma)$ . However, if we commit to the dynamic-stability interpretation of equilibrium, we may wish to strengthen the concept, such that prevailing narratives satisfy NSQD also with respect to any  $\alpha$  in a neighborhood of  $\alpha(\sigma)$ . The reason is that if we perturb  $\alpha$  from its equilibrium level, we do not want the narratives that prevail in  $\sigma$  to be disqualified because they fail to satisfy NSQD. In practice, all the results in this paper remain intact if we adopt this alternative definition.

## A. An Example: Foreign-Policy Narratives

The following example captures a debate over foreign policy in some country. Let m = n = 3. The three variables are as follows. The action *a* represents the attitude toward a rival country having a hostile regime, where a = 1 (0) denotes a hawkish (dovish) attitude. The consequence *y* represents the hostile regime's strength, where y = 1 (0) indicates a weak (strong) regime. The third variable, denoted *s*, represents nationalistic sentiments in the rival country, where s = 1 (0) indicates strong (weak) nationalism.

The exogenous aspects of the objective distribution p are as follows. First, p(y = 1) = 1/2, regardless of the chosen action a. That is, foreign policy has no effect on the hostile regime's strength. Second, p(s = 1 | a, y) = (a + 1 - y)/2. Thus, nationalism is positively correlated with both hawkish policy and regime strength. However, these two correlations have different causal meaning. The correlation between a and s is causal: hawkish (dovish) policy tends

to strengthen (weaken) nationalism in the other country. In contrast, the correlation between *s* and *y* is *not* causal; rather, it is due to confounding by unmodeled exogenous factors.

The set  $\mathcal{G}$  consists of all DAGs that include a (as an ancestral node) and y. The set is classified as follows: the lever narrative  $G^L: a \to s \to y$ ; the threat/opportunity narrative  $G^O: a \to y \leftarrow s$ ; and all remaining narratives, which can be shown to induce the rational-expectations belief ( $p_G(y = 1 | a) = 1/2$  for all a). Finally, the parameter  $\varepsilon$  that defines D is vanishingly small. The cost function is  $C \equiv 0$ , hence the value of  $d^*$  is immaterial.

CLAIM 1: There is a unique equilibrium  $\sigma$ ; supp $(\sigma^*) = \{(G^L, \varepsilon), (G^O, 1 - \varepsilon)\}$ and  $\sigma(G^O, 1 - \varepsilon) \approx 0.57$ .

PROOF:

We first derive  $p_G(y|a)$  for every  $G \in \mathcal{G}$ . Any G that induces  $p_G(y = 1|a) = 1/2$  for all a would generate  $U(G, d; \alpha) = 1/2$  for any  $d, \alpha$ . Now consider the narrative  $G^O$ :

$$p_{G^{0}}(y = 1 | a) = p(s = 1)p(y = 1 | a, s = 1) + p(s = 0)p(y = 1 | a, s = 0).$$

Plugging our specification of p(a, y, s) = p(a)p(y)p(s | a, y), we obtain

$$p(s = 1) = \alpha \cdot \frac{1}{2} \cdot 1 + (1 - \alpha) \cdot \frac{1}{2} \cdot 0 + \left[\alpha \cdot \frac{1}{2} + (1 - \alpha) \cdot \frac{1}{2}\right] \cdot \frac{1}{2} = \frac{1}{4} + \frac{\alpha}{2}$$

and

$$p(y = 1 | a = 1, s = 1) = \frac{\alpha \cdot \frac{1}{2} \cdot \frac{1}{2}}{\alpha \cdot \frac{1}{2} \cdot \frac{1}{2} + \alpha \cdot \frac{1}{2} \cdot 1} = \frac{1}{3},$$

$$p(y = 1 | a = 1, s = 0) = \frac{\alpha \cdot \frac{1}{2} \cdot \frac{1}{2}}{\alpha \cdot \frac{1}{2} \cdot \frac{1}{2} + \alpha \cdot \frac{1}{2} \cdot 0} = 1,$$

$$p(y = 1 | a = 0, s = 1) = 0,$$

$$p(y = 1 | a = 0, s = 0) = \frac{(1 - \alpha) \cdot \frac{1}{2} \cdot 1}{(1 - \alpha) \cdot \frac{1}{2} \cdot 1 + (1 - \alpha) \cdot \frac{1}{2} \cdot \frac{1}{2}} = \frac{2}{3}$$

Therefore,

$$p_{G^o}(y = 1 | a = 1) = \frac{5}{6} - \frac{\alpha}{3},$$
  
$$p_{G^o}(y = 1 | a = 0) = \frac{1}{2} - \frac{\alpha}{3},$$

such that

$$W(G^{O},d;\alpha) = d\left(\frac{5}{6}-\frac{\alpha}{3}\right) + (1-d)\left(\frac{1}{2}-\frac{\alpha}{3}\right).$$

Plugging  $d = \alpha$ , we can confirm that  $V(G^O, \alpha; \alpha) = 1/2$  regardless of  $\alpha$ . Therefore,  $G^O$  satisfies NSQD. Note that for any  $\alpha$ ,  $V(G^O, d; \alpha)$  is strictly increasing in *d*. Therefore, if  $(G^O, d)$  is in the support of the equilibrium, then  $d = 1 - \varepsilon$ . Since  $V(G^O, 1 - \varepsilon; \alpha) \approx (5/6) - (\alpha/3) > 1/2$  for any  $\alpha < 1$ , it follows that no narrative that induces rational expectations can prevail in equilibrium.

Next, consider the narrative  $G^L$ :

$$p_{G^{l}}(y = 1 | a) = p(s = 1 | a)p(y = 1 | s = 1) + p(s = 0 | a)p(y = 1 | s = 0).$$

Plugging our specification of p, we obtain

$$p(s = 1 | a = 1) = \frac{1}{2} \cdot \frac{1}{2} + \frac{1}{2} \cdot 1 = \frac{3}{4},$$
  
$$p(s = 1 | a = 0) = \frac{1}{2} \cdot 0 + \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4},$$

and

$$p(y = 1 | s = 1) = \frac{\frac{\alpha}{2} \cdot \frac{1}{2} + \frac{1 - \alpha}{2} \cdot 0}{\frac{1}{4} + \frac{\alpha}{2}} = \frac{\alpha}{1 + 2\alpha},$$
$$p(y = 1 | s = 0) = \frac{\frac{\alpha}{2} \cdot \frac{1}{2} + \frac{1 - \alpha}{2} \cdot 1}{\frac{3}{4} - \frac{\alpha}{2}} = \frac{2 - \alpha}{3 - 2\alpha}.$$

Therefore,

$$p_{G^{\mathcal{L}}}(y = 1 | a = 1) = \frac{3}{4} \left(\frac{\alpha}{1+2\alpha}\right) + \frac{1}{4} \left(\frac{2-\alpha}{3-2\alpha}\right) = \frac{1+6\alpha-4\alpha^2}{2(1+2\alpha)(3-2\alpha)},$$
  
$$p_{G^{\mathcal{L}}}(y = 1 | a = 0) = \frac{1}{4} \left(\frac{\alpha}{1+2\alpha}\right) + \frac{3}{4} \left(\frac{2-\alpha}{3-2\alpha}\right) = \frac{3+6\alpha-4\alpha^2}{2(1+2\alpha)(3-2\alpha)},$$

such that

(10) 
$$V(G^L, d; \alpha) = d \cdot \frac{1 + 6\alpha - 4\alpha^2}{2(1 + 2\alpha)(3 - 2\alpha)} + (1 - d) \cdot \frac{3 + 6\alpha - 4\alpha^2}{2(1 + 2\alpha)(3 - 2\alpha)}$$

Because  $G^L$  is perfect, it necessarily satisfies NSQD (as can be verified by setting  $d = \alpha$  in (10)). Note that for any  $\alpha$ ,  $V(G^L, d; \alpha)$  is strictly decreasing in d. Therefore, if  $(G^L, d)$  is in the support of the equilibrium, then  $d = \varepsilon$ .

We have seen that any narrative  $G \neq G^O, G^L$  cannot prevail in equilibrium. We now show that both  $G^O$  and  $G^L$  belong in the equilibrium support. Assume the contrary, and suppose  $G^O$  is the only narrative in the support. Then, as shown above, it will be paired with the policy  $d = 1 - \varepsilon$ , such that  $\alpha = 1 - \varepsilon$ . Since  $G^O$  satisfies NSQD,  $V(G^O, 1 - \varepsilon; 1 - \varepsilon) = 1/2$ . But since  $V(G^L, \varepsilon; 1 - \varepsilon) \approx 5/6$ ,  $(G^O, 1 - \varepsilon)$ does not maximize the agent's anticipatory payoff, a contradiction. Similarly, if  $G^L$  is the only prevailing narrative, it is paired with  $d = \varepsilon$ , such that  $\alpha = \varepsilon$  and therefore  $V(G^O, 1 - \varepsilon; \varepsilon) \approx 5/6$ , reaching a similar contradiction. Thus,  $\operatorname{supp}(\sigma)$  consists of exactly two narrative-policy pairs:  $(G^L, \varepsilon)$  and  $(G^O, 1 - \varepsilon)$ . This means that  $V(G^L, \varepsilon; \alpha) = V(G^O, 1 - \varepsilon; \alpha)$ , which for  $\varepsilon \to 0$  can be written as

$$\frac{3+6\alpha-4\alpha^2}{2(1+2\alpha)(3-2\alpha)} \approx \frac{5}{6} - \frac{\alpha}{3}.$$

This equation has a unique solution in [0,1],  $\alpha \approx 0.57$ . Finally, note that in the  $\varepsilon \to 0$  limit,  $\alpha = \sigma(G^0, 1 - \varepsilon)$ .

This example has a number of noteworthy features.

Coupling of Narratives and Policies.—In this example, s is the only variable (other than a and y) that narrators can weave into their stories. However, its location in the narrative turns out to determine the endorsed policy. The narrative that sustains a hawkish policy treats s as an exogenous factor, whereas the narrative that sustains a dovish policy treats s as a lever.

The reason that  $G^L$  promotes dovish policies is that *a* and *s* are positively correlated whereas *s* and *y* are negatively correlated. The lever narrative combines these correlations in a causal chain  $a \rightarrow s \rightarrow y$ . As a result,  $G^L$  (falsely) predicts a negative indirect causal effect of *a* on *y*.

The intuition for why  $G^O$  is coupled with a hawkish policy is subtler. The specification of p(s|a, y) means that s is a (stochastic) function of the difference a - y. This means that for a given s, an increase in a implies an increase in the conditional probability that y = 1. In reality, this effect is purely diagnostic, yet  $G^O$  treats it as causal. Moreover,  $G^O$  regards the distribution of s as independent of a. It follows that  $G^O$  (falsely) predicts a positive causal effect of a on y.

Multiple Prevailing Narratives.—As in the example of Section I, the equilibrium distribution assigns weight to *two* policies. The "cross-sectional" interpretation of this effect is political polarization: two divergent narrative-policy pairs dominate public opinion. As in Section I, the dynamic interpretation of equilibrium can be backed by an explicit local stability argument, thanks to a "diminishing returns" property:  $V(G^L, \varepsilon; \alpha)$  is increasing in  $\alpha$ , whereas  $V(G^O, 1 - \varepsilon; \alpha)$  is decreasing in  $\alpha$ . That is, each narrative's ability to delude the public diminishes as the policy it endorses gets implemented more frequently. If we perturb  $\alpha$  above its equilibrium level (i.e., increase the frequency of a = 1),  $(G^L, \varepsilon)$  becomes more appealing than  $(G^O, 1 - \varepsilon)$ , and therefore the prevailing policy will be dovish for some time. This pushes  $\alpha$  back toward its original level. A similar argument applies to downward perturbation of  $\alpha$ .

*Hawkish Bias.*—The example's primitives treat the two actions symmetrically:  $p(s|a = 1, y) \equiv p(s|a = 0, y)$  and the agent has no intrinsic preference over policies. Nevertheless, the equilibrium action frequency is biased to the right. The reason is that  $G^O$  induces a false correlation  $p_G o(y = 1 | a = 1) - p_G o(y = 1 | a = 0) = 1/3$  (regardless of  $\alpha$ ), which is larger in absolute terms than the correlation  $-1/((1+2\alpha)(3-2\alpha))$  induced by  $G^L$ . At  $\alpha = 1/2$ , this gives  $G^O$  an advantage over  $G^L$  in terms of their induced anticipatory utility. The

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"diminishing returns" property described above means that to equalize the narratives' anticipatory utility,  $\alpha$  has to be greater than 1/2.

*Comment: Mutual Narrative Refutation.*—Our representative agent does not reason "scientifically" about conflicting narratives. He does not actively seek correlational data to test narratives. Instead, he allows "narrators" to determine the data he pays attention to. Thus,  $G^L$  alerts him to the conditional distributions (p(s|a)) and (p(y|s)), whereas  $G^O$  alerts him to (p(s)) and (p(y|a,s)). The data that one narrative invokes also manages to refute the *competing* narrative. The distribution (p(s|a)) referred to by  $G^L$  shows that s and a are correlated, *contra*  $G^O$ . Likewise, the distribution (p(y|a,s)) referred to by  $G^C$  demonstrates that y and a are correlated conditional on s, *contra*  $G^L$ . How would our agent react if this mutual refutation were pointed out to him? A rational reaction would be to distrust all narratives and develop a more "scientific" belief-formation method. Yet an arguably more realistic reaction would be to shrug, conclude that "all models are wrong" and adopt the more hopeful one: especially in the political context, where the agent has virtually no "skin in the game."<sup>10</sup>

## **III.** Analysis

The illustrative examples raise the question of whether policy divergence is an inherent feature of equilibrium. Our first result answers in the affirmative. Throughout the section, we assume that C is strictly convex. While this is not a necessary assumption, it does rule out uninteresting knife-edge cases.

**PROPOSITION 2:** Suppose C is strictly convex. Then, any equilibrium assigns positive probability to exactly two policies,  $d_r \ge d^*$  and  $d_l \le d^*$ .

## PROOF:

Fix an equilibrium  $\sigma$ . First, let us show that every  $(G, d) \in \operatorname{supp}(\sigma)$  induces  $U(G, d; \alpha(\sigma)) \geq \mu$ . Assume the contrary. By minimal richness,  $\mathcal{G}$  includes the DAG  $G^*$ , which consists of two unlinked nodes, a and y. Note that  $p_G(y|a) = \mu$  for every a. It follows that the narrative-policy pair  $(G^*, d^*)$  generates the net payoff  $U(G^*, d^*; \alpha(\sigma)) = \mu$ , contradicting the first part of the definition of equilibrium.

Next, we establish that the support of  $\sigma$  must include at least two distinct policies. Assume the contrary, i.e., the marginal of  $\sigma$  over d is degenerate. Then by definition, it assigns probability one to the steady-state policy  $\alpha(\sigma)$ . By NSQD,  $V(G, \alpha(\sigma); \alpha(\sigma)) = \mu$  for every narrative G in the support of  $\sigma$ . There are now two cases to consider.

**Case 1:**  $\alpha(\sigma) \neq d^*$ . Any narrative G in the support of  $\sigma$  delivers  $U(G, \alpha(\sigma); \alpha(\sigma)) = \mu - C(\alpha(\sigma) - d^*)$ . By assumption, C'(0) = 0 and C''(0) > 0, such that

<sup>&</sup>lt;sup>10</sup>Consider a modified example that replaces *s* with *two distinct variables* with the same conditional distribution. The formal analysis would be the same. However, the two conflicting narratives can invoke different variables, such that the mutual refutation would be infeasible.

 $C(\alpha(\sigma) - d^*) > 0$ . Therefore,  $U(G, \alpha(\sigma); \alpha(\sigma)) < \mu$ , contradicting our previous step.

**Case 2:**  $\alpha(\sigma) = d^*$ . Any narrative *G* in the support of  $\sigma$  delivers  $U(G, \alpha(\sigma); \alpha(\sigma)) = \mu$ . By our assumption that  $(p, \mathcal{G})$  is non-null,  $\mathcal{G}$  contains the DAG  $G^{**}: a \to x_i \to y$ , where  $x_i$  is correlated with both *a* and *y* according to *p*. Without loss of generality, suppose  $p(x_i = 1 | a = 1) > p(x_i = 1 | a = 0)$  and  $p(y = 1 | x_i = 1) > p(y = 1 | x_i = 0)$ . Since  $G^{**}$  is perfect, it satisfies NSQD, such that  $U(G^{**}, \alpha(\sigma); \alpha(\sigma)) = \mu$ . The derivative of  $V(G^{**}, d; \alpha(\sigma))$  with respect to *d* is  $p_{G^{**}}(y = 1 | a = 1) - p_{G^{**}}(y = 1 | a = 0)$ , which can be written as

$$[p(x_i = 1 | a = 1) - p(x_i = 1 | a = 0)] [p(y = 1 | x_i = 1) - p(y = 1 | x_i = 0)].$$

By assumption, both terms in this product are nonzero, hence the derivative of  $V(G^{**}, d; \alpha(\sigma))$  with respect to *d* is nonzero. Since C'(0) = 0, it follows that there is  $d \neq d^*$ , such that  $U(G^{**}, d; \alpha(\sigma)) > \mu$ , again contradicting the first part in the definition of equilibrium.

We now show that the support cannot contain more than two policies. By definition, any  $(G,d) \in \text{supp}(\sigma)$  maximizes  $V(G,d;\alpha(\sigma)) - C(d-d^*)$  subject to the NSQD constraint  $V(G,\alpha(\sigma);\alpha(\sigma)) = \mu$ . This means that we can rewrite  $V(G,d;\alpha(\sigma))$  as follows:

(11) 
$$V(G,d;\alpha(\sigma)) = \frac{d-\alpha}{1-\alpha(\sigma)} \cdot p_G(y = 1 | a = 1) + \frac{1-d}{1-\alpha(\sigma)} \cdot \mu$$
$$= \left(1 - \frac{d}{\alpha(\sigma)}\right) \cdot p_G(y = 1 | a = 0) + \frac{d}{\alpha(\sigma)} \cdot \mu.$$

It follows that the narratives that maximize U given  $(d, \alpha(\sigma))$  subject to NSQD depend only on the *ordinal* ranking between d and  $\alpha(\sigma)$ . That is, for every  $(G,d) \in \text{supp}(\sigma)$ , such that  $d \ge \alpha(\sigma)$ , G maximizes  $p_G(y = 1 | a = 1)$ . Likewise, for every  $(G,d) \in \text{supp}(\sigma)$ , such that  $d \le \alpha(\sigma)$ , G maximizes  $p_G(y = 1 | a = 0)$ . Note that when  $d = \alpha(\sigma)$ , any G that satisfies NSQD maximizes U.

This means that  $\max_G V(G, d; \alpha(\sigma))$  is piecewise linear in d, having a weakly positive slope in the range  $d \ge \alpha(\sigma)$  and a weakly negative slope in the range  $d \le \alpha(\sigma)$ , where at least one of these slopes is nonzero. Because C is strictly convex, it follows that there exist unique  $d_r$  and  $d_l$  that maximize U in the ranges  $d \ge \alpha(\sigma)$  and  $d \le \alpha(\sigma)$ , respectively. It follows that there are at most two policies in the support of the equilibrium distribution, and that they lie (weakly) on different sides of  $\alpha(\sigma)$ .

It remains to establish that  $d_r \ge d^*$  and  $d_l \le d^*$ . We have already shown that it cannot be the case that  $d_r = d_l = d^*$ . Assume  $d_r$  and  $d_l$  are (strictly) on the same side of  $d^*$ . Without loss of generality, let  $d_r > d_l > d^*$ . The second part of the definition of equilibrium implies  $d_l < \alpha(\sigma) < d_r$ . Since  $d_l < \alpha(\sigma)$ , we saw that if  $(G, d_l) \in \text{supp}(\sigma)$ , then G maximizes  $p_G(y = 1 | a = 0)$ . Since  $d^* < d_l$ , it follows that the pair  $(G, d^*)$  would attain a strictly higher U than  $(G, d_l)$ , contradicting the first part of the definition of equilibrium.

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Thus, the support of an equilibrium policy distribution consists of two elements that lie (weakly) on different sides of  $d^*$ . The fundamental insight is that under the NSQD constraint, narratives cannot convey hopeful illusions unless they are coupled with *counterfactual* policies. For this to happen, these policies must depart from the status quo policy  $\alpha(\sigma)$ .

Unlike other results in this paper, the proof does not make explicit use of the DAG formalism. Rather, it relies on non-nullness and the NSQD constraint. NSQD implies that if the equilibrium distribution assigns probability one to a single policy d, prevailing narratives cannot distort the policy's consequences. Non-nullness implies that some other narrative-policy pair could then invade and generate higher anticipatory utility (e.g., if  $d \neq d^*$ , a "narrator" can promote the ideal policy  $d^*$  with a "denialist" narrative that a has no effect on y). This establishes that there must be multiple prevailing policies. But why exactly *two*? By NSQD, the set of narratives that maximize anticipatory utility only depends on whether their accompanying policy is above or below  $\alpha(\sigma)$ . This means that the indirect gross anticipatory utility is piecewise-linear with respect to d. Strict convexity of C then implies a unique optimal policy on each side of  $\alpha(\sigma)$ .

REMARK 1: Proposition 2 allows  $d_r$  or  $d_l$  to coincide with  $d^*$ . Slight modifications of non-nullness rule out this possibility. For instance, suppose that  $d^* > \varepsilon$ and that  $\mathcal{G}$  includes two DAGs G and G', such that  $p_G(y = 1|a)$  and  $p_{G'}(y = 1|a)$  are strictly increasing and strictly decreasing in a, respectively. Then,  $d_l < d^* < d_r$ .

In Section I, we provided a dynamic story that underlies our notion of equilibrium. We now present a formal local-stability result that further substantiates this interpretation.

DEFINITION 4: An equilibrium  $\sigma$  is locally stable if there is a neighborhood of  $\alpha(\sigma)$ , such that for every  $\alpha$  in the neighborhood and every (G,d) that maximizes  $U(G,d;\alpha)$ , sign $(\alpha - \alpha(\sigma)) \cdot \text{sign}(d - \alpha) < 0$ .

Local stability of an equilibrium  $\sigma$  means that if  $\alpha$  is perturbed to one side of  $\alpha(\sigma)$ , all narrative-policy pairs that prevail under the perturbed  $\alpha$  push back toward  $\alpha(\sigma)$ . The examples of Sections I and IIA both exhibited this local stability property.

**PROPOSITION 3:** Suppose C is strictly convex. Suppose further that for every  $G \in \mathcal{G}$  and  $d \in [\varepsilon, 1 - \varepsilon]$ ,  $V(G, d; \alpha)$  is monotone in  $\alpha$ . Then, there is an essentially unique equilibrium, which is also locally stable.<sup>11</sup>

Thus, when V is monotone in  $\alpha$ , the dynamic backstory for our equilibrium concept is well founded. Although the definition of local stability focuses on the dynamics of  $\alpha$ , what ensures that every U-maximizing pair (G, d) under the perturbed  $\alpha$ pushes it back toward  $\alpha(\sigma)$  is a combination of two factors: the monotonicity of V,

<sup>&</sup>lt;sup>11</sup>By essential uniqueness, we mean that the distribution over d is unique, and that the belief induced by the narratives that accompany any given d in the support is unique.

and the equilibrium property that all (G, d) in the support of  $\sigma$  maximize U under  $\alpha(\sigma)$ . Note that thanks to NSQD, monotonicity is in the direction that ensures the "diminishing returns" property highlighted in Section IIA: when a prevailing pair (G, d) satisfies  $d > \alpha(\sigma)$  ( $d < \alpha(\sigma)$ ),  $V(G, \cdot; \alpha)$  will decrease (increase) in  $\alpha$ . A remaining open problem is whether all DAGs satisfy this monotonicity property.

*Comment: Relative Anticipatory Utility.*—Our narrative-selection assumption captured the idea that political narratives are popular when they convey a hopeful message. A different intuition regarding the source of successful narratives is that they make the proposed policy look good *relative* to some other policy (the status quo, or a policy proposed by an opponent).

This intuition can be captured by simple variants on our equilibrium concept: e.g., we can require every (G,d) in  $\operatorname{supp}(\sigma)$  to maximize  $U(G,d;\alpha(\sigma)) - U(G,\alpha(\sigma);\alpha(\sigma))$ , i.e., the public evaluates the proposed policy according to its anticipatory utility relative to the status quo policy. Similarly, we can require every (G,d) in  $\operatorname{supp}(\sigma)$  to maximize  $U(G,d;\alpha(\sigma)) - U(G,d';\alpha(\sigma))$  for some  $(G',d') \in \operatorname{supp}(\sigma)$ , i.e., the public evaluates the proposed policy according to its anticipatory utility relative to a policy promoted by some competing "narrator." In both cases, the anticipatory utility is calculated according to the narrative *G* that carries the proposed policy *d*.

Simple algebra establishes that for any  $(G,d) \in \text{supp}(\sigma)$ , *G* maximizes (minimizes)  $p_G(y = 1 | a = 1) - p_G(y = 1 | a = 0)$  if *d* is above (below) the reference policy. In turn, the NSQD constraint ensures that this is equivalent to maximizing  $p_G(y = 1 | a = 1) (p_G(y = 1 | a = 0))$ . The implication is that the equilibrium characterization is qualitatively the same as in our main model. The set of prevailing narratives is the same, and the only difference may be in the exact location of the narratives  $d_h$  and  $d_l$  (because the trade-off between the gross anticipatory utility term and the cost *C* is different).

## A. Short Narratives

In this subsection we characterize equilibria when narrators can use at most one variable in addition to *a* and *y* (i.e., n = 3). We focus on the case in which *a* and *y* are objectively *independent*. In this setting, the only narratives that can generate a nonconstant  $p_G(y|a)$  are the lever and threat/opportunity narratives. Our objective is to examine which of the two narratives will prevail, and which auxiliary variables they will employ.

For this purpose, we assume that  $m \gg n$  and the supply of potential auxiliary variables (identified with their distribution conditional on a, y) is rich, such that narrators can select the third variable in their narrative from an "ocean" of potential variables. To introduce our notion of richness, let z be an arbitrary binary variable, and define  $Q^*$  to be the set of all conditional distributions (p(z|a,y)) for which p(z|a)p(z|y) = 0 for *some* a, y, z. That is, a conditional distribution in  $Q^*$  allows a particular value of a or a particular value of y to pin down deterministically the value of z. Finally, two sets of conditional distributions are close if the Hausdorff distance between any pair of elements from the two respective sets is below some arbitrarily small threshold.

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DEFINITION 5: Let  $m \gg n = 3$ . An objective distribution p satisfying  $a \perp y$  is  $Q^*$ -rich if  $\{(p(x_i = 1 \mid a, y))\}_{i=2,...,m-1}$  and  $Q^*$  are close.

Note,  $Q^*$ -richness says that the set of conditional distributions (p(z|a, y)) that one can simulate by selecting one auxiliary variable approximately coincides with  $Q^*$ . We impose this domain restriction because on the one hand it is relatively weak (thus allowing for a large supply of potential auxiliary variables), yet on the other hand it is tractable.<sup>12</sup>

Four particular elements in  $Q^*$  will play a special role in our characterization. These are degenerate conditional distributions for which  $p(z = 1 | a, y) \in \{0, 1\}$  for *every a*, *y*. Specifically, define

> $q_1^{\wedge}: \qquad z = \mathbf{1}(a = 1 \text{ and } y = 1),$   $q_1^{\vee}: \qquad z = \mathbf{1}(a = 1 \text{ or } y = 1),$   $q_0^{\wedge}: \qquad z = \mathbf{1}(a = 0 \text{ and } y = 1),$  $q_0^{\vee}: \qquad z = \mathbf{1}(a = 0 \text{ or } y = 1).$

**PROPOSITION** 4: Suppose  $d^* > \varepsilon$ . Then, for a generic  $Q^*$ -rich distribution p, there is an essentially unique equilibrium  $\sigma$ :

- (i) The policy  $d_r > \alpha$  is accompanied by a lever narrative  $a \to x_r \to y$ , where  $(p(x_r | a, y))$  is close to  $q_1^{\wedge}$  or  $q_1^{\vee}$ .
- (ii) The policy  $d_l < \alpha$  is accompanied by a lever narrative  $a \to x_l \to y$ , where  $(p(x_l|a, y))$  is close to  $q_0^{\wedge}$  or  $q_0^{\vee}$ .

Thus, for generic  $Q^*$ -rich distributions, lever narratives prevail. The reason is that narratives that induce rational expectations generate lower anticipatory payoff, whereas threat/opportunity narratives generically violate NSQD, as shown in Step 1 of the proof of Proposition 4 (the foreign policy example of Section IIA was knife-edged in this regard). The lever narratives employ degenerate auxiliary variables. The following result completes the characterization for low  $C, \varepsilon$ .

**REMARK** 2: Let C and  $\varepsilon$  be vanishingly small. Then, the equilibrium  $\sigma$  satisfies

(i) 
$$\alpha(\sigma) \approx \frac{1}{2}$$
.  
(ii) If  $\mu < \frac{1}{2}$ , then  $(p(x_r | a, y)) \approx q_1^{\vee}$  and  $(p(x_l | a, y)) \approx q_0^{\vee}$ .  
(iii) If  $\mu > \frac{1}{2}$ , then  $(p(x_r | a, y)) \approx q_1^{\wedge}$  and  $(p(x_l | a, y)) \approx q_0^{\wedge}$ .

<sup>&</sup>lt;sup>12</sup>Numerical simulations suggest that the results of this subsection will continue to hold if we replace  $Q^*$  with the set of *all* conditional distributions (p(z|a, y)).

For real-life examples of lever narratives that are captured by this characterization, recall the US trade policy debate from the introduction. The lever narrative that sustains a policy with a protectionist bias (relative to the agent's ideal point) will involve a variable like "imports from China," because low imports are associated with trade restrictions as well as high employment in the local manufacturing sector. The narrative is false if the latter correlation is not causal but, say, due to a confounding factor (e.g., exogenous technology changes that affect outsourcing of production). Likewise, the lever narrative that sustains a trade policy with a liberalized bias will select a variable like "industrial exports."

#### **IV. State-Dependent Narrative Selection**

So far, we have assumed that narrative-policy pairs are evaluated without conditioning on any variable. However, the appeal of a given narrative often varies with changing circumstances. In this section, we extend the definition of equilibrium in this direction and illustrate the extended concept.

Recall the collection of variables  $x_1, \ldots, x_m$ , where  $x_1$  (also denoted a) is the action and  $x_m$  (also denoted y) is the consequence. Let  $m \ge 3$  and assume that the variable  $x_2$  (also denoted  $\theta$ ) is realized and publicly observed before the narrative-policy pair is evaluated. We refer to  $\theta$  as a "state variable." For every  $\theta$ , define  $\alpha_{\theta} = p(a = 1 | \theta)$ , and let  $\sigma_{\theta}$  denote a distribution over narrative-policy pairs (G, d) conditional on  $\theta$ . Denote  $\alpha = (\alpha_{\theta})_{\theta}$  and  $\sigma = (\sigma_{\theta})_{\theta}$ . For any  $\sigma$ , we denote  $\alpha_{\theta}(\sigma) = \sum_{(G,d)} \sigma_{\theta}(G,d) \cdot d$  and  $\alpha(\sigma) = (\alpha_{\theta}(\sigma))_{\theta}$ .

Given a DAG G and an objective distribution p, the belief  $p_G$  is defined as before, and the conditional probability  $p_G(y|a, \theta)$  is defined as usual. Define the gross conditional anticipatory utility

$$V(G,d;\alpha | \theta) = d \cdot p_G(y = 1 | \theta, a = 1) + (1 - d) \cdot p_G(y = 1 | \theta, a = 0).$$

Net anticipatory utility is  $U(G, d; \alpha | \theta) = V(G, d; \alpha | \theta) - C(d - d^*)$ .

In this context, we will say that G satisfies NSQD with respect to  $\alpha$  if

$$\sum_{\theta} p(\theta) V(G, \alpha_{\theta}; \alpha \,|\, \theta) \;=\; \mu$$

DEFINITION 6: The conditional distribution  $\sigma$  is an equilibrium if, for every  $\theta$  and every  $(G',d') \in \operatorname{supp}(\sigma_{\theta}), (G',d') \in \operatorname{argmax}_{(G,d)} U(G,d;\alpha(\sigma)|\theta)$  subject to the constraint that G satisfies NSQD with respect to  $\alpha(\sigma)$ .

At first glance, this may seem like an uninteresting state-by-state extension of our equilibrium concept. However, note that the NSQD constraint is global. In addition, depending on how a narrative treats  $\theta$ , the objective distribution of certain variables at one value of  $\theta$  can influence their subjective distribution conditional on another value of  $\theta$ . This externality is what makes the extension interesting, as the following example demonstrates.

An Example: Denialism and Exaggeration.—Let m = n = 3, where the three variables are the action *a*, the consequence *y*, and the state variable  $\theta$ . Let  $p(\theta = 1)$ 

=  $\delta$  and  $p(y = 1 | a, \theta) = (1/2)(a + \theta)$ . Let  $d^* = \varepsilon$ , where  $\varepsilon$  is arbitrarily small. Assume *C* is strictly convex and steep enough, such that C'(1) > 1. Because  $p(y = 1 | a, \theta)$  is additively separable, the optimal policy under rational expectations is  $d^{RE} = \operatorname{argmax}_d((1/2)d - C(d))$ , independently of  $\theta$ . By the assumptions on *C*,  $d^{RE}$  is interior and given by  $C'(d^{RE}) = 1/2$ .

Let  $\mathcal{G}$  be the set of all DAGs with a direct link  $\theta \to a$ . The interpretation is that the representative agent is aware that actions are taken in response to  $\theta$ ; a plausible narrative would incorporate this manifest causal relation. As before, we can assume that y is a terminal node without loss of generality. Then,  $\mathcal{G}$  consists of the following four DAGs:  $G^d: a \leftarrow \theta \rightarrow y$ ;  $G^e: \theta \rightarrow a \rightarrow y$ ; the DAG  $G^n$  that removes the link  $a \rightarrow y$  from  $G^e$ ; and the fully connected DAG  $G^{RE}$  that adds the link  $\theta \rightarrow y$ to  $G^e$ . The latter is the only DAG in  $\mathcal{G}$  that is consistent with p, because all the others rule out the direct effect of a or  $\theta$  on y. All DAGs in  $\mathcal{G}$  are perfect, hence we can take NSQD for granted.

One concrete story for this example is an environmental-policy debate concerning the management of a natural resource. In this context,  $\theta$  represents exogenous fluctuations in the availability of this resource, y represents the resource's net availability, and a represents preservation policy, where a = 1 stands for costly preservation measures (hence the assumption that  $d^* = \varepsilon$ ). Accordingly,  $G^d$  is a "denialist" narrative that neglects the role of policy and attributes the consequence entirely to exogenous forces. In contrast,  $G^e$  is an "exaggerationist" narrative that effectively says "it is all up to us." The DAG  $G^n$  is a "neutral" narrative because it does not attribute the outcome to any of the other variables.

CLAIM 2: There is a unique equilibrium, which is characterized as follows:

(i)  $\operatorname{supp}(\sigma_1) = \{ (G^{RE}, d^{RE}), (G^d, \varepsilon) \};$ (ii)  $\operatorname{supp}(\sigma_0) = \{ (G^e, d^{RE}), (G^n, \varepsilon) \};$ (iii)  $\alpha_1(\sigma) = \alpha_0(\sigma) = d^{RE} - 2C(d^{RE}).$ 

## PROOF:

Let  $\sigma$  be an equilibrium, and use the shorthand notation  $\alpha_{\theta} = \alpha_{\theta}(\sigma)$ . Let us calculate  $p_G(y = 1 | a, \theta)$  for each of the four available narratives:

$$\begin{split} p_{G^{RE}}(y \ = \ 1 \ | \ a, \theta) \ &= \ p(y \ = \ 1 \ | \ a, \theta) \ = \ \frac{1}{2}(a + \theta), \\ p_{G^n}(y \ = \ 1 \ | \ a, \theta) \ &= \ p(y \ = \ 1) \ = \ \frac{1}{2}[\delta(1 + \alpha_1) + (1 - \delta) \, \alpha_0] \\ p_{G^d}(y \ = \ 1 \ | \ a, \theta) \ &= \ p(y \ = \ 1 \ | \ \theta) \ &= \ \frac{1}{2}(\alpha_\theta + \theta), \\ p_{G^e}(y \ = \ 1 \ | \ a, \theta) \ &= \ p(y \ = \ 1 \ | \ a) \ &= \ \frac{1}{2}[a + p(\theta \ = \ 1 \ | \ a)], \end{split}$$

where

$$p(\theta = 1 | a = 1) = \frac{\delta \alpha_1}{\delta \alpha_1 + (1 - \delta) \alpha_0},$$

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$$p(\theta = 1 | a = 0) = \frac{\delta(1 - \alpha_1)}{\delta(1 - \alpha_1) + (1 - \delta)(1 - \alpha_0)}.$$

It follows that the net anticipatory utility induced by a policy d coupled with any of the four narratives is

$$\begin{split} U(G^{RE}, d | \theta) &= \frac{1}{2} \theta + \frac{1}{2} d - C(d), \\ U(G^{n}, d | \theta) &= \frac{1}{2} \big[ \delta(1 + \alpha_{1}) + (1 - \delta) \alpha_{0} \big] - C(d), \\ U(G^{d}, d | \theta) &= \frac{1}{2} (\alpha_{\theta} + \theta) - C(d), \\ U(G^{e}, d | \theta) &= \frac{1}{2} d - C(d) + \frac{1}{2} \bigg[ \frac{\delta \alpha_{1} d}{\delta \alpha_{1} + (1 - \delta) \alpha_{0}} + \frac{\delta(1 - \alpha_{1})(1 - d)}{\delta(1 - \alpha_{1}) + (1 - \delta)(1 - \alpha_{0})} \bigg]. \end{split}$$

The policy that maximizes net anticipatory utility under  $G^d$  or  $G^n$  is  $d^* = 0$ . Therefore, if any of these narratives prevails in some state, it must be coupled with d = 0. Likewise, the policy that maximizes net anticipatory utility under  $G^{RE}$  is  $d^{RE}$ . Therefore, if this narrative prevails in some state, it must be coupled with  $d^{RE}$ . As to the narrative  $G^e$ , the policy  $d^e$  that maximizes net anticipatory utility under this narrative satisfies  $d^e > d^{RE} (d^e < d^{RE})$  whenever  $\alpha_1 > \alpha_0$  ( $\alpha_1 < \alpha_0$ ).

Note that it follows from C'(1) > 1 that even under the most optimistic belief that is induced by one of the narratives, the optimal policy would always be strictly below 1. Hence,  $\alpha_{\theta} < 1$  for all  $\theta$ .

Consider the realization  $\theta = 1$ . Suppose  $\alpha_1 = 0$ . Then,

$$U(G^{RE}, d^{RE} | \theta = 1) = \frac{1}{2} + \max_{d} \left[ \frac{1}{2} d - C(d) \right] > \frac{1}{2},$$

whereas

$$U(G^{n}, 0 | \theta = 1) = \frac{1}{2} [\delta + (1 - \delta) \alpha_{0}] < \frac{1}{2},$$
$$U(G^{d}, 0 | \theta = 1) = \frac{1}{2}.$$

In addition, for any *d* and for all  $\alpha_0$ ,

$$\frac{1}{2}d \cdot \frac{(1-\delta)(1-\alpha_0)}{\delta + (1-\delta)(1-\alpha_0)} - C(d) + \frac{1}{2} \cdot \frac{\delta}{\delta + (1-\delta)(1-\alpha_0)} < \frac{1}{2}d - C(d) + \frac{1}{2}d$$

which implies that  $U(G^e, d^e | \theta = 1) < U(G^{RE}, d^{RE} | \theta = 1)$ . Therefore,  $(G^{RE}, d^{RE})$  must be the prevailing narrative-policy pair, contradicting the assumption that  $\alpha_1 = 0$ .

It follows that  $\alpha_1 > 0$ . Since for any  $\alpha_0$  and for any d,

(12) 
$$\frac{\delta\alpha_1 d}{\delta\alpha_1 + (1-\delta)\alpha_0} + \frac{\delta(1-\alpha_1)(1-d)}{\delta(1-\alpha_1) + (1-\delta)(1-\alpha_0)} < 1$$

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we have that  $U(G^e, d | \theta = 1) < U(G^{RE}, d | \theta = 1)$ , and hence,  $G^e$  cannot be a prevailing narrative in  $\theta = 1$ . Likewise, a simple calculation establishes that  $U(G^d, 0 | \theta = 1) > U(G^n, 0 | \theta = 1)$ . Therefore,  $G^n$  is not a prevailing narrative in  $\theta = 1$ .

It follows that the only narrative-policy pairs that can prevail in  $\theta = 1$  are  $(G^{RE}, d^{RE})$  and  $(G^d, 0)$ . Their induced net anticipatory utility is

$$U(G^{RE}, d^{RE} | \theta = 1) = \frac{1}{2}(d^{RE} + 1) - C(d^{RE}),$$
$$U(G^{d}, 0 | \theta = 1) = \frac{1}{2}(\alpha_{1} + 1).$$

If  $\operatorname{supp}(\sigma_1) = \{(G^d, 0)\}$ , then  $\alpha_1 = 0$ , which we have already ruled out. Suppose  $\operatorname{supp}(\sigma_1) = \{(G^{RE}, d^{RE})\}$ . Then,  $\alpha_1 = d^{RE}$ , in which case it is obvious that  $U(G^{RE}, d^{RE} | \theta = 1) < U(G^d, 0 | \theta = 1)$ , a contradiction. The only remaining case is that  $\operatorname{supp}(\sigma_1) = \{(G^d, 0), (G^{RE}, d^{RE})\}$ . Then,  $U(G^{RE}, d^{RE} | \theta = 1) = U(G^d, 0 | \theta = 1)$ , which implies  $\alpha_1 = d^{RE} - 2C(d^{RE})$ . The first-order-condition characterization of  $d^{RE}$  and the strict convexity of *C* ensure that indeed,  $\alpha_1 \in (0, 1)$ . This completes the characterization of  $\sigma_1$ . Note that it is independent of  $\sigma_0$ .

Next, consider the realization  $\theta = 0$ . For any d, the difference,  $U(G^e, d | \theta = 0) - U(G^{RE}, d | \theta = 0)$ , is equal to half of the left-hand side of (12), which is positive since  $\alpha_1 > 0$ . Therefore,  $G^{RE}$  cannot be a prevailing narrative in  $\theta = 0$ . Likewise,  $U(G^n, 0 | \theta = 0) > U(G^d, 0 | \theta = 0)$ , and hence,  $G^d$  cannot be a prevailing narrative in  $\theta = 0$ . It follows that in  $\theta = 0$  the only narrative-policy pairs that can prevail are  $(G^e, d^e)$  and  $(G^n, 0)$ , where  $d^e = \operatorname{argmax}_d U(G^e, d | \theta)$  (from the strict convexity of C, this function has a unique maximum).

Let us guess an equilibrium in which  $\alpha_0 = \alpha_1$ . Then  $U(G^e, d | \theta = 0) = (1/2)d - C(d) + (1/2)\delta$ , and the policy that maximizes it is  $d^e = d^{RE}$ . Thus,

$$U(G^{e}, d^{e} | \theta = 0) = \frac{1}{2} d^{RE} - C(d^{RE}) + \frac{1}{2} \delta = \frac{1}{2} \alpha_{1} + \frac{1}{2} \delta,$$
  
$$U(G^{n}, 0 | \theta = 0) = \frac{1}{2} [\delta(1 + \alpha_{1}) + (1 - \delta) \alpha_{1}] = \frac{1}{2} \alpha_{1} + \frac{1}{2} \delta,$$

which is consistent with  $\alpha_0 \in (0, 1)$ .

We next show that there exists no equilibrium with  $\alpha_0 \neq \alpha_1$ . Suppose first that  $\alpha_1 > \alpha_0$ . Note that

$$\max_{d} U(G^{e}, d | \theta = 0) \geq U(G^{e}, \alpha_{1} | \theta = 0)$$
  
=  $\frac{1}{2}\alpha_{1} + \frac{1}{2}\delta \left[ \frac{\alpha_{1}^{2}}{\delta \alpha_{1} + (1 - \delta)\alpha_{0}} + \frac{(1 - \alpha_{1})^{2}}{1 - \delta \alpha_{1} - (1 - \delta)\alpha_{0}} \right].$ 

We argue that if  $\alpha_0 \neq \alpha_1$  then

$$\frac{\alpha_1^2}{\delta \alpha_1 + (1-\delta)\alpha_0} + \frac{(1-\alpha_1)^2}{1-\delta \alpha_1 - (1-\delta)\alpha_0} > 1.$$

A bit of algebra confirms that this inequality is satisfied if and only if  $(\alpha_1 - \alpha_0)^2 > 0$ . Hence, when  $\alpha_0 \neq \alpha_1$ ,

$$\max_{d} U(G^{e}, d \mid \theta = 0) \geq U(G^{e}, \alpha_{1} \mid \theta = 0) > \frac{1}{2}\alpha_{1} + \frac{1}{2}\delta.$$

When  $\alpha_0 < \alpha_1$ ,

$$U(G^{n}, 0 | \theta = 0) < \frac{1}{2} [\delta(1 + \alpha_{1}) + (1 - \delta)\alpha_{1}] = \frac{1}{2}\alpha_{1} + \frac{1}{2}\delta,$$

which implies that  $\text{supp}(\sigma_0) = \{(G^e, d^e)\}$ , and hence,  $\alpha_0 = d^e$ . But when  $\alpha_1 > \alpha_0$  we know that  $d^e > d^{RE} = \alpha_1$ . This implies that  $\alpha_0 > \alpha_1$ , a contradiction.

Suppose instead that  $\alpha_0 > \alpha_1$ . If  $\operatorname{supp}(\sigma_0) = \{(G^e, d^e)\}$ , then  $\alpha_0 = d^e < d^{RE} = \alpha_1$ , a contradiction. If  $\operatorname{supp}(\sigma_0) = \{(G^n, 0)\}$ , then  $\alpha_0 = 0 < \alpha_1$ , a contradiction. If  $\operatorname{supp}(\sigma_0) = \{(G^e, d^e), (G^n, 0)\}$ , then  $\alpha_0$  will be a convex combination of  $d^e < \alpha_1$  and  $d^n = 0$ , which is strictly lower than  $\alpha_1$ . But this contradicts our assumption that  $\alpha_0 > \alpha_1$ .

Thus, different states give rise to the same mixture between policies, but these policies are promoted by *different sets of narratives*. The rational and denialist narratives prevail in the good state  $\theta = 1$ , whereas the exaggerationist and neutral narratives prevail in the bad state  $\theta = 0$ . In each case, narratives that neglect the role of *a* legitimize the representative agent's desire to eschew hard trade-offs, and therefore induce his ideal policy  $d^* = \varepsilon$ . And the narratives that account for the role of *a* induce the rational-expectations policy, even if they do not always give it a correct justification.

The result that the mixture over policies is state-independent mirrors the rational-expectations benchmark. However, the reasoning behind it is subtler. The narratives  $G^e$  and  $G^n$  effectively fail to condition anticipatory utility on  $\theta$ . As a result, there is an externality between the two states, which does not exist under rational expectations. In particular,  $\alpha_1$  affects the relative appeal of  $G^e$  and  $G^n$  in  $\theta = 0$ , and therefore could potentially affect  $\alpha_0$ . It is *equilibrium reasoning* that restores state-independent policy mixtures. If  $\alpha_1$  were higher (lower) than  $\alpha_0$ , this would make  $G^e$  more (less) appealing in  $\theta = 0$ , thus leading to a rise (drop) in  $\alpha_0$ .

#### V. Conclusion

The model of competing narratives presented in this paper formalized intuitions regarding the role of narratives in the formation of political beliefs. Our model was based on two main ideas.

What Are Narratives and How Do They Shape Beliefs?—In our formalism, narratives are causal models that map actions into consequences. Different narratives employ different intermediate variables and arrange them differently in the causal scheme. Narratives shape beliefs by imposing a causal interpretation on long-run correlations. These beliefs are used to evaluate policies.

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*How Does the Public Select between Competing Narratives?*—Our behavioral assumption was that in the presence of conflicting narrative-policy pairs, the public (a representative agent in this paper) selects between them according to their induced anticipatory utility. This is consistent with the basic intuition that people are drawn to stories with a "hopeful" message.

The main insights that emerged from our analysis of the model can be summarized as follows. First, at least some prevailing narratives are misspecified causal models that "sell false hopes" regarding the consequences of counterfactual policies. Second, multiplicity of dominant narrative-policy pairs is an intrinsic property of long-run equilibrium in the "battle over public opinion." Indeed, in specific settings, we saw that growing popularity of one policy weakens the appeal of its supporting narrative. This "diminishing returns" aspect leads to additional properties of equilibrium (uniqueness, dynamic stability) in these settings. Finally, we hope that our stylized examples gave a foretaste of the model's ability to shed light on the popularity of certain real-life political narratives and their implications for political outcomes.

## APPENDIX I. PROOFS

We present proofs that are omitted from the main text. Some proofs are relegated to the online Appendix.

## **PROOF OF PROPOSITION 3:**

By Propositions 1 and 2, an equilibrium  $\sigma$  exists. Moreover, every equilibrium  $\sigma$  assigns positive probability to exactly two policies that lie (weakly) on opposite sides of  $d^*$ .

As a preliminary step, let us show that for any equilibrium  $\sigma$  where  $\operatorname{supp}(\sigma) = \{(G_l, d_l), (G_r, d_r)\}, V(G_r, d; \alpha) \text{ is decreasing in } \alpha \text{ and } V(G_l, d; \alpha)$ is increasing in  $\alpha$ . By assumption, V is monotone in  $\alpha$ . Suppose that  $V(G_r, d; \alpha)$ is increasing in  $\alpha$ . By NSQD,  $V(G_r, d_r; d_r) = \mu$ . Since  $d_r > \alpha(\sigma)$ , it follows that  $V(G_r, d_r; \alpha(\sigma)) < \mu$ , contradicting our finding (at the beginning of the proof of Proposition 2) that  $U(G_r, d_r; \alpha(\sigma)) \ge \mu$ . Therefore,  $V(G_r, d; \alpha)$  is decreasing in  $\alpha$ . In the same manner, we can show that  $V(G_l, d; \alpha)$  is increasing in  $\alpha$ .

Let us first establish essential uniqueness of equilibrium. Suppose there are at least two equilibria  $\sigma$  and  $\sigma'$ , such that  $\operatorname{supp}(\sigma) = \{(G_l, d_l), (G_r, d_r)\}$  and  $\operatorname{supp}(\sigma') = \{(G'_l, d'_l), (G'_r, d'_r)\}$ . Without loss of generality,  $\alpha(\sigma') \leq \alpha(\sigma)$ . Assume  $\alpha(\sigma') = \alpha(\sigma) = \alpha$ . Then, from the proof of Proposition 2, both  $G_r$  and  $G'_r$  maximize  $p_G(y = 1 | a = 1)$  given  $\alpha$ . Likewise, both  $G_l$  and  $G'_l$  maximize  $p_G(y = 1 | a = 0)$  given  $\alpha$ . Furthermore, there exist unique  $d_r$  and  $d_l$  that maximize U in the ranges  $d \geq \alpha$  and  $d \leq \alpha$ , respectively. This has two implications. First, by NSQD,  $(p_{G_r}(y|a)) = (p_{G'_r}(y|a))$  and  $(p_{G_l}(y|a)) = (p_{G'_l}(y|a))$ . Second,  $d_r = d'_r$  and  $d_l = d'_l$ . This means that the equilibrium is essentially unique.

Now assume  $\alpha(\sigma') < \alpha(\sigma)$ . By construction,

(13) 
$$U(G_r, d_r; \alpha(\sigma)) = \max_{(G,d)|d > \alpha(\sigma)} U(G, d; \alpha(\sigma)),$$
$$U(G_l, d_l; \alpha(\sigma)) = \max_{(G,d)|d < \alpha(\sigma)} U(G, d; \alpha(\sigma)),$$

and

(14) 
$$U(G_r, d_r; \alpha(\sigma)) = U(G_l, d_l; \alpha(\sigma)).$$

Since  $\alpha(\sigma') < \alpha(\sigma)$ ,  $V(G_r, d; \alpha)$  is decreasing in  $\alpha$  and  $V(G_l, d; \alpha)$  is increasing in  $\alpha$ , it follows that

$$\max_{(G,d)|d>\alpha(\sigma')} U\bigl(G,d;\alpha(\sigma')\bigr) \ > \ \max_{(G,d)|d<\alpha(\sigma')} U\bigl(G,d;\alpha(\sigma')\bigr),$$

contradicting the assumption that  $\sigma'$  is an equilibrium with  $\operatorname{supp}(\sigma') = \{(G'_l, d'_l), (G'_r, d'_r)\}.$ 

We now turn to local stability. Consider an equilibrium  $\sigma$  with  $\operatorname{supp}(\sigma) = \{(G_l, d_l), (G_r, d_r)\}$ , where  $d_l < \alpha(\sigma) < d_r$ . Equalities (13)–(14) hold. Suppose  $\alpha > \alpha(\sigma)$ . Since  $V(G_r, d; \alpha)$  is decreasing in  $\alpha$  and  $V(G_l, d; \alpha)$  is increasing in  $\alpha$ , it follows that

$$\max_{(G,d)|d>\alpha} U\bigl(G,d;\alpha\bigr) \ < \ \max_{(G,d)|d<\alpha} U\bigl(G,d;\alpha\bigr),$$

thus satisfying the condition for local stability. A similar argument applies to the case of  $\alpha < \alpha(\sigma)$ .

## **PROOF OF PROPOSITION 4:**

The assumption that p is  $Q^*$ -rich enables us to apply Remark 1: in any equilibrium, the support of the marginal equilibrium distribution over policies is  $\{d_l, d_r\}$ , where  $d_l < d^* < d_r$ . Furthermore, the policies  $d_r$  and  $d_l$  are accompanied by narratives  $G_r$  and  $G_l$  that maximize  $p_G(y = 1 | a = 1)$  and  $p_G(y = 1 | a = 0)$ , respectively.

The proof proceeds stepwise. We use the shorthand notation  $\alpha = \alpha(\sigma)$  throughout.

**Step 1:** For any k = 2, ..., m - 1, the threat/opportunity DAG  $1 \rightarrow m \leftarrow k$  violates NSQD for almost all rich distributions *p*.

## PROOF:

Let  $G: a \to y \leftarrow z$ , where  $z \in \{0, 1\}$  and (p(z|a, y)) is a generic element in  $Q^*$ . Since *a* is an ancestral node in *G*, we can substitute  $p(a) \equiv p_G(a)$  (see Spiegler 2020), such that the NSQD requirement can be written as

$$\sum_{a} p_G(a) p_G(y = 1 | a) = p(y = 1) = \mu.$$

Since the left-hand side of this equation is by definition  $p_G(y = 1)$ , it follows that NSQD is equivalent to the requirement that  $p_G$  does not distort the objective marginal distribution of y. We can write the condition more explicitly:

$$\sum_{a} \sum_{z} p(a) \left( \sum_{a'} \sum_{y'} p(a') p(y') p(z \mid a', y') \right) \frac{p(a) \mu p(z \mid a, y = 1)}{p(a) \sum_{y'} p(y'') p(z \mid a, y'')} = \mu.$$

This expression can be simplified into

$$\sum_{a} p(a) \sum_{z} \frac{p(z \mid a, y = 1) \sum_{a'} \sum_{y'} p(a') p(y') p(z \mid a', y')}{\sum_{y''} p(y'') p(z \mid a, y'')} = 1.$$

This is an equation in four variables (p(z = 1 | a, y)), where (p(a)) and (p(y)) are given constants. We can multiply both sides of the equations by the four terms  $(\sum_{y''} p(y'')p(z|a, y''))_{a,z}$ , and obtain a polynomial equation in the four variables. The equation is nontautological: it is violated when  $z \approx y + a(1 - y)$ .<sup>13</sup> It is well-known that the Lebesgue measure of the set of solutions of a nontautological polynomial equation over  $[0, 1]^n$  is zero (see Caron and Traynor 2005). This completes the proof.

Thus, for generic  $Q^*$ -rich distributions p, the only DAGs G that can be part of an equilibrium while inducing nonconstant  $p_G(y|a)$  are the lever DAGs  $a \to x_i \to y$ , where  $i = 2, \ldots, m-1$ . The narratives that accompany  $d_r$  and  $d_l$  both have this structure, and thus only differ in the value of i. Here,  $Q^*$ -richness means that the problem of finding the value of i for  $G_r$  is approximated by the following problem:<sup>14</sup>

(15) 
$$\max_{(p(z=1|a,y))_{a,y=0,1}\in\mathcal{Q}^{*}}\sum_{z=0,1}p(z|a = 1)p(y = 1|z)$$
$$=\sum_{z}\left(\sum_{y'}p(y')p(z|a = 1,y')\right)\frac{\mu\sum_{a'}p(a')p(z|a',y = 1)}{\sum_{y''}\sum_{a''}p(a'')p(y'')p(z|a'',y'')}.$$

The problem for  $G_l$  is the same, except that we condition on a = 0 instead of a = 1.

**Step 2:** The solution to (15) is

$$p_G(y = 1 | a) = \max\left\{\frac{\mu}{\mu + p(a)(1-\mu)}, \frac{\mu(2-p(a)-\mu)}{1-\mu p(a)}\right\},\$$

where the left and right arguments are attained at  $q_a^{\vee}$  and  $q_a^{\wedge}$ , respectively. The left argument is weakly higher than the right argument if and only if  $p(a) + \mu \leq 1$ . Denote the solution by  $H_a(\alpha)$ .

#### PROOF:

See the online Appendix.

<sup>13</sup>Suppose z is determined as follows: With probability  $1 - \rho$ , z = y + a(1 - y), and with probability  $\rho$ , z = 0. For  $\rho$  sufficiently close to zero,

$$\sum_{a} p_{G}(a) p_{G}(y = 1 | a) \approx \left[ 1 - \alpha (1 - \mu) \right] \left[ \alpha + (1 - \alpha) \mu \right] > \mu$$

<sup>14</sup>This is only an approximation because we need to incorporate small perturbations to the distribution of the lever variable if the solution to the maximization problem yields distributions without full support for every realization of a and y.

**Step 3:** The equilibrium is generically unique.

## PROOF:

By  $Q^*$ -richness,  $p_{G_r}(y = 1 | a = 1) \approx H_1(\alpha)$  and  $p_{G_l}(y = 1 | a = 0) \approx H_0(\alpha)$ . Use NSQD to define  $p_{G_r}(y = 1 | a = 0)$  and  $p_{G_l}(y = 1 | a = 1)$  in terms of  $H_a(\alpha)$ , and obtain

$$V(G_{r},d;\alpha) \approx \mu \cdot \max\left\{\frac{d(1-\mu)+\mu}{\alpha(1-\mu)+\mu}, \frac{d(1-\mu)+1-\alpha}{\alpha(1-\mu)+1-\alpha}\right\},\$$
$$V(G_{l},d;\alpha) \approx \mu \cdot \max\left\{\frac{(1-d)(1-\mu)+\mu}{(1-\alpha)(1-\mu)+\mu}, \frac{(1-d)(1-\mu)+\alpha}{(1-\alpha)(1-\mu)+\alpha}\right\}.$$

Consider an equilibrium with some given  $\alpha$ . By definition,

$$U(G_r, d_r; \alpha) = \max_{d > \alpha} \left[ V(G_r, d; \alpha) - C(d - d^*) \right],$$
$$U(G_l, d_l; \alpha) = \max_{d < \alpha} \left[ V(G_l, d; \alpha) - C(d - d^*) \right].$$

It is easy to verify that for any fixed d,  $V(G_r, d; \alpha)$  is strictly decreasing with  $\alpha$ , whereas  $V(G_l, d; \alpha)$  is strictly increasing with  $\alpha$ . Consequently, the equation  $U(G_r, d_r; \alpha) = U(G_l, d_l; \alpha)$  that must hold in equilibrium cannot have more than one solution  $\alpha$ . Given  $\alpha$ , the solution of  $G_r$  and  $G_l$  is generically unique, and therefore  $V(G_r, d; \alpha)$  and  $V(G_l, d; \alpha)$  are also pinned down. As a result,  $d_r$  and  $d_l$  are pinned down, which also pins down  $\sigma$ .<sup>15</sup>

## PROOF OF REMARK 2:

When C and  $\varepsilon$  are vanishingly low, it must be the case that  $d_r \approx 1$  and  $d_l \approx 0$ , such that

$$\max\left\{\frac{2-\mu-\alpha}{\alpha(1-\mu)+1-\alpha},\frac{1}{\alpha(1-\mu)+\mu}\right\}$$
  
$$\approx \max\left\{\frac{1-\mu+\alpha}{(1-\alpha)(1-\mu)+\alpha},\frac{1}{(1-\alpha)(1-\mu)+\mu}\right\}.$$

The result follows by solving this equation. ■

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<sup>15</sup>Here, genericity means that when  $p(a) + \mu = 1$ , there are two lever variables that maximize  $p_G(y = 1|a = 1)$ , z = ay and z = y + a(1 - y); and two lever variables that maximize  $p_G(y = 1|a = 0)$ , x = y(1 - a) and x = y + (1 - y)(1 - a). For details, see the online Appendix.

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