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A Hybrid GRASP-VNS for Ship Routing and 1 Scheduling Problem with Discretized Time Windows 2

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7 Abstract

6

This paper addresses the Ship Routing and Scheduling Problem with Discretized Time Windows. Being one of the most relevant and challenging problems faced by decision makers from shipping companies, this tramp shipping problem lies in determining the set of contracts that should be served by each ship and the time windows that ships should use to serve each contract, with the aim of minimizing total costs. The use of discretized time windows allows for the consideration of a broad variety of features and practical constraints in a simple way. In order to solve this problem we propose a hybridazation of a Greedy Randomized Adaptive Search Procedure and a Variable Neighborhood Search, which improves previous heuristics results found in literature and requires very short computational time. Moreover, this algorithm is able to achieve the optimal results for many instances, demonstrating its good performance.

Keywords: Ship Routing and Scheduling Problem, Tramp Shipping,

GRASP, Variable Neighbourhood Search 9

1. Introduction 10

The most important mode of transport for international trade is seaborne 11 shipping. An estimated 80 per cent of world trade is carried by sea [43]. It 12 means that, compared to other modes of freight transportation, ships are far 13 superior for moving large volumes over long distances. Due to the increasing 14 15

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development of economies and globalization, the international trade is continuously rising, and as a consequent the sector of maritime transport has
also shown an enormous growth.

Container ships require a huge capital investment and very high daily 19 operating costs. Investment in a ship may range in the millions and operating 20 costs in the thousands dollars a day. There are three main types of costs in 21 seaborne shipping: capital and depreciation, running, and operating costs. 22 Capital and depreciation costs are related to the loss of ships market value 23 respect to the initial investment. Running costs are usually fixed and include 24 maintenance, insurance, crew salaries, and overhead costs, among others. 25 Operating costs are directly related to ships daily operations, and include 26 fuel consumption, port and customs expenses, tolls at canals, etc. These 27 latter costs depend on characteristics like travel distance, navigation speed, 28 and maritime routes. Therefore, capital and depreciation costs, and running 20 costs are not usually expenses that can be subject to optimization as a result 30 of improvements in routing, but the operating costs can be optimized through 31 better routing as it is the aim in this work. Accordingly, good scheduling is 32 of economical essence in this increasingly competitive area. 33

In this regard, Gatica and Miranda [15] focus on optimally solving a ship 34 routing and scheduling problem with a heterogeneous tramp fleet. They 35 propose a network-based model in which discretized time windows for pick-36 ing and delivering cargoes are defined. Discretized time windows are just 37 time instants in which these picking and delivering cargoes can be carried 38 out. This allows to consider a broad variety of features and practical con-30 straints by simply adding/deleting arcs or modifying the corresponding cost 40 parameters, which has the advantage of preserving the network structure. In 41 particular, they consider problems in which navigation speed can be used to 42 control fuel consumption, which may have a significant impact in the quality 43 of the solution, since fuel consumption follows an approximately cubic func-44 tion of speed [37]. They solved the model by means of the general-purpose 45 solver, CPLEX¹. Numerical results show that the model presents a much 46 better trade-off between solution quality and computing time than a similar 47 constant-speed continuous model. Recently, in order to obtain quality results 48 for real-life-sized problems in less computational time, Castillo-Villar et al. 49 [7] develop a Variable Neighborhood Search (VNS) algorithm to solve this 50

¹http://www-01.ibm.com/software/commerce/optimization/cplex-optimizer/

problem. This VNS is very simple, since it is just a list of neighborhoods sequentially explored. Results reported in that work show that the VNS provides solutions with a gap between 6% and 7% to the optimal solutions.

Due to the fact that this is an operational problem (*i.e.*, it has to be solved 54 daily) and may be integrated with other related problems (Berth Allocation 55 Problem [4], Container Stowage Problem [3], etc.), it is important to solve 56 it quickly and provide results of the highest possible quality. Motivated by 57 that, this work presents a hybridization of a Greedy Randomized Adaptive 58 Search Procedure (GRASP) with a more complex and elaborate VNS to solve 50 the same problem with the aim of reducing the gap and obtaining results in 60 less computational time. 61

The remainder of this article is organized as follows. At first, Section 2 reviews research efforts from earlier studies that are related to the current study. Then, in Section 3 the formulation of the problem is shortly outlined. In Section 4 the main features of the hybrid GRASP-VNS method is described. Experimental tests are performed and results are discussed in Section 5. Finally, in Section 6 the main conclusions extracted in this work and some future work lines are summarized.

⁶⁹ 2. Literature Review

In the literature, the first works about ship routing arose in the 70s [1, 2], but the first survey appeared more than ten years later [36]. Recent reviews on ship routing problems can be found in works by Christiansen et al. [8, 9], where literature contributions are classified.

The majority of papers about ship routing and scheduling problems focus 74 on the development of Mixed Integer Programming (MIP) models or heuris-75 tics/metaheuristics methods to solve them. Fox and Herden [13] describe a 76 MIP model to schedule ships from ammonia processing plants to eight ports 77 in Australia. The objective is to minimize freight, discharge, and inventory 78 holding cots while taking into account the inventory, minimum discharge 79 tonnage, and ship capacity constraints. Moreover, using a MIP model, an 80 inventory routing problem with multiple products was analyzed by Ronen 81 [38] for liquid bulk oil cargo. Sherali et al. [40] present an aggregate MIP 82 model for the problem of transporting refined-oil products from three ports 83 in Kuwait to customers located in Europe, North America, and Japan. The 84 model considers the existence of alternative maritime routes. The authors 85 develop a reformulation of the MIP model and a set of valid inequalities that 86

⁸⁷ allow them to design several algorithmic solution strategies.

In relation to heuristics and metaheuristics, Korsvik et al. [20] use a Tabu 88 Search algorithm which allows infeasible solutions with respect to ship ca-89 pacity and time. Other works in the literature introduce specific concepts 90 in ship routing problems. Romero et al. [35] propose a GRASP and discuss 91 aspects related to data gathering and updating, which are particularly diffi-92 cult in the context of ship routing. Lin and Liu [22] combine ship allocation, 93 routing and freight assignment in a particular kind of ship routing. Kosmas 94 and Vlachos [21] consider a cost function that depends on the wind speed 95 and its direction, as well as on the wave height and its direction, and solve 96 the problem using a Simulated Annealing algorithm. 97

Moreover, in the related literature, depending on the operation mode, 98 three kinds of ship routing problems can be distinguished: liner, industrial, 99 and tramp shipping. Liners [19, 25, 42] operate according to an agreed 100 itinerary and schedule similar to a bus line. In industrial shipping, the cargo 101 owner or shipper controls the ships. Industrial operators strive to minimize 102 the costs of shipping their cargoes. Tramp fleets engage in contracts to trans-103 port specified (usually large) volumes of cargo between two ports within a 104 period of time. They engage in contracts to make one or several trips, each 105 trip having specified origin and destination ports and time windows for pick-106 ing and delivering the cargo. Tramp is usually the operation mode selected 107 to transport liquid and dry commodities, or cargo involving a large number 108 of units. During the last few decades there has been a shift from industrial 109 to tramp shipping [8, 9]. 110

Particularly, the literature on tramp shipping problems is quite sparse 111 and only a few papers tackle such problems. The reason for this lack of re-112 search interest in this shipping sector is attributed to the historic existence 113 of a large number of small tramp shipping companies operating in the mar-114 ket. However, more recently, increased demand and the tendency of larger 115 companies to outsource shipping of their cargoes has led to the growth of 116 small companies, the growth of the associated scheduling problems, and a 117 corresponding increase interest from researchers in this type of problems. A 118 tramp routing and scheduling problem was solved by Brønmo et al. [5], where 110 a multistart Local Search heuristic is developed. The proposed unified Tabu 120 Search heuristic by Korsvik et al. [20] also solves the specific tramp ship-121 ping. In contrast to the procedure followed by Brønmo et al. [5], Malliappi 122 et al. [23] present a VNS heuristic, and the results show that this procedure 123 outperforms the previous heuristics. Norstad et al. [29] address this prob-124

¹²⁵ lem considering speed optimization and develop a multistart Local Search ¹²⁶ heuristic to solve it

Additionally, as introduced above, Gatica and Miranda [15] develop a 127 network-based model for the Ship Routing and Scheduling Problem with Dis-128 cretized Time Windows with a heterogeneous tramp fleet. The objective is 129 to minimize the total operating cost of serving a set of trip cargo contracts, 130 considering time window constraints at both the origin and destination of 131 cargoes. A distinctive aspect of their methodology is that time windows for 132 picking and delivering cargoes are discretized. This leaves room for including 133 a broad variety of features and practical constraints, such as navigation speed 134 to control fuel consumption. More specifically, they assume that pick-up and 135 delivery may start only at a finite set of time instances within the correspond-136 ing time windows. In general (*i.e.* urban) vehicle routing, the only known 137 application of time discretization is for modelling time-dependent travel times 138 (time to traverse an arc depends on the time instance the travel starts). That 139 approach is followed, for example, by Ichoua et al. [18], Woensel et al. [44], 140 and Donati et al. [10]. Gatica and Miranda [15] demonstrate that numerical 141 results considering discretized time windows presents a much better trade-142 off between solution quality and computational time than a similar constant 143 speed continuous model. Recently, Castillo-Villar et al. [7] developed a VNS 144 algorithm to solve this specific tramp shipping problem with discretized time 145 windows, obtaining quality results in less computational time than the nec-146 essary for the initial MIP model implemented in CPLEX. 147

The main contribution of this paper is to propose a hybrid GRASP-148 VNS algorithm that improves upon the results from Castillo-Villar et al. [7]. 149 We have developed a more elaborated VNS with a more complex structure 150 for better exploration of the search space, which jointly with the proposed 151 GRASP as start method, allows to obtain a better performance. The im-152 provement is on achieving smaller gap values than those reported by Castillo-153 Villar et al. [7]. Our technique achieves results of higher quality in short 154 computation times. In this particular problem, the quality of results is very 155 important, since, as stated before, minimizing operating cost is of high rele-156 vance in the competitive area of ship routing. Moreover, the faster the results 157 are obtained, the more agility will have the rest of processes that depend on 158 the pickup or delivery of ships cargoes, so that it is another challenge to 159 achieve. 160

¹⁶¹ 3. Ship Routing and Scheduling Problem with Discretized Time ¹⁶² Windows

This section presents the description of the Ship Routing and Scheduling Problem with Discretized Time Windows (hereinafter SRSPDTW). Firstly, Section 3.1 introduces the details of the discretized modelling approach and the characteristics of the problem. Secondly, Section 3.2 presents the mathematical model proposed by Gatica and Miranda [15] and used by Castillo-Villar et al. [7], which is considered in this paper.

169 3.1. Problem Description

We consider the routing and scheduling problem for tramp shipping which 170 is composed of: (i) a fleet of ships; (ii) a set of cargo contracts that need to 171 be served; (iii) a set of time instants or discretized time windows at which 172 each contract can be served; and (iv) a set of links or arcs between time 173 instants of different contracts for each ship. Each of these arcs represents a 174 ship serving a contract at a time instant and then serving another contract 175 at a different time instant, all this with an associated cost. Each contract 176 is a single trip from one port to another, picking-up and delivering a cargo. 177 A contract must be served at one of the possible time instants that are also 178 called nodes. Therefore, the problem here presented consists of deciding the 179 set of contracts to be served by each ship and the chosen time instants, *i.e.* 180 selecting a set of arcs, with the aim of serving all contracts while minimizing 181 total relevant costs. 182

The fleet of ships is heterogeneous due to differences in capacity, speeds, fuel consumption, etc. Although each ship can serve only one contract at a time, there are incompatibilities between cargoes and ships or between ships and ports, so that not all ships can serve all contracts. Furthermore, two contracts may be incompatible with each other, *i.e.*, the corresponding trips cannot be done consecutively by the same ship, unless a time delay (*e.g.* for cleaning) or a third trip is placed between them.

It is important to notice that given a sequence of contracts to be served by a single ship, an empty trip must take place from the delivery port of each contract to the origin of the next contract in the sequence, unless these two ports coincide. These empty trips represent a significant portion of total avoidable cost and they are taken into account in this problem. Relevant costs are mainly operating costs, but may also include other kinds of costs as long as they can be associated with individual trips.

One of the most important costs corresponds to the fuel consumption 197 expenses. Since fuel consumption depends on navigation speed, controlling 198 the speed impacts not only on the travel time, but also on the travel costs. 199 In this work, a network-based model is used, and it allows for the consid-200 eration of navigation speed and a broad variety of features and practical 201 constraints by simply adding/deleting arcs between contracts or modifying 202 the corresponding cost parameters, which has the advantage of preserving 203 the network structure. This flexibility arises from the discretization of the 204 time windows, which allows for both, the feasibility (existence) and the cost 205 parameter of each potential arc, to be determined outside the model. 206

207 3.2. Mathematical Formulation

As stated above, the discretized modeling approach used in Gatica and Miranda [15] and Castillo-Villar et al. [7] has been adopted. In order to make this work self-contained, the model is explained below.

The SRSPDTW can be defined as follows. Let G = (V, A) be a directed 211 graph, where V is the node set and A is the arc set. Each node $i \in V$ represent 212 a time instant and the contract associated with that node is represented by 213 n(i). On the other hand, each contract n(i) has a set of associate nodes 214 $D_{n(i)}$, *i.e.*, the set of possible starting times for trip n(i). In SRSPDTW, the 215 ships are indexed by means of k = 1, 2, ..., B, where B is the number of 216 available ships. Each arc(i, j, k) represents the service of contracts n(i) and 217 n(j) consecutively by ship k. The arc is included in the network if both, the 218 trips and the ship, are compatible, and if it is feasible for ship k to begin 219 service of contract n(i) at the time instance represented by node i, make the 220 empty trip from the destination port of contract n(i) to the origin of contract 221 n(j), and be available to begin service of contract n(j) at the time instance 222 associated with node j. 223

For each arc, the cost parameter c_{ijk} represents the total minimal cost 224 when the ship delivers contract n(i) immediately followed by contract n(j). 225 To complete the network, a fictitious node 0 is created to represent the source 226 and destination of all ships (ports that can be different). For each ship k and 227 node i, if contract n(i) is compatible with ship k, both an arc(0, i, k) and an 228 arc(i, 0, k) also exist. Cost c_{0ik} is calculated based on the real initial position 229 of ship k, and cost c_{i0k} represents the cost incurred if ship k serves contract 230 n(i) and must go to a final destination port. 231

The mathematical formulation of the problem from Gatica and Miranda [15] is as follows:

$$minimize \sum_{(i,j,k)\in A} c_{ijk} \cdot x_{ijk} \tag{1}$$

234

s.t.:
$$\sum_{i \in V/(0,i,k) \in A} x_{0ik} \le 1 \quad k = 1, 2, \dots, B$$
(2)

$$\sum_{(i,j,k)\in A/j\in D_n} x_{ijk} = 1 \quad n = 1, 2, \dots, N$$
(3)

$$\sum_{i \in V/(i,j,k) \in A} x_{ijk} = \sum_{l \in V/(j,l,k) \in A} x_{jlk} \quad j \in V, \quad k = 1, 2, \dots, B$$
(4)

$$x_{ijk} \in \{0, 1\} \ (i, j, k) \in A$$
 (5)

where N is the number of contracts to be served, V is the set of nodes in the network, D_n is the set of nodes associated with contract n (i.e., set of possible starting times for trip n), A is the set of arcs in the network, c_{ijk} is the cost of arc(i, j, k), and:

$$x_{ijk} = \begin{cases} 1 & \text{if } arc(i, j, k) \text{ is part of the solution} \\ 0 & \text{otherwise} \end{cases}$$
(6)

Selecting arc(i, j, k) as part of the solution $(x_{ijk} = 1)$ implies that ship kwill serve contract n(i) and will serve contract n(j) immediately afterwards. Selecting arc(0, i, k) implies that n(i) is the first contract to be served by ship k, and selecting arc(i, 0, k) implies that n(i) is the last contract to be served by ship k.

The objective function (1) represents the total solution cost. Constraints 245 (2) ensure that each ship is employed in at most one route. A route is 246 defined as a sequence of contracts to be served. Constraints (3) ensure that, 247 for each contract n, exactly one arc entering set D_n is selected, establishing 248 that each contract must be served exactly once, by exactly one ship, which 249 begins service at exactly one of the nodes or time instants in the discretized 250 time window for cargo pick up. For nodes different to the central fictitious 251 node, constraints (4) state that if an entering arc is selected, a leaving arc 252 must also be selected and that both arcs must be associated with the same 253 ship. For the fictitious node, these constraints (4) state that if a leaving arc 254 associated with ship k is selected, then an entering arc associated with the 255 same ship must also be selected (i.e., if a ship exits the node), and then it 256

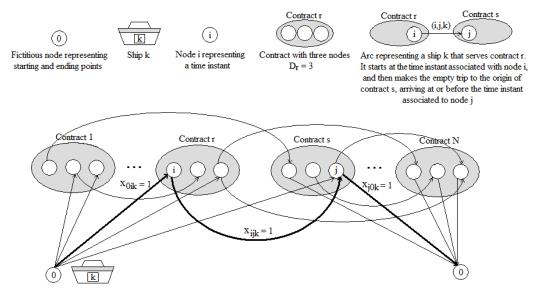


Figure 1: Example of a partial graph of the model for a ship k

must return to it. Arcs leaving the fictitious node represent the ships that are, in fact, used in the solution.

Figure 1 shows an illustrative partial graph of the model, where the nodes 259 of the network represent discrete and feasible starting times for each contract. 260 The ovals group all nodes related to the same contract. Notation is on the 261 top of the figure. As stated before, all ships are supposed to start and end 262 at a fictitious node 0. Some arcs for a single ship k are drawn, based on the 263 feasible trips that can be selected. The chosen route is marked with bold 264 lines. If ship k can serve contract r at time instant of node i, the arc(0, i, k)265 will be selected and x_{0ik} will be equal to 1. Then, if the ship k can serve 266 contract r and go to serve contract s at time instant of node j, the arc(i, j, k)267 will be selected and x_{iik} will be equal to 1. Finally, if ship k does not serve 268 more contracts, it is supposed to go to the fictitious node 0, so that arc(j, 0, k)269 is used and x_{i0k} will be equal to 1. 270

271 4. Hybrid GRASP-VNS Methodology

On the one hand, Greedy Randomized Adaptive Search Procedure (GRASP)
is a metaheuristic algorithm commonly applied to combinatorial optimization
problems, and consists of iterations made up from successive constructions

of a greedy randomized solution and subsequent iterative improvements of 275 it. The greedy randomized solutions are generated by adding elements to the 276 problem solution set from a list of elements ranked by a greedy function ac-277 cording to the quality of the solution they will achieve. To obtain variability 278 in the candidate set of greedy solutions, well-ranked candidate elements are 279 often placed in a Restricted Candidate List (also known as RCL), and chosen 280 at random when building up the solution. GRASP was first introduced in 281 Feo and Resende [12], and some survey papers are Feo and Resende [11] and 282 Resende and Ribeiro [34]. 283

On the other hand, VNS, proposed by Mladenović and Hansen [26], is 284 another metaheuristic for solving combinatorial optimization problems. VNS 285 systematically changes different neighborhoods within a local search, unlike 286 many metaheuristics where only a single neighborhood is employed. The 287 basic idea is that a local optimum defined by one neighborhood structure is 288 not necessary the local optimum of another neighborhood structure, thus the 289 search can systematically traverse different search spaces which are defined 290 by different neighborhood structures. This makes the search much more 291 flexible within the solution space of the problem, and potentially leads to 292 better solutions which are difficult to obtain by using single-neighborhood-293 based local search algorithms. Many extensions of VNS have been made, 294 mainly to be able to solve large problem instances [16, 17, 24, 28, 30]. 295

This paper proposes the use of a hybrid GRASP-VNS algorithm providing a solution to the SRSPDTW. Results are obtained in less computational time than previous approaches [7, 15], and solutions are of high quality, as it is shown in Section 5. Both aspects are specially important when dealing with large-scale instances. The proposed hybrid algorithm incorporates two powerful features, the effective constructive and improving ability of GRASP and the flexibility of VNS to explore different search spaces for the problem. It is important to notice that a solution to the problem consists of a

It is important to notice that a solution to the problem consists of a route for each ship, so that a route is defined as the set of contracts to be performed by the corresponding ship as well as the chosen discretized time windows. The general algorithm (Algorithm 1) proposed in order to obtain these kind of solutions is based on the repetition (L times) of two main steps: the construction of an initial feasible solution using a GRASP, and the improving of this solution applying a VNS algorithm.

Algorithm 1: General Algorithm

	/	/ <u>Initialization</u> .
	1 II	nitialize $BestSol \leftarrow \emptyset$.
	2 W	while (the stopping condition is not met (L is not reached)) do
	3	Generate an initial solution s using GRASP algorithm.
		// <u>VNS</u> .
	4	while (the stopping condition is not met (M is not reached)) do
	5	(1) Set $k \leftarrow 1$;
	6	(2) Repeat the following steps (a), (b), and (c) until $k = k_{max}$:
	7	(a) <u>Shaking</u> . Generate a point s' at random from the k^{th}
		neighborhood of s :
	8	(b) <u>Local Search</u> .
	9	while (improvement is achieved) do
	10	$s'' \leftarrow \text{swapInter}(s');$
310	11	$s'' \leftarrow \text{improveRoutes}(s'');$
	12	while (improvement is achieved) do
	13	$s'' \leftarrow \operatorname{relocation}(s');$
	14	$s'' \leftarrow \text{improveRoutes}(s'');$
	15	while (improvement is achieved) do
	16	$s'' \leftarrow 2 \operatorname{-opt}(s');$
	17	$s'' \leftarrow \operatorname{improveRoutes}(s'');$
	18	while (improvement is achieved) do
	19	$s'' \leftarrow \text{relocationChanging}(s');$
	20	$s'' \leftarrow \operatorname{improveRoutes}(s'');$
	21	(c) <u>Move or not</u> . If this local optimum is better than the
		incumbent, move there $(s \leftarrow s'')$, and continue the search
		$(k \leftarrow 1)$; otherwise, set $k \leftarrow k+1$.
	22	Update BestSol.

311 4.1. GRASP for an Initial Feasible Solution

In order to obtain an initial solution, a GRASP has been developed. This 312 algorithm operates as follows. Firstly, a list composed of ships, contracts, 313 and costs is created, as shown in Figure 2. If the problem is composed of B314 ships, the first B contracts are assigned to each ship with their corresponding 315 costs, as long as the ships can go to perform the contracts. This cost is 316 the least possible cost so that each ship performs the contract using a time 317 node, and taking into account that ships are supposed to be in fictitious 318 node 0 at the beginning. The list is sorted in non-increasing order of cost, 319

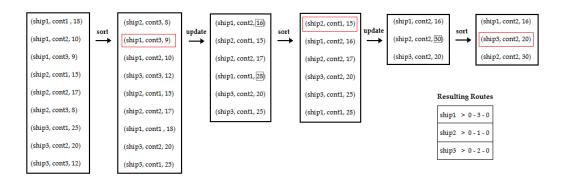


Figure 2: GRASP behaviour example

and the chosen element is randomly selected from the RCL. The RCL is 320 formed by the first three elements of the sorted list, parameter that has been 321 adjusted in order to obtain variable quality solutions. Once the element is 322 chosen, the corresponding contract is assigned to the ship. Then, the element 323 is deleted from the list, as every other element that contains the selected 324 contract. Moreover, for every element containing the selected ship, the cost 325 is updated taking into account that the ship is previously performing the 326 selected contract. This process is repeated until the list is empty, point at 327 which a new list is created with the following B contracts. When there are 328 no more contracts, the process finishes. 329

At this point, we have the route that each ship will perform, but it could 330 happen that some contracts have not been assigned due to arc restrictions. 331 In that case, a new process starts, trying to insert these contracts at some 332 point within the routes. If that is not possible, *swapInter* and *relocation* 333 movements (which are explained in next section) are tried repeatedly seeking 334 to achieve the new contract insertion. After carrying out a certain number 335 of iterations of these movements without achieving the insertion, the process 336 is suspended, as it can happen that it is not possible to obtain an initial 337 feasible solution. 338

Figure 2 shows an example where the problem is composed of three ships and three contracts. The first three contracts are assigned to each ship supposing that they are at the fictitious node at the beginning. Then, the list is sorted by cost and one of the elements of the RCL is selected. This selection is depicted in the figure using a framing red rectangle The list is updated deleting the elements with the selected contract and changing the cost corresponding to the selected ship, since now it is performing the selected contract. This process continues until the list is empty, so that the first three
contracts are just in a ship route. Similarly, the next three contracts will be
assigned to the three ships repeating the process until there are no more
contracts.

350 4.2. Variable Neighborhood Seach Algorithm

As shown in Algorithm 1, unlike the VNS composed of a list of neighborhoods sequentially explored in Castillo-Villar et al. [7], the VNS algorithm applied in this work is composed of three phases: shaking, local search, and move decision. At the beginning, for M times, variable k is set to 1 (line 5), and then the iteration of the three phases starts.

In the shaking phase a solution is randomly generated applying the corre-356 sponding neighborhood structure, *i.e.*, the k^{th} neighborhood structure (line 357 7), with k_{max} representing the total number of neighborhood structures. The 358 sequence of neighborhood structures has been chosen following the ideas 359 described by Repoussis et al. [32] which provided high quality results for 360 a vehicle routing problem that presents many similarities with our prob-361 The sequence is defined as follows: CROSS, $2 - opt^*$, relocation, lem. 362 relocationChanging, and swapInter. This sequential selection is applied 363 based on cardinality, which implies moving from relatively poor to richer 364 neighborhood structures, and significantly increases the possibilities of find-365 ing higher quality solutions. The neighborhood structures GENI and Or – 366 opt used by Repoussis et al. [32] have been discarded because they are 367 not applicable to this particular kind of routes. On the other hand, the 368 relocationChanging structure, similar to relocation, has been added to the 369 sequence. Each operator works randomly, so that the corresponding operator 370 in each iteration of the VNS is performed a limited number of times in order 371 to try obtaining a feasible solution. If it is not possible, the VNS proceeds 372 to next iteration increasing k. The way they work is the following: 373

- The *CROSS* operator [41] selects a subsequence of contracts from a route, other subsequence of contracts from other route, and exchanges both subsequences $(O(P^2n^2)$ being *P* the maximum length of the subsequences).
- The $2-opt^*$ operator [31] chooses two routes and exchange the last part of both routes after two selected point, one from each route $(O(n^2))$.

- The *relocation* operator [6] deletes a contract from a route and inserts 380 it into another route $(O(n^2))$. 381
- The *relocationChanging* operator is a modification of the *relocation* 382 one, where the nodes from contracts between the new one is going to 383 be inserted can change to another node belonging to these contracts, in order to accommodate the new one $(O(n^2))$. 385

384

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• The *swapInter* operator selects a contract from a route, other contract from other route, and swaps them $(O(n^2))$.

In the local search phase (lines 8-20), four different neighborhood struc-388 tures are sequentially applied at each iteration: swapInter, relocation, 2 – 389 opt^* , and *relocationChanging*. These structures are similar to the ones ap-390 plied in the shaking phase, but instead of working randomly, they search the 391 movement that involves the highest reduction of cost, *i.e.*, the best solution 392 of the neighborhood. This way, each structure is applied until no improve-393 ment is achieved (lines 9-20). An improvement method is always applied 394 after performing a neighborhood movement. This method explores all feasi-395 ble combinations of arcs that connect two contracts in the route of a ship, 396 selecting the pair of arcs with lowest cost. It means that this method tries 397 to find an improvement of the solutions based on an analysis of the time 398 windows of each contract, respecting the contracts already assigned to the 399 route of a ship. 400

The order of neighborhood structures exploration in the local search phase 401 has been established by means of the following study. Firstly, each structure 402 has been individually applied in the local search phase of the VNS, in order 403 to asses its contribution during the search process. A representative subset 404 of instances has been used in this analysis, 405

A subset of representative instances - one instance of each group of 15 406 instances explained in Section 5 - has been used in this analysis. In Fig-407 ure 3 the neighborhood structures swapInter, relocation, $2 - Opt^*$, and 408 relocationChanging are identified by N1, N2, N3, and N4, respectively. 409 The first graph shows that the N4 provides the lowest average value of the 410 minimization objective function when used individually. However, applying 411 this neighborhood structure is computationally expensive, so that obtaining 412 results involves large times. For this reason, using N4 as first or second 413 neighborhood structure has been discarded. Thereupon, secondly, each com-414 bination of two structures without N4 has been applied as shown in the 415

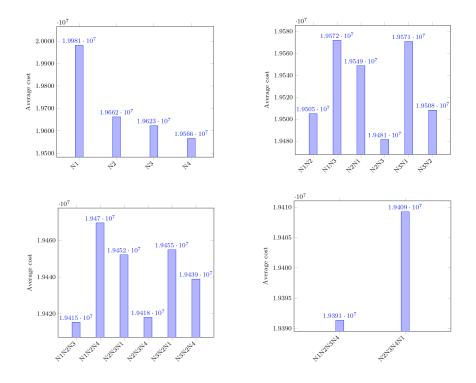


Figure 3: Evaluation of the combination of neighborhood structures

second graph, and the three combinations which involve better results have been selected (N1N2, N2N3, N3N2). Then, each combination of three structures starting from these better ones has been applied as shown in the third graph, and the two combinations which involve better results have been selected (N1N2N3, N2N3N4). As last step, every combination of four structures starting from these better ones has been applied as shown in the fourth graph, and the best one has been selected (N1N2N3N4).

Finally, in the move decision phase (line 21) the new solution is compared to the initial one, and if the new one is better, then the solution is updated and the search starts again setting k to 1. Otherwise, k is increasing by 1 and the next neighborhood in the shaking phase is used.

427 5. Computational Experiments

This section is devoted to analyze the performance of the hybrid GRASP-VNS algorithm introduced in Section 4 for solving the SRSPDTW. Results ⁴³⁰ produced by the proposed algorithm have been compared to exact solutions ⁴³¹ and previous results reported in the literature [7]. For more clarity, here-⁴³² inafter the whole heuristic algorithm proposed by Castillo-Villar et al. [7] is ⁴³³ referenced as CVH, and its greedy start method is referenced as Greedy. Our ⁴³⁴ algorithm has been implemented using Java Standard Edition 7 and compu-⁴³⁵ tational experiments have been performed using a 3.00 GHz Intel Core i-5 ⁴³⁶ processor with 6 GB of RAM running under Ubuntu 12.10.

The set of instances used in this work is the same set generated by 437 Castillo-Villar et al. [7]. There are eighteen groups of instances, each on 438 considering a different combination of ships, time window nodes, and con-439 tracts. The set of discrete time windows (*i.e.* number of possible starting (i.e. number of possib 440 times for each contract) consists of 3, 6, or 15 nodes. The number of ships 441 varies over the values of 4, 5, 7, and 9. The number of contracts varies over 442 the values of 30, 40, and 50. Each group contains 15 different instances. In 443 total, the benchmark is composed of $3 \cdot 4 \cdot 3 \cdot 15 = 540$ instances. 444

In order to obtain the best results using the proposed GRASP-VNS algorithm (Algorithm 1), a parameter setting experimental study has been conducted. Applying the Friedman test [14], M has been fixed to 10, Lto 10, and k_{max} to 5. Moreover, the maximum number of times that each neighborhood structure in the shaking phase is tried until a feasible movement is obtained has been fixed to 30. This is because not all movements corresponding to a neighborhood are feasible due to time windows.

With the aim of demonstrating not only the benefits of our whole pro-452 posal, GRASP-VNS, but also the benefits of both sides, GRASP and VNS, 453 firstly, 20 executions have been made for each instance using our VNS to-454 gether with the Greedy, based on prioritizing the earliest due date contracts 455 and seeking to assign each contract at the earliest possible instant to a ship. 456 This combination is referenced as Greedy-VNS. The average results have 457 been compared to the ones provided by Castillo-Villar et al. [7], where stop-458 ping rules consider a limit time of 7,200 seconds for CPLEX (sometimes its 459 solution does not correspond to an optimal solution) and a maximum number 460 of iterations without improvement in the solution for their whole heuristic 461 method CVH. These results, produced by CPLEX and the heuristic method, 462 have been kindly provided by the authors. This way, it is possible to compare 463 the performance of our VNS algorithm with the performance of the VNS by 464 Castillo-Villar et al. [7]. Secondly, we have made 20 executions using our 465 hybrid GRASP-VNS proposal (see Section 4) in order to show the improve-466 ments provided by our VNS, the improvements provided by the GRASP 467

regarding the Greedy, and the general improvements of the hybrid GRASPVNS regarding the CVH. We have use the same formula than Castillo-Villar
et al. (2014) to calculate the gap values:

$$gap = \frac{Z - CPLEX}{CPLEX} \cdot 100 \tag{7}$$

where Z corresponds to the value obtained by the corresponding heuristic.
Positive gaps are obtained when CPLEX finds better solutions.

Tables 1, 2, and 3 show a summary of all results obtained for these in-473 stances with 30, 40, and 50 contracts, respectively. Each instance type, con-474 sisting of 15 instances, is indicated according to its combination of contracts 475 (Cn.), ships (Sh.), and nodes (Nd.) in columns 1, 2, and 3. The next four 476 columns are related to solutions obtained using CPLEX. Column 4 is the the 477 number of instances from which an optimal solution is found (Opt. found). 478 Column 5 is the number of instances for which an optimal solution is not 479 found, but a feasible solution is found (Only feas. sol.). Column 6 is the 480 number of instances for which no solution is found (Sol. not found). Finally, 481 column 7 is the average time spent to obtain a solution (Avq. time(s.)). It is 482 important to note that sometimes CPLEX is not able to achieve the optimal 483 solution within the limit time, but it might provide a feasible one or not at 484 all. Thus, the value of this column corresponds to the average of the time 485 needed to obtain the optimal or a feasible solution for the 15 instances of 486 each group, so that if there is not solution for an instance this instance is not 487 taken into account to calculate the average. This last consideration is always 488 keeping in mind to calculate the average values in this work. 489

The next three columns present the CVH results: the number of in-490 stances for which solution is not found (Sol. not found), the average time 491 needed by the algorithm to provide a solution taking into account that it 492 is executed considering a maximum number of iterations without any im-493 provement in the solution as stopping criterion (Avg. time(s.)), and the gap 494 between CPLEX and CVH objective function values $(Gap_1(\%))$. Results of 495 Greedy together with our VNS algorithm, *i.e.* Greedy-VNS, are shown in 496 next five columns: the number of instances for which feasible solution is not 497 found by the algorithm (Sol. not found), the average number of executions 498 (of the 20 executions made for each instance) for which an optimal objective 499 value is reached (Avg. opt found), the average time needed to provide a solu-500 tion considering that the algorithm finishes when loops finish, and the loops 501 are controlled by fix parameters L and M (Avg. time(s.)), the gap between 502

CPLEX and Greedy-VNS objective function values $(Gap_2(\%))$, and the gap 503 between CVH and Greedy-VNS objective function values $(Gap_3(\%))$. Finally, 504 results for the GRASP-VNS algorithm proposed here are shown in the six 505 right-most columns. Column Sol. not found gives the number of instances 506 for which a solution is not found by the algorithm. Column Avg. opt found 507 shows the average number of executions for which the optimal objective value 508 is reached. Column Avq. time(s.) shows the average time spent by the al-509 gorithm to obtain solutions. Columns $Gap_4(\%)$, $Gap_5(\%)$, and $Gap_6(\%)$ 510 present the gap between CPLEX and GRASP-VNS objective function val-511 ues, the gap between the CVH and GRASP-VNS objective function values, 512 and the gap between Greedy-VNS and GRASP-VNS objective function val-513 ues, respectively. 514

Table 1 shows results for instances of 30 contracts corresponding to the 515 smallest size instances. In terms of the quality of solutions, using our VNS 516 instead of the VNS by Castillo-Villar et al. [7], *i.e.* the Greedy-VNS algo-517 rithm, the gap with regard to CPLEX solutions is considerably reduced from 518 5.17 to 0.27% on average, and with regard to CVH, solutions are improved 519 on an average of 4.63%. This behavior is repeated with the larger instances 520 as shown in next two tables. This way, we have demonstrated the better 521 performance of our VNS. Additionally, if GRASP replaces Greedy obtaining 522 the GRASP-VNS proposal of this paper, then the results are even better, 523 so that the gap goes from 0.27 to 0.18% regarding CPLEX, and from -4.63524 to -4.70% regarding CVH. Once again, this behavior is repeated with the 525 larger instances as shown in next two tables. Although the improvement 526 introduced by GRASP could seem not very high, an important advantage 527 of using it is that this is able to find more feasible solutions than the other 528 proposals, as shows column 15 (Sol. not found) of each table, and another 529 remarkable aspect is that more than half of the times (11.46 out of 20) that 530 the GRASP-VNS is executed using these instances, an optimal solution is 531 found, demonstrating the robustness of the algorithm. This ratio decreases 532 when the number of contracts increases due to instances complexity, as can 533 be seen in the following tables. However, the approach provided by Castillo-534 Villar et al. [7] did not produce optimal solutions according to their paper. 535 In regard to computation time, results of GRASP-VNS are far better than 536 CPLEX and CVH. It is noteworthy that although execution machines are 537 different, the magnitude of values is not only due to the difference between 538 machines, but also because of the efficiency of the proposed algorithm. 539

⁵⁴⁰ Instances of 40 contracts are medium size instances and results for them

are shown in Table 2. For this set of instances CPLEX and CVH need 541 between 4 and 8 minutes on average to obtain solutions, whereas GRASP-542 VNS requires about 20 seconds on average. The average gap value between 543 CPLEX solutions and GRASP-VNS solutions increase a bit due to the mag-544 nitude of instances, to a value of 0.46%. However, the gap between CVH 545 and GRASP-VNS is even better than the gap obtained with 30-contract in-546 stances (-6.06%). This demonstrates that the performance of CVH worsens 547 when the complexity of instances increase, while this is not the case for the 548 proposed GRASP-VNS algorithm. 549

Table 3 shows instances of 50 contracts corresponding to the largest size 550 instances. The behaviour of the GRASP-VNS algorithm is very similar to the 551 one corresponding to 40-contract instances. One more time, the average gap 552 values in respect to CPLEX is low, 0.58%, and CVH results are improved on 553 an average of 5.14%. Notice that average computation times for these largest 554 instances are shorter than the average times for 40-contract instances, but 555 it is due to a particular 40-contract instance with 5 ships and 15 nodes that 556 consumes particularly longer computation time. 557

An important point that can be highlighted from Tables 1, 2, and 3 is that our GRASP-VNS algorithm always finds a solution if CPLEX has found a solution, and even sometimes GRASP-VNS is able to find a solution when CPLEX has not found a feasible one, as can be seen for 50-contract instances. In contrast, CVH always solves less number of instances than CPLEX.

$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			CF	CPLEX			CVH			Gre	edy - Vi	NS				GRASP	- VNS		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Ont Only	Only	~	Sol.	Avg.	Sol.		Gan	Sol.	Avg.	Avg.	Gano	Gana	Sol.	Avg.	Avg.	Gan	Gan	Gane
		fear fear	fea	<i>i</i>	not	time	not		Idmo	not	opt.	time	7.4mC	(02)	not	opt.	time	(02)	64mD	04m
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	os ninor	š	Ы.	found	(s.)	found		(0/)	found	found	(s.)	(0/)	(0/)	found	found	(s.)	(0/)	(0/)	(0/)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	13		0	2	1.00	3	4.83	4.79	3	10.58	0.55	0.22	-4.32	2	11.84	0.61	0.12	-4.41	-0.10
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	13		0	2	4.84	7	15.92	5.36	2	7.38	1.17	0.36	-4.71	2	9.92	1.33	0.21	-4.84	-0.14
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	13		0	5	171.84	5	93.15	5.53	2	5.46	6.42	0.42	-4.81	5	9.38	7.26	0.22	-4.99	-0.19
0 26.53 5.49 0 11.33 1.30 0.20 -4.98 0 12.53 1.31 0.17 0 151.40 5.49 0 10.33 7.18 0.19 -4.99 0 11.26 7.34 0.20 1.17 49.82 5.17 1.17 9.68 2.87 0.27 -4.63 1.00 11.46 3.08 0.18		15		0	0	1.13	0	7.06	4.34	0	13.00	0.60	0.22	-3.94	0	13.80	0.62	0.18	-3.97	-0.03
0 151.40 5.49 0 10.33 7.18 0.19 -4.99 0 11.26 7.34 0.20 1.17 49.82 5.17 1.17 9.68 2.87 0.27 -4.63 1.00 11.46 3.08 0.18	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	15		0	0	12.73	0	26.53	5.49	0	11.33	1.30	0.20	-4.98	0	12.53	1.31	0.17	-4.99	-0.02
1:17 49.82 5.17 1.17 9.68 2.87 0.27 -4.63 1.00 11.46 3.08 0.18	1.17 49.82 5.17 1.17 9.68 2.87 0.27 -4.63 1.00 11.46 3.08 0.18 -4.70	15		0	0	140.60	0	151.40	5.49	0	10.33	7.18	0.19	-4.99	0	11.26	7.34	0.20	-4.97	0.01
		14.00		0.00	1.00	55.36	1.17	49.82	5.17	1.17	9.68	2.87	0.27	-4.63	1.00	11.46	3.08	0.18	-4.70	-0.08

Table 1: Summary of results for instances with 30 contracts

			CF	CPLEX			CVH			Gre	Greedy - VNS	NS			-	GRASP - VNS	- VNS		
Cn.	Cn. Sh. Nd.	d. Opt.	Only feas.	Sol. not	Avg. time	Sol. not	Avg. time	$\operatorname{Gap}_{(\%)}$	Sol. not	Avg. opt.	Avg. time	$\operatorname{Gap}_{(\%)}^2$	Gap3 (%)	Sol. not	Avg. opt.	Avg. time	Gap4 (%)	Gap5 (%)	$\operatorname{Gap}_{(\%)}^{\mathrm{Gap}_6}$
			sol.	found	(s.)	found	(s.)	(2.)	found	found	(s.)		(2.)	found	found	(s.)		()	()
40	сл С	3 14	0	1	3.85	9	21.55	5.00	9	5.67	0.82	0.50	-4.24	1	5.53	2.63	0.35	-4.39	-0.16
40	5	3 15	0	0	42.00	e S	82.50	8.11	e S	4.75	2.09	0.67	-6.76	0	3.13	11.72	0.61	-6.97	-0.23
40	5 15	5 15	0	0	719.40	°	442.58	7.49	e S	1.42	14.08	0.72	-6.20	0	3.53	87.50	0.54	-6.40	-0.21
40	7 3	3 15	0	0	8.66	0	33.93	6.27	0	1.93	69.03	0.40	-5.47	0	1.73	1.00	0.34	-5.52	-0.05
40	7 6	3 15	0	0	447.53	0	137.13	7.38	0	2.13	2.61	0.49	-6.37	0	3.20	2.64	0.41	-6.44	-0.08
40	7 15	5 12	ŝ	0	1870.86	0	645.53	7.76	0	2.07	16.63	0.54	-6.63	0	1.66	16.97	0.49	-6.66	-0.04
		14.33	0.50	0.17	515.38	2.00	227.20	7.00	2.00	2.99	17.54	0.55	-5.95	0.17	3.13	20.41	0.46	-6.06	-0.13

Table 2: Summary of results for instances with 40 contracts

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		$\substack{\operatorname{Gap}_6\\(\%)}$	-0.18	-0.08	-0.04	-0.04	-0.31	-0.30	-0.16
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			-5.02	-4.46	-4.91	-5.71	-5.59	-5.13	-5.14
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	- VNS	$_{(\%)}^{\rm Gap_4}$	0.58	0.57	0.64	0.54	0.51	0.61	0.58
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$\exists RASP$	Avg. time (s.)	1.61	4.82	34.14	1.61	4.70	33.09	13.33
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	U		0.66	1.53	0.36	0.73	0.86	0.06	0.70
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		Sol. not found	-	1	1	0	0	0	0.50
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		$\substack{\operatorname{Gap}_3\\(\%)}$	-4.85	-4.39	-4.87	-5.68	-5.30	-4.83	-4.99
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$S\Lambda$	$_{(\%)}^{\mathrm{Gap}_2}$	0.76	0.70	0.67	0.59	0.86	0.94	0.75
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	edy - Vl	$\operatorname{Avg.}_{\operatorname{time}}$	1.41	4.35	30.67	1.60	4.70	32.71	12.57
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	Gre_{t}	Avg. opt. found	0.69	0.00	0.14	1.00	0.73	0.13	0.45
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		Sol. not found	2	4	2	0	0	0	1.33
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		$\substack{\operatorname{Gap}_1\\(\%)}$	5.95	5.35	5.87	6.69	6.53	6.09	6.08
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	CVH	Avg. time (s.)	109.30	385.45	1551.38	134.06	558.40	2795.53	922.35
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		Sol. not found	2	4	2	0	0	0	1.33
CPL Opt. Only found sol. 14 0 13 0 7 7 15 0 15 0 15 0 15 2.50		Avg. time (s.)	18.71	183.53	4291.85	23.80	371.53	4450.20	1556.60
Opt. On found sc 14 sc 13 13 15 15 15 15 11.83 2.5	LEX	Sol. not found	1	2	1	0	0	0	0.67
f	CP_{i}	Only feas. sol.	0	0	7	0	0	8	2.50
Ch. Sh. Nd. 50 7 3 50 7 15 50 9 3 50 9 6 50 9 15		Opt. found	14	13	7	15	15	2	11.83
Cn. Sh. 50 7 50 7 50 7 50 9 50 9 50 9		Nd.	3	9	15	ŝ	9	15	
Cn. Cn. 250 Cn.		Sh.	4	7	2	6	6	6	
		Cn.	50	50	50	50	50	50	

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Summary 6
Table 3:

			(Greedy	G	RASP
Cn.	Sh.	Nd.	Gap (%)	Avg. time (s.)	Gap (%)	Avg. time (s.)
30	4	3	44.29	0.10	23.59	0.20
30	4	6	50.56	0.12	27.81	0.31
30	4	15	54.62	0.25	34.75	1.07
30	5	3	54.19	0.10	23.80	0.13
30	5	6	54.56	0.13	26.67	0.19
30	5	15	55.60	0.28	30.57	0.44
			52.30	0.16	27.87	0.39

Table 4: Summary of Greedy and GRASP results for instances with 30 contracts

			(Greedy	G	RASP
Cn.	Sh.	Nd.	Gap $(\%)$	Avg. time (s.)	Gap (%)	Avg. time (s.)
40	5	3	59.54	0.11	28.20	1.67
40	5	6	66.01	0.17	33.09	7.01
40	5	15	59.35	0.41	40.01	8.03
40	7	3	66.01	0.12	25.84	0.17
40	7	6	58.75	0.19	30.34	0.27
40	7	15	59.35	0.54	34.21	0.70
			61.50	0.26	31.95	2.98

Table 5: Summary of Greedy and GRASP results for instances with 40 contracts

			(Greedy	G	RASP
Cn.	Sh.	Nd.	Gap (%)	Avg. time (s.)	Gap (%)	Avg. time (s.)
50	7	3	67.63	0.13	31.70	0.36
50	7	6	73.10	0.23	36.97	0.85
50	7	15	75.02	0.76	43.74	4.66
50	9	3	67.76	0.14	27.96	0.20
50	9	6	68.60	0.27	30.28	0.36
50	9	15	69.48	0.97	33.49	1.35
			70.26	0.42	34.02	1.30

Table 6: Summary of Greedy and GRASP results for instances with 50 contracts

In order to better clarify the impact of the GRASP on the solution of the problem, Tables 4, 5 and 6 provide a comparison of gaps - regarding the CPLEX solutions - when applying the Greedy and the GRASP individually. As can be seen, the GRASP always provides much more quality results than the Greedy in very short time. Therefore, it is reflected once again the improvement made by the GRASP.

Gaps/Ships	4	5	7	9
Gap ₄	0.18	0.34	0.51	0.55
Gap_5	-4.75	-5.28	-5.50	-5.48

Table 7: Gaps per number of ships

Gaps/Nodes	3	6	15
Gap_4	0.35	0.41	0.45
Gap_5	-4.84	-5.55	-5.51

Table 8: Gaps per number of nodes in contracts

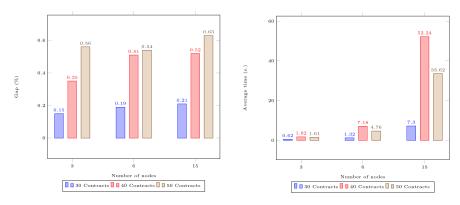


Figure 4: Average time and gaps per number of nodes

From previous tables, it can be deduced that the number of contracts af-569 fects the solutions quality, since the problem complexity increases. In order 570 to know how other instances features influence the quality, Tables 7 and 8 571 report gaps classified according to the number of ships and the number of 572 nodes per contract. As before, $\operatorname{Gap}_4(\%)$ and $\operatorname{Gap}_5(\%)$ present the gap be-573 tween CPLEX and GRASP-VNS objective function values, and between the 574 CVH and GRASP-VNS objective function values, respectively. In Table 7, 575 it can be seen that an increment in the number of ships slightly increases the 576 gap between CPLEX and GRASP-VNS solutions due to the rise in instances 577 complexity. Nevertheless, solutions provided by CVH are continuously im-578 proved by the GRASP-VNS algorithm, giving an indication that the quality 579 of CVH solutions is clearly much more influenced by the increasing complex-580 ity. In Table 8, it can be seen that the increment in the number of nodes 581 also results in an increase of the gap between CPLEX and GRASP-VNS so-582 lutions. Moreover, once again, CVH solutions are widely improved by the 583

⁵⁸⁴ proposed GRASP-VNS algorithm, as shown by the negative gaps.

With the aim of analysing the behaviour of the GRASP-VNS algorithm 585 when time windows are more discretized, Gap_4 from Table 8 has been split 586 by number of contracts requested in the instances, obtaining the first chart 587 of Figure 4. This way, it can be seen that the highest gap is always presented 588 for 50-contract instances and the lowest gap for the 30-contract instances 589 as expected due to the rise in complexity. A slightly tendency of the gap 590 to increase appears for each number of contracts when the number of nodes 591 increases. The same comparison has been made taking into account time 592 instead of gap. However, in this case it is evident that 40-contract instances 593 present more difficulties to be solved than the other ones, since times are 594 always the highest when solving these instances. Additionally, the sharp 595 increase of time going from 6 to 15 nodes is quite clear, which means that 596 the more discretization is used, the higher will increase the time. 597

598 6. Conclusions and Further Research

In this paper, a hybrid GRASP-VNS algorithm for solving a SRSPDTW 599 has been proposed. This problem belongs to the tramp shipping category, 600 which is increasingly present in the field of maritime cargo transport. The 601 objective considered is to minimize the total cost of serving a set of trip 602 cargo contracts, discretized time windows for picking and delivering cargoes. 603 This allows for a broad variety of features and practical constraints, such as 604 navigation speed to control fuel consumption. Moreover, previous works in 605 literature demonstrated that numerical results considering discretized time 606 windows presents a much better trade-off between solution quality and com-607 puting time than a similar constant speed continuous model. Even taking 608 into account discretized time windows, using exact algorithm to obtain the 609 optimal results involves large computational times. The hybrid GRASP-VNS 610 algorithm proposed here achieves high-quality solutions in less computational 611 time, and it has been demonstrated that both parts of the algorithm, GRASP 612 and VNS, contribute to this good behaviour. 613

It is noticeable from the computational experiments that results obtained do not only improve previous approximated solutions in the literature, but they are much closer to the optimal ones, presenting an average gap between 0.18 and 0.58 %. Actually, optimal solutions are obtained for many instances. Additionally, this GRASP-VNS algorithm finds solutions even when CPLEX is not able to find a feasible one in two hours.

On the other hand, an analysis of the proposed hybrid algorithm be-620 haviour was conducted in order to understand how the number of time win-621 dows influences the quality of results. It has been shown that the quality of 622 solutions is slightly affected by the level of discretization, so that the more 623 number of nodes, the higher the gap in respect to optimal solutions but still 624 within an acceptable level. However, the computational time shows a sharp 625 increase when the number of nodes goes from 6 up to 15. This means that 626 although the quality of solutions is acceptable, when the number of nodes 627 increases, the computational effort rises quickly. Hence, implementing the 628 right degree of discretization of the problems instances in hand is a key as-629 pect when solving this problem. 630

On the basis of the contributions presented in this paper, the next stage of the research will be focused on the analysis of how the consideration of the Container Stowage Problem impacts in the selection of contract nodes. The more time containers spend in maritime terminal, the more money should be paid, so this cost should be taken into account. Another open line for future research is applying the proposed hybrid GRASP-VNS algorithm to other tramp shipping or even to other kind of ship routing problems.

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