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1 **Evolutionary, multi-scale analysis of river bank line retreat using**
2 **continuous wavelet transforms: Jamuna River, Bangladesh.**

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20 **Abstract**

21 In this study continuous wavelet transforms are used to explore spatio-temporal
22 patterns of multi-scale bank line retreat along a 204 km reach of the Jamuna River,
23 Bangladesh. A sequence of eight bank line retreat series, derived from remotely-sensed
24 imagery for the period 1987-1999, is transformed using the Morlet mother wavelet.
25 Bank erosion is shown to operate at several characteristic spatial and temporal scales.
26 Local erosion and bank line retreat are shown to occur in short, well defined reaches
27 characterised by temporal persistence at the same location, and separated by relatively
28 stable reaches. In contrast, evidence of downstream propagation of bank line retreat
29 patterns is evident at larger spatial scales. The intensity of localised bank line retreat
30 (i.e. at scales of 0 - 20 km) is strongly related to the magnitude of monsoonal peak
31 discharge, but this relationship weakens as the spatial scale of erosion increases. The
32 potential of continuous wavelet analysis to enhancing our understanding of
33 morphological evolution in complex fluvial systems with multi-channel planforms is
34 discussed.

35 **Keywords**

36 Continuous Wavelet Transform, Jamuna River, Braided river, Time-space, Erosion
37 processes, Embayment pattern, Sediment wave.

38 **1. Introduction**

39 The planform evolution of the Jamuna River, Bangladesh, the distal portion of the
40 Brahmaputra, has been the focus of many studies in which the aim has been to assess,
41 characterise and quantify the magnitude and distribution of bank line migration (e.g.
42 Coleman, 1969; Sarma and Basumallick, 1984; Singh et al., 1990; Thorne et al., 1993,
43 1995; Thorne and Russell, 1993; Halcrow, 1994; Goswami, 1995; Goswami et al., 1999;
44 Ashworth et al., 2000; CEGIS, 2000, 2007; Khan and Islam, 2003; Sarma and Phukan,
45 2004, 2006; Sankhua et al., 2005; Sarma, 2005; Takagi et al., 2007). However,
46 quantification and prediction of the spatio-temporal patterns of bank line migration

47 exhibited by the river are complicated by its large geographical scale (here synonymous
48 with extent) and its complex planform, which features elements of meandering, braiding
49 and anastomosing (Fergusson, 1993). The large geographical scale has thus far
50 precluded the application of well-established hydraulic geometry relationships or
51 process-based explanatory models due to the difficulties associated with up-scaling
52 (Latrubesse, 2008). Furthermore, the river's complex and dynamic planform has also
53 precluded application of conventional, geometric models developed for simpler,
54 meandering channels (e.g. Ikeda et al., 1981; Parker et al., 1983; Johannesson and
55 Parker, 1989; Zolezzi and Seminara, 2001; Camporeale et al., 2005). In fact, the
56 difficulty inherent in large-scale, long-term studies of channel evolution and bank line
57 migration in complex, multi-channel rivers prior to the wide availability of high definition,
58 remotely sensed imagery explains why such studies have, until recently, been rarely
59 conducted (Best and Bristow, 1993; Richardson, 1997). To date, the majority of
60 geomorphological studies of the Jamuna have instead focused on investigating the
61 processes responsible for channel evolution and bank line migration at the scale of the
62 individual geomorphological unit. Examples include studies of channel bifurcations and
63 braid bars (Ashworth et al., 2000; Richardson and Thorne, 2001); braid bars and
64 associated floodplain embayments (Thorne et al., 1993; Halcrow, 1994) and the
65 evolution of meander bends in major anabranches (Thorne and Russell, 1993; Ellis,
66 1993).

67 The bank line adjustment processes associated with these different
68 geomorphological units exhibit non-stationarity (spatial and temporal localization) as
69 well as different, characteristic bank migration rates and scale-dependency in space
70 (circa $10^2 - 10^4$ m) and time (circa $10^0 - 10^1$ yr). It follows that, in rivers with multi-
71 channel planforms, the overall pattern of bank retreat is characterized as a complex non-
72 stationary waveform within which multiple, characteristic erosion patterns co-exist at
73 different scales, and at different downstream locations. For example, Thorne et al.
74 (1993) identified a gross-scale control of planform evolution associated with island and

75 nodal reaches first described by Coleman (1969) that are spaced along the channel at
76 intervals of circa 30 km. They also identified local bank migration processes that are
77 driven by braid bar growth and migration and which operate at smaller spatial (3 - 6 km)
78 and over shorter temporal scales (2 - 5 years). Their findings contrast with those of Ellis
79 (1993), who observed bank erosion and embayment formation related to meander
80 growth and migration in near-bank anabranches that occur at spatial scales of hundreds
81 of metres to several kilometres, persist over periods of 1-12 years, and drive erosion
82 rates ranging from 50 to over 250 m yr⁻¹. More recently, CEGIS (2007) identified bank
83 erosion and floodplain embayment forming processes associated with bar form
84 development in the Jamuna river operating at spatial scales of 3-15 km, over periods of
85 approximately 15 years and with erosion rates of of the order of 200 m yr⁻¹. A finding
86 common to these studies was that rates of downstream migration in the locations of
87 severe bank erosion also appear to be scale-dependent. This is consistent with the
88 downstream movement of sand bars (Coleman, 1969) and changes in the location of
89 relatively stable and unstable reaches over time (Takagi et al., 2007), which all suggest
90 a link to the downstream propagation of sediment waves (Gilbert, 1917; Madej and
91 Ozaki, 1996; Wathen and Hoey, 1998). Indeed both Thorne et al. (1993) and Takagi et
92 al. (2007) identified wave-like patterns of channel migration, with characteristic
93 wavelengths of ~150 km and ~35 km, respectively. These findings suggest that the
94 complex patterns of bank retreat observed in the Jamuna result from the superimposed
95 and cumulative effects of spatially-transient bank erosion processes, operating semi-
96 independently at a range of spatial and temporal scales.

97 Marcus and Fonstad (2010) argue that the development and availability of new
98 remote sensing technologies, coupled with widening accessibility to GIS, have led to the
99 emergence of the 'remote sensing of rivers' as a sub-discipline of fluvial geomorphology.
100 Complex patterns of bank migration are now commonly investigated based on temporal
101 sequences of bank line data, captured from aerial photographs or remotely-sensed
102 imagery. These data are analysed within a geographical information system (GIS) so

103 that rates of bank line retreat during specified periods can be computed (e.g. Gurnell et
104 al., 1994; Mount et al., 2003; Mount and Louis, 2005; Swanson et al., 2011). In such
105 studies, characterisation of downstream migration in bank erosion patterns reduces to a
106 problem of localizing in space the different magnitudes and scales of bank retreat events
107 that can be discerned from the data, and evaluating how these localized patterns vary
108 through time. In the past this has been achieved through a largely qualitative, visual
109 appraisal of the patterns observed in sequential plots of bank position or change (e.g.
110 Downward et al., 1994; Gurnell, 1997; Mount et al., 2003) coupled with examination of
111 summary bank retreat statistics (e.g. CEGIS 2000; 2007). Consequently, relatively little
112 quantitative understanding of either trends in the spatial localization associated with
113 erosion at different scales or the relative rates of erosion driven by the different
114 processes represented in the bank retreat record has been achieved. Moreover, it has
115 been difficult to causally relate the observed patterns of bank retreat to likely
116 geomorphological drivers; especially where these involve processes acting at different
117 spatial and temporal scales. Commenting on this in a recent review, Kleinhans (2010)
118 acknowledged the potential of remotely sensed time-series for unravelling channel
119 pattern changes, but also observed that, 'we need quantifiers for subtle patterns to
120 reveal structure objectively' (Kleinhans, 2010; page 313).

121 A more quantitative approach involves viewing the downstream distribution of
122 bank retreat as a spatial signal of planimetric change. According to this approach, the
123 different scales of erosion are equivalent to the different frequencies contained within the
124 signal and their magnitudes are equivalent to signal amplitude. Accordingly, the
125 downstream signal of erosion becomes the spatial equivalent of a standard time series
126 signal, with distance substituted for time. When re-conceptualised in this way,
127 techniques developed for the characterisation of frequency and amplitude in complex
128 signals, become potentially powerful tools for characterising bank retreat. One common
129 tool is the fast Fourier Transform (FFT), which offers good frequency localisation albeit at
130 the expense of poor spatial localisation (Graps, 1995). However, the FFT requires the

131 data series to be consistent with a statistically stationary model – something that cannot
132 necessarily be assumed when analysing bank retreat sequences in river channels (Van
133 Gerven and Hoitink, 2009). Alternative methods offering *both* frequency and spatial
134 localization, such as the windowed Fourier transform (WFT) (also known as the short-
135 time Fourier transform) and wavelet analysis are therefore, preferable. Both have been
136 applied to the analysis of river patterns (Ferguson, 1975; Camporeale et al., 2005, Van
137 Gerven and Hoitink, 2009). However, the WFT is considerably less adaptable than
138 wavelet analysis in that achieving good spatial resolution requires sacrificing frequency
139 localisation, and *vice versa* (Fournier, 1995 page 11). As a result WFT was not selected
140 for use in this research. While the use of wavelet analysis by geomorphologists remains
141 rare, it has been widely used by hydrologists for the characterisation of runoff time
142 series (e.g. Brillinger, 1994; Fraedrich et al., 1997; Labat et al., 1999, 2000, 2002;
143 Compagnucci et al., 2000; Gaucherel, 2002; Lafreniere and Sharp, 2003; Coulibaly and
144 Burn, 2004; Labat, 2005) Also, its potential in analysing signals in time series of river
145 planform change has recently been recognised by Van Gerven and Hoitink (2009), who
146 used it to characterise meander geometry on the Mahakam River, Indonesia. There are,
147 however, no published examples of its use in characterising bank migration in large
148 rivers with anabranching planforms.

149 In this paper we explore the potential of the continuous wavelet transform (CWT)
150 for the quantitative characterisation of temporal sequences of downstream bank line
151 migration patterns, using data recorded along a 204 km reach of the Jamuna River,
152 Bangladesh. The CWTs presented in this paper quantify changes in bank position in the
153 plane of maximum bank erosion. In line with previous studies of planform change from
154 remotely-sensed data, this is assumed to be orthogonal to the downstream direction.
155 This is believed to be the first time such an approach has been applied in a bank line
156 retreat study. In section 2 we describe the CWT method. Section 3 presents the
157 geomorphologic application, results and interpretation of the CWT to patterns of bank

158 line retreat on the Jamuna River. The key findings from the study are summarised in
159 section 4.

160 **2. Methodology**

161 Wavelet analysis comprises several mathematical transforms from which
162 temporal (or spatial) series can be transformed into a 2-D time (or space)-frequency
163 representation. A detailed treatment of the mathematics of wavelet transforms is
164 beyond the scope of this paper, but may be found in publications covering both wavelet
165 analysis theory (see Daubechies, 1992) and software implementation (Nason, 2008).
166 In this paper we make use of the continuous wavelet transform (CWT) popularised by
167 Torrence and Campo (1998). Our description of the CWT below draws from Torrence and
168 Campo (1998) using the notation and development of Sadowsky (1996), Kumar and
169 Foufoula-Georgiou (1997), and Biswas and Si (2011). In this description, $y(x)$ denotes
170 the spatial series of left bank (LB) downstream distance measurements. We can define
171 the CWT, which we denote by $W(s, \sigma)$, as the complex conjugation of $y(x)$ with a dilated
172 and translated 'mother' wavelet function $\psi_{s,\sigma}(x)$:

$$W(s, \sigma) = \int_{-\infty}^{\infty} y(x) \overline{\psi_{s,\sigma}(x)} dx$$

173 (1)

174 where

$$\psi_{s,\sigma}(x) = \frac{1}{\sqrt{s}} \psi\left(\frac{x - \sigma}{s}\right)$$

175 (2)

176 Here, s represents the dilation (scale) of the wavelet function and σ represents the
177 degree of distance translation along the series. The term $1/\sqrt{s}$ normalises the wavelet
178 function energy at each scale (Kumar and Foufoula-Georgiou, 1997; Torrence and

179 Campo, 1998). Equation (2) emphasises that the wavelet function is in fact a 'basis'
180 function (Fournier, 1995). For the CWT of a discretely sampled spatial series denoted
181 by $W_D(s)$ for a distance index d the integral in Equation (1) is substituted by a
182 summation and the distance x is replaced by increments of size δx (Torrence and Campo,
183 1998; Gurley and Kareem, 1999; Biswas and Si, 2011). Finally, the wavelet power
184 spectrum for a given transform can be defined as $|W_D(s)|^2$ (Torrence and Campo, 1998;
185 Biswas and Si, 2011).

186 Wavelet functions are required to have a compact support (in other words they
187 decrease rapidly to zero) and a mean of zero (Farge, 1992; Kumar and Foufoula-
188 Georgiou, 1997). In spite of these requirements, there are a great number of functions
189 available which satisfy these criteria. These can be classified in various ways such as (a)
190 orthogonal or non-orthogonal; (b) complex or real and in terms of (c) width and (d)
191 shape (see Torrence and Campo, 1998 § 3e). *Non-orthogonal* wavelets (they overlap)
192 are used in the CWT. The CWT therefore incorporates considerable redundancy in the
193 representation of the spatial series (Kumar and Foufoula-Georgiou, 1997) and an
194 alternative to this is to make use of *orthogonal* wavelets which are the basis of the
195 discrete wavelet transform (DWT) which in its simplest form can be thought as a set of
196 slices through the CWT at scales defined by powers of two (Percival et al., 2004).
197 However, it is argued that the non-orthogonal wavelets as used in the CWT are possibly
198 more appropriate for spatial series analysis as they can reveal more information on scale
199 localization (Biswas and Si, 2011). Non-orthogonal versions of the DWT do exist such as
200 the maximal overlap discrete wavelet transform and maximal overlap discrete wavelet
201 packet transform which have also been applied in the analysis of spatial series (Milne et
202 al., 2010).

203 Common examples of complex non-orthogonal wavelets used in the CWT (and
204 the focus of Torrence and Campo, 1998) include the Morlet (Fig. 1 A,B, Equation 3) and
205 the Paul (Fig. 1 C , Equation 4) wavelets, whilst the Derivative of Gaussian (DOG) (Fig. 1

206 D, Equation 5) is an example of a real-valued function (equations modified from
207 Torrence and Campo, 1998):

$$\psi(x) = \pi^{-1/4} e^{ikx} e^{-x^2/2}$$

208 (3)

$$\psi(x) = \frac{2^k i^k k!}{\sqrt{\pi(2k)!}} (1 - ix)^{-(k+1)}$$

209 (4)

$$\psi(x) = \frac{(-1)^{k+1}}{\sqrt{\Gamma(k + \frac{1}{2})}} \frac{d^k}{dx^k} (e^{-x^2/2})$$

210 (5)

211 Here, k is the parameter (known as the wavelet order) that controls the number of
212 oscillations in the wavelet function with the result of altering the resolution (both
213 frequency and distance) of the wavelet transform (De Moortel et al., 2004).

214 The choice of the most appropriate mother wavelet function to use in a wavelet
215 analysis (along with the optimal value of k) depends largely on the characteristics of the
216 signal itself, ideally reflecting the shapes of features present in the data series to be
217 analysed (Lane, 2007). However, there is a distinct lack of advice in the wavelet
218 literature on the optimal choice of these parameters, leading to the development of
219 context dependent criteria for relative comparison (e.g., Fu et al., 2003) which may or
220 may not be universal. Although Torrence and Campo (1998) have suggested that
221 different functions will nevertheless give the same qualitative results for wavelet power
222 spectra (Torrence and Campo, 1998), the practical advice of De Moortel et al. (2004) to
223 experiment with different parameters would seem appropriate.

224 *2.1. Cone of influence and significance levels*

225 As noted by De Moortel et al., (2004) the CWT as implemented in code such as
226 that developed by Torrence and Campo (1998) is often speeded up by transforming to
227 Fourier space. Common to Fourier transforms of finite series this introduces edge effects
228 primarily due to 'spectral leakage' as a result of edge discontinuities (Fougere, 1985).
229 There are a variety of methods to ameliorate such effects: the approach taken in
230 Torrence and Campo (1998) is 'zero padding' whereby zeros are added to the data series
231 up to the next integer power of two. This results in a 'cone of influence' (COI) at the
232 margins of the wavelet transform where the interpretation of the wavelet transform
233 should be considered unreliable (De Moortel et al., 2004).

234 It is also possible to perform a statistical significance test and calculate
235 significance by comparing the wavelet power to an appropriate background noise
236 spectrum. Commonly, either white noise or red noise (increasing power with decreasing
237 frequency) are used with the latter being a more realistic model of many geophysical
238 series that exhibit short distance spatial dependence (see Fougere, 1985). Red noise is
239 therefore often preferred (e.g., Si and Farrell, 2004 and references therein) and can be
240 modelled by a first order autoregressive AR(1) process (modified from Torrence and
241 Campo, 1998):

$$x(t) = c + \alpha x(t - 1) + z(t)$$

242 (6)

243 Where c is a constant, α is the lag-1 autocorrelation and $z(t)$ is white noise. We refer
244 the interested reader to the description of the Fourier power spectrum of (6) and a full
245 explanation with formulae for the quantification of significance levels using a Monte Carlo
246 simulation approach to Torrence and Campo (1998; § 4) as well as a summary
247 treatments by Si and Farrell (2004). If a peak in the wavelet power spectrum is
248 significantly above this background we might ascribe this to a scale dependent
249 pattern/process operating at that frequency. In this study we use a red noise

250 background spectrum with α computed according to the AR(1) coefficient and present all
251 significant results using the 95% confidence level.

252 2.2. Scale-averaging wavelet spectra

253 The fluctuations in wavelet power across discrete scale ranges or bands can be
254 achieved by defining the *scale-averaged wavelet power* as the weighted sum of the
255 wavelet power spectrum over scales s_1 to s_2 (modified from Torrence and Campo, 1998;
256 Coulibaly and Burn, 2004):

$$\bar{W}_D^2 = \frac{\delta j \delta x}{C_\delta} \sum_{j=j_1}^{j_2} \frac{|W_D(s_j)|^2}{s_j}$$

257 (7)

258 where C_δ is a constant that can be derived for any wavelet function via reconstruction,
259 and δj depends on the width of the wavelet function used and should ensure adequate
260 sampling in scale (see Torrence and Campo, 1998 § 5b for the derivation formulae).

261 Significance levels can also be ascribed to the scale averaged wavelet power via an
262 analytical relationship between the significance levels and the scale-averaged wavelet
263 power. For details of this the reader is again directed to Torrence and Campo (1998).

264 The scale averaged wavelet power is a series of the average variance in a certain band.
265 It can, therefore, be used to examine modulation of one series by another and / or
266 modulation of one frequency series by another within the same series.

267 **3. Geomorphologic application: bankline retreat characterisation of the Jamuna** 268 **River**

269 In this study we analyse bank migration along a 204 km reach of the Jamuna
270 river in Bangladesh (Fig. 2), between its confluence with the Teesta River just south of
271 the Indian border, and the Ganges River. The Jamuna is one of the largest and most
272 dynamic rivers in the world ranking fifth in terms of discharge (mean flow 12,200

273 cumecs) and eleventh in terms of drainage area (666,000 km²) (Thorne et al., 1993).
274 Analysis of the long-term evolution of the channel (Coleman, 1969; Burger et al., 1991;
275 Thorne et al., 1993; ISPAN, 1995; CEGIS, 2001; Takagi et al., 2007) has revealed a
276 highly dynamic channel that has undergone westward migration, widening and planform
277 metamorphosis following the creation of the present river by avulsion in 1830. The
278 meandering planform of the 19th century channel has been replaced by a much wider,
279 braided channel throughout the 20th century, and this change has been accompanied by
280 very high rates of bank line retreat. In the last three decades, the majority of this
281 retreat can be related to channel widening rather than centreline migration, although the
282 left hand bank does show a slightly higher average retreat rate (68 m yr⁻¹ between
283 1973 and 2000) than the right hand bank (60 m yr⁻¹) (CEGIS, 2000).

284 In this study we concentrate our analysis on patterns of bank retreat occurring
285 between 1987 and 1999. This period is characterised by particularly rapid channel
286 widening with spatially-variable and non-stationary patterns of stabilisation /
287 destabilisation; possibly associated with propagating sediment waves (Thorne et al.,
288 1993; Takagi, 2007), related to sediment supplied from upstream by the 1950
289 earthquake in Assam (Goswami et al., 1999). The pattern of bank retreat evidences
290 erosion at a wide range of scales from individual embayments to island reach scales. The
291 existence of localised, multi-scale bank retreat patterns, coupled with high retreat rates
292 make the period particularly well suited to wavelet analysis.

293 The floodplain of the left-hand bank (LHB) is comprised of newly accreted land
294 which is characterised by poorly consolidated and easily eroded bank material. This has
295 resulted in much more localised and complex patterns of bank retreat than that of the
296 right-hand bank (RHB) (Thorne et al., 1993). Indeed, between 1973 and 2006, 49,460
297 hectares of land eroded along 190 km of LHB, compared to 38,540 hectares along 245
298 km of RHB (CEGIS, 2007). Similarly, maximum rates of erosion are highest on the LHB
299 with local erosion exceeding 2000 m yr⁻¹ in several locations. As a consequence, the
300 downstream pattern of bank retreat for the LHB is characterised by events of greater

301 amplitude, greater variability of scale and greater spatial variability than the RHB, and
302 we have therefore selected the LHB data for subsequent analysis in this study.

303 *3.1. Bank line delineation methods and data series*

304 The data used in this study have been sourced from the Centre for Environmental
305 and Geographical Information Services (CEGIS), Dhaka. CEGIS have been responsible
306 for quantifying bank retreat rates along the entire length of the Jamuna in Bangladesh
307 from satellite imagery for the period 1973 – present. Their data has formed the baseline
308 geomorphological dataset for the World Bank’s Flood Action Plans (FAP-1, 1991; 1992).
309 We provide a summary below of the methods used to generate the data – further details
310 can be obtained from CEGIS (1997, 2001), including information on ground validation of
311 satellite image analysis.

312 A time-series of dry season Landsat MSS and TM images were used to document
313 historical changes in LHB position along the study reach. The time series of images
314 covered the period 1987-1999 (Table 1), allowing LHB migration to be computed for 8
315 separate periods: 1987-89; 1989-92; 1992-94; 1994-95; 1995-96; 1996-97; 1997-98
316 and 1998-99. All images were mosaiced and georeferenced to a 1:50,000 scale colour
317 base map; originally derived from 1989 high resolution SPOT satellite images, and
318 projected using the UTM-46N projection (CEGIS, 2007). For each image in the mosaic,
319 more than 25 ground control points were used to define a first order transformation to
320 the base map. Where possible, ground control points were taken from recognizable and
321 permanent features such as road intersections, airport runways and large buildings. The
322 maximum root mean square (RMS) error of the transformation was 96 m for the Landsat
323 MSS imagery (1987) and 45 m for the Landsat TM imagery (1989-1999).

324 The Jamuna in Bangladesh flows approximately due south (Fig. 2), and the
325 channel is therefore orientated along a consistent northing ordinate throughout its length.
326 Following the established methods of Gurnell et al. (1994); Gurnell (1997); Mount et al.
327 (2003) and Mount and Louis (2005) maximum bank erosion in the Jamuna can therefore

328 be assumed to occur in a direction orthogonal to the main channel (i.e. in an easterly
329 direction). Bank line position was assessed at a downstream spacing of 500 m; defined
330 by each image's northing coordinate. Consequently, LHB migration between consecutive
331 images at each downstream location was computed as the difference in the easting
332 coordinate of the bank line position, converted to m yr^{-1} according to the capture dates
333 of the imagery (Table 1). Bank lines were defined as the line which separates the
334 floodplain from the active braid belt. In general, bank lines encompass main channels,
335 island chars and sand bars in the river braid belt, except for crevasse splays (the coarse
336 sediments that are spread over the floodplains during floods). Where a major anabranch
337 of the river flows along the edge of the floodplain in a channel (which typically ranges in
338 width from hundreds of meters to several kilometres), the bank line delineation is simple
339 and uncontroversial. However, smaller distributary channels flowing next to the bank are
340 more difficult to define and a number of criteria can be applied to determine whether
341 they should be considered a part of the active braid belt (CEGIS, 1997, 2000):

- 342 (1) channels are outside the bank line if the channel does not return to the main river;
- 343 (2) channels are outside the bank line if the channel is less than 100 m in width;
- 344 (3) channels are outside the bank line if the channel has a meander radius of less than
345 one kilometre.

346 Due to the difficulties associated with determining whether material deposited at
347 the channel margins between images remains active channel or has become
348 incorporated into the floodplain, only bank line retreat rates are recorded in the data
349 series (deposition is recorded as zero). This means that the analysis presented here
350 represents a partial examination of the patterns on planimetric change on the Jamuna,
351 which comprise both bank line retreat and bank advance; the latter occurring through
352 the incorporation of sediments previously considered to be within the active channel into
353 the floodplain. All bank line retreat between consecutive images of 50 m or less was
354 considered to be within the margin of measurement and georeferencing error and was

355 recorded as zero retreat. For the periods 1989-92, 1992-94; 1994-95; 1995-96; 1996-
356 97; 1997-98 and 1998-99, where all images are of 30 m resolution, this margin exceeds
357 the 42 m quadratic sum associated with a ground feature identification error of ± 1 pixel
358 in each image (c.f. Mount and Louis, 2005). For the period 1987-89, in which one 30 m
359 and one 80 m resolution image are used, this value is less than the 85 m quadratic sum
360 of the ± 1 pixel ground feature identification error. Consequently, the magnitude of
361 bank line retreat in this period may be slightly over-estimated in the data. In addition to
362 the bank line data, daily mean discharge records from Bahadurabad (21.15°N , 89.70°E)
363 were also acquired from CEGIS. The resultant temporal sequence of bank line retreat
364 series is provided in Figure 3.

365 *3.2. Wavelet function selection*

366 In this study we consider the three wavelet functions described in Torrence and
367 Campo (1998) and detailed in Equations (3-5). These three functions offer a range of
368 different localisation capabilities (which are described in detail in De Moortel et al. 2004).
369 The Morlet wavelet (Equation 2) offers high frequency localisation capabilities which
370 result from the presence of a large number of oscillations but this increases the wavelet
371 width which in turn reduces spatial localisation capability. The Paul (Equation 3) wavelet
372 offers higher spatial resolution (it has fewer oscillations), but at the expense of
373 frequency localisation. The DOG (Equation 4) offers excellent spatial localisation of
374 individual peaks in the series, but can suffer from discontinuity in the frequency
375 localisation in the transform.

376 To assist in the identification of the preferred wavelet, a CWT decomposition of
377 the 1998-99 bank line retreat data was undertaken using all three wavelet functions
378 using the software developed by Torrence and Campo (1998) and implemented in
379 MATLAB. The 1998-99 data was selected because it represents one of the more complex
380 data series in the temporal sequence with a wide range of spatial scale and magnitudes
381 of bank line retreat evident. The relative lack of local oscillation complexity in the bank

382 line retreat series implies adequate frequency localisation should be achieved with a
383 relatively low wavelet parameter (k) value. Moreover, the use of a small value of k
384 reduces the area of the transform under the COI. Therefore, k was set to 3. However, a
385 transform was also generated using a Morlet, $k = 6$ wavelet to determine the impact of
386 increasing the k value. The results are provided in Figure 4.

387 The Paul $k=3$ and Morlet $k=3$ wavelets can be seen to generate very similar
388 patterns of significant wavelet power, associated with the same local peaks of bank line
389 retreat. There are subtle differences between the two in terms of their space /
390 frequency localisation capabilities. The Morlet $k=3$ transform exhibits some horizontal
391 compression and increased lateral connectivity of the 95% confidence regions in
392 comparison with the Paul $k=3$ transform; thereby highlighting its greater frequency
393 localisation capabilities. The DOG wavelet can be seen to localise peaks particularly well,
394 but at the expense of frequency. The result is lateral discontinuity in the 95%
395 confidence regions (which is also reported in De Moortel et al., 2004) and a frequency
396 localisation that is difficult to interpret. Increasing the Morlet wavelet k value to 6
397 results in a larger COI and a loss of significant wavelet power regions at high frequencies
398 and the loss of spatial localisation (i.e. the 95% confidence regions elongate
399 horizontally); thus making it difficult to map the significant bank line retreat frequencies
400 accurately on the ground. The results indicate that both the Paul $k = 3$ and Morlet $k = 3$
401 represent appropriate wavelet functions for the bank line retreat data series. However,
402 in this paper we use the Morlet $k = 3$ wavelet on the basis that it provides enhanced
403 frequency localisation with minimal loss of spatial localisation.

404 *3.3. Results*

405 *3.3.1. Continuous wavelet transform spectra*

406 The CWT spectra for the 8 bank line retreat series (Fig. 3) calculated using an
407 adaptation of the Torrence and Campo (1998) code are presented in Figure 5. Regions

408 of wavelet power that exceed the 95% confidence level are those within the bold lines,
409 with the dashed line indicating the COI.

410 The CWT spectra highlight two characteristic groupings of bank line retreat
411 patterns over the study period. Zones of significant wavelet power in 1996-97; 1997-98
412 and 1998-99 are largely constrained to wave periods of 16 km or less. These comprise a
413 mixture of small, very short wave periods (1-4 km) with very high spatial and frequency
414 localisation and a broader range of wave periods (2-16 km) in which the spatial and
415 frequency localisation is less well resolved. At both wave periods, significant zones are
416 spatially discrete and separated by downstream distances of between 10 and 20 km.
417 Moreover, there appears to be some temporal persistence in their location. Such
418 patterns are characteristic of locally-persistent bank line retreat events which occur
419 independently of any larger bank line retreat process (i.e. there is little evidence of local
420 bank line erosion patterns being superimposed on larger-scale, regional patterns). In
421 certain cases, the retreat is highly constrained to within a very short stretch of bank (i.e.
422 the 1-4 km wave period regions), whereas in others longer stretches are implicated (2-
423 16 km period regions).

424 By contrast, zones of significant wavelet power in 1987-89; 1989-92; 1992-94
425 1994-95 and 1995-96 are characterised by the existence of longer wave periods (16-64
426 km) extending over substantial downstream distances. These are coupled, to varying
427 extents, with superimposed and locally-discrete short wave period zones, which are
428 similar in character to those of 1996-97; 1997-98 and 1998-99, but less numerous.
429 Importantly, there is some evidence of downstream movement in the locations of the
430 longer wave period significance zones, from 0 – 60 km in 1987-89; 40 – 80 km in 1992-
431 94; 60 – 100 km in 1995 to 95 and 100 – 160 km in 1995-96. Such patterns are
432 difficult to interpret, yet their characteristic long wave periods, coupled with substantial
433 downstream extension and translation, would indicate that they may be characteristic of
434 bank retreat driven by the passage of a sediment-wave, or linked to the presence of
435 large, island char (quasi-stable, mature, vegetated islands within the active channel belt).

436 3.3.2. *Scale averaging*

437 Each of the CWTs was scale averaged into 0-10 km and 10-30 km bands
438 according to the scales of the two major downstream controls of bank retreat pattern
439 identified as operating on the Jamuna (c.f. Thorne et al., 1993). The 0-10 km band
440 encompasses the scale of individual braid-bars responsible for local bank retreat due to
441 embayment (CEGIS, 2007) and local bend evolution (Ellis, 1993). The 10-30 km band
442 encompasses the scale of island / nodal reaches associated with lower frequency
443 patterns of bank retreat governing gross-scale planform evolution (Thorne et al., 1993),
444 and the wavelength of propagating sediment waves (Takagi et al., 2007). The
445 downstream pattern of scale-averaged wavelet power exceeding the 95% confidence
446 level for each time period is plotted onto a single graph for each scale range (Fig. 6).
447 This allows the spatial and temporal persistence of different scales of bank retreat to be
448 investigated. Because the 95% confidence level of the scale-averaged wavelet power
449 varies between each time period, y-axis values are standardised as multiples of the 95%
450 confidence level for each retreat period.

451 At the 0-10 km scale, the LHB can be separated into a number of clearly defined
452 reaches according to the magnitude (i.e. the wavelet power multiples above the 95%
453 confidence level) and spatio-temporal persistence (i.e. the number of consecutive years
454 wavelet power exceeds the 95% confidence level at a given location) of the bank retreat
455 patterns (Table 2). Three low-magnitude, stable reaches, which exhibit little or no
456 significant wavelet power at scales of 0-10 km, at any time period, are visible at ~57-65
457 km, ~120-135 km and ~155-164 km. The last of these is almost certainly related to the
458 existence of stable guide bunds for Jamuna Bridge (Fig. 2). In all cases, these stable
459 reaches are short; not exceeding 15 km in length. In contrast two reaches exhibit
460 persistent significant 0-10 km wavelet power throughout the majority of the study period,
461 which is, at times, of high magnitude. These are located at ~65-85 km and ~135-155
462 km. They represent reaches of moderate length (~20 km), which exhibit consistent and
463 substantive bank line migration operating at scales indicative of embayment and

464 meander bend processes. Importantly, there is little evidence of downstream translation
465 of bank line retreat with the locations of each of the main peaks in wavelet power
466 occurring within ~ 10 km of each other (i.e. within the bounds of the spatial localisation
467 capabilities of the Morlet $k=3$ mother wavelet). Between these two end members are a
468 further three reaches in which the spatio-temporal pattern of bank retreat is transient
469 and of variable magnitude. These reaches range in length from 18 - 39 km.
470 Importantly, the transient reaches show clear evidence of downstream translation of the
471 peaks in wavelet power, as indicated by arrows in Figure 6. This may imply the
472 presence of transfer reaches where sediment eroded from the persistent, high
473 magnitude reaches is transferred downstream; instigating localised bank retreat as it is
474 transported.

475 At the island / node reach scale (10-30 km) there is little temporal persistence in
476 the locations of peak wavelet power; and thus of bank line retreat. However, the
477 existence of a stable, nodal reach at 100 - 120 km is of note. There is clear evidence of
478 downstream propagation of bank retreat. Between 1987-89 and 1995-96 a consistent
479 downstream translation of the peak wavelet power is visible, from ~ 25 km to ~ 75 km,
480 and at a mean annual rate of approximately 8 m yr^{-1} . This pattern is consistent with
481 that of sediment wave propagation observed by Takagi et al. (2007), both in terms of its
482 scale and location.

483 The temporal analysis presented in Figure 6 provides a simplified appraisal of the
484 pattern of location and frequency variation in bank retreat through time, where the
485 complexity has been reduced through the temporal isolation of the scale-averaged power
486 spectra from each CWT. As a result, the analysis does not provide a detailed evaluation
487 of the patterns of covariance from one CWT to the next. Techniques such as cross-
488 wavelet transforms and wavelet coherence analysis (Grinsted et al., 2004), that
489 specifically focus on quantifying the covariance between sequences of CWTs, offer
490 considerable potential in this regard (Torrence and Webster, 1999). Whilst the

491 application of these advanced techniques is beyond the scope of this paper, their
492 importance as a direction for future research should be recognised.

493 *3.3.3. Wavelet power relationship to discharge*

494 One of the key challenges in geomorphologic studies has been establishing and
495 elucidating the relationships between processes operating over different temporal and
496 spatial scales (Rhoads and Thorn, 1996, pp. 145-6; Phillips, 1999a,b; Couper, 2004).
497 Wavelet decomposition of sequential geomorphologic signals offers potential in this
498 regard through the examination of the pattern of variability in the strength of the
499 wavelet power at different frequency localisations and time periods and its relationship
500 with potential physical drivers of the signal.

501 To this end, we also examine the relationship between different scales of bank
502 retreat and discharge by quantifying the definite integral of the downstream scale-
503 averaged wavelet power spectra each time period (i.e. a numerical proxy for the total
504 magnitude of LHB retreat occurring at that scale) and plotting this against two measures
505 of peak discharge: the maximum discharge and the Q^{95} exceedance period (Table 3).
506 Whilst maximum discharge is identified as an important driver of bank retreat (Sarker
507 and Thorne, 2006; CEGIS, 2007), the use of variable time periods in this study means
508 that a time-integrated measure of peak discharge (i.e. Q^{95} exceedance) should also be
509 included in the analysis.

510 The CWT for each time period was scale-averaged into the following regular
511 intervals: 0-10 km; 10-20 km; 20-30 km; 30-40 km; 40-50 km. The definite integral of
512 each of the scale-averaged spectra for each time period was then quantified using the
513 trapezoidal rule and plotted against the peak discharge measures determined from the
514 available discharge records at the gauging station at Bahadurabad (Fig. 7).

515 At 0-10 km and 10-20 km scales, strong positive, exponential relationships are
516 seen to exist between the integral of the wave power spectrum and Q_{Max} / Q^{95}
517 exceedance (Figs. 8 and 9). This indicates that as peak discharge increases, so too does

518 the total amount of bank retreat on the LHB of the Jamuna. It is interesting to note
519 that, in general, the strength of the relationships is stronger for maximum discharge
520 than for Q^{95} exceedance, suggesting that QMax may be a more useful peak discharge
521 parameter when attempting to predict bank retreat on the Jamuna. Positive
522 relationships also exist at larger scales, albeit with far lower integrated power spectrum
523 values, and lower Pearson coefficients. The positive relationships identified are not
524 unexpected as the mean rate of bank retreat on the Jamuna is known to be related to
525 the magnitude of the largest monsoon flood (Sarker and Thorne, 2006; CEGIS, 2007).
526 However, the evidence that the strength of the relationship shows a consistent decrease
527 as scale increases is new and important knowledge. Overall reductions in the magnitude
528 of the wavelet power spectrum integrals are accompanied by a reduction in R^2 values as
529 scale increases. For QMax the reduction is from 0.86 at 0-10 km scales to less than 0.5
530 at scales greater than 30 km. For Q^{95} exceedance the reduction is from ~ 0.5 at scales
531 less than 20 km to ~ 0.3 at scales greater than 40 km. Thus, the pattern is one in which
532 peak discharge is strongly related to the rate of bank retreat on the Jamuna, but only at
533 spatial scales of less than 20 km. As the scale of bank retreat increases the importance
534 and statistical significance of peak discharge as a main driver of bank retreat is
535 substantially reduced.

536 *3.4. Geomorphologic interpretation*

537 A number of key characteristics of bank line retreat on the LHB of the Jamuna
538 river have been identified through the CWT analyses presented. Whilst some can be
539 interpreted with reference to well-understood geomorphologic processes and
540 conventional geomorphological thinking, others are more difficult to interpret and further
541 work is required to provide an adequate geomorphological explanation.

542 The CWT sequence in Figure 5 shows that at different times in the Jamuna river
543 data series varying amounts of significant, short (2-16 km), moderate (16-32 km) and
544 long (>32 km) wave-period bank retreat are evident. In some years (e.g. 1996-97;

545 1997-98 and 1998-99), spatially-discrete regions of short wave-period bank retreat are
546 dominant and there is little evidence of significant retreat at longer periods. This
547 indicates that, at these times, the main mode of planform adjustment is local; through
548 the erosion of individual embayments. At other times (e.g. 1987-89; 1989-92; 1992-94;
549 1994-95 and 1995-96) the co-existence of significant regions of wavelet power at longer
550 wave-periods indicates that a regional mode of planform adjustment at or above the
551 scale of individual chars operates is also in operation. Indeed, in some years (1994-95
552 and 1995-96) significant regions of bank retreat at long wave-periods strongly suggest a
553 macro-scale model of adjustment that exceeds the scale of individual island chars.

554 The scale-averaged data presented in Figure 6 are more easily interpreted and
555 provide important geomorphological insights into the different characteristics of the
556 spatio-temporal patterns of bank retreat operating at different scales. At scales of 0-10
557 km the evidence of locally-persistent retreating banks, separated by stable and/or
558 transient reaches, corresponds well with the findings from other studies of local
559 embayment patterns on the Jamuna (Ellis, 1993). However, the precise reasons for the
560 alternating pattern of stable / transient / eroding reaches at this scale are not fully
561 understood. At the scales at which gross planimetric control of bank retreat by quasi-
562 stable island / node reaches (10-30 km) is thought to dominate (Coleman, 1969; Thorne
563 et al., 1993) there is relatively little evidence that the locations of significant bank
564 retreat can be mapped directly to the locations of island reaches. Indeed, Thorne et al.,
565 (1993) identify seven separate island and nodal reaches located at roughly regular
566 downstream spacing throughout the 204 km study reach. However, no evidence of such
567 spacing in the pattern of significant bank retreat is evident in Figure 6, and only one
568 persistently stable reach is evident. This suggests that the importance of island and
569 nodal reaches on influencing the pattern and magnitude of bank retreat at large spatial
570 scales may be less important than previously thought. Instead, the downstream
571 propagating patterns of retreat observed correspond more closely to the influence of
572 sediment waves; the importance of which has been recognised in earlier studies (Takagi

573 et al., 2007). Indeed, they estimated a wavelength of 35 km and found the best
574 evidence for the propagation between 10 and 80 km downstream - approximately the
575 same wavelength and location of the patterns observed in Figure 6. Thus, additional
576 support is provided to the implication that propagating sediment waves are important
577 drivers of bank retreat patterns operating at scales of tens of kilometres on the Jamuna.

578 Relating the integral of a range of scale-averaged wavelet power spectra to
579 maximum discharge and Q^{95} exceedance, Figures 8 and 9 provide an important and
580 explicit confirmation of conventional geomorphological thinking about the importance
581 that can be ascribed to peak discharge as a driver of bank migration at different scales
582 (e.g. Hooke, 1980; Nanson and Hickin, 1986). On the LHB of the Jamuna the magnitude
583 of the peak discharge is strongly related to the integral of the wavelet power spectrum at
584 0-10 and 10-20 km scales and, hence, the magnitude of erosion at frequencies that
585 coincide with meander bend and embayment processes. At lower frequencies, where the
586 gross planimetric setting and regional factors such as the spatial variability of floodplain
587 substrate cohesiveness become important constraints on erosion, the relationship
588 between measures of peak discharge and wavelet power decreases.

589 **4. Summary and conclusions**

590 The Jamuna river provides an important venue for fundamental research on
591 process-form interactions in large-scale, complex fluvial systems. It is the epitome of a
592 wilful stream representing a complex, non-linear, dynamical system within which fluvial
593 processes, morphological responses and process-response feedback loops operate at
594 multiple scales of time and space. Past efforts at understanding this system have
595 generally focussed on studying the processes governing the evolution of individual
596 geomorphological units operating at a single scale within the channel, (e.g. anabranches,
597 bars, bends and bifurcations within the braided system). Yet, their value in
598 understanding how the system operates across its whole range of scales and periods of
599 adjustment are unavoidably limited by the approaches taken. As a consequence, the

600 multi-scale explanatory linkage between fluvial processes and channel evolution
601 envisaged first by Schumm and Lichty (1965) and later by Lane and Richards (1997)
602 remains poorly developed.

603 CWTs offer an important means by which key signals of planimetric change, in
604 the case of this study captured as sequences of bank migration spatial series, can be
605 localised not only in time, but also in space. This offers a powerful means of
606 characterising where, when and over what spatial scales change occurs. It thus
607 represents the first, vital step in determining a multi-scale, explanatory framework for
608 relating channel process and channel pattern evolution. In many cases, it will be
609 possible to map the patterns observed to the results of past channel evolution process
610 studies. In this context, CWTs offer an important means of identifying spatio-temporal
611 patterns of bank retreat at different scales that can then be linked to fundamental
612 processes of channel adjustment and the findings of past research efforts. In other
613 cases, the patterns observed in the CWT will be more difficult to explain by conventional
614 geomorphological thinking. In these cases, CWTs offer an important means by which
615 new research directions can be identified and directed.

616 However, the outputs from a CWT are only as good as the input data. Indeed,
617 the selection of a planimetric signal capable of providing an adequate characterisation of
618 the evolutionary processes of interest is critical. For example, whilst sequences of bank
619 line retreat series offer important insights into erosion processes, they provide no
620 information about the temporal, spatial and frequency scales at which deposition occurs.
621 This means that an important component of channel change processes are
622 uncharacterised and the links between depositional and erosional channel forms can only
623 be surmised; not explicitly demonstrated. Similarly, by focussing on a single bank line,
624 only half of the channel's erosion response is characterised. Consequently, determining
625 the optimum set of channel response signals to which CWT should be applied in order to
626 gain a more holistic characterisation of the patterns of channel evolution is a pressing
627 research need. Also of importance is the quality and comprehensiveness of the data

628 used. Where the length of the data series is short, the relatively large size of the COI
629 will limit the ability to localise low frequency responses in the data. The downstream
630 resolution of the data will ultimately determine the degree to which high frequency
631 responses can be localised. Similarly, the length of time over which the signal is
632 measured, relative to the return period of the fluvial processes responsible for those
633 changes, may reduce the magnitude of certain responses when the data are converted
634 to annual rates. This in turn will reduce their wavelet power in the CWT and may result
635 in their significance being underestimated.

636 To conclude, the results presented in the paper represent an early, exploratory
637 investigation of the usefulness of wavelet transformation of signals of planimetric change
638 in complex river systems. Considerable potential for the technique is evident, however
639 numerous questions remain and both wavelet analysis in general and CWT in particular
640 offer considerable opportunities for fruitful future research efforts in unravelling river
641 pattern change.

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867

868 **Table 1.** Images used to derive the bank line migration series.

Image Date	Sensor	Resolution	Acquisition Date	Q at Bahadurabad (m³ sec⁻¹)
1987	Landsat MSS	80m x 80m	7 Feb	4000
1989	Landsat TM	30m x 30m	28 Feb	6070
1992	Landsat TM	30m x 30m	8 Mar	4660
1994	Landsat TM	30m x 30m	25 Jan	5070
1995	Landsat TM	30m x 30m	28 Jan	4550
1996	Landsat TM	30m x 30m	31 Jan	4680
1997	Landsat TM	30m x 30m	18 Feb	No Data
1998	Landsat TM	30m x 30m	5 Feb	3710
1999	Landsat TM	30m x 30m	23 Jan	4830

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871 **Table 2.** Characteristic reach types at the 0-10 km scale band.

Downstream Distance	Reach Character	Description
0 - 8 km	COI	Falls within the COI.
8 - 57 km	Transient and Variable Magnitude	Reach contains significant wavelet power of low, moderate and high magnitudes, but which is temporally and spatially transient. Bank retreat is evident at scales of 0-10 km, but its location and magnitude exhibits a high degree of temporal variability. There is strong evidence of downstream migration of bank line retreat.
57 - 65 km	Low Magnitude	Little or no significant wavelet power at any time period. There is little evidence of bank retreat operating at scales between 0-10 km.
65 - 85 km	Persistent and High Magnitude	Reach has a consistent spatial and temporal pattern of significant wavelet power of medium and high magnitude. Substantive bank retreat at scales of 0-10 km is occurring throughout the study period.
85 - 120 km	Transient and Moderate Magnitude	Reach contains significant wavelet power of low and moderate magnitudes and which is temporally and spatially transient. Moderate bank retreat is occurring at scales of 0-10 km. There is evidence of downstream migration of bank line retreat.
120 - 135 km	Low Magnitude	Little or no significant wavelet power at any time period. There is little evidence of bank retreat operating at scales between 0-10 km.
135 - 155 km	Persistent and High Magnitude	Reach has a consistent spatial and temporal pattern of significant wavelet power of moderate and high magnitudes. Substantive bank retreat at scales of 0-10 km is occurring throughout the study period.
155 - 164 km	Low Magnitude	Little or no significant wavelet power at any time period. There is little evidence of bank retreat operating at scales between 0-10 km. This stable reach is probably a result of the guide bunds of the Jamuna Bridge.
164 - 196 km	Transient and Variable Magnitude	Reach contains significant wavelet power of low, moderate and high magnitudes, but it is temporally and spatially transient. Bank retreat is occurring at scales of 0-10 km, but its location and magnitude exhibit a high degree of temporal variability. There is strong evidence of downstream migration of bank line retreat.
COI 196 - 204 km	COI	Falls within the COI.

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873

874 **Table 3.** Maximum daily mean discharge (QMax) and the number of days exceeding the
875 total study period 95th percentile discharge (Q⁹⁵) for each time period.

Time Period	QMax recorded at Bahadurabad (m³ sec⁻¹)	Days exceeding Q₉₅
1987-89	98,300	42
1989-92	84,100	60
1992-94	67,000	18
1994-95	40,900	0
1995-96	87,000	15
1996-97	83,800	21
1997-98	79,219	5
1998-99	103,128	48

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879 **Figure 1.** Mother wavelets for A. Morlet (k=6), B. Morlet (k=3), C. Paul (k=3) and D.
880 DOG (k=3).

881 **Figure 2.** The location of the study reach showing the confluence with the Teesta River
882 (A), the location of the Bahadurabad gauging station (B), the approximate position of the
883 guide bunds of the Jamuna Bridge (C) and the confluence with the Ganges River (D).
884 Note that the main channel is orientated due north-south.

885 **Figure 3.** The temporal sequence of 1987-1999 bank line retreat series for the Jamuna
886 river LHB.

887 **Figure 4.** CWT for 1998-99 bank line retreat series using Morlet $k = 3$ and $k = 6$, Paul k
888 $= 3$ and DoG $k = 3$ mother wavelets. The bold line shows the 95% confidence level (i.e.
889 regions within the line have significant wave power over a background red noise
890 spectrum $\alpha = 0.72$). The thin dashed line shows the COI. Regions within the COI should
891 be interpreted with caution.

892 **Figure 5.** CWT power spectra (Morlet $k=3$ wavelet function) for bank line retreat series
893 for all time periods. The bold line shows the 95% confidence level (i.e. regions within
894 the line have significant wave power over a background red noise spectrum). The thin
895 line indicates the COI. Regions within the COI should be interpreted with caution.

896 **Figure 6.** Scale averaged wavelet power spectra for 0-10 km and 10-30 km scale bands.
897 Data are plotted as multiples of the wavelet power value equal to the 95% confidence
898 level. The analysis ignores the regions of the plots where variation of wavelet power
899 occurs within the cone of influence (labelled COI).

900 **Figure 7.** Daily mean discharge at Bahadurabad for the 1987-1999 study period. The
901 portion of the hydrograph within each time period is indicated.

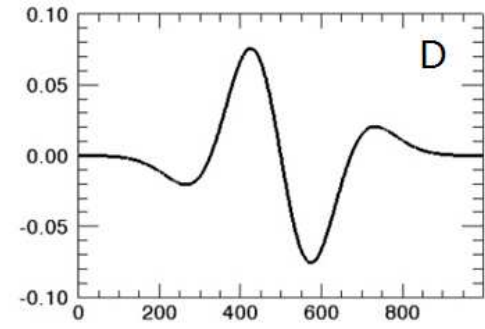
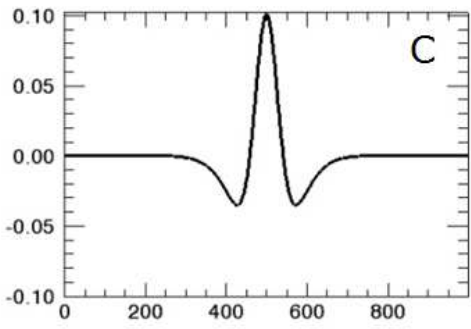
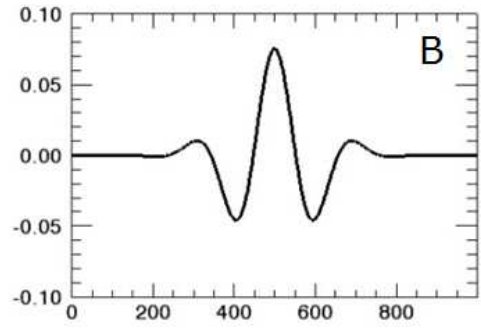
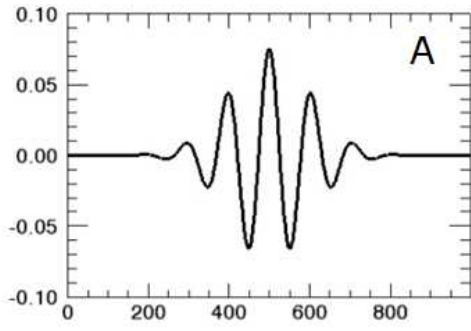
902 **Figure 8.** The relationship between Q_{Max} and the integral of the scale-averaged wavelet
903 power spectrum for scale bands 0-10 km, 10-20 km, 20-30 km, 30-40 km and 40-50 km.

904 **Figure 9.** The relationship between the number of days for which flow exceeds the 95th
905 percentile for the study period (Q_{95}) and the integral of the scale-averaged wavelet
906 power spectrum for scale bands 0-10 km, 10-20 km, 20-30 km, 30-40 km and 40-50 km.

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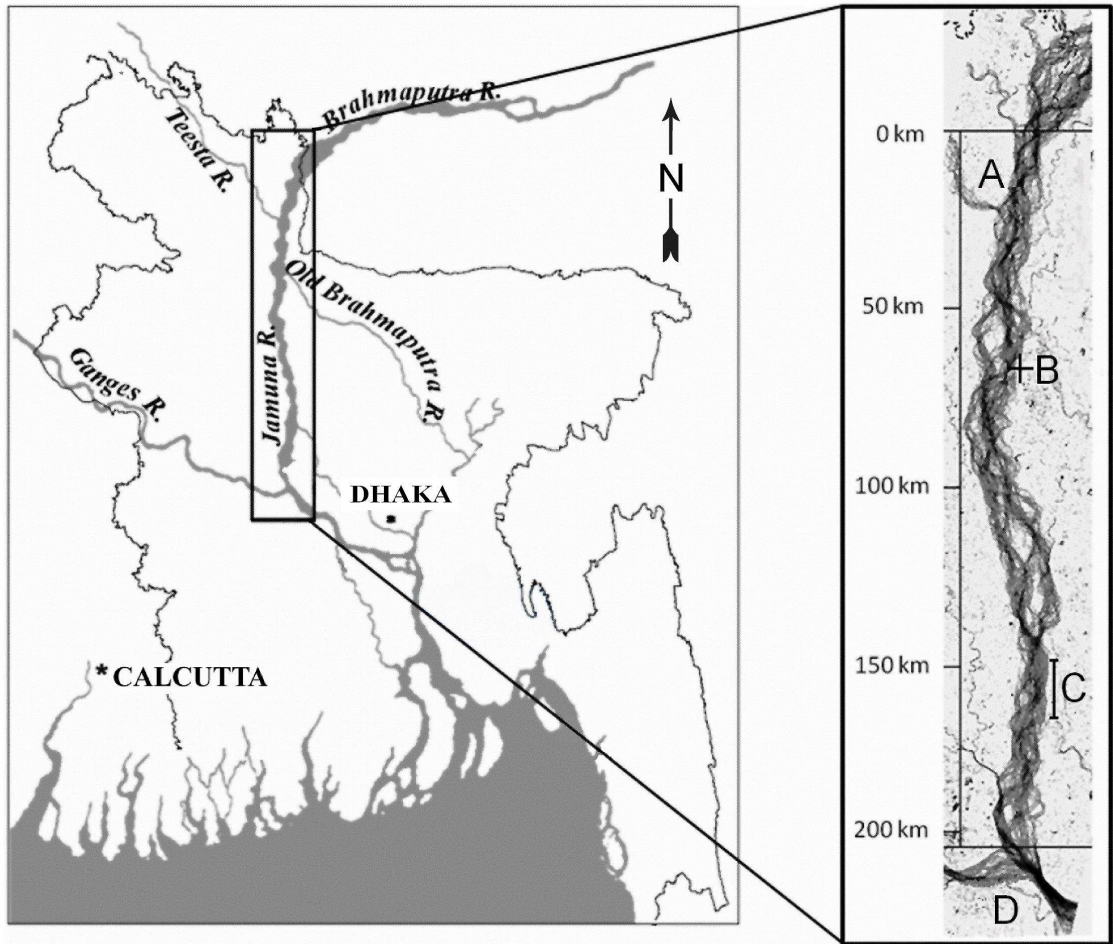
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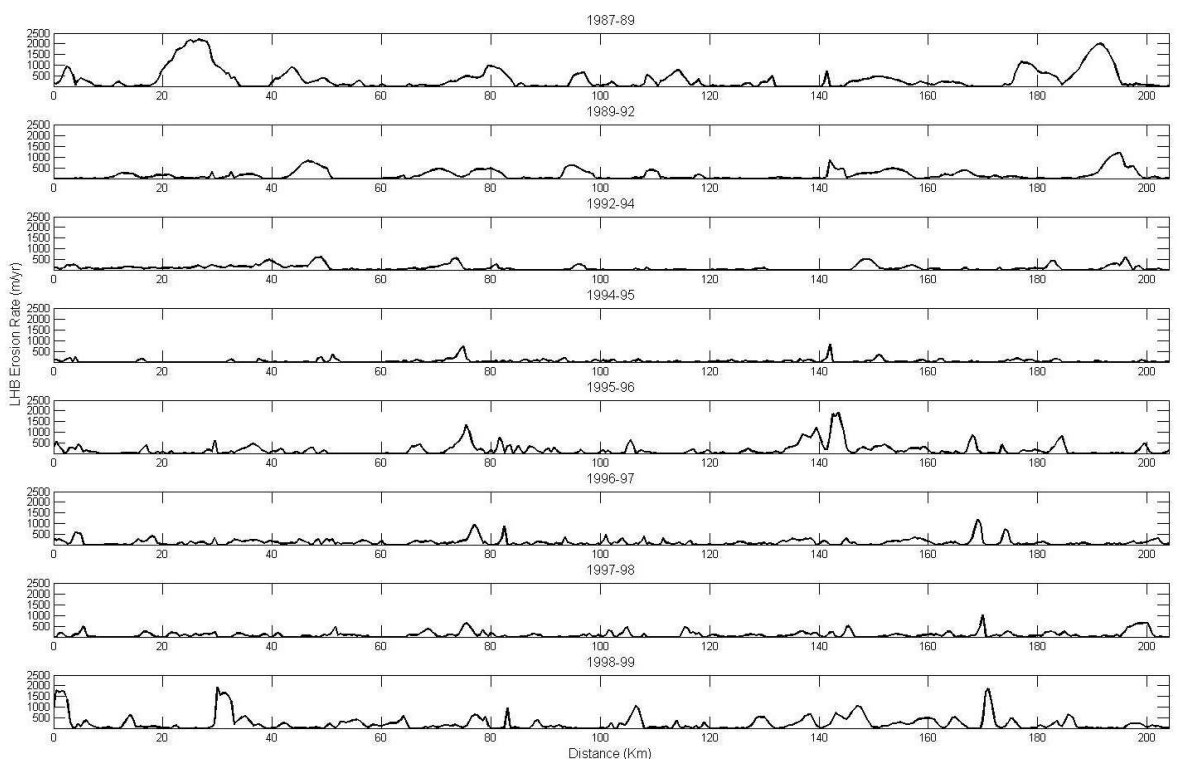
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Figure 1



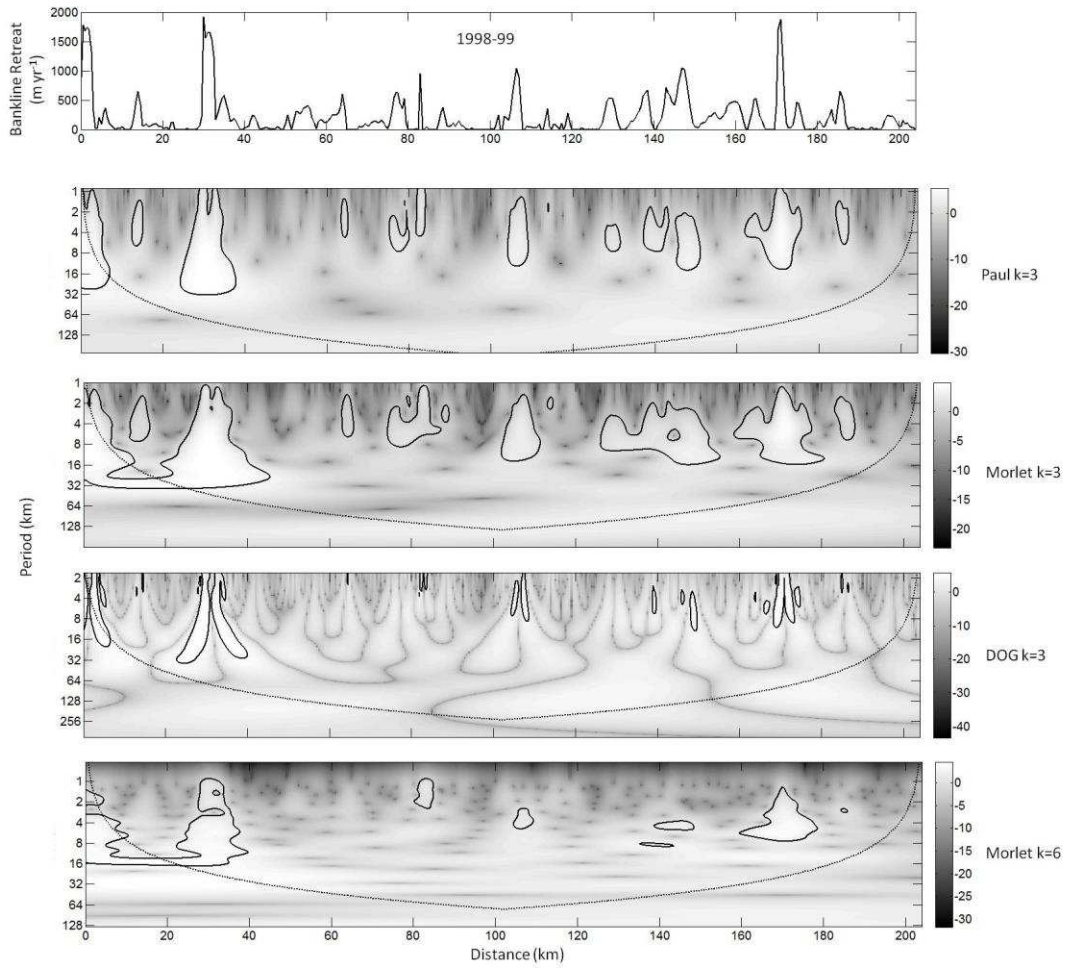
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Figure 2

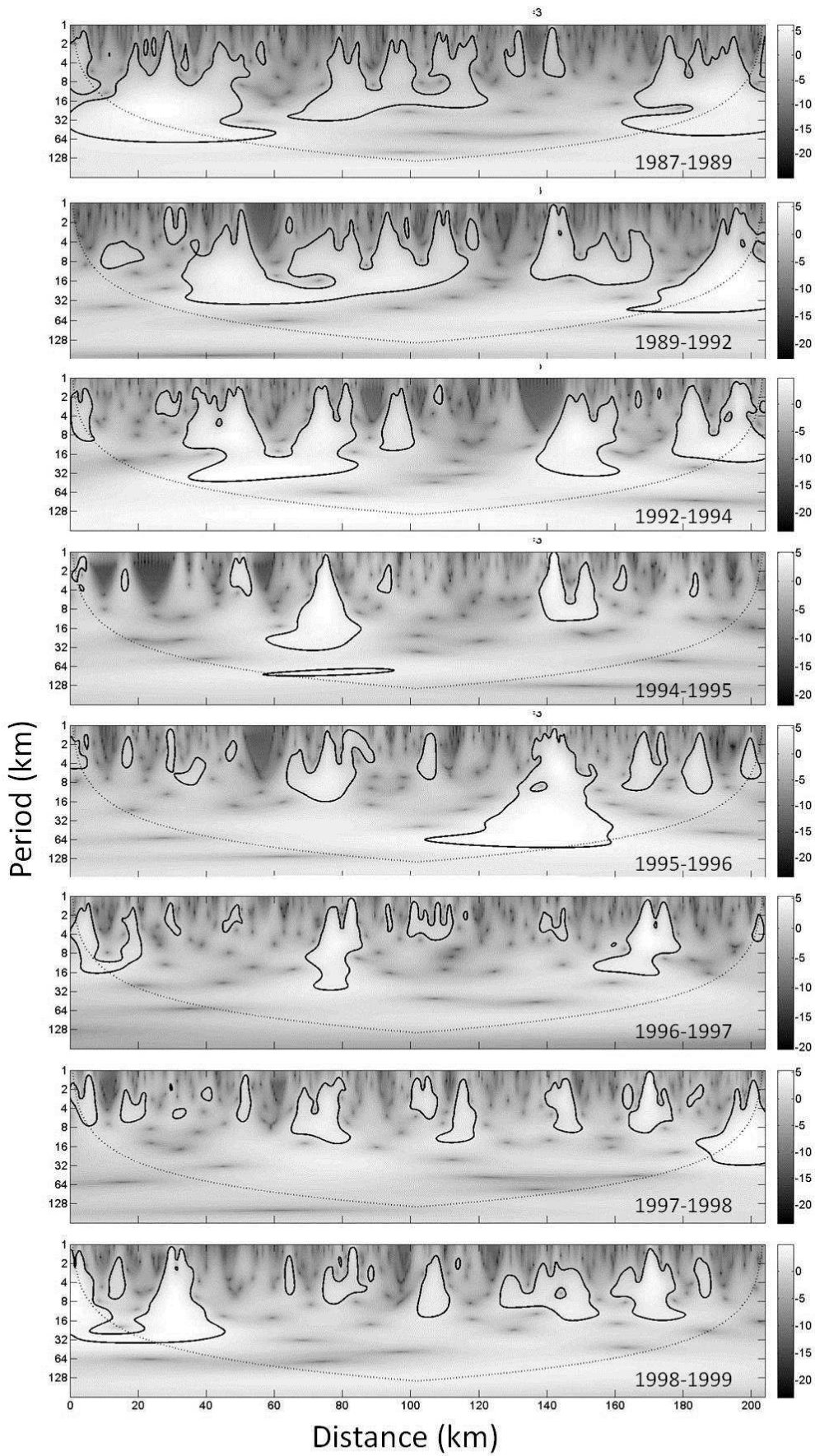


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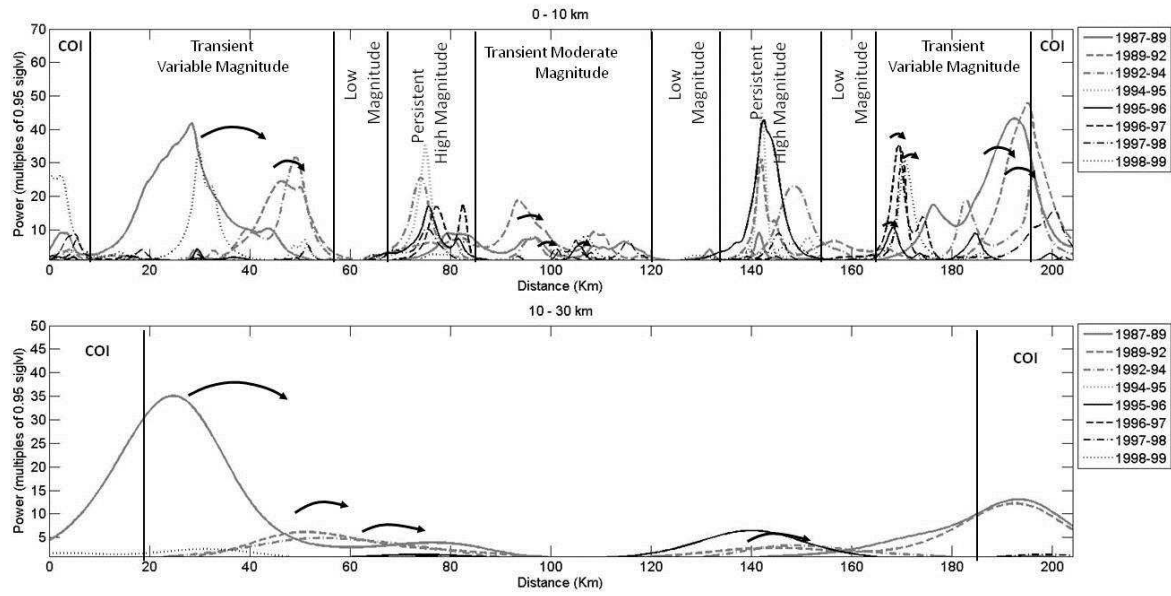
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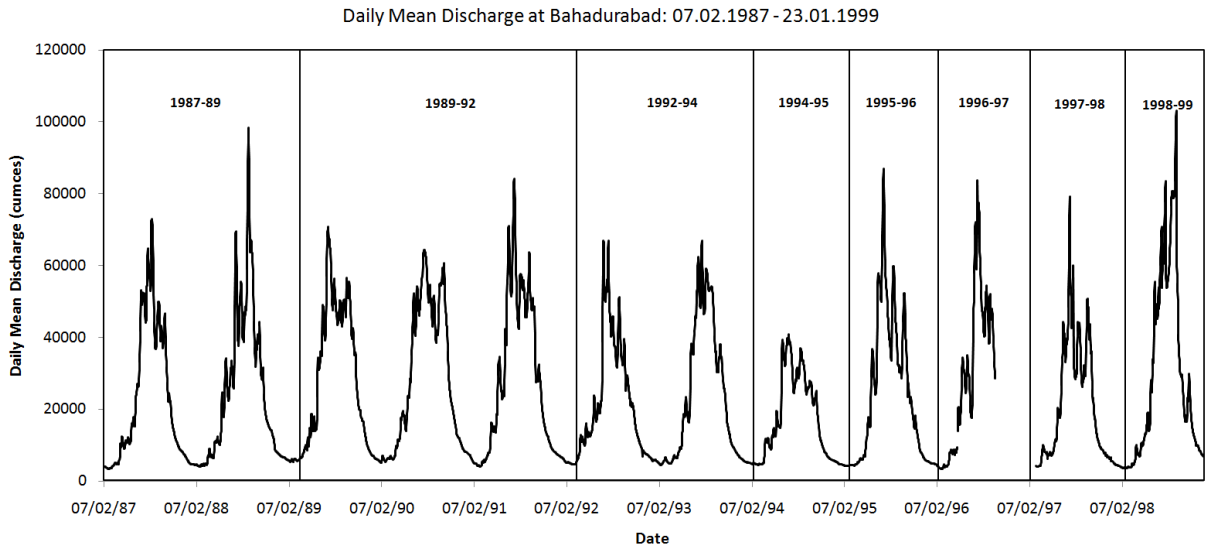
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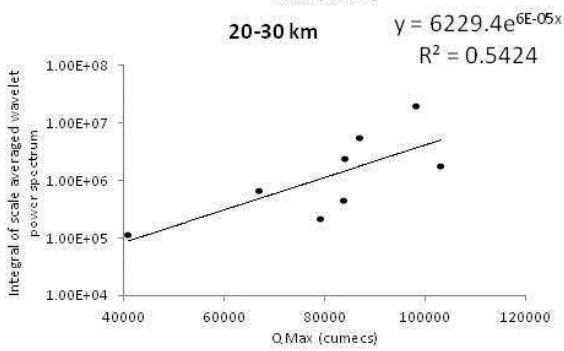
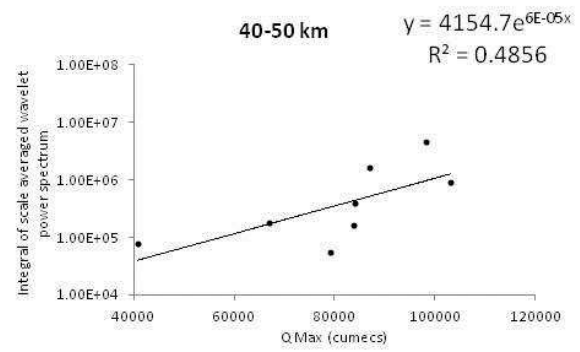
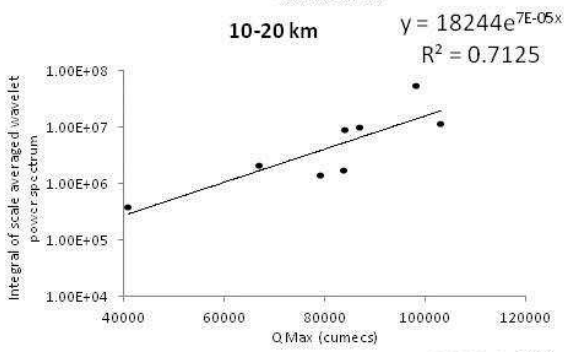
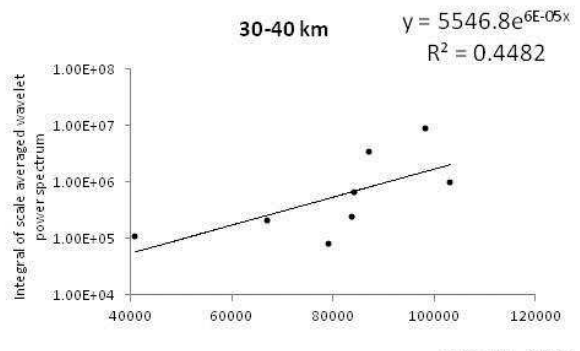
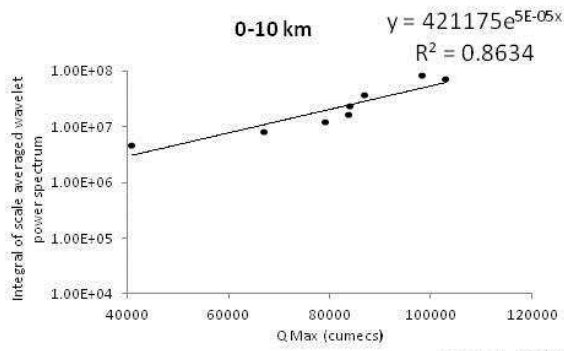
923 **Figure 5**
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925 **Figure 6**
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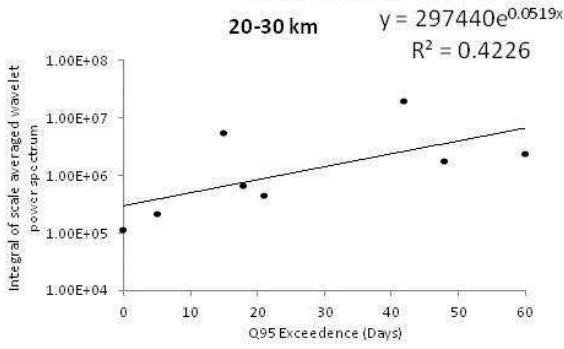
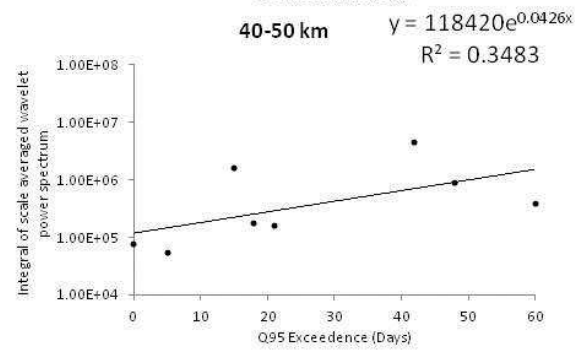
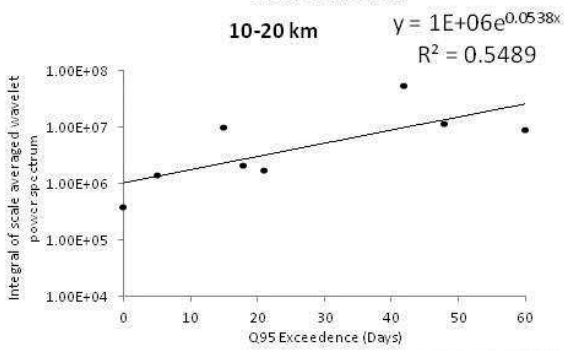
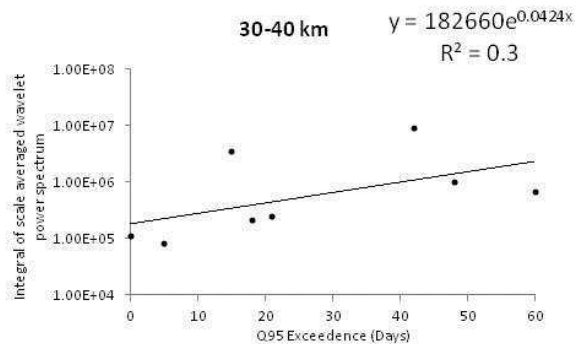
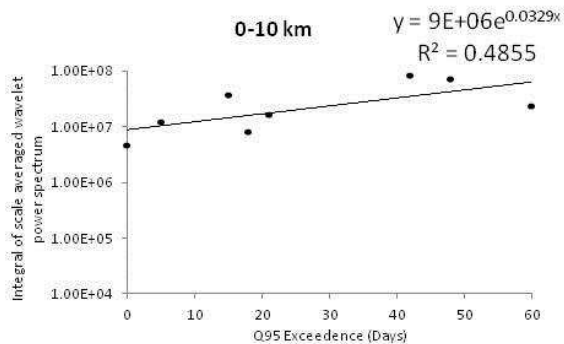


928 **Figure 7**
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Figure 8



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936 **Figure 9**