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On quantifying and resolving the BICEP2/Planck tension over gravitational waves

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The recent BICEP2 measurement of primordial gravity waves $(r = 0.2^{+0.07}_{-0.05})$ appears to be in tension with the upper limit from WMAP (r < 0.13 at 95% CL) and Planck (r < 0.11 at 95% CL). We carefully quantify the level of tension and show that it is very significant (around 0.1% unlikely) when the observed deficit of large-scale temperature power is taken into account. We show that measurements of TE and EE power spectra in the near future will discriminate between the hypotheses that this tension is either a statistical fluke, or a sign of new physics. We also discuss extensions of the standard cosmological model that relieve the tension, and some novel ways to constrain them.

PACS numbers:

The BICEP2 collaboration's potential detection of Bmode polarization in the cosmic background radiation (CMB) has justifiably ignited enormous excitement, signaling as it may the opening of a powerful new window onto the earliest moments of the big bang [1]. The implications are profound, including a possible confirmation of cosmic inflation and exclusion of rival explanations for the origin and structure of the cosmos.

As the BICEP2 collaboration was careful to emphasize, there is some tension between their value of the parameter r which controls the amplitude of the gravitational wave signal, relative to other experiments. BICEP2 detected B-mode polarization corresponding to $r = 0.2^{+0.07}_{-0.05}$ (or $r = 0.16^{+0.06}_{-0.05}$ after foreground subtraction), as compared to upper bounds from the large-scale CMB temperature power spectrum: r < 0.13 (WMAP) or r < 0.11(Planck) at 95% CL [2, 3]. It is the purpose of this Letter to quantify this discrepancy in a simple manner, to point out that measurements of CMB polarization E-modes will either sharpen or resolve it in the near future, and to explore cosmological interpretations.

In Fig. 1, we show current measurements of the temperature power spectrum C_l^{TT} , illustrating a deficit of power at low ℓ . This deficit was highlighted as an important anomaly by the Planck team [4]. However, taken alone, it is still compatible (at the 1% level) with cosmic variance and thus may be explained as a statistical fluctuation due to our only having access to a limited sample of the universe. BICEP2's detection of B-mode polarization, if correctly interpreted as being due to primordial gravitational waves, implies an additional contribution to the large-scale temperature anisotropies. This makes it harder to explain away the observed deficit as a statistical fluke.

We quantify this problem as follows. We compute likelihood functions $\mathcal{L}(r)$ for r inferred from WMAP, Planck, and BICEP2 (Fig. 2). Throughout this Letter, we use "WMAP" as a shorthand for the combination of datasets WMAP+SPT+BAO+ H_0 , and "Planck" as

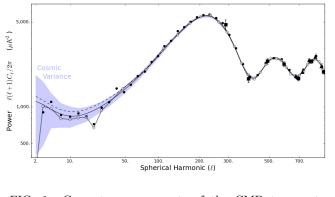


FIG. 1: Current measurements of the CMB temperature power spectrum, from Planck (open circles), WMAP (closed circles), ACT (squares) and SPT (triangles). Error bars include noise variance only; the shaded region represents cosmic variance. There is a small deficit of power on large angular scales relative to an r = 0 model (solid curve) which becomes more statistically significant if r = 0.2 as BICEP2 suggests (dashed curve).

a shorthand for Planck+(WMAP polarization). Notice that the Planck likelihood peaks at negative r. Of course, r < 0 does not make sense physically, but negative values of r may be taken to provide a reasonable parametrization of a possible deficit in low ℓ power, which avoids a *posteriori* choices in the weighting in ℓ .

We find that the Planck r-likelihood peaks 1.6σ below zero, indicating a deficit of large-scale power. The power deficit has been extensively studied by the Planck collaboration [3, 4]; its formal statistical significance can be as high as 3σ if an *a posteriori* choice of ℓ -range is made. Note that the preference for negative r is hidden when an $r \ge 0$ prior is imposed throughout the analysis (as is typically done when quoting upper limits on r from WMAP/Planck). Indeed, a primary purpose of this Letter is to point out that the tension between Planck and

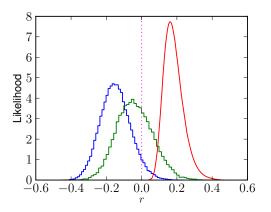


FIG. 2: 1D probability distribution functions for the tensor-to-scalar ratio r using Planck+WP data (blue/left), WMAP+SPT+BAO+ H_0 data (green/middle), and BICEP2 data (red/right). We use the CosmoMC [5] code with the six cosmological parameters { $\Omega_b h^2$, $\Omega_m h^2$, Ω_Λ , A_ζ , τ , n_s } marginalized. As discussed in the text, we allow r to be negative in order to parametrize a possible power deficit on large angular scales.

	$r \ge 0$ assumed		r < 0 allowed	
	WMAP	Planck	WMAP	Planck
No cleaning	0.048	0.007	0.017	< 0.001
BSS cross	0.054	0.009	0.019	< 0.001
BSS auto	0.067	0.012	0.024	< 0.001
DDM1 cross	0.054	0.009	0.020	< 0.001
DDM1 auto	0.095	0.020	0.034	0.001
DDM2 cross	0.089	0.018	0.032	< 0.001
DDM2 auto	0.189	0.057	0.066	0.003
FDS cross	0.040	0.006	0.015	< 0.001
FDS auto	0.059	0.010	0.021	< 0.001
LSA cross	0.052	0.008	0.019	< 0.001
LSA auto	0.059	0.010	0.021	< 0.001
PSM cross	0.046	0.007	0.017	< 0.001
PSM auto	0.114	0.026	0.041	0.001

TABLE I: Probability measure of the tension between Planck/WMAP and BICEP2 results, computed from the rlikelihoods using Eq. (1). (Low probabilities indicate tension.) The probability depends on whether we use Planck or WMAP data, whether we integrate over r < 0, and which of the polarized dust models described in [1] is used. As we have argued in the text, integrating over r < 0 takes the observed deficit of large-scale power into account, and gives $\approx 3\sigma$ tension with Planck regardless of the dust model.

BICEP2 is larger than would be expected by comparing the r constraints with an $r \ge 0$ prior imposed.

To quantify the level of tension, we temporarily imagine that our cosmological model contains two independent parameters r_T and r_B , such that r_T determines the gravitational wave contribution to C_{ℓ}^{TT} and r_B determines the amplitude of C_{ℓ}^{BB} . We obtain a likelihood

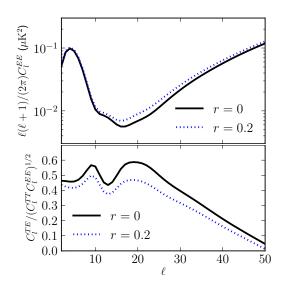


FIG. 3: E-mode power spectrum C_{ℓ}^{EE} (top) and dimensionless TE correlation $C_{\ell}^{TE}/(C_{\ell}^{TT}C_{\ell}^{EE})^{1/2}$ (bottom) compared for r = 0 and r = 0.2. An r = 0.2 signal boosts C_{ℓ}^{EE} by $\approx 30\%$ in the range $15 \leq \ell \leq 30$, making E-modes more sensitive to the tensor-to-scalar ratio r than temperature.

 $L(r_T)$ from Planck (or WMAP) and a likelihood $L(r_B)$ from BICEP2, as shown in Fig. 2. Treating these likelihoods as independent, which is justified since T and Bare uncorrelated, the joint likelihood in the (r_B, r_T) -plane is obtained by multiplying them. If the joint likelihood has most of its support below the diagonal $r_T = r_B$, this provides a statistically significant detection of a deficit in r_T relative to r_B . Thus we quantify the statistical significance of the tension by computing the probability

$$\frac{\int_{r_T > r_B} dr_T \, dr_B \, \mathcal{L}(r_T) \mathcal{L}(r_B)}{\int dr_T \, dr_B \, \mathcal{L}(r_T) \mathcal{L}(r_B)} \tag{1}$$

The closer this probability is to zero, the larger the tension between Planck/WMAP and BICEP2.

The results of this analysis are shown in Tab. I. It is seen that if we integrate over negative values of r and use Planck data, then the statistical significance of the tension is around 3σ . Our perspective is that integrating over negative r is sensible, since the observed deficit of TT power (relative to an r = 0 model) should contribute to the statistical significance of the tension. Indeed, we will see shortly that the Planck/BICEP2 tension can be interpreted as $\approx 3\sigma$ evidence for certain extensions of the 7-parameter model: either nonzero running $\alpha = dn_s/d\log k$, a blue tensor tilt n_t , or a higher effective number of relativistic species, which suggests that the "true" tension is around 3σ .

While this level of tension is not so high that a definite conclusion can be drawn, it is high enough to be worth exploring further. Since large-scale temperature measurements are already sample variance limited, the *only* way to improve statistical errors is by measuring additional large-scale modes. A natural source of such

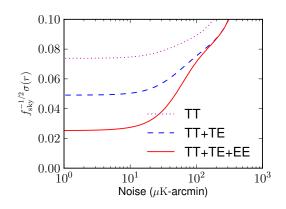


FIG. 4: Statistical errors on r obtained from different combinations of temperature and E-mode power spectra, as a function of noise level. The six parameters $\{\Omega_b h^2, \Omega_c h^2, \Omega_{\Lambda}, A_s, n_s, \tau\}$ have been marginalized.

modes is the *E*-mode polarization of the CMB. The influence of r on *E*-modes is particularly significant for multipoles in the range $15 \leq \ell \leq 30$ due to differences in the behavior of scalar and tensor perturbations just after horizon-crossing [6, 7]. In this ℓ range, an r = 0.2 gravitational wave background boosts C_{ℓ}^{EE} by $\approx 30\%$ and suppresses C_{ℓ}^{TE} by a similar amount (see Figure 3).

In a scenario where the BICEP2 result holds up and and we are left wondering whether the TT deficit is a $\approx 0.1\%$ statistical fluke or a sign of new physics, EE and TE become very interesting since they can discriminate between the two hypotheses (a similar point was made recently by [8]). If the TT deficit is not a statistical fluke, the deficit should be more significant when TE and EE are included. This is illustrated in Fig. 4, where we forecast the statistical error on $\sigma(r)$ which will result from measurements of TE and EE. The forecasted polarization sensitivity of Planck is 70 μ K-arcmin [9], and the width of the Planck+WP likelihood in Fig. 2 is $\sigma(r) = 0.10$. We therefore see from Fig. 4 that the statistical error on the tensor-to-scalar ratio may be reduced by a factor of two or so with Planck, and even further with future experiments [10]. Should Planck and BICEP's central values remain unchanged, the evidence for a deficit of largescale power as may conclusively sharpen. Conversely, if TE and EE measurements by Planck and other experiments provide evidence of additional large-scale power, the current tension between Planck and BICEP may be completely resolved. It will be fascinating to follow these developments.

So far, we have discussed the alternative hypotheses that the Planck/BICEP2 tension is either a statistical fluke or a symptom of needing more parameters in our cosmological model. We conclude by briefly exploring some specific choices of extra parameters which can relieve the tension.

First we identify interesting parameters by the follow-

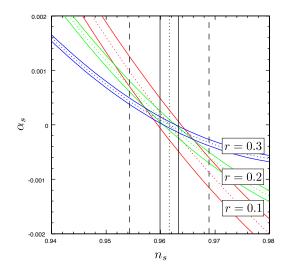


FIG. 5: Forecasted 1 σ errors in the (n_s, α_s) plane, obtained by combining the "standard Big Bang Observer" mission proposal [11]) with a CMB detection of r of 0.1 (red), 0.2 (green) or 0.3 (blue). The vertical lines show the current Planck value for n_s (dotted), the corresponding 1σ errors (dashed), and the forecasted 1σ errors (solid) from a future cosmic-variance limited map of T and E, with $f_{\rm max} = 0.7$ and $l_{\rm max} = 3000$.

ing approach. For each candidate parameter

$$\{\Omega_K, w, N_{\text{eff}}, m_\nu, \alpha, Y_{\text{He}}, n_t\}$$
(2)

we define the parameter to be "interesting" if the goodness-of-fit of the Planck+WP+BICEP2 dataset to the model improves by more than $\Delta(\log \mathcal{L}) = 2$ when the new parameter is included. With this definition, we find using CosmoMC that the parameters which are interesting are the tensor tilt n_t , running $\alpha = dn_s/d\log k$, and effective number of relativistic species N_{eff} . We briefly explore each of these possibilities.

As pointed out by the BICEP2 collaboration, the tension with Planck may be relieved if the running of the spectral index $\alpha_s = dn_s/d\log k$ is nonzero (see also [12– 14]). The combination of Planck and BICEP2 data prefers negative running at almost 3σ , with a best-fit value around $\alpha_s \approx -0.028$. This is around 100 times larger than single-field inflation would predict, but can be realized if V'''/V is about 100 times larger than would be naively expected based on the size of $V'/V \sim (10M_{pl})^{-1}$ and $V''/V \sim (10M_{pl})^{-2}$. Such a large value for V'''makes a leading-order contribution to the scalar bispectrum (in contrast to the usual case, where it is subleading [15]); but this new contribution still seems too small to be detected (roughly $f_{NL} \approx 10^{-2}$). It may be possible to measure α_s with statistical error approaching 10^{-3} in future large-scale structure experiments, if nonlinearity and bias can be modeled to sub-percent accuracy at $k \sim 0.1 \text{ Mpc}^{-1}$ [16].

It is clear that a negative α_s suppresses the smallscale scalar power. It is perhaps less obvious that, if the slow-roll consistency relations are satisfied, such neg-

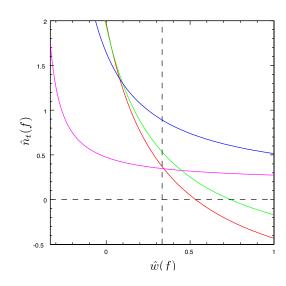


FIG. 6: Upper bounds in the $\{\hat{w}(f), \hat{n}_t(f)\}$ plane from combining CMB detection of $r \gtrsim 0.1$ with: current pulsar timing constraints [22] (blue), current LIGO constraints [23] (green), Big Bang Nucleosynthesis (red), and the requirement that the primordial tensor power is less than unity on all scales to avoid overproduction of primordial black holes (magenta). Here, $\hat{n}_t(f)$ and $\hat{w}(f)$ are appropriately averaged versions of $n_t(k)$ and w(t): see [24] for details. (The standard radiation dominated scenario is $\hat{w} = 1/3$.)

ative α_s also leads to a suppression of the small-scale tensor power [17] that should be readily discernible by a space based laser-interferometric gravitational wave detector like the proposed Big Bang Observer (BBO) mission [11, 18], or perhaps even by the somewhat less sensitive DECIGO mission [19, 20]. To understand this, note that we can use the first few slow roll consistency relations to predict the values of the tensor tilt $n_t = -\tilde{r}$, the running of the tensor tilt $\alpha_t \equiv dn_t/d\ln k = \tilde{r}(\delta n_s + \tilde{r}),$ and the running of the running $\beta_t \equiv d\alpha_t/d\ln k =$ $\tilde{r}(\alpha_s - \delta n_s^2 - 3\tilde{r}\delta n_s - 2\tilde{r}^2)$, where for convenience we have defined $\tilde{r} \equiv r/8$ and $\delta n_s \equiv n_s - 1$. This sensitivity of β_t to α_s , along with the huge difference between $k_{\rm BBO}$ and $k_{\rm CMB}$, provides a tremendous lever arm (roughly $k_{\rm BBO}/k_{\rm CMB} \approx 10^{17}$) to measure α_s ; see Fig. (5). If we assume the slow-roll consistency relations are satisfied, then the CMB+BBO will be able to measure α_s with an error of $\pm 0.001!$ Note that the slow-roll approximation should still be satisfied on BBO scales, since they cross the horizon at least 10 e-foldings before the end of inflation. The slow-roll consistency relations can be used to extrapolate from CMB scales to BBO scales if the slowroll parameters obey the usual hierarchy ($\alpha_s = \mathcal{O}(\epsilon^2)$), etc.) but fail in cases where this hierarchy is badly violated (e.g. models with transient features [21]).

Next consider the tensor tilt n_t . The Planck/BICEP2 tension can be lessened if the tensor power spectrum is

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very blue (n_t positive and of order one), so that the value of r measured by BICEP2 at $\ell \approx 60$ is larger than the value of r measured by Planck at $\ell \approx 30$. The combination Planck+BICEP2 prefers positive n_t at more than 3σ , with best-fit value $n_t \approx 2.0$ (a similar result was reported in [25, 26]). From a theoretical standpoint, a blue tilt would be in conflict with slow roll inflation, which predicts $n_t \leq 0$. From an observational standpoint, it is interesting to explore the extent to which a blue tilt is consistent with other constraints on the primordial gravitational wave spectrum at much smaller comoving scales. Such constraints depend on the equation of state w during the "primordial dark age" from the end of inflation to the start of BBN. In Fig. 6, we show current constraints in the $\{\hat{w}(f), \hat{n}_t(f)\}$ plane, where $\hat{w}(f)$ and $\hat{n}_t(f)$ are appropriately averaged versions of w and n_t [24]. We see that a blue spectrum with $n_t \gtrsim 0.5$ runs into conflict with smaller scale constraints if it extends over too many decades in wavenumber.

Finally, we have identified N_{eff} as an interesting parameter (as also found in [27]). This is best explored in combination with external datasets (ACT, SPT, H_0 , BAO, and cluster abundance); we refer to [28, 29] for an in-depth discussion.

The list of candidate parameters we have considered in Eq. (2) is not intended to be exhaustive, and it will be very interesting to consider other possibilities. For example, a scalar field that was initially "fast-rolling" and then settled into its slow-roll attractor at around the time that the largest CMB scales left the horizon (see e.g. [30–32]) might produce an observationally viable scenario, with $n_t > 0$ over a narrow range of scales near the horizon; we plan to investigate this in future work. The Planck/BICEP2 tension is currently around 3σ , which is not yet enough to discriminate between candidate explanations (e.g. running, tensor tilt, unknown systematics, or a $\approx 0.1\%$ unlikely statistical fluke), so at this stage we are simply enumerating possibilities.

We have carefully quantified the current tension between Planck, BICEP and the 7-parameter model, finding they are only compatible with a probability of around one in a thousand. In the near future, EE and TE measurements will provide a decisive test, and we will know if the tension is a statistical fluke or a sign of new physics.

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