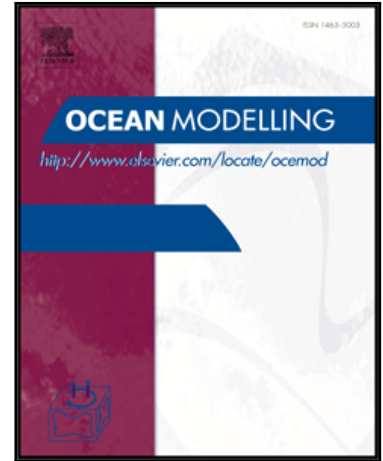


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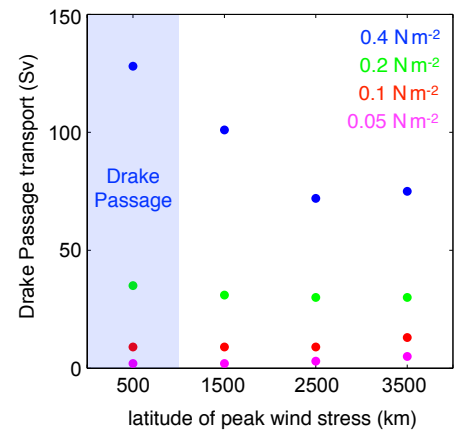
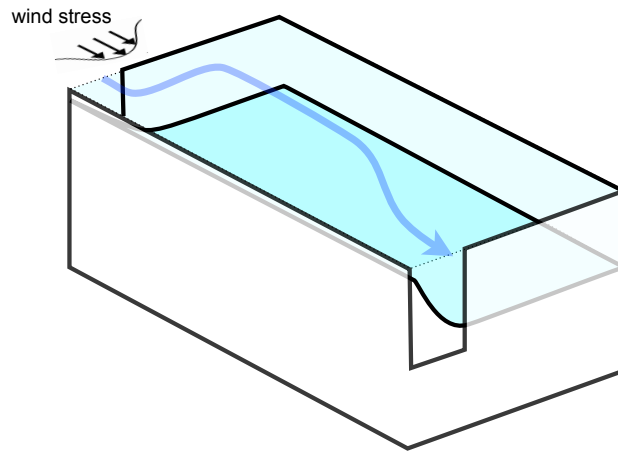
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Highlights

- Adrian Gill's model of the Antarctic Circumpolar Current (ACC) is reinterpreted.
- Eddy-induced vortex stretching plays a key role in the vorticity balance of the ACC.
- A substantial ACC remains when the wind is 3000 km north of Drake Passage.
- The net wind stress over the ACC streamlines is a predictor of its volume transport.
- A correction for basin-wide pressure gradients leads to good quantitative agreement.



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Gill's model of the Antarctic Circumpolar Current, revisited: the role of latitudinal variations in wind stress

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Abstract

Adrian Gill's (1968) model of the Antarctic Circumpolar Current (ACC) is reinterpreted for a stratified, reduced-gravity ocean, where the barotropic streamfunction is replaced by the pycnocline depth, and the bottom drag coefficient by the Gent and McWilliams eddy diffusivity. The resultant model gives a simple description of the lateral structure of the ACC that is consistent with contemporary descriptions of ACC dynamics. The model is used to investigate and interpret the sensitivity of the ACC to the latitudinal profile of the surface wind stress. A substantial ACC remains when the wind jet is shifted north of the model Drake Passage, even by several thousand kilometers. The integral of the wind stress over the circumpolar streamlines is found to be a useful predictor of the magnitude of the volume transport through the model Drake Passage, although it is necessary to correct for basin-wide zonal pressure gradients in order to obtain good quantitative agreement.

Keywords: Antarctic Circumpolar Current, ocean circulation, geostrophic eddies, wind stress, Drake Passage

1. Introduction

The Antarctic Circumpolar Current (ACC) is the only current to circumnavigate the globe, with a thermal wind volume transport through Drake Passage of $137 \pm 7 \text{ Sv}$ ($1 \text{ Sv} \equiv 10^6 \text{ m}^3 \text{ s}^{-1}$), relative to the sea floor (Meredith et al., 2011). The ACC plays a pivotal role in setting the global ocean stratification, heat content and overturning circulation (e.g., Gnanadesikan and Hallberg, 2000; Vallis, 2000), and may also set the time scale on which the ocean equilibrates to changes in forcing (Allison et al., 2011; Jones et al., 2011; Samelson, 2011). Moreover, it has been proposed that changes in the strength and latitude of the

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10 Southern hemisphere wind jet, due to its impact on the circulation along and
11 across the ACC, may have a profound influence both on past climate variations
12 (e.g., Toggweiler et al., 2006) and anthropogenic climate change in the future
13 (e.g., Fyfe et al., 2007; Le Quéré et al., 2007)

14 Despite its global climatic importance, there is no consensus on the dy-
15 namical processes that set the volume transport of the ACC and its lateral
16 structure, i.e., its meridional excursions with longitude, even in simple models.
17 The traditional, textbook view is that the ACC is driven locally by wind and
18 buoyancy forcing, with geostrophic eddies playing a central role in the equili-
19 brated state (for excellent reviews, see Rintoul et al., 2001; Olbers et al., 2012),
20 although more recent developments have challenged this purely local perspective
21 (e.g., Gnanadesikan and Hallberg, 2000; Fučkar and Vallis, 2007; Munday et al.,
22 2011). Diagnostic studies with climate models find no clear relation between
23 the volume transport of the ACC and the strength and latitude of the Southern
24 Ocean wind jet (e.g., Russell et al., 2006).

25 In 1968, Adrian Gill published a seminal paper in which he solved analyti-
26 cally and numerically for the barotropic circulation in an idealized basin with
27 circumpolar connection over a restricted latitude band (Gill, 1968). One of his
28 key objectives was to reconcile zonally-symmetric models of the ACC, in which
29 the volume transport is excessively large, with basin models of the ACC in
30 which the flow consists of a Sverdrup interior and a frictional western bound-
31 ary current (Stommel, 1957). Key findings were that the volume transport is
32 controlled by the bottom friction and the width of the narrowest constriction
33 in Drake Passage, although the current spreads out to several times this width
34 at other longitudes. However, Gill's model has limited applicability due to its
35 assumption of barotropic dynamics, its excessively large volume transport, and
36 the dependence of the latter on the coefficient of bottom friction.

37 A key ingredient of contemporary models of the ACC is the intense geostrophic
38 eddy field. In the simplest, zonally-symmetric models, as first developed by
39 Johnson and Bryden (1989), the ACC volume transport is determined through
40 the zonal momentum budget under so called “non-acceleration conditions”. Due
41 to the absence of continental barriers at the latitude of Drake Passage, the sur-
42 face wind stress is mostly balanced by a bottom form stress (Munk and Palmén,
43 1951). Thus, momentum must be fluxed vertically from the surface to the abyss,
44 which Johnson and Bryden assume is achieved by the eddy form stress. An al-
45 ternative, but equivalent, physical interpretation is that the equilibrium ACC
46 arises through the competition between the wind-driven Ekman cell (the “Dea-
47 con cell”) acting to steepen, and the eddy-induced cell generated through baro-
48 clinic instability acting to flatten, the isopycnals (e.g., see Danabasoglu et al.,
49 1994). Finally a prediction of the ACC volume transport follows on adopting a
50 closure for the eddy buoyancy fluxes following Green (1970) and Stone (1972),
51 and assuming thermal wind balance and vanishing flow at depth.

52 However, the ACC is not zonal, but undergoes significant meridional ex-
53 cursions, which are of dynamical importance because the majority of the wind
54 work on the Southern Ocean occurs north of Drake Passage (e.g., see Fig. 14 of
55 Mazloff et al., 2010). Understanding the cause of these meridional excursions is

56 important as several studies have suggested that the integral of the wind stress
 57 over the circumpolar streamlines of the ACC may serve as a useful predictor
 58 of its volume transport (e.g., Ishida, 1994; Allison et al., 2010; LaCasce and
 59 Isachsen, 2010). The traditional explanation for these northward excursions
 60 is Sverdrup balance (Sverdrup, 1947; Stommel, 1957; LaCasce and Isachsen,
 61 2010). However, if the Ekman driven upwelling is compensated by eddy-induced
 62 downwelling, then, at least for that part of the fluid column with circumpolar
 63 connection, Sverdrup balance should be modified to include the effect of the
 64 eddy-induced downwelling. Intricate interplays between the Sverdrup-like ex-
 65 cursions and eddy dynamics are documented in the series of papers by Nadeau
 66 and Straub (2009, 2012) and Nadeau and Ferrari (2015).

67 Recent developments have included the recognition that the ACC cannot be
 68 considered independent of the depth of the global pycnocline and the merid-
 69 ional overturning circulation (Gnanadesikan, 1999; Gnanadesikan and Hallberg,
 70 2000). The implication is that the ACC volume transport is influenced not only
 71 by Southern Ocean wind forcing and eddies, but also the rate of North Atlantic
 72 Deep Water formation (Fučkar and Vallis, 2007), buoyancy forcing (Hogg, 2010)
 73 and global diapycnal mixing (Munday et al., 2011).

74 Finally, it is important to emphasize that the ACC volume transport exhibits
 75 far less sensitivity to the surface wind stress in models with explicit, rather than
 76 parameterized, eddies, both in equilibrium (Hallberg and Gnanadesikan, 2001;
 77 Tansley and Marshall, 2001b; Munday et al., 2013) and during its adjustment
 78 (Hallberg and Gnanadesikan, 2006; Hogg and Blundell, 2006; Meredith and
 79 Hogg, 2006; Farneti et al., 2010; Farneti and Delworth, 2010). This behavior was
 80 first predicted by Straub (1993) on theoretical grounds and has become known
 81 as “eddy saturation”. Notwithstanding the importance of explicitly resolving
 82 eddies, it is important to understand the dynamics of the ACC in models with
 83 parameterized eddies, not least because such parameterizations will continue to
 84 be used in many climate models for the foreseeable future. Moreover, we have
 85 little chance of understanding the dynamics of the ACC with explicit, turbulent
 86 eddies if we cannot first understand the dynamics of a quasi-laminar ACC in a
 87 model with parameterized eddies.

88 The goal of this contribution is to develop a simple reduced-gravity model
 89 of the ACC that can be used to address three complementary questions:

- 90 • How does the volume transport of the ACC vary as the latitude of wind
 91 stress forcing is varied?
- 92 • Which dynamical processes control the equatorward and poleward excur-
 93 sions of the ACC?
- 94 • Can the volume transport of the ACC be predicted from the surface wind
 95 stress and model parameters?

96 The advantage of using a reduced-gravity model is that it is the simplest model
 97 that can represent each of the most important elements one might wish to
 98 include in a simple theory of the ACC: (i) wind forcing; (ii) basin geometry

99 with partial circumpolar connection; (iii) stratification; (iv) (parameterized)
 100 geostrophic eddy fluxes; (v) surface cooling (through imposed layer outcrop-
 101 ping). Inevitably, a simple model cannot capture every important process and
 102 perhaps the most important processes missing from the present model are ex-
 103 plicit geostrophic eddies, variable bottom topography and a realistic represen-
 104 tation of buoyancy forcing; some likely impacts of these neglected processes are
 105 outlined in the concluding discussion.

106 The model developed here turns out to bear many similarities to the linear
 107 barotropic model derived by Gill (1968), with differences arising through non-
 108 linearity in our equations, boundary conditions, and physical interpretations
 109 of model parameters. Thus, a parallel goal of this contribution is to cast Gill
 110 (1968) in the language of contemporary descriptions of the ACC dynamics and
 111 thereby restore it to the center-stage of theoretical understanding of the ACC.

112 The manuscript is structured as follows. In section 2 we describe the formu-
 113 lation of our model and its relation to Gill (1968). In section 3, the suites of
 114 model calculations are summarized. In section 4, we describe the lateral struc-
 115 ture of a typical model solution and its physical interpretation. In section 5
 116 we investigate how the structure of the solution varies as the wind jet is moved
 117 northward. In section 6 we investigate the extent to which the volume trans-
 118 port through the model Drake Passage can be predicted by integrating the wind
 119 stress over the circumpolar streamlines following the suggestion of Allison et al.
 120 (2010). Finally, a concluding discussion is given in section 7.

121 2. Model formulation

122 2.1. Equations of motion

123 We consider a reduced-gravity model of the Antarctic Circumpolar Current,
 124 forced by surface wind stress. For analytical convenience, we work with a Carte-
 125 sian coordinate system (x, y) on the β plane where x and y are the zonal and
 126 meridional coordinates. The domain extends from $(0, 0)$ to (x_0, y_0) , with a re-
 127 entrant ‘‘Drake Passage’’ between $y = 0$ and $y = y_0/4$. We set $x_0 = 20\,000$ km
 128 and $y_0 = 4\,000$ km, giving a model Drake Passage of width 1 000 km, as sketched
 129 in Fig. 1. The lower, abyssal layer is considered at rest, but plays an important
 130 implicit role in dissipating zonal momentum, transferred downward from the
 131 upper layer through the eddy form stress, across the bottom topography within
 132 the model Drake Passage.

133 We assume the Rossby number is sufficiently small that inertia can be ne-
 134 glected and the equilibrium momentum equation written:

$$f\mathbf{k} \times \mathbf{u} + g_r \nabla h = \frac{\tau_s}{\rho_0 h} - \frac{rg_r}{f} \mathbf{k} \times \nabla h, \quad (2.1)$$

135 where the right-hand side of (2.1) includes a linear drag proportional to the
 136 geostrophic velocity. Here $f = f_0 + \beta y$ is the Coriolis parameter where f_0 is the
 137 Coriolis parameter at the southern boundary and β is its meridional gradient,
 138 \mathbf{k} is the unit vertical vector, \mathbf{u} is the lateral velocity, g_r is the reduced gravity,

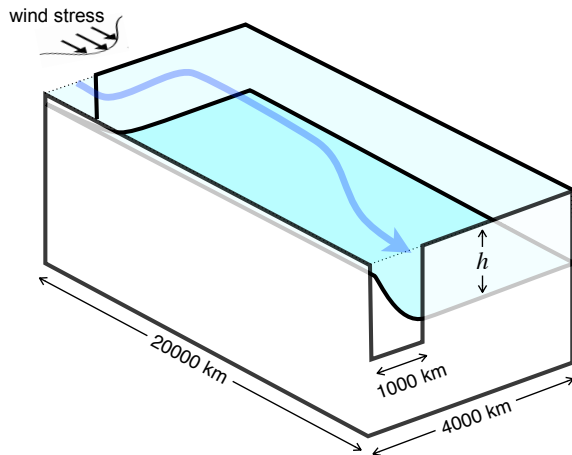


Figure 1: Schematic diagram illustrating the model formulation and domain. Flow is confined to a reduced-gravity layer (shaded) overlaying a motionless abyss. The two layers are separated by a “pycnocline” of depth h , across which the density increases abruptly. The upper layer is forced by a prescribed surface wind stress. A re-entrant channel occupies the most southerly quarter of the domain. The model dimensions are indicated on the figure.

139 h is the layer thickness, τ_s is the surface wind stress, ρ_0 is a reference density
 140 and r is the linear drag coefficient. The linear drag is required to satisfy the no-
 141 normal flow boundary condition in the presence of along-shore pressure (layer
 142 thickness) variations, the latter being an essential element of the solutions as
 143 we shall see in section 4.

144 In addition, the flow satisfies a continuity equation,

$$\nabla \cdot (h\mathbf{u} - \kappa_{gm}\nabla h) = -\Gamma, \quad (2.2)$$

145 where the second term in (2.2) represents the Gent and McWilliams parameteri-
 146 zation of the eddy bolus transport, $\bar{h}\mathbf{u}^* \equiv \bar{h}'\mathbf{u}' = -\kappa_{gm}\nabla h$, where overbars and
 147 primes denote time-mean and time-varying components and κ_{gm} is the eddy
 148 diffusivity (Gent and McWilliams, 1990; Gent et al., 1995). Note that $\bar{h}\mathbf{u}^*$
 149 is proportional to the eddy form stress and can therefore also be interpreted as
 150 transferring zonal momentum downward from the upper to lower layer (e.g.,
 151 see the discussions in Hughes, 1997; Olbers, 1998). The term on the right-hand
 152 side represent “buoyancy forcing” and is included both to prevent the layer
 153 thickness from becoming any smaller than a prescribed minimum value and to
 154 impose that the layer outcrops, at the southern boundary, otherwise Γ is set to
 155 zero;

156 Boundary conditions on the lateral and northern boundaries are no normal
 157 flow and $\kappa_{gm} = 0$ to ensure no normal eddy bolus transport. The wind forcing
 158 is chosen to be zonal, $\tau_s = \tau_s(y)\mathbf{i}$, where \mathbf{i} is the unit vector in the x direction;
 159 τ_s vanishes along all zonal boundaries such that $\mathbf{n} \cdot \mathbf{k} \times \tau_s = 0$ where \mathbf{n} is a unit

160 vector normal to the boundary. With this simplification, the no-normal flow
161 condition can be written as:

$$\mathbf{n} \cdot \{f\mathbf{k} \times \nabla h - r\nabla h\} = 0. \quad (2.3)$$

162 On the southern boundary we set $h = h_0$, where h_0 is a small value (10 m in
163 the solutions shown) as a simple parameterization of buoyancy loss. We also set
164 $h = h_0$ on any points where the solution would otherwise give a smaller value
165 of h , i.e., points that might be considered “outcropped”; this is equivalent to
166 introducing an additional volume source at such points through the term Λ in
167 (2.2), equivalent to buoyancy gain.

168 Equations (2.1) and (2.2) combine to give a single elliptic equation for the
169 layer thickness:

$$-c \frac{\partial h}{\partial x} = \nabla \cdot \{(\kappa_{gm} + c\delta_s) \nabla h\} - w_{ek} - \Gamma \quad (2.4)$$

A B C D

170 where

$$c(h) = \frac{\beta g_r h}{f^2} \quad (2.5)$$

171 is the long Rossby wave speed, $\delta_s = r/\beta$ is the Stommel boundary layer width
172 (Stommel, 1948), and $w_{ek} = \mathbf{k} \cdot \nabla \times (\boldsymbol{\tau}_s / \rho_0 f)$ is the Ekman upwelling velocity
173 (Ekman, 1905).

174 Equation (2.4) is an advection-diffusion equation containing a westward
175 Rossby advection term (A), a nonlinear diffusion term involving both geostrophic
176 eddy fluxes and linear drag (B), forcing by the Ekman upwelling velocity (C),
177 and buoyancy forcing (D). This advection diffusion equation is proportional to
178 the linear vorticity balance for the upper layer, analogous to the linear vorticity
179 equation in Stommel’s models of wind-driven gyres Stommel (1948) and ACC
180 Stommel (1957). Balances between different combinations of the terms in this
181 equation correspond to different limiting dynamical regimes:

- 182 • non-acceleration conditions (terms B and C, neglecting the linear drag by
183 setting $\delta_s = 0$);
- 184 • Sverdrup balance (terms A and C);
- 185 • Stommel western boundary current (terms A and B, with the boundary
186 layer width set by eddy diffusion).

187 Thus, the model seems ideally suited to resolving the relative importance of
188 eddy dynamics, Sverdrup dynamics and western boundary currents in setting
189 the lateral structure and strength of the ACC.

190 *2.2. Relation to Gill (1968)*

191 Equation (2.4) is virtually identical to (2.6) of Gill (1968) for a flat-bottomed,
192 barotropic ocean, except that:

- 193 • Gill solves for the barotropic streamfunction in (2.6) whereas we solve
194 for the pycnocline depth, h , in (2.4), from which the depth-integrated
195 circulation can be inferred using (2.1);
- 196 • (2.4) is nonlinear since the long Rossby speed, c , is proportional to the
197 layer thickness;
- 198 • the boundary condition (2.3) involves a linear combination of normal and
199 tangential gradients whereas a Dirichlet boundary condition is applied in
200 Gill (1968);
- 201 • the inclusion of buoyancy forcing, Γ , on the right-hand side of (2.4), to
202 allow for outcropping at the southern margin of the domain;
- 203 • the linear drag coefficient in Gill is replaced by

$$r^* = r + \frac{\beta \kappa_{gm}}{c}, \quad (2.6)$$

204 where the latter eddy diffusion term dominates in our model;

- 205 • κ_{gm} is tapered to zero at the boundaries in order to ensure no normal
206 eddy bolus transport.

207 Thus, the present model might be interpreted as Gill (1968) after a “makeover”
208 to bring it up-to-date with contemporary descriptions of ACC dynamics involv-
209 ing eddy bolus fluxes and the pycnocline depth. Despite the differences between
210 the two models, their solutions have a lot in common.

211 **3. Model calculations**

212 Equilibrium solutions to (2.1-2.3) are obtained through a simple relaxation
213 method. The grid spacing is 50 km in the basin interior, but decreases in x near
214 the meridional boundaries to enhance resolution within the boundary layers,
215 the finest grid spacing being 0.9 km adjacent to the boundaries. Details of the
216 numerical method are given in the appendix.

217 The wind stress has the same generic spatial profile:

$$\tau_s^{(x)} = \begin{cases} \tau_0 \sin^2 \left(\pi \frac{y - y_s}{y_n - y_s} \right) & \text{if } y_s \leq y \leq y_n; \\ 0 & \text{otherwise.} \end{cases} \quad (3.1)$$

218 However, the latitudinal extent and strength of the wind is varied through the
219 parameters τ_0 , y_s and y_n , as summarized in Table 1. The calculations are clus-
220 tered into sets in which the wind stress profile has widths of $y_0/4$, $y_0/2$, $3y_0/4$

221 and y_0 (recall that the Drake Passage width is $y_0/4$ and the overall basin width
 222 y_0). The wind stress profiles are, in turn, shifted northward across different
 223 starting latitudes as space allows, and four different wind strengths are em-
 224 ployed. While the largest wind stress of 0.4 N m^{-2} is stronger than in reality,
 225 some of the wind profiles are unrealistically narrow in order to isolate the effect
 226 of shifting the latitude of the wind jet. Hence the stronger wind stress is re-
 227 quired to maintain a realistic overall momentum input and circumpolar volume
 228 transport. The calculations are labelled “Wsn τ ” where s and n are y_s and y_n in
 229 10^3 km from the southern boundary, and τ indicates the maximum wind stress
 230 in 0.1 N m^{-2} (except 0 is used for $\tau = 0.05 \text{ N m}^{-2}$).

231 In each experiment, the layer thickness is pinned to $h_0 = 10 \text{ m}$ on the south-
 232 ern boundary, representing the effect of buoyancy loss in outcropping the pycn-
 233 ocline. In most cases, the Gent and McWilliams eddy diffusivity and linear drag
 234 coefficients have control values of $1000 \text{ m}^2 \text{ s}^{-1}$ and 10^{-7} s^{-1} respectively, except
 235 that the eddy diffusivity is scaled to zero adjacent to the western, eastern and
 236 northern boundaries over the Stommel boundary layer scale,

$$\kappa_{gm} = \kappa_{gm0}(1 - e^{\beta x/r}), \text{ etc.} \quad (3.2)$$

237 in order to ensure no normal eddy bolus transport. This choice is fairly ad-hoc,
 238 but does not appear critical as long as the tapering scale is significantly shorter
 239 than the overall width of the boundary layer, κ_{gm}/c (see section 4.3). Ensuring
 240 that these nested boundary layers are well resolved is the primary motivation for
 241 enhancing zonal resolution adjacent to the western (and eastern) boundaries.
 242 Four additional calculations are reported in which the Gent and McWilliams
 243 eddy diffusivity is increased and decreased by a factor of 2, and the linear drag
 244 coefficient is increased by factors of 3 and 10, about the calculation W022; these
 245 are indicated by suffixes K-, K+, R+, R++ respectively.

246 The equilibrium layer thickness at the northern edge of Drake Passage and
 247 the Drake Passage volume transport are listed in the final two columns of Table
 248 1. In the following sections, we discuss the lateral structure of a typical solution,
 249 sensitivity of the solution to the latitude of the wind jet, and the relation of the
 250 Drake Passage volume transport to the surface wind stress.

251 4. Lateral structure of a typical solution

252 In this section, we discuss the lateral structure of a typical solution, W042,
 253 through reference to the diffusive Rossby wave equation (2.4). As indicated in
 254 Table 1, the solution has a fairly realistic, basin-wide wind forcing: $y_s = 0$,
 255 $y_n = y_0$ in (3.1) with $\tau_0 = 0.2 \text{ N m}^{-2}$.

256 Plotted in Fig. 2 are: the layer thickness, h ; the transport streamfunction,
 257 ψ ; the Ekman upwelling, w_{ek} ; the eddy-induced upwelling,

$$w_{eddy} = -\nabla \cdot (\kappa_{gm} \nabla h); \quad (4.1)$$

258 the sum of the “geostrophic” upwelling (equivalent to planetary vorticity advec-
 259 tion),

$$w_{geos} = -c \partial h / \partial x, \quad (4.2)$$

name	wind (km)	latitude	τ_0 ($N m^{-2}$)	κ_{GMO} ($m^2 s^{-1}$)	r (s^{-1})	h_{dp} (m)	T_{dp} (Sv)
W010	0-1000		0.05	1000	1×10^{-7}	229	2
W011	0-1000		0.1	1000	1×10^{-7}	444	9
W012	0-1000		0.2	1000	1×10^{-7}	864	35
W014	0-1000		0.4	1000	1×10^{-7}	1662	128
W120	1000-2000		0.05	1000	1×10^{-7}	214	2
W121	1000-2000		0.1	1000	1×10^{-7}	415	9
W122	1000-2000		0.2	1000	1×10^{-7}	778	31
W124	1000-2000		0.4	1000	1×10^{-7}	1406	101
W230	2000-3000		0.05	1000	1×10^{-7}	231	3
W231	2000-3000		0.1	1000	1×10^{-7}	414	9
W232	2000-3000		0.2	1000	1×10^{-7}	713	27
W234	2000-3000		0.4	1000	1×10^{-7}	1179	72
W340	3000-4000		0.05	1000	1×10^{-7}	300	5
W341	3000-4000		0.1	1000	1×10^{-7}	479	13
W342	3000-4000		0.2	1000	1×10^{-7}	750	30
W344	3000-4000		0.4	1000	1×10^{-7}	1194	75
W020	0-2000		0.05	1000	1×10^{-7}	423	9
W021	0-2000		0.1	1000	1×10^{-7}	806	33
W022	0-2000		0.2	1000	1×10^{-7}	1507	114
W024	0-2000		0.4	1000	1×10^{-7}	2743	375
W130	1000-3000		0.05	1000	1×10^{-7}	381	8
W131	1000-3000		0.1	1000	1×10^{-7}	671	24
W132	1000-3000		0.2	1000	1×10^{-7}	1136	67
W134	1000-3000		0.4	1000	1×10^{-7}	1852	176
W240	2000-4000		0.05	1000	1×10^{-7}	388	8
W241	2000-4000		0.1	1000	1×10^{-7}	622	21
W242	2000-4000		0.2	1000	1×10^{-7}	970	50
W244	2000-4000		0.4	1000	1×10^{-7}	1477	114
W030	0-3000		0.05	1000	1×10^{-7}	533	15
W031	0-3000		0.1	1000	1×10^{-7}	947	46
W032	0-3000		0.2	1000	1×10^{-7}	1634	136
W034	0-3000		0.4	1000	1×10^{-7}	2748	383
W140	1000-4000		0.05	1000	1×10^{-7}	472	12
W141	1000-4000		0.1	1000	1×10^{-7}	770	31
W142	1000-4000		0.2	1000	1×10^{-7}	1219	78
W144	1000-4000		0.4	1000	1×10^{-7}	1877	182
W040	0-4000		0.05	1000	1×10^{-7}	578	18
W041	0-4000		0.1	1000	1×10^{-7}	964	48
W042	0-4000		0.2	1000	1×10^{-7}	1568	127
W044	0-4000		0.4	1000	1×10^{-7}	2501	320
W022K-	0-2000		0.2	500	1×10^{-7}	2425	292
W022K+	0-2000		0.2	2000	1×10^{-7}	836	35
W022R+	0-2000		0.2	1000	3×10^{-7}	1386	95
W022R++	0-2000		0.2	1000	10×10^{-7}	1112	61

Table 1: Summary of the model calculations. The final two columns show equilibrium values of the layer thickness at the northern tip of, and the volume transport through, the model Drake Passage.

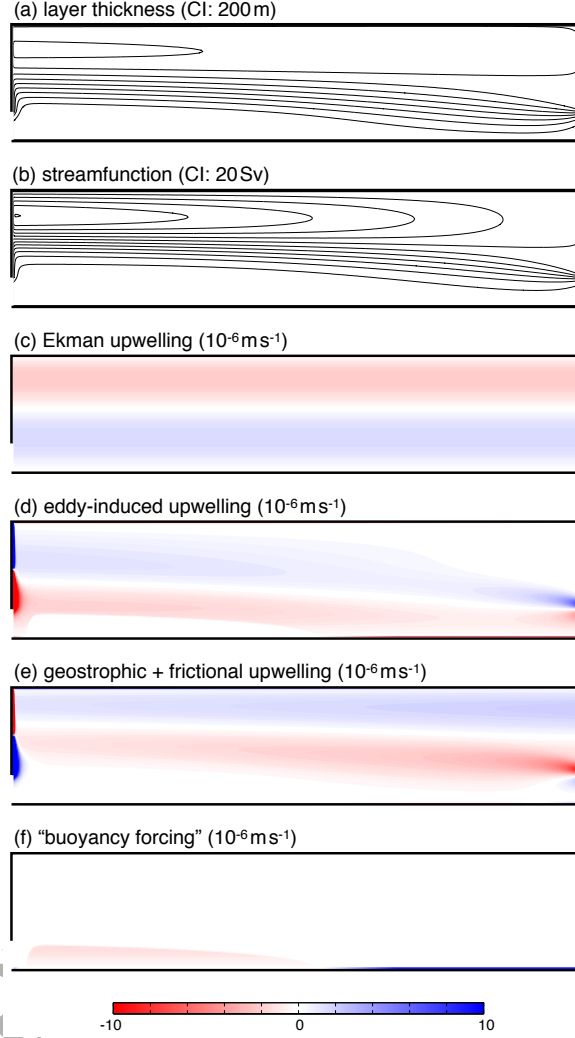


Figure 2: Lateral structure of solution W042. Plotted are: (a) the layer thickness, h (contour interval 200 m, increasing northward from $h_0 = 10$ m on the southern boundary); (b) the transport streamfunction, ψ , as defined in (4.5) (contour interval 20 Sv); (c) the Ekman upwelling, w_{ek} ; (d) the eddy-induced upwelling, w_{eddy} , as defined in (4.1); (e) the sum of the geostrophic and frictional upwellings, $w_{geos} + w_{fric}$, as defined in (4.2) and (4.3); (f) “buoyancy forcing” Γ . Panels (c) - (f) are shaded in units of 10^{-6} m s^{-1} . Red shading corresponds to negative values, i.e., processes that deepen the pycnocline or warm the ocean; blue shading corresponds to positive values, i.e., processes that shallow the pycnocline or cool the ocean.

260 and “frictional” upwelling (equivalent to the frictional vorticity sink),

$$w_{fric} = -\nabla \cdot (c\delta_s \nabla h); \quad (4.3)$$

261 and the “buoyancy forcing”, Γ . The latter five quantities correspond to the
 262 terms in the elliptic equation (2.4), defined such that

$$w_{ek} + w_{eddy} + w_{geos} + w_{fric} + \Gamma = 0. \quad (4.4)$$

263 Red shading corresponds to negative values, i.e., processes that deepen the
 264 pycnocline or warm the ocean; blue shading corresponds to positive values, i.e.,
 265 processes that shallow the pycnocline or cool the ocean. The geostrophic and
 266 frictional upwellings are combined because they are calculated jointly in the
 267 numerical code (see Appendix).

268 The transport streamfunction is defined such that

$$h\mathbf{u} - \kappa_{gm}\nabla h = \mathbf{k} \times \nabla\psi \quad (4.5)$$

269 where $h\mathbf{u}$ includes the Ekman transport velocity and it is implicitly assumed
 270 that buoyancy forcing is negligible. In practice, buoyancy forcing mostly occurs
 271 south of the model ACC jet and thus we calculate ψ by integrating the zonal
 272 component of (4.5) southward from the northern boundary; this means that
 273 streamfunction values south of any buoyancy forcing are degenerate. (We did
 274 consider first decomposing the depth-integrated transport into rotational and
 275 divergent components. However, in practice the latter component is small and
 276 has little discernible effect on the structure of any of the streamfunction fields
 277 plotted in this manuscript.)

278 The solution consists of a circumpolar current with a volume transport of
 279 127 Sv and a subtropical “supergyre” (cf. Ridgway and Dunn, 2007) with a
 280 volume transport of 101 Sv. The layer thickness has its minimum allowed value
 281 of 10 m at the southern boundary and in an outcropped region in the southwest
 282 of the domain. The latter is most easily identified by the positive “buoyancy
 283 forcing” in Fig. 2(f). The layer thickness has a value of 1568 m at the northern
 284 tip of the model Drake Passage, and reaches a maximum of 1843 m at the center
 285 of the supergyre.

286 Physically, it is easiest to interpret the solution for the circumpolar current
 287 by tracing its path backwards from the model Drake Passage. The following
 288 discussion closely follows that of Gill (1968) (sections 3-5); the reader is also
 289 referred to de Ruijter (1980) for further discussion.

290 4.1. Diffusive jet regime

291 First we start with the flow immediately upstream of Drake Passage. An
 292 expanded view of the eddy upwelling, geostrophic plus frictional upwelling and
 293 layer thickness contours is shown in Fig. 3. In this region, the elliptic equation
 294 (2.4) is well approximated by

$$-c \frac{\partial h}{\partial x} \approx \frac{\partial}{\partial y} \left(\kappa_{gm} \frac{\partial h}{\partial y} \right). \quad (4.6)$$

295 where the left-hand side of (4.6) is the Lagrangian rate of change of h following
 296 a Rossby wave trajectory. Treating κ_{gm} and c as a constant (in practice c is a

297 linear function of h), (4.6) can be differentiated with respect to y to give the
 298 same equation for the gradient,

$$-c \frac{\partial}{\partial x} \left(\frac{\partial h}{\partial y} \right) \approx \kappa_{gm} \frac{\partial^2}{\partial y^2} \left(\frac{\partial h}{\partial y} \right); \quad (4.7)$$

299 this is the standard equation for diffusion of a tracer from an initial point source.
 300 The solution, easily confirmed by direct substitution, is

$$\frac{\partial h}{\partial y} \propto \sqrt{\frac{c}{4\pi\kappa_{gm}(x_0-x)}} \exp \left\{ \frac{c(y-y_{dp})^2}{4\pi\kappa_{gm}(x_0-x)} \right\}, \quad (4.8)$$

301 where $y_{dp} = y_0/4$ is the value of y at the northern tip of Drake Passage. Finally,
 302 (4.8) can be integrated across the jet to give the solution for the layer thickness,

$$h \approx h_0 + \frac{\Delta h}{2} \left(1 + \operatorname{erf} \left\{ \sqrt{\frac{c}{4\pi\kappa_{gm}(x_0-x)}} (y-y_{dp}) \right\} \right), \quad (4.9)$$

303 where $\operatorname{erf}\{\dots\}$ is the error function (e.g., page 297, Gautschi, 1964).

304 Taking the argument of the error function to be ± 1 allows us to estimate
 305 the width of the jet, Δy , as the spacing between the contours $h = h_0 + 0.08\Delta h$,
 306 $h_0 + 0.92\Delta h$:

$$\Delta y \approx 4 \sqrt{\frac{\kappa_{gm}(x_0-x)}{c}}. \quad (4.10)$$

307 Putting in typical values of $c \approx 2 \times 10^{-2} \text{ m s}^{-1}$, appropriate with $h \approx 10^3 \text{ m}$
 308 and $f = 10^{-4} \text{ s}^{-1}$ at the latitude of the model Drake Passage, $\kappa_{gm} = 10^3 \text{ m}^2 \text{ s}^{-1}$
 309 and $(x_0-x) = 10^6 \text{ m}$ gives $\Delta y \approx 9 \times 10^5 \text{ m}$, broadly consistent with the rapid
 310 broadening of the jet upstream of the model Drake Passage in Fig. 2(a). At
 311 a more detailed level, it is also evident that the jet broadens over a shorter
 312 distance upstream of the model Drake Passage to the south, consistent with the
 313 reduction of the Rossby speed, c , with decreasing layer thickness.

314 Broadening of the ACC upstream of Drake Passage is realistic (see, e.g., the
 315 observation-constrained Southern Ocean State Estimate of Mazloff et al., 2010),
 316 but whether this is for the correct reasons in the present model will required more
 317 detailed investigation, not least because Rossby wave propagation is eastward,
 318 rather than westward, in the ACC due to Doppler-shifting by the depth-mean
 319 flow (Klocker and Marshall, 2014).

320 4.2. Basin interior

321 Away from the boundaries, the circumpolar current satisfies an approximate
 322 three-way balance in (2.4) involving Ekman upwelling, and eddy-induced and
 323 geostrophic downwelling (Fig. 2). This is equivalent to a modified Sverdrup
 324 balance,

$$\beta v h \approx f(w_{ek} + w_{eddy}), \quad (4.11)$$

325 including the compensating effect of eddies on the net upwelling. Thus, the so-
 326 lution shows elements of both the first and second limiting paradigms discussed

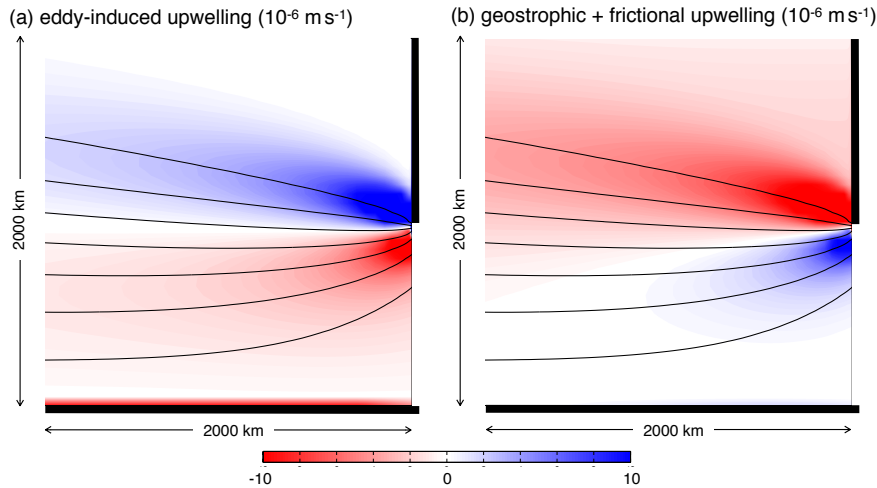


Figure 3: Expanded view of the dynamical balance in the region immediately upstream of the model Drake Passage in solution W042. Shading shows (a) the eddy-induced upwelling, and (b) the sum of the geostrophic and frictional upwellings, $w_{geos} + w_{fric}$ (units: 10^{-6} m s^{-1}). Superimposed on each are layer thickness contours with a contour interval of 200 m (the southernmost contour being the 200 m contour).

327 in section 1, with the Ekman and eddy-induced vertical velocities partially com-
 328 pensating, but a residual between the two allowing fluid columns to deflect pole-
 329 ward as they travel along the circumpolar current through a modified Sverdrup
 330 balance. We defer further discussion of the role of Sverdrup balance in setting,
 331 or otherwise, the volume transport of the circumpolar current until section 6.

332 4.3. Western boundary current

333 In the western boundary current, but outside the frictional sublayer within
 334 which $\kappa_{gm} \rightarrow 0$, the elliptic equation (2.4) is well approximated by

$$-c \frac{\partial h}{\partial x} \approx \kappa_{gm} \frac{\partial^2 h}{\partial x^2}. \quad (4.12)$$

335 The solution is the well-known Stommel (1948) western boundary current, but
 336 with the width of the boundary current set by the Gent and McWilliams eddy
 337 diffusivity,

$$\delta_{wbc} \sim \frac{c}{\kappa_{gm}}. \quad (4.13)$$

338 Taking $c \approx 2 \times 10^{-2} \text{ m s}^{-1}$ and $\kappa_{gm} = 10^3 \text{ m}^2 \text{ s}^{-1}$ gives $\delta_{wbc} \sim 50 \text{ km}$. In
 339 contrast, the Stommel boundary layer width, $\delta_s = r/\beta = 5 \text{ km}$, an order of
 340 magnitude smaller. A similar result has been previously obtained and discussed
 341 by Eden and Olbers (2010).

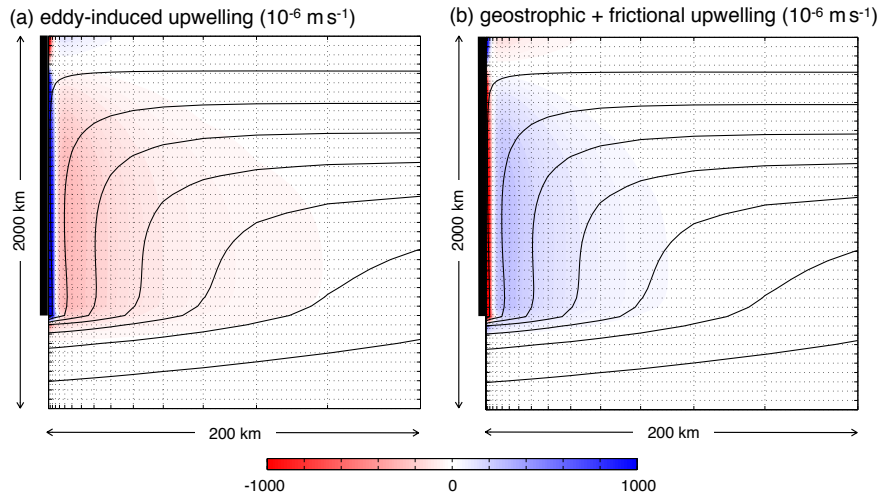


Figure 4: Expanded view of the dynamical balance in the western boundary current of the circumpolar current in solution W042. Note that the zonal dimension is expanded by a factor 10 more than the meridional dimension. Shading shows (a) the eddy-induced upwelling, and (b) the sum of the geostrophic and frictional upwellings, $w_{geos} + w_{fric}$ (units: 10^{-6} m s^{-1} ; note that the color scale is for values 100 times larger than in previous figures). Superimposed on each are layer thickness contours with a contour interval of 200 m (the southernmost contour being the 200 m contour). Also indicated by tick marks and dotted lines is the model grid, indicating the increase in resolution in the zonal direction towards the boundary.

342 An expanded view of the eddy upwelling, geostrophic plus frictional up-
 343 welling and layer thickness contours is shown in Fig. 4; the zonal scale is
 344 magnified by an order of magnitude relative to the meridional scale in order
 345 to reveal the balances adjacent to the solid boundary. The western boundary
 346 current width is in accord with the approximate balance (4.12), within which
 347 there is eddy-induced downwelling due to the convergence of the eddy thickness
 348 fluxes which decay with x . However, there is a narrow region adjacent to the
 349 boundary, of width set by the Stommel boundary layer thickness, in which there
 350 is intense eddy-induced upwelling due to the imposed vanishing of the eddy bo-
 351 lus transport at the solid boundary. However, the details of the width of this
 352 layer of eddy-induced upwelling appear to be of secondary importance to the
 353 overall structure of the solution, as long as it is a small fraction of the overall
 354 width of the boundary current (not shown).

355 4.4. Outcropping and the residual circulation

356 There is a region in the southwestern corner of Fig 2(f) in which the net
 357 upwelling does not vanish. This corresponds to a region in which the layer is
 358 outcropped, analogous to the separated region in Fig. 3(d) of Gill (1968). In
 359 this outcropped region, the eddy-induced, geostrophic and frictional upwellings
 360 all vanish and hence the Ekman upwelling can only be balanced by positive

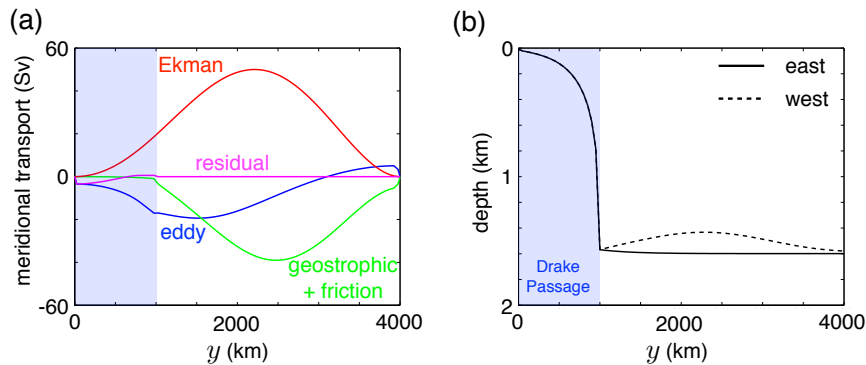


Figure 5: (a) Net northward volume transports in solution W042, decomposed into Ekman (red), eddy (blue), and geostrophic plus frictional components (green); also shown is the residual volume transport (magenta). (b) Variation of the layer thickness, h , with meridional distance, y , along the eastern (solid lines) and western (dashed lines) boundaries in solution W042; within the model Drake Passage, the eastern and western values are equal by definition.

361 “buoyancy forcing”, equivalent to heating, in order to balance the cooling effect
 362 of the upwelling.

363 However, the net “buoyancy forcing” integrated over the entire domain must
 364 vanish to preserve thermodynamic equilibrium. The positive buoyancy forcing
 365 (warming) in the outcropped region is balanced by a narrow strip of intense,
 366 negative buoyancy forcing (cooling) along the southeastern boundary where we
 367 impose that the layer thickness is set to h_0 and there is strong convergence of the
 368 eddy bolus transport, the latter being most easily seen adjacent to the southern
 boundary in Fig. 3(a) but also visible in Figs. 2(d) and (f).

370 Associated with the buoyancy forcing is a water mass transformation, from
 371 the abyssal to surface layer in the outcropped region, and from the surface to
 372 abyssal layer along the south-eastern boundary. In Fig. 5(a), we plot the net
 373 meridional volume transport as a function of latitude in the layer. We indeed see
 374 a residual southward transport across the circumpolar current, strength 3.5 Sv;
 375 while small, it is interesting that the model appears to produce what might
 376 be interpreted as Antarctic Bottom Water along the southern boundary of the
 377 domain, as well as residual upwelling within the core of the circumpolar current,
 378 as an intrinsic part of the solution; this is discussed further in section 7.

379 4.5. Zonal momentum budget

380 Finally we briefly discuss the zonal momentum budget, equivalent to the
 381 meridional volume transport budget shown in Fig. 5(a), after rearranging the
 382 zonal component of the momentum equation (2.1) for v , multiplying by h and
 383 integrating zonally (also see Olbers, 1998).

384 Over the circumpolar latitudes, the Ekman and eddy-induced meridional
 385 volume transports balance to leading order, equivalent to a balance between the

386 surface wind stress and eddy form stress as assumed by Johnson and Bryden
 387 (1989). The slight imbalance is due to the residual southward volume transport
 388 across the circumpolar current, already discussed in section 4.4, and an even
 389 smaller contribution from friction.

390 North of the model Drake Passage, the eddy-induced volume transport con-
 391 tinues to compensate for the Ekman transport, but there is an increasingly large
 392 contribution from the geostrophic transport, equivalent to an east-west pressure
 393 gradient. The origin of this pressure gradient is clear from Fig. 5(b) in which
 394 the layer thickness is shown along $x = 0$ and $x = x_0$, corresponding to the west-
 395 ern and eastern boundaries. Within the circumpolar latitudes, the western and
 396 eastern layer thicknesses are equal, by definition, but further north the layer
 397 thickness, and hence pressure, drops along the western boundary, whereas it
 398 is nearly constant along the eastern boundary. This basin-wide zonal pressure
 399 has an impact on the volume transport of the circumpolar current, as we shall
 400 discuss further in section 6.

401 5. Sensitivity to latitude of the wind jet

402 In this section, we focus on the sensitivity of the solution to the latitude of
 403 the wind jet by discussing the four solutions W014, W124, W234 and W344
 404 (Figs 6-9). While the wind jet is unrealistically narrow in these solutions, this
 405 has the advantage of isolating the effect of wind forcing in different parts of
 406 the basin and, in particular, the role played by Sverdrup balance in setting the
 407 lateral structure and strength of the circumpolar current. The magnitude of
 408 the maximum wind stress is relatively large in each of these experiments, at
 409 0.4 N m^{-2} , but we justify this value by noting that momentum is transferred
 410 to the ocean over a restricted latitude band; for example, the net momentum
 411 input is half that in the solution W022 discussed in section 4.

412 5.1. Lateral structure

413 In the first solution, W014 (Fig. 6), the wind forcing is confined to the
 414 latitude band of the model Drake Passage. The solution corresponds almost
 415 exactly to the first paradigm discussed in section 1 due to Johnson and Bryden
 416 (1989), with pointwise compensation between the Ekman and eddy-induced
 417 upwellings. The slight imbalance is due to the frictional upwelling (indeed, if
 418 the eddy transfer coefficient is reinterpreted as $\kappa_{gm} + c\delta_s$, then the compensation
 419 is virtually exact). Note that there is no outcropping of the layer except on the
 420 southern boundary where this is imposed through the boundary condition.

421 In the second solution, W124 (Fig. 7), the wind forcing is entirely to the
 422 north of the model Drake Passage. Nevertheless, the dominant balance over
 423 most of the basin remains between the Ekman and eddy-induced upwellings,
 424 with weaker contribution from the geostrophic upwelling (and to a lesser ex-
 425 tent, the frictional upwelling). The slight reduction in the eddy-induced up-
 426 welling compared with solution W014 (evident from the larger contribution
 427 from geostrophic upwelling in Fig. 7(e)) means that the layer interface slopes

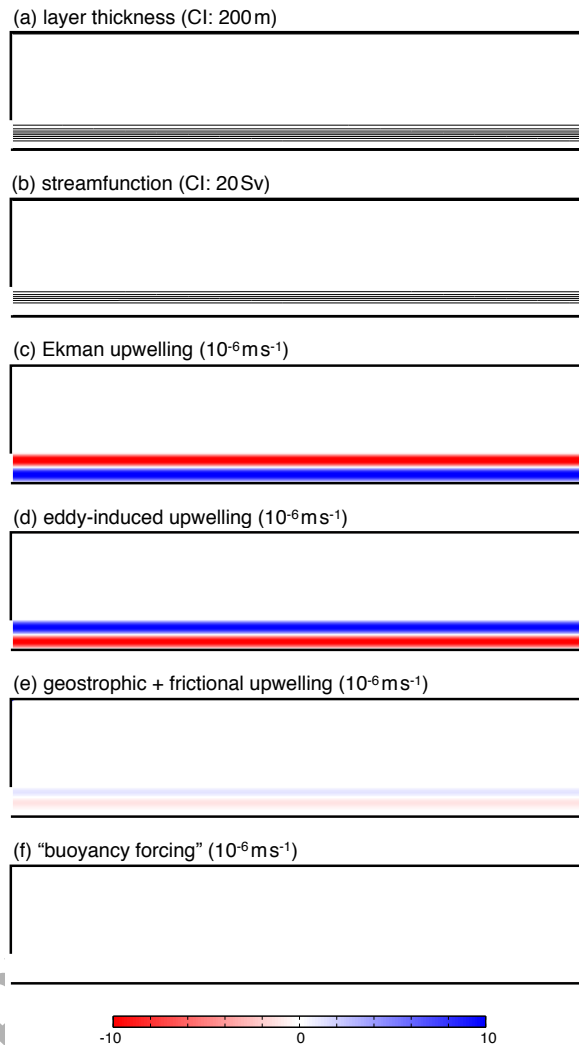


Figure 6: Lateral structure of solution W014. The plotted fields are as in Fig. 2.

428 less steeply in solution W124, leading to a slightly weaker circumpolar volume
 429 transport through thermal wind balance. Note also that the layer outcrops
 430 over a narrow band at the southernmost tip of the prescribed Ekman upwelling
 431 (south of this strip, the layer is close to, but not quite, outcropped). As dis-
 432 cussed in section 4.4, this outcropping is required in order to balance the net
 433 eddy-induced upwelling at the southern boundary.

434 However, the most important result of the second and remaining solutions
 435 is that Sverdrup balance does not set the volume transport through Drake Pas-

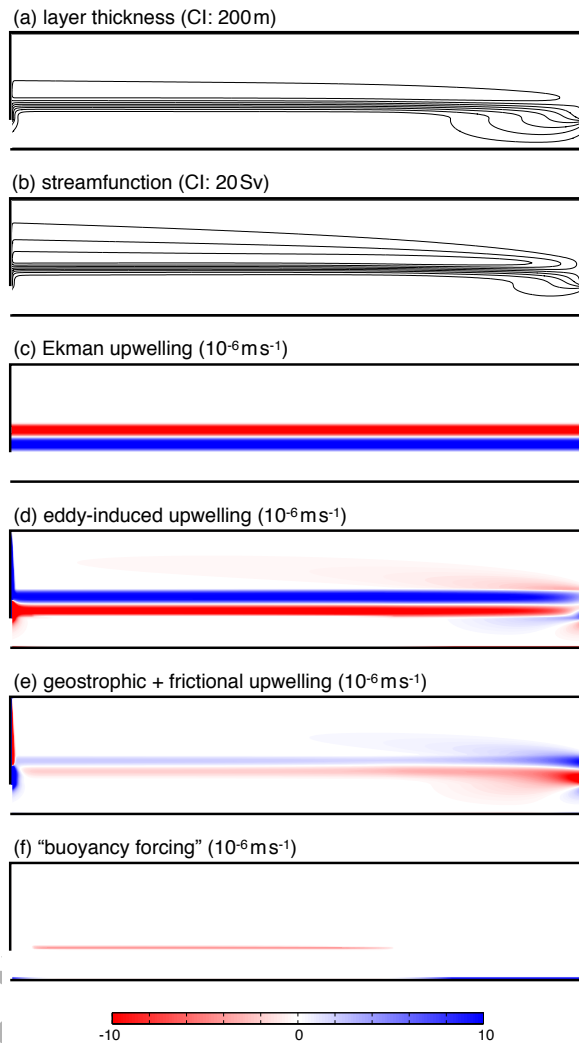


Figure 7: Lateral structure of solution W124. The plotted fields are as in Fig. 2.

436 sage as proposed by Stommel (1957). In solution W124, there is no Ekman
 437 upwelling at the latitude of the northern tip of Drake Passage and thus Stom-
 438 mel's paradigm predicts no circumpolar transport, inconsistent with the plot-
 439 ted solution. Instead, the poleward migration of the fluid columns is achieved
 440 through an "eddy Sverdrup balance" between the eddy-induced and geostrophic
 441 upwellings, or equivalently

$$\beta v h \approx f w_{\text{eddy}}. \quad (5.1)$$

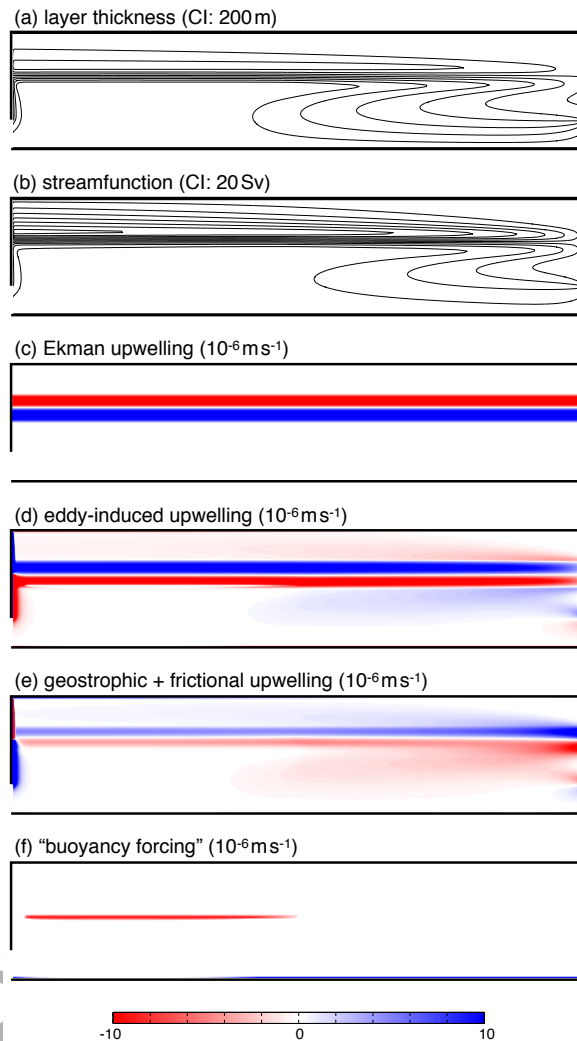


Figure 8: Lateral structure of solution W234. The plotted fields are as in Fig. 2.

442 In the third and fourth solutions, W234 (Fig. 8) and W344 (Fig. 9), in
 443 which the wind forcing is shifted even further north, a similar regime to the
 444 second solution persists, except that the southward deflection of the circumpolar
 445 current occurs over a larger area and there is some retroflexion of the current.
 446 In each case, the narrow outcropped region migrates northward with the wind
 447 jet. For the most northerly wind profile, the retroflexion fills the zonal width
 448 of the basin and there is a weak quasi-zonal transport within the circumpolar
 449 latitudes.

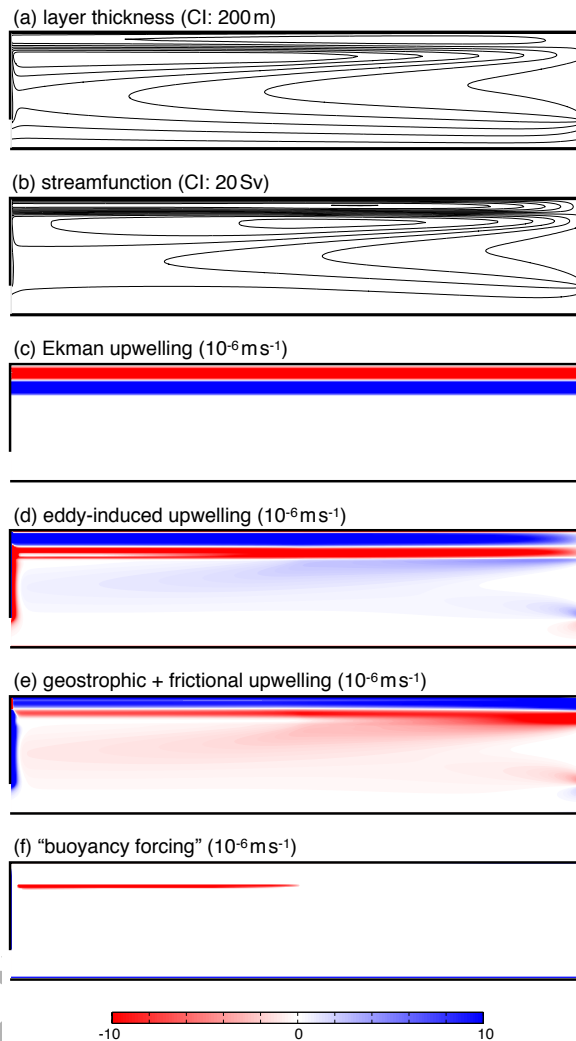


Figure 9: Lateral structure of solution W344. The plotted fields are as in Fig. 2.

450 5.2. Zonal momentum budget

451 The net meridional volume transport, equivalent to the zonal momentum
 452 budget (see section 4.5), and the layer thickness profiles along the eastern and
 453 western boundaries, are plotted in Fig. 10 for each of the four solutions.

454 Consistent with the preceding discussion, the Ekman and eddy-induced up-
 455 wellings compensate, aside from a small frictional contribution, when the wind
 456 forcing is confined to the latitudes of the model Drake Passage (panel (a)) and
 457 there is no residual volume transport. Thus, the momentum balance is be-

458 tween the surface wind stress and eddy form stress, consistent with Johnson
459 and Bryden (1989).

460 However, as the wind jet is shifted progressively further north (panels (b)-
461 (d)), the geostrophic contribution to the meridional volume transport becomes
462 increasingly important. This is associated with an increasingly large zonal pres-
463 sure gradient from the shallowing of the layer interface along the western bound-
464 ary. Nevertheless, note that the eddy contribution remains substantial in each
465 of the four solutions. In addition, the magnitude of the residual southward vol-
466 ume transport increases as the wind profile shifts north. The reason for this
467 remains unclear, but it may be related to the scaling of the Ekman upwelling in
468 the outcropped region with the inverse Coriolis parameter.

469 5.3. Drake Passage volume transport

470 Finally in Fig. 11 we plot the Drake Passage volume transport for each
471 of the four solutions against the latitude of the peak wind stress, and likewise
472 for the equivalent experiments with weaker wind forcing. Shifting the wind
473 stress forcing north of Drake Passage does weaken the Drake Passage volume
474 transport, most dramatically for the strongest wind forcing and only slightly for
475 the weaker wind forcings, but a strong circumpolar current remains in all cases.
476 For the most northerly profile, the Drake Passage volume transport actually
477 increases slightly, due to the variation of the Ekman transport with the inverse
478 Coriolis parameter.

479 The result that a large circumpolar transport remains when the wind is
480 shifted north of Drake Passage is consistent with the earlier findings of Allison
481 et al. (2010) for less extreme shifts. This raises questions about the applicability
482 of mechanisms that have been proposed for the sensitivity of the past and future
483 ocean to relatively subtle variations in the latitude of the southern hemisphere
484 wind jet (e.g., Toggweiler et al., 2006; Fyfe et al., 2007; Le Quéré et al., 2007).

485 6. What sets the Drake Passage volume transport?

486 The Drake Passage volume transport is well approximated by:

$$487 T_{dp} = \int_{dp} hu dy \approx -\frac{g_r h_{dp}^2}{2f_{dp}}, \quad (6.1)$$

488 where the integral is evaluated across the model Drake Passage and h_{dp} and
489 f_{dp} are evaluated at the northern edge of Drake Passage (where the streamlines
490 are concentrated). In deriving (6.1), the velocity has been approximated as
491 geostrophic and the layer thickness neglected to the south of Drake Passage.
492 Note that f_{dp} is negative and thus T_{dp} is positive.

493 Following a similar approach to Allison et al. (2010), an approximate ex-
494 pression is now sought for the circumpolar transport in terms of the wind stress
and model parameters. Combining $h/f \times$ the zonal component of (2.1) with the

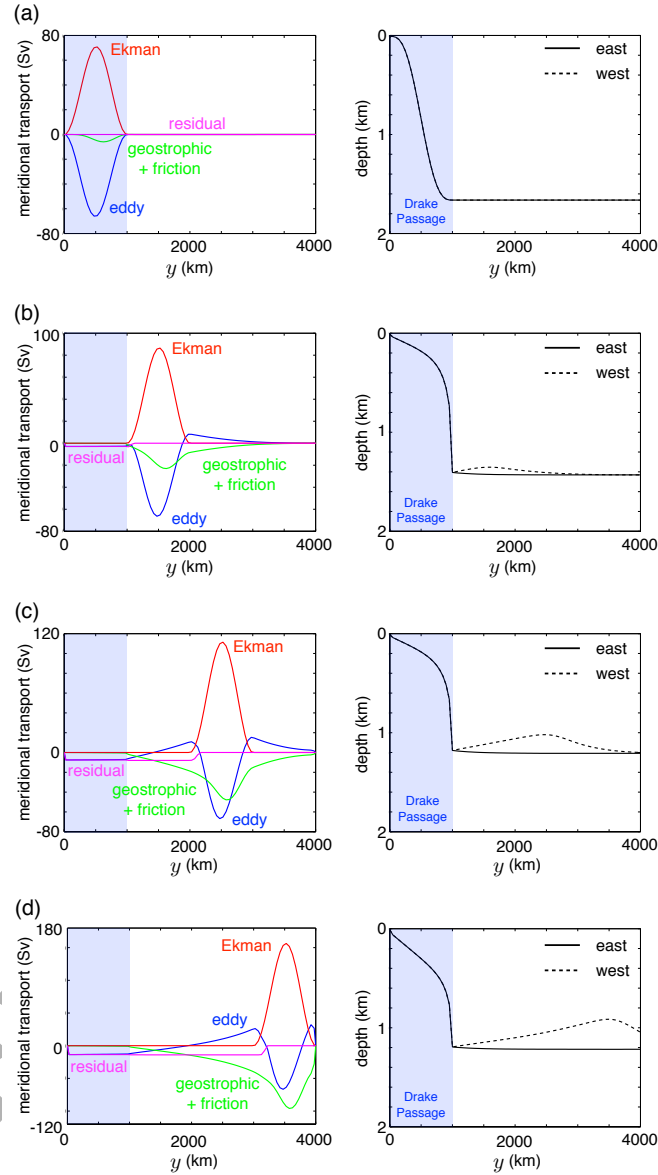


Figure 10: Net meridional volume transport decomposed into constituent terms, and the variation of the layer thickness, h , with meridional distance, y , along the eastern (solid lines) and western (dashed lines) boundaries, in solutions (a) W014, (a) W124, (a) W234, (a) W344. See the caption to Fig. 5 for more details. Note the different scales on the vertical axes of the left panels.

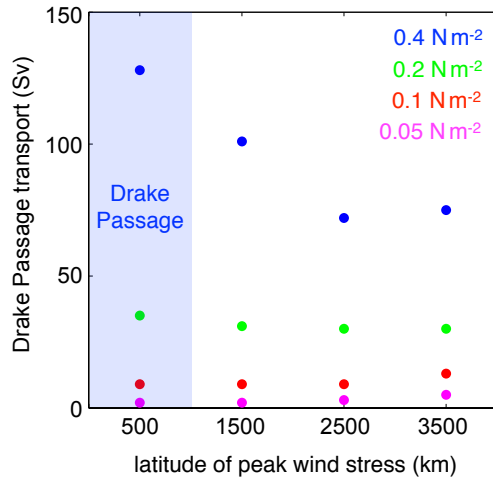


Figure 11: Variation of Drake Passage volume transport with the latitude of the wind jet for the narrow wind jet solutions (W01n, W12n, W23n, W34n; $n=0, 1, 2, 4$). Also shown with light blue shading is the latitude band of the model Drake Passage.

495 meridional component of the eddy bolus transport, the northward transport
496 velocity is

$$h(v + v^*) = \frac{\partial}{\partial x} \left(\frac{g_r h^2}{2f} \right) - \frac{\tau_s^{(x)}}{\rho_0 f} - (\kappa_{gm} + c \delta_s) \frac{\partial h}{\partial y}. \quad (6.2)$$

497 Equation (6.2) is integrated over the area bounded by the streamlines that touch
498 the northern and southern extremes of the model Drake Passage, as sketched
499 in Fig. 12. These streamlines are, in turn, approximated by the geostrophic
500 streamlines (layer thickness contours), except close to the western boundary
501 where, due to the pressure drop across the basin, it is necessary to connect the
502 northernmost layer thickness contour to the western boundary as sketched in

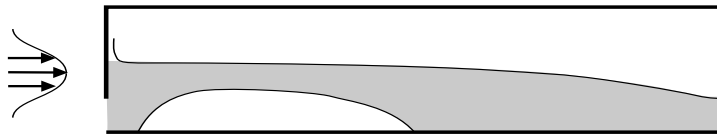


Figure 12: Schematic showing the shaded area over which (6.2) is integrated, bounded by the streamlines that touch the northern and southern extremes of the model Drake Passage. These streamlines are, in turn, approximated by the geostrophic streamlines (layer thickness contours), except close to the western boundary where, due to the pressure drop across the basin, it is necessary to connect the northernmost layer thickness contour to the western boundary. See the text for further details.

503 Fig. 12.

The result, neglecting the frictional term, is

$$\iint h(v + v^*) dx dy \approx \int \frac{g_r}{2f} (h_e^2 - h_w^2) dy - \iint \frac{\tau_s^{(x)}}{\rho_0 f} dx dy - \kappa_{gm} h_{dp} x_0. \quad (6.3)$$

504 Assuming the left-hand-side of this equation approximately vanishes, which
505 holds provided there is no residual northward transport (in which case a stream-
506 line cannot be defined), and neglecting the geostrophic term, a theoretical pre-
507 diction is obtained for the layer thickness at the northern tip of Drake Passage,

$$h_{dp} \approx \frac{1}{\kappa_{gm} x_0} \iint \frac{\tau_s^{(x)}}{\rho_0 f} dx dy, \quad (6.4)$$

508 from which a prediction of T_{dp} follows using (6.1). This is the result of Allison
509 et al. (2010) that the circumpolar transport depends on the *integral* of the wind
510 stress over the circumpolar streamlines. This prediction is tested against the
511 diagnosed model values in the top panels of Fig. 13. In general, the integral wind
512 stress serves as a useful predictor of the Drake Passage transport. However, there
513 is some scatter and the predicted value generally exceeds the actual transport,
514 by a considerable margin in the case of large wind stress, in particular when the
515 wind jet is located far north of the model Drake Passage.

An improved prediction of the circumpolar transport can be obtained by
retaining the geostrophic term,

$$h_{dp} \approx \frac{1}{\kappa_{gm} x_0} \iint \frac{\tau_s^{(x)}}{\rho_0 f} dx dy - \frac{1}{\kappa_{gm} x_0} \int \frac{g_r}{2f} (h_e^2 - h_w^2) dy. \quad (6.5)$$

516 This is tested against the diagnosed model values in the central panels of Fig.
517 13. Note that most of the scatter is now removed, except for the cases in which
518 the wind stress is located far north of the model Drake Passage.

519 In these latter cases, some of the discrepancy can be explained by noting
520 that the residual transport across the model Drake Passage does not vanish (see
521 Fig. 10). To obtain a further improved estimate, the residual transport can be
522 integrated across the model Drake Passage and included in the result,

$$\begin{aligned} h_{dp} &\approx \frac{1}{\kappa_{gm} x_0} \iint \frac{\tau_s^{(x)}}{\rho_0 f} dx dy \\ &\quad - \frac{1}{\kappa_{gm} x_0} \int \frac{g_r}{2f} (h_e^2 - h_w^2) dy \\ &\quad + \frac{1}{\kappa_{gm} x_0} \iint_{dp} h(v + v^*) dx dy. \end{aligned} \quad (6.6)$$

523 This is tested against the diagnosed model values in the lower panels of Fig. 13
524 where we see that yet more of the scatter is removed, except in the cases in which
525 the wind stress is located at the northern extreme of the basin. The final term

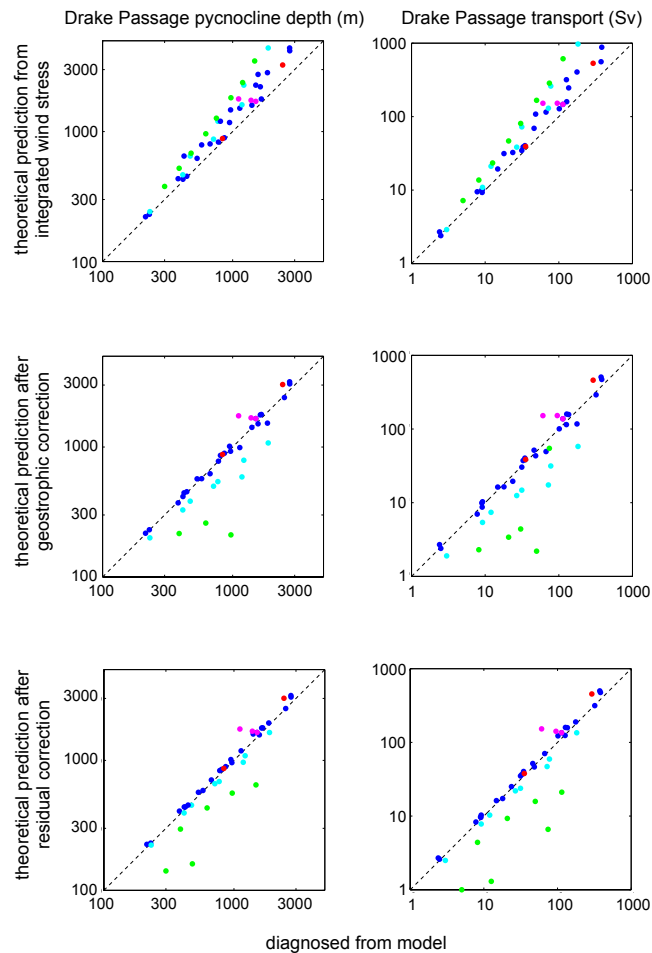


Figure 13: Comparison of the theoretical predictions of the pycnocline depth at the northern tip of “Drake Passage” (left panels) and the “Drake Passage” volume transport (right panels) against values diagnosed from the full model calculations. The three rows show the theoretical predictions obtained by: (i) integrating the zonal wind stress over the circumpolar streamlines; (ii) additionally correcting for the diagnosed northward geostrophic transport; (iii) further correcting for the diagnosed residual transport across Drake Passage. Blue points correspond to wind profiles where the peak wind stress lies at $y \leq L/2$, cyan points where the peak wind stress lies in the range $L/2 < y < 3L/4$, and green points where the wind stress lies at $y \geq 3L/4$. The three magenta points corresponds to the calculations in which the drag coefficient is increased (the control value lying on the dashed line), and the red points to the two additional calculations in which the Gent and McWilliams eddy diffusivity is increased and decreased.

526 in 6.6 neglects any residual transport north of Drake Passage, inclusion of which

527 actually degrades the prediction (not shown) for reasons that remain unclear,
 528 but are probably related to the presence of a retroflexion of the circumpolar
 529 current in the solutions concerned.

530 Finally, we note that an increased the linear drag coefficient leads to a re-
 531 duction in Drake Passage transport. This effect can be incorporated into the
 532 theoretical prediction by replacing the eddy diffusivity, κ_{gm} with $\kappa_{gm} + c\delta_s$
 533 (assuming a mean value of c) and recalculating the integrals through the same
 534 procedure (not shown).

535 Thus, in summary, the integral of the wind stress over the circumpolar
 536 streamlines serves as a useful predictor of the Drake Passage transport in the
 537 model, even when the wind stress is located north of the model Drake Passage.
 538 The simplest measure proposed by Allison et al. (2010) generally overestimates
 539 the circumpolar transport. This can be improved substantially by correcting
 540 for basin-wide pressure gradients, and to a lesser extent for the residual volume
 541 transport across the model Drake Passage. Note that all of these “predictions”
 542 are implicit in the sense that one requires advance knowledge of the path of the
 543 circumpolar streamlines. However, in practice, these can often be anticipated
 544 from the latitude of the peak wind stress, although this relationship can break
 545 down when the latitude of the peak wind stress is not well defined (not shown).

546 In reality, the eddy diffusivity will vary strongly across the ACC and hence
 547 the main value of these predictions is pedagogical, in illustrating that there is a
 548 relation between the volume transport of the ACC and a (weighted) integral of
 549 the wind stress forcing, rather than any practical predictive skill.

550 7. Concluding remarks

551 In this manuscript we have formulated and analyzed solutions of a simple
 552 reduced-gravity model of the ACC. The model bears many similarities to that
 553 developed by Gill (1968) for a barotropic ocean, but with the model parameters
 554 reinterpreted in terms of quantities at the heart of contemporary descriptions of
 555 ACC dynamics, such as the pycnocline depth and Gent and McWilliams eddy
 556 diffusivity. Our main findings are:

- 557 • A substantial circumpolar volume transport is obtained when the latitude
 558 of the wind jet is shifted north of the model Drake Passage, even by several
 559 thousand kilometers.
- 560 • Meridional excursions of the modelled ACC are described by a linear vor-
 561 ticity balance between advection of planetary vorticity and stretching by
 562 the residual of the Ekman and eddy-induced upwellings.
- 563 • The integral of the wind stress over the circumpolar contours is a useful
 564 predictor of the magnitude of the volume transport through the model
 565 Drake Passage, although it is necessary to correct for basin-wide zonal
 566 pressure gradients in order to obtain good quantitative agreement.

567 We hope this work will restore Gill (1968) to its rightful place at the center-stage
568 of theoretical understanding of the ACC.

569 These results have significant implications for studies of past and future
570 climate change that assume a relation between the latitude of the southern
571 hemisphere wind jet and the circulation along and/or across the ACC (e.g.,
572 Toggweiler et al., 2006; Fyfe et al., 2007; Le Quéré et al., 2007). In particular,
573 special emphasis is often placed on the wind stress across the circumpolar lati-
574 tude band, or at the northern tip of Drake Passage. While our model solutions
575 do show variations in circumpolar volume transport as the wind jet is shifted
576 northward, a strong circumpolar volume transport remains even when the wind
577 jet is entirely north of the circumpolar latitudes. It remains to be established
578 whether this result extends to the overturning circulation across the ACC which,
579 for example, is more important for ocean carbon uptake. Nevertheless the re-
580 sults reported here do suggest that current thinking on these topics may be
581 over-simplistic.

582 While the model has proved valuable in addressing some zero-order ques-
583 tions, it has many limitations. An obvious extension is to multiple layers (e.g.,
584 Bell, 2015), particularly in the light of the result that the model selects, through
585 its dynamics, regions of outcropping and dense water formation. A natural ques-
586 tion is to what extent is a multi-layer model able to predict the lateral structure,
587 including the formation sites, of the Antarctic intermediate and bottom water
588 masses through a finite residual circulation across the ACC (Marshall, 1997;
589 Marshall and Radko, 2003) — a “ventilated thermocline” model for the South-
590 ern Ocean (cf. Luyten et al., 1983). It is clear that such a model will require a
591 more realistic representation of buoyancy forcing.

592 A further issue that we have glossed over is the role of the barotropic mode.
593 Firstly, while the eddy-induced upwelling might modify “Sverdrup balance”
594 within a reduced-gravity layer, it cannot affect the vorticity budget of the entire
595 fluid column, at least not directly. Thus, implicit in our reduced-gravity solu-
596 tions is an opposite meridional volume transport in the abyssal ocean (albeit over
597 an infinite depth, so not affecting the path of the surface streamlines). In prac-
598 tice, bottom topography will significantly modify the depth-integrated vorticity
599 budget (e.g., Marshall, 1995a,b; Hughes and Killworth, 1995; Hughes, 2005) so
600 such concerns may be of limited practical significance. Secondly, Rossby waves
601 propagate eastward in the core of the ACC (Hughes et al., 1998; Hughes, 2005),
602 Doppler-shifted by the depth-mean velocity (Klocker and Marshall, 2014). Since
603 westward Rossby propagation plays a role in establishing the structure of the
604 present solutions, it is natural to ask how the solution is modified when the
605 Rossby waves are Doppler-shifted and propagate eastward.

606 Finally, we wish to reiterate that all of the present results have been ob-
607 tained using a model with parameterized eddies. The ACC exhibits far less
608 sensitivity to changes in wind stress forcing in models with explicit, rather than
609 parameterized, eddies (Hallberg and Gnanadesikan, 2001; Tansley and Marshall,
610 2001b; Hallberg and Gnanadesikan, 2006; Hogg and Blundell, 2006; Meredith
611 and Hogg, 2006; Farneti et al., 2010; Farneti and Delworth, 2010; Munday et al.,
612 2013). In addition, eddy activity becomes enhanced in the lee of major topo-

613 graphic features, also leading to the formation of inertial jets (e.g., MacCready
614 and Rhines, 2001; Tansley and Marshall, 2001a; Abernathey and Cessi, 2014).
615 Hence it remains to be seen how the present results apply to an ocean with
616 explicit eddies.

617

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619

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625 **Appendix. Method of solution**

626 The time scale for a time-dependent reduced gravity model of the ACC to
627 equilibrate is several millennia (Allison et al., 2011). Thus for computational
628 efficiency equilibrium solutions to (2.1-2.3) are obtained through a relaxation
629 method. The grid spacing in the basin interior is a uniform 50 km. Variable grid
630 spacing is employed in x near the meridional boundaries to enhance resolution
631 within the boundary layers, as sketched in Fig. 14. Thus, approaching the
632 boundary over the last 14 grid cells, each grid spacing is roughly a factor 0.75
633 smaller than its neighbor. These 14 cells are equivalent to 3 grid cells in the
634 basin interior, the finest grid spacing being 0.9 km adjacent to the boundaries.
635 To maintain a structured grid, the same grid spacings are also applied within
636 the Drake Passage latitude band.

637 We rewrite (2.2) as a finite-difference diffusion equation on a C-grid with a
638 forward Euler time step:

$$h^{\text{new}} = h^{\text{old}} - (\nabla \cdot \mathbf{U} - w_{ek}) \Delta t(x, y). \quad (\text{A.1})$$

639 Here the layer thickness flux excludes the Ekman contribution but includes the
640 eddy bolus transport:

$$\mathbf{U} = \frac{g_r}{2f} \mathbf{k} \times \nabla \bar{h}^{xy} - \kappa_{gm} \nabla h - \frac{rg_r}{2f^2} \nabla h^2 \quad (\text{A.2})$$

641 where \bar{h}^{xy} indicates an average of h between the four adjacent points. The first
642 term on the right-hand side can be decomposed into a westward Rossby flux and
643 a dynamically-inert rotational flux, as in (2.4), but we retain the form in (A.2)
644 for consistency with the boundary condition discussed below. The time-step
645 is allowed to vary spatially and is chosen to ensure both stability and efficient
646 convergence:

$$\Delta t(x, y) = \frac{1}{8(\kappa_{gm} + c\delta_s)} \left(\frac{1}{\Delta x^2} + \frac{1}{\Delta y^2} \right)^{-1}. \quad (\text{A.3})$$

647 The northern half-width boundary cells, shaded grey in Fig. 14, are treated
648 through a separate, two-step procedure. To understand the rationale for this,

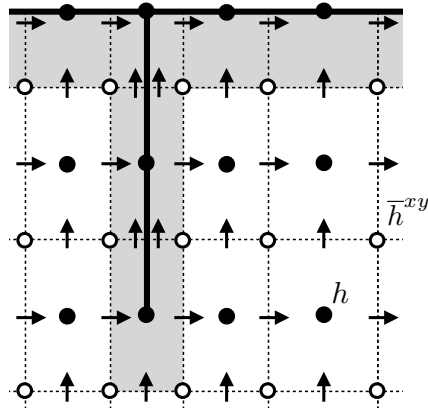


Figure 14: The equations (A.1), (A.2) and (A.4) are solved on a C-grid with a default grid spacing of 50 km, reducing smoothly to 1 km to enhance resolution within the western and eastern boundary layers. Adjacent to the boundaries is a line of half-width cells (shaded) such that the layer thickness, h is located on the boundaries. Also shown are the zonal and meridional transports, U and V , as defined in (A.2), and the averaged layer thickness, \bar{h}^{xy} , required for computation of the geostrophic transports.

649 note that the advective transport on the boundary can be simplified using the
650 boundary condition (2.3):

$$\mathbf{U}_{\perp} = 0, \quad \mathbf{U}_{\parallel} = -\frac{rg_r}{2f^2} \left(1 + \frac{f^2}{r^2} \right) \nabla_{\parallel} h^2. \quad (\text{A.4})$$

651 Thus, the effect of the boundary condition is equivalent to an along-boundary
652 diffusion that can be shown to be a factor $(c\delta_s/\kappa_{gm})f^2/r^2$ larger than in the
653 basin interior; for the majority of the model calculations reported here, this fac-
654 tor is roughly 10^5 . The effect of this rapid along-boundary diffusion is to rapidly
655 remove unbalanced along-boundary pressure gradients and, in conjunction with
656 the thickness flux into the boundary grid cells through (A.2), can be shown to
657 give rise to Kelvin waves (or their low-frequency counterparts; Marshall and
658 Johnson, 2013).

659 For computational efficiency, we first update the mean layer thickness across
660 all of the boundary cells shaded grey in Fig. 14. This is carried out with a time
661 step that is determined empirically to be 20 times that given by (A.3) for one of
662 the northern cells. We then update for the variation of the layer thickness along
663 the boundary with a time step given by (A.3), except replacing the diffusion
664 coefficient by its enhanced along-boundary value.

665 Each equilibrium solution is obtained by stepping forward (A.1) through a
666 minimum of 60 000 iterations, where necessary repeating this process until con-
667 vergence is achieved. To give an idea of the efficiency of the above procedure,
668 the equilibrium solution is achieved after the equivalent of 10 model years of in-
669 tegration of the time-dependent reduced-gravity equations with a uniform grid

670 spacing of 50 km and time step of 5000 s.

671

672 **References**

673 **References**

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