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### ABSTRACT

In this work, three linear isotactic polypropylenes with different weight-average molecular weights,  $M_w$ , and comparable polydispersity were used to produce nonwovens by melt blowing technology at two different temperatures, *T*. The air/polymer flow rate was changed to maintain the same average fiber diameter, resulting in a different broadness of fiber diameter distribution, which was quantified by the coefficient of variation, *CV*. The elasticity of the material was evaluated by the Reptation-mode relaxation time,  $\lambda_l$ , and the Rouse-mode reorientation time,  $\lambda_2$ , determined from the deformation rate dependent shear viscosity data. Extensional rheology was evaluated using uniaxial extensional viscosity measured over a very wide range of strain rates  $(2 \times 10^4 - 2 \times 10^6 \text{ 1/s})$  using entrance pressure drop and Gibson method. Obtained plateau value of uniaxial extensional viscosity at the highest extensional strain rates,  $\eta_{E,\infty}$  (normalized by the three times zero-shear rate viscosity,  $\eta_0$ ) and the minimum uniaxial extensional viscosity,  $\eta_{E,min}$  were related to  $M_w$  and *T* using simple equations. It has been found that the stability of fibers production captured by *CV* depends exclusively on the extensional properties of the polypropylene melts, namely  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  and  $\eta_{E,U,min}$ . These findings are important especially with regard to the stable

production of polymeric nanofibers by melt blowing technology.

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### **INTRODUCTION**

Meltblown (MB) is a one-step process for converting polymeric raw materials into nonwovens with many applications, such as filtration (air or liquid) surgical face masks and gowns, protective overalls, drapes, battery separators, sorbents and wipes, hygiene (diapers, nappies, towels), biosensors, scaffolds for tissue engineering and many other areas [1 - 3]. In this technology, the polymer melt is extruded through small holes into converging hot air streams [4 - 6], typically reaching 50 - 80 % of the speed of sound [2, 7, 8]. The drag force of the air causes a rapid elongation of the melt into a fine fiber with a small diameter [4 - 6], as shown in Figure 1. A typical change in fiber diameter (expressed here as the ratio of die to final fiber diameter), is between 250 and 667 for isotactic polypropylenes [9, 10]. It has been reported that the highest reduction in fiber diameter occurs at very small post die distances (usually between 10 and 20 mm) and at very short times (0.05 ms) [11 – 14]. During fiber thinning process, very high extensional strain rates ( $\sim 10^6$  1/s) are achieved [15]. The collector captures attenuated filament streams, resulting in a nonwoven web formation with an almost random network of fibers [2]. The typical fiber diameter range for MB is  $1 - 2 \mu m$  [2, 10, 16, 17], but in many studies published in recent decades, the average fiber diameter is less than  $1 \mu m [1, 4, 10, 16, 18 - 22]$  and the lowest average fiber diameter ever produced by MB is 36 nm [21].) Polypropylene (PP) is one of the most popular polymers in MB due to its ease of processing and suitability for end use. However, there are flow phenomena (such as whipping [23], fiber breakup, flies, generation of small isolated spherical particles, jam, die drool [24 - 30] and interconnected extrudate swell [31 - 36], secondary flow [37-39] and shots), which significantly increases the unevenness of the polymeric fibers produced [40]. It has been shown that the coefficient of variation, CV, for the average fiber diameter,  $d_{av}$ , can be reduced for polystyrene [15] and PP [9] by increasing the longest melt relaxation time,  $\lambda_{l}$ ,

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or introducing a chain branching (maintaining the same molecular weight and polydispersity of PP), which was attributed to the change in the extensional viscosity. In more detail, the stabilizing effect of chain branching has been attributed to facilitating the intensive fiber thinning process due to reduced extensional viscosity at very high strain rates on the one hand and reduced melt sensitivity to whipping instability due to increased extensional viscosity at medium and low strain rates on the other. Larson and Desai [41] showed for the linear polystyrene, based on the finitely extensible nonlinear elastic model (FENE-P) Doi-Edwards-Marrucci-Grizzuti (DEMG) constitutive equations and supporting data, that as the concentration increases from unentangled dilute, to entangled, to a dense melt, the extensional strain hardening at very high extensional strain rates decreases due to the orientation-induced reduction in friction. This suggests that the molecular characteristics and temperature of linear PPs can affect alignment of polymer chains, monomeric friction and high extensional rate rheology, which is key to understanding the stability of the melt blowing process.

To understand molecular structure-rheology-process temperature-flow stability relations for polymer melts at very high strain rates, three well-characterized linear isotactic polypropylenes (molar mass from 56 to 76 kg/mol) were used to produce nonwovens of comparable average fiber diameter on a multihole Reifenhäuser Reicofil pilot plant meltblown line at two different temperatures. The flow stability was quantified in terms of the coefficient of variation, CV, charactering the broadness of the fiber diameter distribution.

### **EXPERIMENTAL**

### Materials

Linear isotactic polypropylenes (L-PP) Borflow HL504FB, HL508FB and HL512FB produced by Borealis Polyolefine (Linz, Austria), were used in this work. All three samples were carefully characterized in our previous work at 190, 210 and 230 °C by rotational and capillary rheometry as well as by an instrumented injection molding machine to cover a very wide range of shear rates [42] (see Figure 2 – left). The performed measurements allowed direct determination of the zeroshear rate viscosity,  $\eta_0$ , and the infinite shear viscosity,  $\eta_{\infty}$ , together with the corresponding flow activation energies (E<sub>0</sub> and  $E_{\infty}$ ) using a well-known Arrhenius plot. All the above parameters of the polymers used together with the basic molecular characteristics are given in Table 1. The power-law index, n, the reptation-mode relaxation time,  $\lambda_1$ , and the Rouse-mode reorientation time,  $\lambda_2$ , characterizing the melt elasticity at low and very high shear rates, respectively, represent additional key rheological parameters. However, their determination by fitting of shear viscosity data over a very wide range of shear rates by conventional viscosity models can lead to nonphysical values despite giving an excellent numerical fit [9]. In this work, n,  $\lambda_1$  and  $\lambda_2$  were determined directly from the measured shear viscosity data as follows. First, tangents were constructed in the area of the first and second Newtonian plateaus. Second, three points were selected just before the beginning of the second Newtonian plateau. Third, the points were fitted by a straight line and the correlation coefficient was calculated. Fourth, additional points were added to these base points step by step (towards lower shear rate values) and the corresponding correlation coefficient was calculated for each individual linear fit. Fifth, the power-law region was determined by the number of points, which led to the highest linear correlation coefficient. Note that for all three samples, the optimal number of points was 16 (see Figure 2 -right). Finally,

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the parameters  $\lambda_1$  and  $\lambda_2$  were determined as the reciprocal values of the shear rates determined from the intersections between the power-law tangent and the first and second Newtonian plateau tangents (see Figure 2 – left). The parameter *n* is given by the power-law tangent slope, which is equal to n-1. The obtained parameters (i.e.  $\lambda_1$ ,  $\lambda_2$  and *n*) are given in Table 2.

The extensional viscosities for all investigated samples were determined from the measured entrance pressure drop data on the instrumented injection molding machine [42, 43] using the Gibson model, which is based on the sink flow kinematics with no vortices and it is given by the following equations [44 - 46]:

$$\sigma_{\rm E} = \frac{\overline{P_{\rm Ent}}}{\left[2/(3k)\right] \left[1 - \left(\frac{R}{R_{\rm b}}\right)^{3k}\right] + \left\{I(k,\alpha)/[\sin(\alpha)(1+\cos(\alpha))]^n\right\}}$$
(1)

$$\overline{\mathbf{P}_{\text{Ent}}} = \mathbf{P}_{\text{Ent}} - 2\tau_{\text{xy,Cor}} [\sin(\alpha)]^{3n} [1 - (\mathbf{R} / \mathbf{R}_{\text{b}})^{3n}] [(3n+1)/(4n)]^{n} / [3n(\pi/2)^{3n+1}]$$
(2)

$$I(k,\alpha) = \int_{0}^{\alpha} [1 + \cos(\beta)]^{k-1} [\sin(\beta)]^{k+1} d\beta$$
(3)

$$\dot{\varepsilon} = \frac{1}{4} \dot{\gamma}_{App} \sin\left(\alpha\right) [1 + \cos(\alpha)] \tag{4}$$

Here  $\overline{\mathbf{P}_{\text{Ent}}}$  represents the entrance pressure drop arising only from the uniaxial extensional flow, *R* is the radius of the die, *R<sub>b</sub>* is the radius of the barrel,  $\alpha$  is the entrance angle, *n* is the local slope in the corrected shear stress ( $\tau_{xy, Cor}$ ) vs. the apparent shear rate ( $\dot{\gamma}_{\text{App}}$ ) function in the log-log scale, *k* represents the local slope in the  $\overline{\mathbf{P}_{\text{Ent}}}$  vs.  $\dot{\gamma}_{\text{App}}$  function in the log-log scale. The term I(k, $\alpha$ ) given by Eq. 3 must be calculated numerically.

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### Melt blowing experiment

L-PP nonwovens were made on the Reifenhäuser Reicofil pilot plant meltblown line (see Figure 3 and the corresponding video below) utilizing a nosepiece die (having sharp-edged die-nose) with the following characteristics: total and active width equal to 350 mm and 250 mm, respectively; orifice diameter: 0.4 mm; number of holes per active part: 470; processing conditions: melt/air temperature: 250 and 270 °C; collector belt speed: 5 m/min, die-to-collector distances: 500 mm. The air volume flow rate was reduced with reduced temperature or increased molecular weight of the polypropylenes used to achieve a comparable average fiber diameter for all samples, i.e. about 1.5  $\mu$ m, while the mass flow rate for one orifice remained the same (0.0885 g/hole/min). Information on the air volume flow rate used in each case is given in Table 3.

### Morphological characterization

For the given processing conditions and the polymer used, two samples with dimensions 10 mm × 10 mm were cut out from different places of the produced nonwoven sample. A HITACHI Tabletop TM-1000 scanning electron microscope (SEM) was then used to visualize the nonwoven structure for each sample at three different magnifications (500×, 1000×, 2500×) by using a high-sensitive back-scattered electron (BSE) detector. The basic morphological characteristics of the produced nonwovens were determined by using in-house developed software (UTBsoft Filtration) at the Faculty of Technology, Tomas Bata University in Zlín. This software makes it possible to combine all three SEM images with different magnifications and to create one normalized fiber diameter distribution curve via skeletonization image processing according to the technique proposed in [9, 47, 48]. This allows to take into account both nanofibers and microfibers, which



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appear in manufactured meltblown nonwovens [9]. Mean,  $d_{av}$ , standard deviation,  $\sigma$ , and coefficient of variation, *CV* were determined by fitting the fiber diameter distribution by a log-normal function utilizing the following equations [10, 15, 21, 49]:

$$f\left(\log\left(d\right)\right) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left[-\frac{1}{2\sigma^2} \left\{\log\left(d\right) - \mu\right\}^2\right]$$
(5)

$$d_{av} = 10^{\mu \pm \sigma} \tag{6}$$

$$CV = \sqrt{exp(\sigma^2) - 1} \tag{7}$$

### **RESULTS AND DISCUSSION**

### Shear rheology

The reptation-mode relaxation time,  $\lambda_1$ , and the Rouse-mode reorientation time,  $\lambda_2$ , were plotted in Figure 4 as a function of the weight-average molecular weight,  $M_w$ , at 230 °C. As can be seen, both parameters are linearly scaled with  $M_w$  in log-log scale and the power-law exponent for  $\lambda_1$  is higher (3.139) compared to  $\lambda_2$  (1.351) and its values are similar to the values obtained for zero shear,  $\eta_0$ , (3.62 [9, 43]) and infinite,  $\eta_{\infty}$ , (1 [9, 43]) viscosities. Since  $\lambda_1$  and  $\lambda_2$  relate to highly entangled and almost disentangled states, their temperature dependences can be considered the same as for their shear viscosity counterparts  $\eta_0$  and  $\eta_{\infty}$ , i.e.

$$\lambda_{1} = 5.807 \cdot 10^{-19} \exp\left[\frac{E_{0}}{R}\left(\frac{1}{T} - \frac{1}{T_{r}}\right)\right] M_{w}^{3.139}$$
(8)

$$\lambda_2 = 1.526 \cdot 10^{-13} \exp\left[\frac{E_{\infty}}{R} \left(\frac{1}{T} - \frac{1}{T_r}\right)\right] M_w^{1.351}$$
(9)

where *T* is the temperature in Kelvin,  $T_r$  is the reference temperature (equal to 503.15 K),  $E_0$  and  $E_{\infty}$  are the zero and the infinite flow activation energies, *R* is the universal gas constant (8.314 J/K/mol).

### Extensional rheology

The measured uniaxial extensional viscosity,  $\eta_{E,U}$  is plotted as a function of the extensional strain rate,  $\dot{\epsilon}$ , in Figure 5 (top) for all three linear isotactic polypropylene samples. As the strain rate increases,  $\eta_{E,U}$  decreases, reaches the minimum value,  $\eta_{E,U,min}$ , (zone I) and then, it increases due to starting occurrence of the chain stretch (zone II) to the plateau value,  $\eta_{E,U,\infty}$ , which corresponds to the maximum chain stretch (zone III). The transition between zone I and zone II occurs at  $\dot{\varepsilon} = \frac{1}{\lambda_{rel}}$ where  $\lambda_s$  is the stretch relaxation time, which is estimated here by fitting of the measured data with a polynomial function (see Table 2). This behavior is consistent with predictions arising from the molecular based constitutive equations for linear polymer melts [50]. The measured extensional viscosity data can also be discussed in term of the dimensionless Weissenberg number, Wi, defined as the ratio of elastic to viscous forces (see Figure 5, bottom). In zone I, the chain orientation Weissenberg number  $Wi_1 = \lambda_1 \dot{\epsilon} >> 1$  (namely 10 - 300) but the chain stretch Weissenberg number  $Wi_s = \lambda_s \dot{\epsilon}$  is still small (<1), i.e. the maximum orientation of the primitive path of the molecule is reached but there is no stretching. The extensional stress becomes constant (or rises less than linearly with increased  $\dot{\varepsilon}$ ) and hence extensional thinning occurs [41]. In zone II, when

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 $1 \le Wi_s = \lambda_s \dot{\varepsilon}$  < about 7, the polymer molecules becomes fully aligned and stretched, leading to a rapid increase in extensional viscosity (extensional thickening). In zone III, when  $Wi_s = \lambda_s \dot{\varepsilon}$  > about 7, the maxim chain stretch is achieved, extensional stress increases linearly with increased  $\dot{\varepsilon}$  and extensional viscosity becomes constant, equal to high-strain rate plateau, given by  $\eta_{E,U,\infty}$ . It can also be seen in Figure 5 that the decrease in  $M_w$  widens the region at  $\eta_{E,U,min}$ , where the extensional viscosity depends very weakly on the extensional strain rate and also increases Wi at which the maximum chain stretch is reached.

 $\eta_{E,U,min}$  and  $\eta_{E,U,\infty}$  are related to  $M_w$  in Figure 6 at T = T<sub>r</sub> = 230 °C. It is obvious that both variables are linearly scaled with  $M_w$  in a log-log scale and  $\eta_{E,U,\infty}$  shows a very weak dependence on  $M_w$ . The experimental data were fitted with power-law functions and the following relationships were found (considering that both variables have the same Arrhenius temperature dependence as  $\eta_{\infty}$ ).

$$\eta_{E,U,\infty} = 20.853 \exp\left[\frac{E_{\infty}}{R}\left(\frac{1}{T} - \frac{1}{T_{r}}\right)\right] M_{w}^{0.103}$$
(10)

$$\eta_{E,U,min} = 4.837 \cdot 10^{-7} \exp\left[\frac{E_{\infty}}{R}\left(\frac{1}{T} - \frac{1}{T_{r}}\right)\right] M_{w}^{1.580}$$
(11)

As can be seen, both variables decrease with decreased  $M_w$  or with increased temperature.

 $\eta_{E,U}$  normalized by the three times zero-shear rate viscosity,  $\eta_0$ , plotted as a function of the extensional strain rate at T<sub>0</sub> = 230 °C, is shown in Figure 7 for all three samples tested. Very interestingly, samples with  $M_w$  equal to 76 and 64 kg/mol show extensional strain hardening (i.e.

 $\frac{\eta_{E,U}}{3\eta_0}$  >1) at very high extensional strain rates due to chain stretch, but sample with  $M_w$  equal to 56

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kg/mol does not. Thus, there is a critical  $M_{W}$  below which extensional strain hardening starts to occur at very high extensional strain rates. Figure 8 shows the measured maximum extensional strain hardening,  $\frac{\eta_{E,U,\infty}}{3n_0}$ , plotted as a function of  $M_w$  at T = Tr = 230 °C. The measured data were successfully fitted with the following power-law equation considering that the temperature shift factor is the same as for the  $\eta_{\alpha}/\eta_0$  ratio [9].

$$\frac{\eta_{E,U,\infty}}{3\eta_0} = \exp(39.524) \exp\left[\frac{E_{\infty} - E_0}{R} \left(\frac{1}{T} - \frac{1}{T_r}\right)\right] M_w^{-3.518}$$
(12)

 $\eta_{E,U,\infty}$ Since the flow activation energies are not the same in the entangled as disentangled states,  $3\eta_0$ depends not only on  $M_w$ , but also on the temperature. In more detail,  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  increases with decreased  $M_w$  and increased temperature, as can be seen from Eq.12 and its visualization in Figure 8.

### Understanding of melt blowing process dynamics

SEM images, fiber diameter distributions, and log-normal function fits for produced nonwovens from linear isotactic polypropylenes are shown in Figs. 9 - 14. In order to understand the dynamics of the melt blowing process,  $\lambda_1$ ,  $\lambda_2/\lambda_1$  and  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  parameters were calculated for given temperatures and  $M_w$  of processed samples using Eqs. 8, 9, 12 and are summarized in Table 3. The same parameters were also determined for selected experimental data taken from the open

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to select data from the open literature. First, the processing temperature ( $T_{die}$ ) and  $M_w$  of the given PP are provided. Second, the average fiber diameters of produced fibers are comparable with those produced in this work. Third, CV, standard deviation or raw fiber diameter distribution data allowing the CV determination are given. In some studies, [10, 16, 51 – 56],  $M_w$  is provided only for pellets, not for processed samples. Therefore, the  $M_w$  of the processed samples was considered to be 12.5 % less than  $M_w$  of the polymer pellets during the calculation of  $\lambda_1$ ,  $\lambda_2/\lambda_1$  and  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  via

Eqs. 8, 9, 12. The value of 12.5 % was calculated as the average reduction  $M_w$  of the polymer pellets at high strain rates (at  $10^5 - 10^7$  1/s, which are typical for the melt blowing process) and  $T_{die} = 230 \text{ }^{\circ}\text{C}$  (i.e. at a temperature which is the same as for the extensional viscosity measurements performed in this work) using the experimental data shown in Figure 13 in [57].

The *CV* plotted as a function of  $\lambda_1$ ,  $\lambda_2/\lambda_1$  and  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  is shown in the Figures 15 – 17 for all

considered linear isotactic PPs summarized in the Tables 3 – 4. It can be seen that in general, *CV* decreases when  $\lambda_1$  increases or when  $\lambda_2/\lambda_1$  decreases due to increased  $M_w$  or decreased temperature, which is in good agreement with previous experimental reports [9, 15]. This general trend can be understood using the minimum uniaxial extensional viscosity,  $\eta_{E,U,min}$ , which shows a similar functional dependence on  $M_w$  and T as the parameters  $\lambda_1$  and  $\lambda_2$  (compare Eqs. 8, 9 and 11).  $\eta_{E,U,min}$  can be viewed as a rheological parameter that controls stretching ability of the melt at extensional strain rates typical for the melt blowing process. Thus, increasing  $\eta_{E,U,min}$  (by increasing  $M_w$  or decreasing T) helps to resist inhomogeneous stretching in the post-die area, which reduces *CV*. Of course,  $\eta_{E,U,min}$  must be within a certain range, which allows stretching of the polymer melt to the desired fiber diameter. This is because if  $\eta_{E,U,min}$  is too low, and the fiber diameters are too high or  $\eta_{E,U,min}$  is too low, and the fiber

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breaks. However, there are certain specific cases where CV does not correlate with the  $\lambda_1$  and  $\lambda_2/\lambda_1$ variables (i.e. with  $\eta_{E,U,min}$ ). These cases are clearly marked in Figs. 15 – 16. However, if the CV is plotted as a function of  $\frac{\eta_{E,U,\infty}}{3\eta_{\circ}}$  (calculated via Eq.12), a clear functional dependence can be observed in all considered cases (see Figure 17). The following four specific regions can be identified.  $\frac{\eta_{\text{E},\text{U},\infty}}{3\eta_0} \le 1$ , and  $4 < \frac{\eta_{\text{E},\text{U},\infty}}{3\eta_0} \le 5$ , where the increase in  $\frac{\eta_{\text{E},\text{U},\infty}}{3\eta_0}$  increases *CV*;  $1 < \frac{\eta_{\text{E},\text{U},\infty}}{3\eta_0} \le 4$ where the increase in  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  decreases *CV* and finally,  $\frac{\eta_{E,U,\infty}}{3\eta_0} > 5$ , where the increase in  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  has practically no effect on the CV. In the other words, there is a processing window given by 1 < 1 $\frac{\eta_{E,U,\infty}}{3\eta_0} \le 4$ , in which the *CV* is reduced by increasing  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  via reducing of  $M_w$  or by increasing the temperature (see Eq.12 and Figure 17). The observed trend can be understood from a molecular point of view through an increased monomeric friction coefficient, which enhances extensional thickening at very high extensional strain rates and suppresses capillary breakup [41]. The flow stability, here quantified by *CV*, can thus be fully understood by  $\eta_{E,U,min}$  and  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  as follows. If  $\eta_{E,U,min}$  is high and  $\frac{\eta_{E,U,\infty}}{3\eta_0} < 1$  (Case I), the stabilizing effect of high  $\eta_{E,U,min}$  dominates over

destabilizing effect of no extensional strain hardening. If  $\eta_{E,U,min}$  is low and  $1 < \frac{\eta_{E,U,\infty}}{3\eta_0} \le 4$  (Case II),

the stabilizing effect of the present extensional strain hardening is higher than the destabilizing effect of low  $\eta_{E,U,min}$ . If  $\eta_{E,U,min}$  is very low and  $\frac{\eta_{E,U,\infty}}{3\eta_0} > 4$  (Case III), the destabilizing effect of

low  $\eta_{E,U,min}$  dominates over the stabilizing effect of high extensional strain hardening. As can be

seen from Eq.11 and Eq.12,  $\eta_{E,U,min}$  and  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  depend on  $M_w$  and temperature, which allows visualization of all three cases graphically (see Figures 18 – 19). The critical boundaries visualized in these Figures are given by Eqs. 13 – 14 with  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  is equal 1 and 4 for transitions I/II and II/III.

The first equation arises from Eq. 12, while the second from Eq.11 and Eq.13.

$$M_{w} = \left\{ \left( \frac{\eta_{E,\infty}}{3\eta_{S,0}} \right)^{-1} \exp(39.524) \exp\left[ \frac{E_{\infty} - E_{0}}{R} \left( \frac{1}{T} - \frac{1}{T_{r}} \right) \right] \right\}^{\frac{1}{3.518}}$$
(13)

$$\eta_{E,U,min} = 24.831 \left( \frac{\eta_{E,\infty}}{3\eta_{S,0}} \right)^{-0.449} exp \left[ \frac{1.449E_{\infty} - 0.449E_{0}}{R} \left( \frac{1}{T} - \frac{1}{T_{r}} \right) \right]$$
(14)

Figures 18 – 19 and Eq.13 – 14 have very practical implications as they allow the selection of linear isotactic polypropylene (based on  $M_w$  or  $\eta_{E,U,min}$ ) and processing temperature to minimize the non-uniformity of fibers produced, captured here via *CV*. The term "non-uniform" fibers refers to the width of the fiber diameter distribution, the pore size distribution and the structural anisotropy of the meltblown nonwoven fabrics. For example, in the field of filtration (i.e. for HVCA filters, HEPA filters, ULPA filters, medical face-mask, respiratory filters and dry and liquid aerosol filters), the presence of highly non-uniform fibers is intolerable because large fiber diameter changes lead to a wider pore size distribution and formation of more anisotropic structures, which reduces the mechanical and filtration properties of nonwovens [58, 59].

It is interesting to note that extensional thickening has been quite well studied in film blowing process for polyolefins and one could see a similarity with results obtained in this work for melt blowing process. In particular, the observation that there are optimal values for extensional thickening and melt strength with respect to the stability window size. The key difference seems

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to be the mechanism in which the extensional thickening (i.e. the friction) is induced in both processes, because the strain rates are very different. At low strain rates, which are typical for film blowing process (i.e. when the flow starts to orient the primitive path of the molecules), stabilizing extensional thickening can be induced by adding long side branches to the polymer [60]. However, at very high extensional strain rates, which are typical for the melt blowing process (i.e. when chain stretch occurs), extensional thickening can occur even for linear polymers, as long as the coefficient of friction remains high enough. Thus, it can be expected that different monomer chemistries can be used to control high extensional rheology by varying the friction coefficient at very high extensional rates to stabilize the melt blowing process considerably.

### CONCLUSION

In this work, three linear isotactic polypropylenes having different  $M_w$  (56, 64 and 76 kg/mol) and a comparable polydispersity  $M_w/M_n$  (3.95 – 4.41) were used for the production of nonwovens by melt blowing technology at two different temperatures (250 °C and 270 °C) in order to understand role of  $M_w$  and T on the fiber diameter distribution. Melt elasticity was evaluated using the reptation-mode relaxation time,  $\lambda_I$ , and the Rouse-mode reorientation time,  $\lambda_2$ , determined from shear viscosity data covering a very wide range of shear rate (10 – 10<sup>7</sup> 1/s). Extensional rheology was assessed by the strain rate dependent uniaxial extensional viscosity (estimated from the entrance pressure drop using the Gibson method). Obtained plateau value of uniaxial extensional viscosity at the highest extensional strain rates,  $\eta_{E,\infty}$ , (normalized by the three times zero-shear rate viscosity,  $\eta_0$ ) and the minimum uniaxial extensional viscosity,  $\eta_{E,U,min}$  were related to  $M_w$  and Tusing simple analytical equations. The basic morphological characteristics of the produced

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nonwoven samples were determined by digital image analysis of SEM images considering three different magnifications for the capture of nanofibers and microfibers. The obtained data were combined with relevant literature data for linear isotactic polypropylenes having the  $M_w$  between 26 - 224 kg/mol processed by the melt blowing technology over a wide temperature range (180 – 260 °C).

It has been found that firstly, the chosen reptation-mode relaxation time,  $\lambda_1$ , and the Rousemode reorientation time,  $\lambda_2$ , show (in the power-law dependency with  $M_w$ ) a slope of about 3.14 and 1.35, respectively, indicating that  $\lambda_1$  and  $\lambda_2$  characterize elasticity of the melt in highly entangled and almost disentangled states. Second, the extensional viscosity for all three samples decreases with increasing extensional strain rate to its minimum value,  $\eta_{E,U,min}$ , at 20 000 – 200 000 1/s, and then increases to plateau value,  $\eta_{E,\infty}$  at approximately  $2\times10^6$  1/s. Third, the decrease in  $M_w$  widens the region at  $\eta_{E,U,min}$ , where the extensional viscosity depends very weakly on the extensional strain rate. Fourth,  $\eta_{E,U,min}$  shows a slope of 1.58 in the power-law dependency with  $M_w$  (which is comparable to the value of 1.35 for  $\lambda_2$ ), but the dependence of  $\eta_{E,U,\infty}$  on  $M_w$  was found to be very weak, as deduced from very low power-law exponent - equal to 0.1. Fifth, there is a critical  $M_w$ , below which the extensional strain hardening starts to occur at very high strain rates (  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  >1).  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  was related to  $M_w$  and temperature using a simple power-law equation.

Interestingly,  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  was found to be inversely proportional to  $M_w$  and temperature. Finally, it was shown that the stability of fibers production captured by *CV* is complex, depending exclusively on the extensional properties of polypropylene melts, namely  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  and  $\eta_{E,U,min}$ . The existence of

optimal conditions under which the CV is minimal was attributed to the opposite trends of these

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inis is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0020773 two parameters with  $M_w$  and T. Simple mathematical formulas were provided to determine these optimum conditions.

The current understanding for linear isotactic PP melts was that decreased  $M_w$  or increased T (i.e. decreased  $\lambda_I$  or increased  $\lambda_2/\lambda_I$ ) increases CV [9, 15]. This work has shown that this trend is valid only in a certain range of  $M_w$  and T (i.e. in zone I and III in Figures 18 – 19) and that there are process conditions in which a decrease in  $M_w$  (or increase in T) can significantly reduce CV (zone II in Figures 18 – 19) due to the extensional strain hardening, which begins to appear at very high extensional strain rates (i.e. if  $1 < \frac{\eta_{E,U,\infty}}{3\eta_0} \le 4$ ). Since the optimal value for  $\frac{\eta_{E,U,\infty}}{3\eta_0}$  was found to be about 4, one can use Eq. 13 to determine the lowest possible  $M_w$  (for a given temperature), at which the CV is considerably minimized. These findings are particularly important with respect to the stable production of polymeric nanofibers by melt blowing technology, in which low molecular weight polymers and high temperatures are needed to reduce the fiber diameter to the desired level.

### SUPPLEMENTARY MATERIAL

See supplementary material for further details on the determination of average fiber diameter and coefficient of variation from digitized histograms taken from the open literature.

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### DATA AVAILABILITY

The data that supports the findings of this study are available within the article [and its supplementary material].

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Sample Name	Mn (g/mol)	M <sub>w</sub> (g/mol)	Mz (g/mol)	M <sub>z+1</sub> (g/mol)	M <sub>w</sub> /M <sub>n</sub> (-)	<b>η</b> ₀ (Pa·s) T= 230 °C	η∞ (Pa·s) T= 230 °C	E₀ (kJ/mol)	E∞ (kJ/mol)
HL504FB	17200	75850	165500	278000	4.41	22.80	0.229		
HL508FB	14650	63750	138000	235500	4.35	11.27	0.199	56.590	25.204
HL512FB	14250	56250	114500	187500	3.95	7.79	0.165		

**TABLE 1** Basic characteristics of used linear isotactic polypropylene melts (processed samples) taken from [42, 43].

**TABLE 2** Rheological parameters determined from shear ( $\lambda_1$ ,  $\lambda_2$ , n) and uniaxial extensional viscositites ( $\lambda_s$ ,  $\eta_{E,min}$ ,  $\eta_{E,U,\mathscr{A}}(3\eta_0)$ ) measured over a very wide rate range of strain rates for linear isotactic polypropylenes at 230 °C.

Sample Name	λ <sub>1</sub> (ms)	λ₂ (μs)	n (-)	λ <sub>s</sub> (μs)	η <sub>ε,υ,min</sub> (Pa·s)	η <sub>ε,υ,∞</sub> /(3η₀) (-)	
HL504FB	1.201923	0.585	0.3964	4.123	24.95	0.9898	
HL508FB	0.706714	0.491	0.4445	4.600	18.95	1.8243	
HL512FB	0.469484	0.388	0.4569	5.005	15.55	2.8337	

**TABLE 3** Basic rheological characteristics shifted to the meltblown processing temperature via Arrhenius shift factor together with the corresponding coefficient of variation and air volume flow rate to achieve an average fiber diameter about  $1.5\mu m$ . The processing conditions were as follows: orifice diameter: 0.4 mm; number of holes per active part: 470; collector belt speed: 5 m/min, dieto-collector distances: 500 mm; mass flow rate for one orifice: 0.0885 g/hole/min.

Material	T <sub>Die</sub> (°C)	λ <sub>1</sub> (s)	λ₂/λı (-)	η <sub>ε,υ,∞</sub> /(3η₀) (-)	CV (%)	Standard deviation (%)	Air volume flow rate (m <sup>3</sup> /hod)
PP	250	0.0007197	0.0006571	1.3186371	55.35	1.4000	520
Borflow HL504FB	270	0.0004457	0.0008571	1.7199753	54.85	1.3450	410
PP Borflow	250	0.0004171	0.0008966	2.4303743	54.72	0.6400	400
HL508FB	270	0.0002583	0.0011695	3.1700790	51.56	1.9250	320
PP	250	0.0002816	0.0011215	3.7750415	44.88	0.7400	340
HL512FB	270	0.0001744	0.0014629	4.9240070	60.31	2.3850	250

**TABLE 4** Summary of basic rheological characteristics shifted to the meltblown processing temperature via the Arrhenius shift factor together with the average fiber diameter, the corresponding coefficient of variation and given meltblown processing conditions for linear isotactic polypropylenes, which are taken from the open literature.

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Material	T <sub>Die</sub> (°C)	M <sub>w</sub> (g/mol)	λ <sub>1</sub> (s)	λ <sub>2</sub> /λ <sub>1</sub> (-)	η <sub>ε,υ,∞</sub> /(3η₀) (-)	D <sub>Fiber</sub> (μm)	CV (%)	CV <sub>AV</sub> (%)	Standard deviation (%)	DCD (mm)	Throughput (gram/hole/min)	D <sub>Die</sub> (mm)	Notes (-)	Reference
						0.570	37			250			-	
						0.560	21			300				
	240	0 224 000**	0.010256517	0.000104533	0.040592104	0.550	31	27.02	6.600	350	0.022	0 1 2 5 4		F1 F2
PP	240		0.018256517			0.590	19	27.83		300		0.1254	70+	51, 52
						0.560	21						100+	
						0.520	38						140+	
PP PD3495G	260	110 000**	0.001190822	0.000491386	0.653056944	1.980 1.900	33.71 29.30	31.51	2.205	305	0.8	0.381	Setback Face gap	53
PP DAELIM	240	103 000**	0.001593351	0.000419407	0.624548899	1.2-1.5 <sup>c</sup>	57.17	57.17	-	150	-	0.5		54
PP HL512FB	242	90950**	0.001024086	0.000539099	0.995593645	1.067 <sup>d</sup>	46.71 <sup>d</sup>	46.71	-	80	0.03	0.125	Air flow 300 m³/hod	55
PP Exxon 3746G	220	59 000**	0.00047464	0.000842943	3.291381832	0.300	19.89	19.89	-	550	0.035	0.2	L/D = 10	10
PP Exxon, Achieve <sup>™</sup> 230 6936G	220	60.000**	0.000280212	0.000052401	2 612108141	0.780	29.08 <sup>e</sup>	24.04	2 720	250	0.025	0.1254	AGR die	die
	60 000	0.000380313	0.000952401	3.012198141	0.810	34.54 <sup>e</sup>	31.81	2.730	250	0.025	0.01778	HILL die	50	
PP Exxon, Achieve <sup>™</sup> 24		240 60 000**	0.00029218	0.001102349	4.180909757	0.636 <sup>f</sup>	5.71 <sup>f</sup>	6.55	1.241		0.025 0.050 0.1	0.178	-	16
	240					0.867 <sup>f</sup>	8.30 <sup>f</sup>			190				
6936G						1.153 <sup>f</sup>	5.64 <sup>f</sup>							
PP*	200	41 564***	0.000430758	0.000898719	5.10594663	0.767 <sup>g</sup>	75.40 <sup>g</sup>	72.08	3.321	400			Water 5ª	
				0.0000007.20	5.1055 1005	0.913 <sup>g</sup>	68.76 <sup>g</sup>	72.00		200				
			* 0.000408739	0.000925989	5.41524221	0.634 <sup>g</sup>	79.41 <sup>g</sup>	75.46	3.439	200			Water 10 <sup>ª</sup>	
PP*	200	40 875***				0.632 <sup>g</sup>	71.02 <sup>g</sup>			300				
						0.570 <sup>s</sup>	75.95 <sup>®</sup>			400				
PP*	190	190         33 945***           190         33 708***	3 945***       0.000311233         3 708***       0.000304463	0.001086607	8.76332668	0.620 <sup>s</sup>	69.97 <sup>®</sup>	68.98 72.47	0.983	300			Water 10 <sup>a</sup>	
						0.6098	68.00°			400				
PP*	190			0.001100307	8.98203401	0.483*	73.45°		0.978	200	400		Water 5 <sup>ª</sup>	1
						0.430°	71.50°			400				
<b>DD</b> *	100	20.001***	0.000221744	0.001395405	12 1062166	0.797*	71.98°	75.24	2.729	300	1.33	0.5	Nitrogon 10 <sup>b</sup>	61
PP*	190	30 901	0.000231744	0.001285405	12.1903100	0.743	78.03°						Nitrogen 10	
				0.001379586	14.0167182	0.728*	75.06° 84.248	80.14	2.052	200				
DD*	100	20 202***	0.000204694			0.838	79 70 8			200			Air 10 <sup>b</sup>	
FF	190	29 /03****				0.735	77.408		2.952	400			All 10	
PP* 180			0.000211429	0.001361019	16.2421239	0.735	63.998	66.85	2.624	200				
	180	27 065***				0.670 <sup>g</sup>	66.22 <sup>g</sup>			300			Nitrogen 10 <sup>b</sup>	
	100					0.622 g	70.33 <sup>g</sup>	00.05		400				
						0.699 <sup>g</sup>	66.12 <sup>g</sup>			300	1			
PP*	180	26 158***	0.000189976	0.001446561	18.3116090	0.631 <sup>g</sup>	72.44 <sup>g</sup>	69.28	3.159	400	1		Air 10 <sup>b</sup>	

PP were synthesized by the chain scission of the base polymer (Moplen 241R with a MFI of 30 from Lyondellbasell) using radical initiator (combination of 2, 5 dimethyl hexane and 2, 5 bis(tert-butyl peroxide) commonly known as DHBP.

\*\* M<sub>w</sub> values for polymer pellets

\*\*\* M<sub>w</sub> values for processed samples

+ Airflow pressure (kPa)

a ml/min

\*

b g/min

c taken from the histogram visualized in Figure 9 (a) in [53]

d digitized from the histogram visualized in Figure 7 (b) in [54] (see supplementary material [45])

- digitized from the histogram visualized in Figure 6 in [55] (see supplementary material [45]) taken from the Figure 3 in [16] е
- f
- taken from the Figure 8.13 in [59] g

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Figure 1 Scheme of the meltblown process. [62, 63]



Figure 2 Determination of the reptation-mode relaxation time,  $\lambda_1$ , and the Rouse-mode reorientation time,  $\lambda_2$ , at 230 °C for three linear isotactic polypropylenes with  $M_w = 76 \text{ kg/mol}$  (top),  $M_w = 64 \text{ kg/mol}$  (middle) and  $M_w = 56$ kg/mol (bottom). The corresponding coefficient of determination, R<sup>2</sup>, for the power-law model used to fit the different number of points in the pseudoplastic region is shown on the right. Experimental data taken from [42].

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**Figure 3** Reifenhäuser Reicofil pilot plant meltblown line (top - general view, bottom - Multimedia view).

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**Figure 4** Reptation-mode relaxation time,  $\lambda_1$ , and Rouse-mode reorientation time,  $\lambda_2$ , plotted as a function of weight-average molecular weight,  $M_w$ , for linear isotactic polypropylene at 230 °C.

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**Figure 5** Uniaxial extensional viscosity,  $\eta_{E,U}$ , plotted as a function of the extensional strain rate (top) and chain stretch Weissenberg number (bottom) at 230 °C for three linear isotactic polypropylenes differing in weight-average molecular weight.

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**Figure 6** The plateau value of uniaxial extensional viscosity at the highest extensional strain rates,  $\eta_{E,\infty}$ , and the minimum uniaxial extensional viscosity,  $\eta_{E,U,min}$ , plotted as a function of weigh-average molecular weight,  $M_w$ , for linear isotactic polypropylene at 230 °C. In this case, T and  $T_r$  are equal to 503.15 K (i.e. 230 °C).



**Figure 7** Uniaxial extensional viscosity,  $\eta_{E,U}$ , normalized by the three times zero-shear rate viscosity,  $\eta_0$ , plotted as a function of the extensional strain rate at 230 °C for three linear isotactic polypropylenes differing in weight-average molecular weight.

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**Figure 8** The plateau value of uniaxial extensional viscosity at the highest extensional strain rates,  $\eta_{E,U,\infty}$ , normalized by the three times zero-shear rate viscosity,  $\eta_0$ , (i.e. the extensional strain hardening at the maximum chain stretch) plotted as a function of weigh-average molecular weight,  $M_w$ , for linear isotactic polypropylene at 230 °C. The lines represent predictions of Eq.12 for different temperatures by using the flow activation energies given in Table 1.

# HL504FB



**Figure 9** SEM images for L-PP sample (HL504FB), T = 250 °C, belt speed 5 m/min and DCD = 500 mm at two different areas and different magnifications (left –  $500 \times$ , middle –  $1000 \times$ , right –  $2500 \times$ ) together with corresponding final overall fiber diameter distribution.



**Figure 10** SEM images for L-PP sample (HL504FB), T = 270 °C, belt speed 5 m/min and DCD = 500 mm at two different areas and different magnifications (left – 500×, middle – 1000×, right – 2500×) together with corresponding final overall fiber diameter distribution.

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# HL508FB



**Figure 11** SEM images for L-PP sample (HL508FB), T = 250 °C, belt speed 5 m/min and DCD = 500 mm at two different areas and different magnifications (left –  $500 \times$ , middle –  $1000 \times$ , right –  $2500 \times$ ) together with corresponding final overall fiber diameter distribution.



**Figure 12** SEM images for L-PP sample (HL508FB), T = 270 °C, belt speed 5 m/min and DCD = 500 mm at two different areas and different magnifications (left – 500×, middle – 1000×, right – 2500×) together with corresponding final overall fiber diameter distribution.

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# HL512FB



**Figure 13** SEM images for L-PP sample (HL512FB), T = 250 °C, belt speed 5 m/min and DCD = 500 mm at two different areas and different magnifications (left –  $500 \times$ , middle –  $1000 \times$ , right –  $2500 \times$ ) together with corresponding final overall fiber diameter distribution.



**Figure 14** SEM images for L-PP sample (HL512FB), T = 270 °C, belt speed 5 m/min and DCD = 500 mm at two different areas and different magnifications (left – 500×, middle – 1000×, right – 2500×) together with corresponding final overall fiber diameter distribution.

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**Figure 15** Coefficient of fiber diameter variation, *CV*, plotted as a function of the reptation-mode relaxation time,  $\lambda_1$ .

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**Figure 16** Coefficient of fiber diameter variation, *CV*, versus the ratio of the Rouse-mode reorientation time,  $\lambda_2$ , and the reptation-mode relaxation time,  $\lambda_1$ .

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**Figure 17** Coefficient of fiber diameter variation, *CV*, versus the maximum strain hardening in uniaxial extension,  $\eta_{E,U,\infty}/(3\eta_0)$ .

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**Figure 18** Influence of temperature on critical weight-average molecular weight,  $M_w$ , to achieve the given maximum strain hardenings in uniaxial extension,  $\eta_{E,U,\omega}/(3\eta_0)$ , according to Eq. 13 and the flow activation energies provided in Table 1.

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**Figure 19** Influence of temperature on critical minimum uniaxial extensional viscosity,  $\eta_{E,U,min}$ , to reach the given maximum strain hardenings in uniaxial extension,  $\eta_{E,U,\infty}/(3\eta_0)$  according to Eq.14 and the flow activation energies provided in Table 1.