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Predictable Properties of Fitness Landscapes Induced by Adaptational Tradeoffs

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Abstract Fitness effects of mutations depend on environmental parameters. For example, mutations that increase fitness of bacteria at high antibiotic concentration often decrease fitness in the absence of antibiotic, exemplifying a tradeoff between adaptation to environmental extremes. We develop a mathematical model for fitness landscapes generated by such tradeoffs, based on experiments that determine the antibiotic dose-response curves of *Escherichia coli* strains, and previous observations on antibiotic resistance mutations. Our model generates a succession of landscapes with predictable properties as antibiotic concentration is varied. The landscape is nearly smooth at low and high concentrations, but the tradeoff induces a high ruggedness at intermediate antibiotic concentrations. Despite this high ruggedness, however, all the fitness maxima in the landscapes are evolutionarily accessible from the wild type. This implies that selection for antibiotic resistance in multiple mutational steps is relatively facile despite the complexity of the underlying landscape.

Introduction

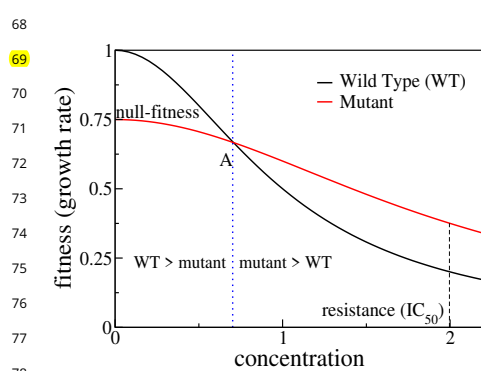
Sewall Wright introduced the concept of fitness landscapes in 1932 (*Wright, 1932*), and for decades afterwards it persisted chiefly as a metaphor, due to lack of sufficient data. This has changed considerably in recent decades (*de Visser and Krug, 2014; Hartl, 2014; Kondrashov and Kondrashov, 2015; Fragata et al., 2019*). There are now a large number of experimental studies that have constructed fitness landscapes for combinatorial sets of mutations relevant to particular phenotypes, such as the resistance of **microbial pathogens** to antibiotics (*Weinreich et al., 2006; DePristo et al., 2007; Marcusson et al., 2009; Lozovsky et al., 2009; Brown et al., 2010; Schenk et al., 2013; Goulart et al., 2013; Mira et al., 2015; Palmer et al., 2015; Knopp and Andersson, 2018*), and the genomic scale of these investigations is rapidly growing (*Wu et al., 2016; Bank et al., 2016; Domingo et al., 2018; Pokusaeva et al., 2019*). Mathematical modeling of fitness landscapes has also seen a revival, motivated partly by the need to quantify and interpret the ruggedness of empirical fitness landscapes (*Szendro et al., 2013; Weinreich et al., 2013; Neidhart et al., 2014; Ferretti et al., 2016; Blanquart and Bataillon, 2016; Crona et al., 2017; Hwang et al., 2018; Kaznatcheev, 2019; Crona, 2020*). Conceptual breakthroughs, such as the notion of sign epistasis (where a mutation is beneficial in some genetic backgrounds but deleterious in others), have shed light on how ruggedness can constrain evolutionary trajectories (*Weinreich et al., 2005; Poelwijk et al., 2007, 2011; Franke et al., 2011; Lobkovsky and Koonin, 2012; Zagorski et al., 2016*).

Despite this progress, a limitation of current studies of fitness landscapes is that they focus

41 mostly on $G \times G$ (gene-gene) interactions, and little on $G \times G \times E$ (where E stands for environment)
 42 interactions, i.e on how changes in environment modify gene-gene interactions. A few recent
 43 studies have begun to address this question (Flynn et al., 2013; Taute et al., 2014; Gorter et al.,
 44 2018; de Vos et al., 2018). In the context of antibiotic resistance, it has been realized that the fitness
 45 landscape of resistance genes depends quite strongly on antibiotic concentration (Mira et al., 2015;
 46 Stiffler et al., 2015; Ogbunugafor et al., 2016). This is highly relevant to the clinical problem of
 47 resistance evolution, since concentration of antibiotics can vary widely in a patient's body as well
 48 as in various non-clinical settings (Kolpin et al., 2004; Andersson and Hughes, 2014). Controlling
 49 the evolution of resistance mutants thus requires an understanding of fitness landscapes as a
 50 function of antibiotic concentration. Empirical investigations of such scenarios are still limited, and
 51 systematic theoretical work on this question is also lacking.

52 In the present work, we aim to develop a theory of $G \times G \times E$ interactions for a specific class of
 53 landscapes, with particular focus on applications to antibiotic resistance. The key feature of the
 54 landscapes we study is that every mutation comes with a tradeoff between adaptation to the two
 55 extremes of an environmental parameter. For example, it has been known for some time that
 56 antibiotic resistance often comes with a fitness cost, such that a bacterium that can tolerate high
 57 drug concentrations grows slowly in drug-free conditions (Andersson and Hughes, 2010; Melnyk
 58 et al., 2015). While such tradeoffs are not universal (Hughes and Andersson, 2017; Durão et al.,
 59 2018), they certainly occur for a large number of mutations and a variety of drugs.

60 Tradeoffs can also arise in complex scenarios involving multiple drugs. It has been reported
 61 in Stiffler et al. (2015) that certain mutations in TEM-1 β -lactamase are neutral at low ampicillin
 62 concentration but deleterious at high concentration, and that a number of the latter mutations
 63 also confer resistance to cefotaxime. Therefore in a medium with cefotaxime and a moderately
 64 high concentration of ampicillin, it is possible that these mutations will be deleterious at low
 65 cefotaxime concentrations but beneficial at high cefotaxime concentration. Fitness landscapes
 66 with adaptational tradeoffs are therefore also of potential relevance to evolution in response to
 67 multi-drug combinations.



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 79 **Figure 1.** Schematic showing dose response
 80 curves of a wild type and a mutant. To the left
 81 of the intersection point A the wild type is
 82 selected over the mutant, whereas to the right
 83 of A the mutant is selected.

84
 85
 86 swapping the rank order between the two fitness values. The intersection point is known as the
 87 minimum selective concentration (MSC), and it defines the lower boundary of the mutant selection
 88 window (MSW) within which the resistance mutant has a selective advantage relative to the wild
 89 type (Khan et al., 2017; Alexander and MacLean, 2018).

90 When there are several possible mutations and multiple combinatorial mutants, a large number
 91 of such intersections occur as the concentration of the antibiotic increases. This leads to a succes-

Our starting point for understanding these landscapes is the knowledge of two phenotypes that are well studied – the drug-free growth rate (which we call the null-fitness) and the IC_{50} (the drug concentration that reduces growth rate by half), which is a measure of antibiotic resistance. These two phenotypes correspond to the two extreme regimes of an environmental parameter, i.e zero and highly inhibitory antibiotic concentrations. The function that describes the growth rate of a bacterium for antibiotic concentrations between these two extremes is called the dose-response curve or the inhibition curve (Regoes et al., 2004). When tradeoffs are present, the dose-response curves of different mutants must intersect as the concentration is varied (Gullberg et al., 2011). This is schematically shown in Figure 1. The intersection of dose-response curves of the wild type and the mutant happen at point A,



92 sion of different fitness landscapes defined over the space of genotype sequences (Maynard Smith,
 93 1970; Kauffman and Levin, 1987). Whenever the curves of two mutational neighbors (genotypes
 94 that differ by one mutation) intersect, there can be an alteration in the evolutionary trajectory
 95 towards resistance, whereby a forward (reverse) mutation now becomes more likely to fix in the
 96 population than the corresponding reverse (forward) mutation. These intersections change the
 97 ruggedness of landscapes and the accessibility of fitness maxima. In this way a rich and complex
 98 structure of selective constraints emerges in the MSW. To explore the evolutionary consequences
 99 of these constraints, we construct a theoretical model based on existing empirical studies as well
 100 as our own work on ciprofloxacin resistance in *E. coli*. Specifically, we address two fundamental
 101 questions: (i) How does the ruggedness of the fitness landscape vary as a function of antibiotic
 102 concentration? (ii) How accessible are the fitness optima as a function of antibiotic concentration?

103 We find that even when the null-fitness and resistance values of the mutations combine in
 104 a simple, multiplicative manner, the intersections of the curves produce a highly epistatic land-
 105 scape at intermediate concentrations of the antibiotic. This is an example of a strong $G \times G \times E$
 106 interaction, where changes in the environmental variable drastically alter the interactions between
 107 genes. Despite the high ruggedness at intermediate concentrations, however, the topology of
 108 the landscapes is systematically different from the oft-studied random landscape models, such as
 109 the House-of-Cards model (Kauffman and Levin, 1987; Kingman, 1978), the Kauffman NK model
 110 (Kauffman and Weinberger, 1989; Hwang et al., 2018) or the Rough Mt. Fuji model (Neidhart et al.,
 111 2014). For example, most fitness maxima have similar numbers of mutations that depend logarith-
 112 mically on the antibiotic concentration. Importantly, all the fitness maxima remain highly accessible
 113 through adaptive paths with sequentially fixing mutations. In particular, any fitness maximum
 114 (including the global maximum) is accessible from the wild type as long as the wild type is viable. As
 115 a consequence, the evolution of high levels of antibiotic resistance by multiple mutations (Hughes
 116 and Andersson, 2017; Wistrand-Yuen et al., 2018; Rehman et al., 2019) is much less constrained by
 117 the tradeoff-induced epistatic interactions than might have been expected on the basis of existing
 118 models.

119 Results

120 Mathematical model of tradeoff-induced fitness landscapes

121 The chief goal of this paper is to develop and explore a mathematical framework to study tradeoff-
 122 induced fitness landscapes. We consider a total of L mutations, each of which increases antibiotic
 123 resistance. A fitness landscape is a real-valued function defined on the set of 2^L genotypes made
 124 up of all combinations of these mutations. A genotype can be represented by a binary string of
 125 length L , where a 1 (0) at each position represents the presence (absence) of a specific mutation.
 126 Alternatively, any genotype is uniquely identified as a subset of the L mutations (the wild type is the
 127 null subset, i.e the subset with no mutations).

128 In this paper, unless mentioned otherwise, we define the fitness f as the exponential growth
 129 rate of a microbial population. The fitness is a function of antibiotic concentration. This function has
 130 two parameters of particular interest to us – the growth rate at zero concentration, which we refer
 131 to as the null-fitness and denote by r , and a measure of resistance such as IC_{50} which we denote
 132 by m . Each single mutation is described by the pair (r_i, m_i) , where r_i and m_i are the null-fitness and
 133 resistance values respectively of the i th single mutant. We further rescale our units such that for
 134 the wild type, $r = 1$ and $m = 1$. We consider mutations that come with a fitness-resistance tradeoff,
 135 i.e a single mutant has an increased resistance ($m_i > 1$) and a reduced null-fitness ($r_i < 1$) compared
 136 to the wild type. To proceed we need to specify two things: (i) how the fitness of the wild type and
 137 the mutants depend on antibiotic concentration, and in particular if this dependence exhibits a
 138 pattern common to various mutant strains; (ii) how the r and m values of the combinatorial mutants
 139 depend on those of the individual mutations. To address these issues we take guidance from two
 140 empirical observations.

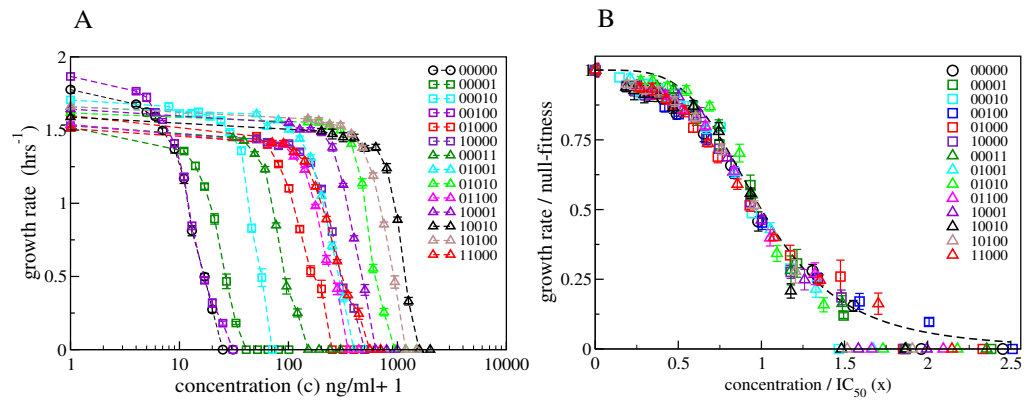


Figure 2. Dose-response curves for *E. coli* in the presence of ciprofloxacin. Each binary string corresponds to a strain, where the presence (absence) of a specific mutation in the strain is indicated by a 1(0). The five mutations in order from left to right are S83L (*gyrA*), D87N (*gyrA*), S80I (*parC*), $\Delta marR$, and $\Delta acrR$. The names of the strains are given in Table 1 in Materials and Methods. **(A)** Dose-response curves of the wild type, the five single mutants and eight double mutants. Unlike the experiments reported in *Marcusson et al. (2009)*, the mutants were grown in isolation rather than in competition with the wild type. **(B)** The same curves, but scaled with the null-fitness and IC_{50} of each individual genotype. The dashed black line is the Hill function $(1 + x^4)^{-1}$.

141 Scaling of dose-response curves

142 *Marcusson et al. (2009)* have constructed a series of *E. coli* strains with single, double and triple
 143 mutations conferring resistance to the fluoroquinolone antibiotic ciprofloxacin (CIP), which inhibits
 144 DNA replication (*Drlica et al., 2009*). In their study they measured MIC (minimum inhibitory con-
 145 centration) values and null-fitness but did not report dose-response curves. Some of the present
 146 authors have recently shown that the dose-response curve of the wild-type *E. coli* (strain K-12
 147 MG1655) in the presence of ciprofloxacin can be fitted reasonably well by a Hill function (*Ojkic et al.,*
 148 **2019**).

149 Here we expand on this work and determine dose-response curves for a range of single- and
 150 double-mutants with mutations restricted to five specific loci known to confer resistance to CIP
 151 (*Marcusson et al., 2009*) (see Materials and Methods). Figure 2A shows the measured curves for
 152 the wild type, the five single mutants, and eight double-mutant combinations. The genotypes are
 153 represented as binary strings, where a 1 or 0 at each position denotes respectively the presence or
 154 absence of a particular mutation. If we rescale the concentration c of CIP by IC_{50} of the corresponding
 155 strain, $x = c/IC_{50}$, and the growth rate by the null-fitness $f(0)$, the curves collapse to a single curve
 156 $w(x)$ that can be approximated by the Hill function $(1 + x^4)^{-1}$ (Figure 2B). The precise shape of the
 157 curve is not important for further analysis. However, the data collapse suggests that we can assume
 158 that the dose-response curve of a mutant with (relative) null-fitness r and (relative) resistance m is

$$f(c) = rw(c/m), \quad (1)$$

159 i.e. it has the same shape as the wild-type curve w except for a rescaling of the fitness and con-
 160 centration axes. Similar scaling relations have been reported previously by *Wood et al. (2014)* and
 161 *Chevreau et al. (2015)*. A good biological understanding of the conditions underlying this feature is
 162 presently lacking, but it seems intuitively plausible that the shape $w(x)$ would be robust to changes
 163 that do not qualitatively alter the basic physiology of growth and resistance.

164 Limited epistasis in r and m

165 An interesting recent finding reported by *Knopp and Andersson (2018)* is that chromosomal re-
 166 sistance mutations in *Salmonella typhimurium* mostly alter the null-fitness as well as the MIC of
 167 various antibiotics in a non-epistatic, multiplicative manner, i.e. if a particular mutation increases
 168 (decreases) the resistance (null-fitness) by a factor k_1 , and another mutation does the same with
 169 a factor k_2 , then the mutations jointly alter these phenotypes roughly by a factor of $k_1 k_2$ (with a

170 few exceptions). We have done a similar comparison for the data on the null-fitness and MIC for
 171 *E. coli* strains in *Marcusson et al. (2009)*. We have analyzed a subset of 4 mutations for which the
 172 complete data set for all combinatorial mutants is available from *Marcusson et al. (2009)*. The data
 173 are shown in Table 1. Out of 11 multiple-mutants, only 2 show epistasis in r and 4 show epistasis
 174 in m . Moreover, in all cases where significant epistasis occurs it is negative, i.e. the effect of the
 175 multiple mutants is weaker than expected from the single mutation effects.

176 Formulation of the model

177 The above observations suggest a model where one assumes, as an approximation, that all the
 178 r and m values of individual mutations combine multiplicatively. A genotype with n mutations
 179 $(r_1, m_1), (r_2, m_2), \dots, (r_n, m_n)$ has a null-fitness r and a resistance value m given by

$$r = \prod_{i=1}^n r_i \quad \text{and} \quad m = \prod_{i=1}^n m_i. \quad (2)$$

180 Moreover, the dose-response curves of the genotypes are taken to be of the scaling form (1),
 181 where the function $w(x)$ does not depend on the genotype. As indicated before, and without any
 182 loss of generality, we choose units such that, for the wild type, $r = 1$ and $m = 1$. Therefore the
 183 dose-response curve of the wild type is $w(x)$ with $w(0) = 1$, and choosing IC_{50} as a measure of
 184 resistance, we have $w(1) = \frac{1}{2}$. Henceforth, we refer to x simply as the concentration. We also recall
 185 that the condition of adaptational tradeoff means that $r_i < 1$ and $m_i > 1$ for all mutations.

186 If the r_i and m_i values combine non-epistatically, and if the shape of the dose-response curve is
 187 known, it is thus possible to construct the entire concentration-dependent landscape of size 2^L from
 188 just $2L$ measurements (of the r_i and m_i values of the single mutants) instead of the measurement
 189 of 2^L fitness values at every concentration. In practice we do not expect a complete lack of epistasis
 190 among all mutations of interest, and the dose-response curve is also an approximation obtained by
 191 fitting a curve through a finite set of fitness values known only with limited accuracy. However, the
 192 fitness rank order of genotypes, and related topographic features such as fitness peaks, are robust
 193 to a certain amount of error in fitness values (*Crona et al., 2017*), and our model may be used to
 194 construct these to a good approximation.

195 Lastly, we require that the dose-response curves of the wild type and a mutant intersect at most
 196 once, which implies that the equation $w(x) = rw\left(\frac{x}{m}\right)$ with $r > 1$ and $m < 1$ has at most one solution.
 197 This then also implies that the curves of any genotype σ and a proper superset of it (i.e. a genotype
 198 which contains all the mutations in σ and some more) intersect at most once. This property holds
 199 for all functions that have been used to represent dose-response curves in the literature, such as
 200 the Hill function, the half-Gaussian or the exponential function, as well as for all concave function
 201 with negative second derivate (see Materials and Methods for details).

202 **Properties of tradeoff-induced fitness landscapes**

203 To understand the evolutionary implications of our model, we first describe how the fitness land-
 204 scape topography changes with the environmental parameter represented by the antibiotic concen-
 205 tration. Next we analyze the properties of mutational pathways leading to highly fit genotypes.

206 Intersection of curves and changing landscapes

207 We start with a simple example of $L = 2$ mutations and a Hill-shaped dose-response curve $w(x) =$
 208 $\frac{1}{1+x^2}$ (Figure 3). At $x = 0$, the rank ordering is determined by the null-fitness. The wild type has
 209 maximal fitness, and the double mutant is less fit than the single mutants. As x increases, the
 210 fitness curves start to intersect, and each intersection switches the rank of two genotypes. In the
 211 present example we find a total of six intersections and therefore seven different rank orders
 212 across the full range of x . This is actually the maximum number of rank orders that can be found
 213 by scanning through x for $L = 2$, see Materials and Methods. The final fitness rank order (in the
 214 region G in Figure 3A) is the reverse of the original rank order at $x = 0$. Figure 3B depicts the

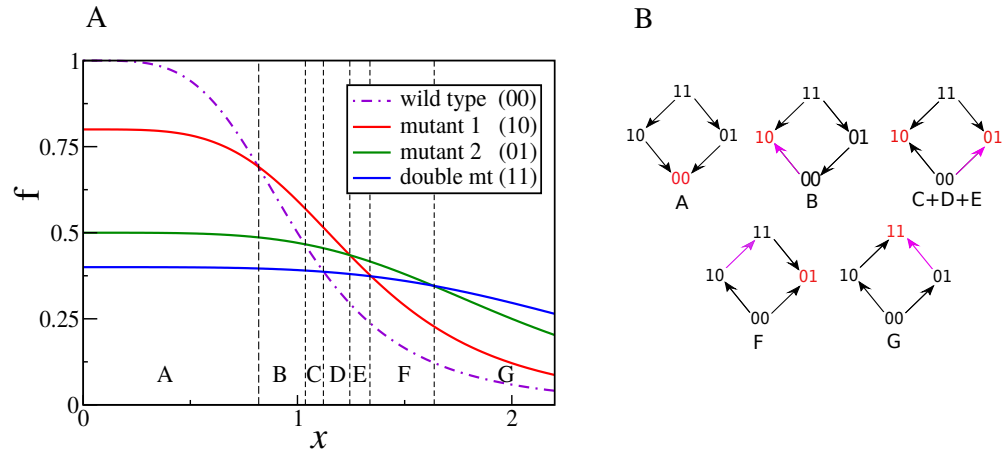


Figure 3. (A) An example of dose-response curves of four genotypes – the wild type (00), two single mutants (10 and 01), and the double mutant (11). The parameters of the two single mutants are $r_1 = 0.8$, $m_1 = 1.3$, $r_2 = 0.5$, $m_2 = 2.5$. Null-fitness and resistance combine multiplicatively, which implies that the parameters of the double mutant are $r_{12} = r_1 r_2 = 0.4$ and $m_{12} = m_1 m_2 = 3.25$. **(B)** Fitness graphs corresponding to antibiotic concentration ranges from panel **(A)**. The genotypes in red are the local fitness peaks. The purple arrows are the ones that have changed direction at the beginning of each segment. All arrows eventually switch from the downward to the upward direction.

215 concentration-dependent fitness landscape of the 2-locus system in the form of fitness graphs.
 216 A fitness graph represents a fitness landscape as a directed graph, where neighboring nodes are
 217 genotypes that differ by one mutation, and arrows point toward the genotypes with higher fitness
 218 (de Visser et al., 2009; Crona et al., 2013). A fitness graph does not uniquely specify the rank
 219 order in the landscape (Crona et al., 2017). For example, the three regions C, D and E have different
 220 rank orders but the same fitness graph. Because selection drives an evolving population towards
 221 higher fitness, a fitness graph can be viewed as a roadmap of possible evolutionary trajectories.
 222 In particular, a fitness peak (marked in red in Figure 3B) is identified from the fitness graph as
 223 a node with only incoming arrows. Fitness graphs also contain the complete information about
 224 the occurrences of sign epistasis. Sign epistasis with respect to a certain mutation occurs when
 225 the mutation is beneficial in some backgrounds but deleterious in others (Weinreich et al., 2005;
 226 Poelwijk et al., 2007). It is easy to read off sign epistasis for a mutation from the fact that parallel
 227 arrows (i.e. arrows corresponding to the gain or loss of the same mutation) in a fitness graph point
 228 in opposite directions.

229 For example, in the graph for the region B there is sign epistasis in the first position, since the
 230 parallel arrows $00 \rightarrow 10$ and $01 \leftarrow 11$ point in opposite directions. Notice that in the current example,
 231 we start with a smooth landscape at $x = 0$ (as seen in the fitness graph for region A), and the
 232 number of peaks and the degree of sign epistasis both reach a maximum in the intermediate region
 233 C+D+E. This fitness graph displays reciprocal sign epistasis, which is a necessary condition for the
 234 existence of multiple fitness peaks (Poelwijk et al., 2011). Beyond the region E, the landscape starts
 235 to become smooth again, with only one fitness maximum and a lower degree of sign epistasis. In
 236 the last region G, the landscape is smooth with only one peak (the double mutant 11) and no sign
 237 epistasis.

238 These qualitative properties generalize to larger landscapes. To show this, we consider a
 239 statistical ensemble of landscapes with L mutations, where the parameters r_i, m_i of single mutations
 240 are independently and identically distributed according to a joint probability density $P(r, m)$. Figure 4
 241 shows the result of numerical simulations of these landscapes for $L = 16$. The mean number of
 242 fitness peaks with n mutations reaches a maximum at $x_{\max}(n)$ where to leading order $\log x_{\max}(n) \sim$

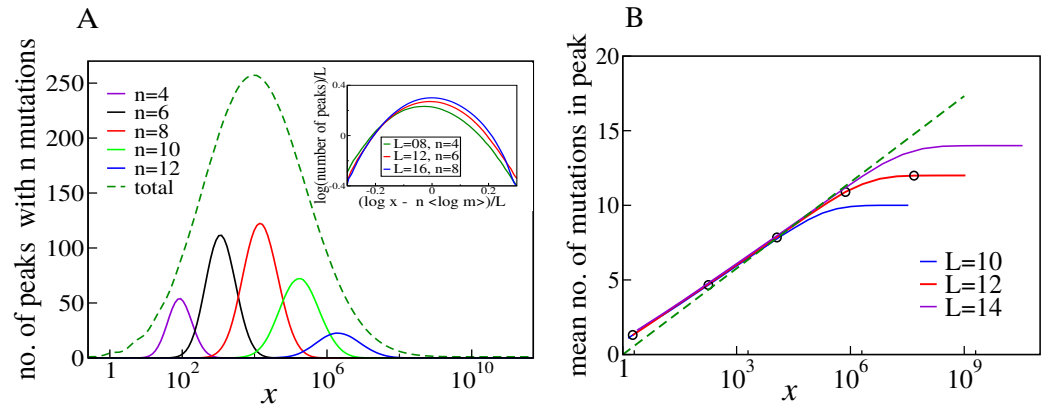


Figure 4. (A) Number of fitness peaks as a function of concentration for different numbers of mutations in the peak, n , and $L = 16$. The dashed green curve is the total number of fitness peaks, summed over n . The peaks were found by numerically generating an ensemble of landscapes with individual effects distributed according to the joint distribution (8). For this distribution, $\langle \log m \rangle = 1.19645$. Inset: The maximal number of peaks for a given value of n occurs at $\log x_{\max}(n) = n \langle \log m \rangle$, and grows exponentially with L . **(B)** Mean number of mutations in a fitness peak as a function of concentration x for the same model. The black circles are the mean number of mutations in the fittest genotype. The green dashed line is $\frac{\log(x)}{\langle \log m \rangle}$, where $\langle \log m \rangle = 1.19645$ as before.

243 $n \langle \log m \rangle$, independent of any further details of the system, as argued in Materials and Methods.
 244 The asymptotic expression works well already for $L = 16$ (see inset of Figure 4A). Figure 4B shows
 245 the mean number of mutations in a fitness peak. This is well approximated by the curve $n =$
 246 $\frac{\log x}{\langle \log m \rangle}$, showing that the mean number of mutations in a fitness peak grows logarithmically in the
 247 concentration. This is consistent with what we would expect from the variation in the number of
 248 peaks with n mutations as shown in Figure 4A. The existence of a typical number of mutations in a
 249 fitness peak is one of the distinctive features of our landscape, a feature typically lacking in other
 250 well-studied random landscape models. This property arises from the existence of adaptational
 251 tradeoffs. Since a high number of mutations is beneficial at higher concentrations but deleterious
 252 at lower concentrations, it is clear that there must be an optimal number of mutations at some
 253 intermediate concentration.

254 As another indicator of ruggedness, we consider the number of backgrounds in which a mutation
 255 is beneficial as a function of x . At $x = 0$, any mutation is deleterious in all backgrounds, whereas at
 256 very large x it is beneficial in all backgrounds. Therefore there is no sign epistasis in either case.
 257 Sign epistasis is maximized when a mutation is beneficial in exactly 1/2 of all backgrounds. Figure 5
 258 shows the mean number of backgrounds n_b (with n mutations each) in which the occurrence a
 259 mutation is beneficial, for two different values of n . The curves have a sigmoidal shape, starting from
 260 zero and saturating at $\binom{L}{n}$, which is the total number of backgrounds with n mutations. The blue
 261 curve shows the mean total number of backgrounds (with any n) in which a mutation is beneficial,
 262 which has a similar shape. Since every mutation in every background goes from being initially
 263 deleterious to eventually beneficial, there must be some x at which every mutation is beneficial in
 264 exactly half the backgrounds. The inset of Figure 5 shows that for backgrounds with n mutations,
 265 the average concentration at which a mutation is beneficial in 1/2 the backgrounds is given by
 266 $\log x \simeq n \langle \log m \rangle$, which is the same concentration at which the largest number of fitness peaks were
 267 found in Figure 4. A derivation of this relation is given in Materials and Methods. Similarly, when
 268 summed over all mutation numbers n , the fraction of beneficial backgrounds reaches 1/2 around
 269 the same concentration at which the total number of fitness peaks is maximal. Since the number of
 270 backgrounds is largest at $n = L/2$ for combinatorial reasons, this concentration is approximately
 271 given by $\log x \simeq \frac{L}{2} \langle \log m \rangle$.

272 **Complementary to these results about the background dependence of the sign of mutational**

effects, it can be shown that any two distinct sets of mutations occurring in any genetic background show sign epistasis at some value of x . This is a consequence of the rank ordering properties of the landscapes that are described in the next subsection (see Materials and Methods for a proof). A special case is that any two single mutations occurring in the wild type background must exhibit pairwise sign epistasis at some concentration.

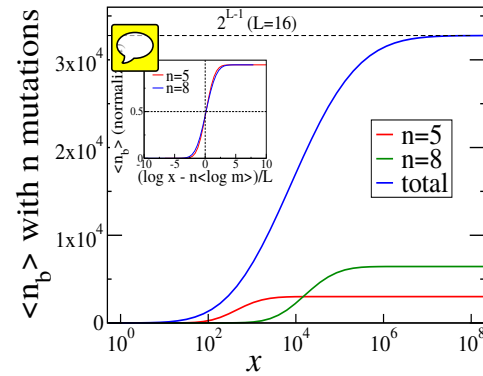


Figure 5. The mean number of genetic backgrounds n_b in which a mutation is beneficial depends on the concentration. The numerically computed mean number is shown in the blue curve. We also computed the mean n_b for genetic backgrounds with a fixed a number n of mutations. The results for two of these values, $n = 5$ and $n = 8$ are also shown. The inset shows these values of mean n_b as a fraction of the total number of backgrounds with n mutations.

path exists from the initial to the final genotype.

The accessibility of peaks in a fitness landscape is determined by the rank ordering of the genotypes. We now show that the rank orders of tradeoff-induced fitness landscapes are constrained in a way that gives rise to unusually high accessibility. Consider two distinct sets of **one or more** mutations A_i and A_j that can occur on the genetic background W , and the four genotypes W , $W A_i$, $W A_j$ and $W A_i A_j$, where a concatenation of symbols represents the genotype which contains all the mutations referred to by the symbols. The **ordering condition** (derived in Materials and Methods) says that whenever W is the fittest among these four genotypes, $W A_i A_j$ must be the least fit, and whenever $W A_i A_j$ is the fittest, W must be the least fit. For the case of two single mutations this situation is illustrated by the fitness graphs in Figure 3B, where the background genotype $W = 00$ is the fittest in the first segment A and the genotype $W A_i A_j = 11$ is the fittest in the last segment G. The ordering condition has the immediate consequence that **at all environments x** , the fittest genotype is *always* accessible from the background genotype W . If the fittest genotype is one of the **single mutants** (segments B, C, D and F), then it is of course accessible. If it is the **double mutant** $W A_i A_j$ (segment G), then the background genotype must be the least fit genotype (from the ordering condition), and therefore $W A_i$ and $W A_j$ should be fitter than W . Then $W A_i A_j$ is accessible from the wild type through the path $W \rightarrow W A_i \rightarrow W A_i A_j$ and the path $W \rightarrow W A_j \rightarrow W A_i A_j$.

To fully exploit the consequences of the ordering property we need to introduce some notation. Let σ be a genotype with n mutations. We define a *subset* of σ as a genotype with l mutations, $l \leq n$, which are all contained in σ as well. Likewise, a *superset* of σ is a genotype with l mutations, $l \geq n$, that contains all the mutations in σ . With this, the ordering condition can be seen to imply that the superset of a fitness peak is accessible from its own supersets. For example, if W is the fittest genotype, then $W A_i$ is a superset of it, and because of the ordering condition, $W A_i$ must be fitter than its superset $W A_i A_j$, and therefore accessible from it. Similarly, it is easy to show that the subset of a fitness peak is accessible from its own subsets. This property can be generalized and

Accessibility of fitness peaks

Having shown that tradeoff-induced fitness landscapes display a large number of fitness peaks at intermediate concentrations, we now ask how these peaks affect the evolutionary dynamics. We base the discussion on the concept of evolutionary accessibility, which effectively assumes a regime of weak mutation and strong selection (Gillespie, 1984). In this regime the evolutionary trajectory consists of a series of fixation events of beneficial single-step mutations represented by a directed path in the fitness graph of the landscape (Weinreich et al., 2005, 2006; Franke et al., 2011). We say that a genotype is *accessible* from another genotype if a directed

323 constitutes our main result on accessibility of fitness peaks.

324 **Accessibility property:** Any genotype Σ that is a superset of a local fitness peak σ is accessible from
 325 all the superset genotypes of Σ . Similarly, any genotype Σ' that is a subset of a local fitness peak σ is
 326 accessible from all the subset genotypes of Σ' .

327 The proof is given in Materials and Methods. Three particularly important consequences are

- 328 • Any fitness peak is accessible from all its subset and superset genotypes.
- 329 • **Any fitness peak is accessible from the wild type.** This is because the wild type is a subset
 330 of every genotype.
- 331 • For the same reason, when the wild type is a fitness peak (e.g., at $x = 0$), it is accessible from
 332 every genotype, and is therefore also the only fitness peak in the landscape. The same holds
 333 for the all-mutant when x is sufficiently large, since it is a superset of every genotype.

334 These properties are illustrated by the fitness graph in Figure 6. We assume in some environment x
 335 that the landscape has (at least) two peaks at the genotypes 1001 (marked in red) and 0111 (marked
 336 in blue). The colored arrows point towards mutational neighbors with higher fitness and are
 337 enforced by the accessibility property. The edges without arrowheads are not constrained by the
 338 accessibility property and the corresponding arrows (which are not shown in the figure) could point
 339 in either direction. Consider the genotype 0111 (marked in blue). It is accessible from all its subsets,
 340 namely 0000, 0010, 0010, 0001, 0110, 0101 and 0011, following the upward pointing blue arrows. These
 341 subsets are in turn accessible from their subsets. For example, 0011 is accessible from all its subsets
 342 – 0000, 0010, and 0001. The fitness peak is also accessible from its superset 1111. The same property
 343 holds for the other fitness peak. The subsets or supersets may access the fitness peaks using other
 344 (unmarked) paths as well, which would include one or more of the undirected lines in conjunction
 345 with some of the arrows. Moreover, other genotypes, which are neither supersets nor subsets, may
 346 also access these fitness peaks through paths that incorporate some of the undirected edges.

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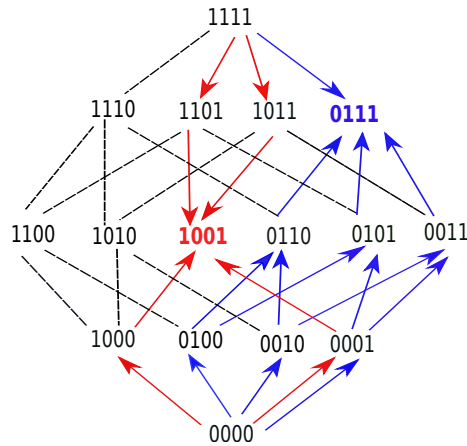


Figure 6. A fitness graph of a landscape with $L = 4$ mutations, illustrating the accessibility property. There are two fitness peaks, 1001 (red) and 0111 (blue). The fitness peaks are accessible from all their subset and superset genotypes following the paths marked by the arrows.

A fitness peak together with its subset and superset genotypes defines a sub-landscape with remarkable properties. It is a smooth landscape with only one peak which is accessible from any genotype via all direct paths, i.e. paths where the number of mutations monotonically increases or decreases. For example, the fitness peak 1001 is accessible from the all-mutant 1111 by the two direct paths – 1111 → 1101 → 1001 and 1111 → 1011 → 1001. Likewise, the peak 0111 is accessible from its subset 0001 via the paths 0001 → 0101 → 0111 and 0001 → 0011 → 0111. In general, a peak with n mutations is accessible from a subset genotype with m mutations by $(n - m)!$ direct paths, and from a superset genotype with m mutations by $(m - n)!$ direct paths. This gives a lower bound on the total number of paths by which a fitness peak is accessible from a subset or superset genotype.

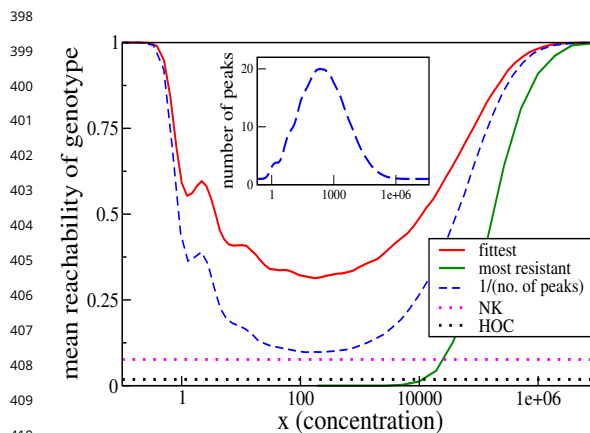
Importantly, the accessibility property formulated above holds under more general conditions than stipulated in the model. We show in Materials and Methods that it holds whenever the null fitness and resistance values of the mutations, r and m , do not show *positive* epistasis. This is a weaker requirement than our original assumption of a strict lack of epistasis in these two phenotypes.

373 In this context it should be noted that the rank orderings forbidden by the ordering condition all
 374 show positive epistasis for the fitness values, whereas all the allowed orderings can be constructed
 375 without positive epistasis. Therefore, any landscape where positive epistasis in fitness is absent will
 376 also display the accessibility property. However, whereas the lack of positive epistasis is a sufficient
 377 condition, it is not necessary. In particular, our model does allow for cases of positive epistasis in
 378 the fitness values.

379 Reachability of the fittest and the most resistant genotype


380 The preceding analyses have shown that within the mutant selection window, where mutants with
 381 higher fitness than the wild type exist, every fitness peak is accessible from the wild type. This
 382 includes in particular the fittest genotype at a given concentration. However, in general there will
 383 be many peaks in the fitness landscape, and it is not guaranteed that evolution will reach the fittest
 384 genotype. One can ask for the probability that the fittest genotype is actually accessed under the
 385 evolutionary dynamics, which we call its reachability. We assume that the dynamics is in the strong
 386 selection weak mutation (SSWM) regime, and the population is large enough such that the fixation
 387 probability of a mutant with selection coefficient s is $1 - e^{-2s}$ for $s > 0$, and 0 for $s \leq 0$ (Gillespie,
 388 1984). In our setting the selection coefficient is $s = \frac{f_1}{f_0} - 1$, where f_1 is the growth rate of a mutant
 389 appearing in a population of cells with growth rate f_0 .

390 Figure 7 shows the numerically obtained reachability for $L = 10$, averaged over the distribution
 391 $P(r, m)$ given in Eq. (8). The reachability of the highest peak is 1 at very low and very high concentra-
 392 tions, since there is only peak, the wild type or the all-mutant, at these extremes. The reachability is
 393 lower at intermediate concentrations, where there are multiple peaks, all of which are accessible
 394 from the wild type. The dashed blue line is the mean of the reciprocal of the total number of fitness
 395 peaks, and is therefore the mean reachability of fitness peaks. The reachability of the highest
 396 peak follows the qualitative behavior of the mean reachability, but remains higher than the mean
 397 reachability everywhere.



411 **Figure 7.** Reachability of fittest genotype and most
 412 resistant genotype. The same model as in the previous
 413 subsection has been used, with $L = 10$. Inset shows the
 414 mean number of fitness peaks as a function of
 415 concentration. Dotted horizontal lines show
 416 comparisons to the HoC model and an NK model with
 417 the same number of mutations. These models were
 418 implemented using an exponential distribution of
 fitness values.

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 421 We would therefore naturally expect a smaller fraction of adaptive walks to
 422 terminate at the fittest peak. A more illuminating comparison is with the NK model (Kauffman and

The green curve is the reachability of the most resistant genotype, i.e the all-mutant. It is extremely low at low and moderate concentrations and grows steeply and saturates quickly at a very large concentration. The all-mutant genotype is less-than-average reachable everywhere except at very high concentration, when it is the only fitness peak and accessible from every other genotype. 

We have compared the reachability to two other widely studied landscape models. One is the House-of-Cards (HoC) model (Kauffman and Levin, 1987; Kingman, 1978), where each genotype is independently assigned a fitness value drawn from a continuous distribution. The reachability is found to be around 0.018, an order of magnitude smaller than the lowest reachability seen in the tradeoff-induced landscape. The mean number of fitness maxima in the HoC landscape is $\frac{2^L}{L+1}$, which in this case is approximately 93.1, much higher than the maximum mean number of peaks in the tradeoff-induced landscape (in-

423 *Weinberger, 1989; Hwang et al., 2018*). Here, once again, $L = 10$, and the mutations are divided
 424 into two blocks of 5 mutations each. As per the usual definition of the model, the fitness of a
 425 genotype is the sum over the contributions of each of the 10 mutations, and the contribution of
 426 each mutation depends only the state of the block to which it belongs. The fitness contribution of
 427 each mutation for any state of the block is an independent random number. The mean number
 428 of fitness maxima here is ≈ 28.44 (*Perelson and Macken, 1995; Schmiegelt and Krug, 2014*), which
 429 is comparable to the maximum mean number in the tradeoff-induced landscapes (see inset of
 430 Figure 7). Nonetheless, the reachability of the fittest peak (dotted pink line) is found to be nearly 4
 431 times smaller than the lowest reachability in our landscape. We found that in a fraction of about
 432 0.64 of the landscapes, the fittest maximum is not reached in any of 32000 dynamical runs, indicating
 433 the absence of an accessible path in most of these cases (*Schmiegelt and Krug, 2014; Hwang et al.,*
 434 *2018*). In contrast, an evolutionary path always exists to any fitness peak in the tradeoff-induced
 435 landscapes, as we saw in the previous subsection. This endows the tradeoff-induced landscapes
 436 with the unusual property of being highly rugged and at the same time having a much higher
 437 evolutionary reachability of the global fitness maximum compared to other models with similar
 438 ruggedness.

439 Discussion

440 Fitness landscapes depend on the environment, and gene-gene-interactions can be modified
 441 by the environment. Systematic studies of such $G \times G \times E$ interactions are rare, but they are
 442 clearly of relevance to scenarios such as the evolution of antibiotic resistance, where the antibiotic
 443 concentration can vary substantially in space and time. In this paper we have explored the structure
 444 of such landscapes in the presence of tradeoffs between fitness and resistance. We summarize the
 445 main findings of our work.

- 446 • We have shown experimental evidence that the dose-response curves of various mutant
 447 strains of *E. coli* to the antibiotic ciprofloxacin have the same shape, except for a rescaling
 448 of the fitness and concentration values. If this shape is known, the fitness of a strain can be
 449 estimated at any antibiotic concentration simply by measuring its null-fitness and IC_{50} (or MIC).
 450 This makes it possible to construct empirical fitness landscapes at any antibiotic concentration
 451 from a limited set of data.
- 452 • Under the assumptions of our model the degree of epistasis, particularly sign epistasis, is
 453 low for zero and high antibiotic concentrations, but it is nevertheless high in the intermediate
 454 concentration regime. The number of local fitness peaks scales exponentially in the number
 455 of mutations at these concentrations. Epistasis is often discussed as a property intrinsic
 456 to mutations and their genetic backgrounds, with limited consideration of environmental
 457 parameters. But in the landscapes studied here, the environmental parameter is of paramount
 458 importance, since changes in it can dramatically alter gene-gene interactions.
- 459 • The expected number of mutations in a fitness peak increases logarithmically with the anti-
 460 biotic concentration. This implies that, at a given concentration, the highly fit genotypes that
 461 make up the fitness peaks carry an optimal number of mutations that arises from the tradeoff
 462 between fitness cost and resistance.
- 463 • Despite the high ruggedness, the landscape displays strong non-random patterns. A rank
 464 ordering condition between sets of mutations holds at all concentrations. A remarkable and
 465 unexpected consequence of this is that any fitness peak is evolutionarily accessible from the
 466 wild type.
- 467 • It is well known from experimental studies of antimicrobial resistance evolution that highly
 468 resistant genotypes often require multiple mutations which can be acquired along different
 469 evolutionary trajectories. Epistatic interactions constrain these trajectories and are generally
 470 expected to impede the evolution of high resistance. We find that strong and complex epistatic
 471 interactions inevitably arise in the mutant selection window, but at the same time the evolution

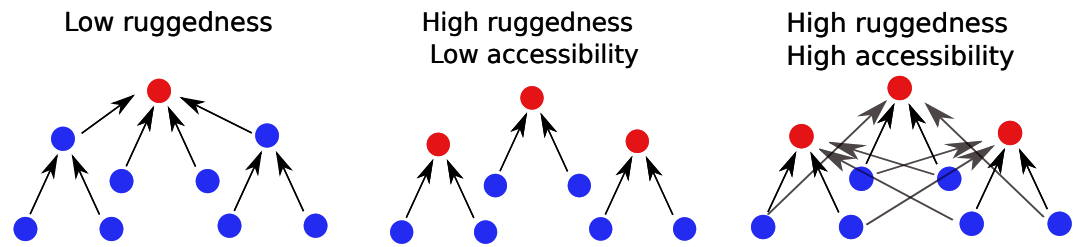


Figure 8. Accessibility and ruggedness in different types of fitness landscapes: The first two landscapes correspond to the typical cases of smooth and rugged landscapes. The third figure describes landscapes with adaptational tradeoffs, where high ruggedness coexists with high accessibility.

472 of the most resistant genotype (the identity of which changes with concentration) remains
473 facile and can occur along many different pathways.

474 All of these conclusions follow from three basic assumptions that are readily generalizable
475 beyond the context of antimicrobial resistance evolution: the existence of tradeoffs between two
476 *marginal phenotypes* that govern the adaptation at extreme values of an environmental parameter;
477 the scaling property of the shape of the tradeoff function; and the condition of limited epistasis
478 for the marginal phenotypes. How generally these assumptions are valid is a matter of empirical
479 investigation. We have shown that they hold for certain cases, and the interesting evolutionary
480 implications of our results indicate that more empirical research in this direction will be useful.

481 In the case of antimicrobial resistance, there can be fitness compensatory mutations (*Levin*
482 *et al., 2000; Brown et al., 2010; Durão et al., 2018*) that do not exhibit any adaptational tradeoffs.
483 These mutations are generally found in a population in the later stages of the evolution of antibiotic
484 resistance, which implies that they emerge in a genetic background of mutations with adaptational
485 tradeoffs. An understanding of tradeoff-induced landscapes is therefore a prerequisite for predict-
486 ing the emergence of compensatory mutations. [While compensatory mutations are expected to](#)
487 [facilitate the evolution of high resistance \(Hughes and Andersson, 2017\), our study shows that the](#)
488 [acquisition of multiple resistance mutations may readily occur even if compensatory mutations are](#)
489 [absent.](#)

490 In the formulation of our model we have assumed for convenience that the marginal phenotypes
491 combine multiplicatively, but this assumption is in fact not necessary for all our results. As shown
492 in Materials and Methods, our key results on accessibility only require the absence of positive
493 epistasis. These results therefore hold without exception for the combinatorially complete data set
494 in Table 1, where epistasis is either absent or negative. More generally, our analysis remains valid in
495 the presence of the commonly observed pattern of diminishing returns epistasis among beneficial
496 mutations (*Chou et al., 2011; Schoustra et al., 2016; Wünsche et al., 2017*). We expect our results
497 to hold approximately even when there is a small degree of epistasis (positive or negative) in r and
498 m , but we do not explore that question quantitatively in this paper.

499 [A strict absence of epistasis, while certainly not universal, can be expected to occur under](#)
500 [certain generic circumstances. Assuming that we deal with a single antibiotic that has a single](#)
501 [target enzyme, we can think of two situations that could lead to a multiplicative behaviour of \$IC_{50}\$.](#)
502 [\(i\) Single mutations occur in different genes that affect the concentration of the antibiotic-target](#)
503 [enzyme complex through independent mechanisms. \(ii\) Single mutations occur in the same gene](#)
504 [but their effect is multiplicative due to the nature of antibiotic-enzyme molecular interactions.](#)
505 [An example of scenario \(i\) would be a combination of mutations in the target gene \(reduction of](#)
506 [the binding affinity\), its promoter \(increase in expression\), genes regulating the activity of efflux](#)
507 [pumps and porins \(decrease in intracellular concentration of the antibiotic\), or genes controlling](#)
508 [the level \(increase in concentration\) or activity of drug-degrading enzymes. These mechanisms are](#)
509 ["orthogonal" to each other, in the sense that they modify independent pathways within the cell. If](#)
510 [each of them affects the concentration of the antibiotic-target complex through first-order kinetics,](#)

511 their cumulative effect will be multiplicative in terms of the IC_{50} s of single mutations.

512 In the case of ciprofloxacin and *E. coli* (Figure 2 and Table 1), we expect mutations in *gyrA* (target)
 513 to be orthogonal mutations in *acrR* and *marR* (efflux pumps). This is borne out by the observed
 514 multiplicativity of IC_{50} (Table 1). As for scenario (ii), the single mutations must affect different parts
 515 of the antibiotic-enzyme binding site independently. This is not the case for two different mutations
 516 in *gyrA* – S83L and D87N (see cases of epistasis in Table 1). An example for scenario (ii) are the
 517 two mutations P21L and A26T in the gene encoding the enzyme dihydrofolate reductase, which
 518 increase the resistance to trimethoprim in a multiplicative way in the absence of other mutations
 519 (Palmer *et al.*, 2015). If the antibiotic has more than one target, multiplicativity would not generally
 520 hold. In particular, topoisomerase IV (gene *parC*) is a secondary target for ciprofloxacin with much
 521 weaker affinity than gyrase. Therefore, mutations in *parC* do not contribute to resistance unless
 522 there is already a mutation in *gyrA*.

523 The co-existence of high ruggedness and high accessibility found in the tradeoff-induced land-
 524 scapes studied here is counterintuitive, and to the best of our knowledge fitness landscape models
 525 with this property have not been described previously. The situation is depicted schematically in
 526 Figure 8. The first landscape is smooth with a single peak that must be accessible from everywhere
 527 else. The second landscape is rugged, and each fitness peak is typically accessible from a few
 528 genotypes only. This is the typical picture of a rugged fitness landscape with limited accessibility, as
 529 it would be predicted by simple statistical models such as the HoC, NK or rough Mt. Fuji models
 530 (Szendro *et al.*, 2013; Neidhart *et al.*, 2014; Hwang *et al.*, 2018). The landscapes we describe here
 531 belong to a third type, where a high number of peaks are accessible from a high number of geno-
 532 types, creating overlapping “valleys” from which a population may evolve towards different local
 533 fitness maxima. Moreover, not only are fitness peaks accessible from all their subset and superset
 534 genotypes, but there are many direct paths leading up to each peak. This appears contrary to
 535 the expectation that in landscapes with high epistasis, accessibility should be facilitated through
 536 mutational reversions, i.e indirect paths (DePristo *et al.*, 2007; Palmer *et al.*, 2015; Wu *et al.*, 2016;
 537 Zagorski *et al.*, 2016).

538 We conclude with some possible directions for future work. Our model provides a principled
 539 framework for predicting how microbial fitness landscapes vary across different antibiotic concen-
 540 trations. This could be exploited to describe situations where the antibiotic concentration varies
 541 on a time scale comparable to the evolution of resistance, either due to the degradation of the
 542 drug or by an externally imposed treatment protocol (Marrec and Bitbol, 2018). In this context it
 543 would be of particular interest to include compensatory mutations that lack the tradeoff between
 544 growth and resistance, since such mutations are expected to strongly affect the extent to which
 545 resistance can be reversed (Andersson and Hughes, 2010). Significant extension of the theory is
 546 required if the drug concentration varies on a faster time scale comparable to the growth time of
 547 the microbial population, in which case the concept of a concentration-dependent fitness would
 548 need to be reconsidered.

549 From the broader perspective of evolutionary systems with adaptational tradeoffs mediated by
 550 an environmental parameter, our study makes the important conceptual point that it is impossible
 551 to have non-epistatic fitness landscapes for all environments. Using the terminology of Gorter *et al.*
 552 (2016), the tradeoffs enforce reranking $G \times E$ interactions which in turn, as we have shown, induce
 553 sign-epistatic $G \times G$ interactions at intermediate values of the environmental parameter. Notably,
 554 this general conclusion does not depend on the scaling property of the tradeoff function. It would
 555 nevertheless be of great interest to identify instances of scaling for other types of adaptational
 556 tradeoffs, in which case the detailed predictions of our model could be applied as well.

557 Acknowledgements

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 559 *et al.* (2009), and Tobias Bollenbach, Michael Brockhurst and Kristina Crona for useful comments.
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564 **Materials and Methods**

565 **Experiments**

566 **Bacterial strains**

567 We used strains from Marcusson et al. (2009) (courtesy of Douglas Huseby and Diarmaid Hughes).
 568 The strains are isogenic derivatives of MG1655, a K12 strain of the bacterium *E. coli*, with specific
 569 point mutations or gene deletions in five different loci: *gyrA:S83L*, *gyrA:D87N*, *parC:S80I*, $\Delta marR$, and
 570 $\Delta acrR$. There are 32 possible combinations of these alleles, but we only used the wild type, single
 571 mutants (5 strains) and double mutants (8 strains of 10 possible combinations): LM179 (00000),
 572 LM378 (10000), LM534 (01000), LM792 (00100), LM202 (00010), LM351 (00001), LM625 (11000),
 573 LM862 (10100), LM421 (10010), LM647 (10001), LM1124 (01100), LM538 (01010), LM592 (01001),
 574 LM367 (00011). A binary sequence after the strain's name represents the presence/absence of a
 575 particular mutated allele (order as in the above list of genetic alterations).

576 **Growth media and antibiotics**

577 LB growth medium was prepared according to Miller's formulation (10g tryptone, 5g yeast extract,
 578 10g NaCl per litre). The pH was adjusted to 7.2 with NaOH, and autoclaved at 121°C for 20 min.
 579 Ciprofloxacin (CIP) solutions were prepared from a frozen stock (10mg/ml ciprofloxacin hydrochloride,
 580 pharmaceutical grade, AppliChem, Darmstadt, in sterile, ultra-pure water) by diluting into LB
 581 to achieve the desired concentrations.

582 **Dose-response curves**

583 We incubated bacteria in 96-well clear flat bottom micro-plates (Corning Costar) inside a plate reader
 584 (BMG LABTECH FLUOstar Optima with a stacker) starting from two different initial cell densities (half
 585 a plate for each), and measured the optical density (OD) of each culture every 2-5 min to obtain
 586 growth curves. Plates were prepared automatically using a BMG LABTECH CLARIOstar plate reader
 587 equipped with two injectors connected to a bottle containing LB and a bottle with a solution of CIP
 588 in LB. The injectors were programmed to create different concentrations of CIP in each column of
 589 the 96 well plate. The injected volumes of the CIP solution were 0, 20, 25, 31, 39, 49, 62, 78, 98,
 590 124, 155, 195 μ l, and an appropriate volume of LB was added to bring the total volume to 195 μ l
 591 per well. Since different strains had MICs spanning almost two decades of CIP concentrations, we
 592 used a different maximum concentration of the CIP solution for each strain (approximately 1.5 - 2
 593 times the expected MIC). Bacteria were diluted from a thawed frozen stock 10^3 and 10^4 times in PBS
 594 (phosphate buffered saline buffer), and 5 μ l of the suspension was added to each well (10^3 dilution
 595 to rows A-D, 10^4 dilution to rows E-H). We used one strain per plate and up to 4 plates per strain
 596 (typically 1-2). After adding the suspension of bacteria to each well, the plates were immediately
 597 sealed with a transparent film to prevent evaporation, and put into a stacker (37°C, no shaking),
 598 from which they would be periodically fed into the FLUOstar Optima plate reader (37°C, orbital
 599 shaking at 200rpm for 10s prior to OD measurement). We then used the time shift methods to
 600 obtain exponential growth rates for each strain and different concentrations of CIP, see *Ojtic et al.*
 601 (2019) for further details.

602 **Mathematical Methods**

603 **Rank orders and fitness graphs**

604 The total number of possible rank orders with L mutations is $2^L!$, which is 24 for $L = 2$. Not all these
 605 rank orders, however, can be realized as one scans through x . Since any two curves intersect at
 606 most once, the maximum number of distinct rank orders that can be reached is the rank order at

607 $x = 0$ plus the total number of possible intersections, which is $\binom{2^L}{2} = 2^{L-1}(2^L - 1)$. Thus the upper
 608 bound on the number of rank orders found by scanning through x is $2^{L-1}(2^L - 1) + 1$, which is smaller
 609 than $2^L!$ for $L \geq 2$.

610 It is also instructive to determine the number of fitness graphs that can be found by varying x for
 611 a system with L mutations. This can be computed as follows: At $x = 0$ every mutation is deleterious,
 612 and every mutational neighbor with one less mutation is fitter; but due to the tradeoff condition, at
 613 sufficiently large x every mutation is beneficial and any mutational neighbor with one less mutation
 614 is less fit. In order for this reversal of fitness order to happen, the dose-response curves of any two
 615 mutational neighbors must intersect at some x . Therefore, the number of fitness graphs generated
 616 is equal to the number of distinct pairs of mutational neighbors, which is $2^{L-1}L$, and the number of
 617 distinct fitness graphs encountered is $2^{L-1}L + 1$. For $L = 2$, this number is 5, as seen in the example
 618 in the main text.

619 **Condition for two dose-response curves to intersect at most once**

620 Consider two DR curves characterized by (r, m) and (r', m') , where $r < r'$ and $m > m'$. We need to
 621 show that for the commonly observed cases, the curves $rw(\frac{x}{m})$ and $r'w(\frac{x}{m'})$ intersect at most once.
 622 First, notice that it is sufficient to prove this for the case $r' = 1, m' = 1$, because any rescaling of the
 623 x and w axes does not alter the number or ordering of intersection points. Therefore we require
 624 $r < 1$ and $m > 1$.

625 Let us consider the case where the dose-response curve is of the form of a Hill function, i.e
 626 $w(x) = \frac{1}{1+x^a}$, with $a > 0$. The intersection of curves happens at the solution of $w(x) = rw(\frac{x}{m})$, which
 627 we denote by $x^*(r, m)$. In this case the solution is given by

$$x^*(r, m) = \left(\frac{1-r}{r - \frac{1}{m^a}} \right)^{\frac{1}{a}}$$

628 which is positive and unique if $rm^a > 1$; otherwise no solution with $x^* > 0$ exists. It is similarly easy
 629 to show that at most one intersection point exists for exponentials, stretched exponentials, and
 630 half-Gaussians.

631 The property also holds for any concave dose-response curve with $w''(x) < 0$. We prove this as
 632 follows. Any intersection point x^* is the solution of

$$F(x^*) = r$$

633 where $F(x) \equiv \frac{w(x)}{w(\frac{x}{m})}$. We will show that $F(x)$ is monotonic and therefore the above equation has at
 634 most one solution. We have

$$F'(x) = \frac{w'(x)w(\frac{x}{m}) - \frac{1}{m}w(x)w'(\frac{x}{m})}{w(\frac{x}{m})^2},$$

635 and $F'(x)$ has the same sign as the numerator $\mathcal{N}(x) = w'(x)w(\frac{x}{m}) - \frac{1}{m}w(x)w'(\frac{x}{m})$. Since $w(x)$ is a
 636 decreasing function and $m > 1$, $w(\frac{x}{m}) > w(x) > \frac{1}{m}w(x)$. When $w''(x) < 0$, we also have $w'(x) < w'(\frac{x}{m})$.
 637 Since $w'(x) < 0$, this implies $|w'(x)| > |w'(\frac{x}{m})|$, and $\mathcal{N}(x) < 0$. Therefore $F(x)$ is monotonically
 638 decreasing.

639 **Proof of the accessibility property**

640 To derive the ordering condition, let us start with the simplest case of two single mutations A_i, A_j
 641 occurring on the wild type background. There are correspondingly four different genotypes $W, A_i,$
 642 $W A_i, W A_j, W A_i A_j$, which are listed in decreasing order of fitness at $x = 0$. Let the intersection of
 643 the DR curves of two genotypes σ_1 and σ_2 occur at $x = X_{\sigma_1, \sigma_2}$. Then $X_{W, W A_j}$ is given by the solution
 644 $x^*(r_j, m_j)$ of

$$w(x) = r_j w\left(\frac{x}{m_j}\right),$$

645 and $X_{W A_i, W A_i A_j}$ is given by the solution of

$$r_i w\left(\frac{x}{m_i}\right) = r_i r_j w\left(\frac{x}{m_i m_j}\right).$$

646 This last equation can be re-written as

$$w(x') = r_j w\left(\frac{x'}{m_j}\right),$$

647 where $x' = \frac{x}{m_i}$. Comparing this with the first equation above, we have

$$X_{W A_i, W A_i A_j} = m_i X_{W, W A_j} > X_{W, W A_j}. \quad (3)$$

648 This equation tells us that whenever the double mutant is fitter than one of the single mutants, the
 649 wild type must be less fit than the *other* single mutant. Consequently, when the double mutant is
 650 fitter than both the single mutants, the WT must be less fit than both the single mutants. In other
 651 words, the number of single mutants fitter than the wild type cannot be less than the number of
 652 single mutants less fit than the double mutant. This is the ordering condition given in the main text.
 653 Any ordering that violates this condition is a *forbidden ordering*. For greater clarity, we list all the
 654 possible forbidden orderings (up to interchange of indices i and j).

$$\begin{aligned} W &> W A_i > W A_i A_j > W A_j \\ W &> W A_i A_j > W A_i > W A_j \\ W A_i A_j &> W > W A_i > W A_j \\ W A_i A_j &> W A_i > W > W A_j \end{aligned} \quad (4)$$

655 Although we showed this for two single mutations in the wild type background, the same argu-
 656 ments hold for any two sets of mutations in any background, since the succession of orderings is
 657 independent of the rescalings of the fitness and concentration axes. To put it more precisely, W , A_i
 658 and A_j are any three non-overlapping sets of mutations, where A_i and A_j are non-empty sets.

659 Next we use this to prove the accessibility property. Let σ have n mutations. It is sufficient to
 660 prove that (i) any superset of σ with m or fewer mutations is accessible from all its own supersets
 661 with m or fewer mutations, for all $m \geq n$ (the statement follows from the case $m = L$); and that (ii)
 662 any subset of σ with m' or more mutations is accessible from any of its own subsets with m' or more
 663 mutations, for all $m' \leq n$ (the statement corresponds to $m' = 0$). We prove this by induction.

664 Firstly, we notice that the case $m = n$ is trivial, since σ is of accessible from itself. For the case of
 665 supersets, our base case is $m = n + 1$, and the assertion above holds because σ is a local fitness peak,
 666 and therefore accessible from all its supersets with $n + 1$ mutations, which are of course accessible
 667 from themselves.

668 Now we prove the induction step. Assume that all supersets of σ that have m or fewer mutations
 669 (where $m \geq n$) are accessible from all their supersets with m or fewer mutations. Consider a superset
 670 Σ of σ with m mutations, and denote it by $\Sigma = \sigma A$, where A is the set of mutations in Σ not present
 671 in σ . By assumption, σ is accessible from Σ . In the following, we use the notation $\sigma_1 > \sigma_2$ to indicate
 672 that a genotype σ_1 is fitter than a genotype σ_2 (we use the " $<$ " and " $=$ " signs in a similar way).
 673 Therefore, we have $\sigma > \Sigma = \sigma A$.

674 Now consider any superset of Σ with $m + 1$ mutations, where the additional mutation not
 675 contained in Σ is denoted B . Then this superset can be denoted by $\Sigma B = \sigma A B$. We must have
 676 $\sigma > \sigma B$ since σ is a local fitness peak. We now have the relation $\sigma > \sigma A, \sigma B$. Therefore we must have
 677 $\sigma A B < \sigma A, \sigma B$, for otherwise we violate the ordering condition. Now since $\Sigma B = \sigma A B < \sigma A = \Sigma$, Σ
 678 must be accessible from ΣB , proving that any superset with m mutations is accessible from any of
 679 its supersets with $m + 1$ mutations. This completes the proof of the induction step.

680 The proof for the case of subsets is essentially the same, utilizing the symmetry between the
 681 wild type and the double mutant in the ordering condition.

682 The accessibility property follows entirely from the ordering condition, and hence any landscape
 683 that obeys the ordering condition will obey the theorem. The ordering condition follows from
 684 $X_{W,W_{A_i}} < X_{W_{A_j},W_{A_i A_j}}$, as obtained in (3). However, this same inequality obtains under more general
 685 conditions. To see this, let us define the null-fitness of the double mutant $W_{A_i A_j}$ as r_{ij} , and the
 686 resistance of the double mutant as m_{ij} . The dose-response curves of W and W_{A_j} intersect at
 687 $X_{W,W_{A_j}} = x^*(r_j, m_j)$, whereas the curves for W_{A_i} and $W_{A_i A_j}$ intersect at

$$X_{W_{A_i},W_{A_i A_j}} = m_i x^*\left(\frac{r_{ij}}{r_i}, \frac{m_{ij}}{m_i}\right).$$

688 Now it is easy to show that $x^*(r, m)$ is a decreasing function of both r and m . Therefore $X_{W_{A_i},W_{A_i A_j}} >$
 689 $X_{W,W_{A_j}}$ holds if $r_{ij} \leq r_i r_j$ and $m_{ij} \leq m_i m_j$.

690 Number of local fitness peaks

691 When dealing with complex fitness landscapes with parameters that can vary across species and
 692 environments, a useful strategy is to model the fitness effects as random variables that are chosen
 693 from a probability distribution (Kauffman and Levin, 1987; Szendro et al., 2013; Hwang et al., 2018).
 694 In the limit of large system size L , many properties emerge that are independent of the details of
 695 the system. In practice, even relatively small system sizes are often approximated well by results
 696 obtained in the asymptotic limit.

697 The mean number of peaks with n mutations in the tradeoff-induced landscapes is

$$K_n(x) = \binom{L}{n} Q_n(x),$$

698 where $\binom{L}{n}$ is the total number of genotypes with n mutations, and $Q_n(x)$ is the probability that
 699 a genotype with n mutations is a fitness maximum at antibiotic concentration x . Then the total
 700 number of peaks at x is $\sum_n K_n(x)$. Let the resistance of a genotype σ be $M = \prod_{i=1}^n m_i$, and likewise its
 701 null-fitness be $R = \prod_{i=1}^n r_i$. The genotype σ is a local fitness maximum if it is fitter than all its subsets
 702 with $n - 1$ mutations and all its supersets with $n + 1$ mutations.

703 To find the concentration at which the curves of σ and its neighboring genotypes intersect, we
 704 start with the simplest case of the dose-response curves of the wild type and a single mutant (r, m) .
 705 These curves intersect at the solution $x^*(r, m)$ of $w(x) = r w\left(\frac{x}{m}\right)$, which is a decreasing function of
 706 r and m . The wild type is fitter than the single mutant when $x > x^*(r, m)$. Now the intersection of
 707 the DR curves of a genotype σ with n mutations and a subset with $n - 1$ mutations that lacks the
 708 mutation (r_i, m_i) occurs at the solution of

$$w\left(\frac{x}{\left(\frac{M}{m_i}\right)}\right) = r_i w\left(\frac{x}{\left(\frac{M}{m_i}\right)m_i}\right)$$

709 which is read off as $\frac{M}{m_i} x^*(r_i, m_i)$. Likewise, the intersection of the DR curves of σ and a superset with
 710 $n + 1$ mutations that contains the additional mutation (r_j, m_j) occurs at $M x^*(r_j, m_j)$. Therefore σ is a
 711 fitness maximum if

$$\frac{x^*(r_i, m_i)}{m_i} < \frac{x}{M} < x^*(r_j, m_j) \quad (5)$$

712 for all i and j with $1 \leq i < n$ and $n < j \leq L$. Alternatively,

$$\log m_i - \log x^*(r_i, m_i) > \log M - \log x > -\log x^*(r_j, m_j). \quad (6)$$

713 Let us consider the regime where $L, n \gg 1$. Then $\log M \sim n \langle \log m \rangle$; if $\log x$ is smaller than $O(n)$,
 714 it is clear that the second inequality is almost certainly satisfied whereas the probability of the
 715 first inequality is vanishingly small. Both the probabilities are finite if $\log x \sim n \langle \log m \rangle$. Thus the
 716 probability of σ being a fitness peak is maximized when $\log x = \log(M) + \eta$, where $\eta \sim O(1)$ and
 717 depends on the details of the distribution $P(r, m)$. Thus the mean number of fitness peaks with n
 718 mutations is maximal at $x_{\max}(n)$ where to leading order $\log x_{\max}(n) \sim n \langle \log m \rangle$, independent of any
 719 further details of the system.

720 The total number of genotypes with n mutations is $\binom{L}{n}$, and $\log \binom{L}{n} \simeq LH(\rho)$, where $\rho = \frac{n}{L}$, and
 721
$$H(\rho) = -[\rho \log \rho + (1 - \rho) \log(1 - \rho)]. \quad (7)$$

722 The mean number of fitness maxima can be found by multiplying this with Q_n . One may expect Q_n
 723 to be exponentially small in L , since a total of L inequalities (as indicated in (6)) need to be satisfied.
 724 However, this is complicated by the fact that the probabilities of the inequalities being satisfied are
 725 not independent. The correlations between the inequalities would depend on the distribution of
 726 $P(r, m)$ and the dose-response curve. If the correlations are sufficiently weak, one might still expect
 727 to find an exponential scaling in large L . To leading order $\binom{L}{n}$ is itself exponential in L , and if the
 728 probability that a genotype is a fitness peak is exponentially small in L , we expect the mean number
 729 of peaks K_n to be exponential in L as well. This is supported by the scaling shown in the inset of
 Figure 4A.

730 For the simulation results shown in the main text we chose a joint distribution of the form

$$P(r, m) = P(r)P(m|r) = 6r(1 - r)\left(m - \frac{1}{\sqrt{r}}\right)e^{-\left(m - \frac{1}{\sqrt{r}}\right)}. \quad (8)$$

731 The conditional distribution $P(m|r)$ is a shifted gamma distribution. The shift ensures that the curves
 732 of a background genotype and a mutant intersect.

733 Sign epistasis

734 Sign epistasis with respect to a certain mutation occurs when the mutation is beneficial in one
 735 background but deleterious in another. We first show that any two distinct sets of mutations on
 736 any genetic background display sign epistasis at some value of the scaled concentration x . Consider
 737 a genetic background W , and two distinct sets of mutations A_1 and A_2 (which share no mutations
 738 with each other or W). At $x = 0$ we have $W > A_1, A_2$ and $WA_1A_2 < WA_1, WA_2$. As x increases, W
 739 must become less fit than either WA_1 or WA_2 before WA_1A_2 becomes fitter than either of these (by
 740 the ordering condition). Without loss of generality, let us assume that W becomes less fit than WA_1
 741 before it becomes less fit than WA_2 . At this point, we must have $W < WA_1$ and $WA_2 > WA_1A_2$.
 742 This means that, in the wildtype background, A_1 is beneficial in the absence of A_2 but deleterious in
 743 the presence of A_2 , indicating pairwise sign epistasis.

744 To quantify the amount of sign epistasis for large L and n , we next ask for the number of
 745 backgrounds n_b in which a mutation is beneficial at concentration x . If one considers only those
 746 backgrounds that have n mutations, then n_b would depend both on n and x . In a statistical ensemble
 747 of landscapes, one may compute the probability P_b that a mutation is beneficial in a background
 748 with n mutations, and of course $\langle n_b \rangle = P_b \binom{L}{n}$. In the limit of large L and n , P_b exhibits some universal
 749 properties to leading order. When $\log x > n \langle \log m \rangle$, we are in the regime of high concentration relative
 750 to n , and we expect a mutation to be beneficial. We find that to leading order $P_b(\rho, x) = 1$, with
 751 corrections that are exponentially small in n . When $\log x < n \langle \log m \rangle$, we are at concentrations that
 752 are too low to prefer additional mutations, and P_b is exponentially small in n . When $\log x = n \langle \log m \rangle$,
 753 we are at the threshold concentration where a new mutation becomes beneficial. Here we find that
 754 $P_b \simeq \frac{1}{2}$. For large L we therefore expect a steep transition from 0 to 1 as the concentration crosses
 755 the threshold value (see inset of Figure 5).

756 Consider a mutation (r, m) in a background with n mutations $(r_1, m_1), (r_2, m_2) \dots (r_n, m_n)$. The mutation
 757 is beneficial in this background if

$$m_1 m_2 \dots m_n x^*(r, m) < x \quad (9)$$

758 Taking logarithms, we have

$$-\log x^*(r, m) > \sum_{i=1}^n \log m_i - \log x. \quad (10)$$

759 Define $\xi = \frac{\log x}{L}$ and $\rho = \frac{n}{L}$, and $z = -\log x^*(r, m)$. Then the above inequality becomes

$$\frac{z}{n} > \frac{1}{n} \sum_{i=1}^n \log m_i - \frac{\xi}{\rho}. \quad (11)$$

760 Let the distribution of z be $P(z)$, and let $C_z(z) = \int_z^\infty P_z(x) dx$. Define the random variable $\omega =$
 761 $\frac{1}{n} \sum_{i=1}^n (\log m_i - \frac{\xi}{\rho})$, and denote its distribution $P(\omega)$. Then the probability that a mutation is beneficial
 762 in a background with n mutations is

$$P_b(\rho, \xi) = \int_{-\infty}^{\infty} P(\omega) C_z(n\omega) d\omega \quad (12)$$

$$(13)$$

763 The mean number of backgrounds with n mutations in which a mutation is beneficial is $n_b(\rho, \xi) =$
 764 $P_b(\rho, \xi) \binom{L}{n}$. Note that $\langle \omega \rangle = \langle \mu \rangle - \frac{\xi}{\rho}$ where $\mu = \log m$. When $n \gg 1$, $C_z(n\omega) \simeq 1$ for $\omega < 0$ and $C_z(n\omega) \simeq 0$
 765 for $\omega > 0$, with a sharp transition from 1 to 0 that happens within a region of width $\sim O(1/n)$ of the
 766 origin. Also for large n , $P(\omega)$ is sharply peaked around $\langle \omega \rangle$ over a region of width $O(1/\sqrt{n})$.

767 When $\langle \omega \rangle < 0$, $C_z(n\omega) \simeq 1$ over this entire region, as observed before. Thus to leading order,
 768 $P_b(\rho, \xi) = 1$. The mean number of backgrounds in which a mutation is beneficial is $n_b(\rho, \xi) =$
 769 $P_b(\rho, \xi) \binom{L}{\rho L}$.

$$n_b(\rho, \xi) \simeq \sqrt{\frac{2\pi}{L}} \frac{1}{\sqrt{\rho(1-\rho)}} e^{LH(\rho)} \quad (14)$$

770 where $H(\rho)$ is defined in (7). Therefore

$$\log n_b \simeq LH(\rho) \quad (15)$$

771 to leading order.

772 When $\langle \omega \rangle > 0$, the dominant contribution to the integral in (12) comes from $\omega \leq 0$, since $C_z(n\omega)$
 773 quickly drops from 1 to zero for $\omega > 0$. Further, since $C_z(n\omega) \simeq 1$ for $\omega < 0$ (except for a region of width
 774 $O(1/n)$ around $\omega = 0$, as observed before), we can approximate $\log P_b(\rho, \xi)$ simply by the probability
 775 that $\omega < 0$. Then

$$\log P_b(\rho, \xi) \simeq -nI\left(-\frac{\xi}{\rho}\right)$$

776 where I is the large deviation function of $-\mu$, and

$$\log n_b(\rho, \xi) \simeq L\left[H(\rho) - \rho I\left(-\frac{\xi}{\rho}\right)\right].$$

777 This implies that n_b is reduced by a factor that is exponentially small in L compared to (15)), and
 778 therefore the fraction of backgrounds in which a mutation is beneficial is very small.

779 Finally, when $\langle \omega \rangle = 0$, i.e. $\xi = \frac{n}{L} \langle \mu \rangle$, $P(\omega)$ is centered at the origin and decays over a width $O(1/\sqrt{n})$.
 780 For $\omega > 0$, $C_z(n\omega)$ is 0 except over a much smaller width $O(1/n)$ to the right of the origin, whereas
 781 for $\omega \leq 0$, it is 1 except for a small region of width $O(1/n)$ left of the origin. Thus the dominant
 782 contribution to the integral in (12) comes from $\omega \leq 0$, and as before, P_b can be approximated by the
 783 probability $\omega \leq 0$. Due to the central limit theorem, $P(\omega)$ is approximately Gaussian and therefore
 784 symmetric around $\omega = 0$, and therefore $P_b \simeq \frac{1}{2}$. Consequently, we should have

$$n_b(\rho, \xi) \simeq \frac{1}{2} \sqrt{\frac{2\pi}{L}} \frac{1}{\sqrt{\rho(1-\rho)}} e^{LH(\rho)},$$

785 which is $\frac{1}{2}$ times the total number of backgrounds given by (14). This proves that the concentration
 786 where the mutation is beneficial in half of the backgrounds is given by $\langle \omega \rangle = 0$ or $\log x = n(\log m)$ for
 787 large L and n .

788 **Epistasis in null-fitness and MIC for *E. coli* in the presence of ciprofloxacin**

789 Primary data shown in Table 1 were obtained from *Marcusson et al. (2009)*. In the third and
 790 fifth columns, the errors in the $\log(x)$ are calculated as $\frac{|\Delta x|}{x}$, where $|\Delta x|$ are the standard error as
 791 calculated from the standard deviations reported in the paper. The errors in columns four and
 792 six were estimated as $\sum_i \frac{|\Delta x_i|}{x_i}$ where the sum is over the mutations present in the combinatorial
 793 mutants. The detectable cases of epistasis are marked in blue. Negative epistasis is found in all
 794 these cases. Also, all the cases with epistasis correspond to two or more mutations that affect the
 795 same chemical pathways.

Strain	String	log null-fitness	Non-epistatic	log MIC	Non-epistatic
MG1655	00000	0.00 (± .004)	NA	0.00 (± .35)	NA
LM378	10000	0.01 (± .016)	NA	3.17 (± .70)	NA
LM534	01000	-0.01 (± .018)	NA	2.75 (± .70)	NA
LM202	00010	-0.19 (± .020)	NA	0.69 (± .70)	NA
LM351	00001	-0.094 (± .014)	NA	1.08 (± .70)	NA
LM625	11000	-0.030 (± .011)	0.0 (± .038)	3.17 (± .70)	5.92 (± 1.1)
LM421	10010	-0.15 (± .019)	-0.18 (± .040)	4.13 (± .70)	3.56 (± 1.1)
LM647	10001	-0.051 (± .013)	-0.084 (± .034)	3.44 (± .70)	4.65 (± 1.1)
LM538	01010	-0.19 (± .020)	-0.20 (± .042)	4.13 (± .70)	3.46 (± 1.1)
LM592	01001	-0.083 (± .015)	-0.10 (± .036)	3.16 (± .70)	3.83 (± 1.1)
LM367	00011	-0.20 (± .026)	-0.28 (± .038)	2.06 (± .70)	1.77 (± 1.1)
LM695	11010	-0.24 (± .017)	-0.19 (± .058)	3.85 (± .70)	6.61 (± 1.1)
LM691	11001	-0.073 (± .013)	-0.094 (± .052)	3.85 (± .70)	7.00 (± 1.4)
LM709	10011	-0.24 (± .027)	-0.274 (± .054)	4.54 (± .70)	4.94 (± 1.4)
LM595	01011	-0.51 (± .051)	-0.294 (± .056)	4.54 (± .70)	4.52 (± 1.4)
LM701	11011	-0.42 (± .037)	-0.284 (± .072)	4.83 (± .70)	7.69 (± 1.8)

Table 1. The names of the strains and values of null-fitness (in competition assays with the wild type) in the third column and MIC (of ciprofloxacin) in the fifth column are obtained from *Marcusson et al. (2009)*. The binary strings represent the same genotypes as given in the caption of Figure 2. The values in parentheses are error estimates. The fourth and sixth columns are respectively the null-fitness and MIC values expected in the absence of epistasis. NA denotes the cases where this is not applicable.

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