# Accurate multiple input switching solution for static timing analysis 

Khaled El-Kinawi

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# THE AMERICAN UNIVERSITY IN CAIRO NANOTECHNOLOGY GRADUATE PROGRAM 

# Accurate Multiple Input Switching solution for Static Timing Analysis 

Khaled El-Kinawi

May 2013

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## Acknowledgments

I would like to thank my supervisor Dr.Yehea Ismail for his efforts and his guidance during my work on this dissertation. I would like to express my gratitude for Dr.Hanadi Salem for her efforts in the continuous development and improvement of the nanotechnology. I would like to also thank my colleagues and friends Mohamed Abdelsalam and Tamer Abdul Aziz for their enlightening discussion that contributed to my understanding of the behavior of CMOS gates. Their help can't be overlooked. I would like also to express my sincere appreciation to my parents and family for their support.

Finally, I would like to thank God for his help and inspiration.


#### Abstract

Multiple Input switching is a problem in Static Timing Analysis of nanoscale electronics, which is ignored in the industry. The methods and techniques of Static Timing analysis are discussed. Effective capacitance technique is presented. The composite current model is described and examined. The Multiple Input switching problem is explored and analyzed. The history effect in Multiple Input switching is explained. The miller capacitance effect is illustrated. A number of solutions, present in the literature, are discussed. A simple and innovative solution for the Multiple Input switching problem is presented. The solution is verified using Spice and matlab. Experimental evidence is presented to show the effectiveness of the solution. Matlab is used to simulate the solution. An Algorithm for minimum and maximum delay analysis is elaborated.


## 1 Introduction

The Integrated Circuit (IC) industry continues to serve the needs of our society for faster and cheaper products. IC industry is reducing the feature size of ICs every two years. Today, ICs are produced with 20 nanometer feature size. This allows the industry to produce ICs with larger number of transistors. The current progress of the industry follows Moore's law. In accordance with Moore's law, it is expected for the number of transistors to continue to increase over the coming years. There are many new challenges in the design and manufacturing aspects in this new era of nano-electronics. The need for smaller feature sizes that passed the lithography limit is one of these challenges for the electronics manufacturing process. This challenge promoted the development of new techniques for resolution enhancement. The new nano-electronics era didn't change only the manufacturing process, but it also affects the design process. It is becoming more difficult to design and verify such complex electronic ICs. The large number of transistor in an IC requires more powerful and efficient tools. The digital design process is becoming more automated in IC industry. The need for automation is stressed due to the importance of earlier market entry and to keep up with Moore's law. The complexity of design is complicated by the increase of transistor count, the need for higher frequency of operation and shorter gate delay. The automated design process requires extensive verification.

The verification process can be divided into physical, logical and timing verification. The physical verification ensures the manufacturability of the design. It
ensures that the produced design follows the lithographical rules. The logical verification, also known as Layout Versus Schematic, compares a logical view of the design to the physical view. It ensures the adherence of the layout to the logical view of the design. Timing verification analyzes the timing behavior of the design. It calculates the maximum operating frequency of the design. There are two type of timing verification: Dynamic Timing Analysis and Static Timing Analysis. This Thesis will focus on an accurate solution for the Multiple Input Switching problem in Static Timing Analysis.

The rest of the thesis dissertation is organized as follows. The second section will discuss the background of Timing verification and Static Timing Analysis (STA). The basics of STA will be explained in the second section. The second section will elaborate about the effective capacitance STA technique and discuss composite current models. These models are the state-of-art models used in the industry. An understanding of these models is essential for understanding the basic ideas of this dissertation. The second section will discuss the Multiple Input switching problem and the solutions in the literature. The Multiple Input switching is dissected and explained in the second section. The third section introduces the ideas of the proposed solution. . A number of Spice simulation and matlab trials are shown in this section. The fourth section explains the algorithm for the solution in max-delay and min-delay analysis scenarios. Conclusion is given in the fifth section. The sixth section will include a proposal for future work. The final section include publication

## 2 Background

### 2.1 Timing Verification

Timing Verification ensures the adherence of the design to design timing requirements. It ensures that the design's data will be correctly handled and will stay uncorrupted. In order to elaborate about timing verification, it is important at this stage to discuss the details of the typical design structure. A typical design uses parallel processing to improve throughput. This is implemented using a series of memory elements, such as a flip-flop, connected with combinational logic that processes the data. There is a global triggering signal that prompts the flip-flop to store information. This signal is known as the clock signal. The maximum frequency for the clock signal is the operating frequency. Figure 2.1 shows a typical stage inside a digital design. This stage is preceded and followed with similar stages. The operating frequency depends on the stage with the longest path. The longest path is called the critical path. The critical path is usually optimized extensively to improve the design's overall performance. However, all flip-flops are subject to two inherit timing constraints to correctly store data. The Flip-flops require that the information to be stored remain unchanged before and after clock signal. The time required for the data to remain constant before the clock signal is called setup-time. The time required for the data to remain constant after the clock signal is called hold-time. It is part of the timing verification to ensure that these constraints are honored. The setup-time is also incorporated in the calculations of the operating frequency and clock period. There are two ways to do timing verifications.

The first way is Dynamic timing analysis.


Figure 2.1 : Flip Flop to Flip Flop path[1]
Dynamic timing analysis is a circuit simulation that uses the complicated physical equations of transistors to calculate delay. Test vectors are need to be specified for dynamic analysis. It is very difficult to cover all possible cases for a chip since Dynamic timing analysis takes a lot of time. There is a need for a fast, exhaustive method to ensure timing integrity. Static timing analysis (STA) uses simplified timing models to analysis the chips. It ignores functionality and concentrates on the timing aspect of the implementation.

### 2.2 Static timing analysis

Static Timing Analysis (STA) is the main method of timing verification in digital IC design. It ensures the performance of an integrated circuit. Static Timing Analysis (STA) offers a compromise between accuracy and run-time. STA uses stripped-down models to estimate delay with a high degree of accuracy without requiring a long run time.

The models are generated using Spice through a characterization process.

Although the characterization process would depend on the slow Spice simulation, they are done once. The models are stored as simple look-up tables. The look-up table
relates the output transition and delay time of gate to the input transition and out capacitance. These models are re-used by the different designers. The STA models relate all inputs to all outputs. However, they relate unrelated signals such as relating a functional mode signal to test mode signal. Therefore, the designer needs to specify for the tool these false paths. The false paths are usually specified by the digital design team. Although these models relate all inputs to all outputs, it assumes that only one input changes at a single moment. The input-output relationship is called a timing arc. The timing arc assumption ignores the possibility of Multiple Input switching at a single moment. The most accurate STA timing model is the recently industrially adopted model, which is the composite current source model. STA also includes a number of techniques to compensate for accuracy while maintaining simplicity. These techniques, such as the effective capacitance technique address changes in the industry without complicating the timing model. In this thesis, a simple technique will be presented to eliminate errors in STA caused by multiple input switching. In the following subsection, the effective capacitance technique and the composite current model will be discussed in more detail.

### 2.3 Effective capacitance

The STA models use look-up tables to relate the voltage transition time of a single input and the output load capacitance to calculate the delay of a gate. These look-up tables are collectively regarded as Non-Linear Delay Models (NLDM). The output load is assumed to be a pure capacitor. This model worked well in large feature size, where the interconnects' resistance were very small. As the feature size decreased,
interconnects' resistance increased. The original model, which depends solely on the capacitance, was ineffective. Since interconnects are a continuous array of resistance and capacitors, they are best estimated through a $\pi$-model. The $\pi$-model is made of a resistor with two capacitors on each end of the resistance. The other terminal of the capacitors is connected to the ground as shown on the left side of the figure. It is very difficult to relate the input transition and the output load represented by the $\pi$-model using a look-up table.

It was proposed to substitute the $\pi$-model with an effective capacitance as shown in Figure 2.2[2]:


Figure 2.2: Effective capacitance replaces $\pi$-model [1]
This effective capacitor produces the same delay as the $\pi$-model. The following equation is used to determine the effective capacitance [2]. The $t_{D}$ is the $50 \%$ delay point time.

The $t_{x}$ is the $20 \%$ point time.

$$
C_{e f f}=C_{2}+C_{1}\left[1-\frac{R C_{1}}{t_{D}-\frac{t_{x}}{2}}+\frac{\left(R C_{1}\right)^{2}}{t_{x}\left(t_{D}-\frac{t_{x}}{2}\right)} e^{\frac{-\left(t_{D}-t_{x}\right)}{R C_{1}}}\left(1-r^{\left.\frac{-t_{x}}{R C_{1}}\right)}\right]\right.
$$

Equation 2.1 : effective capacitance and $\pi$-model [2]
This substitution ensures that the correct delay is reported. However, the output transition time is incorrect using this approach. The waveform of the output voltage
curve is incorrect after the $50 \%$ delay point. In order to correct this issue, the model is substituted by the figure below. The driving resistance of the gate is calculated and the waveform is corrected


Figure 2.3 : Driving resistance model replace effective capacitance [1]
There are several methods to calculate the driving resistance such as using the thevenin equivalent or the simple equation shown below. $t_{80}$ represents the $80 \%$ point delay. $t_{s}$ shows the time, which the effective capacitance model is till valid before switching to the driving resistance model.

$$
R_{d r}=\frac{\left(t_{80}-t_{s}\right)}{\ln \left[\frac{V\left(t_{s}\right)}{V\left(t_{80}\right)}\right] C_{e f f}}
$$

Equation 2.2 : Driving resistance equation [1]
This technique is used with NLDM. This approximation is acceptable because the driving resistance is comparable to the interconnect resistance [3]. In order to deal with highly resistive interconnects, Composite current source models must be used [3]. A technique similar to effective capacitance is used with Composite current source models

### 2.4 Composite Current Source model

As the feature size is reduced, the top-level interconnect is becoming more resistive with narrower metal widths [3]. The industry decided to use the Composite Current Source (CSS) to replace older models such as NLDM because the current-based models improve accuracy since the driver resistance becomes infinite. This model can be divided into a driver and receiver component as shown in Figure 2.4[4]. The receiver components may be composed of two different capacitors. The first capacitor is used before the $50 \%$ delay point. The second capacitor is used after the $50 \%$ delay point. This arrangement mimics the transistor capacitance combination better. The values of the capacitors are pre-characterized using Spice.

The driver model is a voltage-dependent, time-varying current source with infinite resistance. This driver model simulates the transistor better in the nanoscale. The current source is characterized using a number of different input voltage transitions and different load capacitances.


Figure 2.4 : Receiver and driver model in CCS [4]
The current waveforms for each gate are extracted as individual points using a golden simulator such as Spice. These current waveforms are used similarly to NLDM. The STA engine deduces an effective capacitance, whose current match the current for a lumped network. "There will be a unique current that will elicit the same voltage on both a lumped capacitance and the network at the given timestep."[3] Unlike NLDM, the matching factor for the effective capacitance is the voltage. The effective capacitance matching occurs during every time step. "This current is the chosen value for the given timestep, and we reapply this procedure at every subsequent timestep" [3]. This recreates a current waveform. The current waveform is then integrated to extract the gate delay, output transition of this gate and input transition of the subsequent stage. The input transition of the subsequent gates is used to repeat the process.

### 2.5 Multiple Input switching (MIS)

Multiple Input switching is the case, where several input change their values at the same time. The difference between single input switching case and Multiple Input switching case in cell delay and output voltage transition time delay will henceforth be called delay error and transition error respectively. This research focuses mainly on when the change of the inputs occurs simultaneously because the delay error is of maximum value in that case.[5] Simultaneous Multiple Input Switching (MIS) in the worst delay analysis increases the delay. MIS in the minimum delay analysis decreases the delay. As far as we know, there is no proposed solution for minimum delay and transition error in both academia and the industry. We can conclude that best case as
well as the worst case delays comes from MIS cases. Please note the convention used in the Figure 2.5:


Figure 2.5: A simple NAND
In the maximum delay analysis, the worst case is the MIS case for a NAND gate when the NMOS transistors in series simultaneously turn on. This means that Input A \& B change their values simultaneously from ' 0 ' to ' 1 ' and the output changes from logic ' 1 ' to logic ' 0 '. During this scenario, parasitic capacitances would require discharging. The parasitic capacitance that accounts for the effect of the gate drain capacitance is one of the largest parasitic capacitances. When the input \& output of a transistor is switching simultaneously, the gate-drain capacitance is replaced by a capacitance connected to
the ground and the output of transistor. The value of this capacitance is double the gate-drain capacitance. This capacitance is called the miller capacitance.


Figure 2.6 : explanation of the miller capacitance [6]
If the input $A$ is switching individually, the miller capacitance is smaller in that case than the MIS case. When input B is switching, the miller capacitance is smaller than MIS case and the intermediate node (the node between transistor A \& B) capacitance is discharged before $B$ switches. It is theoretically expected to the delay to be larger in the SIS case, when the input A switches individually, than in the SIS case, where the input B switches individually.

According to [7] and [8], the delay error between MIS and SIS may reach up to $100 \%$. The worst delay of the multiple switching scenarios occurs when the multiple switching signals have the same input transition and occur simultaneously [5]. The worst case MIS also depends on the input values before the MIS event. The pre-MIS event input values must induce the storage of charge in the intermediate node capacitance to increase the delay error. In order to induce this scenario, the A NMOS transistor must be turned off first. The B NMOS transistor is then turned off after transistor A. Thus, the worst case MIS will have AB input vector start as ' 01 ' then change to ' 00 ' and then
'11'[8]. This will ensure that intermediate node will maintain a voltage value of threshold voltage subtracted from the supply voltage before becoming a floating node. The intermediate node capacitor will be fully charged. This will delay the change in the output and increase the MIS error. This scenario is used in all of the simulations. This phenomenon is called the history effect.

In the industry, the simultaneous multiple input switching (MIS) is largely ignored. The probability for MIS was relatively low in the past. This probability has increased as the operating frequency increased. There are a number of solutions proposed for MIS problem. The complexity of these solutions reduces their applicability and practicality.

### 2.5.1 MIS existing solutions

There are a number of existing solutions in academia for MIS. However, Academia hasn't provided a satisfactory solution to MIS. This sub-section is dedicated to explain two famous MIS solutions in academia. The current source based solution and the inverter substitution solution will be presented.

### 2.5.1.1 Current based solutions

The most famous solution is the use of the current-based models. In [7] and [8], we find two distinct current-models models to solve the MIS. [7] Presented a model called multi-port current source model. The multi-port current source model is shown in Figure 2.7. It models the gates using a voltage-dependent current source and a voltagedependent charge source. The current and charge source are dependent on the voltage
of all the ports. In Figure 2.7 , ' $p$ ' symbol represents ports. This makes characterization more complicated and increases the run-time of static timing analysis. It would be also very difficult to build a library based on this model. This model "can result in $20 \%$ or higher delay estimation error in some cases" [8]. This large error is unacceptable in STA.


Figure 2.7 : Multi-port CSM [7]
In [8], a two-current source model is used. The second current source is used to determine the value of the intermediate node voltage. As shown in Figure 2.8, the current sources are a function of the voltage at all terminals [7]. $V_{a} \& V_{b}$ represent the voltages of terminal $\mathrm{A} \& \mathrm{~B}$ respectively. $V_{N}$ represents the voltage of the intermediate node. $V_{o}$ represents the voltage of the output. The characterization and the library of this model are very complicated. It would increase the run-time and reduce the advantage of STA.


Figure 2.8 : Complete MIS CSM of a NOR2 gate [8]
These models are very complicated, when compared to CCS. The complexity of the solutions coupled with the low statistical probability of the occurrence of SMIS in older technologies discouraged the industry from including these error correction solutions in the industrial process.

### 2.5.1.2 Inverter solution

The inverter solution transforms the input waveform into an equivalent form. It also replaces the complicated gates into a collection of inverters. In [9], "the waveforms of the switching inputs are replaced by an equivalent waveform and the multi-input gate is collapsed into an inverter by series-parallel reduction of the transistors" [5]. The error presented in [9] is 5\%. This percentage is very high for STA. In [10], the author attempts to modify the Inverter solution to improve accuracy. However, the authors focus on calculating the maximum current. "Both these techniques give significant errors when we measure delay and output transition time" [5]. These techniques are very difficult to implement in STA. They would require significant run-time and it would reduce the advantage of STA. Although this method reduces the error of the Multiple Input
switching, it still has a significant overall error. In the next section, a novel solution is presented that overcomes these limitations.

## 3 MIS Novel Solution

In order for the industry to accept a proposed solution of MIS problem, it must have the following properties:

- It must have low overhead during the transition and delay calculation process.
- The accuracy of the solution must be within 1-2\% of the Spice results.
- It would be optimum if it builds on models that the industry uses such as NLDM or CCS.
- It should have a low number of new timing arcs. The lower number of timing arcs would reduce the complexity of the overall timing analysis.
- The solution should eliminate the error in delay and output transition of the gate. This would ensure the completion of the solution.


### 3.1 Current shift

The MIS delay error could reach up to 100\% [7]. The current shift theory is aimed at reducing this error to an acceptable value. The proposed idea is to shift the output current values in time for one of the SIS case. This would allow the delay of this SIS case to increase. The value of shift should make the delay of the modified SIS current equal to MIS case. This shift is a side effect of the increase of the miller capacitance. The
current shift would maintain the benefit of the current source and would be easily implemented in STA.

### 3.1.1 Current shift experimental observation

The simulation explores a NAND gate. It uses the configuration shown Figure 2.5. The NAND starts with an output of ' 0 ' and switch its output to ' 1 ' and back to ' 0 '. This is done to initiate the NAND in a condition similar to its regular operation conditions. The intermediate capacitor is also allowed to store charge when the output is switched to ' 1 '. This will cause the maximum MIS error and account for the history effect. The simulation uses tsmc 65 nm technology Spice models. The simulation is repeated for different input transitions, load capacitors and transistor widths.

Five hundred and ten simulations were performed using Spice iterating over different variation for the configuration of a tsmc 65 nm NAND gate, input transitions and load capacitances. Each simulation test case includes two SIS cases and the MIS case that has the same load capacitor, transistor sizing and input transition on its inputs. The simulations ensured that the worst case MIS is compared the SIS cases. The current and voltage waveform is produced. The delay, input and output transitions are calculated. The maximum output current is also calculated.

The options "runlvl=6 post=2 brief" were used during Spice simulation to ensure higher accuracy during simulation. The timestep was 1f. The following figures show the input and output of the simulation for SIS \& MIS cases. All current images, delay and transition calculation are done on the second rising edge. Figure 3.1 shows the inputs
for SIS case. The black line represents the voltage for input A. The blue line (grey) represents input B. Figure 3.2 shows the output for the SIS case. In this case, input A is switching.


Figure 3.1 : SIS case inputs


Figure 3.2 : SIS output
In Figure 3.3, the inputs for MIS case are shown. The black line represents the voltage for input A. The blue line (grey) represents input B. The input A falls before the input B to prevent the discharge of the intermediate capacitance. This ensures maximum delay error. The time period of the input is large to ensure stabilization of the output. The Spice simulation of SIS case is meant to mimic the characterization process of CCS model. Figure 3.4 shows the MIS case output.


Figure 3.3 : MIS Inputs


Figure 3.4 : MIS output

The shape of the current in the MIS case is shown in the following figures. Please note that the MIS current (in black) and Input A SIS case current (in blue). The MIS current appears to be a delayed version of the input A SIS case.

These figures show that if the current of the grounded NMOS SIS case is shifted in time. We can reproduce an approximate waveform of MIS. This shift maintains the basic benefits of CCS models. This shift can be added as a variable in the model. The static timing analysis tool can use this variable and re-generate MIS current waveform. Figure 3.5 through Figure 3.10 show a sample of the Spice simulation test cases. These figures illustrate the difference between the SIS and MIS currents. Through observation, a hypothesis can be formed about the relation SIS between MIS. The hypothesis states that MIS current a shift version of the SIS current.


Figure 3.5 : MIS (black) \& SIS currents (light blue) for input transition 10ps, the NMOS transistor width is 390 nm , and the load capacitance is $2 f$ farad


Figure 3.6 : MIS (black) \& SIS (light blue) currents for input transition 50ps, the NMOS transistor width is 390nm, and the load capacitance is $\mathbf{2 f}$ farad


Figure 3.7 : MIS (black) \& SIS currents (light blue) for input transition 100ps, the NMOS transistor width is 390 nm and the load capacitance is $2 f$ farad


Figure 3.8 : MIS (black) \& SIS currents (light blue) for input transition 10ps, the NMOS transistor width is 585 nm and the load capacitance is 1 f farad


Figure 3.9 : MIS (black) \& SIS currents (light blue) for input transition 50ps, the NMOS transistor width is 585 nm and the load capacitance is 1 f farad


### 3.2 Multiplication factor

The transition time error can't be reduced using only the current shift. The current shift would eliminate the delay error. However, the voltage transition time of the shifted current will be the same as the transition time of the original unshifted SIS case. The absolute transition time error is less than $2 \%$ in $44 \%$ of the tested cases. In 79\% of simulation, the MIS case's output voltage has smaller or equal output transition time to its respective SIS case. MIS cases, which have smaller transition time, are less pessimistic. Another solution for the transition time error would be preferred.

The solution is using a multiplication factor. The multiplication factor is multiplied by the current values. After shifting the current, you can easily deduce the mid-point voltage delay using integration. We can then multiple the current values that occur after the delay point to modify the transition time. Since we are multiplying the current values after the delay point, the delay calculations are unaffected. This method is similar to the effective capacitance method, where you use the effective capacitance to find the delay then calculate the transition time using the driving resistance. We use the current shift method to calculate the delay then use the multiple the current values occurring after the voltage mid-point to calculate the transition time. The multiplication factor can reduce or increase the transition time of the altered current waveform. This is essential to correct for decrease or increase of output voltage transition time.

### 3.2.1 Matlab verification

In order to verify these concepts, two cases of the Spice simulations were processed using matlab. The current waveforms of the SIS \& MIS cases were imported in matlab. The current was then integrated to produce the output voltage waveform for both the MIS \& SIS case. The current shift is then performed on the SIS current waveform. The shifted current is then integrated to produce a new voltage waveform. This waveform is compared with the MIS voltage waveform. The shifted SIS current is then manipulated using the multiplication factor. The multiplied shifted current waveform is integrated again. The voltage waveform of that current is compared to the MIS voltage waveform. The delay and transition error of final waveform and MIS error is mentioned. The matlab verification was done on two cases. These cases exemplify the most difficult situation for the implementation of this method. The first test case was chosen because the maximum value of the SIS \& MIS cases has the largest difference. This illustrates that the current manipulation method can overcome large differences in the maximum value of current. The second case has the largest absolute error in transition time in the Spice simulations. The current and voltage waveform are represented graphically and several calculation are made to assess the success of the current manipulation method.

### 3.2.1.1 The first case

This case followed the procedure outlined above. Figure 3.11 shows the original SIS current is in light blue. The MIS is in Black.


Figure 3.11 : Initial MIS (black) \&SIS currents (light blue) in the first case

The second figure shows after shifting the current. The value of the shift is determined through a number of iterations. An estimated initial value is used to shift the current. The current is integrated. The delay of resultant voltage of the shifted current is compared to the MIS delay. If the error is unacceptable, the delta value is changed and the comparison is repeated. This delta value is essential for applying this solution. Figure 3.12 shows the shifted current and the MIS current.


Figure 3.12 : Shifted SIS (light blue) and MIS (black) in the first case


Figure 3.13 : Modified SIS (light blue) and MIS (black) in the first case

After calculating the delay, we then experimentally determine the multiplication factor. The multiplication factor is chosen through an iterative process similar to the shift factor, where we compare the transition time error. Figure 3.13 shows the modified current after shifting and multiplication and the MIS current.

Figure 3.14 shows the voltage waveform of the SIS and MIS cases before modification.

Figure 3.16 shows the close correlation between the voltage waveform after current modifications and MIS voltage. The percentage delay error was reduced from $60 \%$ in the original case to- $0.34 \%$ in the modified case. The percentage transition error was reduced from $9.19 \%$ in the original case to $0.19 \%$ in the modified case. The degree of error correction is dependent on the iterative process. The error could have been reduced further but these error values are acceptable for STA.


Figure 3.14 : Original SIS voltage (light blue) and MIS voltage (Black) in the first case


Figure 3.15 : Shifted SIS voltage (light blue) and MIS voltage (Black) in the first case


Figure 3.16 : Modified SIS voltage (light blue) and MIS voltage (Black) in the first case

### 3.2.1.2 The Second Case

We applied the previously described process on another case. This case has the largest transition time error. Figure 3.17 shows the unmodified current and MIS current. Figure 3.18 shows the SIS current shifted in comparison to the MIS current. Figure 3.19 shows the SIS current after modification in its final form compared to MIS currents. As we can see the voltage waveforms show a huge reduction in transition as well as delay percentage error. The delay percentage error in delay reduced from $82.69 \%$ to- $0.31 \%$. The transition percentage error reduced from $-10.73 \%$ to $0.43 \%$.


Figure 3.17 : Initial MIS (black) \&SIS currents (light blue) in the second case


Figure 3.18 : Shifted SIS (light blue) and MIS (black) in the second case


Figure 3.19 : Modified SIS (light blue) and MIS (black) in the second case


Figure 3.20 : Original SIS voltage (light blue) and MIS voltage (Black) in the second case


Figure 3.21 : Shifted SIS voltage (light blue) and MIS voltage (Black) in the second case


Figure 3.22 : Modified SIS voltage (light blue) and MIS voltage (Black) in the second case

## 4 Complete current manipulation solution

In the previous section, we proved the basic concepts of the current shifting and scaling method. In this section, the algorithm, that comprises these basic concepts, will be detailed. The algorithm can be divided into two major scenarios. The scenarios represent the type of analysis. There is a max-delay and min-delay scenario.

### 4.1 Max delay scenario

### 4.1.1 Characterization Procedure

The procedure for the characterization of the max delay scenario requires, in addition to the simulation of the two SIS cases, the simulation of the MIS case. The MIS case will have its inputs switch simultaneously. The input transition time of both inputs
in the MIS case must be equal. The delay and transition time error is recorded. The current shift value and multiplication factor are calculated. These values are recorded in the library.

Figure 4.1 illustrated the exact procedure for the characterization step after alteration. The addition step is an overhead on the characterization process. The overhead is significant. The addition MIS case for a 2-input gate will represent a new arc in addition to the original two arcs. This is a $33 \%$ increase to processing time. In 3-inputs gate, there would be 4 MIS cases. There is one MIS case that account for switching of the three inputs simultaneously. The other three MIS cases occur when you iterate the stabilization of one of the input on a specific value. The 4 MIS cases are added to the 3 SIS cases. This would lead to a total of 7 cases. This would account for an increase of $133 \%$. If we apply the same concept to a 4-input gate, the MIS cases would be 11 cases. The number of SIS cases for a 4-input gate is 4 cases. The increase in the number of cases is $275 \%$. Although the increase of cases in the characterization process is significant, the characterization process occurs once. The correction possible by this method would justify the increase in the processing time in characterization time. The number of case increase is inherent in the Multiple Input problem.

Figure 4.2 shows an example of CCS model library. The figure illustrates how the current table is stored in index_3. Index_1 and index_2 store the input voltage transition time and out capacitance respectively for this specific current table. The value for the current shift value and multiplication factor will be added as index_3 and index_4
respectively. The current table will have index_5 as an identifier. The model will not
suffer major increase in the data. This would maintain the model size.


Figure 4.1 : Max delay scenario characterization procedure

```
pin (OUT) {
    timing () {
            related_pin : "IN"-;
        output_current_fall () {
            vector ("LOOKUP_TABLE_1\times1\times5") {
                reference_time : 5.06; /* Time of input crossing
                    threshold */
                    index_1("0.040"); /* Input transition */
                    index 2("0.900"); /* Output capacitance */
                    index_3("5.079e+00,5.093e+00,5.152e+00,
                                    5.170e+00, 5.352e+00");/* Time values */
            /* Output charging current: */
            values("-5.784e-02, -5.980e-02, -5.417e-02,
                                    -4.257e-02, -2.184e-03");
            }
            . . .
        }
        • . .
    }
}
```

Figure 4.2 : CCS model library [1]

### 4.1.2 Run-time procedure

The run-time procedure for max-delay analysis after characterization is very simple. The STA engine would initiate the error correction, if the following conditions are satisfied:

- The two inputs switching windows coincide.
- If the transition times of the inputs are within a pre-set tolerance of each other.

The second condition concerning the tolerance is meant to safe guard against variation.

It would ensure the detection of any possible MIS event. If these conditions are
satisfied, the STA engine would use the current shift value and multiplication factor and apply it on the SIS current values as stated in the matlab verification section.


Figure 4.3 : Max-delay scenario run-time procedure

### 4.2 Min-delay scenario

The minimum delay scenario requires a correction in the run-time only. This alleviates the overhead in the characterization time. The run-time procedure is very simple. The STA engine checks that the inputs have the same switching windows. When this condition is satisfied, the current values are added together incorporating any delay between the inputs. This means that the current would be delayed depending on the occurrence of the input edge. This method is accurate, flexible and simple


Figure 4.4 : Min-delay scenario run-time procedure

## 5 Conclusion

This dissertation presented a simple, flexible and diverse solution for the MIS problem in STA. The solution changes in the characterization process for STA models. The current shift value and multiplication factor are calculated during the modified characterization process. They are then used during the run-time processing. This thesis also present the only solution for the minimum delay analysis MIS prolem. The solution takes advantage of the CCS model and maintains its accuracy. The study included a practical and realistic algorithm that can guide the reader through implementation of this solution. The implementation of this solution would improve ASIC designed chips by increasing their yield. The idea should spark interest of the industry in this problem and motivate the implementation of this solution.

## 6 Future works

The next phase should include relating the current shift value to the time separation between the edges during MIS. The characterization tools and flows should be modified to calculate the shift value and multiplication factor. The introduction of more efficient and accurate method for calculating the current shift value and multiplication factor should be explored. An accuracy study using modified CCS model, which would require syntax modification and modified STA engine is needed. This study is needed to assure the feasibility and applicability of this.

## 7 Publication

Khaled EI-Kinawi, Yehea Ismail "Current manipulation technique for multiple input switching problem in Static Timing Analysis" (in preparation)

## Works Cited

[1] Rakesh Chadha J. Bhasker, Static Timing Analysis for Nanometer Designs: A Practical Approach. United States of America: Springer, 2009.
[2] J. Qian, S. Pullela, and L. Pillage, "Modeling the "effective capacitance" for the RC interconnect of CMOS gates," IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems, vol. 13, no. 12, pp. 1526-1535 , December 1994.
[3] Synopsys Inc. (2006, December) Open Source Liberty. [Online]. www.opensourceliberty.org/ccspaper/ccs timing wp.pdf
[4] Synopsys George Mekhtarian. (2005, November) Open source liberty. [Online]. http://www.opensourceliberty.org/ccspaper/ccs bgr.pdf
[5] V. Chandramouli and Karem A. Sakallah, "Modeling the Effects of Temporal Proximity of Input Transitions on Gate," in Proceedings of the 33rd annual Design Automation Conference, New York, 1996, pp. 617-622.
[6] Anantha Chandrakasan, Borivoje Nikolic Jan M. Rabaey, Digital integrated circuits : A Design Perspective, 2nd ed. Upper Saddle River, N.J., United Stated of America: Prentice Hall, 2003.
[7] C. Amin, C. Kashyap, N. Menezes, K. Killpack, and E. Chiprout, "A multi-port current source model for multiple-input switching effects in CMOS library cells," in

ACM/IEEE Design Automation Conference, 2006, pp. 247-252.
[8] Safar Hatami, Hanfi Fatemi, Massoud Pedram Behnam Amelifard, "A current source model for CMOS logic cells considering multiple input switching and stack effect," in conference on Design, Automation and Test in Europe, Newyork, 2008, pp. 568-573.
[9] K. Jun, and S.-B. Park Y.-H. Jun, "An Accurate and Efficient Delay time Modeling for MOS Logic Circuits using Polynomial Approximation," IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems, vol. 8, no. 9, pp. 10271032, September 1989.
[10] A. Nabavi-Lishi and N. C. Rumin, "Inverter Models of CMOS Gates for Supply Current and Delay Evaluation," IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems, vol. 13, no. 10, pp. 1271-1279, October 1994.

## Appendix

## Spice code

```
$NAND
.param LL =0.06um WW=0.195um TWW='4*WW/3' TT=100p vdd=1.2V period=10n
vdc d 0 de vdd
SLower input switching structure
va a 0 PULSE (0 vdd delay TT TT 'period/2' period)
vb b 0 dc vdd
mnl net1 a 0 0 nch L=LL W=WW
mn2 out1 b net1 0 nch L=LL W=WW
mp1 d a out1 d pch L=LL W=TWW
mp2 d b out1 d pch L=LL W=TWW
Cl out2 0 cc
vtest out1 out2 dc OV
Supper input switching
vau au 0 dc vdd
vbu bu 0 PULSE(0 vdd delay 'nn*TT' TT 'period/2' period)
mnu1 netul au 0 0 nch L=LL W=WW
mnu2 outul bu netul 0 nch L=LL W=WW
mpul d au outul d pch L=LL W=TWW
mpu2 d bu outu1 d pch L=LL W=TWW
Cul outu2 0 cc
vutest outul outu2 dc OV
$Simultaneous structure
valpha alpha 0 PULSE (0 vdd 'delay' TT TT 'period/3' period)
vbeta beta 0 PULSE (0 vdd 'delay+shift' 'nn*TT' TT 'period/2' period)
mnsl netsl alpha 0 0 nch L=LL W=WW
mns2 outs1 beta nets1 0 nch L=LL W=WW
mps1 d alpha outs1 d pch L=LL W=TWW
mps2 d beta outs1 d pch L=LL W=TWW
Csl outs2 0 cc
```

```
vstest outs1 outs2 dc OV
.op
.option runlvl=6 post=2 brief dccap
.TRAN If 17n sweep DATA=DATAN
$.TRAN lf 17n sweep DATA=DATAR
$.TRAN 1f 17n sweep DATA=DATAM
$.TRAN 1f 16n sweep DATA=DATAO
.MEAS TPHLLS TRIG PAR('V(a) -0.5*VDD') VAL=0 RISE=2
+ TARG PAR('V(out1) -0.5*VDD') VAL=0 FALL=2
.MEAS TPHLUS TRIG PAR('V(bu) -0.5*VDD') VAL=0 RISE=2
+ TARG PAR('V(outu1) -0.5*VDD') VAL=0 FALL=2
.MEAS TPHLSS TRIG PAR('min(V(alpha),V(beta)) -0.5*VDD') VAL=0 RISE=2
+ TARG PAR('V(outs1) -0.5*VDD') VAL=0 FALL=2
.MEAS FALITIMEL TRIG PAR('V(out1)-0.9*VDD') VAL=0 FALL=2
+ TARG PAR('V(out1)-0.1*VDD') VAL=0 FALL=2
.MEAS FALLTIMEU TRIG PAR('V(outu1)-0.9*VDD') VAL=0 FALL=2
+ TARG PAR('V(outu1)-0.1*VDD') VAL=0 FALL=2
.MEAS FALLTIMES TRIG PAR('V(outs1)-0.9*VDD') VAL=0 FALL=2
+ TARG PAR('V(outs1)-0.1*VDD') VAL=0 FALL=2
.MEAS TRAN ivtestz when I(vtest)=0 FROM=15ns TO=16ns FALL=2
.MEAS TRAN ivstestz when I(vstest)=0 FROM=15ns TO=16ns FALL=2
.MEAS idelay PARAM='ivstestz-ivtestz'
.MEAS TRAN IMINL MIN I (vtest) FROM=14ns TO=16ns
.MEAS TRAN IMINU MIN I (vutest) FROM=14ns TO=16ns
.MEAS TRAN IMINS MIN I(vstest) FROM=14ns TO=16ns
```



| 102 | 2p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff |
| :---: | :---: | :---: | :---: | :---: |
| 103 | 2p | 0.195 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 104 | 2p | 0.195 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 105 | 2p | 0.195 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 106 | 2p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 107 | 2p | 0.195 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 108 | $5 p$ | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 109 | 5p | 0.195 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 110 | 5p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 111 | 5p | 0.195 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 112 | $5 p$ | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 113 | 5 p | 0.195 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 114 | 10p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 115 | 10p | 0.195 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 116 | 10p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 117 | 10p | 0.195 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 118 | 10p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 119 | 10p | 0.195 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 120 | 20p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 121 | 20p | 0.195 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 122 | 20p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 123 | 20p | 0.195 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 124 | 20p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 125 | 20p | 0.195 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 126 | 50p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 127 | 50p | 0.195 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 128 | 50p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 129 | 50p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 130 | 50p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 131 | 50p | 0.195 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 132 | 75p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 133 | $75 p$ | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 134 | 75p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 135 | 75p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |


| 136 | 75p | $0.195 u m 0.0$ | $0 \mathrm{E}+00$ | 4ff 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 137 | 75p | $0.195 u m 0.0$ | OE+00 | 5ff 1 |  |
| 138 | 100p | 0.195 um | $0.00 \mathrm{E}+00$ | 0.5 ff |  |
| 139 | 100p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 140 | 100p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 141 | 100p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 142 | 100p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | - 4ff 1 |  |
| 143 | 100p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 144 | 150p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5ff |  |
| 145 | 150p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 146 | 150p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 147 | 150p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 148 | 150p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 149 | 150p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | - 5ff 1 |  |
| 150 | 200p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5ff |  |
| 151 | 200p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 152 | 200p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 153 | 200p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 154 | 200p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | - 4ff 1 |  |
| 155 | 200p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | - 5ff 1 |  |
| 156 | 250p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5ff |  |
| 157 | 250p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 158 | 250p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 159 | 250p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | - 3ff 1 |  |
| 160 | 250p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | - 4ff 1 |  |
| 161 | 250p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | - 5ff 1 |  |
| 162 | 300p | 0.195 um | $0.00 \mathrm{E}+00$ | 0.5ff |  |
| 163 | 300p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 164 | 300 p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | - 2ff 1 |  |
| 165 | 300p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 166 | 300p | 0.195 um | $0.00 \mathrm{E}+00$ | - 4ff 1 |  |
| 167 | 300p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 168 | 350p | $0.195 u m$ | $0.00 \mathrm{E}+00$ | 0.5ff | 1 |
| 169 | 350p | $0.195 u m$ | 0.00E+00 | 1ff 1 |  |



| 204 | 2p | 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| :---: | :---: | :---: | :---: | :---: |
| 205 | 2p | 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 206 | 2p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 207 | 2p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 208 | 2p | 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 209 | 2p | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 210 | $5 p$ | 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 211 | $5 p$ | 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 212 | 5p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 213 | $5 p$ | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 214 | 5p | 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 215 | $5 p$ | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 216 | 10p | 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 217 | 10p | 0.39 um | $0.00 \mathrm{E}+00$ | 1 ff 1 |
| 218 | 10p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 219 | 10p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 220 | 10p | 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 221 | 10p | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 222 | 20p | 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 223 | 20p | 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 224 | 20p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 225 | 20p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 226 | 20p | 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 227 | 20p | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 228 | 50p | 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 229 | 50p | 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 230 | 50p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 231 | 50p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 232 | 50p | 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 233 | 50p | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 234 | 75p | 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 235 | $75 p$ | 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 236 | 75p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 237 | 75p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |


| 238 | 75p | 0.39 um 0.0 | $0 \mathrm{E}+00$ | 4ff 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 239 | 75p | 0.39 um 0. | OE + 00 | 5ff 1 |  |
| 240 | 100p | - 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 241 | 100p | 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 242 | 100p | - 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 243 | 100p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 244 | 100p | - 0.39 um | $0.00 \mathrm{E}+00$ | - 4ff 1 |  |
| 245 | 100p | 0.39 um | $0.00 \mathrm{E}+00$ | -5ff 1 |  |
| 246 | 150p | - 0.39 um | $0.00 \mathrm{E}+00$ | 0.5ff | 1 |
| 247 | 150p | - 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 248 | 150p | - 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 249 | 150p | O 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 250 | 150p | - 0.39 um | $0.00 \mathrm{E}+00$ | - 4ff 1 |  |
| 251 | 150p | - 0.39 um | $0.00 \mathrm{E}+00$ | - 5ff 1 |  |
| 252 | 200p | O. 0.39 um | $0.00 \mathrm{E}+00$ | 0.5ff | 1 |
| 253 | 200p | O. 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 254 | 200p | 0.39um | $0.00 \mathrm{E}+00$ | - 2ff 1 |  |
| 255 | 200p | - 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 256 | 200p | 0.39um | $0.00 \mathrm{E}+00$ | - 4ff 1 |  |
| 257 | 200p | O.39um | $0.00 \mathrm{E}+00$ | -5ff 1 |  |
| 258 | 250p | - 0.39 um | $0.00 \mathrm{E}+00$ | 0.5ff | 1 |
| 259 | 250p | - 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 260 | 250p | O.39um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 261 | 250p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 262 | 250p | O 0.39 um | $0.00 \mathrm{E}+00$ | - 4ff 1 |  |
| 263 | 250p | 0.39um | $0.00 \mathrm{E}+00$ | -5ff 1 |  |
| 264 | 300p | 0.39um | $0.00 \mathrm{E}+00$ | 0.5ff | 1 |
| 265 | 300p | 0.39um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 266 | 300p | 0.39um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 267 | 300p | 0.39um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 268 | 300p | 0.39um | $0.00 \mathrm{E}+00$ | - 4 ff 1 |  |
| 269 | 300p | 0.39um | $0.00 \mathrm{E}+00$ | - 5ff 1 |  |
| 270 | 350p | 0.39um | $0.00 \mathrm{E}+00$ | 0.5ff | 1 |
| 271 | 350p | - 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |


| 272 | 350p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 273 | 350p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 274 | 350p | O.39um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 275 | 350p | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 276 | 400p | O. 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 277 | 400p | 0.39um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 278 | 400p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 279 | 400p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 280 | 400p | 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 281 | 400p | - 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 282 | 450p | O.39um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 283 | 450p | 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 284 | 450p | O. 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 285 | 450p | O.39um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 286 | 450p | 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 287 | 450p | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 288 | 500p | 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 289 | 500p | 0.39 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 290 | 500p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 291 | 500p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 292 | 500p | O. 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 293 | 500p | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 294 | 750p | 0.39 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 295 | 750p | 0.39 um | $0.00 \mathrm{E}+00$ | 1 ff 1 |  |
| 296 | 750p | 0.39 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 297 | 750p | 0.39 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 298 | 750p | 0.39 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 299 | 750p | 0.39 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 300 | 1p | $0.585 u m 0$. | OE+00 0 | $0.5 \mathrm{ff} \quad 1$ |  |
| 301 | 1 p | $0.585 u m 0.0$ | $0 \mathrm{E}+00$ | 1ff 1 |  |
| 302 | 1p | 0.585 um 0.0 | OE+00 | 2ff 1 |  |
| 303 | 1 p | 0.585 um 0.0 | OE +00 3 | 3ff 1 |  |
| 304 | 1p | $0.585 u m 0.0$ | $0 \mathrm{E}+00$ | 4ff 1 |  |
| 305 | 1p | 0.585 um 0.0 | OE+00 | 5ff 1 |  |


| 306 | 2p | 0.585 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 307 | 2p | 0.585 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 308 | 2p | 0.585 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 309 | 2p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 310 | 2p | 0.585 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 311 | 2p | 0.585 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 312 | 5p | 0.585 um | $0.00 \mathrm{E}+00$ | 0.5 ff |  |
| 313 | 5 p | 0.585 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 314 | 5p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 315 | 5p | 0.585 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 316 | 5p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 317 | $5 p$ | 0.585 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 318 | 10p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 319 | 10p | 0.585 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 320 | 10p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 321 | 10p | 0.585 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 322 | 10p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 323 | 10p | 0.585 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 324 | 20p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 325 | 20p | 0.585 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 326 | 20p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 327 | 20p | 0.585 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 328 | 20p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 329 | 20p | 0.585 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 330 | 50p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 331 | 50p | 0.585 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 332 | 50p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 333 | 50p | 0.585 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 334 | 50p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 335 | 50p | 0.585 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 336 | 75p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 337 | $75 p$ | 0.585 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 338 | 75p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 339 | 75p | $0.585 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |  |


| 340 | 75p | 0.585 um $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| :---: | :---: | :---: | :---: | :---: |
| 341 | 75p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 342 | 100p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 343 | 100p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 344 | 100p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 345 | 100p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 346 | 100p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 347 | 100p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 348 | 150p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 349 | 150p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 350 | 150p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 351 | 150p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 352 | 150p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 353 | 150p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 354 | 200p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 355 | 200p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 356 | 200p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 357 | 200p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 358 | 200p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 359 | 200p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 360 | 250p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 361 | 250p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 362 | 250p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 363 | 250p | 0.585 um $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 364 | 250p | 0.585 um $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 365 | 250p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 366 | 300p | 0.585 um $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 367 | 300p | 0.585 um $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 368 | 300p | 0.585 um $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 369 | 300p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 370 | 300p | 0.585 um $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 371 | 300p | 0.585 um $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 372 | 350 p | 0.585 um $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 373 | 350p | $0.585 \mathrm{um} 0.00 \mathrm{E}+00$ | 1ff 1 |  |



| 408 | 2p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| :---: | :---: | :---: | :---: | :---: |
| 409 | 2p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 410 | 2p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 411 | 2p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 412 | 2p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 413 | 2p | 0.78 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 414 | 5p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 415 | 5p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 416 | 5p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 417 | 5p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 418 | 5p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 41.9 | $5 p$ | 0.78 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 420 | 10p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 421 | 10p | $0.78 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 422 | 10p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 423 | 10p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 424 | 10p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 425 | 10p | $0.78 u m$ | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 426 | 20p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 427 | 20p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 428 | 20p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 429 | 20p | $0.78 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 430 | 20p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 431 | 20p | 0.78 um | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 432 | 50p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 433 | 50p | $0.78 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 434 | 50p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 435 | 50p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |
| 436 | 50p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |
| 437 | 50p | $0.78 u m$ | $0.00 \mathrm{E}+00$ | 5ff 1 |
| 438 | 75p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff |
| 439 | $75 p$ | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |
| 440 | 75p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |
| 441 | $75 p$ | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |


| 442 | 75p | 0.78 um 0.0 | $0 \mathrm{E}+00$ | 4ff 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 443 | 75p | 0.78 um 0. | OE+00 | 5ff 1 |  |
| 444 | 100p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 445 | 100p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 446 | 100p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 447 | 100p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 448 | 100p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 449 | 100p | 0.78 um | $0.00 \mathrm{E}+00$ | 5 ff 1 |  |
| 450 | 150p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff |  |
| 451 | 150p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 452 | 150p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 453 | 150p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 454 | 150p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 455 | 150p | 0.78 um | $0.00 \mathrm{E}+00$ | $5 f f 1$ |  |
| 456 | 200p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 457 | 200p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 458 | 200p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 459 | 200p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 460 | 200p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 461 | 200p | 0.78 um | $0.00 \mathrm{E}+00$ | 5 ff 1 |  |
| 462 | 250p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 463 | 250p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 464 | 250p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 465 | 250p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 466 | 250p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 467 | 250p | 0.78 um | $0.00 \mathrm{E}+00$ | $5 f f 1$ |  |
| 468 | 300 p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 469 | 300p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 470 | 300 p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 471 | 300p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 472 | 300 p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 473 | 300p | 0.78 um | $0.00 \mathrm{E}+00$ | 5 ff 1 |  |
| 474 | 350p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 475 | 350p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |


| 476 | 350p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 477 | 350p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 478 | 350p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 479 | 350p | 0.78 um | $0.00 \mathrm{E}+00$ | 5 ff 1 |  |
| 480 | 400p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 481 | 400p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 482 | 400p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 483 | 400p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 484 | 400p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 485 | 400p | 0.78 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 486 | 450p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 487 | 450p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 488 | 450p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 489 | 450p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 490 | 450p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 491 | 450p | 0.78 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 492 | 500p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 493 | 500p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 494 | 500p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 495 | 500p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 496 | 500p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 497 | 500p | 0.78 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 498 | 750p | 0.78 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 499 | 750p | 0.78 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 500 | 750p | 0.78 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 501 | 750p | 0.78 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 502 | 750p | 0.78 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 503 | 750p | 0.78 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 504 | 1 p | 0.975 um 0. | $0 \mathrm{E}+00$ | $0.5 \mathrm{ff} \quad 1$ |  |
| 505 | 1p | 0.975 um 0.0 | $0 \mathrm{E}+00$ | 1ff 1 |  |
| 506 | 1p | 0.975 um 0.0 | OE +00 | 2ff 1 |  |
| 507 | 1p 0 | 0.975 um 0.0 | $0 \mathrm{E}+00$ | 3ff 1 |  |
| 508 | 1p | 0.975 um 0.0 | $0 \mathrm{E}+00$ | 4ff 1 |  |
| 509 | 1p 0 | 0.975 um 0.0 | $0 \mathrm{E}+00$ | 5ff 1 |  |


| 510 | 2p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 511 | 2p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 512 | 2p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 513 | 2p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 514 | 2p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 515 | 2p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 516 | 5p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 517 | 5 p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 518 | $5 p$ | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 519 | 5p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 520 | 5p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 521 | 5 p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 522 | 10p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 523 | 10p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 524 | 10p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 525 | 10p | $0.975 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 526 | 10p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 527 | 10p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 528 | 20p | $0.975 u m$ | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 529 | 20p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 530 | 20p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 531 | 20p | $0.975 u m$ | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 532 | 20p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 533 | 20p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 534 | 50p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 535 | 50p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 536 | 50p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 537 | 50p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 538 | 50p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 539 | 50p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 540 | 75p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 541 | 75p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 542 | 75p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 543 | 75p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |



| 578 | 350p | 0.975 um | $0.00 \mathrm{E}+00$ | 2 ff 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 579 | 350p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 580 | 350p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 581 | 350p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 582 | 400p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 583 | 400p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 584 | 400p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 585 | 400p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 586 | 400p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 587 | 400p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 588 | 450p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 589 | 450p | $0.975 u m$ | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 590 | 450p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 591 | 450p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 592 | 450p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 593 | 450p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 594 | 500p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 595 | 500p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 596 | 500p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 597 | 500p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 598 | 500p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 599 | 500p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 600 | 750p | 0.975 um | $0.00 \mathrm{E}+00$ | 0.5 ff | 1 |
| 601 | 750 p | 0.975 um | $0.00 \mathrm{E}+00$ | 1ff 1 |  |
| 602 | 750p | 0.975 um | $0.00 \mathrm{E}+00$ | 2ff 1 |  |
| 603 | 750 p | 0.975 um | $0.00 \mathrm{E}+00$ | 3ff 1 |  |
| 604 | 750p | 0.975 um | $0.00 \mathrm{E}+00$ | 4ff 1 |  |
| 605 | 750 p | 0.975 um | $0.00 \mathrm{E}+00$ | 5ff 1 |  |
| 606 | .END |  |  |  |  |
| 607 |  |  |  |  |  |
| 608 | .lib "./crn65gplus 2d5 1 k v1d0.1" tt bip npn |  |  |  |  |
| 609 | .lib "./crn65gplus_2d5_lk_v1d0.1" tt_rfres_sa |  |  |  |  |
| 610 | .lib "./crn65gplus_2d5_lk_v1do.1" tt_rfmvar |  |  |  |  |
| 611 | .lib "./crn65gplus_2d5_1k_v1do.1" tt_dio_esd |  |  |  |  |


| 612 | . 1 ib "./crn65gplus 2d5 lk v1d0.1" tt rtmom |
| :---: | :---: |
| 613 | .lib "./crn65gplus_2d5_lk_v1d0.1" tt_rfmvar_25 |
| 614 | .lib "./crn65gplus 2d5 lk v1do.1" tt disres |
| 615 | .lib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_na |
| 616 | .lib "./crn65gplus_2d5_lk_v1do.1" tt |
| 617 | .lib "./crn65gplus_2d5_1k_v1d0.1" tt_mim |
| 618 | .lib "./crn65gplus_2d5_lk_v1d0.1" tt_rfrtmom |
| 619 | .lib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_na25od33 |
| 620 | .lib "./crn65gplus_2d5_lk_v1do.1" tt_rfres_rpo |
| 621 | .lib "./crn65gplus_2d5_lk_v1do.1" tt_dio_hvt |
| 622 | .lib "./crn65gplus_2d5_1k_v1d0.1" tt_na25od33 |
| 623 | .lib "./crn65gplus_2d5_1k_v1d0.1" tt_rfmim |
| 624 | .lib "./crn65gplus_2d5_lk_v1d0.1" tt_25od33 |
| 625 | . lib "./crn65gplus_2d5_lk_v1d0.1" tt_res |
| 626 | .lib "./crn65gplus_2d5_1k_v1do.1" tt_dio_lvt |
| 627 | .lib "./crn65gplus_2d5_lk_v1do.1" tt_25udis |
| 628 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_bip |
| 629 | .lib "./crn65gplus_2d5_lk_v1d0.1" tt_mos_cap |
| 630 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_na33 |
| 631 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_25udi8 |
| 632 | .lib "./crn65gplus_2d5_lk_v1d0.1" tt_na33 |
| 633 | .lib "./crn65gplus_2d5_1k_v1do.1" tt_18 |
| 634 | .lib "./crn65gplus_2d5_1k_v1do.1" tt_na |
| 635 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_dio |
| 636 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_25od33 |
| 637 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_hvt |
| 638 | .lib "./crn65gplus_2d5_1k_v1d0.1" tt_rfind |
| 639 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_rfmos_33 |
| 640 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_lvt |
| 641 | .lib "./crn65gplus_2d5_lk_v1d0.1" tt_na25 |
| 642 | . 1 ib "./crn65gplus_2d5_1k_v1do.1" tt_rfmos_25 |
| 643 | .lib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_dnw |
| 644 | .lib "./crn65gplus_2d5_lk_v1do.1" tt_rfjvar |
| 645 | .lib "./crn65gplus_2d5_lk_vldo.1" tt_rfmos |
| 646 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_na25 |
| 647 | . lib "./crn65gplus_2d5_1k_v1d0.1" tt_rfmos_18 |
| 648 | .1ib "./crn65gplus_2d5_1k_v1do.1" tt_mos_cap_25 |
| 649 | .lib "./crn65gplus_2d5_1k_v1do.1" tt_33 |
| 650 | . 1 ib "./crn65gplus_2d5_1k_v1do.1" tt_25 |
| 651 | .lib "./crn65gplus_2d5_1k_v1do.1" tt_dio_33 |
| 652 | . 1 ib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_25 |
| 653 | .lib "./crn65gplus_2d5_1k_v1d0.1" tt_dio_18 |
| 654 | . end |

## Matlab code for first case

```
Time = [ 1.490000E-08 1.490001E-08 1.490002E-08 1.490C
Itest = [ [ 8.66E-09 8.66E-09 8.66E-09 8.66E-09 8.67E-09
Istest = [ 5.46E-09 5.46E-09 5.46E-09 5.46E-09 5.46E-C
deltao =1533
delta =1250
mult = 1.15
Itest2 = [zeros(1,delta) Itest]
Itest3 = Itest2 (1:110001)
Itest3(19573:110001) = Itest2(19573:110001).*mult
Itestsum = cumtrapz(Itest).*20
Istestsum = cumtrapz(Istest).*20
Itest3sum = cumtrapz(Itest3).*20
[c] = find(Istestsum<=-0.6 & Istestsum>-0.61)
tsmid = Time(c(1))
[c] = find(Itest3sum<=-0.6 & Itest3sum>-0.61)
tmmid = Time(c(1))
[c] = find(Itestsum<=-0.6 & Itestsum>-0.61)
tomid = Time(c(1))
delerr = tsmid - tmmid
[c] = find(Istestsum<=-0.12 & Istestsum>-0.15)
tsup = Time (c(1))
[c] = find(Itest3sum<=-0.12& Itest3sum>-0.15)
tmup = Time (c(1))
[c] = find(Itestsum<=-0.12 & Itestsum>-0.15)
toup = Time(c(1))
[c] = find(Istestsum<=-1.08 & Istestsum>-1.1)
tslow = Time(c(1))
[c] = find(Itest3sum<=-1.08& Itest3sum>-1.1)
tmlow = Time(c(1))
[c] = find(Itestsum<=-1.08 & Itestsum>-1.1)
tolow = Time(c(1))
trano = tolow -toup
trans = tslow - tsup
tranm = tmlow - tmup
tranerror = trans - tranm
pererr = delerr/2.06E-11
pertran = tranerror/trans
```


## Matlab code for second case

```
Time = [ 14.90000e-09 14.90001e-09 14.90002e-09 14.9@
Itest = [ -1.3042e-09 -1.3047e-09 -1.3051e-09 -1.3056
Istest = [ -1.2836e-09 -1.2840e-09 -1.2845e-09 -1.285
deltao =1533
delta =4500
Itest2 = [zeros(1,delta) Itest]
Itest3 = Itest2(1:110001)
Itestsum = cumtrapz(Itest).*20
Istestsum = cumtrapz(Istest).*20
mult = 1.15
Itest3(40427:110001) = Itest2(40427:110001).*mult
Itest3sum = cumtrapz(Itest3).*20
[c] = find(Istestsum<=-0.6 & Istestsum>-0.61)
tsmid = Time(c(1))
[c] = find(Itest3sum<=-0.6& Itest3sum>-0.61)
tmmid = Time(c(1))
[c] = find(Itestsum<=-0.6& Itestsum>-0.61)
tomid = Time(c(1))
delerr = tsmid - tmmid
    [c] = find(Istestsum<=-0.12 & Istestsum>-0.15)
    tsup = Time (c(1))
    [c] = find(Itest3sum<=-0.12 & Itest3sum>-0.15)
    tmup = Time(c(1))
    [c] = find(Itestsum<=-0.12 & Itestsum>-0.15)
    toup = Time(c(1))
    [c] = find(Istestsum<=-1.08 & Istestsum>-1.1)
    tslow = Time(c(1))
    [c] = find(Itest3sum<=-1.08 & Itest3sum>-1.1)
    tmlow = Time(c(1))
    [c] = find(Itestsum<=-1.08 & Itestsum>-1.1)
    tolow = Time(c(1))
    trano = tolow -toup
    trans = tslow - tsup
    tranm = tmlow - tmup
    tranerror = trans - tranm
    pertran = tranerror/trans
    pererr = delerr/5.41E-11
```

