

RESEARCH PAPER

A Novel CFD Method to Estimate Heat Transfer Coefficient for High Speed Flows

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ABSTRACT

Accurate prediction of surface temperature of high speed aerospace vehicle is very necessary for the selection of material and determination of wall thickness. For aerothermal characterisation of any high speed vehicle in its full trajectory, it requires number of detailed computational fluid dynamics (CFD) calculations with different isothermal calculations. From the detailed CFD calculations for different flow conditions and geometries, it is observed that heat transfer coefficients scale with the difference of adiabatic wall temperature and skin temperature. A simple 'isothermal method', is proposed to calculate heat flux data with only two CFD simulations one on adiabatic condition and other on isothermal condition. The proposed methodology is validated for number of high speed test cases involving external aerodynamic heating as well as high speed combusting flow. The computed heat fluxes and surface temperatures matches well with experimental and flight measured values.

Keywords: Aerodynamic heating, heat flux, thermal analysis, computational fluid dynamics, scramjet combustor

1. INTRODUCTION

Certain critical applications where working temperature is very high, it is necessary to calculate the temperature distribution in the solid to ensure it should not cross the metallurgical limit. The selection of material and wall thickness of high speed aerospace vehicle flow is largely dependent on accurate estimation of wall temperature distribution in the solid. Aerospace vehicles during ascent phase trajectory experience aerodynamic heating caused by viscous dissipation and the conversion of kinetic energy into thermal energy in the boundary layers surrounding the object. The combustion of fuel in high speed air stream (Ramjet/scramjet engines) also cause significant heat transfer to the combustor walls and fuel injecting devices.

In the past, the problem was simplified by calculating aerodynamic field and the temperature inside the solid body separately by imposing a prescribed wall heat flux or temperature at the interface. Thus, the complexity of heat transfer processes between the fluid and the vehicle structure is described by a pre-determined heat transfer coefficient which shows that the heat transfer process is independent of the solid properties. Different engineering methods¹⁻³ are proposed in the literature based on empirical formulae to estimate heat transfer coefficients for high speed flows. Eckert's method¹ uses reference enthalpy and boundary layer edge data for the estimation of heat transfer coefficient. Van Driest method² are based on flow past flat plates under zero pressure gradient and uses Reynold's analogy principle to calculate heat transfer coefficients. Fay and Riddle method³ calculates the stagnation point heat flux from the numerical solution of chemically reacting boundary layer flows under equilibrium conditions. Although, these methods

predicts heat transfer coefficients for engineering design for simple attached flows, but their applications to complex separated flows are not beyond doubt. To cater the uncertainty in the methodology, various design factors are introduced and vehicle structures become heavier. With the advent of powerful computer and robust numerical algorithms, conjugate heat transfer (CHT) methods⁴⁻⁶ are introduced in high speed fluid flow by solving simultaneously Navier Stokes Equations in fluid region and heat conduction equation in solid region. Although these method are promising, but they are yet to fully mature for engineering design. Moreover, these methods require extensive computer speed and memory.

Due to inadequacy of empirical correlations and high turn about times of CHT methods, transient thermal analysis of high speed aerospace vehicle structures mostly depend on heat flux calculated from high fidelity CFD solution. CFD based heat transfer prediction requires number of isothermal calculations to determine the heat flux data base for different wall temperatures. From detailed flow calculations for different geometries, it is observed that heat transfers coefficients (h) scale with the difference of adiabatic wall temperature (T_{aw}) and skin temperature (T_w) as $h = \dot{q} / (T_{aw} - T_w)$. Based on this observation a simple method, referred as 'isothermal method', is proposed to calculate heat flux with only two CFD simulations one on adiabatic condition and other on isothermal condition. The proposed methodology is validated for number high speed test cases for both external and internal flows.

2. ANALYSIS

The heat transfer to a surface in high-speed flow⁷ can be calculated as,

$$q = S_t * \rho_e * U_e * (E_{aw} - E_w) \quad (1)$$

where S_t is the stanton number and E_{aw} and E_w are the adiabatic

wall enthalpy and the wall enthalpy respectively. To take into account irreversible processes in the boundary layer flow, the adiabatic wall enthalpy may be expressed in terms of a recovery factor r as

$$E_{aw} = E_e + r*(E_0 - E_e) \quad (2)$$

where E_e and E_0 are the free-stream static and total enthalpies, respectively. The recovery factor (r) is typically written in terms of the Prandtl number $\left(\text{Pr} = \frac{\mu \times C_p}{K}\right)$ and is taken as $Pr^{1/2}$ for laminar flow and $Pr^{1/3}$ for turbulent flow⁷. Where C_p is the specific heat at constant pressure, μ is the free-stream dynamic viscosity and K is the thermal conductivity of the fluid.

High fidelity RANS simulations with fine resolution of boundary layer ($Y^+ \sim 1$), gives directly the wall heat flux for a fixed wall temperature. Heat flux obtained from one fixed wall temperature is not same for different wall temperatures. In the proposed 'isothermal method' methodology, cold wall heat flux (\dot{q}_{cw}) is calculated based on cold wall temperature (T_{cw}) and wall heat fluxes (\dot{q}_w) at other wall temperatures are scaled to the local wall temperature utilizing adiabatic wall temperature as given below,

$$\text{Local wall heat flux } \dot{q}_w = \dot{q}_{cw} \times \left[\frac{T_{aw} - T_w}{T_{aw} - T_{cw}} \right]$$

This 'isothermal method' requires one CFD simulation with isothermal wall and another CFD simulation with adiabatic wall at every trajectory point.

2.1 The CFD Methodology

Commercial CFD software Ansys Fluent⁸ is used for simulating three validation cases namely, turbulent flow past circular cylinder at Mach 6.47, Kinetic heating of nose cone of an aerospace vehicle from subsonic to Mach 8 and Hydrogen fuelled scramjet combustor with wall injection; while, CFX-Tasc flow⁹ is used for the simulation of hydrocarbon fuelled scramjet combustor with strut injection. Ansys Fluent⁸ solves three-dimensional Navier Stokes equations (conservation of mass, momentum, energy and species continuity) in a hybrid grid system using a collocated variable arrangement. Density based solver along with Roe flux difference splitting scheme¹⁰ is used to simulate high Mach number compressible flow.

CFX is a fully implicit three dimensional Reynolds Averaged Navier-Stokes (RANS) code. The code is fully implicit, finite volume method with finite element based discretisation of geometry. The method retains much of the geometric flexibility of finite element methods as well as the important conservation properties of the finite volume method. It utilises numerical upwind schemes to ensure global convergence of mass, momentum, energy and species. The convective terms are discretised using a 2nd order scheme. Turbulence was modeled using k - ϵ model¹¹ and wall functions were used to model flow near the walls.

For combustion, the eddy dissipation model (EDM)¹² is used for its simplicity and robustness in predicting the performance of reactive flows in many engineering applications. The eddy dissipation model is based on the concept that chemical reaction is fast compared to the transport

process in the flow. The model assumes that the reaction rate may be related directly to the time required to mix reactants at molecular level. In turbulent flows, the burning rate is assumed to be proportional to the rate at which turbulent kinetic energy is dissipated i.e., reaction rate is proportional to ϵ/k , where, k is the turbulent kinetic energy and ϵ is its rate of dissipation. Both hydrogen fuel and kerosene fuels are used for the reacting flows in the present simulation. Hydrogen oxidation is modelled with single step reaction $2H_2 + O_2 \rightarrow 2H_2O$, while, kerosene ($C_{12}H_{23}$) oxidation is represented on a molar basis by $C_{12}H_{23} + 17.75O_2 = 12CO_2 + 11.5H_2O$. The mixing rate determined from the EDM is given as.

$$R_{k,EDM} = -A_{ebu} \rho \frac{\epsilon}{k} \min \left\{ y_f, \frac{y_{ox}}{r_k}, B_{ebu} \frac{y_p}{1+r_k} \right\}$$

where ρ and y_f, y_{ox} and y_p are the density and mass fractions of fuel, oxidizer and products, respectively, A_{ebu} and B_{ebu} are the model constants and r_k is the stoichiometric ratio.

Lagrangian particle tracking method (LPTM) is used for discrete phase model to characterise the flow behavior of the dispersed phase fluid (kerosene liquid) alongwith the flow of the continuous phase predicted using a discretised form of the RANS equations. Log-normalised maximum residue of -04 is considered as the convergence criteria. The software is thoroughly validated for nonreacting flows as well as reacting flow with hydrogen and hydrocarbon fuels and the simulation results were published¹³⁻¹⁶.

3. VALIDATION TEST CASES

Following four test cases are selected for the validation of the proposed method described above.

- (i) Turbulent flow past circular cylinder at Mach 6.47
- (ii) Kinetic heating of nose cone of an aerospace vehicle from subsonic to Mach 8
- (iii) Hydrogen fuelled scramjet combustor with wall injection.
- (iv) Hydrocarbon fuelled scramjet combustor with strut injection.

First two test cases pertain to external aerodynamic heating where free stream Mach number ranges from low supersonic to hypersonic; while next two cases relate to internal heating in a scramjet combustor where flow velocities are of the order of 1000 m/s. Computed heat fluxes and surface temperatures are compared with the available literature and flight data.

3.1 Test case-1: Turbulent Flow Past Circular Cylinder at Mach 6.47

A 76.2 mm diameter, 12.7 mm thick 610 mm long cylinder made of AISI-321 is tested at Mach 6.47 in the 8 ft high temperature hypersonic blowdown tunnel¹⁷ as shown in Fig. 1. The vitiated gas at test section is having Mach number, pressure, temperature, and Reynolds number of 6.47, 648 Pa, 241.5 K, and 1.312×10^6 per m, respectively. Pressure transducers and high response coaxial thermocouples were used to measure the flow field and heating rate distribution at various locations. Details of the experimental configurations, the tunnel flow conditions, and the experimental results are given¹⁷. As shown in Fig. 1.

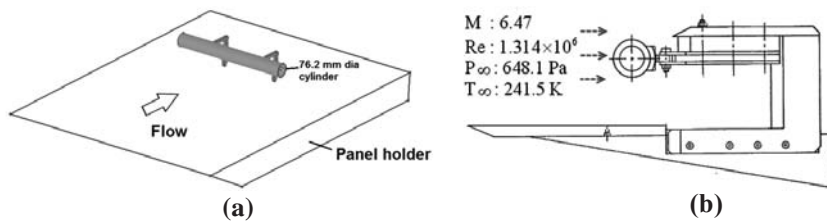


Figure 1. Schematic of (a) experimental setup¹⁷ and (b) tunnel flow conditions.

Very fine structured grid involving 140 X 110 grid points with minimum grid spacing of 1 μm is employed. To predict the heating rate accurately, wall boundary layer is resolved with very fine mesh which corresponds to Y^+ of 0.2. A very fine mesh (140x20) is also taken in the solid region of the cylinder. Time step of 1 ms is employed in the solution of RANS equations using Ansys Fluent⁸. The grid independence of the simulation results are presented¹⁸ and are not repeated here. As the Reynolds number in the test section is 1.312×10^6 per meter, transitional simulation is performed by employing Menter’s 4 equation transition model¹⁹. The predicted pressure and temperature behind the shock wave are in good agreement with other calculation reported²⁰ indicating that overall flow features are well captured.

The constancy of heat transfer coefficient for different wall temperature is shown in Fig. 2. It is clearly observed that azimuthal distribution of heat transfer coefficients collapsed into a single curve for different wall temperatures. The computed cold wall heat flux is compared with the experimental and other numerical results²⁰ in Fig. 3. There is

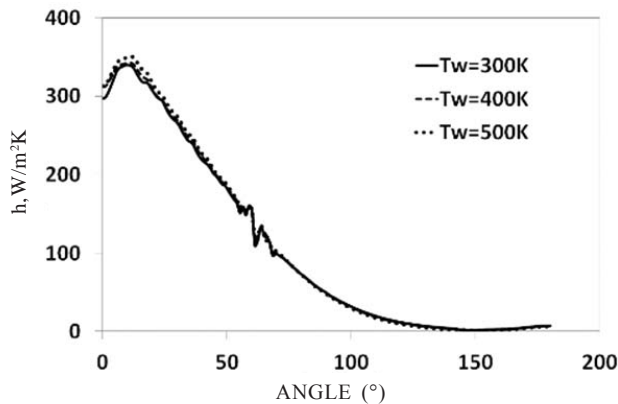


Figure 2. Azimuthal variation of heat transfer coefficients for different wall temperatures.

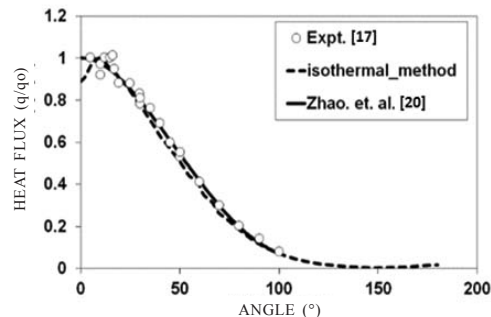
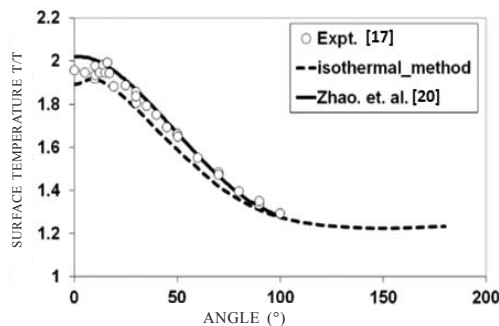


Figure 3. Heat flux and surface temperature variation along cylinder.

close agreement for the results of isothermal method with experiment. As we proceed away from the stagnation point, the heat flux is reducing exponentially. In the region $10^\circ < \theta < 25^\circ$, the experimental heat flux rate is showing some oscillatory trend which is not observed in the computed values. The circumferential variation of predicted surface temperature is compared with experimental results and computed results of Zhao²⁰, *et al.* in Fig 3. The computed heat flux and surface temperature matches well with the experimental results; while the computation of Zhao²⁰, *et al.* showed higher values in the region $10^\circ < \theta < 25^\circ$.

3.2 Kinetic Heating of Nose Cone of an Aerospace Vehicle from Subsonic to Mach 8

The schematic of the nose cone section of a high speed aerospace vehicle with temperature measurement locations are shown in Fig. 4. Eight Number of temperature sensors were located at $X/d=1$ and $X/d=2$ locations. The peak Mach number, altitude, angle of attack and side slip angle are 7 km, 45 km, 12° and 10° , respectively. About 70 points are selected along the trajectory to perform a detailed kinetic heating analysis along the trajectory with detailed 3D RANS calculation with $k-\epsilon$ turbulence model using Ansys Fluent⁸. Axial distribution of heat transfer coefficients with different wall temperature is shown in Fig. 5 to depict constancy of heat transfer coefficients with different wall temperatures.

Figures 6 and 7 show the comparison of predicted wall temperatures with flight measured values for locations T1 to T8. Isothermal method captured the trend of flight measurements for all locations and performed very well for the first axial location ($X/d = 1$). The method over predicts the surface temperature (about 15% - 20%) for second axial location ($X/d = 2$).

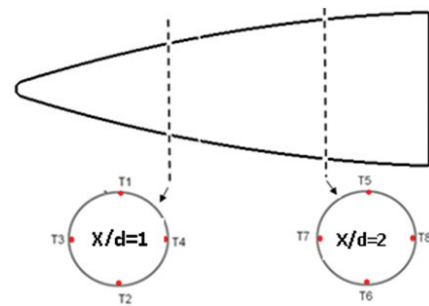


Figure 4. Schematic of nose cone with temperature measurement locations.

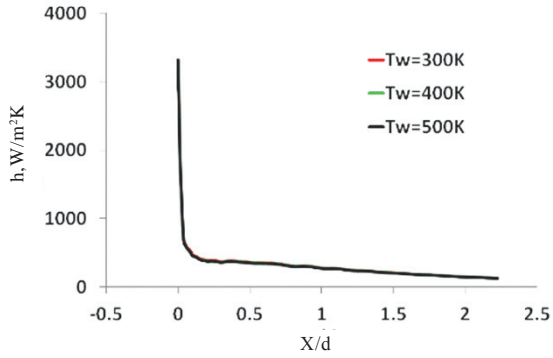


Figure 5. Heat transfer coefficient (h) distribution along axial direction for nose cone.

3.3 Hydrogen Fuelled Scramjet Combustor with Wall Injection

Development of scramjet engine is being pursued from early 1960s for hypersonic air breathing propulsion system for civil and military applications. Hydrogen fuelled scramjet combustor has been investigated experimentally and numerically for the last few decades. Efforts have continued to conduct well instrumented experimentation of scramjet combustor flow field to validate CFD data. The SCHOLAR experiment conducted at NASA Langley’s Direct Connect Supersonic Test facilities²¹⁻²² gives detailed measurements of temperatures and species mass fraction at various cross sections as well as wall pressures for hydrogen fuel is injected at 30° angle to Mach 2

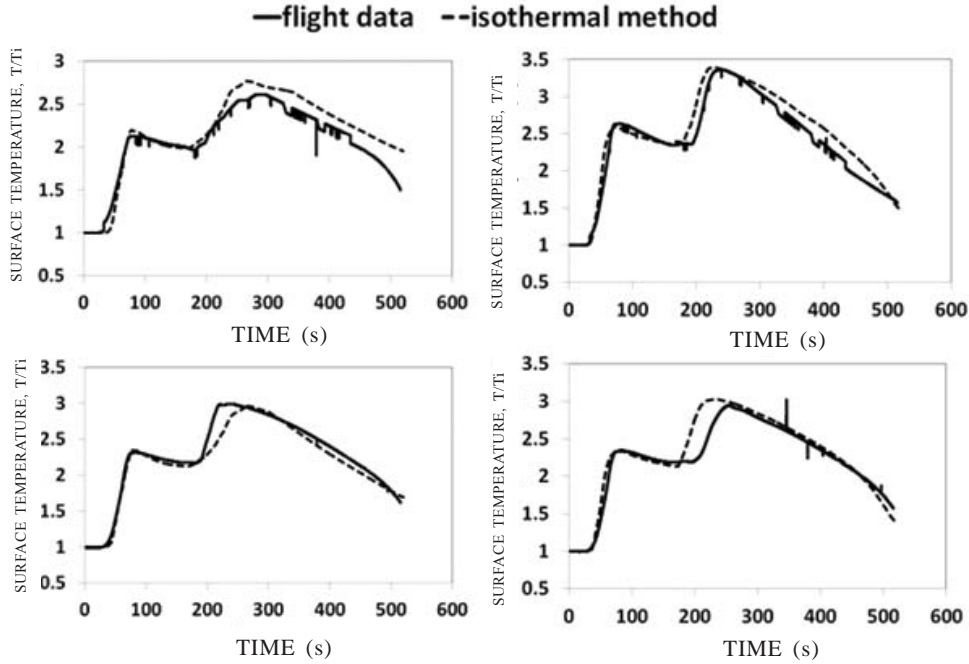


Figure 6. Comparison of wall temperature at $x/d = 1$ (a) T1, (b) T2 (c) T3 (d) T4.

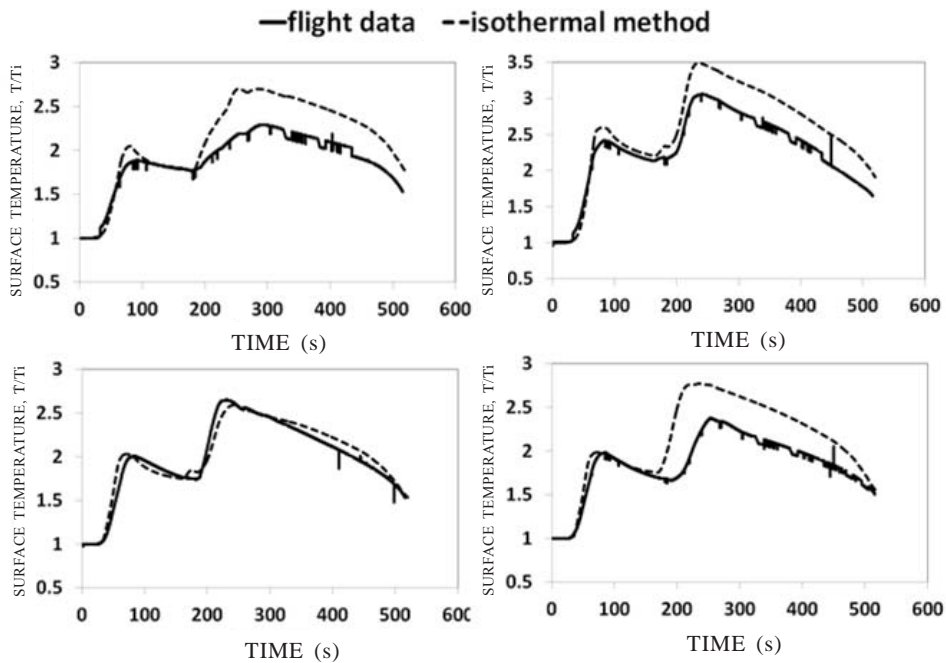


Figure 7. Comparison of wall temperature at $x/d = 2$ (a) T5, (b) T6 (c) T7 (d) T8.

airstreams with 1200 K temperature in a divergent duct. The schematic of the experimental condition is shown in Fig. 8. The reacting flow field of SCHOLAR experiment was simulated extensively numerically through RANS as well as LES models by many researchers with different chemical kinetics schemes, turbulence models and well reported in the literature²³⁻²⁷.

Front section of the combustor (containing the isolator and injector) is made of copper while the rear section is made of carbon steel. The thickness of the copper section is 45 mm while the thickness of the carbon steel section is 18 mm. The wall thickness and the conductivity of the materials allow the combustor to run without cooling. Since, the duct is uncooled, surface temperatures vary greatly during the test. Temperature history is measured in the combustor at two locations ($X=197$ mm and 426 mm) for the copper section and one location for the carbon steel block ($X=978$ mm). Three dimensional unsteady heat conduction equation is solved to determine the thermal response of the combustor wall to the hot combusting gas in the duct using CFD generated convective heat flux data with different isothermal conditions (300 K, 500 K, 750 K, 1000 K). The axial distribution of heat transfer coefficient $h = \dot{q} / (T_{aw} - T_w)$ is presented in Fig. 9. We can observe that for different isothermal calculations, heat flux distribution collapse into regular curve when scaled with $(T_{aw} - T_w)$ for the entire domain. Hence, for thermal response calculations, it is sufficient to carryout two different CFD simulations (one adiabatic and one isothermal). For any other isothermal condition heat flux can be estimated by employing $h = \dot{q} / (T_{aw} - T_w)$. The computed wall temperature history at two different locations $X = 426$ mm (near the end of copper section) and $X = 978$ mm (middle of carbon steel section) are compared with experimental data in Fig. 10. Computed temperature over predicts ($\sim 10\%$) the experimental value at $X = 426$ mm and under predicts ($\sim 10\%$) the temperature

at $X = 978$ mm. Whether the temperature dependent material properties can narrow these differences further is not investigated.

3.4 Hydrocarbon Fuelled Scramjet Combustor with Strut Injection

Due to higher energy density and easier handling issue, liquid hydrocarbons fuels are considered for the scramjet engine for volume limited applications in the lower hypersonic ($M < 8$) flight regimes. Atomisation, vaporisation, mixing and slow chemical reactions are some of the major technical and scientific problems in the realisation of liquid hydrocarbon based scramjet engine. Strut based injection systems are being considered to alleviate the problem of slow lateral fuel transport in the air stream. Kerosene fuelled scramjet combustor for an hypersonic airbreathing mission²⁸ are numerically explored for design optimisation and important reacting flow field results including grid independence studies are presented^{29,30}. Typical half scale scramjet combustor is shown in Fig. 11 which has divergence in vehicle upper surface. Kerosene fuel is injected through 220 injection holes (with 0.5 mm diameter for each hole) provided through 10 struts. For doing detailed thermostructural analysis of the combustor wall, number of reacting simulations with equivalence ratio 1.0 is carried out for different wall temperatures. The distribution of average heat transfer coefficient for top wall for three isothermal wall conditions (600 K, 800 K, and 1000 K) are shown in Fig. 12. The constancy of heat transfer coefficients for different wall temperatures are also observed in the simulation. Similar observations are also found for the heat transfer coefficients of other walls. Typical heat flux distribution on all the walls of the combustor is shown in Fig. 13. The computed heat flux is used in transient thermal analysis to select the material and thickness of combustor wall. It was observed that for both high

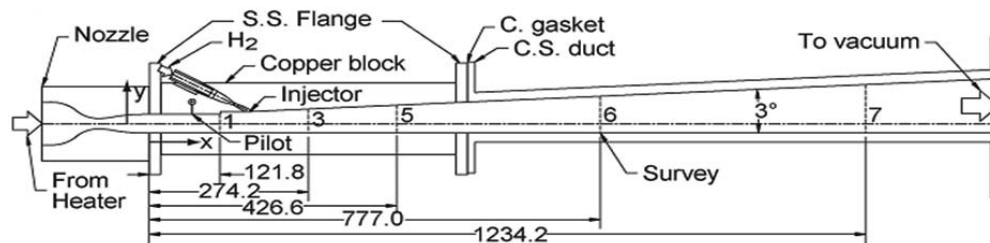


Figure 8. Schematic of Scholar experiment geometry²¹.

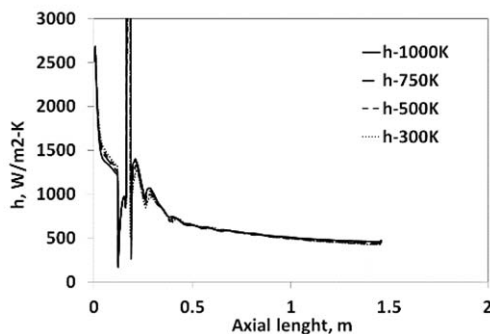


Figure 9. Axial distribution of convective heat transfer coefficient for different wall temperature

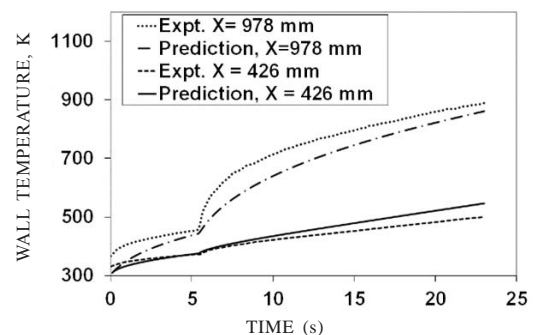


Figure 10. Comparison of wall temperature at locations $X = 426$ mm and 978 mm.

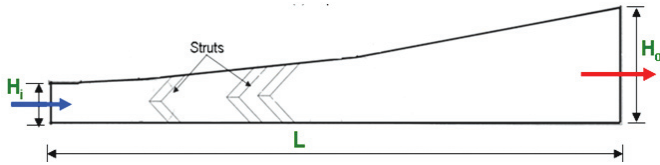


Figure 11. Schematic of the scramjet combustor.

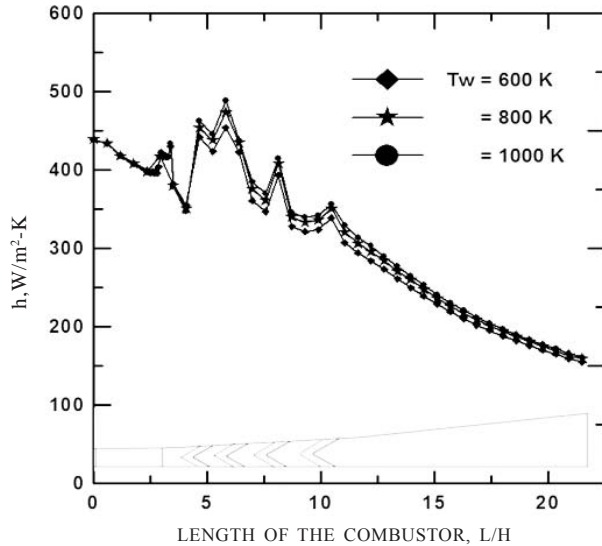


Figure 12. Axial distribution of heat transfer coefficients at upper wall.

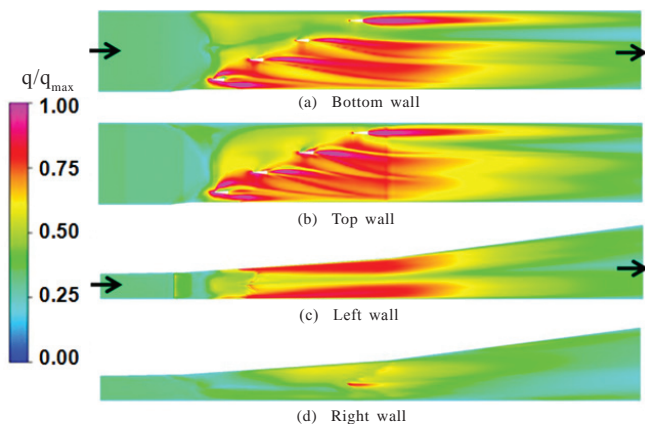


Figure 13. Heat flux distribution at scramjet combustor walls.

speed external and internal flows, the role of gas dynamics is very prominent and the flow is governed more by kinetic energy of the flow and less by sensible enthalpy.

4. CONCLUSION

Detailed aerothermal analysis is performed for high speed vehicle airframe using heat flux data from high fidelity CFD calculations. Reynolds Averaged Navier Stokes (RANS) equations are solved alongwith turbulence and combustion models using using commercial CFD software. It is observed that heat transfer coefficients scales with the difference of adiabatic wall temperature and skin temperature for different geometries and flow conditions. A new 'isothermal method', is proposed to calculate heat flux data for different wall temperature with only two CFD simulations one on adiabatic

condition and other on isothermal condition. The proposed methodology is validated for different test cases including high Mach number turbulent flow past a cylinder, kinetic heating of nose-cone of high speed aerospace vehicle in its full trajectory, hydrogen and kerosene fuelled scramjet combustor airframe. The predicted surface temperatures matches well with experimental and flight measured values. The methodology reduces the need to perform number of high fidelity CFD calculation with different isothermal conditions and is being used to perform detailed aerothermal analysis for the airframe of different high speed vehicles for material selection and wall thickness determination. It was observed that for both high speeds external and internal flows, kinetic energy govern the flow dynamics more than the sensible enthalpy.

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In current study, he has carried out grid generation, numerical simulation and analysis of the results for turbulent flow past circular cylinder and kinetic heating of nose cone.

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In current study, he has carried out grid generation, numerical simulation and analysis of the results of hydrocarbon fuelled scramjet combustor with strut injection.

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