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1 Investigation of aerodynamic performance
2 characteristics of a wind-turbine-blade profile using the
3 finite-volume method

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14 **Abstract**

15 Two-dimensional incompressible flow around a NACA 63-415 airfoil,
16 which is encountered in engineering applications as a typical
17 wind-turbine-blade profile, is investigated computationally. Aerodynamic
18 loads and the flow mechanism over this particular blade profile are
19 examined in detail to determine the optimum angle of attack. Simulations
20 are performed in the range of the typical operating conditions encountered
21 for commercial-scale wind turbines with Reynolds numbers
22 $10^5 \leq Re \leq 3 \times 10^6$ and for angles of attack $0^\circ \leq \alpha \leq 20^\circ$. The turbulent
23 flow was modelled by means of the Spalart-Allmaras and the Shear-Stress
24 Transport (SST) $k-\omega$ turbulence models to provide a direct comparison
25 between data obtained with different models. The results obtained are
26 compared to numerical and experimental data available in literature for

27 validation. The aerodynamic performance analysis reveals that the optimum
28 angle of attack for this blade profile is $\alpha = 6^\circ$ for $Re \leq 10^6$ and $\alpha = 7^\circ$ for
29 $Re \geq 1.6 \times 10^6$.

30 *Keywords:* Aerodynamic performance, Blade profile, Finite volume
31 method, Numerical simulation, Wind turbines

32 1. Introduction

33 The global usage of renewable energy, as an alternative to conventional
34 energy resources, has reached approximately 10.4% of the total energy
35 production and continues to increase [1]. Wind energy, specifically, is one of
36 the most important renewable resources since it is accessible in most parts
37 of the world and since it constitutes a continuous and reliable energy source
38 to drive wind turbines.

39 Although wind energy can provide almost steady and dependable power,
40 using this energy effectively can be difficult. The very first constraint
41 regarding the generation of electricity using wind turbines is the Betz
42 coefficient. This is known as Betz's law which indicates the limitations of a
43 wind turbine as regards extracting a fraction of the available total kinetic
44 energy of the wind [2]. According to this law, the efficiency of wind turbines
45 is restricted to approximately 59.3%. In addition to this limit, unavoidable
46 factors such as surface roughness due to contamination, erosion and icing,
47 as well as design parameters (e.g. the angle of attack) have a significant
48 effect on the aerodynamic efficiency of wind turbine blade profiles. Due to
49 the large number of the relevant parameters, investigations on wind-turbine
50 efficiency remain to be a challenging and vibrant research topic [3].

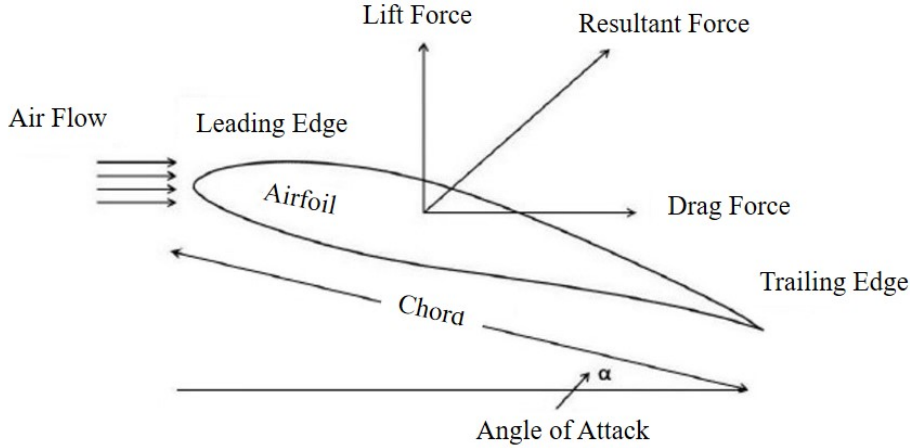


Figure 1: Forces acting on an airfoil [4].

51 The angle of attack, α , of the wind turbine blade (cf. Figure 1) as a
 52 design parameter is one of the most crucial aspects in the industrial wind-
 53 turbine design and it has been intensively studied for many different profiles
 54 of turbine blades [5, 6, 7, 8, 9]. The current investigation focusses on the
 55 determination of the lift to drag ratio of the blade. This represents the
 56 ratio of the acting lift and drag force, indicated in Figure 1, on the blade
 57 geometry. Following Liu et al. [10], the lift force and the drag force are given
 58 by, respectively, Equation 1 and Equation 2.

59

$$60 \quad F_L = \frac{1}{2} \times \rho \times C_L \times A_L \times V^2 \quad (1)$$

61

$$62 \quad F_D = \frac{1}{2} \times \rho \times C_D \times A_D \times V^2 \quad (2)$$

63 Here, ρ is the density of air, A_L is the projected wing area, A_D is the
64 rotor blade's cross-sectional area and V is the velocity of the oncoming air.
65 The quantities C_L and C_D are referred to, respectively, as the lift and the
66 drag coefficients. The lift to drag ratio is defined as C_L/C_D and is mostly
67 used as an indicator of efficiency [9, 11, 12, 13]. Note that Equations 1
68 and 2 are not predictive. Knowledge of C_L and C_D is required to find F_L
69 and F_D but the two coefficients remain unknown unless experiments or
70 computational simulations have been performed for the particular airfoil
71 under consideration.

72 The US National Advisory Committee for Aeronautics (NACA) has
73 developed numerous different airfoil shapes. These are referred to by the
74 prefix NACA followed by a series of digits identifying the characteristics of
75 the particular airfoil (cf. Section 2.1). The NACA 63-415 airfoil is one of
76 the most commonly used blade profiles for commercial wind turbines [14].
77 For instance, a wind turbine with a power capacity of 1.8 MW, produced by
78 the manufacturer Vestas Wind Systems A/S, is composed of a NACA 63
79 XXX blade profile between the blade tip and its centre [15]. However, the
80 determination of the optimum angle of attack for this specific airfoil has
81 been rarely studied in the literature.

82 Chaudhary and Nayak [12], for instance, examined the flow over the
83 NACA 63-415 profile using only the Shear-Stress Transport (SST) $k - \omega$
84 turbulence model and within limited ranges of the angle of attack and the
85 Reynolds number, for the purpose of comparison with data for a NACA
86 63-412 airfoil. They concluded that the NACA 63-415 airfoil performs
87 better as a wind turbine blade than NACA 63-412 for the particular flow

88 conditions investigated in that study. The results of Chaudhary and
89 Nayak [12] motivated the current study to investigate the optimum angle of
90 attack for the NACA 63-415 airfoil for a broader range of flow conditions
91 and, in particular, by also implementing different turbulence models. In the
92 current study, the analyses were, therefore, performed in the range of
93 $Re = 10^5 \leq Re \leq 3 \times 10^6$ and angles of attack $0^\circ \leq \alpha \leq 20^\circ$. The Reynolds
94 number used in this study is given by Equation 3 where c is the chord
95 length and μ is the dynamic viscosity of air.

96

$$97 \quad Re = \frac{\rho V c}{\mu}. \quad (3)$$

98 Moreover, Vendan et al. [16] investigated the flow over the NACA 63-415
99 profile for low Reynolds numbers by means of solely the Spalart-Allmaras
100 turbulence model. They reported that the optimum angle of attack under
101 their low Reynolds number flow conditions is $\alpha = 2^\circ$. However, the optimum
102 angle of attack needs to be considered not only for low Reynolds numbers
103 but also for the parameter regime that covers the operating conditions of a
104 commercial-scale wind turbine.

105 The shortcomings of the studies by Chaudhary and Nayak [12] and
106 Vendan et al. [16] motivated the current research to analyze the flow over
107 the NACA 63-415 airfoil as a wind turbine blade over a wider range of the
108 Reynolds numbers and for various angles of attack. Here incompressible,
109 two-dimensional (2D) flow over the NACA 63-415 airfoil is examined
110 computationally by means of the commercial Computational Fluid
111 Dynamics (CFD) software, Fluent, and by using the Reynolds-Averaged
112 Navier Stokes (RANS) based Spalart-Allmaras [17] and SST $k - \omega$ [18]

113 schemes to model turbulence. The Spalart-Allmaras turbulence model is a
114 well-known approach to model aerodynamic flows [19, 20, 21]. Similarly,
115 the SST $k-\omega$ model is widely used for the investigation of flow over NACA
116 airfoils [22, 23, 24]. Suvanjumrat [25], for instance, compared different
117 turbulence models and concluded that the SST $k-\omega$ model is suitable for
118 the simulations of flow over NACA airfoils. Furthermore, it has been shown
119 that the SST $k-\omega$ model can provide precise results for flows with an
120 adverse pressure gradient [23] and flows over airfoils where flow separation
121 of the boundary layer occurs [26, 27].

122 Moreover, the application of CFD for the investigations of the flow
123 mechanism around turbine blades is quite common since it can provide
124 valuable insights into rotor aerodynamics which is a principal factor for
125 maximizing the efficiency of transforming wind energy into mechanical
126 energy [22]. Currently, commercial wind-turbine blade-design procedures
127 are based on Blade Element Momentum (BEM) theory [28]. Nevertheless,
128 numerical studies concerning the aerodynamic performance of a rotor can
129 range from BEM models integrated by CFD simulations to full
130 three-dimensional (3D) Navier-Stokes solutions. Prior to the comprehensive
131 design of the wind turbine power production, investigations of the rotor
132 aerodynamics by means of 2D CFD approaches can represent valuable
133 contributions to the research area of wind energy. Furthermore, as it is
134 stated by Ge et al. [24], 3D secondary flows, such as the spanwise flow, are
135 often less important for a rotor blade section far away from the hub and the
136 tip since the flow here is governed by the streamwise flow.

137 Sayed et al. [9], for instance, investigated the flow over blade profiles

138 S809 and S826 at low Reynolds numbers by means of 2D numerical
139 finite-volume simulations. Successively, Sayed et al. [22] performed 2D
140 aerodynamic examinations for different blade profiles at high wind speeds.
141 Moreover, NACA 0008 and NACA 0012 blade profiles were
142 aerodynamically analysed by Hoogedoorn et al. [29] at high Reynolds
143 numbers ($Re > 10^6$) using 2D CFD-RANS simulations. Mohamed [30],
144 additionally, performed 2D numerical investigations for 20 different airfoils
145 including NACA 00XX and NACA 63XXX series for comparison.
146 Two-dimensional CFD simulations were also compared with experimental
147 results by Singh et al. [31] and a good agreement was observed in pressure
148 distribution over their blade profile. Another comparison with experimental
149 results were carried out by Daróczy et al. [32] for the flow over H-Darrieus
150 rotor blades. Experimental data were compared with 2D CFD results
151 obtained by various turbulence models and eventually, the Realizable k- ϵ
152 and the SST k- ω models were reported as best prediction models in 2D
153 numerical examinations. Wang et al. [33] compared their 2D numerical
154 results of power coefficients for the airfoil shapes investigated with the
155 experimental data of Castelli et al. [34] and stated that there is a
156 reasonable agreement between their results even though the tip losses are
157 ignored in 2D modelling.

158 Consequently, the current study will initially proceed to compare and
159 validate the different turbulence models to establish that they represent
160 suitable means for investigating flows around NACA airfoils. In the main
161 part of the study, the optimum angle of attack for the NACA 63-415 airfoil
162 is determined for a wide parameter range covering the typical operation

163 conditions of wind turbines. The results of this research benefit the design
164 process of new commercial wind-turbine blades, modifying existing ones
165 and it can serve as a benchmark simulation study in the area of the
166 applications of CFD to practical engineering problems.

167 **2. Material and method**

168 The characteristics of the airfoil considered in this study are summarized.
169 Thereafter the governing equations and the numerical scheme employed for
170 the research are introduced.

171 *2.1. The airfoil*

172 Airfoils from the NACA family have been widely used as blades for
173 commercial wind turbines since experimental data for most of these profile
174 types are readily available in the literature and through NACA [35, 36, 37].
175 The NACA 63-415 profile was used in the current research due to the lack
176 of comprehensive examination of the flow over this particular airfoil type
177 [14]. Furthermore, the NACA 63-415 airfoil has been shown to display good
178 stall characteristics such that it is often used for stall-regulated wind
179 turbines [38].

180 Each digit following the NACA series prefix in the name of the airfoil
181 quantifies a characteristic of the airfoil [35, 36, 38, 39]:

- 182 • The first digit states the series of the airfoil {6}.
- 183 • The second digit identifies the distance of the minimum pressure area
184 in tens of percent of chord {3}.

- 185 • The third digit specifies the lift coefficient in tenths {4}.
- 186 • The last two digits indicate the maximum thickness as percent of chord
- 187 {15}.

188 2.2. Governing Equations

189 A steady-state, two-dimensional, incompressible flow over the rotor
 190 blade profile is considered. The flow is governed by the steady-state
 191 Reynolds-averaged Navier-Stokes (RANS) equations, describing momentum
 192 conservation, together with requirement for mass conservation. The two
 193 relevant expressions are given by, respectively, Equation 4 and Equation 5
 194 [40, 41, 26].

$$\begin{aligned}
 \frac{\partial}{\partial x_j} (\rho u_i u_j) = & -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \left[\mu \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} - \frac{2}{3} \delta_{ij} \frac{\partial u_l}{\partial x_l} \right) \right] \\
 & + \frac{\partial}{\partial x_j} (-\overline{\rho u_i' u_j'})
 \end{aligned}
 \tag{4}$$

$$\frac{\partial}{\partial x_i} (\rho u_i) = 0
 \tag{5}$$

199 In these two expressions ρ is the average density, p is the average pressure,
 200 μ is the dynamic viscosity and $(-\overline{\rho u_i' u_j'})$ is the Reynolds stresses. For a
 201 proper turbulence modelling, in the Reynolds-averaged method, the Reynolds
 202 stresses need to be suitably modeled. A common approach adopted employs
 203 the Boussinesq hypothesis [42] relating the Reynolds stresses to the mean
 204 velocity gradients as shown in Equation 6.

$$-\overline{\rho u_i' u_j'} = \mu_t \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \left(\rho k + \mu_t \frac{\partial u_i}{\partial x_i} \right) \delta_{ij}
 \tag{6}$$

207 To close the RANS equations, that is to obtain a sufficient number of
208 equations for all unknowns of the problem, the turbulent (eddy) viscosity μ_t
209 and the turbulent kinetic energy k need to be described by means of
210 additional transport equations that depend on the particular turbulence
211 model used.

212 *2.3. The CFD model*

213 The geometry considered in the CFD simulations is shown in Figure 2,
214 it was defined by means of coordinate data acquired from the NACA airfoil
215 tools web site [37].

216 The discretization of the CFD model employs the C-type structured mesh
217 shown in Figure 3. This mesh structure is known to minimize the calculation
218 time for the type of CFD problems considered here [43, 44]. The proper
219 discretization of the computational domain is crucial since there may be
220 boundary layer separation over the blade profile at higher angles of attack
221 and, moreover, because von Kármán vortices can be formed downstream of
222 the airfoil. Accordingly, a careful mesh independence test was conducted and
223 the details of this test are discussed in Section 3.1.

224 Velocity inlet and pressure outlet boundary conditions were assigned to
225 regions A and B in Figure 2, respectively. The pressure outlet was defined as
226 atmospheric pressure and velocities at the inlet were calculated for associated
227 the Reynolds numbers of $Re = 10^5$, $Re = 5 \times 10^5$, $Re = 7 \times 10^5$, $Re = 10^6$,
228 $Re = 1.6 \times 10^6$, and $Re = 3 \times 10^6$. Different angles of attack, in the range
229 of $0^\circ \leq \alpha \leq 20^\circ$, were set by means of the components of the inlet velocity.
230 The main geometric parameters of the tested airfoil and the computational
231 domain together with the boundary conditions are listed in Table 1 where c

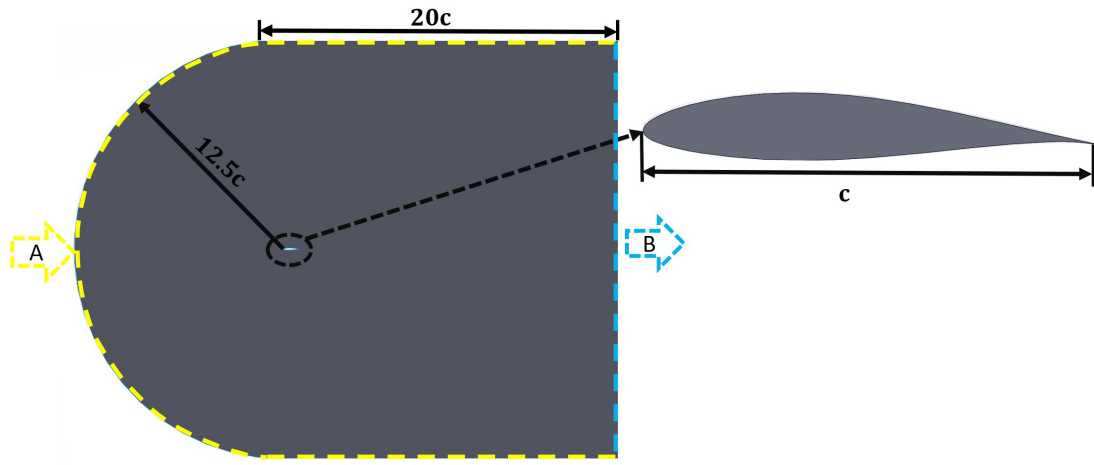


Figure 2: The CFD model and boundary conditions.

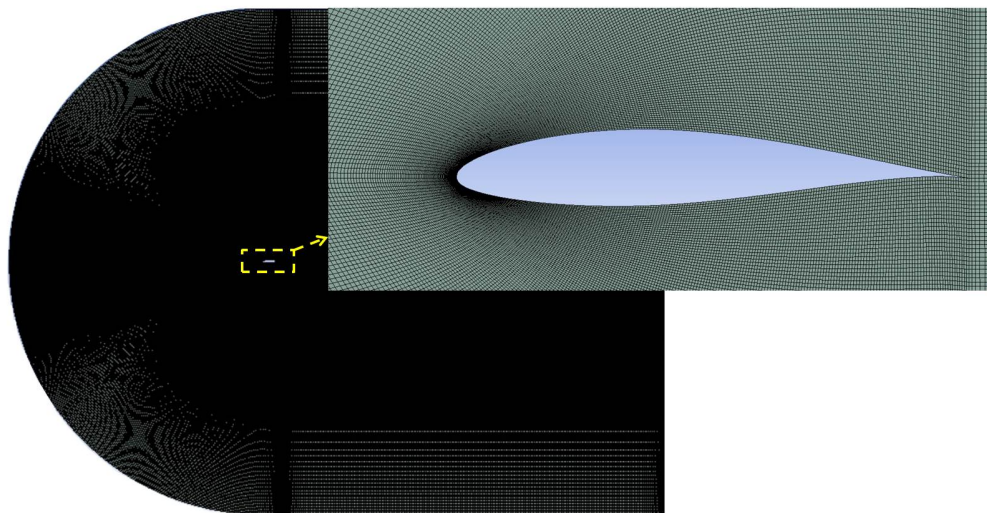


Figure 3: The discretization of the CFD model using C-type structured mesh.

Table 1: The main geometric parameters of the tested airfoil and the computational domain together with the boundary conditions (c is the chord length).

Airfoil Features		Computational Domain		Boundary Conditions	
Airfoil Category	NACA 6-Series	Rectangle Width	20c	Section A	Velocity Inlet
Airfoil Name	NACA 63-415	Radius	12.5c	Section B	Pressure Outlet
Max. Thickness Value	0.15c			Airfoil Surface	Smooth Wall
Max. Thickness Position	0.35c				
Max. Camber Value	0.022c				
Max. Camber Position	0.5c				

232 represents the chord length of the airfoil.

233 The surface of the blade profile was defined as a smooth wall and a no-slip
 234 boundary condition was applied at this surface. Values $\rho = 1.1614kg/m^3$ for
 235 the density of air and $\mu = 1.846 \times 10^{-5}kg/ms$ for the dynamic viscosity were
 236 used. The convergence criterion was chosen as 10^{-10} for all flow simulations
 237 involving both the Spalart-Allmaras and the SST $k - \omega$ turbulence model.

238 Despite the fact that the Spalart-Allmaras turbulence model was also used
 239 for comparison, the main outcome of this research was obtained by means of
 240 the SST $k - \omega$ turbulence model since it is proven to be the best option for the
 241 predictions of rotor aerodynamics [23, 32, 33, 45, 46, 47]. SIMPLE algorithm
 242 for pressure-velocity coupling was employed to solve the RANS equations

243 and the convection terms were discretized with second-order upwind scheme.
244 Following Ge et al. [24], the transition from laminar to turbulent flow was
245 simulated by means of the $\gamma - Re_\theta$ transition model.

246 **3. Results and discussion**

247 *3.1. Mesh independence test*

248 As indicated in Section 2.3 the importance of the mesh structure for this
249 particular problem results from the high possibility of the occurrence of the
250 boundary layer separation on the blade surface and the formation of eddies
251 downstream of the blade. These flow phenomena usually cause stability issues
252 and, thus, convergence problems. Therefore, a thorough mesh independence
253 test was conducted as a part of this study.

254 Simulations were initially conducted using coarse mesh structures with
255 16,950 mesh elements. The number of mesh elements was then increased
256 in successive steps to investigate the effects on the overall results of the
257 simulations. The lift coefficient C_L and the drag coefficient C_D of the blade
258 profile were used as control parameters for each mesh configuration and the
259 results are shown in Figure 4. The data displayed in the figure reveal that
260 the lift coefficient and the drag coefficient remain nearly constant, at $C_L \cong$
261 0.8 and $C_D \cong 0.012$, for the number of mesh elements 218,163 and above.
262 Therefore, the number of mesh elements used in this research was chosen as
263 322,806 to ensure stable solutions and convergence.

264 The mesh structure determined by the independence test provided a value
265 for the nondimensional wall distance in the range of $1 \leq y^+ \leq 5$ which is
266 appropriate for the investigations of boundary layer flows [48, 49].

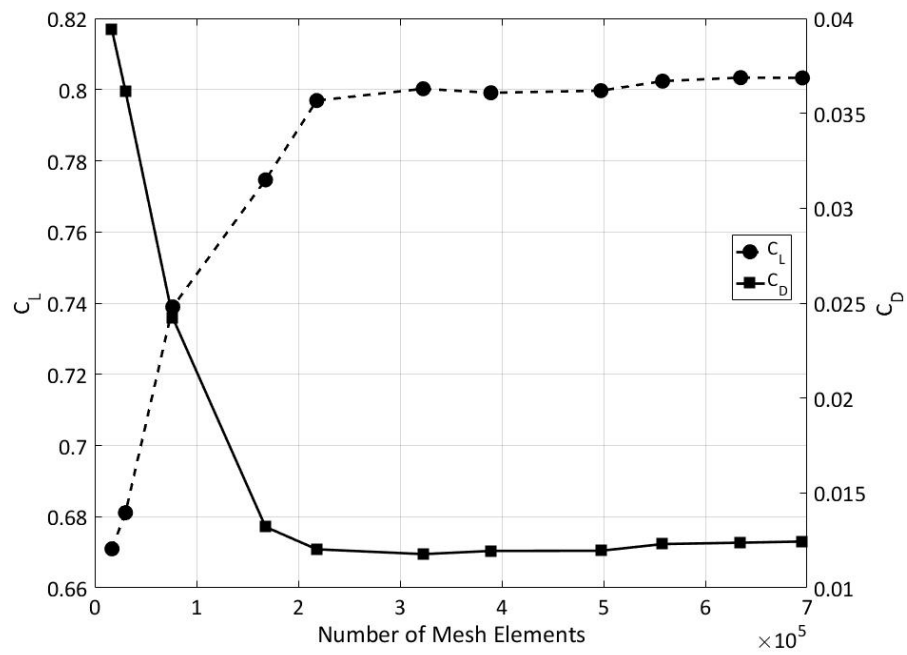


Figure 4: The results of the mesh independence test at $Re = 10^5$ and $\alpha = 5^\circ$.

267 The wall y^+ value is given by Equation 7 where τ_w is the wall-shear stress,
 268 ρ is the density of air, y is the distance of the centre of the first cell to the
 269 nearest wall and ν is the kinematic viscosity of air. In addition to the first
 270 mesh element near the wall that provides the range of $1 \leq y^+ \leq 5$, there are
 271 20 grid points in the viscous sub-layer to secure the solution of high velocity
 272 and pressure gradients in the vicinity of walls.

273

$$274 \quad y^+ = \frac{\sqrt{\tau_w/\rho} \times y}{\nu}. \quad (7)$$

275 3.2. Validation of the numerical model

276 The lift coefficient was acquired for twenty different angles of attack in
 277 the range of $0^\circ \leq \alpha \leq 20^\circ$ and by means of both turbulence models. These
 278 results were then compared with the available numerical and experimental
 279 data in literature.

280 Figure 5 displays experimental data obtained by Abbott and von Doenhoff
 281 [35] at $Re = 3 \times 10^6$ in comparison to associated computational results of
 282 the current study. The figure reveals an overall good agreement between the
 283 experimental data and the simulations based on the two different turbulence
 284 models used. In particular, Figure 5 shows that, for higher angles of attack
 285 ($\alpha \geq 13^\circ$), the SST $k - \omega$ turbulence model predicts the lift coefficient better
 286 than the Spalart-Allmaras turbulence model .

287 Figure 6 shows computational results of the current study in comparison
 288 to numerical data reported by Villalpando et al. [6] for $Re = 5 \times 10^5$. It
 289 is clear from the figure that, especially in the range of $0^\circ \leq \alpha \leq 7^\circ$, there
 290 is a very close agreement between the current numerical results and the

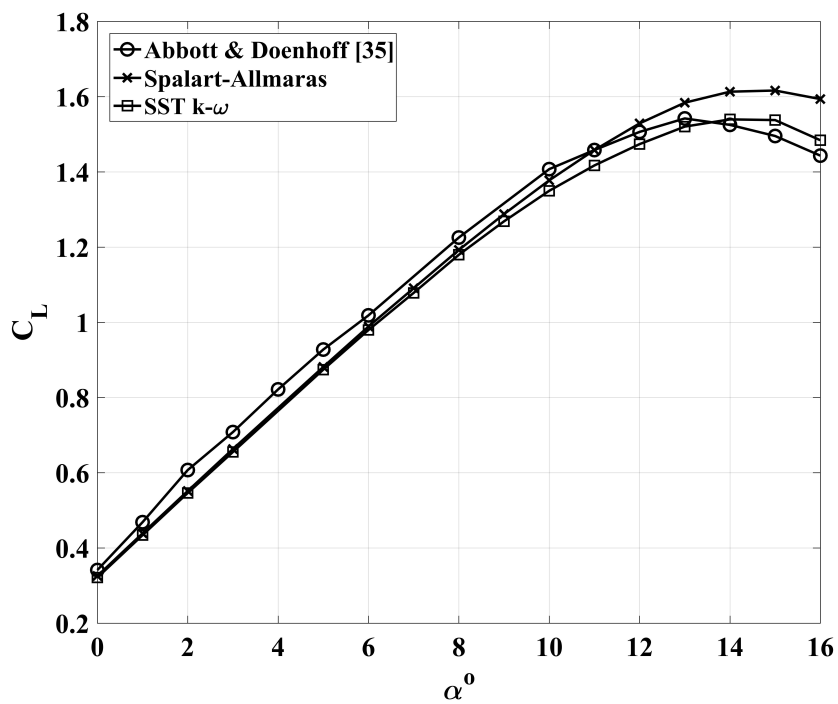


Figure 5: Comparison between computational C_L results of the current study and the experimental data of Abbott and von Doenhoff [35] for $Re = 3 \times 10^6$.

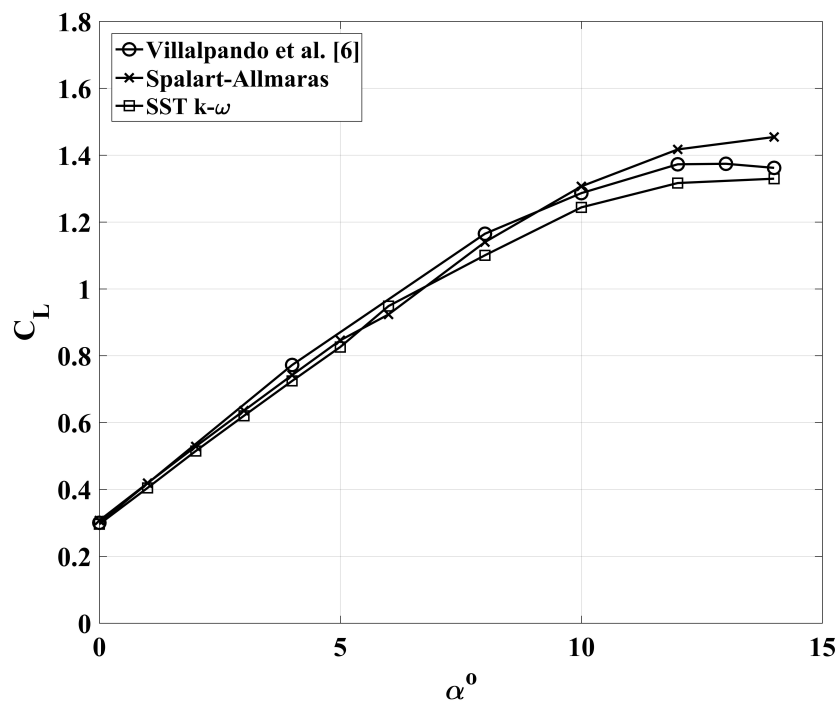


Figure 6: Comparison between the computational C_L data of the current study and the numerical data of Villalpando et al. [6] for $Re = 5 \times 10^5$.

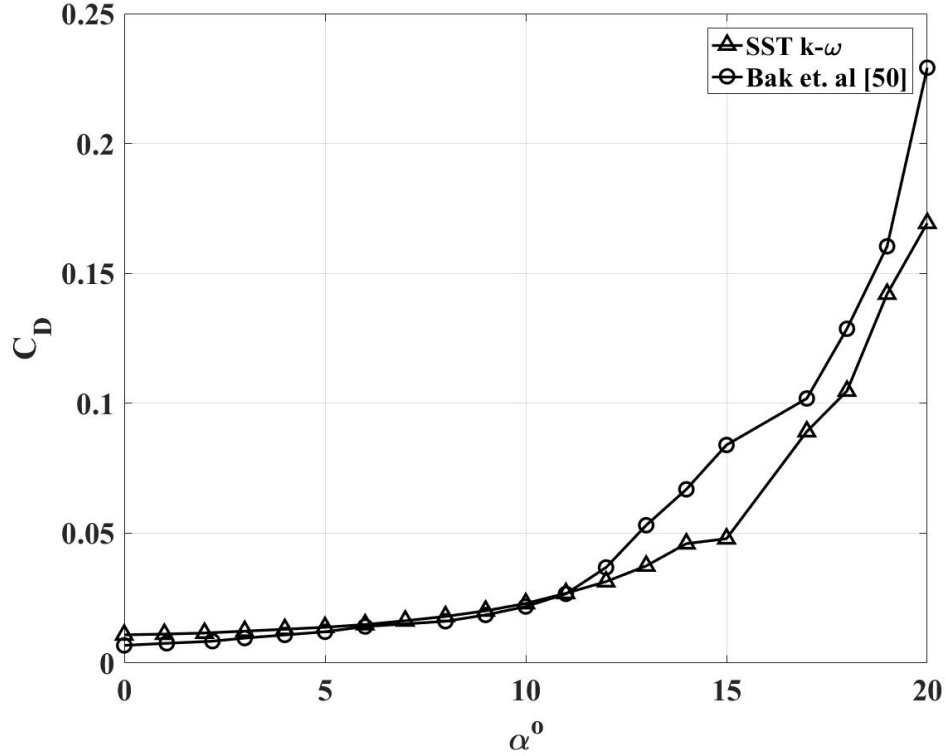


Figure 7: Comparison between the computational C_D data of the current study and the experimental data of Bak et al. [50] for $Re = 1.6 \times 10^6$.

291 computational data provided by Villalpando et al. [6]. For $\alpha \geq 7^\circ$, the
 292 agreement still continues with insignificant discrepancies.

293 The computational drag coefficient data of the current study produced
 294 by the SST k- ω turbulence model is also compared with the experimental
 295 data of Bak et al. [50] in Figure 7. Bak et al. [50] conducted their 2D wind
 296 tunnel experiments of a NACA 63-415 airfoil for $Re = 1.6 \times 10^6$ with
 297 minimizing the 3D effects by means of end plates. They reported that the
 298 stall characteristics of this commonly used airfoil as a wind turbine blade

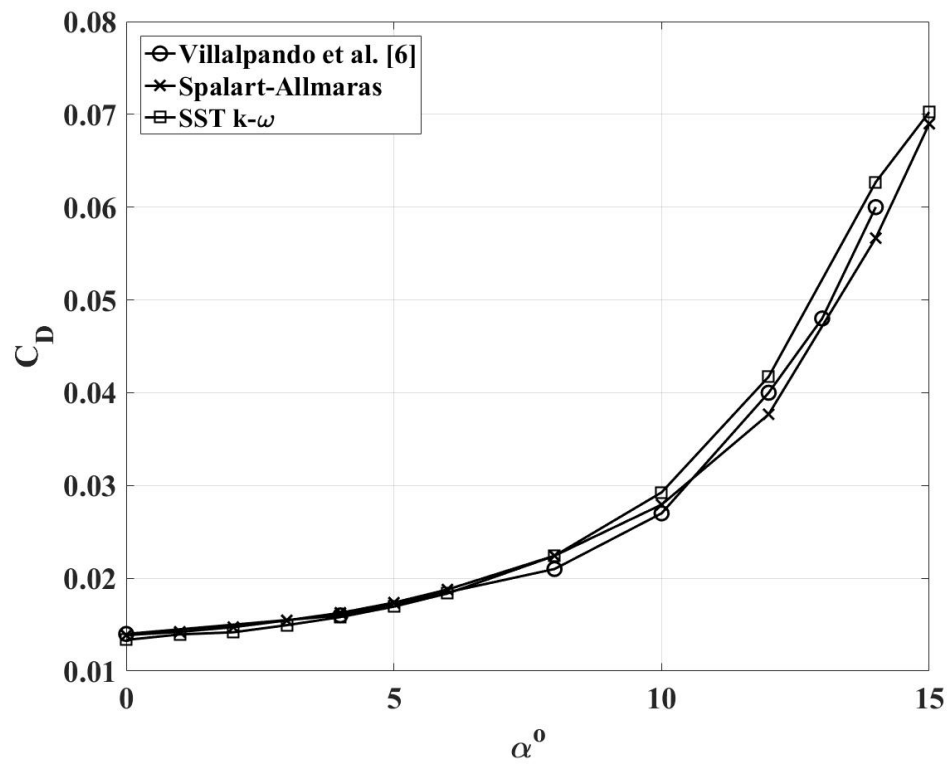


Figure 8: Comparison between the computational C_D data of the current study and those of Villalpando et al. [6] for $Re = 5 \times 10^5$.

299 profile can be improved by using a modified profile introduced by Fuglsang
300 and Bak [51]. This comparison shows a very good agreement between the
301 present numerical data and the experimental results for approximately
302 $\alpha \leq 12^\circ$. Above this angle of attack, there is a strong possibility of a flow
303 separation but the CFD model can still reasonably predict the experimental
304 data.

305 The capability of the current numerical models for predicting the drag
306 coefficient is also verified by means of the comparison with the computational
307 data of Villalpando et al. [6] which is displayed in Figure 8. As previously
308 stated for Figure 7, two numerical models of the current study completely
309 agree in Figure 8. The predictions of the current study also agree very well
310 with the results of Villalpando et al. [6] up to approximately $\alpha \leq 10^\circ$. Above
311 this angle of attack very minor discrepancies are observed. Additionally, the
312 SST $k - \omega$ model seems to better produce the data of Villalpando et al. [6]
313 in the range of $10^\circ \leq \alpha \leq 15^\circ$.

314 The data in figures 5, 6, 7 and 8 have shown that the computational results
315 of the current study employing the SST $k - \omega$ model agree more favourably
316 with both computational and experimental data from the literature than our
317 data obtained by means of the Spalart-Allmaras model. For the investigation
318 of the optimum angle of attack in the remainder we will, therefore, proceed
319 by employing the SST $k - \omega$ model only.

320 3.3. *Optimum angle of attack*

321 The optimum angle of attack for the NACA 63-415 airfoil, using the SST
322 $k - \omega$ turbulence model, was determined for twenty different angles of attack,
323 equally spaced between $0^\circ \leq \alpha \leq 20^\circ$, at each of the six Reynolds numbers

324 of $Re = 10^5$, $Re = 5 \times 10^5$, $Re = 7 \times 10^5$, $Re = 10^6$, $Re = 1.6 \times 10^6$ and
325 $Re = 3 \times 10^6$.

326 Figure 9 displays the variation of the lift coefficient C_L as a function of the
327 angle of attack, α , for the six different Reynolds numbers investigated. The
328 figure shows that the lift coefficient increases with the angle of attack up to
329 $\alpha \approx 12^\circ$. For larger angles of α , there are slight changes in the tendencies of
330 the plots for each of the six Reynolds numbers investigated. Subsequently, the
331 lift coefficient drops at $\alpha \gtrsim 15^\circ$. This is a well-known, general phenomenon
332 known as stall for such flows over blade profiles. The phenomenon occurs for
333 sufficiently large angles of α when the boundary layer is no longer able to stay
334 attached to the surface of the body and separates from it. This boundary-
335 layer separation is associated with a sudden decrease in the lift force. The
336 flow separation at $\alpha = 15^\circ$ and for $Re = 7 \times 10^5$ can be clearly seen in
337 Figure 10. Figure 9 reveals, moreover, that the lift coefficient, characterizing
338 to the lift force, is obviously larger for higher Reynolds numbers.

339 The values of the drag coefficient C_D for different angles of attack α
340 and for the six Reynolds numbers investigated are illustrated in Figure 11.
341 The range of the drag coefficient displayed by this figure is in the range
342 $0 \leq C_D \leq 0.3$, this agrees with data reported by several other studies for such
343 airfoils [12, 52]. Similar to the lift coefficient, the drag coefficient increases
344 with the angle of attack. However, unlike in the case of the lift coefficient,
345 there is no sudden decrease in the drag coefficient after a specific value of the
346 angle of attack.

347 Additionally, Figure 11 reveals that for smaller α , the drag coefficient
348 only increases weakly with the angle of attack. However, for $\alpha \gtrsim 12^\circ$, this

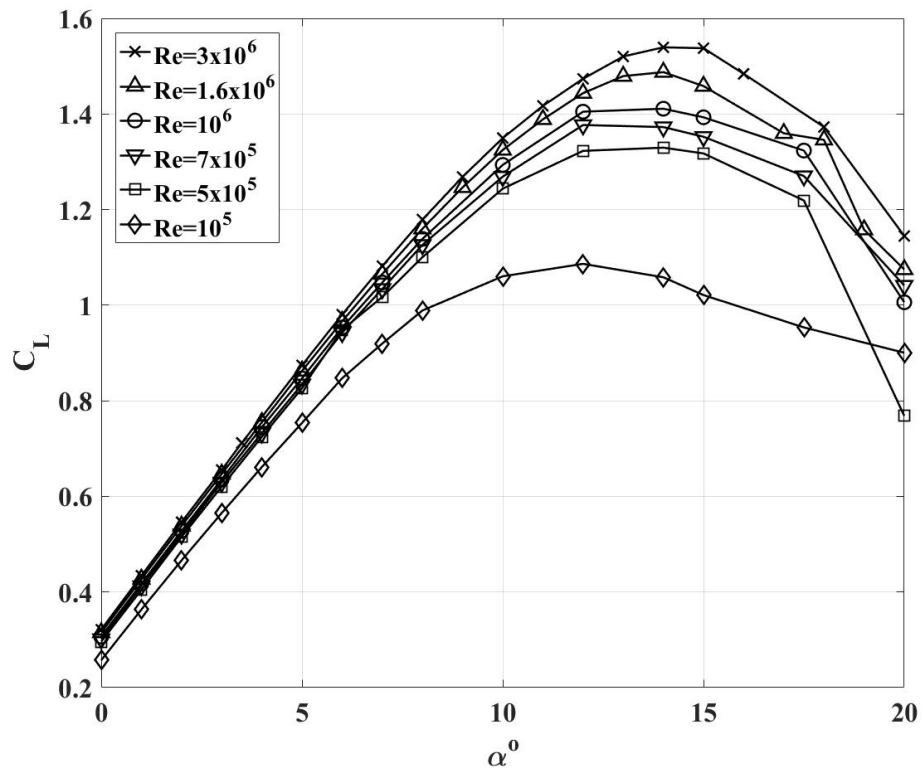


Figure 9: The change in the lift coefficient C_L as a function of the angle of attack α for the six different Reynolds numbers investigated.

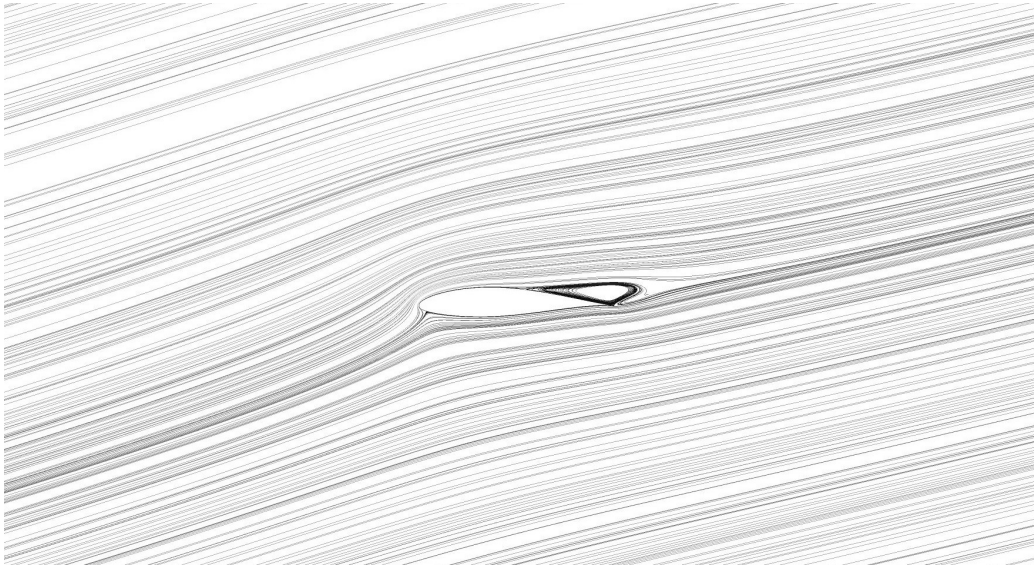


Figure 10: Flow separation over the blade profile for $\alpha = 15^\circ$ and $Re = 7 \times 10^5$.

349 increase is exponential. This is also expected since for low angles of attack
350 the drag force mainly arises from viscous effects (skin friction) but at higher
351 angles of attack, boundary layer separation occurs and form drag effects are
352 included which then constitute the dominant factor.

353 Furthermore, the drag coefficient decreases with increasing Reynolds
354 number. This is due to the fact that a turbulent boundary layer occurs
355 with an increase in Reynolds number. By this means the flow remains
356 attached to the surface and the boundary layer separation does not occur.
357 Therefore, the drag force is reduced with an increase in Reynolds number.

358 It is difficult to determine the optimum angle of attack by considering the
359 lift and drag coefficients separately because as the lift coefficient is raised,
360 the lift force acting on the blade profile that powers the turbine is increased.
361 However, an increase in the drag force is also observed which is not desired

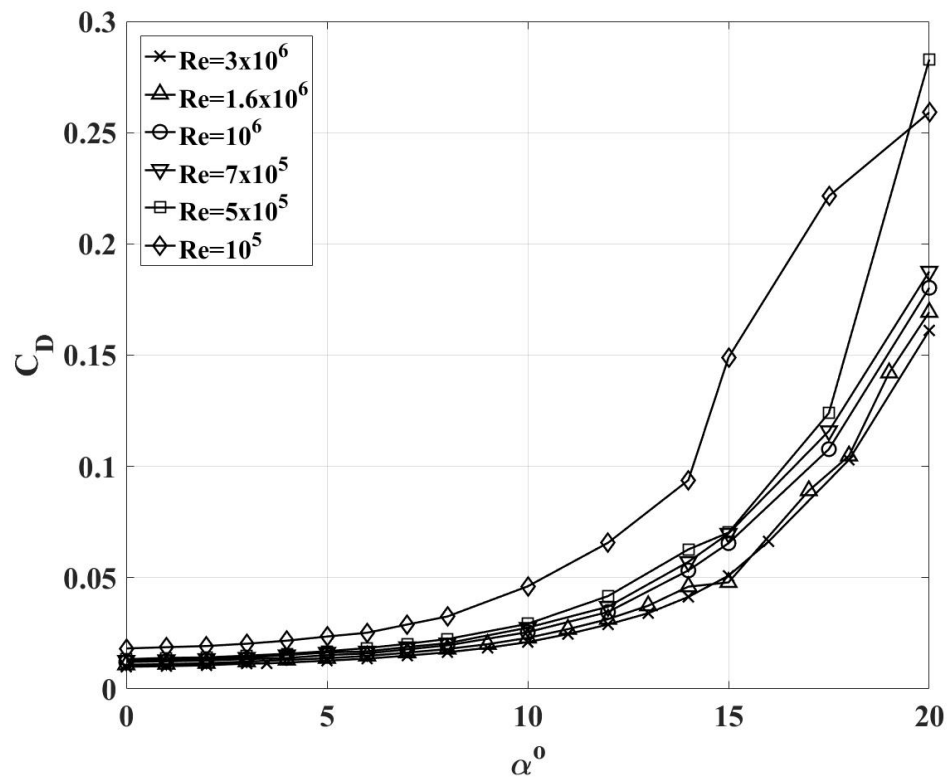


Figure 11: The change in the drag coefficient C_D as a function of the angle of attack α for the six different Reynolds number values investigated.

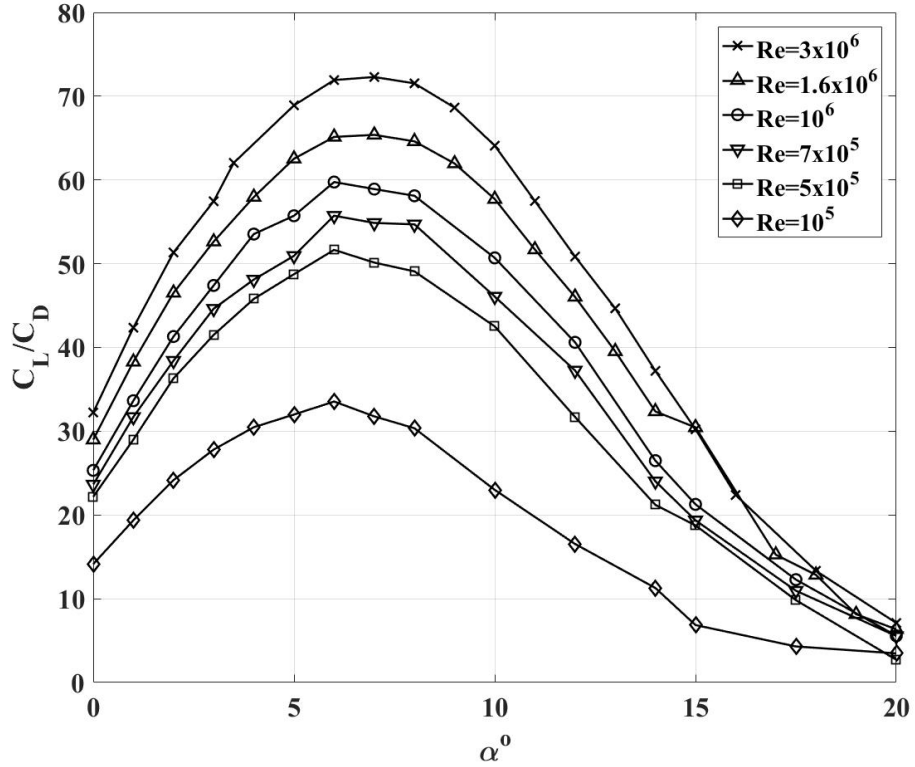


Figure 12: The lift to drag ratio C_L/C_D as a function of the angle of attack α for simulations employing the SST $k-\omega$ turbulence model.

362 as it reduces the output power produced by the wind turbine. Therefore, the
 363 lift to drag ratio C_L/C_D is considered as an indicator of efficiency.

364 The change of the lift to drag ratio is shown in Figure 12. The maximum
 365 value of this ratio should indicate the optimum angle of attack for the blade
 366 profile investigated. Thus, it can be seen from the figure that for every
 367 Reynolds number, the maximum of C_L/C_D occurs somewhere between 5° and
 368 8° . For determining a specific value for the optimum angle of attack, maxima
 369 of C_L/C_D ratio at each value of Reynolds number investigated are plotted

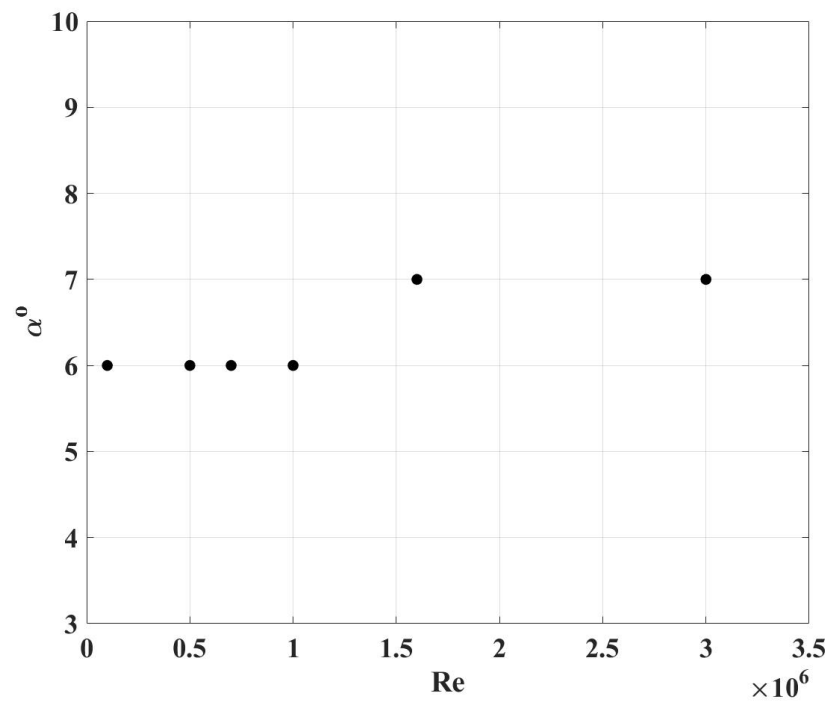


Figure 13: The optimum angle of attack α at each value of Reynolds number investigated.

370 in Figure 13. From this figure it can be concluded that the optimum angle
371 of attack is $\alpha = 6^\circ$ for the Reynolds number of $Re \leq 10^6$ and $\alpha = 7^\circ$ for
372 $Re \geq 1.6 \times 10^6$.

373 Previously, optimum angles of attack of $\alpha = 2^\circ$ [12] and $\alpha = 5.25^\circ$ [16]
374 were found. Moreover, Yilmaz et al. [52] reported values of the optimum
375 angle of attack in the very broad range of 4° to 12° . The current study,
376 nevertheless, precisely provides the optimum angle of attack as $\alpha = 6^\circ$ or 7°
377 depending on the Reynolds number for the NACA 63-415 type blade profile
378 by means of a turbulence model whose reliability is proven in literature by
379 many different studies.

380 To further examine the effects of the acquired optimum angle of attack
381 on rotor aerodynamics, the distribution of the surface pressure coefficient
382 C_p is shown in Figure 14 for $\alpha = 0^\circ$ and in Figure 15 for $\alpha = 8^\circ$. The
383 distribution of C_p for $\alpha = 8^\circ$ instead of the optimum angle of attack is
384 provided since Bak et al. [50] only reported values for $\alpha = 8^\circ$ which is very
385 close to the optimum value nevertheless. It can be seen from these figures that
386 the current numerical results are entirely consistent with the experimental
387 data. Moreover, the differential pressure between the pressure side and the
388 suction side is not dissimilar at the trailing edge of the airfoil for both angles
389 of attack. However, the difference in pressure between the pressure and the
390 suction side at the leading edge is increased with the application of the angle
391 of attack $\alpha = 8^\circ$. Consequently, transforming wind energy into mechanical
392 energy is more effective with the attack angle of $\alpha = 8^\circ$ that is close to the
393 optimum values found as $\alpha = 6^\circ$ and 7° .

394 Moreover, Figures 16 and 17 show the pressure contours for the NACA

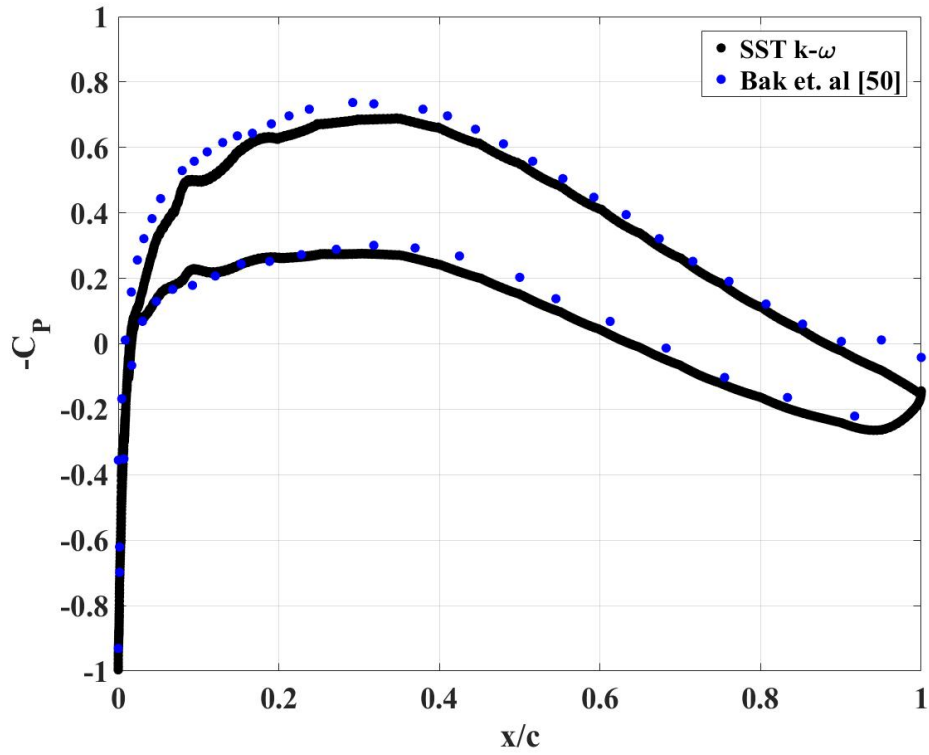


Figure 14: Distribution of the surface pressure coefficient C_p for the NACA 63-415 airfoil at $Re = 1.6 \times 10^6$ and $\alpha = 0^\circ$. Black dots indicate current computational data and blue dots indicate the experimental data of Bak et al. [50].

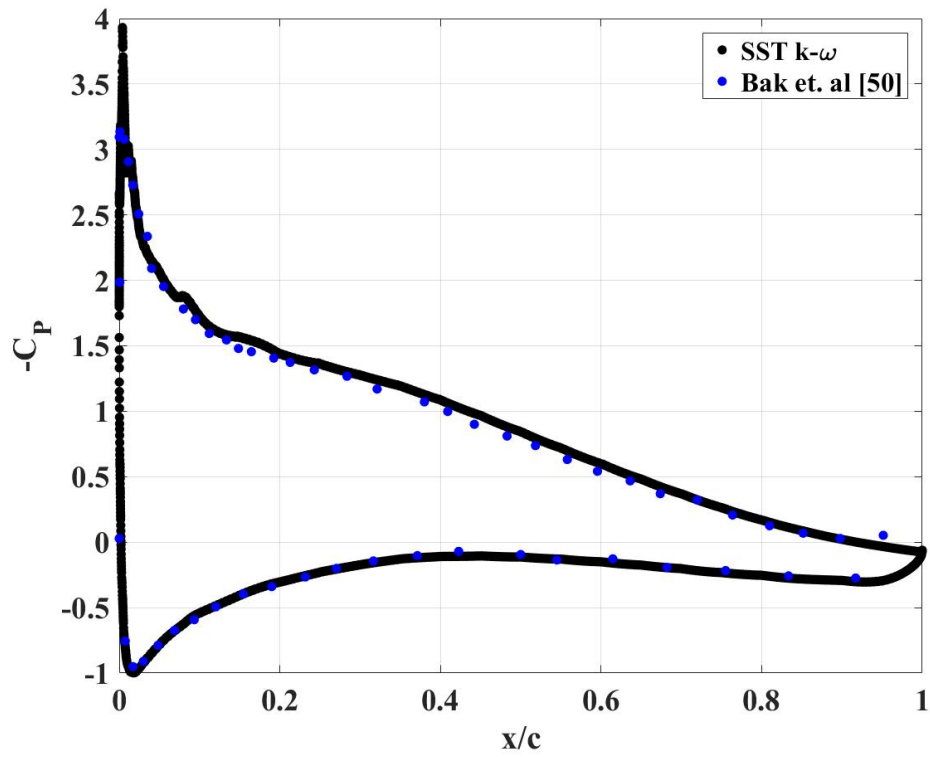


Figure 15: Distribution of the surface pressure coefficient C_p for the NACA 63-415 airfoil at $Re = 1.6 \times 10^6$ and $\alpha = 8^\circ$. Black dots indicate current computational data and blue dots indicate the experimental data of Bak et al. [50].

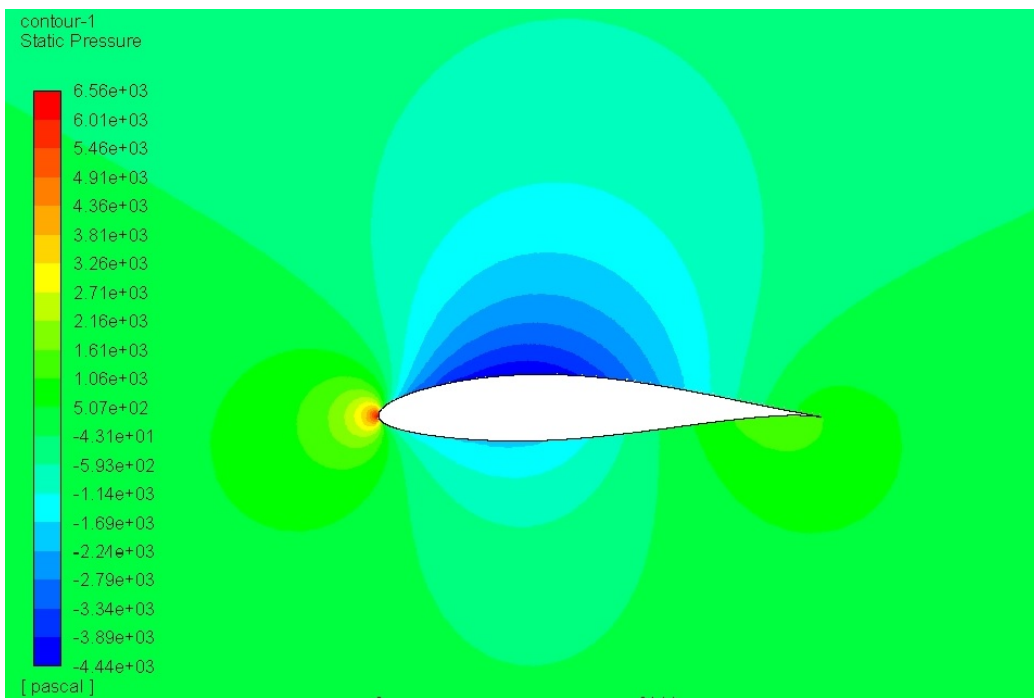


Figure 16: Pressure contours for the NACA 63-415 profile at $\alpha = 0^\circ$ and $Re = 7 \times 10^5$.

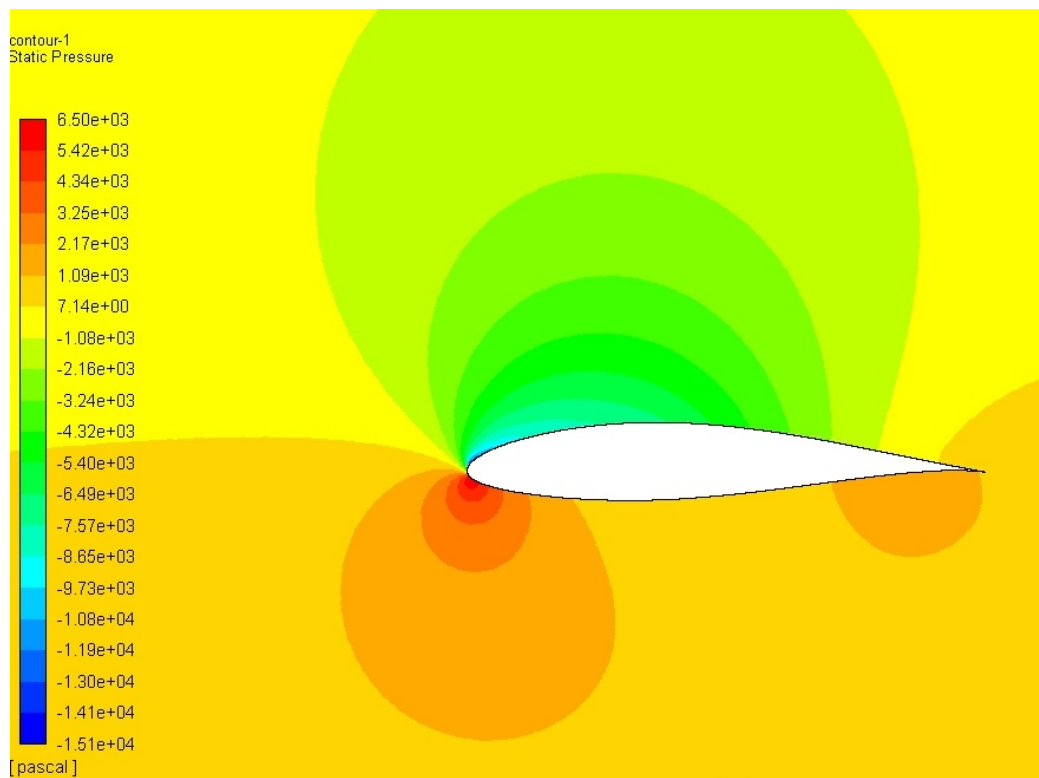


Figure 17: Pressure contours for the NACA 63-415 profile at $\alpha = 6^\circ$ and $Re = 7 \times 10^5$.

395 63-415 blade profile at $\alpha = 0^\circ$ and $\alpha = 6^\circ$, respectively. The pressure
396 distributions are obtained for the wind speed that is corresponding to
397 $Re = 7 \times 10^5$. In both figures, the pressure is lower at suction side than the
398 pressure side as a result of the increase in the velocity above the airfoil.
399 This pressure difference, as stated in Figure 14 and Figure 15, causes the
400 lift force that rotates the wind turbine. Furthermore, the pressure above
401 the blade profile raises from the leading edge to the trailing edge. Due to
402 the fact that the pressure is higher at the trailing edge than the leading
403 edge, the adverse pressure gradient is encountered which is related to the
404 boundary-layer transition and perhaps the separation, if this gradient is
405 excessively strong. The comparison between pressure contours, which is
406 another example of insights into flow mechanisms, displays that with the
407 use of the optimum angle of attack, the blade profile becomes
408 aerodynamically more effective.

409 **4. Conclusion**

410 The efficiency of a wind turbine depends on many aspects such as the
411 characteristics of the wind, which cannot be controlled, and the surface
412 roughness of the blades resulting from contamination, erosion, icing and
413 etc. Obviously, the design parameters of the blades also have crucial effects
414 on the effectiveness. The angle of attack is the most critical design
415 parameter for turbine blades and therefore its influence on the efficiency
416 needs to be studied by means of investigating the flow over these airfoils.

417 Hence, in this study, a two-dimensional, steady-state, incompressible flow
418 over a NACA 63-415 airfoil, which is widely used as blades of commercial

419 wind turbines, was examined numerically by means of CFD model introduced
420 in preceding sections.

421 Simulations were carried out in the range of Reynolds number between
422 $Re = 10^5 \leq Re \leq 3 \times 10^6$ and for the angles of attack $0^\circ \leq \alpha \leq 20^\circ$.
423 These two parameter ranges cover the most commonly encountered operating
424 conditions for commercial-scale wind turbines.

425 The Spalart-Allmaras and the SST $k-\omega$ turbulence models were used to
426 simulate turbulent flow. This enabled a direct comparison between results
427 obtained by two different turbulence models and also provided data for
428 comparison with literature data. An in-depth mesh independence test was
429 performed followed by the validation of the CFD model.

430 The data obtained revealed that the SST $k-\omega$ turbulence model produces
431 results which compare more favourably to computational and experimental
432 literature data than the Spalart-Allmaras turbulence model. The SST $k-\omega$
433 model was employed to determine the range for the optimum angle of attack.

434 The lift coefficient and the drag coefficient, which characterize the lift
435 force and the drag force acting on the airfoil, were examined for various
436 angles of attack at different Reynolds numbers. Both coefficients increase
437 with an increase in the angle of attack. However, there is a critical range of
438 the angle of attack, $12^\circ - 15^\circ$, after which a decrease in the lift coefficient
439 observed.

440 Separate investigations of these two coefficients revealed no clear
441 information regarding the performance of the blade and thus the wind
442 turbine. Therefore, the lift to drag ratio is considered as an indicator of the
443 effectiveness of the blade. The observation of the maxima of this ratio for

444 various angles of attack shows that the optimum angle of attack is $\alpha = 6^\circ$
445 for the Reynolds number of $Re \leq 10^6$ and $\alpha = 7^\circ$ for $Re \geq 1.6 \times 10^6$. The
446 turbine blade is considered to have the highest aerodynamic performance at
447 these values.

448 In addition to the angle of attack as a design parameter, the surface
449 roughness of the blade can be implemented in the subsequent studies to
450 investigate the flow and to see whether that parameter influence the optimum
451 angle of attack for the NACA 63-415 airfoil since the surface roughness is
452 mostly an unavoidable aspect for wind turbine blades.

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