G. KHAYATI and M. SHAHRIARI, Measurement and Correlation of Phase Diagram..., Chem. Biochem. Eng. Q., 30 (1) 73-80 (2016)

Measurement and Correlation of Phase Diagram Data of Hydrophilic Alcohols (1-Propanol/2-Propanol) + + Salts $(Na_2SO_4/(NH_4)_2SO_4/NH_4NO_3)$ + Water Systems

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Binodal data and the ternary liquid–liquid equilibria (LLE) was experimentally determined at 298.15 K for hydrophilic alcohols (1-propanol or 2-propanol) + salts (Na₂SO₄, (NH₄)₂SO₄ or NH₄NO₃) + water systems. The salting-out and the phase-forming abilities of the salts and alcohols for the investigated ATPSs were discussed. The salting-out abilities of the investigated salts follow the order Na₂SO₄ > (NH₄)₂SO₄ > NH₄NO₃, which can be indicated by the location of the binodal curves plotted in mass fraction, the effective excluded volume (EEV), the salting-out coefficient (K_s), the size of the ions, and the Gibbs free energy of hydration of the ions. The phase-separation ability of the studied hydrophilic alcohols. The results show that the phase-separation capability of the system consists of different hydrophilic alcohols in the order: 1-propanol>2-propanol. Furthermore, the binodal curves of the studied systems were satisfactorily correlated by a nonlinear equation with four parameters. The reliability of the calculation method and the corresponding LLE data was successfully proved by the Othmer-Tobias equation and the Bancroft equation.

Key words:

liquid-liquid equilibrium, aqueous two-phase system, hydrophilic alcohols, salting-out effect, phase-forming ability

Introduction

Aqueous two-phase systems (ATPSs) are composed of two immiscible aqueous phases that are in equilibrium. As one of the separation methods, aqueous two-phase extraction (ATPE) has advantages of biocompatibility, process integration capability, and large-scale feasibility¹. As far as we know, ATPE has been used for the separation of proteins², enzymes³⁻⁴, organic acids⁵⁻⁶, and so on. Based on the composition of ATPS, they can be classified into the following categories: polymer-based ATPS, ionic liquid (IL)-based ATPS, surfactant-based ATPS, and hydrophilic alcohols-based ATPS. Among the ATPS mentioned above, the weaknesses of the polymer-based ATPS are high price and high viscosity. The ionic liquid (IL)-based ATPS also shares the disadvantage of high cost. In comparison with other ATPSs, the hydrophilic alcohol-based have advantages of low viscosity and low cost simultaneously⁷. And they have the potential to achieve the desired purification and concentration

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of the product in a single step⁸. In addition, the hydrophilic alcohol can be recycled and reused in some way⁷, which will further cut the process costs.

Based on our knowledge, there are only two works in the literature describing phase diagrams of ternary systems composed by 2-propanol+(NH₄)₂SO₄+ +H₂O⁹ and 2-propanol+Na₂SO₄/(NH₄)₂SO₄+H₂O¹⁰. None of these reports have conducted a systematic study on the phase-formation ability of the sulfate salts in hydrophilic alcohol + salt + water systems. Also, no LLE data have been previously reported in the literature for the 1-propanol + $Na_2SO_4/(NH_4)_2SO_4$ + water systems, and aliphatic alcohols + NH₄NO₃ + water systems. Therefore, the aim of this work is to systematically investigate the liquid-liquid equilibria for ternary systems of [hydrophilic alcohols (1-propanol/2-propanol)+salts (Na₂SO₄/(NH₄)₂SO₄/ NH₄NO₃)+water]. The salting-out ability of the salts and the phase-forming ability of the hydrophilic alcohols were discussed by the effective excluded volume (EEV) and salting-out coefficient (K_{i}) of the mentioned salts. Furthermore, the dependability of the calculation method was tested by the Othmer-Tobias and Bancroft equations.

73

Materials and methods

Materials

The chemicals 1-propanol, 2-propanol, Na₂SO₄, $(NH_4)_2SO_4$ and NH_4NO_3 were supplied from Merck with a minimum purity of 99.5 %, 99.8 %, 98.5 %, 99.5 %, and 95.0 %, respectively. The salts were dried in an oven at about 393.15 K for 24 h before use. All chemicals were used without further purification. Double distilled deionized water was used in all experiments.

Apparatus and procedure

The experimental apparatus employed is similar to the one used previously¹¹. A glass vessel with 50 cm³ volume was used to carry out the experiments. It was provided with an external jacket in which water was circulated from a controlled thermostat at constant temperature (with a precision of \pm 0.1 K), and a magnetic stirrer was used to agitate the liquid mixture in the cell. The cloud point titration method was performed to collect the binodal curve data. In this method, the salt solution of known concentration was titrated with 1-propanol/2-propanol or vice versa, until the clear solution turned turbid. Water was then added to the mixture to make it clear again. The procedure was repeated to obtein more cloud points, and compositions for each point were determined by using an analytical balance with an uncertainty of ± 0.0001 g.

The phase equilibrium experiments were carried out to determine the tie-lines. The feed samples were prepared by mixing an appropriate mass of alcohols (2-propanol/1-propanol), salts (Na₂SO₄/ $(NH_{4})_{2}SO_{4}/NH_{4}NO_{3}$) and water in a vessel, and the mass of each composition was determined by the same analytical balance mentioned above. After two hours of mixing, equilibrium was achieved by letting the mixture rest for more than 10 h at the desired temperature (298.15 K) until it was separated into two clear phases. After phase separation, the top phase was carefully withdrawn and the mass measured by the analytical balance, while the mass of the bottom phase was determined by mass balance equation. Also, the densities of both phases were determined using measurements of weight and volume.

The salt concentration in each phase was determined gravimetrically by transferring a liquid sample to a watch glass, and evaporating the solution at 403.15 K until a constant mass was achieved. The mass fractions of alcohols were analyzed using a Konik gas chromatography (GC) system equipped with a thermal conductivity detector (TCD) and Shimadzu C-R2AX integrator. The GC oven temperature was held at 40 °C for 5 minutes and then programmed to attain a temperature of 270 °C at 10 °C min⁻¹. The injector temperature was 280 °C with a split ratio 20:1. Helium was used as a carrier gas with a constant flow rate of 1.3 mL min⁻¹. The measurements were repeated at least three times.

The tie-line length (TLL) and the slope (S) of the tie-line at different compositions were also calculated by using the following two equations respectively:

$$TLL = \sqrt{(w_1^t - w_1^b)^2 + (w_2^t - w_2^b)^2}$$
(1)

$$S = \frac{w_1^t - w_1^b}{w_2^t - w_2^b}$$
(2)

where w_1^{t} and w_2^{t} represent the equilibrium compositions (in mass fraction) of hydrophilic alcohol (1) and salt (2) in the top phase, respectively, w_1^{b} and w_2^{b} represent the equilibrium compositions (in mass fraction) of hydrophilic alcohol (1) and salt (2) in bottom phase, respectively.

Results and discussion

Liquid-liquid equilibria (LLE) are the key in improving the performance of an extraction process and understanding the phase behavior of systems exhibiting two liquid phases¹². Only a few reports found in the literature focus on the study of ternary systems composed by 2-propanol $+Na_2SO_4/(NH_4)_2SO_4+H_2O$ systems⁹⁻¹⁰. Fig. 1B compares the binodal curves obtained in this work for 2-propanol $+Na_2SO_4/(NH_4)_2SO_4 + H_2O$ systems with those obtained from literature data. According to this figure, our measurements agree with literature values. Also, scattering of the new experimental data was less than 5 %, which can be related to experimental uncertainties. Therefore, we systematically studied the liquid-liquid phase equilibrium and binodal data for the ternary hydrophilic alcohols (2-propanol/1-propanol) +salts $(Na_2SO_4/(NH_4)_2SO_4/NH_4NO_3)$ +water systems. The results are shown in Table 1. Also, the tie-line lengths (TLL) and slopes (S) for ternary systems are shown in Table 2 as mass fractions at 298.15 K, and the tie-lines at 298.15 K are drawn in Fig. 2. It can be observed that, when the salts concentration are constant (in 1-propanol + NH_4NO_3 + H_2O and 2-propanol + $(NH_4)_2SO_4$ + H_2O systems), the increase in the amount of hydrophilic alcohols leads to the increase in the tie-line length. Also, increasing both the amounts of hydrophilic alcohols and the salts (in 1-propanol + $(NH_4)_2SO_4 + H_2O$) can result in the increase in the tie-line length (Table 2 and Fig. 2). The results show that increasing the tie-line can promote phase-separation. Therefore, in studying the phase-separation of hydrophilic alcohol-salt ATPS, we should increase the

G. KHAYATI and M. SHAHRIARI, Measurement and Correlation of Phase Diagram..., Chem. Biochem. Eng. Q., 30 (1) 73-80 (2016)

panol/2-propanol) (1) + salts (Na_2SO_4 , (NH_4) $_2SO_4$ / NH $_4NO_3$) (2) + H $_2O$ (3) systems at T = 298.15 K										
100w ₁	100w ₂	100w ₁	100w ₂	100w ₁	100w ₂	100w ₁	100w ₂			
1-propanol + Na ₂ SO ₄										
3.77	19.24	6.00	14.56	9.69	10.51	14.38	7.70			
3.96	18.72	6.71	13.99	9.73	10.20	15.40	7.20			
4.84	17.39	7.10	13.46	10.66	9.83	16.28	6.65			
5.56	16.53	7.72	12.92	11.54	9.28	21.96	5.24			
5.44	16.07	7.81	12.44	12.79	8.72					
5.35	15.61	8.77	11.86	12.99	8.26					
1-propanol + NH ₄ NO ₃										
5.10	56.94	6.55	49.52	9.18	43.59	12.91	37.45			
5.48	53.87	7.20	48.25	9.89	42.35	14.03	36.10			
5.82	52.73	7.37	47.24	9.80	41.49	16.76	33.80			
6.34	51.51	8.24	45.88	11.05	40.00	20.69	29.40			
6.13	50.69	8.85	44.66	12.08	38.68					
		1-pr	opanol -	+ (NH ₄)	$_{2}SO_{4}$					
5.96	18.53	7.69	15.69	11.94	11.00	18.73	7.31			
5.53	19.22	8.21	15.14	12.83	10.46	20.88	6.72			
5.79	18.84	8.43	14.65	12.72	10.03	22.43	6.20			
6.27	18.27	9.90	13.51	14.17	9.44	27.45	5.36			
6.78	17.24	10.10	13.03	14.22	9.00	32.45	4.22			
7.24	16.69	10.24	12.57	15.55	8.44					
7.30	16.22	11.10	11.55	16.88	7.89					
		2-j	propanol	$1 + Na_2S$	SO_4					
29.77	6.10	18.80	9.50	10.90	15.30	7.98	19.80			
27.21	6.50	17.30	9.90	10.40	16.30	6.61	22.00			
25.70	6.80	14.87	11.40	9.97	16.90	6.18	22.70			
23.80	7.20	13.10	13.20	9.40	17.90	5.66	24.50			
21.10	8.10	12.03	13.45	8.98	18.39	5.02	28.20			
19.60	8.80	11.58	14.21	8.50	19.05					
		2-р	ropanol	$+ NH_4$	NO_3					
50.31	21.37	19.85	40.08	10.42	50.15	7.00	58.60			
43.47	24.88	18.12	41.78	10.10	51.24	5.56	60.45			
40.18	27.09	16.38	43.49	8.84	52.86	5.88	61.18			
36.10	29.63	14.92	45.08	7.37	55.58					
29.29	33.94	13.10	46.93	7.74	56.29					
25.86	36.34	11.19	48.84	6.82	57.77					
		2-pr	opanol -	$+ (NH_4)$	$_{2}SO_{4}$					
9.62	19.78	14.92	15.67	22.46	10.47	36.84	5.68			
10.54	19.23	15.11	15.28	23.89	9.89	41.21	5.12			
10.84	18.72	15.67	14.76	26.10	8.50	45.60	4.48			
10.44	18.36	16.67	14.17	30.68	7.59	50.67	3.89			
13.06	17.28	19.81	12.03	33.08	7.03					
13.01	16.88	21.14	11.43	34.13	6.59					
13.95	16.35	22.28	10.88	37.45	5.94					

Table 1 – Binodal data for the hydrophilic alcohols (1-pro-

 w_1 , mass fractions of hydrophilic alcohol

 w_2 , mass fractions of salt

Table 2 – Tie-line data for the hydrophilic alcohol (1) + salt (2) + H_2O (3) systems at T = 298.15 K

ATPS									
Total compositions		Organi	c phase	Aqueous phase		TLL	S		
$100w_{1}$	$100w_{2}$	$100w_{1}$	$100w_{2}$	$100w_{1}$	$100w_{2}$				
	•	SO ₄							
11.92	12.44	55.42	2.20	6.45	13.79	0.49	-4.18		
14.00	10.50	49.81	2.31	8.31	11.99	0.42	-4.30		
17.97	12.44	63.55	1.81	4.92	15.45	0.60	-4.29		
24.00	12.46	68.09	1.77	4.62	17.35	0.65	-4.06		
		1-p	ropanol	$+ NH_4N$	NO ₃				
13.96	44.84	57.05	13.72	7.14	49.49	0.61	-1.40		
18.16	44.77	73.86	8.31	6.65	52.58	0.80	-1.51		
22.04	44.96	80.25	7.53	4.86	56.31	0.89	-1.54		
26.01	44.84	83.75	7.02	4.35	59.07	0.94	-1.52		
1-propanol + $(NH_{A})_{2}SO_{A}$									
16.15	10.98	50.63	2.95	10.99	12.23	0.40	-4.27		
23.97	10.97	67.22	1.58	9.13	14.49	0.59	-4.49		
32.06	10.98	73.61	1.17	6.51	17.10	0.68	-4.23		
40.00	11.00	81.96	1.07	6.06	18.99	0.78	-4.21		
		2-1	oropano	$1 + Na_2S$	SO ₄				
17.07	12.15	37.05	5.31	12.49	13.55	0.25	-2.97		
20.04	12.02	40.89	5.10	11.78	15.24	0.30	-2.87		
24.00	12.02	44.02	4.99	9.11	17.33	0.37	-2.82		
28.01	11.88	49.59	4.69	8.01	19.09	0.44	-2.88		
		2-р	ropanol	$+ NH_4N$	NO ₃				
13.85	49.88	53.04	20.54	7.13	55.07	0.57	-1.33		
15.97	49.96	56.51	19.08	7.15	57.06	0.62	-1.30		
18.00	50.00	59.09	18.03	6.64	59.10	0.66	-1.27		
19.81	49.93	61.50	17.04	5.21	61.50	0.71	-1.26		
		2-рі	opanol	+(NH ₄) ₂	SO_4				
23.00	12.00	41.75	5.03	15.89	14.64	0.27	-2.69		
26.04	12.00	46.44	4.37	13.06	16.83	0.35	2.67		
30.00	12.00	52.01	3.75	10.15	19.44	0.44	-2.66		
34.00	12.00	58.22	3.22	8.34	21.31	0.53	-2.75		

 w_1 , mass fractions of hydrophilic alcohol

 w_2 , mass fractions of salt

amount of alcohol and salt. Such results were reported by Han *et al.*⁷ for hydrophilic alcohol + sodium hydroxide + water systems.

Effect of different salts on the phase formation

The salting-out effect in ATPS is noteworthy for industrial applications relevant to separation technologies. In aqueous two-phase systems, the salt type is an important factor, while the salting-out effect is the driving force for the formation of ATPS. The conditions of LLE and the distribution of com-

ponents in the ATPS are usually under the influence of the electrolytes present¹³. In order to better study the phase-separation abilities of salts, the binodal curves of alcohols-salts ATPSs at 298.15 K are shown in Fig. 1. It can be seen from Fig. 1 that the two-phase area of alcohols + Na₂SO₄ systems is larger than that of alcohols + $(NH_{4})_{2}SO_{4}$ systems. Also, the two-phase area of alcohols + (NH₄)₂SO₄ systems is larger than that of alcohols $+ NH_4NO_2$ systems. In other words, the phase-forming ability of the investigated salts follows the order: $Na_2SO_4 >$ $(NH_4)_2SO_4 > NH_4NO_3$. This is mainly due to the higher salting-out effect of the Na₂SO₄ salt. The Na₂SO₄ salt has higher salting-out effect than the $(NH_4)_2SO_4$, and the $(NH_4)_2SO_4$ has higher salting-out effect than the NH₄NO₃ salt. The salting-out ability of a cation or anion is related to its ionic charge and hydration radius⁶. The strength of ion solvation mainly depends on electrostatic attraction. Since two the salts, Na_2SO_4 and $(NH_4)_2SO_4$, have the same anion, the different cations have an im-



Fig. 1 – Effect of salt type on the binodal curves in mass fraction for hydrophilic alcohols(1)+salts(2)+water(3) systems at 298.15 K: (A) 1-propanol and (B) 2-propanol; (Bold symbols) this work [alcohols+ salts (\blacktriangle NH₄NO₃, \circ (NH₄)₂SO₄, \bullet Na₂SO₄)+ H₂O] and (open symbols) literature data [alcohols + salt (\diamond (NH₄)₂SO₄, \circ Na₂SO₄)+ H₂O]¹⁰.

portant influence on their electrostatic attractions. Sodium and ammonium ions have radii of 102 and 148 pm, respectively. It can be seen that the salting-out effect increases as the size of the cation decreases. It seems that in these systems, the size of the cation may be responsible for this trend. Similar results were observed by Chen et al.14 They showed that, in water + 1-propanol systems, the two-phase region with a certain composition of KCl is larger than the one with identical composition of NH₄Cl. The salting-out ability can also be related to the Gibbs free energy of hydration of ions (ΔG_{hvd}), as proposed by Marcus¹⁵. It was found that better salting-out is observed when the ions have a more negative Gibbs free energy. The Gibbs free energies of hydration for sodium and *ammonium* ions are -365 and -285 kJ mol⁻¹ respectively, which also certify the conclusion that the salting-out ability of Na₂SO₄ is stronger than that of $(NH_4)_2SO_4$. The more negative is the ΔG_{hvd} value of an ion, the greater is the salting out ability. This behavior can be explained by comparing the ΔG_{hyd} values for the anions sulfate and nitrate (-1080 and -300 kJ mol⁻¹ respectively), it can be concluded that the salting-out ability of $(NH_{4})_{2}SO_{4}$ is stronger than $NH_{4}NO_{3}$ (the two salts have the same cation). Furthermore, cations with a higher valence are better salting-out agents than cations with a lower-valence, because higher-valence cations are hydrated by more water than lower valence cations, thus decreasing the amount of water available to hydrate alcohols.

Furthermore, we calculated the effective excluded volume (EEV) and the salting-out coefficient (K_s) to evaluate the salting-out ability of Na₂SO₄, (NH₄)₂SO₄ and NH₄NO₃ in alcohol+water systems.

In this work, the EEV theory¹ proposed by Guan *et al.*¹⁶ was used to correlate binodal data and calculate the effective excluded volume of salts. The EEV of Na_2SO_4 , $(NH_4)_2SO_4$ and NH_4NO_3 in different hydrophilic alcohol–water component solvents was calculated by the following equation:

$$\ln\left(V_{213}^* \frac{w_2}{M_2} + f_{213}\right) + \left(V_{213}^* \frac{w_1}{M_1}\right) = 0 \tag{3}$$

where V_{213}^* and f_{213} state the scaled EEV of the salt and the effective volume fraction of the salt in the network structure of hydrophilic alcohol, respectively. *M* and *w* represent the molecular mass and the mass fraction, subscripts "1" and "2" show the hydrophilic alcohol and salt, respectively. Values of V_{213}^* and f_{213} obtained from the correlation of exper-

¹This theory is based on the statistical geometry methods developed, and states that any molecule species in a solution is distributed at random and every system composition on the solubility curve is a geometrically saturated solution of one solute in the presence of another.

G. KHAYATI and M. SHAHRIARI, Measurement and Correlation of Phase Diagram..., Chem. Biochem. Eng. Q., 30 (1) 73–80 (2016)

Table	3 - Values of parameter	s of	Eq.	(3)	for	the	studied
	ATPS at temperature	T =	<i>29</i> 8.	15 F	Ϋ́ Κ		

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ATPS	V [*] ₂₁₃ g mol ⁻¹	<i>f</i> ₂₁₃	R^2	100 sd ^a
1 -propanol + $Na_2SO_4 + H_2O$	632.8	-0.1281	0.9897	0.77
1 -propanol + $NH_4NO_3 + H_2O$	217.8	-0.4496	0.9779	4.86
$1\text{-propanol} + (\mathrm{NH}_4)_2 \mathrm{SO}_4 + \mathrm{H}_2 \mathrm{O}_4$	538.4	-0.1192	0.9873	1.27
2-propanol + Na ₂ SO ₄ + H ₂ O	460.9	-0.0833	0.9789	1.74
$2\text{-propanol} + \text{NH}_4\text{NO}_3 + \text{H}_2\text{O}$	115.1	0.0792	0.9840	2.80
$2\text{-propanol} + (\mathrm{NH}_4)_2 \mathrm{SO}_4 + \mathrm{H}_2 \mathrm{O}_4$	389.9	-0.7962	0.9965	1.15
	\0.5			

^a $sd = \left(\sum_{i=1}^{n} (\mathbf{w}_{1}^{cal} - w_{1}^{exp})^{2} / n\right)^{6.5}$, where *n* represents the number of binodal data. w_{1}^{exp} is the experimental mass fraction of hydrophilic alcohols listed in Table 1, and w_{1}^{cal} is the corresponding data calculated using Eq. (3).

imental binodal along with the corresponding correlation coefficients (R^2) and standard deviations (sd) are given in Table 3. The effective excluded volume represents the smallest spacing of an individual alcohol that will accept another individual salt molecule¹⁷. The larger the EEV value, the higher the salting-out ability of salts. As shown in Table 3, the EEV values of the systems containing the salt with divalent anions (sulfate) are significantly higher than of those with monovalent anions (nitrate). Therefore, at the same cation, the salts with higher-valence anion are more likely to form a twophase system because water molecules are hydrating them, thus the amount of water available for alcohol molecules is decreased. Therefore, the salting-out ability increases. From Table 3, the EEV value of alcohol+Na₂SO₄ system is larger than that of the alcohol+ $(NH_4)_2SO_4$ and the alcohol+ NH_4NO_3 system with the same alcohols, which indicates that the phase-forming strength and the salting-out ability of Na_2SO_4 is stronger than $(NH_4)_2SO_4$ and NH₄NO₃, which is certainly consistent with the observations in Fig. 1. It can be seen from Fig. 1 that the two-phase area of alcohols + Na_2SO_4 systems are larger than that of the alcohols + $(NH_4)_2SO_4$ and alcohols + NH_4NO_3 systems.

Also, a two-parameter equation (Eq. (4)) which is based on the binodal theory¹⁶ and has been successfully used for the LLE data of hydrophilic alcohol + salt and polymer + salt ATPSs, was used to predict the salting-out ability of the studied salts.

$$\ln \frac{w_1^t}{w_1^b} = \beta + K_s(w_2^b - w_2^t)$$
(4)

In the equation, w is the mass fraction, subscripts "1" and "2" represent the alcohols and salts, superscripts "t" and "b" stand for the top and the bottom phases, respectively. β is the constant relat-

Table 4 – Values of parameters of Eq. (4) for the studied AT-PSs at temperature T = 298.15 K

ATPS	K _s	β	R^2	$\frac{100}{sd_1^{a}}$	$\frac{100}{sd_2^a}$
1-propanol + Na ₂ SO ₄ + H ₂ O	15.73	0.3105	0.9659	2.90	0.41
1 -propanol + $NH_4NO_3 + H_2O$	5.49	0.0849	0.9670	3.40	1.15
$1\text{-propanol} + (\text{NH}_4)_2\text{SO}_4 + \text{H}_2\text{O}$	12.69	0.3609	0.9929	1.88	0.27
$2\text{-propanol} + \text{Na}_2\text{SO}_4 + \text{H}_2\text{O}$	12.32	0.0419	0.9902	0.85	0.23
$2\text{-propanol} + \text{NH}_4\text{NO}_3 + \text{H}_2\text{O}$	4.54	0.3922	0.9045	2.25	1.20
$2\text{-propanol} + (\text{NH}_4)_2 \text{SO}_4 + \text{H}_2 \text{O}_4$	11.48	-0.1500	0.9984	0.54	0.12

^a $sd = \left[\sum_{i=1}^{N} ((w_{i,j,\text{cal}}^{t} - w_{i,j,\text{exp}}^{t})^{2} + (w_{i,j,\text{cal}}^{b} - w_{i,j,\text{exp}}^{b})^{2})/2N\right]^{0.5}$, where N is the number of tie lines, w is the mass fraction, superscripts "t" and "b" are the top and the bottom phases and i = 1 and j = 2, sd_{1} and sd_{2} represent the mass percent standard deviations for alcohols and salts, respectively.

ed to the activity coefficient, and K_s is the salting-out coefficient. Table 4 shows the fitting parameters along with the correlation coefficient (R^2) and standard deviations (*sd*) values in the studied systems. On the basis of the value of R^2 and *sd*, it can be concluded that Eq. (4) shows satisfactory accuracy in correlation of the tie-line data fitting for the investigated systems.

Recently, some authors have attempt to illustrate the salting-out effect on the basis of the value of $K_{\rm s}$ coefficient^{1,18}, in which the larger value of the $K_{\rm s}$ coefficient was attributed to the more salting-out ability of the salt. The results show that the value of salting-out coefficient for alcohols $+ Na_2SO_4$ systems is nearly equivalent to the value in the systems composed of alcohols + $(NH_{4})_{2}SO_{4}$ because both of these systems are composed of monovalent cation and divalent anion salts that have close salting-out ability. The salting-out coefficient values of systems containing alcohols + NH₄NO₃ are remarkably smaller than other ATPSs (Table 4). Overall, the changing trend of the EEV and the K_s coefficient values of these three salts in a same hydrophilic alcohol (in Tables 3–4) are in agreement with the visual comparison of the experimental data (Fig. 1).

Effect of alcohols on phase separation

The effect of the alcohol type on the binodal curves of the studied systems at 298.15 K is shown in Fig. 2. As it can be seen from Fig. 2, for the same salts in different component solvents, the phase separation ability of 1-propanol is higher than that of 2-propanol, and the area of the two-phase region has the following order: 1-propanol > 2-propanol. There can be two reasons for this phenomenon. The dielectric constant of 1-propanol and 2-propanol is 20.6 and 19.4 at 298.15 K, respectively. The dielectric constant, which is a usable tool to measure the



Fig. 2 – Effect of alcohol type on the binodal curves in mass fraction and tie-lines for the studied systems at 298.15 K; (\diamond) 1-propanol, (Δ) 2-propanol, ($\diamond \diamond$) LLE compositions of 1-propanol+salts+H₂O systems and ($\Delta \diamond$) LLE compositions of 2-propanol+salts+H₂O systems.

molecule's polarity, is higher for 1-propanol than 2-propanol, and the phase separation ability of the alcohols is related to the polarity of alcohol molecules. So the phase separation ability of 1-propanol is higher than that of 2-propanol.

On the other hand, since 1-propanol has a higher boiling point than 2-propanol (370.35 K and 355.45 K, respectively), the boiling point may be considered an efficient criterion to represent the self-interaction forces between the alcohol molecules, as pointed out by Wang *et al.*¹⁹ Therefore, self-interaction forces between the molecules of the alcohol with the higher boiling point are stronger, so this alcohol can be easily excluded from the rest of the solution as a separated phase.

Also, in Table 3, it is shown that the value of V_{213}^* of the same salt in a solution increases from 2-propanol to 1-propanol. This could indicate that 1-propanol is easier to exclude from the aqueous (salt-rich) phase to the organic (alcohol-rich) phase. In other words, the phase-separation ability of alcohol increases with the increase in EEV. Thus, the phase-separation ability of the investigated alcohols is in the order 1-propanol > 2-propanol, which is also proved by the area of the biphasic region shown in Fig. 2.

Correlations

Correlation of binodal data

The binodal data of the investigated systems were correlated using a four-parameter equation (Eq. 5), which has been successfully used by Han *et al* 7 :

$$w_1 = \exp\left(a + bw_2^{0.5} + cw_2 + dw_2^2\right)$$
(5)

where w_1 , w_2 represent the mass fraction of hydrophilic alcohol (1) and salt (2) respectively, and *a*, *b*, *c*, and *d* are fitting parameters. The fitting parameters, correlation coefficients (R^2), and standard deviations (*sd*) are listed in Table 5. According to the obtained R^2 and standard deviations, it can be concluded that, Eq. (5) can successfully correlate the binodal curves of the investigated systems.

Table 5 – Values of parameters of Eq. (5) for the studied ATPSs at temperature T = 298.15 K

ATPS	а	b	С	d	R^2	100 <i>sd</i> ^a
1 -propanol + $Na_2SO_4 + H_2O$	1.793	-20.360	27.910	-40.160	0.9976	0.22
1 -propanol + $NH_4NO_3 + H_2O$	-14.050	62.220	-82.250	33.780	0.9973	0.21
$1\text{-propanol} + (\mathrm{NH}_4)_2 \mathrm{SO}_4 + \mathrm{H}_2 \mathrm{O}$	1.338	-14.680	14.030	-11.920	0.9958	0.41
2-propanol + Na ₂ SO ₄ + H ₂ O	2.601	-23.000	32.320	-32.820	0.9979	0.33
$2\text{-propanol} + \text{NH}_4\text{NO}_3 + \text{H}_2\text{O}$	-4.220	19.140	-26.300	6.587	0.9991	0.40
$2\text{-propanol} + (\text{NH}_4)_2 \text{SO}_4 + \text{H}_2\text{O}$	1.592	-16.160	25.240	-43.990	0.9981	0.52

^a $sd = \left(\sum_{i=1}^{n} (w_1^{cal} - w_1^{exp})^2 / n\right)^{0.5}$, where *n* represents the number of binodal data. w_1^{exp} is the experimental mass fraction of hydrophilic alcohols listed in Table 1, and w_1^{cal} is the corresponding data calculated using Eq. (5).

Correlation of tie-line data

The reliability of the measured tie-line compositions was ascertained by the correlation equations given by Othmer–Tobias²⁰ (Eq. (6)) and Bancroft²¹ (Eq. (7)). These equations have been widely used in the correlation of tie-line compositions of LLE systems¹¹ as well as the hydrophilic alcohol–salt ATPS^{1,7}:

$$\left(\frac{1 - w_1^t}{w_1^t}\right) = k_1 \left(\frac{1 - w_2^b}{w_2^b}\right)^n \tag{6}$$

$$\left(\frac{w_3^b}{w_2^b}\right) = k_2 \left(\frac{w_3^t}{w_1^t}\right)^r \tag{7}$$

where w_1^{t} , w_3^{t} represent the equilibrium compositions (in mass fraction) of the hydrophilic alcohol (1) and $H_2O(3)$ in the top phase, and w_2^{b} , w_3^{b} represent equilibrium compositions (in mass fraction) of the salt (2) and H₂O (3) in the bottom phase, respectively. k_1 , k_2 , n and r are fitting parameters. The linear relationship between $\ln((1 - w_1^{t})/w_1^{t})$ against $\ln((1 - w_2^{b})/w_2^{b})$, and $\ln(w_3^{b}/w_2^{b})$ against $\ln(w_3^{t}/w_1^{t})$ are feasible in order to calculate the parameters k_1, k_2, n, r , and the corresponding correlation coefficient (R^2) as well as standard deviation (sd), and the results are given in Table 6. According to the value of R^2 and sd, it can be concluded that Othmer-Tobias and Bancroft equations can be satisfactorily applied to the correlation of tieline data of the investigated systems, and the results show that the calculated values and experimental data are in good agreement.

Conclusions

Phase diagram data for 2-propanol/1-propanol + three different salts of $Na_2SO_4/(NH_4)_2SO_4/NH_4NO_3$ + water systems were experimentally determined at 298.15 K. The salting-out and the phase-forming ability of the mentioned ATPSs have been studied based on the effective excluded volume (EEV), the salting-out coefficient (K_s), the size and the Gibbs free energy of hydration of the ions. The salting-out ability of the investigated salts follows the order Na₂SO₄ > (NH₄)₂SO₄ > NH₄NO₃. Also, the phase-forming ability of hydrophilic alcohols is in the order: 1-propanol > 2-propanol. The results show that the two parameters K_s and EEV can be used to evaluate the salting-out ability of other phase-forming salts, and will be very useful for designing an ATPS.

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Table 6 – Values of parameters of Eqs. 6 and 7 for the studied ATPSs at temperature T = 298.15 K

ATDS		Othmer-Tob	ias equation		Bancroft equation			
AIPS	k_{1}	n	R^2	100 sd	<i>k</i> ₂	r	R^2	100 <i>sd</i> ^a
1-propanol + Na ₂ SO ₄ + H ₂ O	0.0265	1.8333	0.9798	1.01	6.7033	0.4759	0.9789	2.45
1 -propanol + $NH_4NO_3 + H_2O$	0.6086	3.3780	0.9335	2.73	1.0348	0.2221	0.9755	6.47
$1\text{-propanol} + (\text{NH}_4)_2\text{SO}_4 + \text{H}_2\text{O}$	0.0043	2.7207	0.9790	1.66	6.5156	0.3206	0.9838	4.7
2-propanol + Na ₂ SO ₄ + H ₂ O	0.1846	1.2037	0.9741	0.75	3.9622	0.6867	0.9767	1.26
$2\text{-propanol} + \text{NH}_4\text{NO}_3 + \text{H}_2\text{O}$	1.1268	1.2864	0.9830	0.41	1.1042	0.6771	0.9992	0.18
$2\text{-propanol} + (\text{NH}_4)_2 \text{SO}_4 + \text{H}_2 \text{O}$	0.1174	1.4174	0.9803	0.85	4.0734	0.5576	0.9800	1.69

^a $sd = \left(\sum_{i=1}^{n} (w_1^{cal} - w_1^{exp})^2 / n\right)^{0.5}$, where *n* represents the number of tie-lines. w_1^{exp} is the experimental mass fraction of hydrophilic alcohols in the top phase mentioned in Table 2, and w_1^{cal} is the corresponding data calculated using Eqs. (6–7). sd_1 and sd_2 show the standard deviations in Eq. 6 and Eq. 7, respectively.

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