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# The Development of Conceptual, Mathematical and System Dynamics Model for Food Industry Wastewater Purifying System

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### Abstract

The paper presents the development of the conceptual, mathematical and system dynamics model for the food industry wastewater purification system which removes organic matter. The food industry often located in places where is difficult to install large systems for water purification while small sophisticated systems are expensive. Wastewater food industry is contaminated with organic matter, phosphorus and nitrogen compounds. This paper presents a model of the small, cheap and effective cleaner water. The goal of the scientific investigation is developing such a model for purification wastewater and methodology design suitable to significant behavior patterns of contamination matter. Developed conceptual model is a computer variables model uses randomly chosen values from the theoretical probability distribution of the variable applied. For the validation of the model, considering that the distributions are asymmetrical non-Gaussian distributions, a non-parametric test was applied. Methodology proposed in the paper is mostly based on the simulation modeling.

Keywords: Conceptual model, Mathematical model, System Dynamics model, Wastewater Purifying System

## 1. Introduction

Environmental protection as an interdisciplinary scientific discipline is rapidly developing, using information and communication technology (ICT). Discovering, integrating and analyzing huge amounts of heterogeneous data is crucial in exploring the complex issues in environmental protection. Environmental informatics offers tools and approaches for the management of environmental data and transforms it into information and knowledge. The development of information technology affects the quality of data and research itself and moreover, it provides a stable base for their further development.

The goal of the simulation modeling is purification wastewater optimization process and methodology design suitable to significant behavior patterns of contamination matter. Mathematical models for the modeling and analyzing system, such as models of differential equations in continuous time models of differential equations with discrete time, the techniques of operations research and simulation models of discrete events, are well described in the literature, but the overall analysis behavior of technical systems including a dynamic approach (P. T. Hello<sup>6</sup>).

The choice of methodology for the analysis and design of water treatment processes continuous-discrete processes very sensitive. Analyzing, modeling and optimization of the

system behavior is based on the process modeling approach. This approach ensures the correct description of the structure, the entities and features relationships of the system, while modeling allows development of technical systems models regardless the diversity of behavior of their components. Studies on process modeling and model selection can be found in other works in this field (Pidd<sup>18</sup>). As simulation modeling, includes methods and techniques for the development of continuous and discrete systems models, as and the mechanism of the transition from one to the other components stage, assure correct choice for model designing (P. Klingstam<sup>12</sup>).

Also, simulation modeling can display the system at various levels. Conceptual models offer a presentation given to the lawfulness of its behavior and structure, and thus allow the study of the most important parameters of the functioning the entire system or its components. Using mathematical, statistical and algorithmic presentation system, allowing to explore the legality of the system behavior, as well as the interdependence of its entities, and the development of a system dynamics model of the system. In this way, simulation modeling is a powerful tool for analyzing the state system, alignment parameters and the selection of the appropriate mode of operation of technical systems.

The focus of this paper is modeling the purifying systems for food industry wastewater. In order to make the systems work in optimal conditions that are based on the concentrations of pollution data, the designing of a conceptual as well as a mathematical model was required. These models can show the reduction in the observed pollutants concentration, by using the systems of differential-difference equations for the purifiers considered, along with function equations for each substance. After checking the goodness of these models by comparing the actual output value of the pollution concentration with the outputs of experiments, it was verified, that they adequately represent the real system.

Following the mathematical model functions work development, it was necessary to design a computer model as well. Mathematical functions present independent variables, while the water quality in the supplied water purification systems, presents a dependent variable.

### 2. The Conceptual Model of Real System

From Water and Environment Joint Stock Company (WACO) database in Čakovec, North Croatia, the actual water treatment data, for the period of 5 years, was obtained. Due to the limited research material, the samples were based on the organic matter concentration. The weekly mean value of the data was calculated, while the Missing data (P.D. Allison<sup>1</sup>) belongs to Missing at random (MAR)), the sample remains representative. For the data processing (J.G. Ibrahim<sup>5</sup>, L. Gotal Dmitrović<sup>3</sup>) the recommended deletion method is Listwise deletion, which is only used for the complete rows of table data.

Values Missing at random (MAR) is an alternative to data Missing completely at random (MCAR), which occurs when the missing data is relating to a particular variable, like for example an accidentally skipped answer from a questionnaire (Little, R.J.A.<sup>13</sup>).

When one or more values are missing in a set of numbers, most software packages use Listwise Deletion Method. It is a simple method, most commonly used for missing data management. This method deletes rows containing gaps, and uses only the complete ones (P.D.Allison<sup>1</sup>; J.G.Ibrahim<sup>8</sup>). The interesting fact (L. Gotal Dmitrović<sup>5</sup>) is that the Listwise Deletion Method, which is the simplest method, provides very good matching results with the probability distributions. This method, in non-Gaussian probability distribution, closely follows the observed distributions, with the exception of a deviation from the actual value at the peak of the distribution.

For the purposes of this study, the actual, empirical data was collected and used from the non-Gaussian probability distribution of the observed technical system. These are asymmetric probability distributions with a tail, as is often the case in modeling complex technical systems (GotalDmitrović, L.<sup>6</sup>).

To achieve the authenticity of the model, it is necessary to incorporate the actual system behavior using the weekly mean concentration values, which were determined from the typical theoretical distribution of probability for every particular event frequency.

Using the applications Stat::Fit simulation packages Servicemodelv4.2., the characteristic theoretical distribution of the organic matter concentration, as well as the basic characteristics of descriptive statistics, were obtained at each checkpoint (at the entrance and the exit). These data is shown in Table 1.

	The entrance to the	Output from to the bioaeration
	bioaeration tank	tank
Theoretical	Lognormal (-207; 6,63;	Lognormal (4,68; 3,28; 0,576)
distribution	0,483)	
Data points	261	260
Minimum (mgO <sub>2</sub> /l)	36,1429	9,71429
Maximum (mgO <sub>2</sub> /l)	1 947,43	146,857
Mean (mgO <sub>2</sub> /l)	641,144	36,0885
Median (mgO <sub>2</sub> /l)	548,429	32
Mode (mgO <sub>2</sub> /l)	243,786	24,1429
Standard deviation (mgO <sub>2</sub> /l)	403,587	19,9632
Variance $((mgO_2/l)^2)$	162 882	398,529
Coefficient of variation (mgO <sub>2</sub> /l)	62,9479	55,3174

Table 1 Descriptive statistics and characteristic theoretical probability distribution of organic matter in the control point

After processing the data, the conceptual model was developed. The conceptual model of real system in the Diagram cycle activity - DCA(or Activity cycle diagram - ACD) form was created (Diagram 1), as well as Ishikawa diagram (Diagram 2).

There are many known modeling paradigms to describe the dynamics of system in process-oriented, event-based and activity-based viewpoints. Among those modeling paradigms, the activity-based modeling is a natural way to represent the activity paradigm of discrete event simulation, our knowledge about a system components patterns behavior. In activity-based modeling the dynamics of system is represented as an ACD (activity cycle diagram) which is a network model of the logical and temporal relationships among the activities (Shi, J.<sup>19</sup>). An ACD is easily implemented with the activity scanning method of simulation execution (Page, Jr., E.H.<sup>16</sup>).

The activity cycle diagram (ACD) is a method to describe the interactions of objects in a system. It uses the common graphical modeling notation to explain series of activities in reallife diverse circumstances. The core idea of the ACD was conceived by Tocher to describe the congestion problem at the steel plant in a general framework, called flow diagram with the three-phase rule (Kang, D.<sup>11</sup>). The objects in a system can be classified into two classes:

1) Transient object or entity that receives the services and leaves the system,

2) Resident object or resource that serves the entities.

In the ACD, the behavior or lifecycle of an entity or resource in the system is represented by an activity cycle, which alternates the active states with the passive states. The passive state of an entity or resource is called a queue in a circle, and the active state is called an activity in a rectangle as shown in Diagram 1. The arc is used to connect the activity and queue. The activity represents the interaction between an entity and resource(s), which usually takes a time delay to finish it. The token is used to represent the state of the queue and activity. All activity cycles are closed on itself ((Kang, D.<sup>11</sup>).



Diagram 1 DCA (ACD) system

Ishikawa diagrams (also called fishbone diagrams, herringbone diagrams, cause-andeffect diagrams, or Fishikawa) are causal diagrams created by Kaoru Ishikawa (1968) that show the causes of a specific event (Ishikawa, K.<sup>9</sup>). Common uses of the Ishikawa diagram are product design and quality defect prevention to identify potential factors causing an overall effect. Each cause or reason for imperfection is a source of variation. Causes are usually grouped into major categories to identify these sources of variation.

Cause and Effect Analysis gives you a useful way of doing this. This diagram-based technique, which combines Brainstorming with a type of Mind Map, pushes you to consider all possible causes of a problem, rather than just the ones that are most obvious (Jackson, K.<sup>10</sup>).

Although it was originally developed as a quality control tool, it can use the technique just as well in other ways. For instance, Ishikawa diagram can use it to:

- Discover the root cause of a problem.
- Uncover bottle neck sin processes.



Diagram 2 Ishikawa diagram of the system

# 3. The Mathematical Model of Real System

The mathematical model of real system was created, based on the system of differentialdifference equations. The Runge-Kutta method was used to solve equations system. Mathematical modeling framework was applied to develop the model component of water treatment system using differential and difference-differential equations. This occurs for the component according to the following reaction (1) written as differential equation.

$$\mathbf{S} = \left(\mathbf{D} \cdot (\mathbf{I} - \mathbf{S}) - \mathbf{dS}/\mathbf{dt}\right) / \left(\mathbf{K} + \mathbf{D}\right)$$
(1)

Whereas:

I – input concentration in system (mg/l), S – output concentration in system (mg/l),

dS/dt - changes in water cleanliness (mg/l/h),

K – goodness of purification (1/h),

1/D – time in the water holding in components (h).

The changes in water cleanliness are:

$$dS/dt = D \cdot (I-S) - S \cdot (K+D)$$
(2)

Initial equation in system component, according to equation (2), is:

$$dS/dt = D \cdot (I - S) - K \cdot S$$
(3)

$$dS/dt = (-D - K) \cdot S + D \cdot I$$
(4)

 $dS/dt + (D + K) \cdot S = D \cdot I$ (5)

Written in the form of difference equations:  

$$S(t+\Delta t) = S(t) + D \cdot (I - S) \cdot \Delta t - K \cdot S \cdot \Delta t$$
(6)

In the component, the difference equation was generated by using the Runge-Kutta method. Assuming that t(0) = 0, that is, at time t(0), the output S(0) = 0, according to the Runge-Kutta (IV) method, applies:

$$S(t_{i+1}) = S(t_i + \Delta t_i) = S(t_i) + 1/6 [K_1^{(i)} + K_2^{(i)} + K_3^{(i)} + K_4^{(i)}]$$
(8)

Whereas:

$$K_{1}^{(i)} = \Delta t_{i} \cdot F(t_{i}, S(t_{i}))$$

$$F(t_{i}, S(t_{i})) = D \cdot (I(t_{i}) - S(t_{i}) - K(t_{i}) \cdot S(t_{i})$$

$$(9)$$

$$(10)$$

$$K_{2}^{(i)} = \Delta t_{i} \cdot F(t_{i} + \Delta t_{i}/2, S(t_{i}) + 1/2K_{1}^{(i)})$$
(11)

 $F(t, S) = (-D - K) \cdot S + D \cdot I$   $F(t; + \Delta t; /2 \quad S(t;) + \frac{1}{2} K_1^{(i)}) =$ (12)

$$= (-D - K(t_i + \Delta t_i/2)) \cdot [S(t_i) + 1/2 K_1^{(i)} + D \cdot I(t_i + \Delta t_i/2)]$$
(13)

$$K_{3}^{(i)} = \Delta t_{i} \cdot F(t_{i} + \Delta t_{i}/2, S(t_{i}) + 1/2K_{2}^{(i)})$$

$$F(t_{i} + \Delta t_{i}/2, S(t_{i}) + \frac{1}{2}K_{2}^{(i)}) =$$
(14)

$$= (-D - K(t_i + \Delta t_i/2)) \cdot [S(t_i) + 1/2 K_2^{(i)} + D \cdot I(t_i + \Delta t_i/2)]$$

$$K_{4}^{(i)} = \Delta t_{i} \cdot F(t_{i} + \Delta t_{i}/2, S(t_{i}) + K_{3}^{(i)})$$

$$F(t_{i} + \Delta t_{i}, S(t_{i}) + K_{3}^{(i)}) =$$
(16)

$$= (-D - K(t_i + \Delta t_i)) \cdot [S(t_i) + K_3^{(i)} + D \cdot I(t_i + \Delta t_i)]$$
(17)

The goodness of purification isn't constant and it is presented as a theoretical probability distribution (Table 2):

$$\mathbf{K} = \mathbf{f}(\mathbf{S})/\mathbf{S} = \{ [(\mathbf{I} \cdot \mathbf{S}) \cdot \mathbf{D}] \cdot \mathbf{d}\mathbf{S}/\mathbf{d}\mathbf{t} \} / \mathbf{S}$$
(18)

A variables model uses randomly chosen values from the theoretical probability distribution of the applied variable (Table 1 for input concentration (I) and Table 2 for goodness of purification (K)).

(15)

	Goodness of purification in the bioaeration tank (K)
Theoretical distribution	Lognormal (-21,3; 3,63; 0,239)
Data points	260
Minimum (1/h)	0,856716
Maximum (1/h)	55,7228
Mean (1/h)	17,504
Median (1/h)	15,8148
Mode (1/h)	15,1228
Standard deviation (1/h)	9,35954
Variance (1/h) <sup>2</sup>	87,6011

 
 Table 2 Descriptive statistics and characteristic theoretical probability distribution for goodness of purification

Retention time (1 / D) is obtained from the expression: 1/D=V/O

(19)

Whereas :

V - volume component (m<sup>3</sup>) and

Q - flow rate of water through a component  $(m^3 / day)$ .

# 4. The System Dynamics Model of Real System

System dynamics is an approach to understanding the nonlinear behavior of technical systems over time using stocks and flows, internal feedback loops and time delays (MIT<sup>15</sup>).

John Sterman, in his book "Business Dynamics: Systems Thinking and Modeling for a Complex World" said: "System dynamics is a perspective and set of conceptual tools that enable us to understand the structure and dynamics of complex systems. System dynamics is also a rigorous modeling method that enables us to build formal computer simulations of complex systems and use them to design more effective policies and organizations. Together, these tools allow us to create management flight simulators-micro worlds where space and time can be compressed and slowed so we can experience the long-term side effects of decisions, speed learning, develop our understanding of complex systems, and design structures and strategies for greater success" (Sterman, J.D.<sup>20</sup>).

The system dynamics model was created using the Powersim Constructor program v. 2.51 (Figure 1).



Figure 1 System dynamics model of water purification of organic matter in the bioaeration tank (L. Gotal Dmitrović<sup>3</sup>)

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The model system pseudo code is shown in Figure 2.

Figure 2 Pseudo code model systems

The main object of interest was exploring the behavior of the crucial variable driving the purifying process (values of waste concentration and parameters of purifying equipment). Within the researched complex technical purifying system, all variables are non-Gaussian. According to the amount of data and its occupancy and behavior, the exploratory statistics along with a nonparametric test were applied for the validation of the model.

The two independent samples were used for the rank the sum test (the Mann-Whitney Utest). In statistics, the Mann-Whitney U test (also called the Mann-Whitney-Wilcoxon (MWW), Wilcoxon rank-sum test (WRS), or Wilcoxon-Mann-Whitney test) is a nonparametric test of the null hypothesis that two samples come from the same population against an alternative hypothesis, especially that a particular population tends to have larger values than the other. It can be applied on unknown distributions contrary to t-test which has to be applied only on normal distributions, and it is nearly as efficient as the t-test on normal distributions. (Mann, H.B.<sup>14</sup>).

The test involves the calculation of a statistic, usually called U, whose distribution under the null hypothesis is known. The U test is included in most modern statistical packages. It is also easily calculated by hand, especially for small samples. There are two ways of calculating U.

1. For comparing two small sets of observations, a direct method is quick, and gives insight into the meaning of the U statistic, which corresponds to the number of wins out of all pairwise contests. For each observation in one set, count the number of times this first value wins over any observations in the other set (the other value loses if this first is larger). Count 0.5 for any ties. The sum of wins and ties is U for the first set. U for the other set is the converse.

2. Assign numeric ranks for larger samples to all the observations, beginning with 1 for the smallest value. Where there are groups of tied values, assign a rank equal to the midpoint of unadjusted rankings [e.g., the ranks of (3, 5, 5, 9) are (1, 2.5, 2.5, 4)].

U is then given by (Zar, J.H.<sup>21</sup>):

$$U_1 = R_1 - \frac{n_1(n_1+1)}{2} \tag{20}$$

where  $n_1$  is the sample size for sample 1, and  $R_1$  is the sum of the ranks in sample 1.

Note that it doesn't matter which of the two samples is considered sample 1. An equally valid formula for U is

$$U_2 = R_2 - \frac{n_2(n_2+1)}{2} \tag{21}$$

The smaller value of  $U_1$  and  $U_2$  is one consulting significance tables. The sum of the two values is given by

$$U_1 + U_2 = R_1 - \frac{n_1(n_1+1)}{2} + R_2 - \frac{n_2(n_2+1)}{2}$$
(22)

Knowing that  $R_1+R_2=N(N+1)/2$  and  $N=n_1+n_2$ , and doing some algebra, we find that the sum is

$$U_1 + U_2 = n_1 n_2 \tag{23}$$

After confirming the goodness of the model, the actual system was designed (Table 3) to experiment with concentrations of organic matter in the food industry unpurified wastewater. The environmental data was transferred to the adaptive model within the various conditions, by the means of visualization and manipulation of basic system parameters, which are portable and adaptable to possible crisis situations.

		Real v.	Model	Mann-
				Whitney U test
The bioaeration tank - organic matter	Minimum (mgO <sub>2</sub> /l)	9,71	10,09	$H_0$
	Maximum (mgO <sub>2</sub> /l)	146,85	135,03	Z = -1,62996
	Mean (mgO <sub>2</sub> /l)	36,18	41,25	p= 0,103106

Table 3 Comparison of the real data and the data obtained by model

### 5. The Model of Food Industry Wastewater Purifying System

The adaptability of this model has been verified by the experiment in which the input variables were the organic matter concentrations from food industry wastewater (Table 4).

Organic compounds consist mainly of carbon, hydrogen and oxygen. The organic matter in wastewaters is typically a mixture of proteins and carbohydrates as well as oils and fats. In the slaughterhouse and meat industry wastewaters, for example, the organic content is mainly composed of grease which can be solid, suspended or emulsified.

The low solubility of fats and oils reduces the rate of their biological decomposition while in the wastewater treatment plant, fats can block up the wastewaters' treatment devices. If grease is not removed before the discharge of the treated wastewater, it can interfere with biological life in surface waters.

Wastewater also contains urea and small quantities of simple and extremely complex synthetic organic molecules. There are different analyses to determine the organic content of wastewater. The analyses can be divided into those that are used for measuring aggregate organic matter content in wastewater and those that are used for analyzing the individual organic compounds quantity. As a rule, only the aggregate organic matter content is measured. It consists of biochemical oxygen demand (BOD), chemical oxygen demand (COD) and total organic carbon (TOC).

	Conc. of org. matter in the wastewater
Theoretical distribution	Exponential (8,33; 223)
Data points	17
Minimum (mgO <sub>2</sub> /l)	8,33
Maximum (mgO <sub>2</sub> /l)	677
Mean (mgO <sub>2</sub> /l)	231,722
Median (mgO <sub>2</sub> /l)	176

Mode (mgO <sub>2</sub> /l)	8,33	
Standard deviation (mgO <sub>2</sub> /l)	204,544	
Variance (mgO <sub>2</sub> /l)	41 838,2	
$\chi^2$ -test	p-value: 0,662	H <sub>0</sub>
Kolmogorov-Smirnov test	p-value: 0,952	H <sub>0</sub>
Anderson-Darling test	p-value: 0,054	H <sub>0</sub>

Table 4 Descriptive statistics and theoretical probability distribution of organic matter in food industry wastewater

The system dynamics model of food industry wastewater purifying system is shown in Figure 3.



Figure 3 System dynamics model of food industry wastewater purifying system

Pseudo code of food industry wastewater purifying system is shown in Figure 4.

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Figure 4 Pseudocode of food industry wastewater purifying system

As the result, the wastewater has been purified from organic matter and turned into quality water suitable for releasing into a public sewerage system (Figure 5).



Figure 5 Results output concentrations (maximum allowable value is 125 mg O<sub>2</sub>/l)

Maximum Permissible Concentration (MPC) for the organic matter in effluents from wastewater, discharged into the public sewage system is 125 mg  $O_2/l$ . According to the concentration of the organic matter at the exit from the model (after waste water treatment) will not exceed a value of 90 mg  $O_2/l$ .

#### 6. Conclusion

Based on the study and the developed model, the food industry wastewater purifying system has been designed and recommended. Academic literature frequently publishes articles in which such systems describe the construction and technological solutions.

Discovering, integrating and analyzing huge amounts of heterogeneous data, often referred to as 'big data', is a key point in exploring complex technical systems. The development of information technologies with a special emphasis on the research methods of gathering and analyzing data and their storage and data access, have significantly enhanced the laboratory methods and their reports. Relational database allows employing constraints and roles on data types that can be entered (e.g. data typing), which can be used to assure the data quality with great multimedia approach involving related to adequate data or system representation on different level. Therefore, databases are crucial for analyzing and metadata preparation, as well as simulation modeling in order to establish conceptual models. Statistical software tools support many functions of simulation modeling, providing the additional benefit of supporting robust calculations, data analysis, quality assurance, visualization and data sub-setting.

The scientific community (as are G. H. Huang, N. B. Chang<sup>7</sup> in Journal of Environmental Informatics, or Marie S. Burbano<sup>2</sup> leads CDM Smith's wastewater modeling group etc.), has recently highlighted the need for the conceptualization and parameterization of the system model before the construction of the system itself. Also, large amounts of data often require special attention during their analysis and purification especially in the case of significant number of non-existing data. Large amounts of data requires in-depth analysis as well as a post hoc analysis, because a large amount of data can contain hidden knowledge reaching only by data mining in their depth, required to detect patterns of behavior observed entities and the media system as a whole.

The model was developed in order to gain the information on water purification. The input variables were used according to the results of the organic matter concentrations from

the waste water. What is more, the model is adaptable and can also be used for other concentrations or for studying the contamination of other substances. The methods of modeling and conceptualization of such situations contribute significantly to environmental protection and human health.

In addition, the economic component of the system should also be taken into consideration. The developed adaptive model allows setting the optimal structure of the model according to the needs and working environment.

Based on conducted research, developed and designed wastewater purification system, simulation model for food industry was done. Authors recommended implementations of developed model to optimized purification process parameters in accordance to legislation.

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