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Load Rating of Complex Bridges

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Load Rating of Complex Bridges

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2010

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Disclaimer

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Abstract

The National Bridge Inspection Standards require highway departments to inspect, evaluate, and determine load ratings for structures defined as bridges located on all public roads. Load rating of bridges is performed to determine the live load that structures can safely carry at a given structural condition. Bridges are rated for three types of loads, design loads, legal loads, and permit loads, which is a laborious and time-consuming task as it requires the analysis of the structure under different load patterns. Several tools are currently available to assist bridge engineers to perform bridge rating in a consistent and timely manner. However, these tools support the rating of conventional bridge systems, such as slab, I-girder, box girder and truss bridges. In the last decade, NDOR has developed innovative bridge systems through research projects with the University of Nebraska-Lincoln. An example of these systems is tied-arch bridge system adopted in Ravenna Viaduct and Columbus Viaduct projects. The research projects dealt mainly with the design and construction of the new system, while overlooking the load rating. Therefore, there is a great need for procedures and models that assist in the load rating of these new and complex bridge systems.

The objective of this project is to develop the procedures and models necessary for the load rating of tied-arch bridges, namely Ravenna and Columbus Viaducts. This includes developing refined analytical models of these structures and performing rating factor (RF) calculations in accordance to the latest Load and Resistance Factored Rating (LRFR) specifications. Two-dimensional and three-dimensional computer models were developed for each structure and RF calculations were performed for the primary structural components (i.e. arch, tie, hanger, and floor beam). RFs were calculated assuming various percentages of section loss and using the most common legal and permit loads in the state of Nebraska in addition to

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AASHTO LRFD live loads. In addition, the two structures were analyzed and RFs were calculated for an extreme event where one of the hangers is fully damaged.

Chapter 1 Introduction

1.1 Background

The National Bridge Inspection Standards requires highway departments to inspect, assess the condition, and calculate load ratings for structures defined as bridges and located on all public roads. Load rating of bridges is performed to determine the live load that structures can safely carry at a given structural condition. According to the Recording and Coding Guide for Structure Inventory and Appraisal of the Nation's Bridges, bridges are rated at three different stress levels, referred to as Inventory Rating (items 65 and 66 of Structural Inventory and Appraisal sheet), Operating Rating (items 63 and 64 of SI&A sheet), and Posting Rating (item 70 of SI&A sheet). Inventory rating is the capacity rating for the vehicle type used in the rating that will result in a load level which can safely utilize an existing structure for an indefinite period of time. Inventory load level approximates the design load level for normal service conditions. Operating rating will result in the absolute maximum permissible load level to which the structure may be subjected for the vehicle type used in the rating. This rating determines the capacity of the bridge for occasional use. Allowing unlimited numbers of vehicles to subject the bridge to the operating level will compromise the bridge life. This value is typically used when evaluating overweight permit vehicle moves. The posting rating is the capacity rating for the vehicle type used in the rating that will result in a load level which may safely utilize an existing structure on a routine basis for a limited period of time. The posting rating for a bridge is based on inventory level plus a fraction of the difference between inventory and operating. Structural capacities and loadings are used to analyze the critical members to determine the appropriate load rating. This may lead to load restrictions of the bridge or identification of components that require rehabilitation or other modification to avoid posting of the bridge (DelDOT 2004).

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Load rating is a laborious and time-consuming task as it requires the structural analysis of all primary structural components at different loading conditions. Several tools were developed to assist bridge engineers to perform bridge rating in a consistent and timely manner. Bridge Analysis and Rating System (BARS) is an AASHTO licensed product that is used to analyze and rate structures. This program was developed more than twenty years ago and the code was originally written in FORTRAN to run on Mainframe computers. A newer version BARS-PC was developed in 1993 to be used on personal computers. Several states are using BARS to analyze and rate the bridges, while others are using different products, such as VIRTIS, BRASS, LARS, etc. In Nebraska, LARS and it companion program "Complex Truss" are being used for rating and super-load analyses. However, this program supports only the rating of conventional bridge systems, such as slab, I-girder, box girder and truss bridges.

In the last decade, NDOR has developed innovative bridge systems through research projects with the University of Nebraska-Lincoln. An example of these systems is tied-arch bridge system used in Ravenna and Columbus Viaducts. The research projects dealt mainly with the design and construction issues of the new systems and not with their load rating. Therefore, there is a great need for procedures and models that assist NDOR bridge engineers in the load rating of such complex bridge systems that cannot be rated by the existing commercial programs.

The objective of this project is to develop the analytical models required for load rating of tied-arch bridges and perform rating factor (RF) calculations for a given set of super-loads and section loss percentages. The primary structural components of the Ravenna Viaduct and Columbus Viaduct will be analyzed using three-dimensional models and rated for design loads, legal loads, and permit loads according to the latest AASHTO Load and Resistance Factor Rating (LRFR) procedures. The tables shown below summarize the outcome of the project.

2

Primary Structural	Primary Structural Capacity at Different Section Loss Percentages			entages	Demand														
Element	0%	10%	20%	30%	40%	6 50%	DC	Р	DW	(LL+I) _{HL-93}	(LL+I) _{HS2}	(LL+I) _{N3}	(LL+I) _{N352}	(LL+I) _{N3-3}	(LL+I) _{SP1}	(LL+I) _{SP2}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SP5}
Floor beams																			
Hangers																			
Tie Beams																			
Arch Pipes																			
	Rating Factor																		
(LL+I) _{HL-93}	(LL-	+I) _{HS2}	₀ (۱	.L+I) _N	з	(LL+I),	V352	(LL+I)	N3-3	(LL+I)) _{SP1}	(LL+I) _{spz}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+	I) _{SP5}
			+		+														
			+		+														

1.2 Report Organization

The report is organized as follows. Chapter 2 summarizes the load rating procedures followed in this project. These procedures are in accordance to the AASHTO Manual for Bridge Evaluation, 1st Edition 2008. A description of the applied loads, load factors, and resistance factors is given. Chapter 3 presents the analytical models, capacity calculations, and load ratings of the Ravenna Viaduct. Chapter 4 presents the analytical models, capacity calculations, and load ratings of the Columbus Viaduct. Chapter 5 summarizes the project outcomes and the appendixes list the internal forces and moments in all the structural components of the two viaducts under all loading conditions.

2.1 General

Three load-rating procedures that are consistent with the load and resistance factor philosophy have been provided in Article 6A.4 of the 2008 AASHTO Manual for Bridge Evaluation for the load capacity evaluation of in-service bridges: design load rating (first level evaluation); legal load rating (second level evaluation); permit load rating (third level evaluation). Each procedure is geared to a specific live load model with specially calibrated load factors aimed at maintaining a uniform and acceptable level of reliability in all evaluations. The load rating is generally expressed as a rating factor for a particular live load model, using the general load-rating equation:

$$RF = \frac{C - (\gamma_{DC})(DC) - (\gamma_{DW})(DW) \pm (\gamma_{P})(P)}{(\gamma_{LL})(LL + IM)}$$
(6A.4.2.1-1)

For the Strength Limit States:

$$C = \varphi_c \varphi_s \varphi_n \tag{6A.4.2.1-2}$$

Where the following lower limit shall apply:

$$\varphi_c \varphi_s \ge 0.85$$
 (6A.4.2.1-3)

For the Service Limit States:

$$C = f_R$$
 (6A.4.2.1-4)

where:

RF = Rating factor

C = Capacity

- f_R = Allowable stress specified in the LRFD code
- R_n = Nominal member resistance (as inspected)

- DC = Dead load effect due to structural components and attachments
- DW = Dead load effect due to wearing surface and utilities
- P = Permanent loads other than dead loads

- IM = Dynamic load allowance
- γ_{DC} = LRFD load factor for structural components and attachments
- $\gamma_{DW} =$ LRFD load factor for wearing surfaces and utilities
- γ_p = LRFD load factor for permanent loads other than dead loads = 1.0
- γ_{LL} = Evaluation live load factor
- φ_c = Condition factor
- $\varphi_s = \text{System factor}$
- ϕ = LRFD resistance factor

The Rating Factor (RF) obtained may be used to determine the safe load capacity of the bridge in tons as follows:

 $RT = RF \times W \tag{6A.4.4.4-1}$

where:

- RT = Rating in tons for truck used in computing live load effect
- W = Weight in tons of truck used in computing live load effect

When the lane-type load model (see Figures D6A-4 and D6A-5) governs the load rating, the equivalent truck weight W for use in calculating a safe load capacity for the bridge shall be taken as 80 kips.

Strength is the primary limit state for load rating. Service and fatigue limit states are selectively applied in accordance with the provisions of this manual. Applicable limit states and the corresponding load factors are summarized in table 6A.4.2.2-1.

				Desig	n Load		
		Dead Load	Dead Load	Inventory	Operating	Legal Load	Permit Load
Bridge Type	Limit State*	γ _{dc}	ŶDW	γ _{ll}	γ _{ll}	γ_{LL}	ΥLL
	Strength I	1.25	1.50	1.75	1.35	Tables 6A.4.4.2.3a-1	—
						and 6A.4.4.2.3b-1	
Steel	Strength II	1.25	1.50	—	—	_	Table 6A.4.5.4.2a-1
	Service II	1.00	1.00	1.30	1.00	1.30	1.00
	Fatigue	0.00	0.00	0.75	-	—	—
Reinforced	Strength I	1.25	1.50	1.75	1.35	Tables 6A.4.4.2.3a-1 and 6A.4.4.2.3b-1	—
Concrete	Strength II	1.25	1.50	_	_	_	Table 6A.4.5.4.2a-1
	Service I	1.00	1.00	_	_	—	1.00
Prestressed	Strength I	1.25	1.50	1.75	1.35	Tables 6A.4.4.2.3a-1 and 6A.4.4.2.3b-1	—
Concrete	Strength II	1.25	1.50	—		_	Table 6A.4.5.4.2a-1
Concrete	Service III	1.00	1.00	0.80	_	1.00	—
	Service I	1.00	1.00	—	_	—	1.00
	Strength I	1.25	1.50	1.75	1.35	Tables 6A.4.4.2.3a-1	—
Wood						and 6A.4.4.2.3b-1	
	Strength II	1.25	1.50		—		Table 6A.4.5.4.2a-1

Table 6A.4.2.2-1-Limit States and Load Factors for Load Rating

* Defined in the AASHTO LRFD Bridge Design Specifications.

Strength I of prestressed concrete bridges was adopted for the load rating of the primary structural components of Ravenna and Columbus Viaducts in this report. According to equation 6A.4.2.1-2, the ultimate capacity of these components should be further multiplied by condition and system factors. The condition factor provides a reduction to account for the increased uncertainty in the resistance of deteriorated members and the likely increased future deterioration of these members during the period between inspection cycles. Since Ravenna and Columbus Viaducts are relatively new structures, this factor was taken 1.0 according to table 6A.4.2.3-1

Structural Condition of Member	φε
Good or Satisfactory	1.00
Fair	0.95
Poor	0.85

Table 6A.4.2.3-1—Condition Factor: φ_c

System factors are multipliers applied to the nominal resistance to reflect the level of redundancy of the complete superstructure system. Bridges that are less redundant will have their factored member capacities reduced, and, accordingly, will have lower ratings. The system factors in table 6A.4.2.4-1 are more conservative than the LRFD design values and may be used at the discretion of the evaluator until they are modified in the AASHTO LRFD Bridge Design Specifications. Therefore, it was decided that a system factor of 1.0 be used in rating all the structural components of Ravenna and Columbus Viaducts.

Superstructure Type	φε
Welded Members in Two-Girder/Truss/Arch Bridges	0.85
Riveted Members in Two-Girder/Truss/Arch Bridges	0.90
Multiple Eyebar Members in Truss Bridges	0.90
Three-Girder Bridges with Girder Spacing 6 ft	0.85
Four-Girder Bridges with Girder Spacing ≤4 ft	0.95
All Other Girder Bridges and Slab Bridges	1.00
Floorbeams with Spacing >12 ft and Noncontinuous Stringers	0.85
Redundant Stringer Subsystems between Floorbeams	1.00

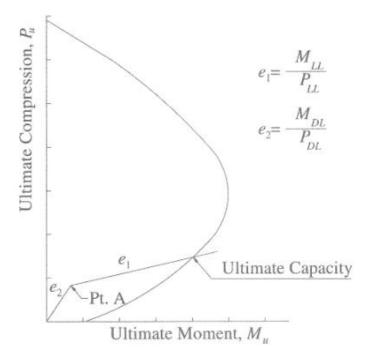
Table 6A.4.2.4-1—System Factor: ϕ_s for Flexural and Axial Effects

For rating concrete components subjected to both axial load and bending moment, the following steps were applied to obtain the rating factor:

- 1. Develop the interaction diagram, as shown below, using as-inspected section properties.
- 2. Locate point A that represents the factored dead load moment and axial force.
- Using the factored live load moment and axial force for the rating live load, compute the live load eccentricity e₁.
- 4. Continue from Point A with the live load eccentricity to the intersection with the interaction diagram.
- 5. Read the ultimate moment and axial capacities from the diagram.

6. Moment
$$RF = \frac{\text{Moment Capacity} - \text{Factored } M_{DL}}{\text{Factored } M_{TL-PL}}$$

 $\label{eq:axial_RF} \text{Axial} \; RF = \frac{\text{Axial Capacity} - \text{Factored} \; P_{DL}}{\text{Factored} \; P_{LL+DM}}$



2.2 Design Load Rating

Design load rating is a first-level assessment of bridges based on the HL-93 loading and LRFD design standards, using dimensions and properties of the bridge in its present as-inspected condition. It is a measure of the performance of existing bridges to current LRFD bridge design standards. Under this check, bridges are screened for the strength limit state at the LRFD design level of reliability (Inventory level), or at a second lower evaluation level of reliability (Operating level). Design load rating can serve as a screening process to identify bridges that should be load rated for legal loads per the following criteria:

- Bridges that pass HL-93 screening at the Inventory level will have adequate capacity for all AASHTO legal loads and State legal loads that fall within the exclusion limits described in the AASHTO LRFD Bridge Design Specifications.
- Bridges that pass HL-93 screening only at the Operating level will have adequate capacity for AASHTO legal loads, but may not rate (RF < 1) for all State legal loads, specifically those vehicles significantly heavier than the AASHTO trucks.

The figure shown below describes the HL-93 load (truck/tandem and lane loads), while table 6A.4.3.2.2-1 lists the live load factors for both inventory and operation rating levels. A dynamic load allowance of 33% (LRFD Design Article 3.6.2) was applied to the truck/tandem load only, while a multiple presence factor according to LRFD Design Article 3.6.1.1.2 was applied to both truck/tandem and lane loads. It should be noted that the design truck controlled the rating of all the primary structural components of Ravenna and Columbus Viaducts except the floor beams, where the design tandem controlled the rating.

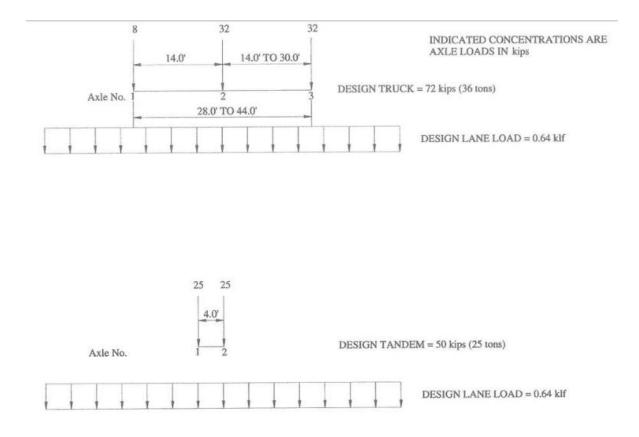


Table 6A.4.3.2.2-1—Load Factors for Design Load: γ_L

Evaluation Level	Load Factor			
Inventory	1.75			
Operating	1.35			

2.3 Legal Load Rating

Bridges that do not have sufficient capacity under the design-load rating shall be load rated for legal loads to establish the need for load posting or strengthening. This second level rating provides the safe load capacity of a bridge for the AASHTO family of legal loads or State legal loads, whichever is greater. The figures that follow present Nebraska legal loads (Type 3, Type 3S2, and Type 3-3), which are heavier than AASHTO legal loads, in addition to the lanetype loading for spans greater than 200 ft (i.e. Columbus Viaduct only).

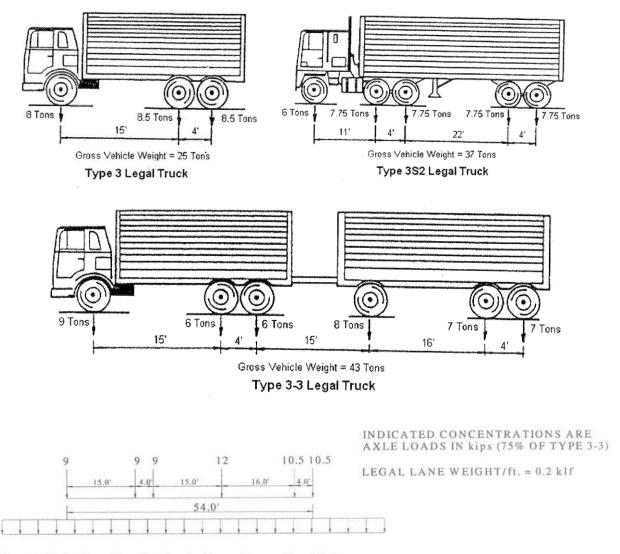


Figure D6A-4—Lane-Type Loading for Spans Greater than 200 ft

Strength is the primary limit state for legal load rating. Live load factors were selected based on the ADTT at the bridge as shown in table 6a.4.4.2.3a-1. The traffic data listed on project drawings indicates that future ADTT on Ravenna Viaduct is 235 and on Columbus Viaduct is 2,087. Based on these data, the live load factor was estimated to be 1.45 for Ravenna Viaduct and 1.70 for Columbus Viaduct. The dynamic load allowance and multiple presence factor of design loads were also applied to the legal loads.

	Load Factor for Type 3,
Traffic Volume	Type 3S2, Type 3-3 and
(One direction)	Lane Loads
Unknown	1.80
$ADTT \ge 5000$	1.80
<i>ADTT</i> = 1000	1.65
$ADTT \le 100$	1.40

Table 6A.4.4.2.3a-1—Generalized Live Load Factors, γ_L for Routine Commercial Traffic

Linear interpolation is permitted for other ADTT.

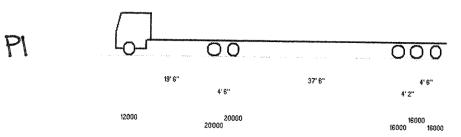
2.4 Permit Load Rating

Bridge Owners usually have established procedures and regulations which allow the passage of vehicles above the legally established weight limitations on the highway system. These procedures involve the issuance of a permit which describes the features of the vehicle and/or its load and, in most jurisdictions, which specifies the allowable route or routes of travel. Permits are issued by States on a single trip, multiple trip, or annual basis. Routine or annual permits are usually valid for unlimited trips over a period of time, not to exceed one year, for vehicles of a given configuration within specified gross and axle weight limits. Special permits are usually valid for a single trip only, for a limited number of trips, or for a vehicle of specified configuration, axle weights, and gross weight. Depending upon the authorization, these permit vehicles may be allowed to mix with normal traffic or may be required to be escorted in a manner which controls their speed, lane position, the presence of other vehicles on the bridge.

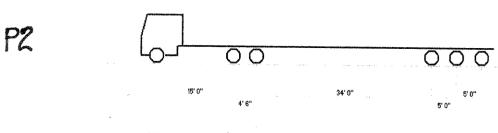
Permit load rating checks the safety of bridges in the review of permit applications for the passage of vehicles above the legally established weight limitations. This is a third level rating that should be applied only to bridges having sufficient capacity for legal loads. The figure that

follows presents the configurations of the most common permit trucks in Nebraska, which were used in this report. For spans up to 200 ft, only the permit vehicle shall be considered present in the lane. For spans between 200 and 300 ft, an additional lane load shall be applied to simulate closely following vehicles. The lane load shall be taken as 0.2 klf in each lane superimposed on top of the permit vehicle (for ease of analysis) and is applied to those portions of the span(s) where the loading effects add to the permit load effects.



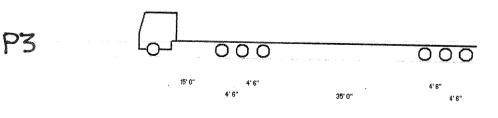






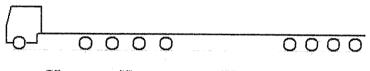


Weight: 140000



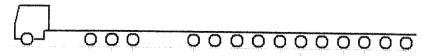
20000 20000 20000 20000 20000 20000

Weight: 180000



20000 20000 20000 20000 20000 20000 20000 20000

Weight: 300000



P5

P4

Table 6A.4.5.4.2a-1 specifies live load factors for permit load rating that are calibrated to provide a uniform and acceptable level of reliability. Load factors are defined based on the permit type, loading condition, and site traffic data. Permit load factors given in table 6A.4.5.4.2a-1 for the Strength II limit state are intended for spans having a rating factor greater than 1.0 when evaluated for AASHTO legal loads. Permit load factors are not intended for use in load-rating bridges for legal loads. For the rating of the primary structural components of Ravenna and Columbus Viaducts, it was assumed that permit vehicles will have multiple trips on the bridge with only one lane loaded at a time and will be mixed with other traffic vehicles. Based on the traffic data, the live load factor was estimated to be 1.6 for Ravenna Viaduct and 1.80 for Columbus Viaduct. The dynamic load allowance of design loads was applied to the permit loads with a multiple presence factor of 1.0. For other loading condition, rating factors should be multiplied by the ratio of the new load factor to existing one.

					Load Factor by Permit Weight ^b	
Permit Type	Frequency	Loading Condition	DF^{a}	ADTT (one direction)	Up to 100 kips	≥150 kips
Routine or	Unlimited	Mix with traffic (other	Two or more	>5000	1.80	1.30
Annual	Crossings	vehicles may be on the	lanes	=1000	1.60	1.20
		bridge)		<100	1.40	1.10
					All V	Veights
Special or Limited	Single-Trip	Escorted with no other vehicles on the bridge	One lane	N/A	1	.15
Crossing	Single-Trip	Mix with traffic (other	One lane	>5000	1	.50
		vehicles may be on the		=1000	1.40	
		bridge)		<100	1	.35
	Multiple-Trips	Mix with traffic (other	One lane	>5000	1	.85
	(less than 100	vehicles may be on the		=1000	1	.75
	crossings	bridge)		<100	1	.55

Table 6A.4.5.4.2a-1—Permit Load Factors: γ_L

^a DF = LRFD distribution factor. When one-lane distribution factor is used, the built-in multiple presence factor should be divided out.

^b For routine permits between 100 kips and 150 kips, interpolate the load factor by weight and ADTT value. Use only axle weights on the bridge.

2.5 Rating Assumptions

Below is a summary of the assumptions adopted in rating factor calculations:

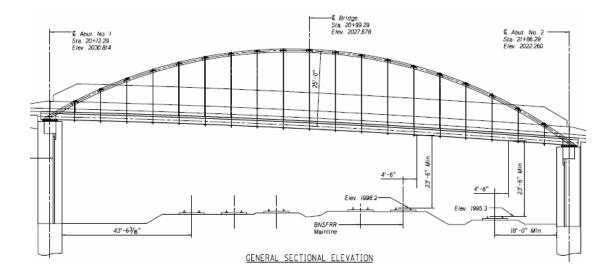
- All load rating analysis results include a dynamic load allowance of 33% applied to the truck load only and a multiple presence factors of 1.20 for one loaded lane, 1.0 for two loaded lanes, 0.85 for three loaded lanes, and 0.65 for four or more loaded lanes
- Section loss percentages represent the loss in the thickness of the structural steel, reinforcing steel, and prestressing steel. No loss in the concrete section is considered. For example, 20% section loss in the concrete-filled ¹/₂" thick arch pipe represents a concretefilled arch pipe that is 0.4 in. thick.
- The effect of steel confinement on the compressive strength of the filling concrete was considered in calculating the capacity of the arch. Below is an example of calculating the compressive strength of confined concrete. It should be noted that a reduced value of the hoop stress in the pipe is used due to the axial stresses in the pipe.

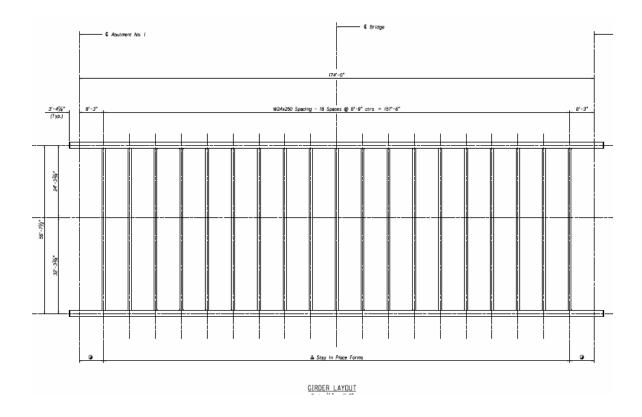
Thickness of the Tube t (in)	0.5	2t				
Outside Diameter of the Tube D _{out} (in)	12	$f_{22} = \frac{2t}{D} f_{sp}$				
Inside Diameter of the Tube D _{in} (in)	11	D_{in}				
Tube Yield Strength f_y (ksi)	50	$f_{c2} = f_{c0} + 4.1 f_{22}$				
*Reduced Tube Hoop Strength f_{yr} (ksi)	9.5					
*Reduced Tube Axial Strength f_{yr} (ksi)	44.5	$\int \int f_{c2} d$				
Steel Modulus of Elasticity E_s (ksi)	29,000	$\varepsilon_{c2} = \varepsilon_{c0} \left(5 \frac{f_{c2}}{f_{c0}} - 4 \right)$				
Unconfined Compressive Strength f_{co} (ksi)	8	() c0)				
Unconfined Concrete Strain ϵ_{co}	0.00201					
Confining Stress f 22 (ksi)	0.79					
Confined Compressive Strength f_{c2} (ksi)	11.25					
Confined Concrete Strain ϵ_{c2}	0.0060789					
* Sakino, Nakahara, Morino, and Nishiyama (2004)						

Chapter 3 Ravenna Viaduct

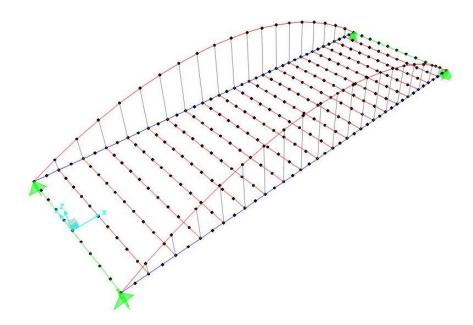
3.1 Analysis Model

The following figures present the general sectional elevation and plan view of Ravenna Viaduct. The analytical model was developed using the as-designed information available in the project specifications. The structural analysis of the viaduct was performed using the structural analysis software SAP2000 Advanced v.14.1.0.





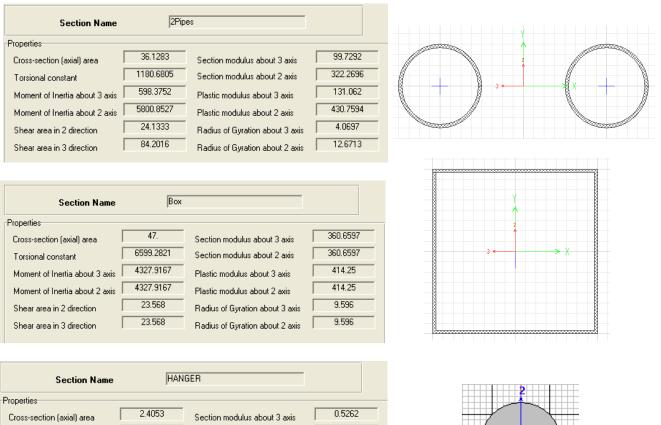
The viaduct was modeled as a 3-D structure using frame elements for ties, arches, cross beams; cable elements for hangers; and tendon elements for post-tensioning strands as shown by the following figure.



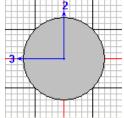
The analysis of the structure was performed in three stages that represent the construction sequence. The section properties and loads applied in each stage are as follows.

Stage I:

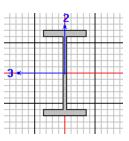
- Structure: Arch (steel only), tie (steel only), hangers, and cross beams.
- Loads: Own weight steel structure, metal decking (4 psf) and filling concrete.



Section Malile	li nerete	aen	
Properties			
Cross-section (axial) area	2.4053	Section modulus about 3 axis	0.5262
Torsional constant	0.9208	Section modulus about 2 axis	0.5262
Moment of Inertia about 3 axis	0.4604	Plastic modulus about 3 axis	0.8932
Moment of Inertia about 2 axis	0.4604	Plastic modulus about 2 axis	0.8932
Shear area in 2 direction	2.1648	Radius of Gyration about 3 axis	0.4375
Shear area in 3 direction	2.1648	Radius of Gyration about 2 axis	0.4375



Section Name	W24	×250	
Properties			
Cross-section (axial) area	73.5	Section modulus about 3 axis	645.6274
Torsional constant	66.6	Section modulus about 2 axis	109.697
Moment of Inertia about 3 axis	8490.	Plastic modulus about 3 axis	744.
Moment of Inertia about 2 axis	724.	Plastic modulus about 2 axis	171.
Shear area in 2 direction	27.352	Radius of Gyration about 3 axis	10.7476
Shear area in 3 direction	41.58	Radius of Gyration about 2 axis	3.1385



Stage II:

- Structure: Arch (filled with concrete), tie (filled with concrete), hangers, and cross beams.
- Loads: Post-tensioning of ties (2x19-0.6" strands) and weight of 8" thick concrete deck.

Section Name	2Pipe	58		v	
perties				*	
ross-section (axial) area	69.3394	Section modulus about 3 axis	141.3209		
orsional constant	1721.4898	Section modulus about 2 axis	601.8223	3	
oment of Inertia about 3 axis	847.9255	Plastic modulus about 3 axis	570.4662	1	
oment of Inertia about 2 axis	10832.801	Plastic modulus about 2 axis	2696.9286		
hear area in 2 direction	57.7207	Radius of Gyration about 3 axis	3.4969		
	165.2103		10,4001		
hear area in 3 direction Section Name	Box	Radius of Gyration about 2 axis	12.4991		
Section Name			, 12.4991		
Section Name		- 	702.4196		
Section Name operties iross-section (axial) area	, Box 140.031	Section modulus about 3 axis	702.4196		
Section Name	Box 140.031 14641.683	- 	702.4196		
Section Name operties iross-section (axial) area	Box 140.031 14641.683	Section modulus about 3 axis	702.4196		×
Section Name operties iross-section (axial) area irosional constant	Box 140.031 14641.683 8429.0348	Section modulus about 3 axis Section modulus about 2 axis	702.4196	1	× · · · · · · · · · · · · · · · · · · ·
Section Name operties iross-section (axial) area iorsional constant foment of Inertia about 3 axis	Box 140.031 14641.683 8429.0348	Section modulus about 3 axis Section modulus about 2 axis Plastic modulus about 3 axis	702.4196 702.4196 3456. 3456.		

Stage III:

• Structure: Arch (filled with concrete), tie (filled with concrete) and composite with 7.5" deck, hangers, end beams, cross beam composite with 7.5" concrete deck.

• Loads: Wearing surface (20 psf), barriers (0.4 k/ft), and live loads.

	Section Name	Box			
	Properties				
	Cross-section (axial) area	490.089	Section modulus about 3 axis	1532.3835	
	Torsional constant	28574.396 Section modulus about 2 axis 35901.27 Plastic modulus about 3 axis 3622894. Plastic modulus about 2 axis		20584.624	
	Moment of Inertia about 3 axis			14612.364	
	Moment of Inertia about 2 axis			251264.	
	Shear area in 2 direction	180.4282	Radius of Gyration about 3 axis	8.5589	
	Shear area in 3 direction	329.5319	Radius of Gyration about 2 axis	85.9786	
			xxxxx		
			,		
Section Na	ame FloorBeam				
perties					
ross-section (axial) area	171.7706 Section	modulus about 3 ay	uia 927.8679		
orsional constant	Jection	modulus about 3 as			3
	, 21222.202		2027.000		
foment of Inertia about 3	axis Plastic m	modulus about 3 axi	\$ 2027.000		> X

19772.746

11.1415

21.734

Analysis results for each member in the tied-arch shown below under each load case are given in a companion spreadsheet. The axial forces and bending moment at critical sections were used for load rating.

Plastic modulus about 2 axis

Radius of Gyration about 3 axis

Radius of Gyration about 2 axis

81138.74

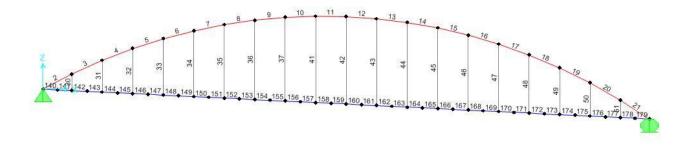
40.6969

104.2465

Moment of Inertia about 2 axis

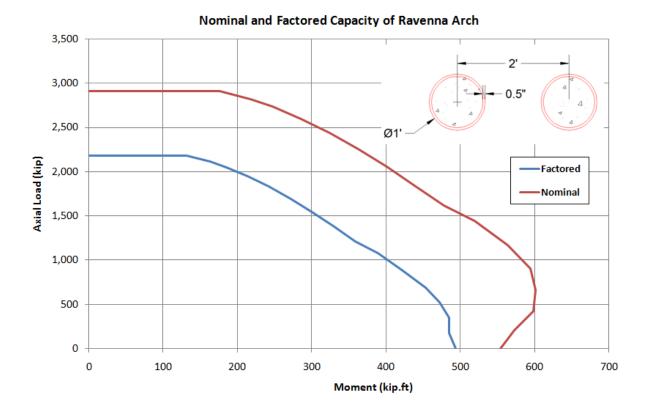
Shear area in 2 direction

Shear area in 3 direction

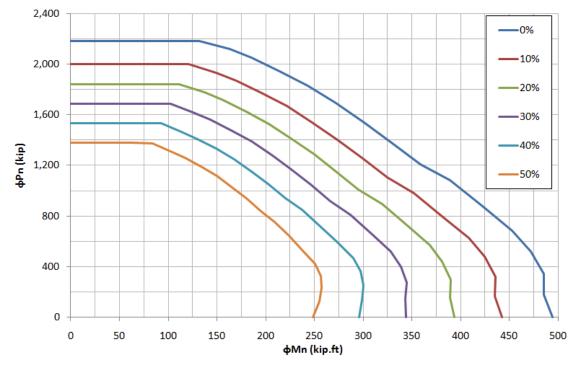


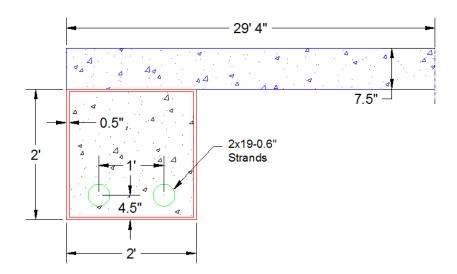
3.2 Capacity Charts

The section capacity of primary structural components of the Ravenna Viaduct was determined assuming section loss percentages ranging from 0% to 50%. These percentages of section loss represent the corrosion that might occur in the steel portion of these components and, consequently reducing the thickness of structural steel and/or the diameter of prestressing strands. Reduction in the concrete dimensions and/or strength was considered negligible and was not included in these percentages. The following figures present the factored and nominal capacity charts for arch, tie, hanger, and floor beam sections respectively. These capacity charts were developed using the strain compatibility approach and the AASHTO LRFD strength reduction factors.

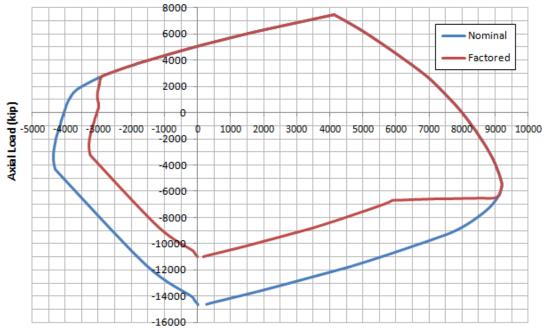




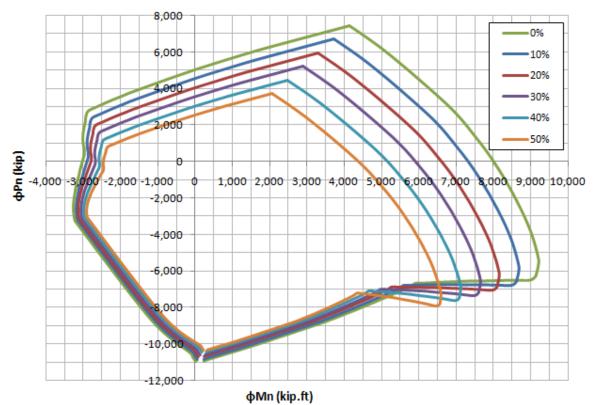




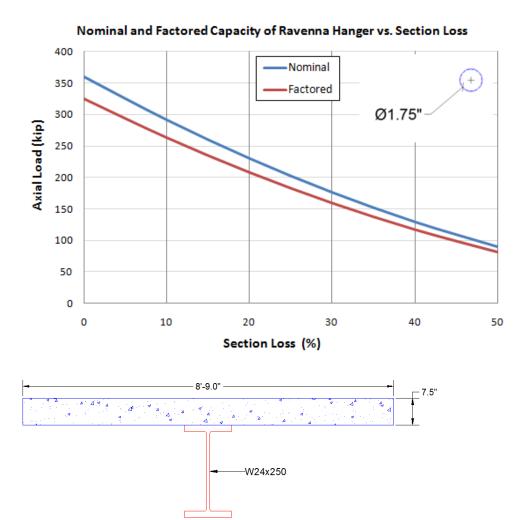
Nominal and Factored Capacity of Ravenna Tie



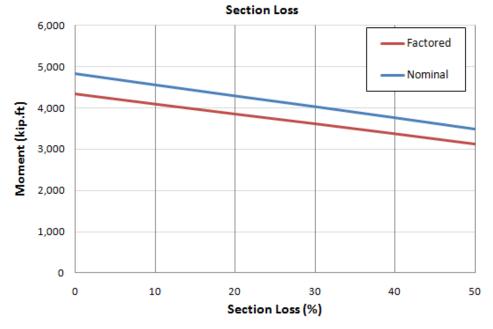
Moment (kip.ft)



Factored Capacity of Ravenna Tie at vs. Section Loss



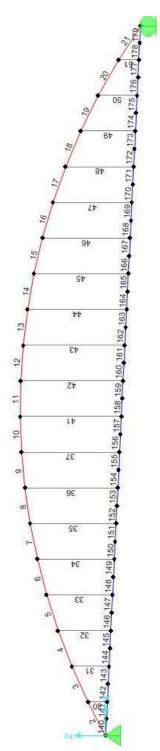
Nominal and Factored Capacity of Ravenna Floor Beams vs.



3.3 Rating Factors

The next table lists the capacity of each of the primary structural component of Ravenna Viaduct as well as the demand at the most critical sections based on the 3D analysis.

Primary Structural	ructural	Cap	Capacity at Different Section Loss Percentages	t Different Se Percentages	ent Se Itages	ction L		Elem.								Demand						
Element	ent	%0	10%	20%	30%	40%	50%	9	DC	d	DW TO	TOTAL (IL	(LL+I) _{HL-93} ((LL+I) _{HS20} (LL+I) _{N3}	(LL+I) _{N3}	(LL+I) _{N3S2}	(LL+I) _{N352} (LL+I) _{N3-3} (LL+I) _{SP1}	(LL+I) _{SP1}		(LL+I) _{SP2} (LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SP5}
Floor beams M (kip.ft)		4345	4100	3860	3625	3383	3135	N/A	466	0	70 6	687 1	1450	1084	889	813	732	650	751	796	751	751
Hangers	P (kip)	325	263	208	159	117	81	20	49.7	-3.1 6	6.5	69	27.9	15.9	11.1	15.9	18	10.3	12.5	14.5	18.5	30.9
Tie Beams	M (kip.ft) 7200 6500	7200	6500	5900	5000	4300	3650	172	-316	- 727	-23 2	298	2166	1704	1269	1342	1194	629	808	935	1061	1835
(+ve)	P (kip)	2250	2100 2000	-	1700	1650	1500	172	777	0	83 10	1096	360	204	142	205	232	132	159	185	235	394
Tie Beams	M (kip.ft) -3000 -2800 -2700	-3000	-2800	-	-2500	-2500 -2000 -1700	-1700	172	-316	- 727	-23 2	- 298	-1579	-1068	-749	-1032	-1121	-560	-691	-789	-991	-1678
(-ve)	P (kip)	1900	1850	1800	1700	1600	1500	172	777	0	83 10	1096	360	204	142	205	232	132	159	185	235	394
Arch Disco	M (kip.ft)	-160 -145	-145	-135	-122	-110	-100	20	-41	-39	-1	- 16-	-25.0	-16.4	-11.5	-16.0	-17.6	-9.1	-11.1	-12.8	-16.1	-27.2
	P (kip)	-2130	-2130 -1950 -1780 -1620 -1480 -1320	-1780	-1620	-1480	-1320	20	-892	47 -	-96 -1	-1213 -4	-415.4	-237.3	-165.4	-238.2	-269.9	-154.9	-187.6	-217.3	-277.2	-463.2

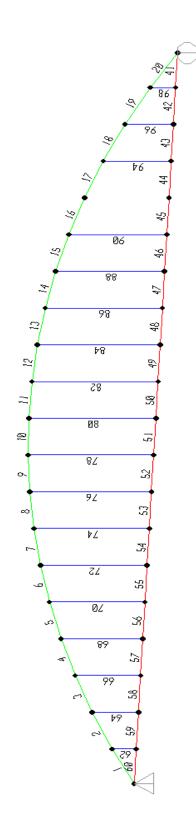


The capacity and demand values were used to calculate the rating factor based on the equation 6A.4.2.1-1 presented in Chapter 2. The table shown below lists the rating factor in ratios and in tons. Section loss percentage, system factor and live load factors used in the calculations are highlighted in yellow and can be easily modified in the spreadsheet as needed.

					I	ive Load I	actors				
System Factor	1.0	1.	75		1.45				1.6		
Section Loss	0%	(LL+I) _{HL-93}	(LL+I) _{HS20}	(LL+I) _{N3}	(LL+I) _{N3S2}	(LL+I) _{N3-3}	(LL+I) _{SP1}	(LL+I) _{SP2}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SP5}
Floor beams	M (kip.ft)	1.44	1.93	2.84	3.10	3.45	3.51	3.04	2.87	3.04	3.04
Hangers	P (kip)	5.25	9.21	15.92	11.11	9.82	15.55	12.81	11.04	8.66	5.18
Tie Beams	M (kip.ft)	1.82	2.31	3.75	3.55	3.99	<mark>6.</mark> 55	5.34	4.61	4.07	2.35
(+ve)	P (kip)	1.83	3.23	5.61	3.88	3.43	5.47	4.54	3.90	3.07	1.83
Tie Beams	M (kip.ft)	1.19	1.76	3.04	2.20	2.03	3.68	2.98	2.61	2.08	1.23
(-ve)	P (kip)	1.28	2.25	3.91	2.71	2.39	3.81	3.16	2.72	2.14	1.28
Auch Din ex	M (kip.ft)	1.58	2.41	4.15	2.99	2.71	4.76	3.90	3.38	2.69	1.59
Arch Pipes	P (kip)	1.26	2.21	3.83	2.66	2.34	3.70	3.06	2.64	2.07	1.24
Rating in	Tons	80	36	25	37	43	50	60	70	100	150
Floor beams	M (kip.ft)	115.3	69.4	70.9	114.8	148.2	175.7	182.5	201.0	304.2	456.4
Hangers	P (kip)	419.8	331.5	398.0	411.2	422.1	777.4	768.7	773.1	865.6	777.4
Tie Beams	M (kip.ft)	145.7	83.3	93.8	131.2	171.4	327.3	320.4	323.0	406.6	352.6
(+ve)	P (kip)	146.6	116.4	140.1	143.7	147.5	273.3	272.2	273.0	307.0	274.6
Tie Beams	M (kip.ft)	95.5	63.5	75.9	81.5	87.2	184.0	179.0	182.8	208.0	184.2
(-ve)	P (kip)	102.1	81.1	97.7	100.1	102.8	190.4	189.7	190.2	213.9	191.4
Arch Direct	M (kip.ft)	126.7	86.9	103.9	110.5	116.7	237.9	234.0	236.8	268.9	238.8
Arch Pipes	P (kip)	101.0	79.5	<mark>95.6</mark>	98.3	100.8	185.1	183.4	184.7	206.9	185.7

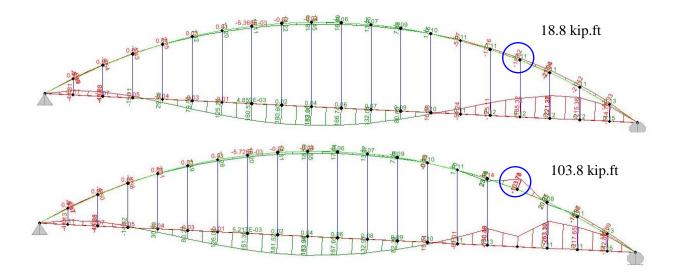
Ravenna Viaduct was also analyzed in case of one of the hangers was totally damaged. This analysis was performed in a two dimensional model by eliminating the hanger at the location of the tie section with the highest bending moment. The next tables list the capacity and demand of each structural member as well as the calculated rating factors.

Primary Structural	ctural	Cap	Capacity at Different Section Percentages	t Diffe Percer	t Different Se Percentages	_	Loss	Elem.								Demand						
Element	L.	%0	10%	20%	30%	40%	50%	9	DC	P I	DW T	TOTAL (I	LL+I) _{HL-93}	(LL+I) _{HL-93} (LL+I) _{HS20}	(LL+I) _{N3} ((LL+I) _{N352}	(LL+I) _{N3-3}	(LL+I) _{SP1}	(LL+I) _{SP2}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SP5}
Floor beams M (kip.ft) 4345	1 (kip.ft)	4345	4100	3860	3625	3383	3135	N/A	466	0	70	687	1450	1084	889	813	732	650	751	796	751	751
Hangers	P (kip)	325	263	208	159	117	81	98	75	-5	7	66	44	29	19	26	28	18	22	25	30	43
Tie Beams M	M (kip.ft)	7200	6500	5900	5000	4300	3650	45	-449	669	-30	92	2173	1683	1244	1363	1257	969	855	766	1145	2037
(+ve)	P (kip)	2250	2100	2000	1700	1650	1500	45	681	0	63	946	363	206	143	207	234	136	164	190	243	406
Tie Beams	M (kip.ft) -3000 -2800 -2700 -2500 -2000 -1700	-3000	-2800	-2700	-2500	-2000	-1700	45	-449	- 669	-30	92	-1580	-1075	-806	-1102	-1186	-599	-740	-845	-1059	-1833
(-ve)	P (kip)	1900	1850	1800	1700	1600	1500	45	681	0	63	946	363	206	143	207	234	136	164	190	243	406
M Dince	M (kip.ft)	-340	-305 -275		-245	-225	-200	16	-180 -10		-15	-257	-132	-83	-58	-83	-92	-52	-63	-73	-93	-156
	P (kip) -1320 -1205 -1140 -1040 -930	-1320	-1205	-1140	-1040	-930	-800	16	-839	53 -	-68 -	-1098	-389	-221	-154	-222	-252	-146	-177	-205	-262	-437



					I	Live Load I	Factors				
System Factor	1.0	1.3	75		1.45				1.6		
Section Loss	0%	(LL+I) _{HL-93}	(LL+I) _{HS20}	(LL+I) _{N3}	(LL+I) _{N3S2}	(LL+I) _{N3-3}	(LL+I) _{SP1}	(LL+I) _{SP2}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SP5}
Floor beams	M (kip.ft)	1.44	1.93	2.84	3.10	3.45	3.51	3.04	2.87	3.04	3.04
Hangers	P (kip)	2.92	4.51	8.04	5.95	5.51	7.69	6.54	5.67	4.74	3.26
Tie Beams	M (kip.ft)	1.87	2.41	3.94	3.60	3.90	6.39	5.20	4.45	3.88	2.18
(+ve)	P (kip)	2.05	3.62	6.27	4.35	3.84	6.00	4.96	4.28	3.36	2.01
Tie Beams	M (kip.ft)	1.12	1.64	2.65	1.94	1.80	3.23	2.61	2.29	1.82	1.05
(-ve)	P (kip)	1.50	2.65	4.59	3.18	2.81	4.39	3.63	3.13	2.45	1.47
Arch Pipes	M (kip.ft)	0.36	0.57	0.99	0.70	0.62	1.00	0.82	0.71	0.56	0.34
Arch Pipes	P (kip)	0.33	0.57	0.99	0.69	0.61	0.95	0.78	0.68	0.53	0.32
Rating in 1	Fons	80	36	25	37	43	50	60	70	100	150
Floor beams	M (kip.ft)	115.3	69.4	70.9	114.8	148.2	175.7	182.5	200.9	304.2	456.3
Hangers	P (kip)	233.4	162.5	201.1	220.1	236.7	384.4	392.7	397.1	473.7	488.6
Tie Beams	M (kip.ft)	149.5	86.9	98.5	133.1	167.7	319.3	311.9	311.8	387.8	327.2
(+ve)	P (kip)	164.3	130.3	156.9	161.1	165.1	300.2	297.7	299.7	335.6	301.3
Tie Beams	M (kip.ft)	89.5	59.2	66.1	71.6	77.3	161.4	156.7	160.2	182.5	158.2
(-ve)	P (kip)	120.2	95.3	114.7	117.8	120.8	219.6	217.8	219.2	245.5	220.4
Arch Pipes	M (kip.ft)	29.0	20.6	24.8	25.8	26.8	50.0	49.3	49.9	56.0	50.3
ArchiPipes	P (kip)	26.0	20.6	24.9	25.5	26.1	47.3	47.0	47.3	53.0	47.6

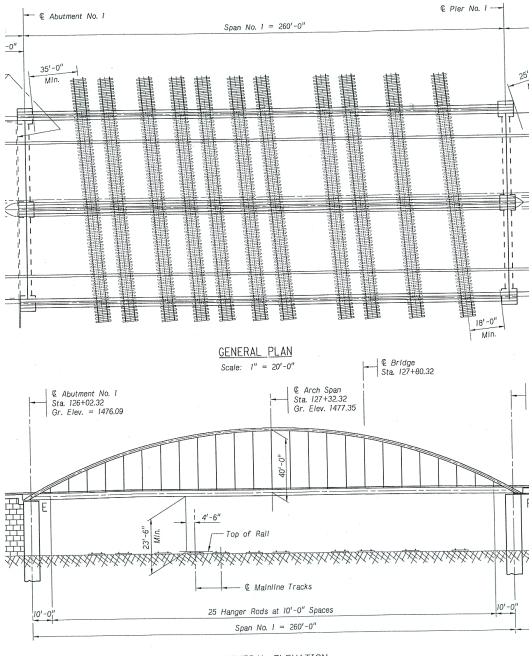
Below are the bending moment diagrams of the arch and tie due to deck weight only before and after the loss of one hanger. These diagrams show the significant increase in the arch moment.



Chapter 4 Columbus Viaduct

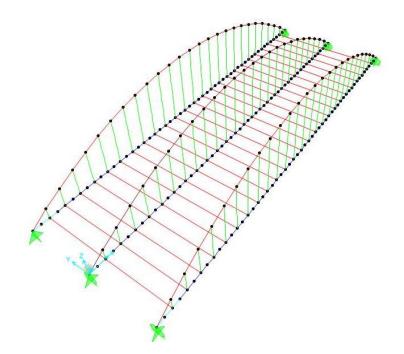
4.1 Analysis Models

The figures shown in the following pages present the general sectional elevation and plan view of Columbus Viaduct. The analytical model was developed using the as-designed information available in the project specifications. The structural analysis of the viaduct was performed using the structural analysis software SAP2000 Advanced v.14.1.0.



GENERAL FLEVATION

The viaduct was modeled as a 3-D structure using frame elements for ties, arches, cross beams; cable elements for hangers; and tendon elements for post-tensioning strands as shown next.

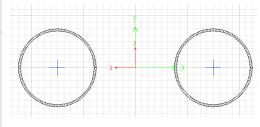


The analysis of the structure was performed in three stages that represent the construction sequence. The section properties and loads applied in each stage are as follows:

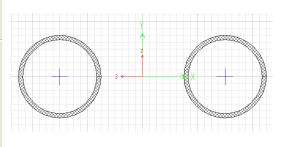
Stage I:

- Structure: Arch (steel only), tie (steel only), hangers, and cross beams.
- Loads: Own weight steel structure, metal decking (4 psf) and filling concrete.

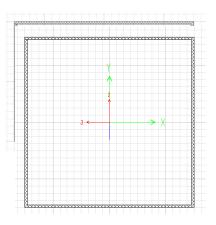
Section Name	2Pipe	28	
Properties			
Cross-section (axial) area	54.9779	Section modulus about 3 axis	234.0377
Torsional constant	4155.4189	Section modulus about 2 axis	737.747
Moment of Inertia about 3 axis	2106.3397	Plastic modulus about 3 axis	303.3903
Moment of Inertia about 2 axis	19919.17	Plastic modulus about 2 axis	983.2552
Shear area in 2 direction	36.6441	Radius of Gyration about 3 axis	6.1897
Shear area in 3 direction	5.936E-13	Radius of Gyration about 2 axis	19.0345



Section Name	2Pipe	esMid	
Properties			
Cross-section (axial) area	100.5571	Section modulus about 3 axis	407.8032
Torsional constant	7242.7315	Section modulus about 2 axis	1342.6193
Moment of Inertia about 3 axis	3670.2289	Plastic modulus about 3 axis	541.4239
Moment of Inertia about 2 axis	36250.72	Plastic modulus about 2 axis	1798.4194
Shear area in 2 direction	67.3167	Radius of Gyration about 3 axis	6.0414
Shear area in 3 direction	5.945E-13	- Radius of Gyration about 2 axis	18.9868

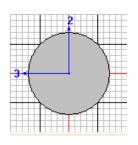


Section Name	Box		
Properties			
Cross-section (axial) area	59.	Section modulus about 3 axis	498.7431
Torsional constant	11958.281	Section modulus about 2 axis	618.6065
Moment of Inertia about 3 axis	5984.9167	Plastic modulus about 3 axis	555.25
Moment of Inertia about 2 axis	11134.917	Plastic modulus about 2 axis	732.25
Shear area in 2 direction	23.7757	Radius of Gyration about 3 axis	10.0717
Shear area in 3 direction	35.024	Radius of Gyration about 2 axis	13.7378



Section Name	BoxE	ND	
Properties			
Cross-section (axial) area	71.	Section modulus about 3 axis	828.662
Torsional constant	22628.535	Section modulus about 2 axis	828.662
Moment of Inertia about 3 axis	14915.917	Plastic modulus about 3 axis	945.25
Moment of Inertia about 2 axis	14915.917	Plastic modulus about 2 axis	945.25
Shear area in 2 direction	35.4489	Radius of Gyration about 3 axis	14.4943
Shear area in 3 direction	35.4489	Radius of Gyration about 2 axis	14.4943

Section Name	HAN	GER	
Properties	2.4053		0.5262
Cross-section (axial) area	2.4053	Section modulus about 3 axis	J 0.5262
Torsional constant	0.9208	Section modulus about 2 axis	0.5262
Moment of Inertia about 3 axis	0.4604	Plastic modulus about 3 axis	0.8932
Moment of Inertia about 2 axis	0.4604	Plastic modulus about 2 axis	0.8932
Shear area in 2 direction	2.1648	Radius of Gyration about 3 axis	0.4375
Shear area in 3 direction	2.1648	Radius of Gyration about 2 axis	0.4375



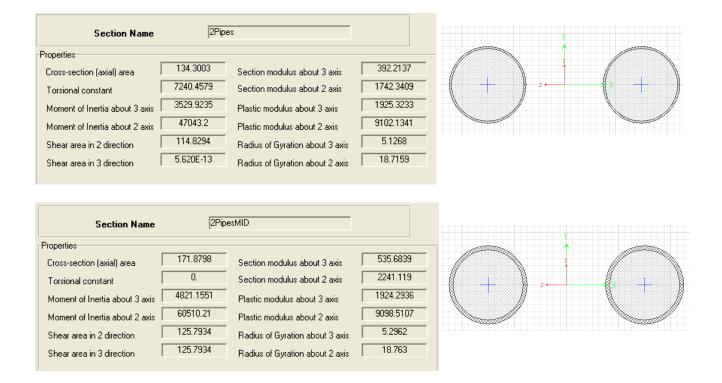
Section Name	W24	×162	
Properties			
Cross-section (axial) area	47.7	Section modulus about 3 axis	413.6
Torsional constant	18.5	Section modulus about 2 axis	68.1538
Moment of Inertia about 3 axis	5170.	Plastic modulus about 3 axis	468.
Moment of Inertia about 2 axis	443.	Plastic modulus about 2 axis	105.
Shear area in 2 direction	17.625	Radius of Gyration about 3 axis	10.4108
Shear area in 3 direction	26.4333	Radius of Gyration about 2 axis	3.0475

1.		

Stage II:

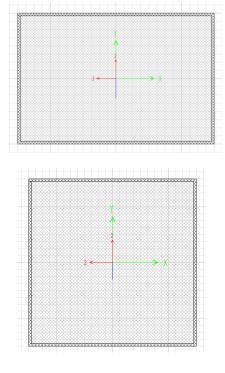
- Structure: Arch (filled with concrete), tie (filled with concrete), hangers, and cross beams.
- Loads: Post-tensioning of ties (2x19-0.6" strands for outside ties and 2x37-0.6" strands

for median ties) and weight of 8" thick concrete deck.



Section Name	Box		
Properties			
Cross-section (axial) area	200.569	Section modulus about 3 axis	1018.8124
Torsional constant	29095.787	Section modulus about 2 axis	1421.486
i orsional constant			
Moment of Inertia about 3 axis	12225.749	Plastic modulus about 3 axis	5184.
Moment of Inertia about 2 axis	25586.749	Plastic modulus about 2 axis	7776.
Shear area in 2 direction	156.9875	Radius of Gyration about 3 axis	7.8074
	162,6403		11,2947
Shear area in 3 direction	102.0403	Radius of Gyration about 2 axis	11.2347

Section Name	ВожЕ	ND	
Properties	286.431		2050 4353
Cross-section (axial) area	200.401	Section modulus about 3 axis	2000.4000
Torsional constant	64935.18	Section modulus about 2 axis	2050.4353
Moment of Inertia about 3 axis	36907.83	Plastic modulus about 3 axis	11664.
Moment of Inertia about 2 axis	36907.83	Plastic modulus about 2 axis	11664.
Shear area in 2 direction	231.4441	Radius of Gyration about 3 axis	11.3514
Shear area in 3 direction	231.4441	Radius of Gyration about 2 axis	11.3514

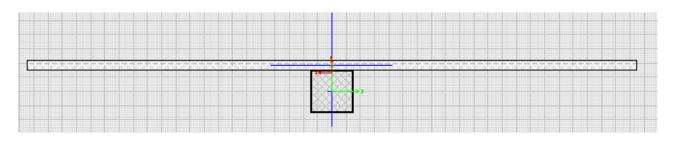


Stage III:

- Structure: Arch (filled with concrete), tie (filled with concrete) and composite with 7.5" deck, hangers, end beams, cross beam composite with 7.5" concrete deck.
- Loads: Wearing surface (20 psf), barriers (0.4 k/ft), and live loads.

Section Name	Medi	anBox	
roperties			
Cross-section (axial) area	738.3103	Section modulus about 3 axis	1949.9985
Torsional constant	53023.4	Section modulus about 2 axis	48864.27
Moment of Inertia about 3 axis	47414.54	Plastic modulus about 3 axis	21701.623
Moment of Inertia about 2 axis	12582550	Plastic modulus about 2 axis	538226.
Shear area in 2 direction	218.2639	Radius of Gyration about 3 axis	8.0138
Shear area in 3 direction	532.4806	Radius of Gyration about 2 axis	130.5464

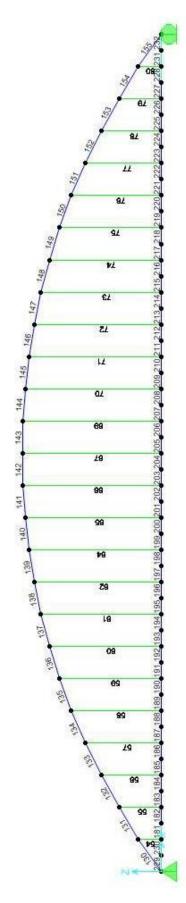
Section Name	Medi	anBoxEnd	
Properties			
Cross-section (axial) area	808.2414	Section modulus about 3 axis	3491.5446
Torsional constant	87480.19	Section modulus about 2 axis	48901.92
Moment of Inertia about 3 axis	116855.84	Plastic modulus about 3 axis	593891.1
Moment of Inertia about 2 axis	12592245	Plastic modulus about 2 axis	542114.
Shear area in 2 direction	261.8336	Radius of Gyration about 3 axis	12.0242
Shear area in 3 direction	537.0784	Radius of Gyration about 2 axis	124.8191



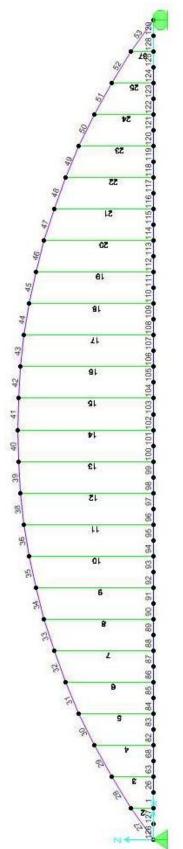
Section Name	Outsi	deBox	
Properties			
Cross-section (axial) area	474.0345	Section modulus about 3 axis	1815.5731
Torsional constant	46915.69	Section modulus about 2 axis	14121.786
Moment of Inertia about 3 axis	40416.21	Plastic modulus about 3 axis	23055.917
Moment of Inertia about 2 axis	1945276.	Plastic modulus about 2 axis	159576.5
Shear area in 2 direction	202.3154	Radius of Gyration about 3 axis	9.2336
Shear area in 3 direction	320.2887	Radius of Gyration about 2 axis	64.0598

Section Name	Outsi	ideBoxEnd	
Properties Cross-section (axial) area Torsional constant Moment of Inertia about 3 axis Moment of Inertia about 2 axis Shear area in 2 direction Shear area in 3 direction	493.9138 61761.04 65317.59 1948583.4 222.7259 322.5901	Section modulus about 3 axis Section modulus about 2 axis Plastic modulus about 3 axis Plastic modulus about 2 axis Radius of Gyration about 3 axis Radius of Gyration about 2 axis	2488.875 14145.796 34965.92 161520.5 11.4998 62.8107

Analysis results for each member in the tied-arch shown below under each load case are given in a companion spreadsheet. The axial forces and bending moment at critical sections were used for load rating.



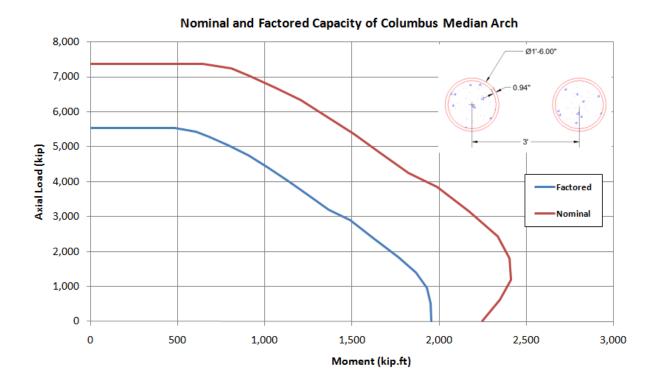
Outside Arch



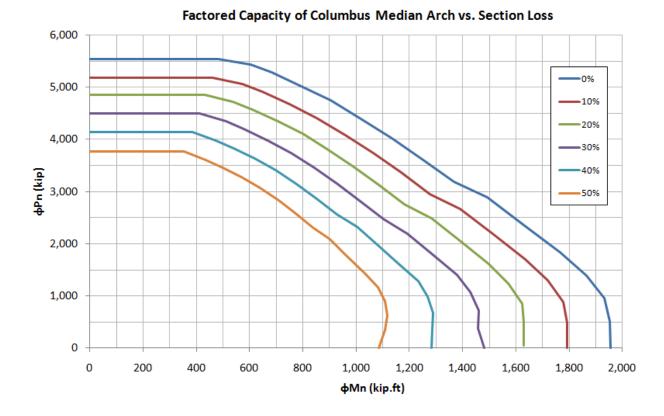
Median Arch

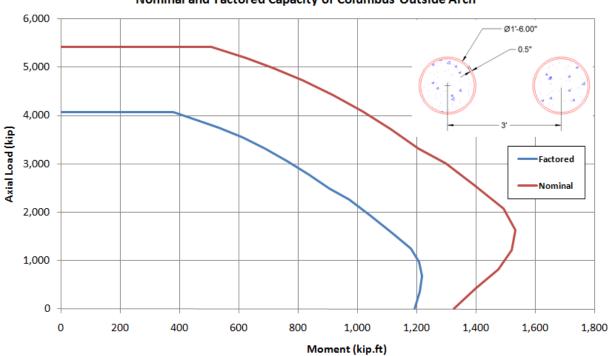
4.2 Capacity Charts

The section capacity of primary structural components of the Columbus Viaduct was determined assuming section loss percentages ranging from 0% to 50%. These percentages of section loss represent the corrosion that might occur in the steel portion of these components and, consequently reducing the thickness of structural steel and/or the diameter of prestressing strands. Reduction in the concrete dimensions and/or strength was considered negligible and was not included in these percentages. The following figures present the factored and nominal capacity charts for arch, tie, hanger, and floor beam sections respectively. These capacity charts were developed using the strain compatibility approach and the AASHTO LRFD strength reduction factors.

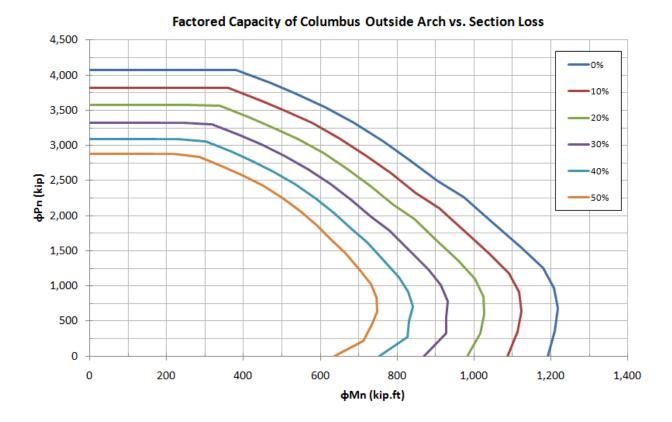


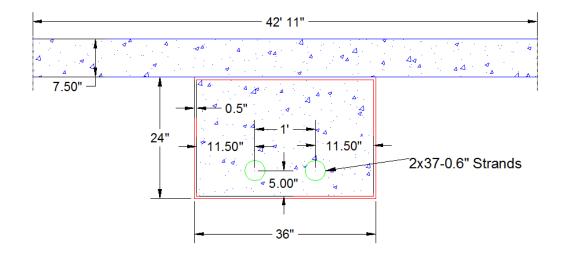
40

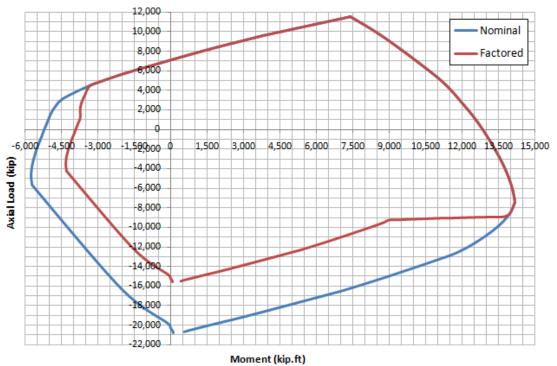




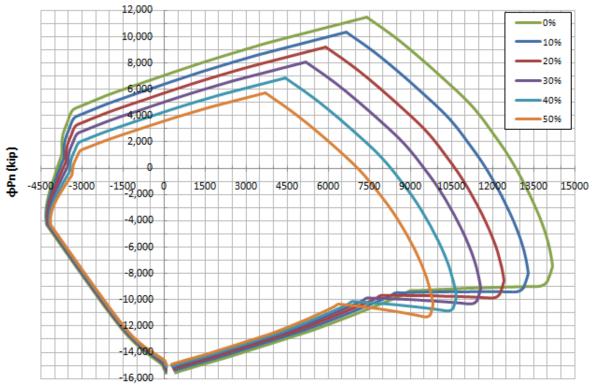
Nominal and Factored Capacity of Columbus Outside Arch





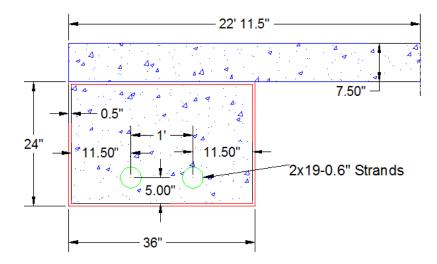


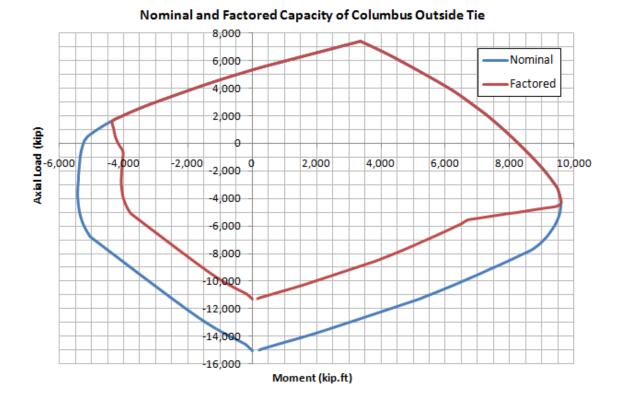
Nominal and Factored Capacity of Columbus Median Tie



Factored Capacity of Columbus Median Tie vs. Section Loss

φMn (kip.ft)

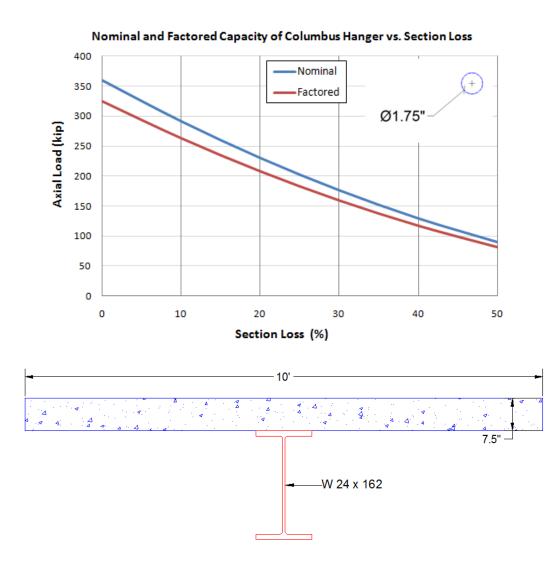


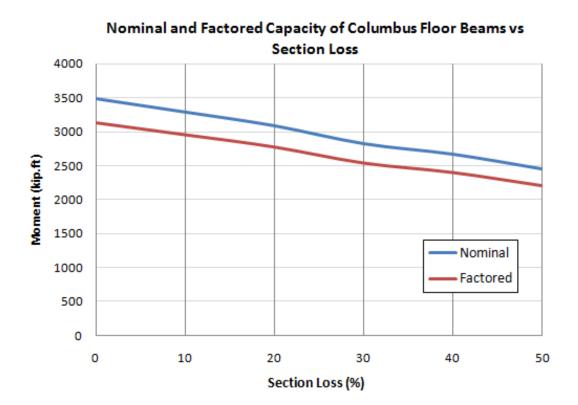


8,000 0% 6,000 10% 20% 4,000 30% 40% 2,000 50% ф<mark>Ри (kip)</mark> 0 -4,000 8,000 -2,000 -1,000 1,000 2,000 3,000 4,000 5,000 6,000 7,000 8,000 9,000 10,000 -2,000 4,000 6,000 -8,000 10,000 -12,000

Factored Capacity of Columbus Outside Ties vs. Section Loss

φMn (kip.ft)





4.3 Rating Factors

The table shown next lists the capacity of each of the primary structural component of Columbus Viaduct as well as the demand at the most critical sections based on the 3D analysis.

		10%		7000																		
M (kip.ft) P (kip) M (kip.ft)			20%	av ne	40%	50%	Q	DC	P D	DW TO	TOTAL (LL	(LL+I) _{HL-93} (I	(LL+I) _{HS20} ((LL+I) _{N3}	(LL+I) _{N3S2}	(LL+I) _{N3-3}	(LL+I) _{3-3L}	(LL+I) _{SP1}	(LL+I) _{SP2}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SPS}
P (kip) M (kip.ft)		2958	2777	2541	2402	2207	N/A	277	0 4	46 4	415 9	8.86	700.5	302.7	267.1	249.3	249.3	502.9	589.2	618.6	589.2	589.2
M (kip.ft)		263	208	159	117	81	2	109	6 1	12 1	161	35	17	12	18	20	21	14	17	19	23	37
	007/	6500	5750	5000	4250	3500	190	-298 7	750 -:	-28 3	335 2	2285	1658	1202	1460	1473	1296	1404	1691	1962	2322	3895
r (kip)	2200	2100	2000	1900	1800	1700	190	927	0	83 11	1283	277	133	92	135	155	162	185	215	243	301	477
Outside M (kip.ft) -3500	3500	-3100 -2700	2700 -	-2300 -	-1700 -	-1300	190	-298	750 -:	-28 3	335	-1658	-991	-692	-986	-1110	-1044	-1196	-1414	-1608	-1998	-3233
Tie Beams (-ve) P (kip)	2600	2400	2200	2000	1900	1800	190	927	0	83 II	1283	277	133	92	135	155	162	185	215	243	301	477
Outside M (kip.ft)	006	840	770	710	650	590	142	195	39 1	10 2	298	132	98	70	83	83	73	73	06	103	123	222
Arch Pipes P (kip)	-2500	-2500 -2400 -2250	- 2250 -	-2100 -	-1950 -	-1850	142	-926	22 -{	-83 -1	-1259	-282	-135	-94	-137	-157	-164	-188	-219	-248	-307	-486
Median M (kip.ft) 11500 10500	11500		9250	8000	6750	5500	87	-461 1	1472 -4	-49 8	822 3	3501	2556	1857	2236	2237	1977	1290	1555	1806	2127	3536
Tie Beams (+ve) P (kip)	4000	3600	3400	3200	3000	2900	87	1553	0 1	163 2:	2187	457	220	153	223	256	267	183	213	242	299	474
Median M (kip.ft) -3750 -3500 -3250	3750	-3500 -	3250 -	- 3000 -	-2250 -	-1500	87	-461 1	1472 -4	-49 8	822	-2516	-1499	-1045	-1495	-1684	-1584	-1089	-1288	-1464	-1819	-2943
Tie Beams (-ve) P (kip)	3100	3000	2900	2800	2700	2600	87	1553	0 1	163 2:	2187	457	220	153	223	256	267	183	213	242	299	474
Median M (kip.ft)	1290	1200	1100	1010	910	800	40	411	95 2	21 6	641	249	184	131	157	157	138	82	101	115	138	250
Arch Pipes P (kip)	3450	-3450 -3250 -3050	3050 -	-2800 -	2800 -2650 -2450	-2450	40 -	-1556	43 -1	-165 -2	-2148	-472	-227	-158	-231	-265	-276	-189	-220	-250	-309	-490

The capacity and demand values were used to calculate the rating factor based on the equation 6A.4.2.1-1 presented in Chapter 2. The table that follows lists the rating factor in ratios and in tons. Section loss percentage, system factor and live load factors used in the calculations are highlighted in yellow and can be easily modified in the spreadsheet as needed.

						Live L	oad Facto	rs				
System Factor	1.00	1.	75		1.	70				1.80		
Section Loss	0%	(LL+I) _{HL-93}	(LL+I) _{HS20}	(LL+I) _{N3}	(LL+I) _{N3S2}	(LL+I) _{N3-3}	(LL+I) _{3-3L}	(LL+I) _{SP1}	(LL+I) _{SP2}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SP5}
Floor beams	M (kip.ft)	1.56	2.22	5.28	5.99	6.42	6.42	3.00	2.56	2.44	2.56	2.56
Hangers	P (kip)	2.67	5.45	8.04	5.51	4.82	4.59	6.51	5.36	4.79	3.96	2.46
Outside	M (kip.ft)	1.73	2.38	3.38	2.79	2.76	3.14	2.74	2.27	1.96	1.65	0.99
Tie Beams (+ve)	P (kip)	1.89	3.95	5.85	4.00	3.49	3.33	2.75	2.37	2.10	1.69	1.07
Outside	M (kip.ft)	1.32	2.21	3.26	2.29	2.03	2.16	1.78	1.51	1.33	1.07	0.66
Tie Beams (-ve)	P (kip)	2.72	5.67	8.40	5.75	5.01	4.78	3.96	3.40	3.01	2.43	1.53
Outside	M (kip.ft)	2.60	3.51	5.06	4.27	4.27	4.85	4.58	3.72	3.25	2.72	1.51
Arch Pipes	P (kip)	2.51	5.25	7.76	5.33	4.64	4.45	3.67	3.15	2.78	2.24	1.42
Median	M (kip.ft)	1.74	2.39	3.38	2.81	2.81	3.18	4.60	3.82	3.28	2.79	1.68
Tie Beams (+ve)	P (kip)	2.26	4.71	6.97	4.77	4.16	3.99	5.50	4.73	4.16	3.37	2.13
Median	M (kip.ft)	1.04	1.74	2.57	1.80	1.60	1.70	2.33	1.97	1.73	1.40	0.86
Tie Beams (-ve)	P (kip)	1.14	2.37	3.51	2.40	2.09	2.01	2.77	2.38	2.10	1.70	1.07
Median	M (kip.ft)	1.49	2.02	2.92	2.43	2.43	2.77	4.40	3.57	3.14	2.61	1.44
Arch Pipes	P (kip)	1.58	3.28	4.85	3.31	2.89	2.77	3.83	3.29	2.89	2.34	1.48
Rating in 1	ons	80	36	25	37	43	80	50	60	70	100	150
Floor beams	M (kip.ft)	124.4	79.8	132.1	221.5	275.9	513.2	150.2	153.8	170.9	256.4	384.5
Hangers	P (kip)	213.5	196.1	200.9	203.9	207.3	367.4	325.3	321.5	335.6	396.0	369.3
Outside	M (kip.ft)	138.4	85.8	84 . 6	103.1	118.7	251.1	136.8	136.3	137.1	165.4	147.9
Tie Beams (+ve)	P (kip)	151.3	142.2	146.2	148.1	150.0	266.4	137.7	142.2	146.8	169.3	160.2
Outside	M (kip.ft)	105.7	79.6	81.6	84.6	87.4	172.9	89.1	90.4	92.8	106.6	98.9
Tie Beams (-ve)	P (kip)	217.2	204.3	209.9	212.7	215.4	382.6	197.8	204.2	210.8	243.1	230.1
Outside	M (kip.ft)	207.9	126.4	126.5	157.9	183.5	388.2	229.2	223.1	227.4	272.0	226.1
Arch Pipes	P (kip)	201.1	189.0	194.1	197.1	199.4	356.0	183.3	188.8	194.5	224.5	212.7
Median	M (kip.ft)	139.4	85.9	84.6	103.9	120.7	254.2	229.9	228.9	229.9	278.9	251.7
Tie Beams (+ve)	P (kip)	181.2	169.5	174.2	176.6	178.9	319.6	275.2	283.7	291.4	336.9	318.8
Median	M (kip.ft)	83.1	62.7	64.3	66.6	68.7	135.8	116.6	118.3	121.4	139.6	129.5
Tie Beams (-ve)	P (kip)	91.3	85.4	87.7	88.9	90.1	160.9	138.6	142.9	146.7	169.7	160.5
Median	M (kip.ft)	119.2	72.6	72.9	90.0	104.6	221.5	220.0	214.3	219.6	261.5	216.5
Arch Pipes	P (kip)	126.1	118.0	121.2	122.6	124.2	221.9	191.3	197.2	202.5	234.0	221.4

The Columbus Viaduct was also analyzed in case of one of the hangers was totally damaged. This analysis was performed in a two dimensional model by eliminating the hanger at

the location of the tie section with the highest bending moment. The next tables list the capacity and demand of each structural member as well as the calculated rating factors.

Primary Structural	ctural		Section Loss Percentages	oss Pe	rcentag	es	Elem.	i							Den	Demand						
Element	it	0%	10% 20	20% 3	30% 40	40% 50	50% ID	DC	d	DW		(LL+I) _{HL-93}	(LL+I) _{HS20}	(LL+I) _{N3}	TOTAL (LL+I) _{HL-93} (LL+I) _{HS20} (LL+I) _{N3} (LL+I) _{N352}	(LL+I) _{N3-3}	(LL+I) _{3-3L}	$ (LL+I)_{N33} \left((LL+I)_{2:91} \left[(LL+I)_{SP1} \left[(LL+I)_{SP2} \left[(LL+I)_{SP3} \left[(LL+I)_{SP3} \right] (LL+I)_{SP4} \right] \right] \right) \\ $	(LL+I) _{SP2}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SP5}
Floor beams	M (kip.ft)	3134	2958 27	2777 2	2541 24(2402 22	2207 N/A	A 277	•	46	415	998.8	700.5	302.7	267.1	249.3	249.3	502.9	589.2	618.6	589.2	589.2
Hangers	P (kip)	325	263 2	208 1	11 11	117 8	81 2	109	9	12	161	35	17	12	18	20	21	14	17	19	23	37
Outside	M (kip.ft)	6500	6000 52	5250 4	4500 375	3750 30	3000 41	-473	8698	-33	57	1998	1200	1122	1416	1429	1171	1294	1504	1779	2110	3564
Tie Beams (+ve)	P (kip)	2000	1900 18	1800 1	1700 16(1600 15	1500 41	913	0	69	1245	260	79	70	107	122	138	140	161	182	224	350
Outside	M (kip.ft) -3500	-3500	-3100 -2	2600 -2	-2200 -17	-1700 -13	-1200 41	-473	8698	-33	57	-1728	-733	-658	-978	-1101	-1021	-1147	-1339	-1520	-1877	-2986
Tie Beams (-ve)	P (kip)	2000	1900 1	1800 1	1700 16(1600 15	1500 41	913	•	69	1245	260	62	70	107	122	138	140	161	182	224	350
Outside	M (kip.ft)	-860	280	- 730	-670 -61	-610 -5	-560 6	-192	2 -20	-12	-278	-107	74 -	-40	-59	-67	-63	-70	-82	-93	-115	-182
Arch Pipes	P (kip)	-2750 -2600		2450 -2	-2300 -21	-2150 -2(-2000 6	-968	3 24	-73	-1296	-275	-83	-75	-113	-129	-146	-149	-171	-193	-237	-371
Median	M (kip.ft) 11500 10500	11500		9250 8	8000 675	6750 55	5500 41	-744	1360	-92	292	3794	2737	1979	2418	2443	2169	1304	1526	1819	2169	3714
Tie Beams (+ve)	P (kip)	4000	3600 34	3400 3	3200 300	3000 25	2900 41	1567	7 0	165	2206	401	189	131	192	221	232	147	170	194	241	383
Median	M (kip.ft)	-3750	-3500 -3	3250 -3	-3000 -22	-2250 -1	-1500 41	-744	1360	-92	292	-2873	-1690	-1178	-1690	-1907	-1799	-1171	-1379	-1572	-1956	-3149
Tie Beams (-ve)	P (kip)	3100	3000 25	2900 2	2800 270	2700 26	2600 41	1567	2 0	165	2206	401	189	131	192	221	232	147	170	194	241	383
Median	M (kip.ft) -1380 -1260	-1380		-1150 -1	-1030 -92	-920 -8	-800 6	-444	t -74	-37	-685	-331	-195	-220	-195	-220	-208	-135	-159	-181	-226	-363
Arch Pipes	P (kip)	-3170	-3020 -2	2- 068	2890 -2780 -2650	550 -2	-2470 6	-1661	1 44	-175	-2295	-425	-200	-139	-204	-234	-246	-156	-181	-206	-256	-406
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						Live L	oad Facto	ors				
System Factor	1.00	1.	75		1.	70				1.80		
Section Loss	0%	(LL+I) _{HL-93}	(LL+I) _{HS20}	(LL+I) _{N3}	(LL+I) _{N3S2}	(LL+I) _{N3-3}	(LL+I) _{3-3L}	(LL+I) _{SP1}	(LL+I) _{SP2}	(LL+I) _{SP3}	(LL+I) _{SP4}	(LL+I) _{SP5}
Floor beams	M (kip.ft)	1.56	2.22	5.28	5.99	6.42	6.42	3.00	2.56	2.44	2.56	2.56
Hangers	P (kip)	2.67	5.45	8.04	5.51	4.82	4.59	6.51	5.36	4.79	3.96	2.46
Outside	M (kip.ft)	1.84	3.07	3.38	2.68	2.65	3.24	2.77	2.38	2.01	1.70	1.00
Tie Beams (+ve)	P (kip)	1.66	5.46	6.35	4.15	3.64	3.22	3.00	2.61	2.31	1.87	1.20
Outside	M (kip.ft)	1.18	2.77	3.18	2.14	1.90	2.05	1.72	1.48	1.30	1.05	0.66
Tie Beams (-ve)	P (kip)	1.66	5.46	6.35	4.15	3.64	3.22	3.00	2.61	2.31	1.87	1.20
Outside	M (kip.ft)	3.11	7.56	8.56	5.80	5.11	5.43	4.62	3.94	3.48	2.81	1.78
Arch Pipes	P (kip)	3.02	10.01	11.41	7.57	6.63	5.86	5.42	4.73	4.19	3.41	2.18
Median	M (kip.ft)	1.69	2.34	3.33	2.73	2.70	3.04	4.78	4.08	3.42	2.87	1.68
Tie Beams (+ve)	P (kip)	2.56	5.42	8.05	5.50	4.77	4.55	6.78	5.86	5.14	4.13	2.60
Median	M (kip.ft)	0.80	1.37	2.02	1.41	1.25	1.32	1.92	1.63	1.43	1.15	0.71
Tie Beams (-ve)	P (kip)	1.27	2.70	4.01	2.74	2.38	2.27	3.38	2.92	2.56	2.06	1.30
Median	M (kip.ft)	1.20	2.04	1.86	2.10	1.86	1.97	2.86	2.43	2.13	1.71	1.06
Arch Pipes	P (kip)	1.18	2.50	3.70	2.52	2.20	2.09	3.12	2.69	2.36	1.90	1.20
Rating in T	ons	80	36	25	37	43	80	50	60	70	100	150
Floor beams	M (kip.ft)	124.4	79.8	132.1	221.5	275.9	513.2	150.2	153.8	170.9	256.4	384.5
Hangers	P (kip)	213.5	196.1	200.9	203.9	207.3	367.4	325.3	321.5	335.6	396.0	369.3
Outside	M (kip.ft)	147.4	110.4	84.4	99.0	114.0	258.9	138.3	142.8	140.8	169.6	150.6
Tie Beams (+ve)	P (kip)	132.8	196.7	158.7	153.6	156.6	257.5	149.9	156.4	161.4	187.3	179.8
Outside	M (kip.ft)	94.1	99.8	79.5	79.2	81.7	164.0	86.1	88.6	91.0	105.3	99.3
Tie Beams (-ve)	P (kip)	132.8	196.7	158.7	153.6	156.6	257.5	149.9	156.4	161.4	187.3	179.8
Outside	M (kip.ft)	248.7	272.1	214.0	214.7	219.7	434.7	231.0	236.6	243.4	281.2	266.5
Arch Pipes	P (kip)	241.8	360.5	285.2	280.1	285.2	468.8	271.2	283.5	293.1	341.0	326.7
Median	M (kip.ft)	135.0	84.2	83.3	100.9	116.0	243.2	238.8	244.8	239.6	287.1	251.5
Tie Beams (+ve)	P (kip)	204.5	195.2	201.4	203.3	205.3	363.8	339.0	351.7	359.6	413.5	390.3
Median	M (kip.ft)	64.3	49.2	50.5	52.1	53.6	105.7	95.9	97.7	100.0	114.8	107.0
Tie Beams (-ve)	P (kip)	101.9	97.3	100.3	101.3	102.3	181.3	168.9	175.2	179.2	206.0	194.5
Median	M (kip.ft)	96.1	73.4	46.5	77.6	80.0	157.4	143.1	145.8	149.4	171.0	159.7
Arch Pipes	P (kip)	94.1	90.0	92.6	93.4	94.6	167.4	155.8	161.2	165.2	189.9	179.6

Chapter 5 Conclusions

Based on the analysis results of Ravenna and Columbus Viaducts, and the calculation of rating factors according to the 2008 AASHTO Manual for Bridge Evaluation, the following conclusions are made:

- The primary structural components of Ravenna Viaduct (i.e. arches, ties, hangers, and floor beams) have RF > 1 under all design loads, legal loads, and permit loads using load factors of 1.75, 1.45, and 1.6 respectively, and assuming a system factor of 1.0 and section loss of 0%.
- In an extreme event that results in a complete damage of one hanger in Ravenna Viaduct, the RF of the arch will be less than 1 and the bridge need to be closed or posted until the damaged hanger is replaced.
- The primary structural components of Columbus Viaduct (i.e. arches, ties, hangers, and floor beams) have RFs > 1 under all design loads, legal loads, and permit loads except P5 using load factors of 1.75, 1.7, and 1.8 respectively, and assuming a system factor of 1.0 and section loss of 0%.
- In an extreme event that results in a complete damage of one hanger in Columbus Viaduct, the RF of the median tie under design load will be less than 1 and the bridge need to be closed or posted until the damaged hanger is replaced. It should be noted that RFs will remain greater than 1 in case of a complete damage of one hanger in the outside arch.

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