



Lang, B., Beggs, D. M., Young, A. B., Rarity, J., & Oulton, R. (2015). Stability of polarization singularities in disordered photonic crystal waveguides. Physical Review A, 92, [063819]. 10.1103/PhysRevA.92.063819

Publisher's PDF, also known as Final Published Version

Link to published version (if available): 10.1103/PhysRevA.92.063819

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Stability of polarization singularities in disordered photonic crystal waveguides

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(Received 1) August 2013, Tevised manuscript received 27 October 2015, published 11 December 2015)

The effects of short-range disorder on the polarization characteristics of light in photonic crystal waveguides were investigated using finite-difference time-domain simulations with a view to investigating the stability of polarization singularities. It was found that points of local circular polarization (C points) and contours of linear polarization (L lines) continued to appear even in the presence of high levels of disorder, and that they remained close to their positions in the ordered crystal. These results are a promising indication that devices exploiting polarization in these structures are viable given current fabrication standards.

DOI: 10.1103/PhysRevA.92.063819

PACS number(s): 42.25.Ja, 42.70.Qs, 42.50.Tx

I. INTRODUCTION

A polarization singularity occurs at a position in a vector field where one of the parameters describing the local polarization ellipse (handedness, eccentricity, or orientation) becomes singular [1]. With the vector nature of electromagnetic fields, optics is an obvious place for the study and application of polarization singularities, and they can be found in systems ranging from tightly focused beams [2] to speckle fields [3,4] to photonic crystals [5] and others [6-8]. For example, at circular polarization points, the orientation of the polarization ellipse is singular, whereas along contours of linear polarization the handedness is singular. The former are called C points and the latter L lines. Recently, the use of polarization singularities for quantum information applications is generating much interest, as they can couple the spin states of electrons confined to quantum dots to the optical modes of a waveguide [9]. For example, at a circular point (C point), the sign of the local helicity or polarization is governed by the propagation direction of the optical mode, which allows spin-photon coupling to one direction only, sometimes referred to as the "chiral waveguide" effect [10-15].

A photonic crystal (PhC) is a periodic modulation of the refractive index, typically provided by etching holes in a transparent membrane, such as a semiconductor above its band edge. PhC waveguides (PhCWGs) are strong candidates for finding applications for polarization singularities. As Bloch waves, the eigenmodes of PhCWGs possess a strong longitudinal, as well as transverse, component of their electric field profile. The spatial dependence of both these components and the phase between them ensures a rich and complex polarization landscape in the vicinity of the waveguide, and leads to the occurrence of polarization singularities [5,16,17]. However, any real system will inevitably contain imperfections that deviate away from this perfectly periodic pattern; for example, the hole size and position can vary, or etching can cause surface roughness. To be useful in applications, the polarization structure should be robust to such real-world disorder. To this end, studies of how disorder affects the complex polarization structure and existence of polarization singularities are needed.

In this work, we use calculations of the eigenmodes of disordered PhCWGs to demonstrate that the polarization singularities (C points and L lines) present in the ideal waveguide persist far beyond realistically expected levels of disorder. By calculating the positions of these C points and L lines for a statistical ensemble of disordered waveguides, we demonstrate that not only do they persist, but also their mean positions are close to those predicted for the ideal structure.

II. METHODS

Our PhCWG [shown in Fig. 1(a)] is a single row of missing air holes from a hexagonal lattice of holes spaced a apart and with a diameter of d = 0.48a in a dielectric slab with refractive index n = 3.54 and thickness h = 0.56a. The lattice constant a can be chosen freely for different operating regimes, but with a = 250 nm these values are suitable for a PhCWG in a GaAs membrane embedded with quantum dots emitting at 900 nm. We chose to work with a mode located at $ka/2\pi = 0.35$ with a eigenfrequency of $\omega a/2\pi c = 0.255$ and group velocity $v_g = c/7$. We chose this mode because it possesses a significant number of C points in the vicinity of the waveguide core, making it well suited to collecting statistics when disorder is introduced. Also the relatively modest slow-down factor ensures that the disorder localization length remains longer than our waveguide supercell length, even for the largest disorder considered, ensuring that we remain in the ballistic photon transport regime and avoid complications caused by the formation of localized states in the disordered waveguides [18,19]. The eigenmodes are calculated using a finite-difference time-domain (FDTD) method [20] with a grid resolution of a/24 and periodic boundary conditions in the direction of the waveguide (absorbing boundaries on all other edges). In the course of the simulation a large number of modes are excited by dipole sources placed in the waveguide, but letting the simulation evolve in time causes most of these modes to decay such that the remaining power is in the waveguide's eigenmode $\mathbf{E}(\mathbf{r})$, as shown in Fig. 1(b).

After finding the eigenmodes $\mathbf{E}(\mathbf{r})$, the polarization structure in the vicinity of the waveguide is examined by calculating the four Stokes parameters, $S_{0,1,2,3}$, as a function of position **r**. Together, the Stokes parameters completely specify the polarization of the electric field on the Poincaré

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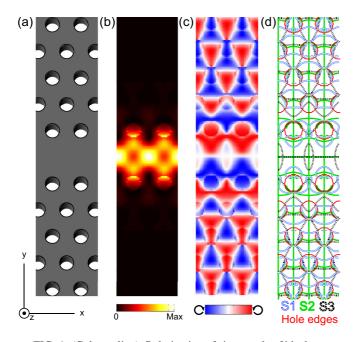


FIG. 1. (Color online) Polarization of eigenmode of ideal waveguide. (a) Schematic of PhCWG, showing gallium arsenide membrane (n = 3.54) etched with air holes. (b) Eigenmode of ideal waveguide $|E|^2$. (c) S_3 , the extent to which the light is circularly polarized. (d) Zero contours of the Stokes parameters $S_{1,2,3}$ shown by lines of the indicated types. This figure and all others in this paper show the fields at z = 0 (center of the slab).

sphere [21]:

$$S_{0}(\mathbf{r}) = |E_{x}(\mathbf{r})|^{2} + |E_{y}(\mathbf{r})|^{2},$$

$$S_{1}(\mathbf{r}) = (|E_{x}(\mathbf{r})|^{2} - |E_{y}(\mathbf{r})|^{2})/S_{0}(\mathbf{r}),$$

$$S_{2}(\mathbf{r}) = 2\operatorname{Re}[E_{x}^{*}(\mathbf{r})E_{y}(\mathbf{r})]/S_{0}(\mathbf{r}),$$

$$S_{3}(\mathbf{r}) = 2\operatorname{Im}[E_{x}^{*}(\mathbf{r})E_{y}(\mathbf{r})]/S_{0}(\mathbf{r}).$$
(1)

 S_0 specifies the total electric field strength, $|\mathbf{E}|^2$, and $-1 \leq$ $S_{1,2,3} \leq 1$ are the positions on the Poincaré sphere. Figure 1(b) shows the calculated value of S_0 in the central plane (z = 0) of the membrane for the ideal photonic crystal waveguide, and Figure 1(c) shows the value of S_3 . S_3 is of particular interest to us, because it measures the extent of circular polarization in the electric field profile. Positions where $S_3 = \pm 1$ are C points with fully left and right circularly polarized fields, whereas contours where $S_3 = 0$ are L lines with linear polarization. S_1 and S_2 indicate the degree of linear polarization in the rectilinear and diagonal basis; specifically the values of ± 1 in S_1 denote vertical and horizontal polarization, while in S_2 they denote diagonal and antidiagonal polarization. Figure 1(d) shows the contours of $S_{1,2,3} = 0$ for our PhCWG, with piped, solid, and dashed lines, respectively. The $S_3 = 0$ contour marks the L lines, whereas the C points are marked by the crossing of the $S_1 = 0$ and $S_2 = 0$ contours (so points where $S_1 = S_2 = 0$), which coincide with positions where $S_3 = \pm 1$ [see Fig. 2(b)] [22].

III. DISORDER RESULTS

We now consider the effect of disorder on the Stokes parameters. All disorder and imperfections in the waveguide are modeled as random shifts in the positions of the holes, with each hole displaced a small distance selected from a normal distribution with a mean of zero and a standard deviation of $a\delta$ in a random direction θ (selected from a uniform distribution $0 \leq \theta < \pi$). The parameter δ therefore characterizes the level of disorder in the simulation. Although this model may not realistically represent all of the errors that occur in a typical fabrication process (it ignores the ellipticity, hole-size variation, side-wall roughness, and angle), the displacement of the holes can be exaggerated in order to crudely account for these effects, and similar models of disorder are widely used [19,23–27]. Each simulation of a disordered waveguide used a supercell of dimensions $15a \times 24a \times 5a$, containing 15 unit cells along the direction of the waveguide. This length of 15 unit cells was chosen by checking that it is longer than the distance over which individual cells are significantly correlated with their neighbors, while being significantly shorter than the disorder localization length (see discussion in the Supplemental Material [28]). An example of part of a disordered supercell is illustrated in Figure 2(a).

As described above, the position of the *C* points are found in the eigenmodes of the disordered waveguides by examining where the zero contours of S_1 and S_2 cross, which is equivalent to finding positions where $S_3 = \pm 1$. Figure 2(b) shows the position of the *C* points in one half of the unit cell of the ideal structure, in the vicinity of the hole closest to the waveguide. The contours of $S_{1,2,3} = 0$ are shown by piped, solid, and dashed lines, respectively, and the *C* points are shown by the large dots. The *L* lines are located simply by the contours where $S_3 = 0$ (dashed lines). Figure 2(c) shows the response of the polarization landscape to the introduction of disorder in the waveguide. The top panel shows the ideal case ($\delta = 0$), the middle shows $\delta = 0.03$, and the bottom $\delta = 0.09$.

The most obvious feature apparent in Fig. 2(c) is that the zero contours of the the Stokes parameters $S_{1,2,3}$ lose all sense of the symmetries present in the ideal structure. In particular, the *L* lines ($S_3 = 0$) lose the crossings seen in the core of the ideal waveguide, even for small disorder. However, despite the apparent lack of order in Fig. 2(c), a more through analysis reveals that the polarization singularities are remarkably robust to disorder.

Although not shown by Fig. 2(c) the number of points where the zero contours of each Stokes parameter crosses itself falls rapidly with the introduction of disorder. Self-crossings of this type imply the existence of two regions in which the Stokes parameter takes positive values and two where it takes negative ones meeting at a corner in a "chess board" like arrangement. In principle even the smallest amount of disorder will be sufficient to disturb this arrangement, creating a bridge connecting either the positive regions or the negative ones [1,29]. We find that these points disappear extremely rapidly with the introduction of disorder, and believe that the surviving cases can be attributed to the finite resolution of the simulations.

Figure 3 shows a summary of the main findings of this work. The top row considers the C points. Each panel in the

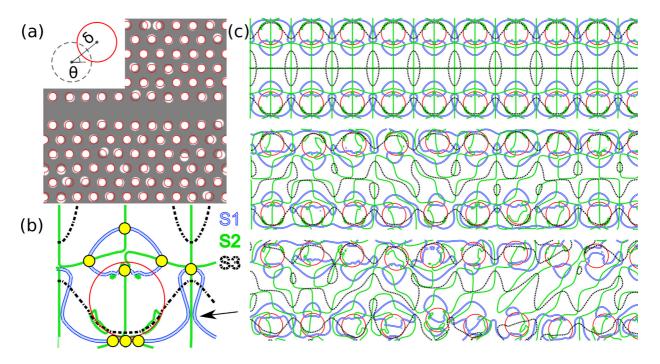


FIG. 2. (Color online) Effect of disorder on Stokes parameters. (a) Schematic of the disorder, the positions of the air holes in the ideal waveguide are shown in with lines, with a specific instance of a disordered crystal shaded in grey. Inset: the disorder model for an individual hole. (b) The zero contours of $S_{1,2,3}$ are shown with piped, solid and dashed lines, respectively. The large circle denotes an air hole. *C* points are marked with circles and *L* lines by dashed lines. (c) More zero contours (same symbols), this time for supercells in three specific simulation runs with $\delta = 0, 0.03, \text{ and } 0.09$.

top row marks with a gray dot the calculated positions of C points found in each unit cell after 32 calculations performed with an independent realization of the disordered structure for

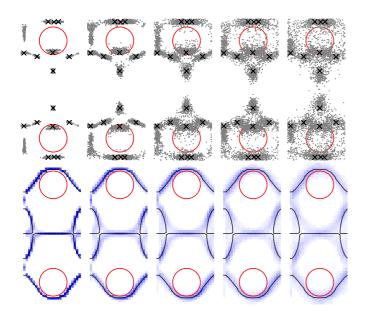


FIG. 3. (Color online) Top: the locations of *C* points. Each panel shows all the *C* points found for a particular choice of δ folded into a single unit cell (using data from 32 separate simulations). Crosses: locations of the *C* points with no disorder. Bottom: probability density of *L* lines. Black lines: locations of the *L* lines with no disorder. The circles (in both sets of panels) show the positions of the air holes (without disorder).

the values of the disorder parameter $\delta = 0.01, 0.03, 0.05, 0.07$, and 0.09. The crosses mark the positions of the *C* points in the ideal structure. The bottom row considers the *L* lines. Each panel in the bottom row shows the location of the *L* lines in the same disordered waveguides. Specifically the probability of finding an *L* line crossing a pixel in the calculation grid is plotted using a color scale of white (zero probability) to dark blue (high probability). The *L* lines in the ideal waveguide are shown by black lines.

First, it is clear that the existence of polarization singularities is largely robust to the addition of disorder. A few C points are eliminated, but the majority survive in displaced locations (see below). For the smallest levels of disorder, the C points and L lines cluster very closely to their positions in the ordered waveguide, but they gradually move away with increasing disorder. For $\delta = 0.01$, the C points move a mean distance of just 0.06a away from their positions in the ideal case, and the L line just 0.04a, although these distances steadily increase with disorder, as shown in Fig. 4(b).

As well as the elimination and displacement of *C* points, the addition of disorder also causes their creation. Such *C* points are apparent in Fig. 3, where clusters of *C* points form that are not associated with any from the ideal waveguide (bottom-left and top-left of each panel). In the ideal structure near these locations, there exist regions where the the ellipticity is high (>0.9), despite a *C* point not being formed. The zero contours of S_1 and S_2 come very close to crossing in the ideal waveguide [indicated by the arrow in Fig. 2(b)], and when disorder is introduced, these contours move and can sometimes cross and thus form extra *C* points. In fact, for the smallest levels of disorder considered ($\delta < 0.02$), there are on average more *C*

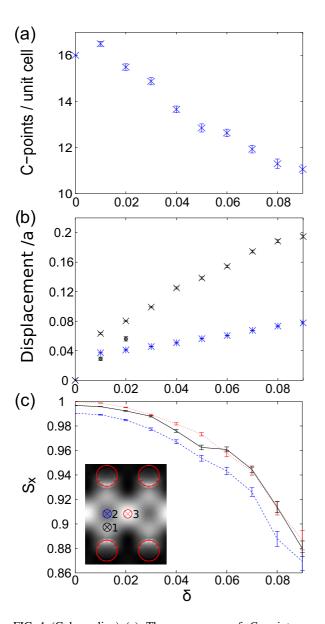


FIG. 4. (Color online) (a) The occurrence of C points as a function of disorder. (b) Crosses (stars): mean distance of C points (L line vertices) in simulations of disordered structures from the nearest C point (L line) in a simulation of the ideal structure. Circles: mean displacement of C points when newly created C points are ignored. (c) The change in polarization with disorder is plotted for three points, one of right circular polarization (1) and two of transverse linear polarization (2, 3), for each the relevant Stokes parameter is plotted (3, 1, 1, respectively). Note that they do not begin at exactly 1; this is a result of finite resolution. The inset shows the locations of points 1, 2, and 3 relative to the air holes.

points found in the disordered waveguides than in the ideal one. However, for $\delta > 0.02$, the number of *C* points found per unit cell falls slowly with increasing disorder, until for the highest levels of disorder considered, a mean of 11.1 ± 0.3 from the original 16 per unit cell remain. Figure 4(a) shows a plot of the mean number of *C* points found per unit cell as a function of the disorder parameter δ .

The creation of these new C points increases the average separation between the C points in disordered structures and

those in the ideal structure. The two circles in Fig. 4(b) show the mean displacement of *C* points when the new *C* points are excluded.

To further examine the effects of disorder on the polarization singularities, we plot the mean values of the Stokes parameters at several key positions in the waveguide. These positions are at a *C* point and on an *L* line, and are shown in detail by the inset in Fig. 4(c). The first point (labeled "1") is located at a *C* point in the ideal structure, near the center of the waveguide. Figure 4(c) shows the mean value of S_3 averaged over all unit cells in all simulations as a function of the disorder parameter δ at this position. Being at a (right-handed) *C* point means that the value in the ideal waveguide is $S_3 = 1$, but this reduces as disorder is introduced and the *C* point is displaced or destroyed.

Also shown are two points (labeled "2" and "3") that are both located on an *L* line in the center of the waveguide. Both these points have $S_1 = 1$ and $S_3 = 0$ in the ideal waveguide, and the mean value of S_1 averaged over the disordered structures are shown in Fig. 4(c) as a function of δ . Again, as disorder is introduced, the mean value of S_1 deceases, slowly at first, but then faster for higher disorders. The pattern is very similar to that of the value of the ellipticity S_3 at the *C* point. Using the value of S_1 as a proxy for the "amount of *L*-line-ness" at the points considered, it can thus be said that the *L* lines and *C* points display remarkably similar robustness to the introduction of disorder.

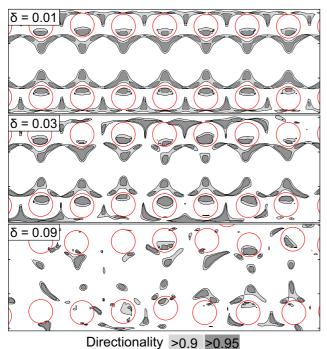
Taking Figs. 3 and 4 as a whole, we conclude that the existence of C points and L lines are remarkably robust to disorder in the waveguide, and their positions in the disordered waveguides are on average very close to the positions in the ideal waveguide.

Our analysis so far has concentrated on the extremal points of polarization (i.e., the *C* points and *L* lines). However, many applications may only require a large degree of polarization to be viable. For example, while *C* points with $S_3 = \pm 1$ are strictly the only locations in the waveguide where a circular dipole will emit light in only one direction (unit directionality), regions possessing a high value of ellipticity $|S_3|$ will emit predominantly in one direction, as the directionality is equal to the ellipticity. Figure 4(c) shows the decay of the ellipticity or directionality at the position of the *C* point nearest to the center of the waveguide, and from it we note that disorder parameters of $\delta \leq 0.085$ possess a mean directionality of greater than 90% at this position, and $\delta \leq 0.065$ a mean directionality of greater than 95%.

Figure 5 shows the regions where a circular dipole emitter embedded in the waveguide would possess a high directionality for a particular instance of a disordered waveguide; directionality above 0.9 in the lightly shaded regions and above 0.95 in the darker ones. It can be seen that moderate disorder ($\delta \le 0.03$, middle panel) does not greatly impact these regions, but that very high disorder ($\delta = 0.09$, bottom panel) has a large detrimental impact.

IV. CONCLUSION

We have shown that polarization singularities in photonic crystal waveguides are remarkably robust to disorder in the waveguide, at least for this choice of mode. Using comparisons



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FIG. 5. (Color online) Regions of high directionality (\equiv ellipticity) for three specific instances of disorder. Circles show the locations of the air holes.

between experiment and calculations made with a disorder model similar to ours in Ref. [30], we estimate that real photonic crystal waveguides display a level of disorder equivalent to $\delta = 0.003$, more than 3 times smaller than the lowest disorder considered in this paper (note that the comparison used a InGaAsP photonic crystal with a hole

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spacing of a = 400 nm for wavelengths around 1550 nm). Waveguide modes with smaller group velocities may be less robust than the mode studied here (with $v_o = c/7$), but our calculations suggest that even in the case of modes that are an order of magnitude more sensitive to disorder there will still be usable polarization singularities. One proposal is to place a quantum dot at a C point, where the electron spin will be coupled with the path information in the waveguide, useful in quantum information applications. For a quantum emitter placed at the C point closest to the waveguide core, we find that the emission directionality is 99.6% \pm 0.3% for a disorder of $\delta = 0.01$. Given that site-control placement of quantum dots can be achieved with 50 nm accuracy [31], our results indicate that a fabrication yield of 54% can be expected for emission directionality >90%, a number almost independent of the disorder parameter (for small δ). For comparison of quantum dots grown randomly in the waveguide vicinity, 21% can be expected to have an emission directionality >90% (dropping only to 20% for small δ). The route to higher yields is to improve the quantum dot placement rather than the disorder in the PhCWG. By outlining the tolerances to disorder, our results are an important step in realizing spin-to-path behavior in PhCWGs using current fabrication technologies.

ACKNOWLEDGMENTS

This work has been funded by the project SPANGL4Q, under FET-Open Grant No. FP7-284743. R.O. was sponsored by the EPSRC under Grant No. EP/G004366/1, and J.G.R. is sponsored under ERC Grant No. 247462 QUOWSS. D.M.B. acknowledges support from a Marie Curie Individual Fellowship QUIPS. This work was carried out using the computational facilities of the Advanced Computing Research Centre, University of Bristol.

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