

Empirical Mode Decomposition (EMD) Based Denoising Method for Heart Sound Signal and Its Performance Analysis

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ABSTRACT

In this paper, a denoising method for heart sound signal based on empirical mode decomposition (EMD) is proposed. To evaluate the performance of the proposed method, extensive simulations are performed using synthetic normal and abnormal heart sound data corrupted with white, colored, exponential and alpha-stable noise under different SNR input values. The performance is evaluated in terms of signal-to-noise ratio (SNR), root mean square error (RMSE), and percent root mean square difference (PRD), and compared with wavelet transform (WT) and total variation (TV) denoising methods. The simulation results show that the proposed method outperforms two other methods in removing three types of noises.

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1. INTRODUCTION

Cardiovascular disease (CVD) has long been the leading cause of death throughout the world with an estimate of 17.3 million people died in 2008 and is predicted to reach 23.3 million in 2030 [1]. According to WHO report, more than three quarters of the death takes place in low- and middle-income countries [2]. A low-cost and non-invasive diagnosis system based on heart sound can be used to minimize the risk of patients going into severe condition and reduce the financial burden through an early accurate diagnosis followed by appropriate treatment. This electronic auscultation technique utilizes advanced signal processing with fast computation capability, thanks to the advancement of computer technology.

However, to produce an accurate diagnosis result is not an easy task since, in practice, heart sound signal is always contaminated with noise and interference from various sources such as background noise, power interference, breathing or lung sounds, and skin movements in the surrounding environment. Thus, signal denoising method is of paramount importance to remove all these unwanted noise. A poor signal denoising method can lead to catastrophic result.

The most widely used method for denoising heart sound signal is based on wavelet transform (WT) [3–5], a powerful signal analysis tool with the ability to represent a signal simultaneously in the time and frequency. Despite the fact that the wavelet based denoising method has been proven to be able to provide good denoising performance, however, it suffers from several limitations. It requires predefined basis function selection (from too many choices) suited to signal under consideration, which limits the flexibility of the method. In addition, the decomposition level and thresholding technique of wavelet denoising also need to be carefully considered. Failing to choose the right decomposition level and thresholding technique will result in bad denoising performance. Varghees and Ramachandran employed another alternative method based on Total Variation (TV) [6]. TV method has been mostly used for image denoising due to its great benefit of preserving and enhancing important features such as edge in images. Even though it can be used for denoising 1D signal, nevertheless, there are very few literatures exploiting TV method for denoising heart sound. The highly non-stationary property of heart sound signal is not suitable to the nature of TV method which performs best on piecewise constant signals [7]. In addition, Figueiredo et. al. mentioned that the performance of TV

method could produce better result than older wavelet based methods, but it was outperformed by recent state-the-art wavelet based methods [8].

Empirical mode decomposition (EMD), a relatively new non-linear and non-stationary signal analysis method [9], offers interesting feature of adaptive and data-driven decomposition capability. Since its inception, EMD has attracted many researchers around the globe to utilize it as denoising method [10–12]. However, the mechanism of discriminating the noise and useful information within decomposed signal and fitting it to heart sound signal to get good signal reconstruction performance remains challenging.

In this paper, we propose an EMD based denoising method for heart sound signals. To measure the performance of our proposed method, we perform repeated simulation over normal and abnormal synthetic heart sound signal burried under different types of noise with SNR input values ranging from 0 to 15 dB. The qualitative evaluation is performed by visual inspection while quantitative evaluation is carried out by using three standard metrics: signal-to-noise ratio (SNR), root mean square error (RMSE), and percent root mean square difference (PRD).

The rest of this paper is organized as follows. Section 2. describes EMD denoising method with brief introduction to its theoretical background and mathematical notation. Section 3. explains the imulation setting and data. The simulation results and performance analysis of both qualitative and quantitative are given in Section 4. Finally the conclusion is drawn in Section 5.

2. EMD DENOISING METHOD

2.1. Empirical Mode Decomposition (EMD)

Empirical mode decomposition (EMD), since firstly proposed by Huang in 1998 [9], has gained popularity as data analysis method especially for non-stationary and non-linear signals such as biomedical (including heart sound) signals. EMD, in contrast to other methods such wavelets and fourier which require predefined basis function, is fully data-driven method that does not require any *a priori* known basis. EMD adaptively decomposes a signal into a series of simple oscillatory AM-FM components called as intrinsic mode functions (IMFs) through iterative procedure (known as *sifting*). An IMF is defined as a function that satisfies two conditions: the number of extrema (maxima and minima) and zero crossing must be equal or differ by at most 1; and the average value of the envelopes derived from local maxima and minima is (approximately) zero.

Despite EMD still being lack of a solid mathematical foundation which could be used for theoretical analysis and performance evaluation, it has been proven to provide interesting and useful results. The sifting procedure of EMD for decomposing the signal $x(n)$ into IMFs is systematically described as follows:

1. Specify all the local extrema (maxima and minima) of $x(n)$
2. Interpolate between local maxima using cubic spline line to form upper envelope $e_{max}(n)$ and local minima to form lower envelope $e_{min}(n)$
3. Calculate the local mean based on formed upper and lower envelopes, $m(n) = (e_{max}(n) + e_{min}(n))/2$
4. Substract this mean from the original signal to extract the detail $d(n) = x(n) - m(n)$. If $d(n)$ does not satisfy IMF conditions (stopping criteria), the procedure 1) to 4) are iterated with new input signal $d(n)$
5. If $d(n)$ satisfies the criteria of an IMF, it is stored as an IMF, $h^i(n) = d(n)$ where i refers to i th IMF. Residue signal is obtained by substracting the IMF from the original signal, $r(n) = x(n) - h^i(n)$
6. Perform the same step from 1) with the new signal $r(n)$ until the final residue signal is constant or monotonic function.

After the completion of EMD process, the original signal can be written in terms of its IMF and residue signal as follows:

$$x(n) = \sum_{i=1}^{L-1} h^i(n) + r^L(n) \quad (1)$$

where L refers to decomposition level and i denotes IMF order. Lower-order of IMFs contains fast oscillation modes (high frequency) while higher-order of IMFs represent slow oscillation modes (low frequency).

2.2. EMD Denoising

EMD, whose decomposition is based on elementary substractions, enables perfect reconstruction of a signal. The EMD denoising method starts by identifying which IMFs carry dominantly noise and which IMFs contain primarily useful information. This is done by comparing the actual energy density with the estimated energy density (to

form noise-only model [10]) of IMFs. The actual energy density of IMFs is calculated as follows

$$E_i = \frac{1}{N} \sum_{n=1}^N h^i(n), \quad i = 1, 2, 3, \dots, L \quad (2)$$

with i corresponds to IMF order. The estimated energy density (variance) of IMFs can be approximated using the formula [13] below

$$V_1 = \left(\frac{\text{median}(|h^1 - \text{median}(h^1)|)}{0.6745} \right)^2 \quad (3)$$

$$V_i = \frac{V_1}{\beta} \rho^{-j}, \quad i = 2, 3, 4, \dots, L \quad (4)$$

where β and ρ equal to 0.719 and 2.01, respectively [10]. The IMFs whose actual energy density exceed the value of their estimated energy density defined by noise-only model are categorized as information-dominated signal and should be included in signal reconstruction step; otherwise those IMFs will be excluded.

Due to the fact that the noise embedded in IMFs is colored (not Gaussian distributed), even the information-dominated IMFs still may contain noise having different energy density. To remove those colored noise, IMF-dependent threshold value is required. Considering that IMFs have zero mean and in any interval of zero crossing $[z_j^i, z_{j+1}^i]$ the absolute amplitude of i th IMF is very small, the thresholding scheme will be based on the single extrema $h^i(r_j^i)$, where r_j^i corresponds to the extrema's time instance on this interval. The thresholding scheme which follows the hard thresholding is expressed as follows

$$\tilde{h}^i([z_j^i, z_{j+1}^i]) = \begin{cases} h^i([z_j^i, z_{j+1}^i]), & |h^i(r_j^i)| > T_i \\ 0 & |h^i(r_j^i)| \leq T_i \end{cases} \quad (5)$$

where $h^i([z_j^i, z_{j+1}^i])$ represents the samples from time instant z_j^i to z_{j+1}^i of i th IMF. The threshold value used in this scheme is expressed below

$$T_i = C\sqrt{V_i 2 \ln N}, \quad i = 1, 2, 3, \dots, L \quad (6)$$

where C is 0.1 found by empirical simulations and V_i is estimated energy density (variance) of i th IMF. This thresholding scheme which is inspired and adapted from wavelet [11] will set to zero all the samples from time instant $[z_j^i, z_{j+1}^i]$ if the single extrema amplitude below the threshold value meaning that there is no useful information (only noise) in the specified time instant. Otherwise, all the samples will be retained.

The final signal reconstruction can be obtained by summing up all the included IMFs (whose actual energy density exceeding its estimated energy as described previously) using the following formula

$$\hat{y} = \sum_{i=p}^q \tilde{h}^i(n) \quad (7)$$

where p and q indicates the lowest and highest index of included IMF.

3. SIMULATION SETTING

To evaluate the qualitative and quantitative performance of our proposed method, we performed repeated simulations using synthetic heart sound data obtained from University of Michigan's Heart Sound & Murmur Library [14]. In this simulations, three types of heart sound signals used for simulations and their respective recording location are 'Normal S1 S2' (Apex, Supine, Bell), 'S3 Gallop' (Apex, Left Ducubitus, Bell) and 'S4 Gallop' (Apex, Left Ducubitus, Bell). These data are encoded in 44,100 Hz sample rate, 16 bits/sample, and 1 minutes of data length. The data was then down-sampled into 2000 Hz to increase the computation process without violating Nyquist theorem, since the frequency content of heart sound data is maximum at around 700 Hz. The simulations were carried out 100 times in each case using MATLAB 2015a which runs on Intel(R) Core(TM) i7-4790 CPU @3.6 GHz Windows 7 environment. To measure the performance under various noises, we added four types of noises, which are white, colored (brown), exponential and alpha-stable noise to the clean input signal $y(n)$ to form noisy signal $x(n)$. In each noise case, we used different input SNR level of 0, 5, 10, and 15 dB. The noisy heart sound signal, $x(n)$, is expressed as

$$x(n) = y(n) + e(n), \quad n = 0, 1, 2, \dots, N - 1 \quad (8)$$

where $y(n)$ and $e(n)$ denotes the clean signal and noise, respectively.

For the purpose of performance benchmark, we also performed simulations over the same data using Wavelet Transform (WT) and Total Variation (TV) based denoising methods. In WT based simulation, Daubechies db10 wavelet function was used since it highly resembles the heart sound signal, which lead to yield better performance. In addition, db10 wavelet has orthogonal property which enables perfect reconstruction of signal and have been reported to produce best result among others [3]. The decomposition level, $N = 5$, is chosen as recommended in [4]. Hard thresholding technique is selected as it provides better result compared to soft thresholding technique. MATLAB has built-in function `wden` for wavelet denoising as described in [15]. Several input parameters and their setting for this function are explained in Table 1 [16]. Parameter `rigsure` represents the selection using the principle of Steins Unbiased Risk Estimate (SURE), `h` means hard thresholding, and `mln` denotes threshold rescaling using a level-dependent estimation of the level noise.

Table 1. Input parameters setting

Parameter	Description	Chosen Setting
<code>s</code>	original signal	$x(n)$
<code>tptr</code>	threshold selection rule	<code>rigsure</code>
<code>sorh</code>	thresholding technique	<code>h</code>
<code>scal</code>	threshold's rescaling method	<code>mln</code>
<code>n</code>	decomposition level	5
<code>wav</code>	(mother) wavelet function	<code>db10</code>

As for TV based denoising method, a Majorization-Minimization (MM) algorithm [7] was used to solve a sequence of optimization problems. The parameter λ is set to 0.3 based on the experiment of and characteristic heart sound signals. The algorithm is run for 50 iterations to find more accurate result.

4. RESULTS AND ANALYSIS

Figure 1(a) and Figure 1(b) shows 'Normal S1 S2' heart sound signal $x(n)$ decomposition into 11 IMFs along with its final residue signal and the IMFs' energy density comparison under 0 dB level of white noise, respectively. As shown in Figure 1(b), only information-dominated IMFs (number 3, 4, 5, 6, 7, and 11) will be processed for final reconstruction, which leads to a term "partial reconstruction" of a signal.

The qualitative performance evaluation of our proposed method compared to other denoising methods were performed by visual inspection and comparison. Figure 2 presents the input clean signal, noisy signal, and denoised (reconstructed) signal of 'S4 Gallop' using wavelet, TV, and EMD denoising methods. In each noise case, only one simulation result under 5 dB input SNR level is shown. Based on Figure 2, it is shown that EMD denoising method performs better among others in three types of noises: white (a), brown (b) and exponential noise (c) as its denoised signal most resembles the original signal. If we look closely and zoom in the figure, we will know that the amplitude of denoised signal by TV method are slightly reduced. Even though the denoised signal by TV method keeps the amplitude of its main components almost the same as original one, the amplitude outside the main components interval

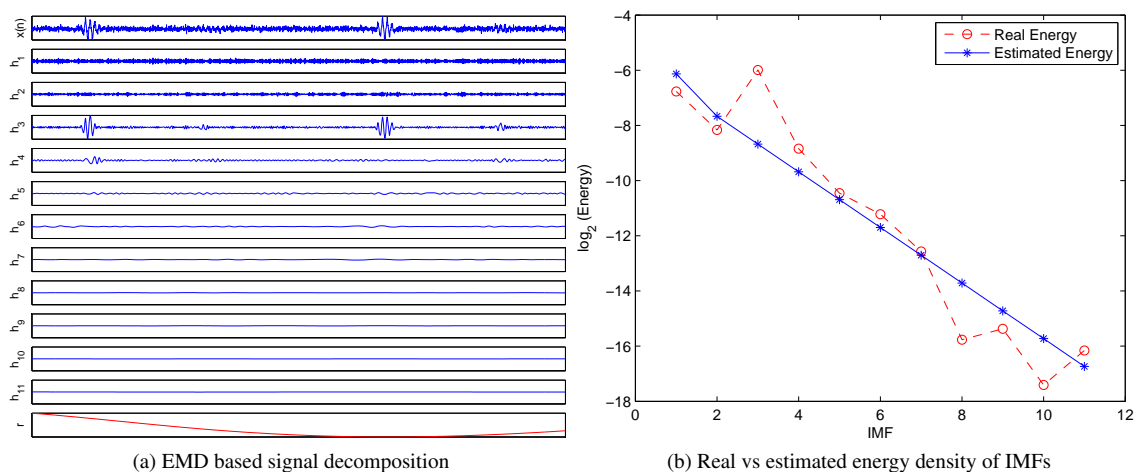


Figure 1. Signal decomposition and energy density comparison of IMFs under 0 dB level of white noise

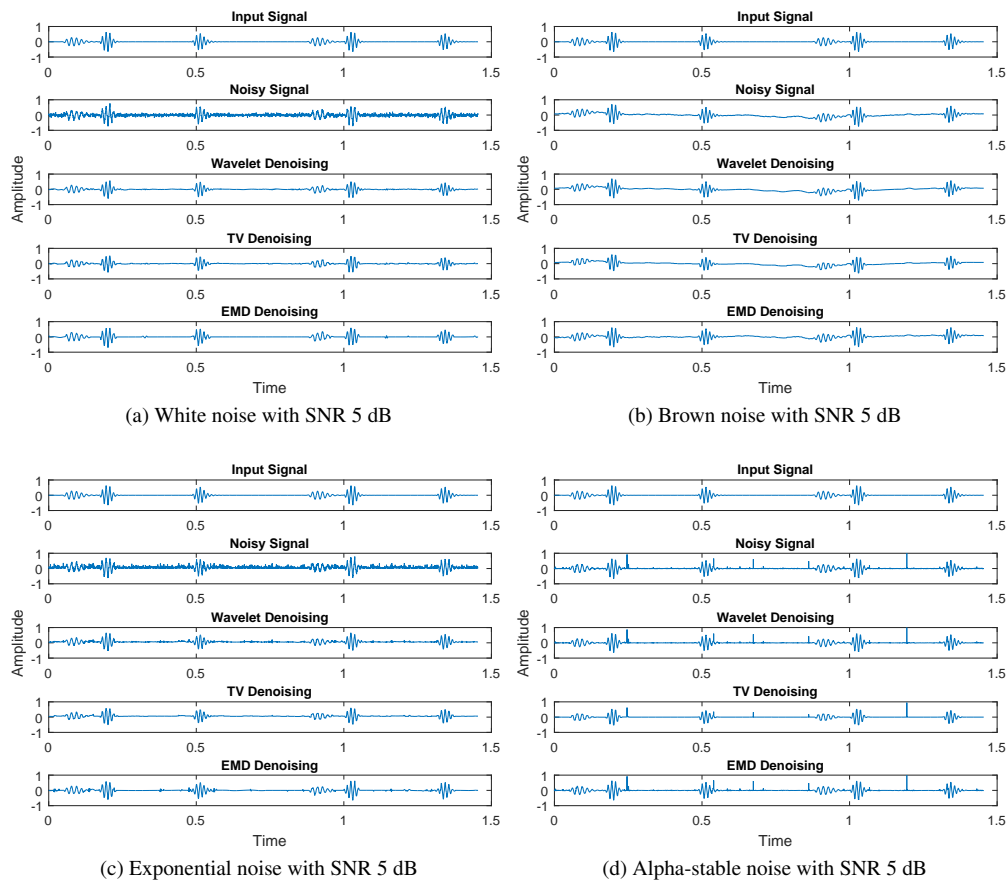


Figure 2. Visual performance comparison of 'S4 Gallop' heart sound signal denoising methods

is slightly changed compared to the original signal. As for alpha-stable noise as shown in Figure 2(d), WT and TV denoising methods performs better than EMD method.

In order to obtain more exact comparison, a quantitative performance was evaluated based on three metrics namely signal-to-noise ratio (SNR), root mean square error (RMSE), and percent root mean square difference (PRD),

Table 2. Performance comparison of denoising methods for 'S3 Gallop' heart sound data

Noise Type	Input SNR	SNR (dB)			RMSE			PRD (%)		
		WT	TV	EMD	WT	TV	EMD	WT	TV	EMD
White	0	8.9463	7.6747	9.9222	0.0391	0.0452	0.0352	35.7720	41.3448	32.1339
	5	12.7895	11.8554	13.2863	0.0251	0.0280	0.0240	22.9760	25.5490	21.9542
	10	16.6698	13.6183	17.6169	0.0161	0.0228	0.0145	14.6864	20.8534	13.2708
	15	20.5798	14.2784	20.9220	0.0102	0.0211	0.0101	9.3646	19.3253	9.3160
Brown	0	-1.3465	-1.3822	0.58753	0.1329	0.1334	0.1071	121.4947	121.9054	97.8917
	5	3.4123	3.1738	5.0755	0.0768	0.0786	0.0641	70.1732	71.8188	58.5944
	10	8.3727	7.5069	9.8494	0.0431	0.0471	0.0374	39.4378	43.0857	34.1929
	15	13.1883	10.8689	15.1542	0.0246	0.0316	0.0205	22.499	28.8733	18.6951
Exponential	0	-0.9209	-0.8023	6.2413	0.1217	0.1200	0.0537	111.2174	109.7049	49.0467
	5	4.0152	4.1953	10.1811	0.0689	0.0675	0.0349	63.0014	61.7036	31.8804
	10	8.8459	8.4530	14.5646	0.0395	0.0413	0.0223	36.1247	37.7918	20.3669
	15	13.6832	11.6200	18.3461	0.0226	0.0287	0.0157	20.6983	26.2448	14.3572
Alpha-stable	0	9.8326	10.1323	8.0622	0.0440	0.0423	0.0564	40.2600	38.6638	51.5371
	5	15.7833	13.0523	11.3505	0.0220	0.0272	0.0392	20.1374	24.8517	35.8671
	10	20.1803	13.8206	14.2772	0.0158	0.0259	0.0336	14.4564	23.6848	30.6898
	15	25.2577	14.3523	18.3497	0.0073	0.0213	0.0262	6.6370	19.4375	23.9710

which are calculated as follows:

$$SNR = 10 \log_{10} \frac{\sum_{n=1}^N [y(n)]^2}{\sum_{n=1}^N [y(n) - \hat{y}(n)]^2} \quad (9)$$

$$RMSE = \sqrt{\frac{\sum_{n=1}^N [y(n) - \hat{y}(n)]^2}{N}} \quad (10)$$

$$PRD = \sqrt{\frac{\sum_{n=1}^N [y(n) - \hat{y}(n)]^2}{\sum_{n=1}^N [y(n)]^2}} \times 100 \quad (11)$$

where $y(n)$ denotes the clean original signal, $\hat{y}(n)$ refers to the denoised (reconstructed) signal, and N represents the length of the signal.

SNR is defined as the ratio of the power of a signal (useful information) and the power of noise (irrelevant signal). RMSE is used to measure the accuracy of denoising method in preserving the quality of information in the denoised signal by calculating the sample standard deviation of the differences between denoised signal and original signal. PRD is frequently used as a method of quantifying the distortion or the difference between the original and the reconstructed signal. The PRD indicates reconstruction fidelity by point wise comparison with the original data. A denoising method is said to perform better if at a particular input SNR, the value of output SNR is larger while the value of RMSE and PRD are smaller.

Comparative simulation results of three denoising methods (WT, TV, and EMD) over ‘S3 Gallop’ heart sound data on the basis of SNR, RMSE, and PRD are shown in Table 2. The simulation result values were rounded into 4 digits after comma. Highlighted (bold) values indicates the best performance among others. It is shown that for three cases of noises (white, brown, and exponential) under different input SNR values (0, 5, 10, and 15 dB), EMD denoising method consistently yields largest SNR value, and smallest RMSE and PRD values (see bold values). For instance in white noisy environment with 0 dB input SNR level, EMD method shows SNR value 9.9222 dB, RMSE 0.0352 and PRD 32.1339 % where as WT (TV) method shows 8.9463 (7.6747) dB SNR, 0.0391 (0.0452) RMSE, and 35.7720 % (41.3448 %) PRD. The performance of EMD method in these three types of noises for other heart sound signals (‘Normal S1 S2’ and ‘S4 gallop’) over input SNR level range (0 dB - 15 dB) is superior as well compared to WT and TV methods. However, for heart sound signals contaminated with alpha-stable noise, EMD method does not perform well compared to its counterparts especially for input SNR level 0 - 10 dB. In this type of noise, on average, WT method outperforms other two methods, except for the case of 0 dB input SNR where TV method produces the best performance on all three metrics. Alpha-stable noise being used in this simulation represents the impulsive noise or disturbance characterized by high amplitude and short time duration within arbitrary location along the data. This impulsive disturbance usually occurs when there is quick movement or friction between chest skin and stethoscope during recording heart sound data. This alpha-stable noise has four parameters: α (characteristic exponent), β (skewness), γ (scale) and δ (location) [17]. Parameter α indicates the tail of distribution while β specifies whether the distribution is right- or left-skewed. In this simulation, we used $\alpha = 1.6$, $\beta = 1$, $\gamma = 0.1$ and $\delta = 0$.

Graphical visualization of comparative simulation results of ‘S4 Gallop’ heart sound signal under four types of noises is depicted in Figure 3. Figure 3(a-c) shows the comparative output SNR, RMSE and PRD value of three denoising methods with respect to different input SNR levels in white noisy environment. It is shown that EMD method (blue line with triangle point) on average performs better than WT (black line with rectangle point) and TV (red line with circle point), indicated by larger output SNR value and smaller RMSE and PRD values. The same trend is also observed in simulation results over brown and exponential noisy signal as shown in Figure 3(d-f) and Figure 3(g-i). EMD is equivalent to dyadic filter structure which can effectively decompose fractional Gaussian noise processes such as white and colored (brown) noises. This leads to effective denoising method over different class of fractional Gaussian noises [18–20]. Moreover, EMD method does not require any predefined basis function and is fully data-driven which offers more flexibility and adaptability to any signal under consideration. However, EMD method does not perform well compared to its counterparts under alpha-stable noise simulation as shown in Figure 3(j-l). According to our observation during repeated simulations, we chose constant value $C = 0.6$ in threshold value calculation within EMD denoising mechanism to obtain good performance. This constant value applies well on three types of noises (white, brown and exponential). However, based on our simulation, the performance of EMD denoising method under alpha-stable noise can be improved by increasing the constant value C up to 1.5. In addition, to mitigate this impulsive disturbance in heart sound analysis, an adaptive selection algorithm based on Heron’s formula can be employed in the subsequent process [21].

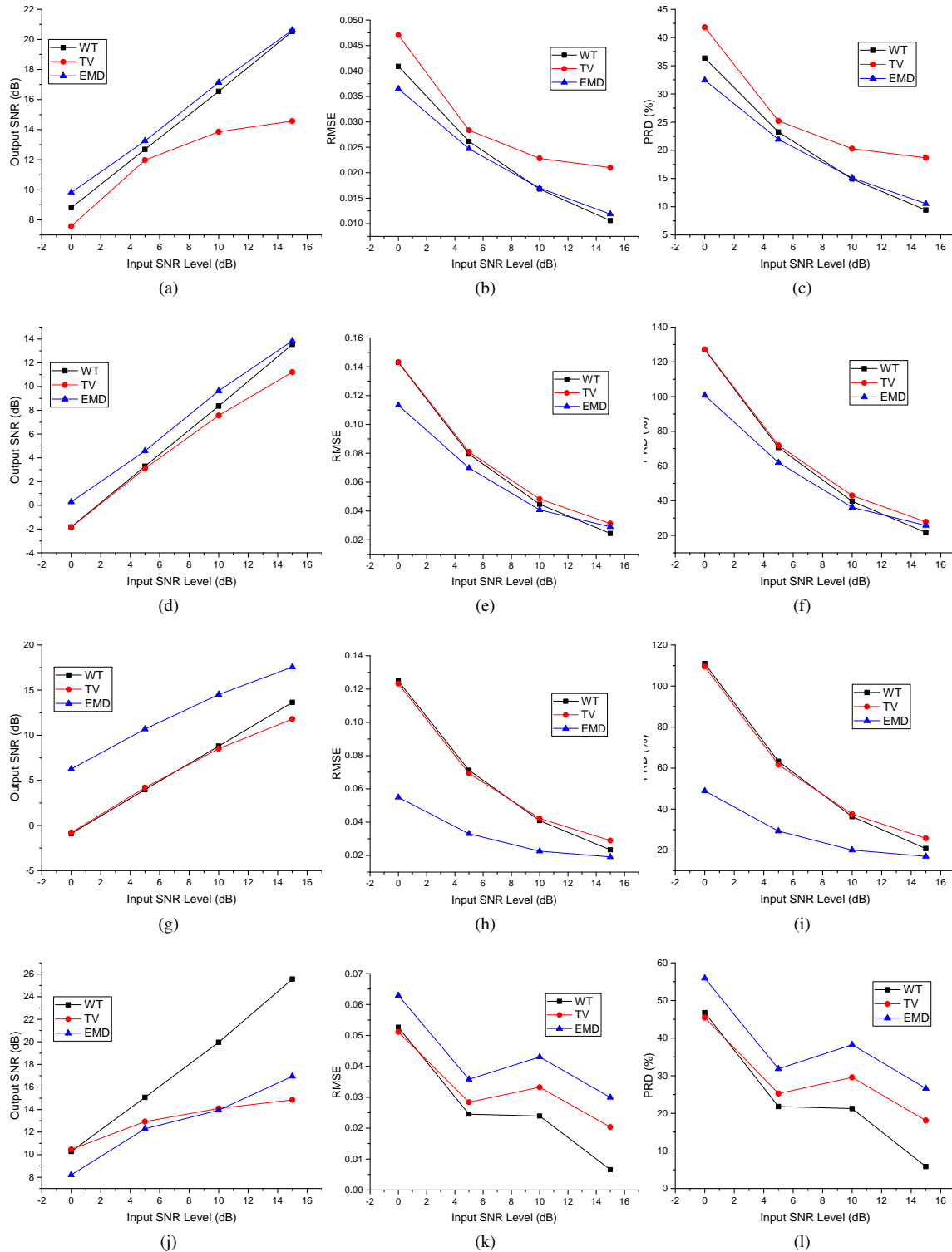


Figure 3. Performance comparison over ‘S4 Gallop’ heart sound signal under (a-c) white (d-f) brown (g-i) exponential and (j-l) alpha-stable noise

5. CONCLUSION

Empirical Mode Decomposition (EMD) based denoising method is proposed in this paper. Its performance and analysis compared to other two methods based on wavelet transform (WT) and total variation (TV) are presented. Four types of noises with input SNR level 0 dB, 5 dB, 10 dB and 15 dB are artificially added to clean original normal and abnormal heart sound signals obtained from the University of Michigan Health System. Based on extensive simulations, our proposed EMD based denoising method consistently yields better performance in terms of three standard metrics: signal-to-noise ratio (SNR), root mean square error (RMSE), and percent root mean square difference (PRD) under white, colored (brown) and exponential noises. As for alpha-stable noise, on average, WT and TV based denoising methods perform better than EMD method.

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