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Discrete Markov Chain Based Spectrum Sensing for Cognitive Radio

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ABSTRACT

Spectrum sensing is one of the functionalities of cognitive radios to exploit spectrum holes without interrupting primary users transmission. The more efficient of the spectrum sensing, the highest the throughput of secondary and primary network. This paper presents spectrum sensing method based on phase type modelling that is simple to do for secondary users to conclude about the channel state (idle or busy) under collision constraint. The parameters of phase type model can be adjusted based on desired operating point of the receiver sensor in its ROC curve. The presented approach can run a trade off between sensing time and the two error probabilities of sensor false alarm and miss-detection.

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1. INTRODUCTION

Since spectrum in wireless communications has become valuable, cognitive radios are developed to exploit the spectrum holes in licensed bands under protective constraints for incumbent users [1, 2]. So the cognitive users (secondary users) should act intelligently in order to use the spectrum for data transmission and not to interfere with the primary users (PU) simultaneously [3, 4, 5]. In such a case, opportunistic spectrum access (OSA) named Interweave model has been evolved to enable the users dynamically access the spectrum [6, 7]. OSA has two main steps, spectrum sensing and spectrum access [8, 9]. In the sensing step, a secondary user (SU) evaluates the spectrum bands to find idle channels and in the second step, the SU should decide on its access for data transmission [10, 11, 12]. At the end of sensing phase the SU concludes about the state of channel occupancy and there is a level of uncertainty in its decision. Some of spectrum sensing methods such as feature detection, cyclo-stationary detection and matched filter have considered physical characteristics of PU signal [13,14,15] while the others exploit some general parameters of signal such as energy level along with statistical analysis to conclude about the channel occupancy [16, 17]. In this paper we propose spectrum sensing method based on phase type modelling for channel state detection. The presented approach can run a trade off between sensing time and the two error probabilities of sensor false alarm and miss-detection

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SYSTEM MODEL AND PROBLEM FORMULATION

In our proposed model, at the beginning of the sensing process the SU is in the zero state of Markov chain shown in figure 1 and starts to transit between states based on the probabilities depending upon received signal values sampled in each time step. The process continues till the Markov chain enters the absorb state of A. Depending on which path was traversed to enter the absorb state, the channel state is decided. With the mentioned description, the Markov chain is a discrete phase type model $PH_d(\tau, T)$ [18]. The discrete phasetype distribution is dense in the field of all discrete positive-valued distributions, that is, it can be used to approximate any discrete positive-valued distribution [19, 20].

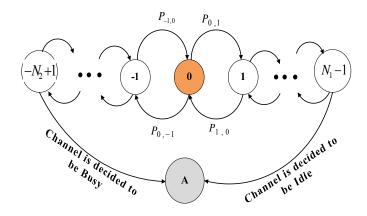


Figure 1. Phase type representation of sensing procedure

Suppose at the k^{th} time step (k^{th} sample) the SU is in the n^{th} state ($-N_2+1 \le n \le N_1-1$). Having sampled the signal r(t), the SU in the chain transits to state n+1 with probability $f_0(y_k)$ and to state n-1 with probability $(1 - f_0(y_k))$, in which y_k is the observation variable, see Figure 2 the observation variable is the one that a decision about channel state could be made based on such as energy level of samples. In this paper we define $y_n \triangleq |r_n|^2$. These transition probabilities are equal to likelihood value of signal sample due to H₀ and H₁ hypotheses:

$$\begin{cases}
H_0^{k}, & r(k) = Z(k) \\
H_1^{k}, & r(k) = h(k) * S(k) + Z(k)
\end{cases}$$
(1)

in which y_k is the k^{th} sample of signal, Z(k) is the Gaussian random variable with mean zero and some variance σ^2 and h(k) and S(k) are the channel coefficient and PU transmitted signal respectively. If we neglect the variation of channel coefficient during the sensing time (because the sensing phase is a short period of time) and if the samples are considered as i.i.d random variables, it can be shown that the distribution $f_0(y_k)$ and $f_1(y_k)$ are chi-square which are shown in equation (2) and (3) [21, 22].

$$f_0 = P(y_n | H_0) = \frac{1}{\sigma^2} e^{-\frac{y_n}{\sigma^2}} \mathbb{I}(y_n > 0)$$
 (2)

$$f_0 = P(y_n | H_0) = \frac{1}{\sigma^2} e^{-\frac{y_n}{\sigma^2}} \mathbb{I}(y_n > 0)$$

$$f_1 = P(y_n | H_1) = \frac{1}{\sigma^2} e^{-\frac{y_n + g}{\sigma^2}} I_0(\sqrt{\frac{gy_n}{\sigma^2/2}})$$
(3)

in which the function $\, \mathbb{I} \,$ is :

$$\mathbb{I}(y_n > 0) = \begin{cases} 0 & y_n < 0 \\ 1 & y_n > 0 \end{cases}$$

and I₀ is the modified Bessel function of the first kind and g is the channel gain.

Because signal samples are random variables due to stochastic behaviour of channel, the Markov chain is non-homogeneous and depends on k^{th} sample at k^{th} time step.

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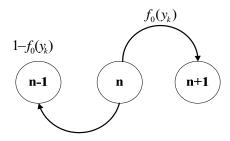


Figure 2. Transition between states for secondary user

So the equivalent phase type model (that describes the distribution of total number of samples needed to decide about channel occupancy) has the initial probability matrix τ and the transition probability matrix T_k (at k^{th} time step) described below:

$$\tau = \llbracket \tau_j \rrbracket_{1 \times (N_1 + N_2)} \tag{4}$$

$$\tau_j = \begin{cases} 1, \ j == 0 \\ 0, & \text{o.w} \end{cases}$$
 (5)

$$T_k = [P_{i,j}]_{(N_1 + N_2 - 1) \times (N_1 + N_2 - 1)}$$
(6)

The probabilities $P_{i,j}$ for $i = -N_2 + 1, ..., N_1 - 1$ can be described as below:

$$\begin{split} &P_{i,i+1=}f_0(y_k) = P(y_k|H_0) \\ &P_{i-1,i=}1 - f_0(y_k) = P(y_k|H_1) \\ &P_{i,j} = 0 \ \text{ for } j \neq i+1 \text{ and } j \neq i-1 \end{split}$$

Now we have to answer two questions.

- 1- How to compute N₁ and N₂ for the chain?
- 2- How to introduce the collision probability constraints in to the sensing scheme to protect PU signal from interference?

It is obvious that the more the value of N_1 , the more samples needed to decide about being idle and also the more the value of N_2 , the more samples needed to decide about being busy. If both N_1 and N_2 increase the final decision has high level of certainty but the time to decision about channel occupancy grows rapidly. In other words, the values of N_1 and N_2 directly impact on the probability of false-alarm and miss-detection. Therefore if these probabilities are known previously, the values for N_1 and N_2 can be calculated accordingly. To meet the collision constraint, the operating point of sensor in its ROC curve must be adjusted so that:

$$\begin{cases} P_{miss-det} = P_{collision} \\ P_{fa} = P_{prescribed \, value} \end{cases}$$
 (7)

then the problem of finding N_1 and N_2 turns to calculating these probabilities. So we have:

$$P_{miss-det} = P(H_0|H_1) = \sum_{N=N_1}^{\infty} P(H_0 \text{ and } n_s = N | H_1)$$

$$P_{fa} = P(H_1|H_0) = \sum_{N=N_2}^{\infty} P(H_1 \text{ and } n_s = N | H_0)$$

where n_s is the total number of samples needed for decision. Conditioned on samples value the probability of miss-detection can be derived as:

$$P_{miss-det} = \sum_{N=N_1}^{\infty} \int ... \int P(H_0 \text{ and } n_s = N \mid H_1, Y^{(N)} = y^{(N)}) \times f_{Y^{(N)}}^{y(N)} d(y^{(N)})$$

Assuming signal samples are i.i.d and considering the condition H₁ it can be written as:

$$f_{Y^{(N)}}^{y(N)} = \prod_{i=1}^{N} (f_1(y_i))$$

We have also:

$$\begin{split} P\big(H_0 \text{ and } n_s &= N \mid H_1, Y^{(N)} = y^{(N)}\big) \\ &= P(SU \text{ goes from state 0 to } N_1 - 1 \text{ in } (N-1) \text{steps } \Big| |H_1, Y^{(N)} = y^{(N)}) \times P(SU \text{ goes from state } N_1 - 1 \text{ to A at the final step } \Big| |H_1, Y^{(N)} = y^{(N)}) \end{split}$$

Proceeding to compute we have:

$$P\left(\text{SU goes from state 0 to N}_1 - 1 \text{ in (N-1)steps} \left| |H_1, Y^{(N)} = y^{(N)} \right) = [T_1, ... T_{N-1}]_{0, N_1 - 1} \right. \\ P\left(\text{SU goes from state N}_1 - 1 \text{ to state A at the final step } \left| |H_1, Y^{(N)} = y^{(N)} \right| = f_0(y_N) \right.$$

where T_i is the probability matrix of phase type computed for i^{th} sample and $[P]_{i,j}$ means the entry of matrix P in row i and column j.

$$P_{miss-det} = \sum_{N=N_1}^{\infty} \int ... \int \left[\left\{ \prod_{j=1}^{N-1} T_j \right\}_{0,N_1-1} f_0(y_N) \prod_{i=1}^{N} (f_1(y_i)) \right] d(y^{(N)})$$
(8)

in which $f_1(y_i)$ is the probability density function of observation variable under H_1 hypothesis. The same procedure can be applied for the false-alarm probability to derive:

$$P_{fa} = P(H_1|H_0) = \sum_{N=N_1}^{\infty} P(H_1 \text{ and } n_s = N | H_0)$$

$$P_{fa} = \sum_{N=N_2}^{\infty} \int ... \int \left[\left\{ \prod_{j=1}^{N-1} T_j \right\}_{0,-N_2+1} \times \left(1 - f_0(y_N)\right) \prod_{i=1}^{N} \left(f_0(y_i)\right) \right] d(y^{(N)})$$
(9)

Considering the equations (7), (8) and (9) can be solved numerically for the minimum values of N_1 and N_2 to have the minimum sensing time. Remember that P_{fa} and $P_{miss-det}$ are non-increasing function of computation of N_1 and N_2 respectively so the integrals go to zero quickly as N_1 and N_2 increase. In general the two derived probabilities are not so tractable to work with, that is because of non-homogeneous property of a Markov chain. Changing the transition law between the states results in more tractable equations which is in our next study.

3. NUMERICAL RESULT

In this section probability of false-alarm and miss-detection are plotted versus N_1 and N_2 . It should be noted that probability of miss-detection and false-alarm are dependent on both N_1 and N_2 but it can be easily inferred that their dependencies are insignificant to N_2 and N_1 respectively. Simulation parameter and their values are shown in the Table1. Figure3 and 4 show the two probabilities versus N_1 and N_2 . To have a certain probability of false-alarm and collision, such curves can be drawn to calculate the number of states or equations (8) and (9) can be solved numerically for N_1 and N_2 .

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Table 1. Simulation parameters	
Parameter	Value
σ	1
g	1

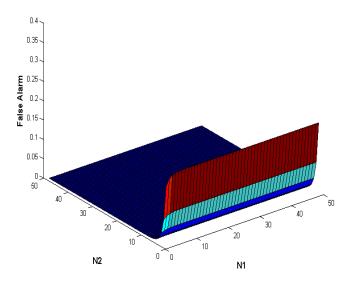


Figure 3. False alarm probability versus N1 and N2

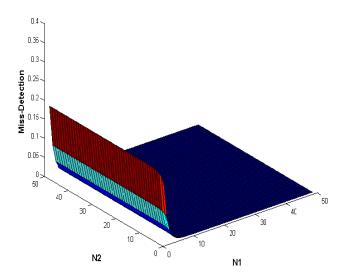


Figure 4. Miss-Detection probability versus N1 and N2

In this part, we compare our presented method with the most common spectrum sensing algorithm, i.e., energy detector. Energy detectore are known because they are simple to do for cognitive radios and do not need prior information of PU signal. Other sensing approaches are complex and have to know some prior knowledge about PU signal. The relation between the two probabilities in such a detector under the assumption of independency of primary signal and noise and the assumption of Gaussian zero mean for noise is as follows [23].

$$P_{fa}(\tau) = Q\left(\sqrt{2\gamma + 1}Q^{-1}(P_d) + \sqrt{\tau f_s}\gamma\right) \tag{10}$$

In which τ , γ , f_s are the sensing time, signal to noise ratio and sampling frequency respectively. P_d is the probability of detedction which is the complement of $P_{miss-det}$. Equivalently, based on the number of sensing samples (N) equation (10) will be changed to:

$$N = \frac{1}{\gamma^2} \left(Q^{-1} (P_{fa}) - Q^{-1} (P_d) \sqrt{(2\gamma + 1)} \right)^2 \tag{11}$$

If we assume that the noise power (variance) is unity (to compare with the achieved curves in the numerical results) and under the same simulation environment, the expected number of samples needed to reach a decision about the channel state with $P_{fa} = 0.1$ and $P_{miss-det} = 0.05$ is plotted in Figure 5. As it can be seen, the number of samples to decide about the channel state is considerably lower in the presented method than to the energy detector; hence the sensing time becomes less.

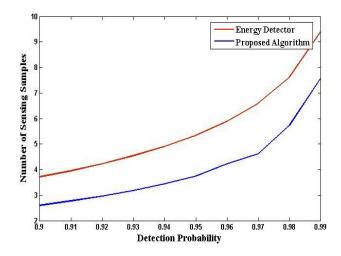


Figure 5. A decision about the channel state with $P_{fa} = 0.1$ and $P_{miss-det} = 0.05$

4. CONCLUSION

In this paper spectrum sensing based on discerete Markov chain was presented. The presented approach is so simple to do to for secondary users to decide on channel occupancy. The parameters of the proposed model are adjusted so that the collision probability imposed by the primary network on the secondary network is met. Furthermore the presented approach gives us to adapt the sensing time. It means when the received signal power of primary user is high, the sensing time takes much less than that of for low signal power, while maintaining the operating point of the sensor constant (the false alarm and miss-detection probabilities remain unchanged). We validate our analysis by simulation and compared the proposed method with energy detector, the most common spectrum sensing algorithm.

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