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Online signature verification using hybrid wavelet transform

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ABSTRACT

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Keywords:

HMM HWT Left Right Model Online Signature Verification Online signature verification is a prominent behavioral biometric trait. It offers many dynamic features along with static two dimensional signature image. In this paper, the Hybrid Wavelet Transform (HWT) was generated using Kronecker product of two orthogonal transform such as DCT, DHT, Haar, Hadamard and Kekre. HWT has the ability to analyze the signal at global as well as local level like wavelet transform. HWT-1 and -2 was applied on the first 128 samples of the pressure parameter and first 16 samples of the output were used as feature vector for signature verification. This feature vector is given to Left to Right HMM classifier to identify the genuine and forged signature. For HWT-1, DCT HAAR offers best FAR and FRR. For HWT-2, KEKRE 128 offers best FAR and FRR. HWT-1 offers better performance than HWT-2 in terms of FAR and FRR. As the number of states increase, the performance at 275 symbols whereas for HWT-2, best performance is at 475 symbols by KEKRE 128.

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1. INTRODUCTION

Handwritten Signatures have been used for centuries for identification and authentication of a person as well as documents [1, 2]. In biometrics classification, it is part of behavioral characteristics like voice, gait etc. whereas physical characteristics include fingerprint, palm print, face, iris, retina etc. [3]. Biometric characteristics are universal, unique and measurable and are better than personal ID cards, PIN or passwords [4-6]. Biometric system for signatures can operate in two ways. First Verification, in which the individual's signature will be compared with his stored signature in a database to verify that the individual is the same who he says to be. Second Identification, in which the signature will be compared with the many signatures in the database to identify an individual out of many unknowns.

Automating the process of Handwritten Signature Verification will be useful for document verification in various sectors such as banking, legal documentation etc. There are two types of Signature Verification; offline (static) or online (dynamic). Offline signatures offer two dimensional image of the signatures whereas online signatures have added advantage that it also measures pressure applied by the user, speed of writing, inclination of pen along with the two dimensional signature image [7]. Dr. Kekre proposed Hybrid Wavelet Transform (HWT) which is formed by combining the two orthogonal transforms using Kronecker product. It has the ability to analyze the signal at global as well as local level like wavelet transform [8]. HWT is of two types and are explained below. Consider matrices X and Y as shown below.

	[<i>x</i> ₁₁	<i>x</i> ₁₂	 x_{1a}	[<i>y</i> ₁₁	y_{12}	 y_{1b}
X =	<i>x</i> ₂₁	<i>x</i> ₂₂	 $ \begin{array}{c} x_{1a} \\ x_{2a} \\ \dots \\ x_{aa} \end{array} $	$\mathbf{Y} = \begin{bmatrix} y_{11} \\ y_{21} \\ \dots \\ y_{b1} \end{bmatrix}$	<i>y</i> ₂₂	 y_{2b}
	x_{a1}	x_{a2}	 x_{aa}	y_{b1}	y_{b2}	 y_{bb}

HWT-1 matrix ' T_{XY} ' of size (NxN), as shown in Table 1, can be formed by the Kronecker product of two orthogonal transform matrices X and Y respectively, with sizes (a x a) and (b x b), such that N=a x b. For HWT-1, first 'b' number of rows of the HWT matrix are calculated as the product of each element of first row of the orthogonal transform X with each of the columns of the orthogonal transform Y. For next 'b' number of rows of HWT matrix the second row of the orthogonal transform matrix X is shift rotated after being appended with zeros. Similarly the other rows of HWT matrix are generated as set of b rows each time for each of the 'a-1' rows of orthogonal transform matrix X starting from second row up to last row.

Table 1. HWT-1 Matrix

				1 401	/ 1. 11 11	I-I Wiau	іл			
y11x11	y11x12	 y11x1a	y12x11	y12x12		y12x1a		 y1bx11	y1bx12	 y1bx1a
y21x11	y21x12	 y21x1a	y21x12	y22x12		y22x1a		 y2bx11	y2bx12	 y2bx1a
yb1x11	yb1x12	 yb1x11	yb2x11	yb2x12		yb2x1a		 yb1x11	yb1x12	 yb1x12
x21	x22	 x2a	0	0		0		 0	0	 0
0	0	 0	x21	x22		x2a		 0	0	 0
0	0	 0	0	0		0		 x21	x22	 x2a
x31	x32	 x3a	0	0		0		 0	0	 0
0	0	 0	x31	x32		x3a		 0	0	 0
0	0	 0	0	0		0		 x31	x32	 x3a
xa1	xa2	 xaa	0	0		0		 0	0	 0
0	0	 0	xa1	xa2		xaa		 0	0	 0
0	0	 0	0	0		0		 xa1	xa2	 xaa

HWT-2 matrix of size (NxN) is also formed by the Kronecker product of two orthogonal transform matrices X and Y. First N/2 rows of the matrix are formed by product of each element of first a/2 rows of the matrix X with each of the columns of the matrix Y. For next 'b' number of rows of matrix, the 'a/2+1'th row of the orthogonal transform matrix X is shift rotated after being appended with zeros. Next N/2 rows are generated as set of b rows each time for each of the 'a/2' rows of orthogonal transform matrix X starting from 'a/2+1'th row up to last row.

HWT offers better performance in image compression than the orthogonal transforms used to generate them [9, 10]. HWT is also used for water marking [11] and to convert color image to gray image [12]. Various classifiers based on KNN, SVM and NN [13, 14] have been used for verification of signatures. In [15], KNN classifier was used with, HWTs of the pressure map of online signatures as feature vector. It offered an EER of 30%. In [16], SVM classifier was used with, a kernel function of online signature time series, based on LCSSs detection, as a feature vector. It offered an EER of 6.84%. Using SVM in conjunction with HMM offered FAR of 1.96% and FRR of 60.43%. In [17], neural network classifier was used with, the approximation and detail component of DWT of the pen postion and pen movement angle as feature vector. Using all coefficients of DWT, success rate was 100% with trained signature, 90% with untrained signatures and FRR of 24%. Using selected 25 coefficients of DWT, success rate was 100% with trained signature, 95% with untrained signatures and FAR of 8%.

In this paper, we propose a method for online signature verification using Hybrid Wavelet Transform and Hidden Markov Model classifier. The proposed method is shown in Figure 1. We have used SVC2004 database which is a large database containing signatures from 40 individuals. It has total of 1,600 signatures, obtained using a Wacom Intuos tablet. It consists of 20 genuine and 20 forgery signatures collected for each person. Genuine signatures are collected in two different sessions. Forgeries for each person are provided by at least four other individuals from the database. The performance results of various signature verification systems that participated in the SVC2004 competition is available. The best performance for 40 available users is average EER 6.90% with standard deviation of 9.45%, minimum value of 0.00 and maximum value of 50.00%. The best performance for 60 other users is average EER 2.89% with standard deviation of 5.69%, minimum value of 0.00 and maximum value of 30.00% [18]. Every signature sample consist of X-coordinate-scaled cursor position along the x-axis, Y-coordinate-scaled cursor position along the y-axis,

Time stamp-system time at the time of signing, Button status-current button status (0 for pen-up and 1 for pen-down), Azimuth-clockwise rotation of cursor about the z-axis, Altitude-angle upward toward the +ve z-axis, Pressure-normal pressure applied by hand. Pressure applied by the tip of the pen on the pressure sensitive pad is used for generating the feature vector. We have used Discrete Cosine transform (DCT), Discrete Hartley transform (DHT), Discrete Walsh transform (DWT) and Discrete Kekre transform (DKT) to form the HWT-1 and HWT-2 matrix. The output of HWT is given to HMM for classification.



Figure 1. Proposed System

2. RESEARCH METHOD

Signature database of 1600 signatures, provided by The First International Signature Verification Competition (SVC 2004) is used. It has signatures of 40 users. Every user has 40 signatures, out of which, 20 are genuine and 20 are skilled forgeries. The first 128 samples of every signature is used to find HWT. The signatures, having samples less than 128, will be padded with zeroes. The first 16 samples of the HWT output are used as feature vector. Discrete Cosine transform (DCT), Discrete Hartley transform (DHT), Discrete Walsh transform (DWT) and Discrete Kekre transform (DKT) are used to form the HWT [19, 20]. There are many topologies of HMM such as Left to Right, Ergodic and Ring. Left to Right topology as shown in Figure 2, is found to be best suited for the Signature modelling [21, 22].

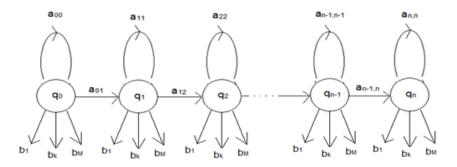


Figure 2. Left to Right HMM model

HMM is represented by the transition probability matrix (A), Observation matrix (B) and initial probability distribution matrix (π). [23, 24] Consider a system which is in a distinct state (S1, S2, ..., SN) at any point of time. In this experiment the number of states (N) of the model are varied from 2 to 5. As the number of states increase, the time needed for training increases. The number of observations (M) corresponding to each state are varied from 200 to 750 in the increments of 25. The output of HWT is a matrix of dimension [1×128]. The matrix elements from 1 to 16 are chosen as a feature vector. Feature vectors are scaled into M number of observations.

Initial Probability Distribution (π): $\pi_i = P$ ($q_1 = S_i$); $1 \le i \le N$. We assume the initial probability of the first state is 1 and the others are 0 which implies that in the beginning HMM is always in state 1. State transition probability (a_{ij}): $a_{ij} = P$ ($S_t=j / S_{t-1}=i$). For the left-to-right HMM, $a_{ij}=0$ when i>j. we are using the HMM of first order so that $a_{ij}=0$ when j>i+1. Initially, the state transition matrix is generated using the random numbers such that $\sum_{j=1}^{N} a_{ij} = 1$; $1 \le i \le N$. Observation probability (b_j): $b_j(k) = P$ (V_k at $t / q_t = S_j$); $1 \le j \le N$; $1 \le k \le M$; the probability of generating a symbol V_k in state j.

Statistics and machine learning toolbox of the MATLAB 13 was used for implementation of HMM. Initially a randomly generated transition probability Matrix (A) is generated using MATLAB. We assume observation probability matrix (B) to have equal probability for every symbols and HMM to be in state 1. HMM is trained using the function 'hmmtrain' for 3 to 20 genuine training signature samples, number of states from 2 to 5 and symbols from 200 to 750. After HMM is trained, it is used to test 20 genuine and 20 forged signatures of 40 users.

3. RESULTS AND DISCUSSION

Performance of the system will be measured on the basis of False Rejection Ratio (FRR) and False Acceptance Ratio (FAR). FRR refers to false rejection of genuine signature and FAR refers to false acceptance of forged signature [25]. FRR is computed as ratio of the number of signatures detected as forged to the total number of genuine signatures tested. FAR is computed as ratio of the number of signatures detected as detected as genuine to the total forged signatures tested. Testing has been carried out for 40 users and then the average FRR and FAR are calculated. In FRR-FAR plot shown in Figure 3, the point where two graphs cross each other is referred as Equal Error Rate (EER). At this point the value of FRR and FAR is minimum. The results obtained by the first 1–16 samples of HWT-1 and 2 for DCT, DHT, HAAR, HADAMARD and KEKRE combinations is shown in the Tables 2-4.

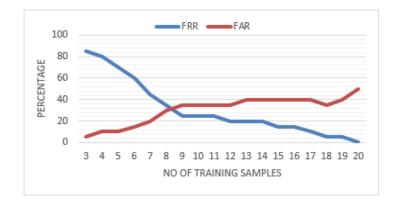


Figure 3. FRR – FAR plot

The comparison of HWT-1 and 2 for 1–16 bit for DCT combinations is shown in the Tables 2-4.

- Best FRR-FAR: FRR-FAR should be as low as possible. For HWT-1, DCT HAAR offers best performance with FRR & FAR of 0 %. For HWT-2, DCT KEKRE offers best performance with FRR & FAR of 9%. The performance offered by DCT HAAR HWT for HWT-1 is better than HWT-2. The performance offered by DCT combinations for HWT-1 is better than HWT-2. For HWT-1, the performance offered by DCT combinations except DCT DHT is better than Orthogonal DCT transform. For HWT-2, only DCT KEKRE offers better performance than DCT combinations than Orthogonal DCT transform.
- Best Number of Training Samples: The number of training samples should be as low as possible. For HWT–1, DCT DHT offers best performance of 12 compared to 15 training samples for Orthogonal DCT transform. For HWT–2, Orthogonal DCT transform offers best performance of 4 training samples compared to all combinations of DCT HWT. The performance offered by DCT combinations for HWT-2 is better than HWT-1.
- Best state wise FRR–FAR: FRR–FAR should be as low as possible for the given state from 2 to 5. For HWT-1, DCT HAAR offers best performance for 2, 4 and 5 states, DCT KEKRE for state 3 and DCT HAAR for state 5 compared to orthogonal DCT transform. For HWT-2, DCT KEKRE offers best performance for 2 to 5 states compared to orthogonal DCT transform. The performance offered by DCT combinations for HWT-1 is better than HWT-2.
- Best Number of Symbol: It should be as low as possible. Testing was carried out for number of symbols from 200 to 750. It evident that the best performance in terms of FRR–FAR, AAR–ARR, EER is offered by 275-325 symbols for HWT-1 and 450–500 symbol for HWT-2. The performance offered by DCT combinations for HWT-1 is better than HWT-2.

The comparison of HWT-1 and 2 for 1–16 bit for DHT combinations is shown in the Table 2-4.

Best Number of Training Samples: For HWT-1, DHT KEKRE offers best performance with FRR & FAR of 5 %. For HWT-2, DHT KEKRE offers best performance with FRR 13% & FAR of 19%. The performance offered by DHT KEKRE HWT for HWT-1 is better than HWT-2. The performance offered by DHT combinations for HWT-1 is better than HWT-2. For HWT-1, the performance offered by DHT DCT, DHT KEKRE is better than Orthogonal DHT transform. For HWT-2, only DHT KEKRE offers better performance than Orthogonal DHT transform.

- Best Number of Training Samples: For HWT-1, DHT HADAMARD offers best performance of 10 training samples compared to 13 training samples for Orthogonal DHT transform. For HWT-2, DHT HADAMARD offers best performance of 5 training samples compared to 7 training samples for Orthogonal DHT transform. DHT combinations offer better performance for HWT-2 than HWT 1.
- Best state wise FRR–FAR: For HWT-1, DHT KEKRE offers best performance for 2, 3 and 4 states and DHT DCT for state 5 compared to orthogonal DHT transform. For HWT-2, DHT KEKRE offers best performance for 2 to 5 states compared to orthogonal DHT transform. DHT combinations offer better performance for HWT-1 than HWT-2.
- Best Number of Symbol: Testing was carried out for number of symbols from 200 to 750. It evident that the best performance in terms of FRR–FAR, AAR–ARR, EER is offered by 275 symbols for HWT-1 and 450–500 symbols for HWT-2. DHT combinations offers better performance for HWT-1 than HWT-2.

The comparison of HWT-1 and 2 for 1–16 bit for HAAR combinations is shown in the Tables 2-4.

- Best FRR–FAR:For HWT-1, HAAR DCT and HAAR KEKRE offers best performance with FRR & FAR of 0 %. For HWT-2, HAAR KEKRE offers best performance with FRR 11% & FAR of 12%. The performance offered by HAAR DCT and HAAR KEKRE HWT for HWT-1 is better than HWT-2. The performance offered by HAAR combinations for HWT-1 is better than HWT-2. For HWT-1, the performance offered by all combinations of HAAR is better than Orthogonal HAAR transform. For HWT-2, HAAR DHT and HAAR KEKRE offers better performance than Orthogonal HAAR transform.
- Best Number of Training Samples: For HWT-1, HAAR DHT offers best performance of 12 training samples with FRR, FAR of 15%, 15% respectively compared to 13 training samples with FRR, FAR of 10%, 30% respectively for Orthogonal DHT transform. For HWT-2, HAAR HADAMARD offers best performance of 5 training samples compared to 6 training samples for Orthogonal HAAR transform. HAAR combinations offer better performance for HWT-2 than HWT-1.
- Best state wise FRR–FAR: For HWT-1, HAAR KEKRE offers best performance for 2 to 5 states. HAAR DCT offers best performance for state 5 compared to orthogonal HAAR transform. For HWT-2, HAAR KEKRE offers best performance for 2 to 5 states compared to orthogonal HAAR transform. HAAR combinations offer better performance for HWT-1 than HWT-2.
- Best Number of Symbol: Testing was carried out for number of symbols from 200 to 750. It evident that the best performance in terms of FRR–FAR, AAR–ARR, EER is offered by 275 symbols for HWT-1 and 450–500 symbols for HWT-2. HAAR combinations offer better performance for HWT-1 than HWT-2.

The comparison of HWT-1 and 2 for 1-16 bit for HADAMARD combinations is shown in the Table 2-4.

- Best FRR–FAR: For HWT-1, HADAMARD KEKRE offers best performance with FRR & FAR of 0%. For HWT-2, HADAMARD KEKRE offers best performance with FRR 25% & FAR of 22%. The performance offered by HADAMARD KEKRE HWT for HWT-1 is better than HWT-2. The performance offered by HADAMARD combinations for HWT-1 is better than HWT-2. For HWT-1, the performance offered by all combinations of HADAMARD except HADAMARD DCT is better than Orthogonal HADAMARD transform. For HWT-2, the performance offered by all combinations of HADAMARD is better than Orthogonal HADAMARD transform
- Best Number of Training Samples: For HWT–1, Orthogonal HADAMARD transform offers best performance of 8 training samples compared to all combinations of HADAMARD HWT. For HWT–2, Orthogonal HADAMARD transform offers best performance of 5 training samples compared to all combinations of HADAMARD HWT. HADAMARD combinations offer better performance for HWT-2 than HWT-1.
- Best state wise FRR–FAR: For HWT-1, HADAMARD KEKRE offers best performance for 2 and 5 states. HADAMARD DHT offers best performance for state 4 and 5 compared to orthogonal HADAMARD transform. For HWT-2, HADAMARD KEKRE offers best performance for 2 to 5 states compared to orthogonal HADAMARD transform. HADAMARD combinations offer better performance for HWT-1 than HWT-2.
- Best Number of Symbol :Testing was carried out for number of symbols from 200 to 750. It evident that the best performance in terms of FRR–FAR, AAR–ARR, EER is offered by 275-300 symbols for HWT-1 and 500 symbols for HWT-2. HADAMARD combinations offer better performance for HWT-1 than HWT-2.

The comparison of HWT-1 and 2 for 1–16 bit for KEKRE combinations is shown in the Tables 2-4. Best FRR–FAR: For HWT-1, KEKRE DCT, KEKRE HAAR and KEKRE128 offers best performance with FRR & FAR of 0 %. For HWT-2, KEKRE 128 offers best performance with FRR 5% & FAR of

2%. The performance offered by KEKRE DCT, KEKRE HAAR and KEKRE128 HWT for HWT-1 is better than HWT-2. The performance offered by KEKRE combinations for HWT-1 is better than HWT-2. For HWT-1, the performance offered by KEKRE 128 is better than all combinations of KEKRE HWT. For HWT-2, the performance offered by KEKRE 128 is better than all combinations of KEKRE HWT.

- Best Number of Training Samples: For HWT-1, KEKRE DHT offers best performance of 11 training samples compared to 20 training samples for Orthogonal KEKRE transform. For HWT-2, KEKRE HADAMARD offers best performance of 6 training samples compared to 16 training samples for Orthogonal KEKRE transform. KEKRE combinations offer better performance for HWT-2 is better than HWT-1.
- Best state wise FRR–FAR: For HWT-1, KEKRE 128 offers best performance for 2 TO 5 states compared to combinations of KEKRE HWT. For HWT-2, KEKRE 128 offers best performance for 2 TO 5 states compared to combinations of KEKRE HWT. KEKRE combinations offer better performance for HWT-1 is better than HWT-2.
- Best Number of Symbol: Testing was carried out for number of symbols from 200 to 750. It evident that the best performance in terms of FRR–FAR, AAR–ARR, EER is offered by 275 symbols for HWT-1 and 450-500 symbols for HWT-2. KEKRE combinations offer better performance for HWT-1 is better than HWT-2.

		HWT-1						HWT-2			
Combinations	States	Symbols	Training sanples	FRR	FAR	Combinations	States	Symbols	Training sanples	FRR	FAR
DCT 128	2	300	16	5	10	DCT 128	5	475	11	27	32
DCT DHT	3	300	13	10	10	DCT DHT	5	400	10	31	34
DCT Haar	5	325	18	0	0	DCT Haar	4	425	9	30	33
DCT Hadamard	5	300	17	0	5	DCT Hadamard	5	400	10	30	42
DCT Kekre	3	300	17	5	5	DCT Kekre	5	500	18	9	9
DHT 128	4	350	15	5	10	DHT 128	5	500	12	24	30
DHT DCT	5	275	18	5	5	DHT DCT	4	500	9	31	37
DHT Haar	5	275	17	5	10	DHT Haar	5	500	10	29	37
DHT Hadamard	4	300	14	10	15	DHT Hadamard	5	500	11	31	28
DHT Kekre	4	275	20	0	5	DHT Kekre	5	475	16	13	19
Haar 128	2	275	13	10	30	Haar 128	5	475	13	24	28
Haar DCT	5	275	20	0	0	Haar DCT	5	500	11	31	24
Haar DHT	5	300	15	5	15	Haar DHT	5	450	11	26	21
Haar Hadamard	2	300	14	5	10	Haar Hadamard	5	425	10	30	33
Haar Kekre	3	275	19	0	0	Haar Kekre	5	500	17	11	12
Hadamard 128	5	350	14	5	15	Hadamard 128	5	475	9	32	32
Hadamard DCT	5	300	17	10	10	Hadamard DCT	5	500	12	27	26
Hadamard DHT	4	300	14	5	5	Hadamard DHT	5	500	10	29	29
Hadamard Haar	4	275	16	5	5	Hadamard Haar	4	500	10	31	30
Hadamard Kekre	5	275	20	0	0	Hadamard Kekre	5	500	14	25	22
Kekre 128	2	275	20	0	0	Kekre 128	4	475	19	5	2
Kekre DCT	5	275	20	0	0	Kekre DCT	5	500	13	27	27
Kekre DHT	5	275	18	5	5	Kekre DHT	4	350	8	30	36
Kekre Haar	2	525	20	0	0	Kekre Haar	5	500	14	21	21
Kekre Hadamard	2	550	19	100	0	Kekre Hadamard	5	500	13	23	21

		HWT-1	10 01 2000	1101 01		g samples for f		HWT-2			
Combinations	States	Symbols	Training sanples	FRR	FAR	Combinations	States	Symbols	Training sanples	FRR	FAR
DCT 128	3	300	15	15	15	DCT 128	2	275	4	35	63
DCT DHT	2	300	12	15	25	DCT DHT	3	325	7	33	50
DCT Haar	3	300	13	5	20	DCT Haar	3	375	6	33	47
DCT Hadamard	2	275	12	30	30	DCT Hadamard	4	325	6	30	51
DCT Kekre	3	300	17	5	5	DCT Kekre	2	450	11	22	30
DHT 128	2	350	13	10	20	DHT 128	2	375	7	32	40
DHT DCT	4	275	15	5	10	DHT DCT	2	500	8	33	43
DHT Haar	2	275	13	20	20	DHT Haar	2	350	6	34	46
DHT Hadamard	2	300	10	20	25	Dht Hadamard	4	275	5	29	52
DHT Kekre	2	275	19	5	5	DHT Kekre	2	475	12	23	27
Haar 128	2	275	13	10	30	Haar 128	2	325	6	32	57
Haar DCT	2	275	13	15	0	Haar DCT	4	350	7	32	52
Haar DHT	3	275	12	15	15	Haar DHT	2	375	6	37	49
Haar Hadamard	3	275	13	10	20	Haar Hadamard	3	275	5	32	57
Haar Kekre	3	275	19	0	0	Haar Kekre	3	400	12	20	33
Hadamard 128	2	275	8	35	30	Hadamard 128	2	475	5	38	52
Hadamard DCT	2	275	11	20	15	Hadamard DCT	2	375	6	30	45
Hadamard DHT	2	275	11	15	20	Hadamard DHT	3	300	6	31	49
Hadamard Haar	2	275	14	5	15	Hadamard Haar	2	425	8	34	37
Hadamard Kekre	2	275	18	10	10	Hadamard Kekre	2	500	11	34	31
Kekre 128	2	275	20	0	0	Kekre 128	2	450	16	11	16
Kekre DCT	2	275	13	10	15	Kekre DCT	2	425	9	31	37
Kekre DHT	2	275	11	15	25	Kekre DHT	4	350	8	30	36
Kekre Haar	2	525	20	0	0	Kekre Haar	2	500	10	33	38
Kekre Hadamard	2	550	19	100	0	Kekre Hadamard	2	375	6	34	49

Table 3. Best No. of training samples for HWT-1 and 2

Table 4. Best Statewise FRR FAR for HWT-1 and 2

		HWT-1						HWT-2			
Combinations	States	Symbols	Training sanples	FRR	FAR	Combinations	States	Symbols	Training sanples	FRR	FAR
DCT Haar	2	300	14	5	10	DCT Kekre	2	450	11	22	30
DCT Kekre	3	300	17	5	5	DCT Kekre	3	450	13	19	20
DCT Haar	4	275	15	10	10	DCT Kekre	4	450	15	17	18
DCT Haar	5	325	18	0	0	DCT Kekre	5	500	18	9	9
DHT Kekre	2	275	19	5	5	DHT Kekre	2	475	12	23	27
DHT Kekre	3	275	19	5	5	DHT Kekre	3	500	13	22	20
DHT Kekre	4	275	20	0	5	DHT Kekre	4	450	15	15	14
DHT DCT	5	275	18	5	5	DHT Kekre	5	475	16	13	19
Haar Kekre	2	275	19	5	5	Haar Kekre	2	450	12	21	35
Haar Kekre	3	275	19	0	0	Haar Kekre	3	400	12	20	33
Haar Kekre	4	275	20	0	5	Haar Kekre	4	475	16	14	22
Haar Kekre	5	275	20	0	0	Haar Kekre	5	500	17	11	12
Hadamard Kekre	2	275	18	10	10	Hadamard Kekre	2	500	11	34	31
Hadamard DHT	3	275	12	10	10	Hadamard Kekre	3	500	15	16	44
Hadamard DHT	4	300	14	5	5	Hadamard Kekre	4	500	13	25	27
Hadamard Kekre	5	275	20	0	0	Hadamard Kekre	5	500	14	25	22
Kekre 128	2	275	20	0	0	Kekre 128	2	450	16	11	16
Kekre 128	3	275	20	0	0	Kekre 128	3	500	17	10	11
Kekre 128	4	275	20	0	0	Kekre 128	4	475	19	5	2
Kekre 128	5	275	20	0	0	Kekre 128	5	475	19	5	2

From Tables 2-4, we get following important results.

- FRR–FAR: For HWT-1, DCT HAAR offers best performance with FRR and FAR of 0 %. For HWT-2, KEKRE 128 offers best performance of FRR 5 % and FAR 2 %. HWT-1 offers better performance than HWT-2.
- Number of training samples: For HWT-1, Orthogonal HADAMARD transform offers best performance of 8 training. For HWT-2, Orthogonal DCT transform offers best performance of 4 training samples. HWT-2 offers better performance than HWT-1.
- State wise FRR–FAR: For HWT-1, KEKRE 128 offers best performance for 2 to 5 states. For HWT-2, KEKRE 128 offers best performance for 2 to 5 states. HWT-1 offers better performance than HWT-2. As the number of states increase, the performance of the system improves. HWT-1 found to offer better performance for 3 to 5 states and HWT-2 for 5 states.
- Number of Symbol: For HWT-1, KEKRE 128 offers best performance at 275 symbols whereas for HWT-2, best performance is at 475 symbols by KEKRE 128.

The proposed system is compared with existing systems in Table 5. The proposed system offers better performance than the existing systems.

Table 5. C	Comparision	of proposed	system with	existing systems
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Paper	FAR (%)	FRR (%)
[13]	30	30
[14]	1.96	60.93
[15]	0	8
Proposed system	0	0

4. CONCLUSION

In the proposed system for online signature verification with pressure as feature vector, HWT-1 offers better performance than HWT-2 for various combinations of DCT, DHT, Haar and Hadamard orthogonal transform. But Kekre transform offers better performance than its various combination of HWT-1 and HWT-2. Comparing KNN, SVM and NN classifier with various dynamic parameters as feature vector, HMM offers better performance. This findings show that the HWT with HMM has been a feasible method for feature vector extracton of online signature vector based biometric systems.

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