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A Novel Method for Rotor Field-Oriented Control of Single-Phase Induction Motor

M. Jannati*, T. Sutikno**, N.R.N. Idris*, M.J.A. Aziz*

* UTM-PROTON Future Drive Laboratory, Faculty of Electrical Engineering, Universiti Teknologi Malaysia, 81310 Skudai, Johor Bahru, Malaysia

** Department of Electrical Engineering, Universitas Ahmad Dahlan, Yogyakarta, Indonesia

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ABSTRACT

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Keyword:

Drive system MATLAB Rotor field-oriented control Single-phase induction motor Transformation matrix This paper presents a novel rotor field-oriented control (RFOC) method for asymmetrical single-phase induction motor (SPIM). It is shown in this paper that by using a suitable transformation matrix (TM) for stator current variables, the asymmetrical equations of SPIM are transformed into symmetrical equations. Based on this similarity, a novel vector conrol technique for SPIM is presented. Performance of the proposed method is assessed using MATLAB/SIMULINK software. Simulation results showed the excellence speed and torque responses obtained using the proposed technique.

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Corresponding Author:

M. Jannati, UTM-PROTON Future Drive Laboratory, Faculty of Electrical Engineering, Universiti Teknologi Malaysia, 81310 Skudai, Johor Bahru, Malaysia. Email: jannatim94@yahoo.com

1. INTRODUCTION

Single-phase induction motors (SPIMs) are broadly implemented in low-power applications such as sub fractional and fractional horsepower applications for their low-cost and substantial reliability. A SPIM is fundamentally an unbalanced IM since it is constructed with two asymmetrical stator windings (main and auxiliary windings) with a squirrel-cage rotor.

To effectively control the torque and/or speed, SPIM is normally fed by power electronics converters. Different topologies of power converter have been used for variable-speed drives of SPIM [1]-[5]. Two-leg, three-leg, and four-leg converters are the three most widely used converters for SPIM. In general, three-leg and four-leg converters are more efficient as well as produce less harmonic distortion than a two-leg converter [4]. However, since two-leg configuration is cost-effective than the three-leg and four-leg, this configuration has been assumed in this study. The configuration of the two-leg SPIM drive system is shown in Figure 1 [4].

Scalar control method is quite popular technique for speed control of SPIM drive [6]-[8]. This control strategy is simple, economical, and well implementable. However, this control strategy provides slow reaction to transient and cannot be considered as an appropriate control strategy. Nowadays, direct torque control (DTC) [9], [10] and field-oriented control (FOC) [3]-[5] and [11]-[21] techniques have been widely adopted for SPIM drives for applications that require high performance torque control. Correa et al. has proposed FOC strategy using positive-negative double sequence current controller [5]. Although the proposed method, eliminate the torque pulsation of the SPIM but this method is complex, due to the using many PI controllers. In [11], decoupling vector control method with maximum torque per ampere was

proposed for vector control of SPIM. In [12]-[15], Stator FOC and Rotor FOC techniques for SPIM using feed forward decoupling controller have been presented. The presented control methods in [11]-[15] are extremely depends on variations of SPIM parameters. In [16]-[20], some methods for FOC of SPIM based on using transformation matrices (TMs) have been proposed. These methods are also depended on motor parameters.

In this paper it is shown that using suitable TM for stator current variables, the equations of the asymmetrical SPIM can be transformed into a structure of equations, which are similar to the 3-phase IM equations. Based on this, a novel and simple RFOC strategy for SPIM is developed and through simulation, is shown to give excellent dynamic performance. The remainder of this paper is organized as follows. The d-q model of the SPIM is presented in section 2. In section 3, the main idea of proposed vector control for SPIM is discussed and subsequently a novel control strategy based on RFOC is presented. The effectiveness of the proposed method is verified and presented using MATLAB/SIMULINK software in section 4. Finally, conclusion is presented in section 5.

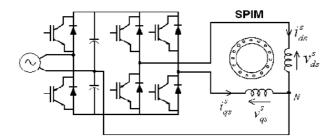


Figure 1. Configuration of the two-leg SPIM drive system

2. MATHEMATICAL MODELING

The SPIM equations in the stationary reference frame (superscript "s") can be written as (1) as presented in [5]:

$$\begin{aligned} \mathbf{v}_{dh}^{s} &= r_{dh} \dot{t}_{dh}^{s} + \frac{d\lambda_{dh}^{s}}{dt} \quad , \quad \mathbf{v}_{qr}^{s} = r_{qr} \dot{t}_{qr}^{s} + \frac{d\lambda_{qs}^{s}}{dt} \\ 0 &= r_{r} \dot{t}_{dr}^{s} + \frac{d\lambda_{dr}^{s}}{dt} + \omega_{r} \lambda_{qr}^{s} \quad , \quad 0 = r_{r} \dot{t}_{qr}^{s} + \frac{d\lambda_{qr}^{s}}{dt} - \omega_{r} \lambda_{dr}^{s} \\ \lambda_{ds}^{s} &= L_{ds} \dot{t}_{ds}^{s} + M_{d} \dot{t}_{dr}^{s} \quad , \quad \lambda_{qs}^{s} = L_{qs} \dot{t}_{qs}^{s} + M_{q} \dot{t}_{qr}^{s} \\ \lambda_{dr}^{s} \quad M_{d} \dot{t}_{dt}^{s} + L_{r} \dot{t}_{dr}^{s} \quad , \quad \lambda_{qr}^{s} \quad M_{q} \dot{t}_{qs}^{s} + L_{r} \dot{t}_{qr}^{s} \\ \tau_{o} &= \frac{Pole}{2} (M_{q} \dot{t}_{qs}^{s} \dot{t}_{dr}^{s} - M_{d} \dot{t}_{dt}^{s} \dot{t}_{qr}^{s}) \end{aligned}$$

$$\tag{1}$$

In (1), v_{ds}^s , v_{qs}^s are the stator d-q axes voltages i_{ds}^s , i_{qs}^s are the stator d-q axes currents i_{dr}^s , i_{qr}^s are the rotor d-q axes currents λ_{ds}^s , λ_{qs}^s are the stator d-q axes fluxes and λ_{dr}^s , λ_{qr}^s are the rotor d-q axes fluxes. r_{ds} , r_{qs} and r_r denote the stator and rotor d-q axes resistances. L_{ds} , L_{qs} , L_r , M_d and M_q indicate the stator, the rotor self and mutual inductances. ω_r is the motor speed. τ_e and τ_l are electromagnetic torque and load torque respectively. Moreover, J and F are the moment of inertia and viscous friction coefficient, respectively. As can be seen from (1), the structure of SPIM equations is similar to the 3-phase IM equations. In fact, by substituting $r_{ds}=r_{qs}=r_s$, $L_{ds}=L_{qs}=L_s$ and $M_d=M_q=M$ the familiar equations of 3-phase IM are obtained.

3. RFOC EQUATIONS OF SPIM

Since the SPIM studied is asymmetrical, the use of conventional FOC method for 3-phase IM requires a special attention. This asymmetry in SPIM model causes oscillations in the SPIM electromagnetic torque [5]. In this paper, it is shown using an appropriate TM for stator current variables, this asymmetry can be removed. The electromagnetic torque of SPIM can be written as:

$$\tau_e = \frac{Pole}{2} \left(M_q i_{qs} i_{dr} - M_d i_{ds} i_{qr} \right) \tag{2}$$

Using following substitutions,

$$i_{DS} = i_{ds} - ji_{qs}$$

$$i_{QS} = j \frac{M_d}{M_q} i_{ds} + \frac{M_d}{M_q} i_{qs}$$
(3)

The electromagnetic torque equation can be written as equation (4).

$$\tau_e = \frac{Pole}{2} \left(M_d i_{QS} i_{dr} - M_d i_{DS} i_{qr} \right) \tag{4}$$

As can be seen from (4), the SPIM torque equation becomes similar 3-phase IM torque equation. Equation (3) can be written as:

$$\begin{bmatrix} i_{DS} \\ i_{QS} \end{bmatrix} = \begin{bmatrix} 1 & -j \\ j \frac{M_d}{M_q} & \frac{M_d}{M_q} \end{bmatrix} \begin{bmatrix} i_{ds} \\ i_{qs} \end{bmatrix}$$
(5)

Using following substitutions,

$$1 \rightarrow \cos \theta_{e} \quad j \rightarrow \sin \theta_{e}$$

$$i_{DS} \rightarrow i_{ds}^{s} \qquad i_{ds} \rightarrow i_{ds}^{e}$$

$$i_{QS} \rightarrow i_{qs}^{s} \qquad i_{qs} \rightarrow i_{qs}^{e}$$
(6)

The TM for stator current variables can be obtained as equation (7).

$$\begin{bmatrix} i_{ds}^{s} \\ i_{qs}^{s} \end{bmatrix} = \begin{bmatrix} \cos\theta_{e} & -\sin\theta_{e} \\ \frac{M_{d}}{M_{q}}\sin\theta_{e} & \frac{M_{d}}{M_{q}}\cos\theta_{e} \end{bmatrix} \begin{bmatrix} i_{ds}^{e} \\ i_{qs}^{e} \end{bmatrix}$$
(7)

The inverse of (7) gives the proposed TM for stator current variables.

$$\begin{bmatrix} i_{ds}^{e} \\ i_{qs}^{e} \end{bmatrix} = \begin{bmatrix} T_{is}^{e} \end{bmatrix} \begin{bmatrix} i_{ds}^{s} \\ i_{qs}^{s} \end{bmatrix} = \begin{bmatrix} \cos \theta_{e} & \frac{M_{q}}{M_{d}} \sin \theta_{e} \\ -\sin \theta_{e} & \frac{M_{q}}{M_{d}} \cos \theta_{e} \end{bmatrix} \begin{bmatrix} i_{ds}^{s} \\ i_{qs}^{s} \end{bmatrix}$$
(8)

In (8), θ_e is the angle between the stationary reference frame and the rotating reference frame. In this paper superscript "e" indicates that the variables are in the rotating reference frame. Using (8) new mathematical model is obtained as (9)-(11). It can be noted that in the process of obtaining these equations (equations (9)-(11)) the assumption $\lambda_{dr}^e = |\lambda_r|, \lambda_{qr}^e = 0$ is considered.

Rotor flux equations:

$$\begin{bmatrix} |\lambda_r| \\ 0 \end{bmatrix} = \begin{bmatrix} M_d & 0 \\ 0 & M_d \end{bmatrix} \begin{bmatrix} i_{ds}^e \\ i_{qs}^e \end{bmatrix} + \begin{bmatrix} L_r & 0 \\ 0 & L_r \end{bmatrix} \begin{bmatrix} i_{dr}^e \\ i_{qr}^e \end{bmatrix}$$

$$T_r \frac{d}{dt} |\lambda_r| + |\lambda_r| - M_d i_{ds}^e = 0$$
(9)

Electromagnetic torque equation:

$$\tau_e = \frac{Pole}{2} \frac{M_d}{L_r} |\lambda_r| i_{qs}^e \tag{10}$$

Speed equation:

$$T_r(\omega_e - \omega_r)|\lambda_r| - M_d i_{as}^e = 0 \tag{11}$$

In (9) T_r is the rotor time constant $(T_r=L_r/r_r)$. As can be seen using (8), the asymmetrical equations of SPIM changed into symmetrical equations. The comparison between the RFOC equations of SPIM and RFOC equations of 3-phase IM is given in Table 1.

Table 1. The comparison between RFOC equations of SPIM and RFOC equations of 3-phase IM

	3-Phase IM	SPIM
Flux equation based on [22], (9)	$\left \lambda_{r}\right = \frac{Mi_{ds}^{e}}{1 + T_{r}\frac{d}{dt}}$	$\left \lambda_{r}\right = rac{M_{d}i_{ds}^{e}}{1+T_{r}rac{d}{dt}}$
	where:	where:
	$M=\frac{3}{2}L_{ms}$	$M_d = \frac{3}{2}L_{ms}$
Torque equation based on [22], (10)	$\tau_e = \frac{Pole}{2} \frac{M}{L_r} \lambda_r i_{qs}^e$	$ au_e = rac{Pole}{2} rac{M_d}{L_r} \lambda_r i_{qs}^e$
Speed equation based on [22], (11)	$\omega_e = \omega_r + \frac{M i_{qs}^e}{T_r \lambda_r }$	$\omega_e = \omega_r + \frac{M_d i_{qs}^e}{T_r \lambda_r }$

Therefore, using some changes in the conventional RFOC block diagram of 3-phase IM, vector control of SPIM is possible. The proposed block diagram of SPIM based on Indirect RFOC is shown in Figure 2. In Figure 2, $|\lambda_r^*|$ and τ_e^* represent the reference flux and torque respectively. In this Figure, the arrows show that the changes to the conventional vector control, that it can be applied to the SPIM. In summery the comparison between the proposed vector control of SPIM and conventional vector control of 3-phase IM is given in Table 2.

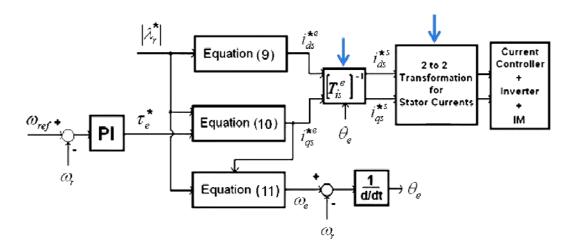


Figure 2. Proposed block diagram of IRFOC for SPIM

	phase IN	
	3-Phase IM	SPIM
$\begin{bmatrix} T_{is}^{e} \end{bmatrix} \text{based on [22],} $ (8)	$\begin{bmatrix} T_{is}^{e} \end{bmatrix} = \begin{bmatrix} \cos \theta_{e} & \sin \theta_{e} \\ -\sin \theta_{e} & \cos \theta_{e} \end{bmatrix}$	$\begin{bmatrix} T_{is}^{e} \end{bmatrix} = \begin{bmatrix} \cos \theta_{e} & \frac{M_{q}}{M_{d}} \sin \theta_{e} \\ -\sin \theta_{e} & \frac{M_{q}}{M_{d}} \cos \theta_{e} \end{bmatrix}$
2 to 2 or 2 to 3 transformation for stator current variables based on [22]	$\begin{bmatrix} i_{as} \\ i_{bs} \\ i_{cs} \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} +1 & 0 \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} i_{ds}^{s} \\ i_{qs}^{s} \end{bmatrix}$	$\begin{bmatrix} i_{as} \\ i_{bs} \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} i_{ds}^s \\ i_{qs}^s \end{bmatrix}$

Table 2. The comparison between proposed vector control of SPIM and conventional vector control of 3phase IM

4. SIMULATION RESULTS

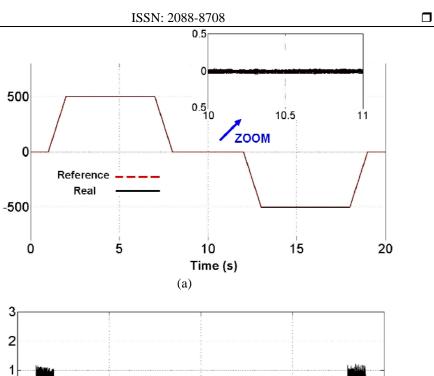
To verify the effectiveness of the proposed IRFOC for SPIM, simulations under different conditions are conducted using MATLAB/SIMULINK simulation package. In the simulations the reference rotor flux is set to 1wb. A vector control system, based on Figure 2 is used for a standard 0.25 HP SPIM with the rated values and parameters as shown in Table 3.

Voltage	90V
Frequency (f)	60Hz
No. of Poles	4
Power	0.25IIp
r _{ds}	7.14Ω
r _{as}	2.02Ω
M_q	0.1772H
r _y	4.12Ω
7. _{d5}	0.1885H
T, _{qs}	0.1844H
J	0.0146kg.m ²
F	0.0N.m.s

Table 3. Ratings and parameters of the simulated SPIM

Figure 3 (a) shows the simulation results of the reference and actual rotor speed based on proposed controller for a trapezoidal speed reference between 500rpm and -500rpm. It is evident from Figure 3 (a) that the real speed follows the reference motor speed even at zero reference speed. The electromagnetic torque and main and auxiliary stator currents for trapezoidal reference speed are shown in Figure 3 (b) and Figure 3 (c) respectively. It is shown that the proposed IRFO controller for vector control of SPIM has a good speed control and sufficient vector control characteristics.

Speed (rpm)



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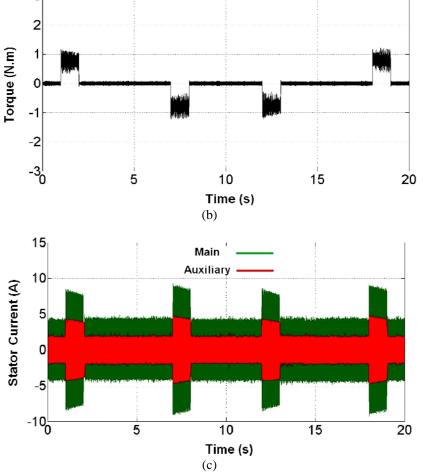


Figure 3. Simulation results of IRFOC for a trapezoidal reference speed

Figure 4 (a) shows the reference and real motor speed signals with a step reference speed from zero to the rated value at t = 2s. A load torque equal to 1Nm is introduced at t = 9s and removed at t = 11s. Due to the accuracy of the torque control, the actual speed follows the reference even when a load disturbance is introduced at t = 2s. The corresponding motor torque is shown in Figure 4 (b). It can be seen that the torque response rapidly with no pulsations.

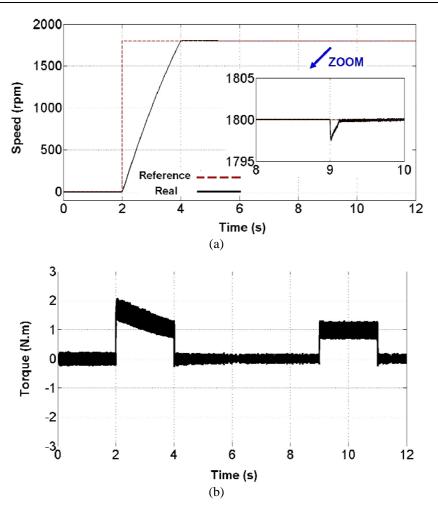


Figure 4. Simulation results of IRFOC at nominal reference speed and under load

5. CONCLUSION

In this paper, a novel method for speed control of SPIM based on IRFOC has been proposed. It is shown that using an appropriate transformation matrix (TM) for stator current variables, the unbalanced SPIM equations can be changed into balanced equations. Simulation results showed the excellence speed and torque responses obtained using the proposed technique. The drawback of presented method is that the motor speed of SPIM must be measured, which needs a speed sensor. To overcome this difficulty, a research to be conducted applying a novel method for speed sensorless FOC of SPIM.

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