pflow.py a Potential Flow Solver and Visualizer

Mechanical Engineering Technical Report 2017/12 Ingo Jahn School of Mechanical and Mining Engineering The University of Queensland.

July 28, 2018

Abstract

plow.py is a simple teaching and analysis tool for 2-D Potential Flows. It is a collection of code, that allows the construction of simple flow fields that meet the Potential Flow governing Equations. A range of plotting and visulisation tools are included.

This report is a brief userguide and example book.

Contents

1 Introduction

Potential Flow is a simple but powerful analysis approach to simulate inviscid flow. This report is the userguide for pflow.py a tool to analyse simple 2-D flows together with a selection of plotting and post-processing tools. The code allows flow-fields, consisting of the following building blocks to be analysed: Uniform Flow, Sink/Source, Irrotational Vortex, Doublet, and other user-define options.

The post-processing tool allows plotting of stream functions ψ , velocity vectors, velocity contour plots, and pressure contours. In addition post-processing tools are included to extract point data and data along lines.

1.1 Getting the Code

The code is distributed as part of the $HTDT$ - Heat engine $\mathcal C$ Turbomachinery Design Tools code under a GNU General Public License 3 license. The code can be downloaded from [https:](https://bitbucket.org/uqturbine/htdt/src) [//bitbucket.org/uqturbine/htdt/src](https://bitbucket.org/uqturbine/htdt/src). The source code and examples are located in the htdt/src/PotentialFlow/ and htdt/examples/PotentialFlow/ sub-directories respectively.

1.2 Dependencies and Installation

pflow.py is written in python. The following packages are required:

- python 2.7 or python 3.x- any standard distribution
- numpy
- matplotlib

There are two options to run and install pflow.py.

1.2.1 Easy Installation - Windows Users

- 1. Copy the file pflow.py and jobfile.py and any other files you want to use into the same directory.
- 2. Open spyder3 (available to download from <https://anaconda.org/anaconda/python>)
- 3. Navigate to the directory containing the files.
- 4. Run pflow.py with the following command in the spyder console: %run pflow.py --job=jobfile.py
- 5. The results will appear in the spyder console

1.2.2 More Complex Install - Linux Users & OS X users

This installation path is slighty more complex, but allows easier use of the code. For OS X:

From terminal, execute the following command: $\$ vi γ . profile and add the following two lines:

export PYTHONPATH=\${PYTHONPATH}:\${HOME}/path-to-file export PATH=\${PATH}:\${HOME}/path-to-file followed by restarting the terminal.

For Linux (e.g. UBUNTU): From terminal, execute the following command: $\$ gedit γ . profile and add the following two lines: export PYTHONPATH=\${PYTHONPATH}:\${HOME}/path-to-file export PATH=\${PATH}:\${HOME}/path-to-file followed by restarting the terminal.

The above steps ensure that $pflow.py$ is on the search path for executables and python modules. This allows the code to be executed from any directory using the command: \$\$ pflow.py --job=jobfile.py

1.3 Citing this tool

When using the tool in simulations that lead to published works, it is requested that the following works are cited:

• Jahn, I. (2017), pflow.py a Potential Flow Solver and Visualizer, *Mechanical Engineering* Technical Report 2017/12, The University of Queensland, Australia

2 Distribution

pflow.py is distributed as part of the code collection maintained by the CFCFD Group at the University of Queensland [\[1\]](#page-14-3). This collection is free software: you can redistribute it and/or modify it under the terms of the GNU General Public License as published by the Free Software Foundation, either version 3 of the License, or any later version. This program collection is distributed in the hope that it will be useful, but WITHOUT ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License for more details <http://www.gnu.org/licenses/>. Alternatively the code is included in the Appendix.

2.1 Modifying the code

You can modify and adjust the code to your heart's content. If you want to share the updated and modified code, please email an updated version together with a short description of the changes to the authors. Once reviewed the changes will be included in future versions of the code.

3 Using the Tool: 5-minute version for experienced python Users

If you understand python and know how the potential flow building blocks work, this is for you.

- 1. Find an existing example file, e.g. jobfile.py.
- 2. Change the number and type of building blocks used to assemble your potential flow field, e.g. $a1 = UniformFlow(1.0, 0.0)$. A full list of options is available in section [4.1.1.](#page-5-2)
- 3. Change the settings for how the flow will be visualised. E.g. plot.psi()
- 4. (Optional) Ask the code for an on-screen display of local flow conditions. E.g. screen.locations([[0.,-0.5], [0.,0.5]])
- 5. Save the job file.
- 6. Run the code:

If using spyder:

- Start spyder
- Navigate to the directory containing $pflow.py$ and your input file.
- Run the code from the spyder console with: %run pflow.py --job=jobfile.py (Replace jobfile.py with the name of your input file)

If running from terminal in Linux or OS X

- Open a terminal
- Navigate to the directory containing your input file (and pflow.py if you haven't added it to PATH and PYTHONPATH).
- Run the code from the terminal with the command pflow.py --job=jobfile.py (Replace jobfile.py with the name of your input file)
- 7. If you want to save your data, add the option --out-file=data.txt to your file

4 Using the Tool: Detailed explanation

4.1 Creating your Flow field

In potential flow, different flow features, *building blocks*, that full-fill Laplace's equation by themselves, are superimposed (added) in order to generate complex flow-field solutions. The first step in pflow.py is to define these building blocks, which can be combined to create the complex flow-field.

Step: 1

Create a file that details the simulation you want to perform. In this document the file is called jobfile.py. Within this file start by defining the model reference data. The following variables are available. If skipped the

mdata.name : (default $=$ "") name of simulation case.

mdata.dimensions : (default $= 2$) dimensions of domain. Currently limited to 2.

mdata.Pinf : (default $= 0$ Pa) free-stream pressure used for calculations

mdata.rho: (default = 1.225 kg/m^3) density used for flow calculations

mdate.Uinf: (default $=$ np.nan') If 'nan', this parameter will be calculated based on vector sum of all uniform flow fields that are defined. Alternatively if an integer or float is defined, this value will be used.

Step: 2

 \overline{C}

Within the file define the building blocks you are using to construct your flow solution. The following code section defines Uniform Flow with $U = 5$ m/s, $V = 0$ m/s and a Source located at $(0.5, 0.1)$ with a net flow rate of 5 kg/s/m :

```
# Uniform Flows
A1 = UniformFlow (5., 0., \text{label} = \text{U-Flow'})# Sources
D1 = Source(0.5, 0., 5., label='Source 1')
```
See section [4.1.1](#page-5-2) for a list of possible options and detailed descriptions.

4.1.1 Building Blocks

Currently the following Building Blocks are supported.

Uniform Flow: UniformFlow(u, v, label=')'

This creates a uniform flow with the velocity components u and v in the x- and y-direction respectively. The velocity vectors for the flow-field are shown in Fig. [1a.](#page-7-2) The streamfunction is defined as:

$$
\Psi = u \, y - v \, x \tag{1}
$$

Source: Source(x0, y0, m, label=')'

This generates a source (use -ve m for sink) located at the position defined by (x_0, y_0) . Velocity vectors for the flow-field are shown Fig. [1b.](#page-7-2)

The streamfunction is defined as:

$$
\theta = \tan^{-1}\left(\frac{y - y_0}{x - x_0}\right) \tag{2}
$$

$$
\Psi = \theta \frac{m}{2\pi} \tag{3}
$$

Vortex: $Vortex(x0, y0, Gamma=Gamma, label=')'$ or $Vortex(x0, y0, K=K, label=')'$

This generates an irrotational vortex of circulation Γ or strength K, depending on whether **Gamma=** or K= is specified, with the core locates at $(x0, y0)$ (If K is supplied, circulation is calculated as $\Gamma = 2 \pi K$). Velocity vectors for the flow-field are shown Fig. [1c.](#page-7-2) The streamfunction is defined as:

$$
r = \left[(x - x_0)^2 + (y - y_0)^2 \right]^{\frac{1}{2}}
$$
 (4)

$$
\Psi = -\frac{\Gamma}{2\pi} \ln r = -K \ln r \tag{5}
$$

Doublet: Doublet(x0,y0,a,U_inf,label=')'

This generates the flow field known as a doublet. This is generated if a source and sink are brought very close together with a separation $s = \frac{a^2 \pi U_{\infty}}{m}$ in the flow direction. $\pm m$ is the strength of the source and sink. The center of the doublet is located at (x_0, y_0) . Velocity vectors for the flow-field are shown Fig. [1d.](#page-7-2)

The streamfunction is defined as:

$$
\Psi = U_{\infty} (y - y_0) \frac{-a^2}{(x - x_0)^2 + (y - y_0)^2}
$$
\n(6)

This doublet works only for flow in the $+x$ directions. For other flows modify the code or manually generate a doublet by bringing together a source and sink, aligned with the flow direction.

User defined: User_Defined(x0,y0,n,label=')'

This generates the streamlines for flow around a 90[°] corner, located at position. Velocity vectors for the flow-field are shown Fig. [1e.](#page-7-2)

The streamfunction is defined as:

$$
\Psi = n (x - x_0) (y - y_0) \tag{7}
$$

Name Name(x0,y0,Var1,Var2,Var3,label=')'

This is a template for future building blocks that you may want to implement. The block class must have the following functions and components:

- instances = [] This ensures all instances of the class are collected.
- \bullet $__init__ (self, \ldots)$ This initializes the function and reads in the initial settings self.__class__.instances.append(self) This appends the current instance to the instances list.
- evaP(self,x,y) This returns the value of the stream function, Ψ at the point defined by the coordinates (x, y)
- eval(self,x,y) This returns the value of the u and v velocity at the point defined by the coordinates (x, y) . This should be the analytical solution to $\frac{d\Psi}{dy}$ and $-\frac{d\Psi}{dx}$.

Figure 1: Building Blocks available to generate Potential Flow solutions.

4.2 Define the range and resolution for your simulation

After the building blocks have been defined, the next step is to define the range over which the data will be solved and how the data is visualised and plotted. This is done by adjusting the settings of the visual class.

Step: 3 (optional)

Use the following settings to adjust how much (x-range and y-range) is plotted and the resolution of the data:

visual.xmin : (default = -1.) sets x_{min} for plots

visual.xmax : (default = 1.) sets x_{max} for plots

visual.ymin : (default = -1.) sets y_{min} for plots

visual.ymax : (default = 1.) sets y_{max} for plots

visual.Nx : (default = 50) number of points used for discretisation in x-direction. Larger values will create better plots, but this will slow down the code.

visual. Ny : (default $= 50$) number of points used for discretisation in y-direction

visual.subplot : (default $= 0$) sets whether to plot individual graphs or to plot all graphs in a single figure.

0 - all individual graphs;

1 - subplots in single figure.

4.3 Plotting the results for PSI, U, V, ...

Once the area and visualisation settings have been defined, you now must define what is plotted.

Step: 4

Use the following commands to create different types of graphs.

- plot.psi(levels=20) : plots 'real' streamlines, contours of psi. Use levels to set number of contours.
- plot.psi_magU(min=[], max=[], levels=20) : create contour plot of velocity magnitude with overlaid stream functions. Use min and max to specify range and levels to set numbers of contours.
- plot.vectors() : plots nice looking velocity vectors. Note these are not equi-potentials of streamfunction, Ψ.
- plot.vectors_magU(min=[], max=[], levels=20) : create contour plot of velocity magnitude with overlaid velocity vectors. Use min and max to specify range and levels to set numbers of contours.
- plot.magU(min=[], max=[], levels=20) : create contour plot of velocity magnitude. Use min and max to specify range and levels to set numbers of contours.
- plot.U(min=[], max=[], levels=20) : create contour plot of U velocity. Use min and max to specify range and levels to set numbers of contours.
- plot. V(min=[], max=[], levels=20) : create contour plot of V velocity. Use min and max to specify range and levels to set numbers of contours.
- plot.P(min=[], max=[], levels=20) : create contour plot of pressure. $P = P_{inf} \frac{1}{2} \rho |U|^2$. Use min and max to specify range and levels to set numbers of contours. P_{inf} and ρ are defined as part of the model settings (see section [4.1\)](#page-5-1).
- plot.Cp(min=[], max=[], level=20) : create contorus of pressure coefficient C_p . $C_p = 1$. $P/(\frac{1}{2} \rho U_{inf}^2)$. Use min and max to specify range and levels to set numbers of contours. U_{inf} and ρ are defined as part of the model settings (see section [4.1\)](#page-5-1).

For example, to create two graphs, one showing stream-functions, Ψ , and one showing velocity vectors super-imposed with velocity magnitude (velocity range limted to $[0., 10.]$), use the following code:

plot \cdot vectors_magU(min = [0.], max = [10.], levels = 20) $plot.psi (levels = 20)$

The results are shown in Fig. [2.](#page-9-1)

4.4 Extracting data

In addition to plotting the data it is also possible to evaluate the properties at single points or along lines.

Step: 5

 Γ

The display of data on screen is achieved using the following commands

screen.variables(['Psi', 'magU', 'P']) : This defines the parameters that will be evaluated. The following variables are available:

Psi : Value of streamfunction magU : Velocity magnitude U : x-component of velocity

locity magnitude (magnitude capped at 10 m s^{-1}).

Figure 2: Streamline and Streamline + Velocity magnitude plots generated for flow-field generated by UniformFlow and Source

- V : y-component of velocity
- P : pressure Cp : pressure coefficient
- screen.locations($\left[x0,y0\right], \left[x1,y1\right], \ldots \right]$) : Extracts the local values at the points with coordinates $(x0, y0)$ and $(y0, y1)$.
- screen.Lineval($[x0,y0], [x1,y1], N=10$) : Extracts the local values at $N = 10$ equally spaced points between $(x0, y0)$ and $(y0, y1)$.

The following code extracts stream function, Ψ , velocity magnitude, and pressure at the points $(-0.5, -0.5)$ and $(-0.5, 0.5)$, and also along the line between $(-1.0, 0.0)$ and $(1.0, 0.0)$.

 $#$ Extract data along lines screen.locations ($[[-0.5, -0.5], [-0.5, 0.5]$]) screen. Lineval $(-1., 0.], [1., 0.], N=9)$

A screen grab of the result is shown in Fig. [3.](#page-10-0) As expected, pressure and velocity are infinite at the center of the source.

4.5 Saving data

The setup of a simulation and the data displayed on screen can also be written to an output file. To achieve this run pflow.py with the --out-file=datafile.txt, where *datafile.txt* can be any file name. For example:

```
%run pflow.py --job=jobfile.py --out-file=Test1.txt (For use in spyder)
pflow.py --job=jobfile.py --out-file=Test1.txt (For use in from terminal)
will save your data to Test1.txt, which can be opened with any text editor.
```


Figure 3: Stream function value, velocity magnitude and pressure evaluated at discrete points.

5 Example - Vortex near wall

This example shows how Potential_Flow.py can be used to analyse the flow field generated by a uniform flow parallel to a wall and a vortex positioned at a distance of 0.5 m from the wall. The problem is illustrated in Fig. [4a.](#page-11-1)

positioned behind the wall, a straight streamline representing the wall is created.

Figure 4: Example case, consisting of uniform flow and a vortex positioned near a wall.

In order to generate the effect of a wall (straight streamline) one can use the principle of symmetry. Thus the problem we actually solve using Potential Flow theory is the one shown in Fig. [4b,](#page-11-1) which consists of three building blocks. The Uniform Flow, the Vortex at (0.0, 0.5) and a mirror image (about the x-axis) of the Vortex, located at $(0.0, -0.5)$. By symmetry this generates a straight streamline along the x-axis, which is equivalent to a wall (by definition no flow crosses a streamline, making it equivalent to a wall).

The appropriate code, defining the Uniform Flow, with a strength of 5.0 and vortices with a strength of ± 5.0 is given below. First the building blocks are generated as variables A1, C1, and C2. Then the extend of the grid over which we solve the flow-field is defined as ± 2 in the x-direction and ± 1 in the y-direction.

The results from the plotting functions, showing field data and data along the wall, are shown in Fig. [5.](#page-13-0) The obtained velocity in the wall parallel direction equals the analytical solution to the problem, given by

$$
U_T(x) = U_{\infty} + \frac{\Gamma h}{\pi (x^2 + h^2)}
$$

= 5.0 + $\frac{5.0 \times 0.5}{\pi (x^2 + 0.5^2)}$

$$
U_T(0) = 5.0 + 3.18 = 8.18
$$
 (8)

 $#$ set model parameters

mdata . name $=$ 'Vortex $+$ Uniform Flow adjacent to a wall ' $mdata$. dimensions = 2

```
# Define the Components
a1=Vortex (0.0, 0.5, Gamma=-5., label='Vortex')a2=Vortex (0.0, -0.5, Gamma=5., label='Vortex')b=UniformFlow(5.,0.)# Define how the solution will be visualised.
v is u al . xmin =−2.
visual . xmax =2.visual.subplot = 0plot. psi (levels = 20)
plot vectors_magU (min=0., max=20.)
plot.P(min=-100, max=0)# Define what is printed to screen
s c r e e n . v a r i a b l e s ( [ 'Psi', 'U', 'V', 'P'] )screen. Lineval ([-2.0, 0.0], [2.0, 0.0], N=19)
```
(see section [7.1](#page-14-2) for a more detailed input template)

As expected along the wall $(y = 0.0)$ the flow velocity in the vertical direction (V) is zero, as one would expect for a wall. Similarly the component of fluid velocity along the wall (U) is seen to accelerate, which results in a pressure reduction.

These results show the ability of potential flow to create simple flow fields, but it also highlights that potential flow is inviscid. If a real fluid, with viscosity, was used the x-component of velocity would be zero also. Nevertheless solutions created using potential flow are accurate for conditions and geometries, where the effects of viscosity are small.

Figure 5: Flow field and flow properties obtained from a uniform flow with u-velocity of $5.0 \,\mathrm{m/s}$ and a vortex with a strength of −5.0 positioned 0.5 m from a wall running along the x-axis.

6 References

References

7 Appendix

 Γ

7.1 Template for jobfile.py

```
1 """
 2 Template input file for HX_solver.py
3 """
 4
 5\# set model parameters
 6 """
7 Set parameters that define model conditions (optional)
\begin{array}{ll}\text{s} \; m \; data.\; Pinf & - \; (default = 0 \; Pa) & \text{s} \;ets \; P-infinity \; used \; in \; calculations\; \text{s} \; m data. \; rho & - \; (default = 1.225 \; kq/s) & \text{s} \;ets \; density \; used \; for \; calculations \end{array}\theta mdata . rho - ( default = 1.225 kg/s) sets density used for calculations
10 mdata. Uinf - (default = np.name \, m/s) sets U-infinity used in calculations.
11 If NaN this will be calculated automatically.
12 """
13 \text{ mdata.name} = 'Vortex + Uniform Flow adjacent to a wall'_{14} mdata. dimensions = 2
15
16 \# Define the Building Blocks
17 """
18 The following is a short summary of the supported components. See the User-Guide
19 for more detailed instructions and detailed definition.
20
21 A = UniformFlow(Vx, Vy, lab\,el = 'UFlow1'')22 creates a uniform with velocity magnitude and direction defined by the
23 x and y components Vx and Vy
24
25 B = Vortex (Cx, Cy, K=K, lab \, e \, l = 'Vortex 1')26→> creates a irrotational vortex located at (Cx, Cy) with a strength27 K = Gamma / (2 * pi). A positive Gamma results in a vortex rotating in
28 the anticlockwise direction.
29
30 B = Vortex (Cx, Cu, Gamma = Gamma, la b e l = Vortex 1')31 \rightarrow creates a irrotational vortex located at (Cx, Cy) with a strength Gamma. A
32 positive K results in a vortex rotating in the anticlockwise direction.
33
34 C = Source (Cx, Cy, m, lab \, el = 'Source1')35 \rightarrow creates a source/sink located at (Cx, Cy). m is the mass flow rate (per unit
36 depth) coming out of the source. Use +ve m for source and -ve m for sinks
37
38 D = Double t (Cx, Cu, R, Unf, lab e l = 'Double t1'')39 \rightarrow creates a doublet (co-located source and sink) located at (Cx, Cy). R sets
40 the radius of the enclosing streamline that is generated. When used in
41 conjunction with a uniform flow to show the flow around a cylinder, set
\Delta 42 Ux and Uy to match the x and y components of the uniform flow.
43
44 E = User\_Defined(Cx, Cy, n, label = 'user1')45 \rightarrow Secret. Try it out and see if you can work out what it is.
```
^[1] CFCFD, The Compressible Flow Project <http://cfcfd.mechmining.uq.edu.au> The University of Queensland

```
47 """
48
49 a1=Source (0.5, 0.0, 10., label='Source')
_{50} b=UniformFlow (5., 0.)51
52 \# Define how the solution will be visualised.
53 \stackrel{\prime}{\overline{\phantom{0}}\phantom{0}} 53 \stackrel{\prime}{\overline{\phantom{0}}\phantom{0}}54 By use the following settings to adjust the visaulisation.
55 -−−− Define plotting Window -<br>56 visual.xmin - (default =
 56 visual.xmin - ( default = -1.) sets x_min for plots
 57 \; visual \; . \; max \qquad - \; ( \; default \; = \; 1 \; . \; ) \; \; sets \; \; x \; \textit{max} \; \; for \; \; plots58 visual . ymin -(default = -1.) sets y_min for plots<br>59 visual . ymax -(default = 1.) sets y_max for plots
                       \overline{\phantom{x}} ( default = 1.) sets y_max for plots
60 v i s u al . Nx - ( default = 50) number of points used for discretisation
\sum_{i=1}^{n} \frac{1}{i} \sum_{i=1}^{n} \frac{1}{i62 \text{ visual } Ny = (default = 50) \text{ number of points used for discretisation}is a linear function in x-direction64 visual . subplot - ( default = 0) 0 - all individual graphs; 1 - subplots in\begin{array}{c} \text{65} \\ \text{65} \end{array} single figure
66
67 -− Define what is plotted –
68 plot psi (levels = 20) - plots 'real' streamlines, contours of psi. Use levels to
69 set number of contours.
70 plot . psi_magU(min=[], max=[], levels=20) – create contour plot of velocity
71 magnitude with overlaid stream functions. Use min and
\begin{array}{ccc} \textit{max} & \textit{to} & \textit{specify} \textit{range} & \textit{and} & \textit{levels} & \textit{sets} & \textit{numbers} & \textit{of} & \textit{contours} \,. \end{array}73~plot. vectors() - plots nice looking streamlines. Note these are not{ <br>equ qipotentials \hspace{.2in} of \hspace{.2in}psi} .
75 plot . vectors_magU(min=[], max=[], levels=20) - create contour plot of velocity
<sup>76</sup> magnitude with overlaid velocity vectors. Use min and
max to specify range and levels sets numbers of contours.
78 plot mapU(min=[], max=[], levels = 20) - create contour plot of velocity magnitude.
79 Use min and max to specify range and levels sets numbers
\delta so \delta f contours.
s_1\ plot\ J(\ min = []\ ,\ \ max = []\ ,\ \ level = 20) - create\ contour\ plot\ of\ U\ velocity\ .\ Use\ min\begin{array}{c} \text{82} \\ \text{83} \end{array} and max to specify range and levels sets numbers of
                                       control.83 plot V(min=|], max=|], levels=20 – create contour plot of V velocity. Use min
\begin{array}{c} \text{84} \\ \text{84} \end{array} and max to specify range and levels sets numbers of
                                       \cot\theta \cos\theta\textit{ s5 plot.} P\big(\,P\_\textit{inf} = 0\,\textit{.,}\quad\textit{rho} = 1.225\,,\;\; \textit{min} = [\,]\,,\;\;\textit{max} = [\,]\,,\;\;\textit{level}\,s = 20\big) \;-\;\textit{create contour plot of}86 pressure, using P-inf and rho to perform the calculation.
 87 P = P_{in}f - 1/2 * rho * magU**2. Use min and max to
88 specify range and levels sets numbers of contours.
89 plot . Cp (U \_in f = 1., rho = 1.225, min = [], max = []) – create contorus of pressure
90 coefficient C_p, using U-inf and rho to perform the
a \, l \, c \, u \, l \, a \, t \, i \, o \, n \;.92 Cp = P / (1/2 * rho * U_inf**2)93 """"
94
95 visual.xmin=−2.
96 v i s u a l . xmax = 2.
97 \text{ visual } . \text{ subplot} = 098
99 plot psi ( levels = 20 )
100 plot . vectors_magU (min=0., max=20.)
_{101} plot . P(min=−100, max=0)
102
103
104 \# Define what is printed to screen
105
```
46

```
106−−−− De f ine what i s d i s p l a y e d −−−−
107 screen.variables (['Psi','magU','U','V','P','Cp']) - provide list of parameters
       th a twill be evaluated. (default ['Psi', 'P'); 'magU'])109\;s\,c\,reen\;.\;loc\;ations\; (\left(\begin{array}{c} \left\lceil x0\,,y0\right\rceil,\;\;\left\lceil x1\,,y1\right\rceil,\;\;\left\lceil x2\,,y2\right\rceil,\;\;\ldots\;\right\rceil\;\;\right)\;-\;\;provided\;list\; of\;points110 where to evaluate data
111 screen. Lineval ([x0, y0], [x1, y1], N=5) -evaluates conditions at N equally
112 spaced points between (x0, y0) and (x1, y1)113 """
114
115 screen variables([ 'Psi', 'U', 'V', 'P')]116 screen.Lineval ([-2.0,0.0], [2.0,0.0], N=19)
```
7.2 Source Code: pflow.py

 \mathbb{R}^n

The source code for pflow.py is available from the htdt repository. [https://bitbucket.org/](https://bitbucket.org/uqturbine/htdt/src) [uqturbine/htdt/src](https://bitbucket.org/uqturbine/htdt/src) and located in the htdt/src/PotentialFlow/ directory