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Type Ic supernova of a $22 M_{\odot}$ progenitor

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ABSTRACT

Type Ic supernovae (SNe Ic) are a sub-class of core-collapse SNe that exhibit no helium or hydrogen lines in their spectra. Their progenitors are thought to be bare carbon–oxygen cores formed during the evolution of massive stars that are stripped of their hydrogen and helium envelopes sometime before collapse. SNe Ic present a range of luminosities and spectral properties, from luminous GRB-SNe with broad-lined spectra to less luminous events with narrow-line spectra. Modelling SNe Ic reveals a wide range of both kinetic energies, ejecta masses, and ^{56}Ni masses. To explore this diversity and how it comes about, light curves and spectra are computed from the ejecta following the explosion of an initially $22 M_{\odot}$ progenitor that was artificially stripped of its hydrogen and helium shells, producing a bare CO core of $\sim 5 M_{\odot}$, resulting in an ejected mass of $\sim 4 M_{\odot}$, which is an average value for SNe Ic. Four different explosion energies are used that cover a range of observed SNe. Finally, ^{56}Ni and other elements are artificially mixed in the ejecta using two approximations to determine how element distribution affects light curves and spectra. The combination of different explosion energy and degree of mixing produces spectra that roughly replicate the distribution of near-peak spectroscopic features of SNe Ic. High explosion energies combined with extensive mixing can produce red, broad-lined spectra, while minimal mixing and a lower explosion energy produce bluer, narrow-lined spectra.

Key words: radiative transfer – supernovae: general.

1 INTRODUCTION

Stripped envelope supernovae (SESNe) are the explosions following core collapse of stars which experience significant mass-loss during their evolution (Woosley & Eastman 1997). This mass-loss may be due to binary interaction or may occur through periods of high mass-loss, with rates of 10^{-4} to $10^{-5} M_{\odot} \text{ yr}^{-1}$ (Nomoto, Iwamoto & Suzuki 1995; Trammer, Sana & de Koter 2016). If the hydrogen envelope is mostly stripped away the SN is of Type IIb; if the entire hydrogen envelope and parts of the helium are stripped the SN is of Type Ib, and if all of the hydrogen and most of the helium are stripped a Type Ic results (Filippenko et al. 1995). With no hydrogen envelope recombining to power a plateau-like phase typical of Type IIP (Eastman et al. 1994), the primary source of luminosity in these SESNe is thought to be the radioactive decay of ^{56}Ni .

Prentice & Mazzali (2017) described a way to sub-classify SESNe starting from two basic classes: He-rich and He-poor SNe. For He-rich SNe, like Type IIb/Ib, the classification scheme is based

on the strength, velocity, and absorption/emission ratio of the $H\alpha$ lines. For He-poor SNe, like Type Ic/Ic-BL, the focus is instead on the number of commonly visible absorption lines, defined as N , present in the spectra at or near maximum luminosity, in the commonly observed wavelength range 4000–8000 Å. The number of absorption features in the spectra is dependent on the density and velocity profiles of the line-forming region, the composition of the ejecta, and the epoch of observation. These factors determine the strength and degree of blending of the various features, which can change over the evolution of the ejecta as the line-forming region recedes deeper into the ejecta. A set of absorption features commonly observed in the spectra of Type Ic SNe, including the three strongest Fe II multiplet 48 lines near 5000 Å, Na I D 5895, Si II 6355, the O I 7774 feature, and the Ca II NIR triplet, are considered (Filippenko 1997). These lines are in the optical part of the spectra and are observable from ground-based telescopes, but good S/N is needed to prevent erroneous classifications, especially in the Fe II lines.

A number of methods can be used to determine the basic properties of the explosion, such as ejected mass (M_{ej}), kinetic energy (E_{k}), and the mass of newly synthesized ^{56}Ni , and therefore

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Table 1. The kinetic energy, total mass, ejecta mass, ^{56}Ni mass, and the ratio E_k/M_{ej} for the four models used in this work. The difference in total and ejected mass is related to the explosion mechanism used and is discussed in Section 2.1 along with the possibly uncertain ^{56}Ni mass.

Energy [10^{51} erg]	M_{tot}/M_{\odot}	M_{ej}/M_{\odot}	M_{Ni}/M_{\odot}	E_k/M_{ej} (10^{51} erg/ M_{\odot})
1	4.46	3.35	0.097	0.29
3	5.15	3.74	0.147	0.80
5	5.26	4.01	0.187	1.24
8	5.3	4.05	0.224	1.97

infer the mass of the progenitor star. The methods described in Arnett (1982) (Arnett’s Rule) use the light curve of the SNe to estimate the kinetic energy of the explosion and approximate the mass of the ejecta. The light curves of Type Ic SNe can be reproduced with multiple combinations of E_k , mass M_{ej} , and the opacity of the ejecta (Iwamoto et al. 1998). Photospheric and nebular spectra of the SNe can be used to refine the M_{ej} measurement as well as determine the elemental abundances in the ejecta (Stehle et al. 2005; Mazzali et al. 2008). Photospheric spectra are obtained early in the evolution of the SN and thus can only probe the outer layers of the ejecta. The transition from the photospheric phase to the nebular phase occurs approximately 6–12 months after the explosion. At this point the ejecta has expanded and become sufficiently optically thin, so that the spectrum changes from a blackbody-like continuum with absorption features to an emission-line spectrum (Maurer et al. 2010). Nebular-epoch spectroscopy probes the innermost region of the ejecta. Modelling the spectra at both these stages, one can determine the density/abundance structure in the ejecta. This density structure can be used to calculate a mass and combined with the abundance stratification, a synthetic light curve can be computed that can be compared to the observed light curve.

Evidence from photospheric and nebular spectra shows that the explosion mechanism of the ejecta of SESNe are likely asymmetric in nature (Mazzali et al. 2005; Maeda et al. 2008; Wang & Wheeler 2008; Tanaka et al. 2009; Taubenberger et al. 2009; Chornock et al. 2011; Mauerhan et al. 2015; Stevance et al. 2017). Asymmetry in the explosion mechanism can lead to significant amounts of turbulent mixing, which is probably a key factor in the explosion mechanism of core-collapse SNe (Burrows, Hayes & Fryxell 1995; Herant 1995; Janka & Mueller 1996). Other work regarding the effect mixing has on the light curve and spectra of Type Ib/c has been done by Dessart et al. (2012) and Yoon et al. (2019), but focus mostly on the extremely early phases of the SNe. The extent of this mixing is important in matching models to observations, such as the case of SN 1987A, which contained high-velocity ^{56}Ni bullets in the hydrogen-rich outer ejecta (Hanuschik 1988; Shigeyama & Nomoto 1990). Taddia et al. (2019) also require high mixing of ^{56}Ni to replicate the light curves of broad-lined Type Ic SNe. However, mixing this material in a 1D code is an approximation to an inherently 3D process and requires a method to emulate the range of possible mixing processes. 3D simulations can match the observed ^{56}Ni velocity in SN 1987A (Utrobin et al. 2019) but the time and computing costs of these simulations limit their modelling efficiency.

In this work, we consider an evolved stellar model and explore its predictive ability as a progenitor. The model is evolved in a single star calculation and prior to collapse it is artificially stripped of its H/He layers, such that the resulting spectra should resemble those of SNe Ic. The methodology of the synthetic spectroscopy and photometry is discussed in Section 2. We consider the original model, a partially mixed model, and a fully mixed model. In Section 3, we

present the bolometric light curves and synthetic spectra generated for all explosion energies and mixing approximations. In Section 4, we classify our synthetic spectra based on the physical classification system previously discussed. In Section 5, we compare the models to the time-dependent spectra and photometry of several well-sampled SNe. In Section 6, we discuss the results and in Section 7, we summarize our results and consider future extensions.

2 METHODS

In the following sections, we describe the methods used to generate the bolometric light curves and synthetic spectra.

2.1 Progenitor models

The $22 M_{\odot}$ progenitor model used in this work is a modified version of the $22 M_{\odot}$ non-rotating solar metallicity model generated by Woosley, Heger & Weaver (2002). This model is artificially stripped of its outer hydrogen and helium shells as the physical mechanism to remove the mass is not the focus of this work. This leaves a carbon–oxygen (CO) core of ≈ 4.5 to $5.25 M_{\odot}$. The mass of the CO core changes as the explosion energy increase due to the explosion mechanism used and is discussed in detail later. After a compact remnant is formed and removed from the model, the final ejected mass is ≈ 3.3 – $4 M_{\odot}$, depending on the explosion energy, as shown in Table 1. α -rich freeze-out in the innermost core produces helium, but no He is present in the atmosphere as any helium in the outermost region that was produced or mixed during the evolution of the star is stripped from the model prior to core collapse.

Some SNe Ic, such as SN 1998bw, may eject as much as 8– $10 M_{\odot}$ of material with E_k of several 10^{52} erg after the stripping of a 30– $50 M_{\odot}$ progenitor (Galama et al. 1998; Iwamoto et al. 1998; Mazzali et al. 2001b), while others, such as SN 1994I, have ejecta masses estimated to be ~ 1 – $2 M_{\odot}$ and $E_k \sim 1$ – 2×10^{51} erg (Sauer et al. 2006). Prentice et al. (2019) estimated ejecta masses using Arnett’s rule and found that SNe Ib/c have a broad range of masses. Using this method, GRB-associated SNe Ic have a mean $M_{\text{ej}} = 4.7 \pm 1.5 M_{\odot}$, while more narrow-lined SNe Ic have a mean $M_{\text{ej}} = 3.2 \pm 2.4 M_{\odot}$. The mass ejected in our models is thus a ‘mean’ SN Ic mass, but it does not represent any group in particular, and is only the first step in our effort to model various progenitor masses.

Using the physical classification system from Prentice & Mazzali (2017), GRB-SNe have $N = 3$ – 4 , while more narrow-lined SNe have $N = 6$ – 7 , where N is defined as the number of visible features, such that increased blending leads to a smaller value of N . The value of N is set primarily by E_k . Just like M_{ej} , E_k also covers a wide range. In order to represent this spread of E_k , we exploded our $22 M_{\odot}$ progenitor with four different energies.

The SN explosion is simulated with a 1D hydrodynamics code with neutrino transport called PROMETHEUS-HOTB, described in

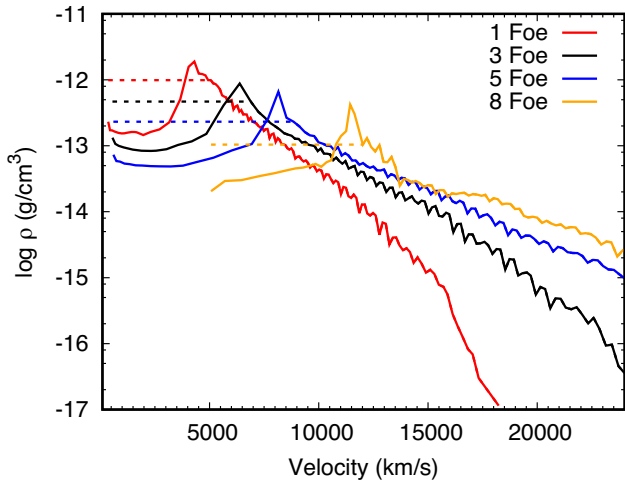


Figure 1. The density profiles of the four explosion models at the onset of homologous expansion, or approximately five days after the onset of the explosion (fully drawn lines). The dashed lines show the flattened density structures used for the fully/partially mixed models. The mass of the flattened region is 0.997, 1.33, 1.35, and 1.66 M_{\odot} for the 1, 3, 5, and 8 foe models, respectively. The majority of this mass is contained with the density peaks visible in the original density structures. The jagged behaviour of the density profiles is magnified by the logarithmic scaling and does not affect the evolution as much as the primary density spike.

more detail in Janka & Mueller (1996) and Ugliano et al. (2012). The neutrino heating used to generate the explosion is artificially enhanced in order to achieve final explosion energies of 1, 3, 5, and 8×10^{51} erg, respectively. This energy is deposited after core bounce in the surroundings of the newly formed neutron star over a time-scale of several seconds. This is supposed to mimic, in a parametric way, the dynamical consequences of an engine that generates thermal energy by neutrinos or magnetic field effects as required to explode the 22 M_{\odot} star at the chosen E_k . The density profiles of the four models are shown in Fig. 1. They are characterized by distinctive spikes, which mark the outer boundary of the region where explosive nucleosynthesis affects the composition.

The density inversion is a consequence of the fast neutrino-driven wind, which is stronger for more energetic explosions. It pushes the slower ejecta expanding behind the outgoing SN shock and accumulates them in a dense shell surrounding a lower density central bubble. This central bubble is filled by high-entropy wind matter and can be recognized in Fig. 1, at a much later stage when the ejecta have reached homologous expansion, by the density trough around the coordinate origin. In 1D simulations including nickel decay the density spike is inflated by the radioactive decay heating (Jerkstrand et al. 2018). In 3D simulations it is further smoothed by Rayleigh–Taylor mixing of the ejecta, see fig. 8 in Utrobin et al. (2017); compare panels b and c there at times $t < 1$ h, i.e. before the reverse shock from the He/H interfaces moves inwards through the expanding stellar debris.

This spike in the density profile results in a relatively large amount of material in a small velocity range. For the 1 foe model, the density spike ranges from approximately 3000 to 5500 km s^{-1} and contains 1.6 M_{\odot} of material while the 8 foe model has a similar $\approx 3000 \text{ km s}^{-1}$ range starting from 10 500 to 13 600 km s^{-1} that contains 1.24 M_{\odot} of material.

The model is evolved in PROMETHEUS-HOTB until the shock leaves the star and the ejecta are in homologous expansion, such that $r \propto vt$. As part of the explosion mechanism, the final ejected masses in the

Table 2. The total mass of He, ^{56}Ni , the X_{56} tracer used to track the iron-group rich material, and 50 % of X_{56} that is added to the ^{56}Ni mass.

Energy [10^{51} erg]	M_{He}/M_{\odot}	M_{Ni}/M_{\odot}	$M_{X_{56}}/M_{\odot}$	50 % $M_{X_{56}}$
1	0.059	0.083	0.029	0.0147
3	0.119	0.090	0.114	0.057
5	0.180	0.079	0.215	0.107
8	0.245	0.066	0.315	0.158

various models differ somewhat (see Table 1). This is because a larger mass of neutrino-heated ejecta is needed to account for higher values of E_k .

For explosive nucleosynthesis, the code uses a 13-species α -network and a 15-species solver for nuclear statistical equilibrium that tracks the bulk production of α -elements up to ^{56}Ni . ^{56}Ni production is exclusively confined to the innermost region. The ^{56}Ni masses listed in Table 1 include the ^{56}Ni that is produced explosively by nuclear burning in shock-heated ejecta as well as 50 % of the so-called tracer material. This material, defined as X_{56} , accounts for iron-group nuclei in slightly neutron-rich neutrino-heated ejecta, whose exact composition depends on details of the neutrino transport. Its exact composition is therefore uncertain because of the use of an approximate description of the neutrino physics in the explosion simulations (Ertl et al. 2016; Sukhbold et al. 2016). Therefore, we take $X_{\text{Ni}} + 50\%$ of X_{56} to be a reasonable approximation for the ^{56}Ni mass.

Table 2 shows the mass of the He, ^{56}Ni , and the X_{56} . The explicitly tracked ^{56}Ni formation is under 0.1 M_{\odot} for all four explosion energies while the X_{56} increases by almost 0.1 M_{\odot} for each ‘jump’ in E_k . The total ^{56}Ni mass used for the light curve and spectral calculations (column 4 in Table 1) is increasingly comprised of the X_{56} tracer instead of M_{Ni} as E_k increases, as shown in columns 3 and 5 of Table 2.

2.2 Abundance profiles

The abundance distribution of the original models is shown in the four panels of Fig. 2. An expanded view of the regions in and near the density spikes is shown in Fig. 3. In the original models, ^{56}Ni is confined to the lowest velocities, which is known not to be realistic. In most SNe Ic that have been modelled, it is necessary for ^{56}Ni to be present at intermediate/high velocities in order for synthetic light curves to match the observed ones. The outer part of the ejecta is comprised predominantly of C, Ne, O, and Mg, with the bulk of the intermediate-mass elements (IME) produced at the edge of the ^{56}Ni -forming region. ^{56}Ni produced by the explosion is contained within and behind the density peak near 4000, 6000, 9000, and 11 000 km s^{-1} for the four models, in order of increasing E_k .

In order to explore the properties of element mixing, we use three approximations in this work. First, we assume that the original model explodes ‘as is’ and nothing is changed. We call these models ‘unmixed’ or ‘non-mixed’ with the abundance profiles of these models shown in Figs 2 and 3. A second approximation is to mix the region that undergoes explosive nucleosynthesis in both density and abundances. The range of velocities that this region encompasses changes with E_k . To account for this, we choose a boundary point just beyond the peak of the density structure, shown in Fig. 1, that defines our density and compositional mixing region. The result is a flat density structure and constant composition. Similar to the original model, this mixing approach would keep ^{56}Ni centrally located, which we know is unlikely to be correct. To mix out this

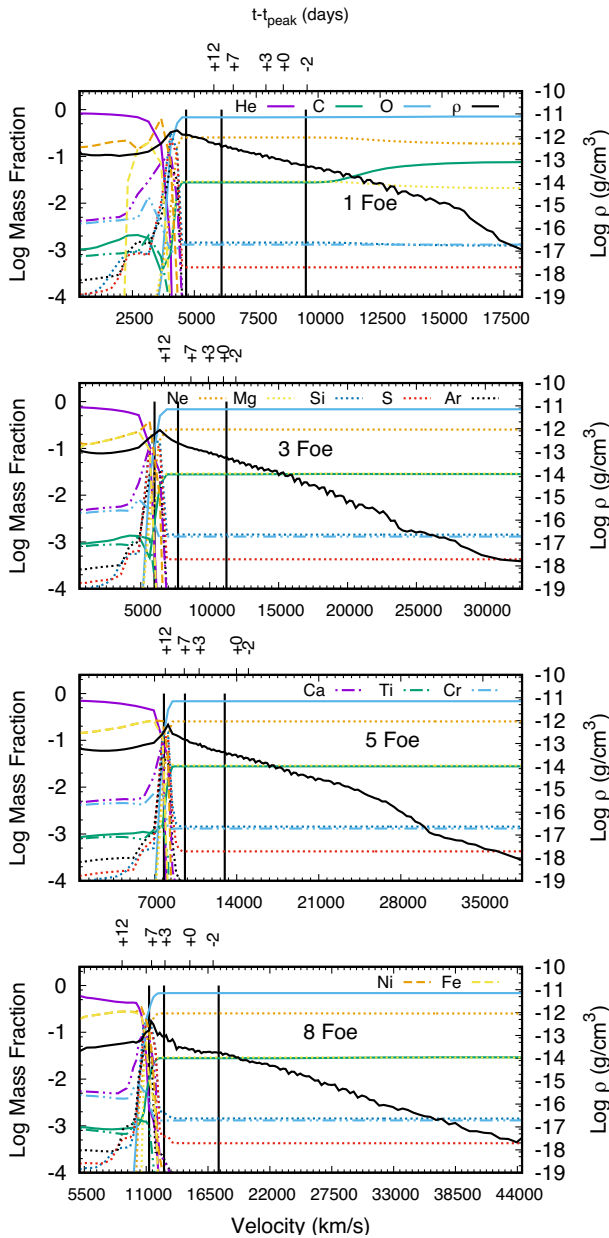


Figure 2. The abundance (left-hand scale) and density (right-hand scale) profiles of the 1, 3, 5, and 8 foe models (from top to bottom, respectively) with no mixing applied at approximately five days after the onset of the explosion. The Fe line represents Fe and the other 50% of the X_{56} tracer not included in the ^{56}Ni abundance. Notice that the x -axes of the four plots have different ranges to account for the different E_k . The tick marks at the top of each panel represent the position of the photosphere at the epochs indicated (relative to bolometric maximum). The black vertical lines define the velocities within which 1, 2, and $3 M_\odot$ of material are enclosed (from low to high velocities).

material, a running boxcar average is used to only mix the ^{56}Ni and Fe abundances in ejecta. This results in a partially centrally located ^{56}Ni with decreasing ^{56}Ni further into the outermost regions. We call these models ‘partially mixed’ and the abundance profiles are shown in Fig. 4. In a third approximation, we assume that the ejecta are completely mixed, while keeping the density structure as in the second approximation. We call these models ‘fully mixed’ and their abundance profiles are shown in Fig. 5.

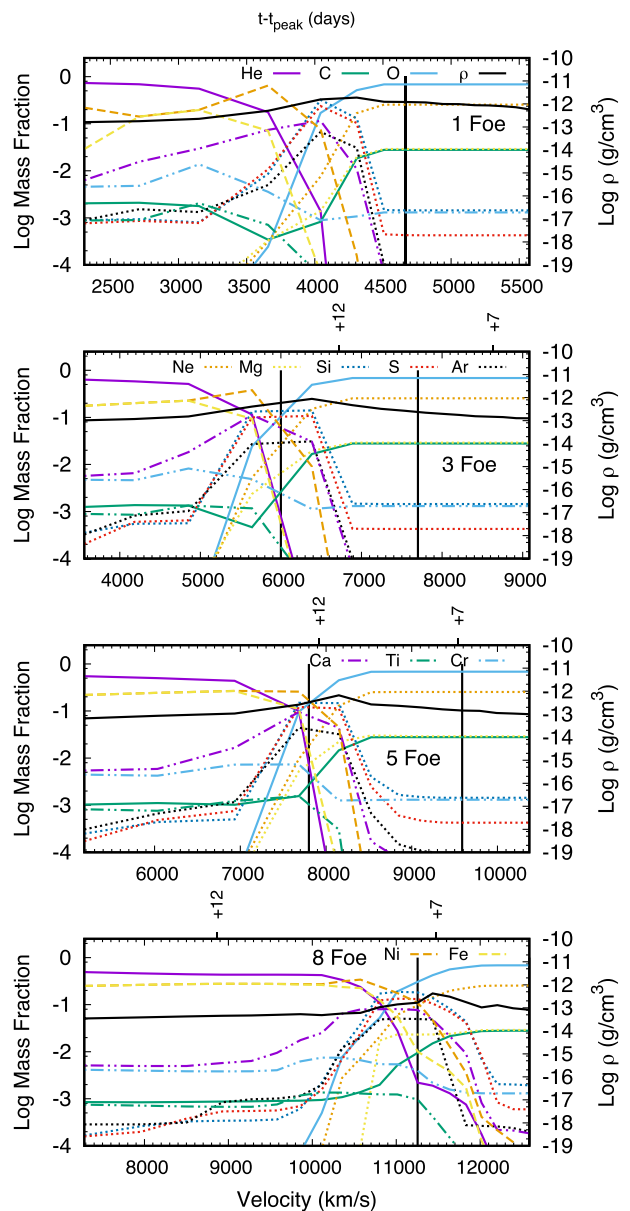


Figure 3. The inner region of the non-mixed models at approximately five days after the onset of the explosion are shown here as the velocity range is too narrow in Fig. 2. Symbols and labels are the same as in Fig. 2.

The unmixed models contain some helium at the lowest velocities (Fig. 2 and 3). This is produced during α -rich freeze-out. Complete mixing extends this material to the entire range of velocities, as seen in Fig. 5. While it is hard to imagine that such extreme mixing is feasible for a 1 foe explosion of a $3.35 M_\odot$ CO core, we treat it as a theoretical endpoint in the mixing approximations. Extremely mixed ejecta may be linked with highly asymmetric explosions and possibly related to gamma-ray bursts or hypernovae, which often have larger ejecta masses and explosion energies (Mazzali et al. 2004; Ashall et al. 2019).

Table 2 shows the total mass of He for each E_k . Because of the choice of outer mass-cut, no He is located in the outer layers of the ejecta (Fig. 2). The partially mixed models do not mix beyond the innermost region and the He abundance outside the mixing region is poor or non-existent. Only in the fully mixed models

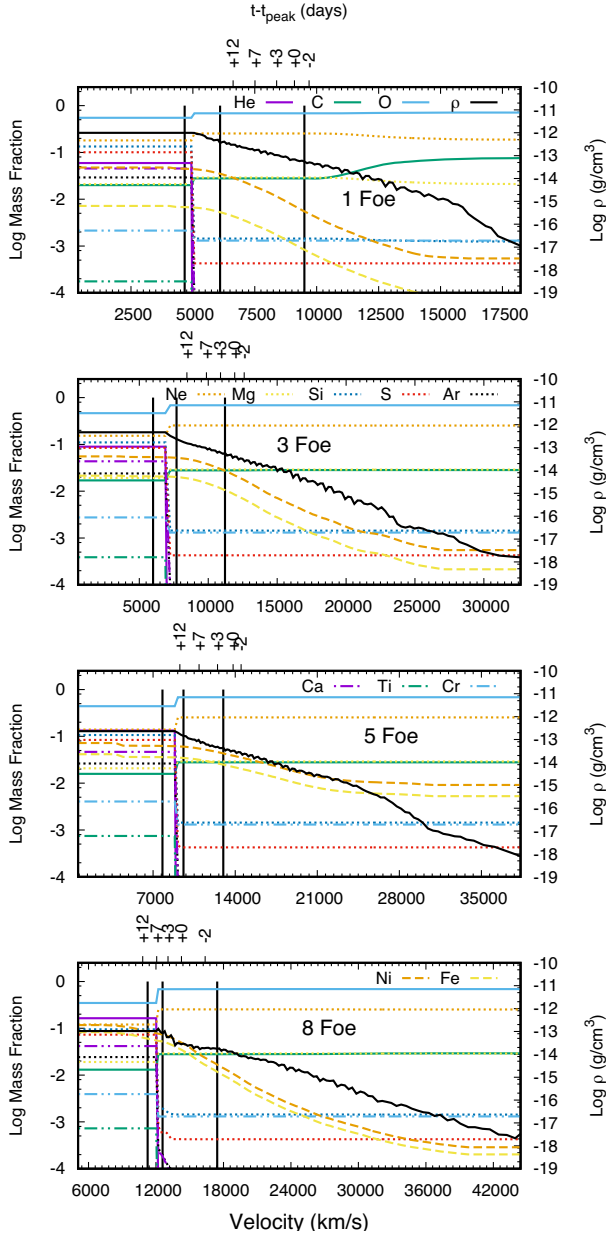


Figure 4. The abundance (left-hand scale) and density (right-hand scale) profiles of the 1, 3, 5, and 8 foe partially mixed models (from top to bottom, respectively) at approximately five days after the onset of the explosion. The Fe line represents Fe and the other 50% of the X_{56} tracer not included in the ^{56}Ni abundance. Notice that the x -axes of the four plots have different ranges to account for the different E_k . The tick marks at the top of each panel represent the position of the photosphere at the epochs indicated (relative to bolometric maximum). The black vertical lines define the velocities within which 1, 2, and 3 M_{\odot} of material are enclosed (from low to high velocities).

does helium extend to the outer layers and higher velocities. For the fully mixed models, the mass fraction of the He is $\sim 10^{-3}$. For the 1, 3, and 5 foe fully mixed models, the latest spectra are at $t-t_{\text{peak}} + 12$ d and is either at or above the $2 M_{\odot}$ line in the models. This leaves approximately $1.5\text{--}2 M_{\odot}$ of material in the line-forming region of which $0.02\text{--}0.04 M_{\odot}$ of this is He. Hachinger et al. (2012) showed that approximately $0.06\text{--}0.14 M_{\odot}$ of helium in the line-forming region is required to form He lines in the spectra. Given that He line formation is sensitive to the location of ^{56}Ni , this

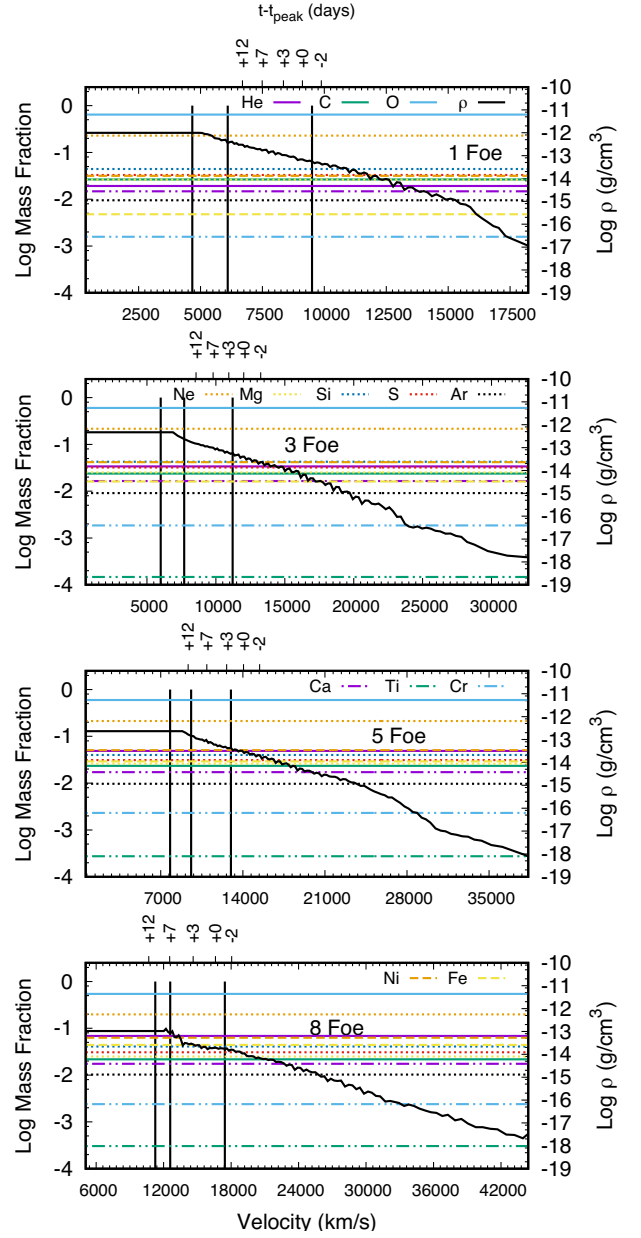


Figure 5. The abundance (left-hand scale) and density (right-hand scale) profiles of the 1, 3, 5, and 8 foe fully mixed models (from top to bottom, respectively) at approximately five days after the onset of the explosion. The Fe line represents Fe and the other 50% of the X_{56} tracer not included in the ^{56}Ni abundance. Notice that the x -axes of the four plots have different ranges to account for the different E_k . The tick marks at the top of each panel represent the position of the photosphere at the epochs indicated (relative to bolometric maximum). The black vertical lines define the velocities within which 1, 2, and 3 M_{\odot} of material are enclosed (from low to high velocities).

suggests that despite the low mass of He present in the line-forming region, the extra ^{56}Ni may lead to the formation of He lines via non-thermal processes (Lucy 1991; Hachinger et al. 2012). However, the extensive mixing also places ^{56}Ni alongside this helium. As such, the fully mixed models will include the non-thermal effects of He regardless of the approximate mass in the line-forming regions.

For the 8 foe unmixed model, the latest epoch places the photosphere deep in the innermost region where the abundance of He is $\sim 40\%$, shown in Fig. 2. The mass of the innermost core

is $\sim 1 M_{\odot}$, but only 25–50 % of this mass is above the photosphere with the abundance of He dropping towards the density spike. This puts approximately $0.1\text{--}0.2 M_{\odot}$ of He in the line-forming region of the latest epoch of non-mixed 8 foe model. This layer is in a region in which the elemental abundances are comprised of approximately 40% He, 30% Fe, and 30% Ni, which may not be a realistic or observable layer.

2.3 Light curve and spectral synthesis codes

After the explosions have entered the homologous expansion phase and we apply one of the three mixing approximations, we then continue the simulation workflow with our light curve code. The code, described in detail in Cappellaro et al. (1997), calculates the emission and propagation of gamma-rays and positrons produced by the decay of ^{56}Ni and, subsequently, ^{56}Co , into the homologously expanding ejecta using a Monte Carlo method. Constant values for both positron and gamma-ray opacity are used, with values of 7 and $0.027 \text{ cm}^2 \text{ g}^{-1}$, respectively (Axelrod 1980). The code does not take into account post-breakout emission phase. The energy that is deposited is then recycled into optical photons, whose propagation is also followed in a Monte Carlo scheme. A time- and metallicity-dependent but frequency-independent optical opacity is used (Mazzali et al. 2001a). This aims at reproducing the dominance of line opacity in the ejecta (Ashall et al. 2019). A constant time-step of one day is used and the calculation is run to 200 d. The position of the photosphere is approximately determined by integrating inwards until the radius where an optical depth of $\tau \geq 1$ is found. The zone that includes this radius is used to determine the photospheric velocity. This velocity, combined with the luminosity, abundances, and epoch are used as inputs in the spectral code.

The synthetic spectra are calculated using a Monte Carlo code discussed in detail in Mazzali & Lucy (1993), Lucy (1999), and Mazzali (2000). The code reads in the density structure as a function of velocity, stratified composition, luminosity, and velocity of the photosphere at a given epoch. When modelling observed SNe, these variables can be inferred by fitting the observed spectra and light curves. As the photosphere recedes into the expanding ejecta, the near-photospheric region, where line formation is most likely to occur, can be characterized by a varying composition. A detailed depth-dependent composition can be inferred by matching the spectra in a process called abundance tomography (Stehle et al. 2005). If the ejecta has He or H in abundances greater than 10^{-10} , the non-thermal effects of these elements are included into the code by the use of a non-local thermodynamic equilibrium (NLTE) module discussed in Hachinger et al. (2012). The formation of H/He lines results from significant deviations from LTE as shown in detail by Lucy (1991). For these SNIc models, the progenitor was stripped such that the outer layers contain an abundance of helium smaller than 10^{-10} , but the α -rich freeze-out results in some He mass as discussed in Section 2.2

For all models, t_{peak} is defined as the time when the bolometric light curve reaches a maximum luminosity (L_{max}). For easier comparison among the models, synthetic spectra for all energies and mixing approximations are generated at the same five epochs relative to t_{peak} rather than at fixed epochs relative to the time of explosion. This is because t_{peak} occurs at different times after explosion for different models owing to the different E_k , mass and distribution of ^{56}Ni . We choose times of -2 , 0 , $+3$, $+7$, and $+12$ d with respect to t_{peak} . These times are chosen to cover ~ 2 weeks of observations, in order to capture the evolution of the main spectral features and match the epochs of most available data.

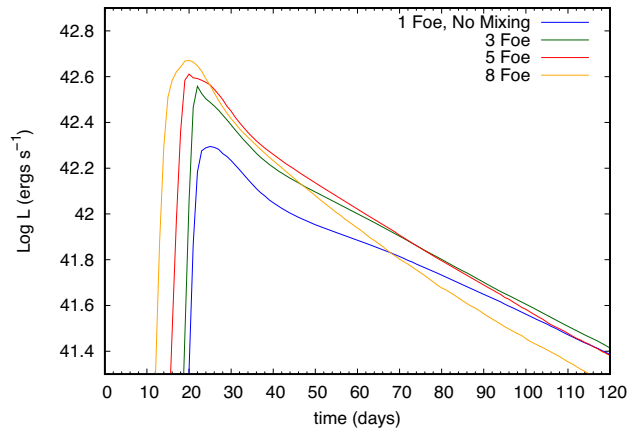


Figure 6. Synthetic light curves for the unmixed models for all four energies.

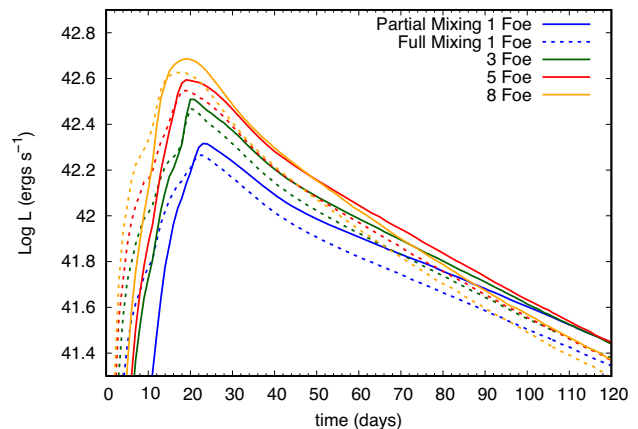


Figure 7. Synthetic light curves for the mixed models light curves for all four energies. In contrast to the unmixed models, these models have much broader light curves and longer $t_{1/2}$.

Observationally, well-sampled SN spectra prior to peak are rarer than post-peak so more spectra are generated after t_{peak} (Shivvers et al. 2019). Extensions to this would be considering nebular spectra generated at 180–220 d post-peak.

3 RESULTS

3.1 Light curves

Figs 6 and 7 show the bolometric light curves generated for the three mixing approximations for each of the four energies. The density spike separating the ^{56}Ni production and the rest of the CO core, shown in Figs 1 and 2, acts as a barrier to photon diffusion and causes the rise time to be at least 18 d for all unmixed models. The mixed model tend to have shorter rise times because the density spike is smoothed out and ^{56}Ni is distributed to higher velocities. Another parameter used to describe SESNe is $t_{\pm 1/2}$, defined as the time it takes for the luminosity to rise from $L_{\text{max}}/2$ to L_{max} for $t_{-1/2}$ or to decline from L_{max} to $L_{\text{max}}/2$ for $t_{+1/2}$ (Prentice et al. 2019). The unmixed models have short $t_{-1/2}$ because initially photons cannot diffuse out because of the density spike, but when density decreases sufficiently by expansion the release of trapped photons is immediate. Therefore, in the unmixed models $t_{+1/2} \gg t_{-1/2}$,

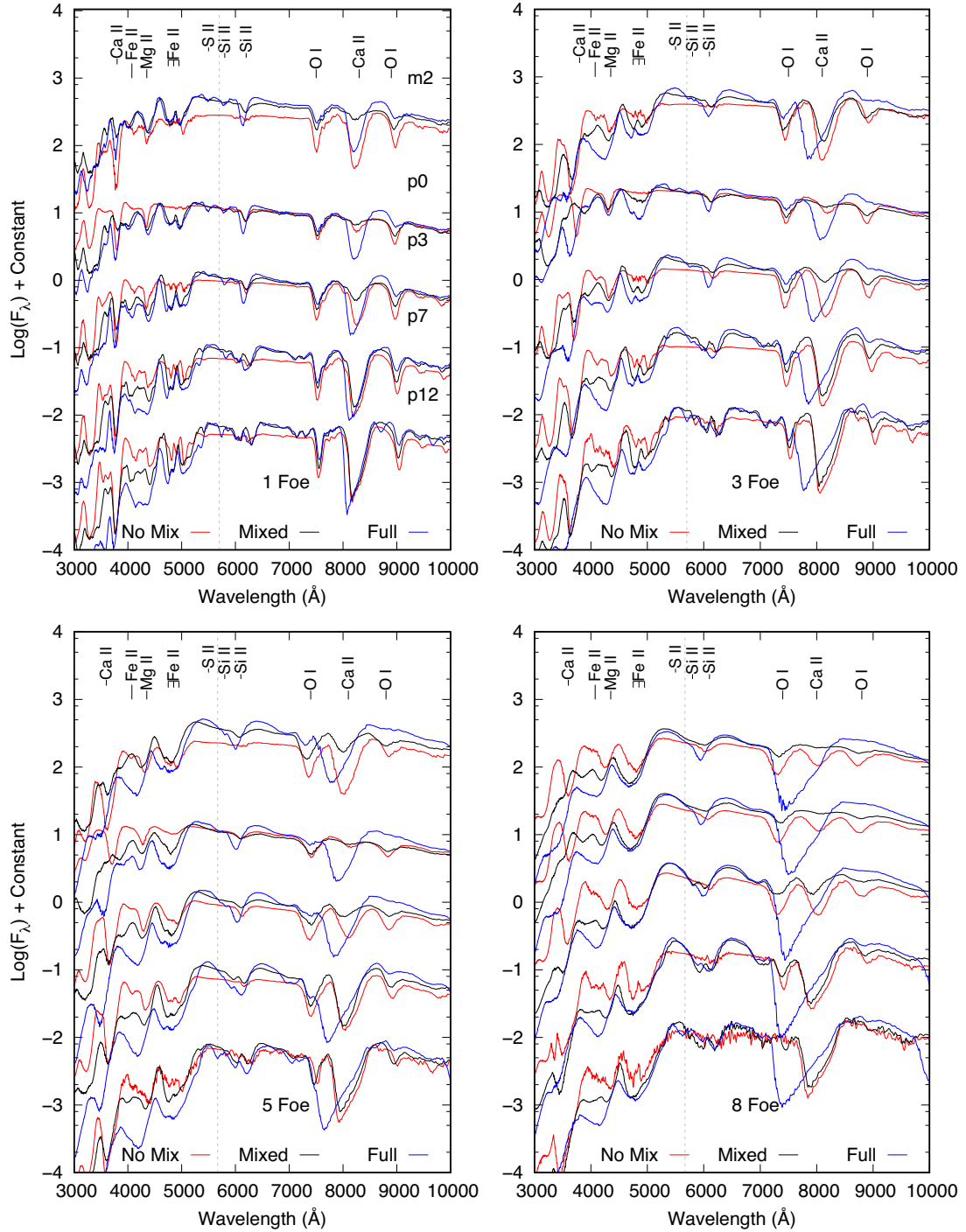


Figure 8. The synthetic spectra for all mixing approximations and E_k . The flux is in log scale and offset for visibility. The dashed grey line represents the strongest optical He I line at 5875Å. All line identifiers are approximate and may not represent the exact minima for the identified spectral feature.

while both sets of mixed models are more symmetric about L_{\max} . Smoothing the density spike and mixing the ^{56}Ni outwards allow a much smoother rise time for all energies, resulting in earlier t_{peak} but a larger $t_{-1/2}$ indicating a slower rise.

The models in this work do follow Arnett’s models to an extent but we do not expect a replication of the exact results. Arnett assumes a point-like distribution of ^{56}Ni , which is not realistic (see e.g. Mazzali et al. 2017) and is not what we use. As ^{56}Ni is produced further out with increasing E_k , diffusion of photons is easier and

peak is reached earlier. The declining part, on the other hand, tends to follow Arnett more closely, as the dominant factor that controls opacities then is indeed E_k .

3.2 Spectra

The spectral evolution of the 1 foe models for all three mixing approximations is shown in the top left plot in Fig. 8. The photospheric temperatures at each epoch are shown in Fig. 9. As

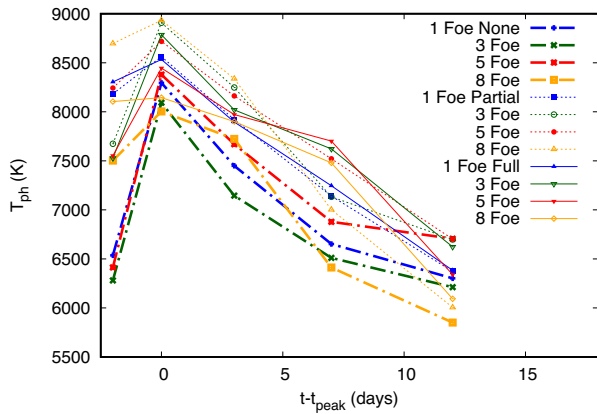


Figure 9. The evolution of the photospheric temperatures for all combinations of explosion energy and the mixing approximations.

mixing increases from no mixing to fully mixed, the wavelength range of $\lambda < 4500 \text{ \AA}$ begins to lose features because the increasing abundance of Fe-group elements in the line-forming region causes more line blanketing. This is less noticeable in the early phases, but at t_{+7} and t_{+12} this region flattens noticeably. The broadness of many optical features also increases as a function of mixing, with several lines becoming indistinguishable. The S II and Si II lines near $5500\text{--}5800 \text{ \AA}$, on the other hand, are visible only in the fully mixed case. Both S and Si are produced deep in the ejecta and only mixed outwards significantly in the fully mixed case. The Fe II multiplet 48 lines near 5000 \AA are split owing to the relatively low velocity of the ejecta, such that all three strongest lines can be identified at some epoch in the evolution of the spectra for all three mixing approximations. The fully mixed model includes the non-thermal effects of He and the 5875 \AA line is present in the last two epochs with two weaker lines in the $t_{\text{peak}} + 12 \text{ d}$ at 6500 and 6700 \AA . Prior to these epochs, the total mass of He in the line-forming region is too small to produce strong or easily observable lines. He lines visible in the NIR region of the spectrum are discussed later.

The spectral evolution of the 3 foe models for all three mixing approximations is shown in the top right plot of Fig. 8. These are similar to the 1 foe models with respect to the presence of features. The breadth and visibility of several features increases as the amount of mixing increases, as does line blanketing in the bluer portion of the spectra. The Fe II lines near 5000 \AA are not as easily identifiable in the fully mixed case, as the higher energy leads to higher velocities, producing line blending. The ejecta do not have enough velocity or energy to blend O I 7774 and the Ca II IR triplet, even under the full mixing approximation. Similar to the 1 foe fully mixed model, only the day 7 and 12 spectra show evidence of He in the fully mixed model at this E_k . Unlike the 1 foe model, the region where the 6500 and 6700 \AA He lines would form has two much stronger Fe II lines that make observing the weaker He I lines challenging.

The bottom left plot in Fig. 8 shows the time-series of spectra for the 5 foe models for all three mixing approximations. Similar to the 1 and 3 foe models, mixing alters the breadth and visibility of several features as well as increases line blanketing in the near-UV. The Fe II lines are now mostly blended together as the ejecta velocities are much higher. The O I 7774 and Ca NIR triplet near $7500\text{--}8000 \text{ \AA}$ are much broader and begin to show signs of blending, at least in the fully mixed case when more calcium is present at high velocity. Continuing the trend, only the day 7 and 12 spectra show He I at

5875 \AA , however the overall blending and broadening of the spectra in general makes the day 7 He I line at 5875 \AA less discernible from the rest of the spectra.

The bottom right plot in Fig. 8 shows the time-series of spectra for the 8 foe models for all three mixing approximations. The higher ejecta velocity produces consistent blending of the three Fe II multiplet 48 lines for all the mixing approximations and epochs chosen. The fully mixed case also blends together the Ca II IR triplet and the O I 7774 lines due to the higher energy ejecta and the mixing resulting in Ca and O across the entire velocity range. The partially mixed and unmixed models do not mix out the calcium present at the edge of the ^{56}Ni -rich region to the same velocity where oxygen is dominant. The calcium abundance in the outer atmosphere is $\sim 10^{-5}$ in these models, which is too little to cause strong features. The regions where the calcium abundance is significant has velocities that are too low for blending to occur. The near-UV line blanketing is stronger in the fully mixed models as the metal-rich core is mixed into the outer layers. This is particularly strong in comparison to the fully mixed models with lower E_k . This shows that $E_k \approx 5 \times 10^{51} \text{ erg}$ (or higher depending on mixing) is required for significant blending to occur. This could be seen as the lower boundary for hypernovae. The He I line at 5875 \AA is only partially observable at day 7 and stronger at day 12 in the fully mixed models.

At $t_{\text{peak}} + 12 \text{ d}$ for the 8 foe non-mixed model, the photosphere has receded into the core, which is comprised of 40% He, 30% ^{56}Ni , and 30% Fe. This is shown in the 8 foe models at the bottom of Figs 2 and 3. At this late epoch, approximately 30 d after the start of the explosion, some of the ^{56}Ni has decayed into ^{56}Co . This material is contained in a very narrow velocity range ($\sim \Delta v 2500 \text{ km s}^{-1}$) just above the photosphere. The proximity of this region to the photosphere results in the formation of a high number of narrow Fe/Co/Ni lines. Such a narrow-lined spectrum is not observed in Type Ic-BL SNe, of which the 8 foe model would likely be classified, suggesting that the models with a non-mixed Fe/Ni/Co core do not reflect realistic SNe at some or most epochs.

For all values of E_k , mixing of Fe group elements and ^{56}Ni outwards produces stronger line blanketing. The Si II features near 6000 \AA are consistently weak in the unmixed case as Silicon is located too deep in the ejecta, formed either by the progenitor or during the explosive nucleosynthesis. In the later epochs of the mixed models, the 6000 \AA region near the stronger Si II and S II lines show the formation of several Fe II lines. These are separable and identifiable in the lower energy models at the late epochs due to the ejecta have insufficient energy to blend these lines.

The Ca abundance at $t_{-2} \text{ d}$ for the unmixed and partially mixed models is approximately $\sim 10^{-5}$, below the lower limits of the abundance plots in Section 2.2, while the abundance of Ca in the fully mixed model is $\sim 10^{-2}$. In the fully mixed model, Ca produces a strong and broad Ca II NIR triplet line at all epochs. The ionization ratios of Ca in the non-mixed and partially mixed models are different, resulting in different strengths of this line at the t_{-2} epoch. In the unmixed models, 1–10 % of Ca is Ca II, while in the partially mixed models only 0.1–1.0 % of Ca is Ca II. Therefore, the unmixed show in a stronger Ca II line. Ionization ratios are related to both the density and luminosity variations for each model and change as a function of time.

Mixing the ^{56}Ni and Fe-group elements further out into the ejecta is noticeable in the spectra. The additional Fe-group elements form lines in the bluer part of the spectra, blanketing the other lines that are visible in the unmixed case as the photosphere recedes deeper into the ejecta near $t_{\text{peak}} + 12 \text{ d}$. The Ca II H & K lines near

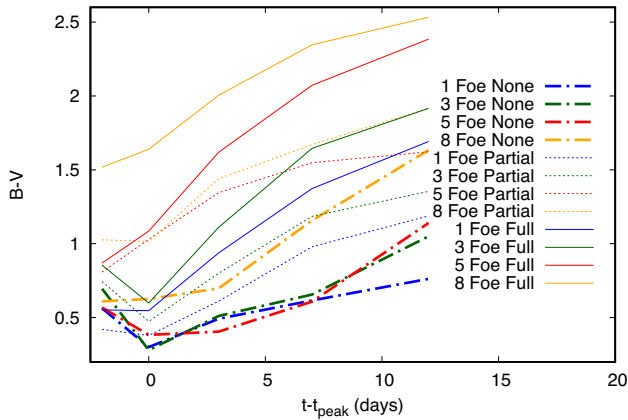


Figure 10. The $B - V$ colour evolution of the spectra with all explosion energies and mixing approximations.

4000 Å are an example of this behaviour as the bluer side of these lines is blended at higher explosion energies with increased mixing. This line blanketing effect is also correlated with explosion energy as the spectrum blue of 4000 Å is nearly devoid of identifiable lines.

The $B - V$ colour evolution shown in Fig. 10 is mixed with respect to both explosion energy and with the mixing approximations. After t_{peak} , all of the SNe become redder, but at different rates given the mixing approximation. The non-mixed models have a shallower slope, going from an approximate peak $B - V$ of 0.3 for the 1, 3, and 5 foe models at t_{peak} to a $B - V \sim 1.0$ –0.6 at day 12. The 8 foe model has a steeper slope starting from day 3 that matches the day 7 to day 12 slope of the 1, 3, and 5 foe models. The fully mixed models have the steepest slope, with a peak to 12 day $B - V$ change of ~ 1.0 –1.5. This is likely due to the extent of ^{56}Ni mixing as the centrally located ^{56}Ni in the non-mixed models heats the ejecta for a longer period of time. The fully mixed models have more ^{56}Ni further out, which can escape the ejecta without heating the material.

Fig. 11 shows the spectra of only the fully mixed models at all epochs and E_k in order to show how the constant He abundance changes the He features in the spectra. No other mixing approximations are shown as none have helium in the chosen epochs, other than the 8 foe no mixing model. In the previous spectral plots (Fig. 8), the wavelength range was plotted from 3000 to 10 000 Å to cover the commonly observed range of 4500–9000 Å. Two very strong He I features are present at 10 830 and 20 581 Å, however this wavelength range is not often observed by ground-based telescopes. At the early epochs, the abundance of He is high enough that the He I line at 10 830 Å is observable at all explosion energies. This line grows in strength as the ejecta evolves. As the explosion energy increases, the strength of this line is also increased. This is due to the higher energy ejecta placing more He and ^{56}Ni at higher velocities than in the lower explosion energy models. The 20 581 Å line is only observable at late epochs in the 1, 3, and 5 foe models and weakly visible in 8 foe models at $t_{\text{peak}} + 7$ d. The 5875 Å line that is commonly used to help classify Type Ib SNe is weak or non-existent for most of the epochs, excluding the $t_{\text{peak}} + 12$ d.

4 PHYSICAL CLASSIFICATION

Using the method suggested in Prentice & Mazzali (2017) and discussed in Section 1, we categorize our explosion models for all

explosion energies and mixing approximations. In this classification system, SNe Ic-BL show strong line blending and are classified as $N = 3$ –4. These events are often related to GRBs and have high E_k . Our spectral classifications are summarized in Table 3. The N -values for our spectra show two basic trends. First, as E_k increases, the value of N typically decreases. The spectra for the 8 foe model, for example, show very broad features compared to the narrow lines in the spectra of the 1 foe model. Secondly, for a given E_k , the unmixed models have an N -value that is one greater than for the fully mixed models while generally sharing a similar N -value with the partially mixed models. At the epochs considered the photosphere is still mostly outside the partially mixed region, so that the partially and unmixed models show similar features. After peak the value of N changes somewhat as the photosphere forms at lower velocities and line blending decreases. In particular, the top left plot in Fig. 8 shows non-blended Fe II lines in the spectra of the 1 foe model, changing N from 5(6) to 6(7), where the number in parenthesis is the value of N assuming that Na II is observable. The peak spectra for the no mixing models do not show the Fe II multiplet 48 lines but the $t_{\text{peak}} - 2$ and $+3$ both show the lines, so for that mixing approximation, we consider the near peak spectra.

5 SPECTRAL COMPARISONS

Having computed synthetic spectra at a number of epochs for all E_k and mixing approximations, we now turn to observational data to check if the results show realistic behaviour. Unlike the previous figures that show the synthetic spectra, we do not plot the logarithmic flux, instead we scale the flux of each SNe, both the synthetic and observed, by the maximum flux value. Fig. 12 shows all synthetic spectra at peak luminosity against those of a set of eight observed SNe. These eight SNe are a subset of the SNe that are classified in Prentice & Mazzali (2017). This subset is chosen because the SNe share N -values with those of our synthetic spectra (Table 3). The scaling of the spectra in flux can suppress the impact of luminosity. These factors are an important limitation to keep in mind when trying to make accurate predictions of the ejecta properties based on Fig. 12 only. For all of the synthetic spectra shown, we do not include any elements, in particular Na, that were not in the original hydrodynamic model.

The SNe and models in Fig. 12 are arranged in order of colour at peak, with redder colours at the top. The N -value for the observed SNe is from Prentice & Mazzali (2017). Because of the sometimes limited wavelength coverage of the spectra, for some SNe it is unclear whether or not the Ca II NIR triplet and the O I 7774 line are blended, which would affect the value of N . In these cases, Prentice & Mazzali (2017) also consider spectra close to, but not exactly at peak. If the two features are present in those spectra, then it is assumed that they would likely appear at peak, with similar profiles, and this information is used to compute N . The unmixed models for all E_k are the bluest of all synthetic spectra, and are bluer than all observed SNe. Thus, they are clustered at the bottom despite the N -value. The observed $N = 4$ SNe, the closest to Type Ic-BL in the sample shown, are the reddest observed SNe and are clustered near the top. The 8 foe fully and partially mixed models replicate most of the broad features observed in the near-peak spectra of these SNe. Fig. 12 shows a slight trend whereby data and models with a smaller N are also redder. At a constant mass, the behaviour of the synthetic spectra reflects the increasing line blanketing in models with larger E_k and more mixing. The observed SNe appear to follow a similar trend, at least with respect to E_k , but more data would be helpful in defining the range of properties.

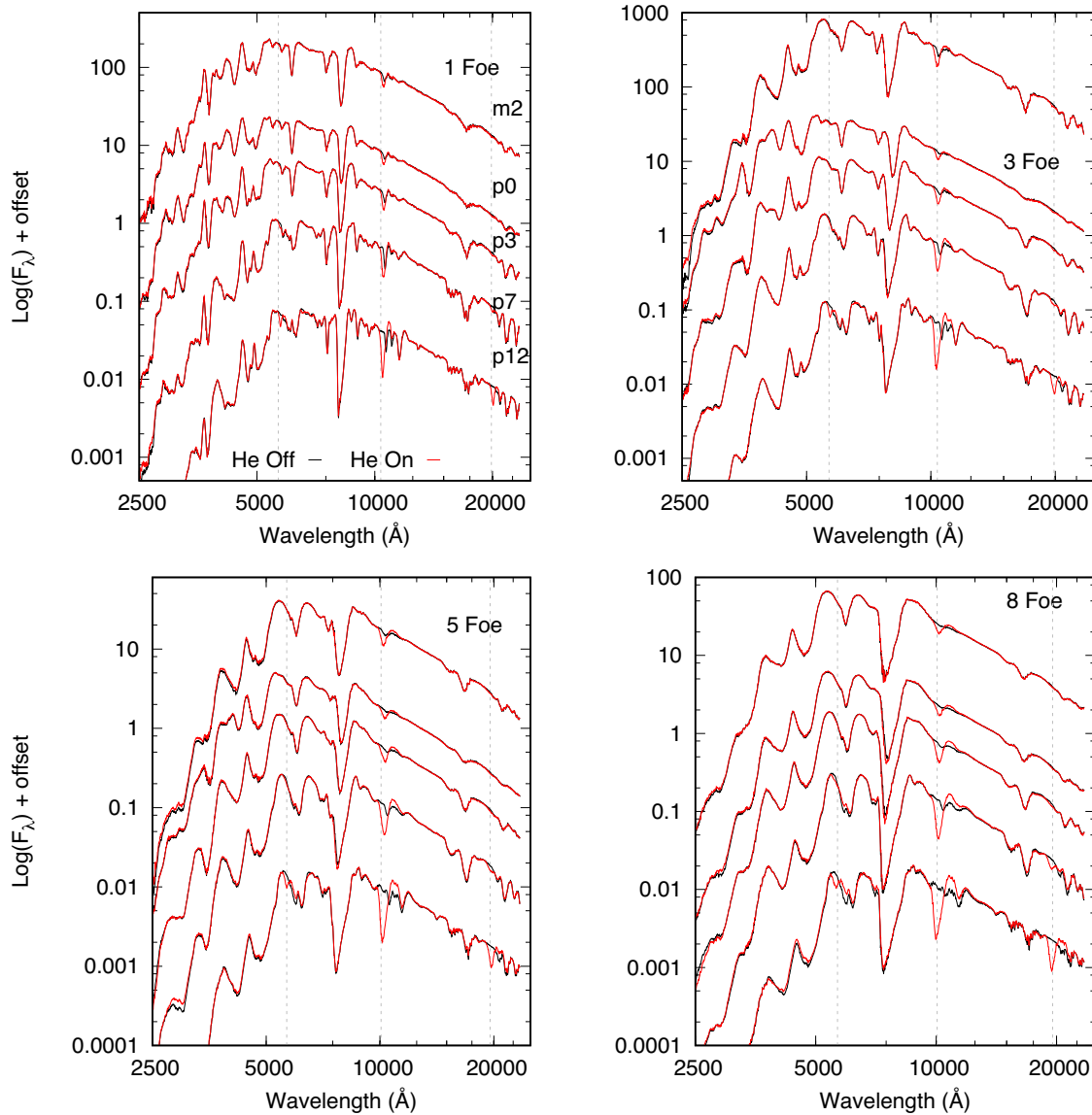


Figure 11. The fully mixed SNe for all four explosion energies. The red line includes the non-thermal effects due to He while the black line shows the same model without the non-thermal effects of He. The dashed grey lines represent three He I lines at rest wavelengths of 5875, 10830, and 20581 Å.

SN2016coi shares similar features with the synthetic spectra from the 8 foe fully and partially mixed models, except that the possible Na ID line in SN2016coi may not be observable in the fully mixed 8 foe model. A mixture of Si and S lines nearby may blend with or swamp the Na ID feature, depending on the abundance of Na. The Ca II NIR triplet and O I 7774 are blended in the fully mixed 8 foe model, but not in the partial and unmixed cases. Prentice et al. (2018) obtained an ejecta mass of 4–7 M_{\odot} and $E_k \approx 4.5$ –7 foe. The masses of our bare CO cores are at the low end of this range, but the E_k we used covers the estimated range.

Of the eight observed SNe, five have $N = 6$ –7, while eight of the 12 synthetic spectra have values of $N = 6$ –7 if we assume that the Na ID line would be visible. Spectra with $N = 7$ show fully unblended Fe II multiplet 48 lines, resulting in three features near 5000 Å. The two bluer features, which are closer in velocity space, are blended in $N = 6$ spectra. On the observational side, SNe 2004fe and 1994I share a similar set of absorption features from 3900 to 4250 Å. This is reproduced by the partially mixed

and unmixed 1 and 3 foe models. SN1994I has been modelled to have a low-mass ejecta of $\sim 1 M_{\odot}$ and $E_k \sim 10^{51}$ erg (Nomoto et al. 1994). Adopting a combined spectroscopic and photometric approach, Sauer et al. (2006) found $M_{ej} \approx 1.1 M_{\odot}$ and $E_k \approx 10^{51}$ erg. The ^{56}Ni mass was estimated as 0.07 M_{\odot} . The requirement that ^{56}Ni is mixed out to reproduce the light curve was taken as evidence of some asymmetry. No detailed fits are available for SN2004fe. The lack of a GRB connection for these SNe may also suggest that mixing was not as extensive as in GRB/SNe, such that the less mixed model spectra should share more similarities with the data, as they do.

Fig. 12 shows that the scaled synthetic spectra of the 22 M_{\odot} progenitor, given the various combinations of E_k and ejecta mixing, can replicate the bulk spectral features of both narrow- and broad-lined SNe. While it may be tempting just to read off values for the properties of the SNe plotted from that figure, this may lead to incorrect results, as we discussed above, because a single M_{ej} is used and the data are not flux-calibrated. Thus, the only information

Table 3. Visibility of the spectral features used in the computation of the N -value from Prentice & Mazzali (2017), and N -value for the various models in our set. Lines that are identified at or near peak luminosity, in the t_0 spectra, and unblended, are labelled with ‘yes’. If the line appears blended with another line, it is defined as ‘blended’ and the blend is counted as one feature. The Na ID line is not present in the models because Na is not part of the initial composition of the ejecta. The Na ID line is therefore marked as *. This is represented by the number in parenthesis in the N column, where the first number is without Na and the second includes Na.

Energy	Mixing?	Fe II 4924 Å	Fe II 5018 Å	Fe II 5198 Å	Na I 5895 Å	Si II 6347 Å	O I 7774 Å	Ca II NIR triplet	N
1 foe	No	Yes	Yes	Yes	Yes*	Yes	Yes	Yes	6(7)
	Partial	Blended	Blended	Yes	Yes*	Yes	Yes	Yes	5(6)
	Full	Blended	Blended	Yes	Yes*	Yes	Yes	Yes	5(6)
3 foe	No	Yes	Yes	Yes	Yes*	Yes	Yes	Yes	6(7)
	Partial	Yes	Blended	Blended	Yes*	Yes	Yes	Yes	5(6)
	Full	Yes	Blended	Blended	Yes*	Yes	Yes	Yes	5(6)
5 foe	No	Blended	Blended	Yes	Yes*	Yes	Yes	Yes	5(6)
	Partial	Blended	Blended	Yes	Yes*	Yes	Yes	Yes	5(6)
	Full	Blended	Blended	Blended	Yes*	Yes	Yes	Yes	4(5)
8 foe	No	Blended	Blended	Blended	Yes*	Yes	Yes	Yes	4(5)
	Partial	Blended	Blended	Blended	Yes*	Yes	Yes	Yes	4(5)
	Full	Blended	Blended	Blended	Yes*	Yes	Blended	Blended	3(4)

that can reliably be obtained from the comparison is about E_k/M_{ej} , which is mostly responsible for the spectra shape (Mazzali et al. 2017). While keeping this in mind, we continue the comparison as an exercise.

SN 1994I is matched well by the spectrum of the fully mixed 1 foe model and the partially mixed 3 foe model, so we may guess that E_k was 1–3 foe and $E_k/M_{ej} \sim 1$, in accordance with the results of detailed modelling. SN 2004aw best matches the 3 foe partially and fully mixed models and is in a reasonably good agreement with detailed modelling, which also suggests that M_{ej} was similar to that of the models used here (Mazzali et al. 2017). SN 2002ap (Mazzali et al. 2002) is placed between the 8 foe partially and fully mixed models, suggesting $E_k/M_{ej} \sim 2$. This is in good agreement with detailed modelling, which however favoured a lower M_{ej} of $\approx 2.5 M_{\odot}$, and E_k of $\approx 4 \times 10^{51}$ erg, but the actual ejected mass was smaller than in the models computed here. Finally, SN 2016coi is also well matched by the partially and fully mixed 5 foe models, but it has not been modelled.

Given the success of the comparison between synthetic and observed spectra at peak, we can then consider the time evolution of the spectra. Observations of SNe in general may not coincide with the dates of the synthetic spectra. For this reason, the nearest epoch with respect to peak luminosity is used to compare to our synthetic spectra for all observed SNe.

Fig. 13 shows the time-series of spectra of SN 2016coi compared to that of the 5 foe models for the three mixing approximations. None of the spectra match the observed ones perfectly, but the partially and fully mixed models behave better. Only the fully mixed models are able to blend the O I 7774 line and the Ca II NIR triplet.

Fig. 14 shows the 1 foe models for all three mixing approximations and compares them to the time-series of spectra of SN 1994I. The low-velocity ejecta of the 1 foe model replicate the basic features of the observed spectra for all mixing approximations. The Fe II line complex is correctly reproduced. The full mixing models best represent these features. This is in agreement with the results of Sauer et al. (2006), who do not find large changes in the near-photospheric abundances as a function of time. All mixing approximations also reproduce the O I 7774 line and the Ca II NIR triplet quite well, except for the possible O I line near 9000 Å.

Fig. 15 shows the 3 foe models for all three mixing approximations compared to the time-series of spectra of SN 2004aw. While

all models reproduce the observations qualitatively, the partially mixing models appear to be the most accurate, especially in the blue and in the O I 7774/Ca II NIR triplet region. In the fully mixed models the Si II lines near 6000 Å are significantly too strong throughout the evolution of the ejecta, suggesting this degree of mixing may be too extreme. SN 2002aw was modelled in detail (Mazzali et al. 2017), whose results agree with the values used in these models.

Fig. 16 shows the 8 foe models for all three mixing approximations compared to the time-series of spectra of SN 2002ap. The overall shape of the spectra is best reproduced by the fully and partial mixing models, but the detail match is never perfect, most likely because SN 2002ap had a smaller ejected mass than the models presented here. Nevertheless, the similarity of the spectral features is striking. All three mixing approximations for the 8 foe model show blended Fe II features, but only the fully mixed model blends the Ca II NIR triplet and O I 7774.

Overall, the synthetic and observed spectra do not show a one-to-one comparison, but this was to be expected. The diversity of Type Ic SNe suggests that they do not share a single unified progenitor and when using models to fit to observed SNe, significant work must be done to identify the most likely progenitor. To expand this, Fig. 17 shows the pseudo-bolometric light curves of the four previously mentioned SNe compared to all of our synthetic light curves. Our initial guess for the E_k of SN 1994I was in the 1 foe range, however the light curves of the 1 foe models are too broad when compared to SN 1994I. This suggests that the mass ejected by SN 1994I was smaller than in our set of models, in accordance with detailed modelling results. The light curve of SN 2002ap matches best in shape the 3 and 5 foe models, but it did not reach comparably high luminosities. Given the uncertainty of the ^{56}Ni mass in the models, the peak luminosity could match by choosing a ^{56}Ni mass that falls within the uncertainty in production. For SN 2004aw, the light curve matches best the 5 foe models in shape, although it is somewhat brighter. This E_k is higher than the 3 foe guess suggested by Fig. 12, but both values are not inconsistent with the modelling results. Finally, SN 2016coi, for which no detailed model exists shows a broad light curve, suggestive of a low E_k/M_{ej} ratio, and is reasonably well matched by the 1 foe models with full mixing, which is at odds with the spectroscopic results above. Accurate modelling of this SN would be desirable.

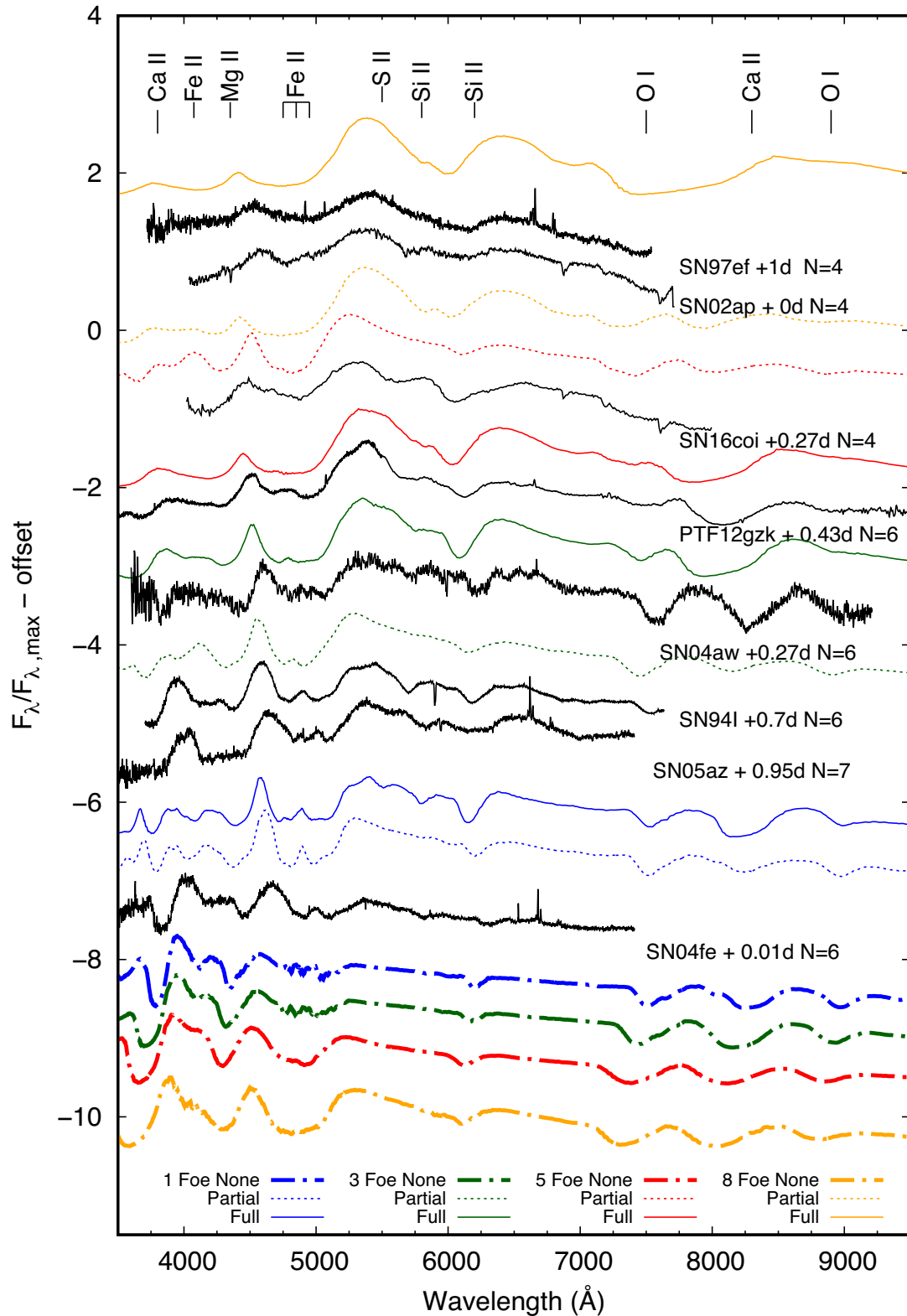


Figure 12. Synthetic spectra of all models at bolometric peak compared to a set of observed SNe Ic. SNe classified in Prentice & Mazzali (2017) that share N -values with those of the models in Table 3 are selected. All spectra are arranged in order of colour at peak, with the reddest spectra at the top. SN 2004aw has been scaled by $1.5 \times$ its own maximum for visibility of its features. As stated in Fig. 8, the absorption feature identifiers are approximate. Observational information related to the individual SNe spectra is given in Modjaz et al. (2014) for SNe 1997ef, 2002ap, 1994I, 2004aw, 2005az, and 2004fe, Prentice et al. (2018) for SN 2016coi, and Childress et al. (2016) for PTF12gzk. The spectral data were downloaded from WISEREP (Yaron & Gal-Yam 2012).

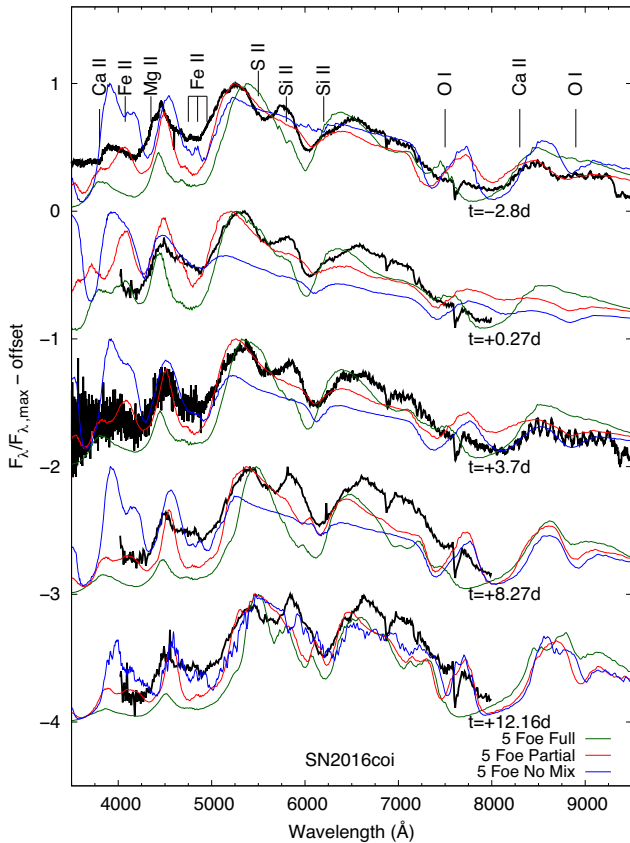


Figure 13. The time-series of spectra of the 5 foe model for all three types of mixing compared to the closest available epochs of SN2016coi. As stated in Fig. 8, the absorption feature identifiers are approximate.

6 DISCUSSION

The comparisons given in Section 5 show some similarities in the spectral evolution between the various SNe and the synthetic spectra, but only SNe 2004aw and (partially) 2016coi show similarities in their photometric behaviour, as seen in Fig. 17. The fact that synthetic spectra do not perfectly replicate observed SNe is to be expected, as our models were not fine-tuned to fit any specific event. ^{56}Ni and ejecta mass vary as a function of E_k in our models, but were not free parameters in this work. The observed light curves suggest some degree of freedom that affects M_{Ni} was not accounted for in the explosion models as discussed in Section 2.2. As was noted previously and repeatedly, simply using Arnett’s rule to determine bulk properties of the ejecta such as mass and – in particular – E_k may yield a set of values that match the light curve width but are then unable to replicate the spectral features if used in an explosion model. Looking at the mixing approximations we used, we can also begin to understand how complex the reality of these events. For example, the fully mixed 5 foe explosion replicates some features in SN2016coi, which has $N = 4$, that the partially and unmixed models cannot match, but no approximation works throughout the observed spectrum at all epochs. The fully mixed models are uniform in composition as shown in Fig. 5, and the divergence from the observed SNe suggests that in reality mixing is not as uniform. SN2004aw ($N = 6$) was a moderately high-energy SNe but with no coincident GRB. In this case, the fully mixed 5 foe explosion model has features that are too broad when compared to SN2004aw’s spectra. The partially mixed model has

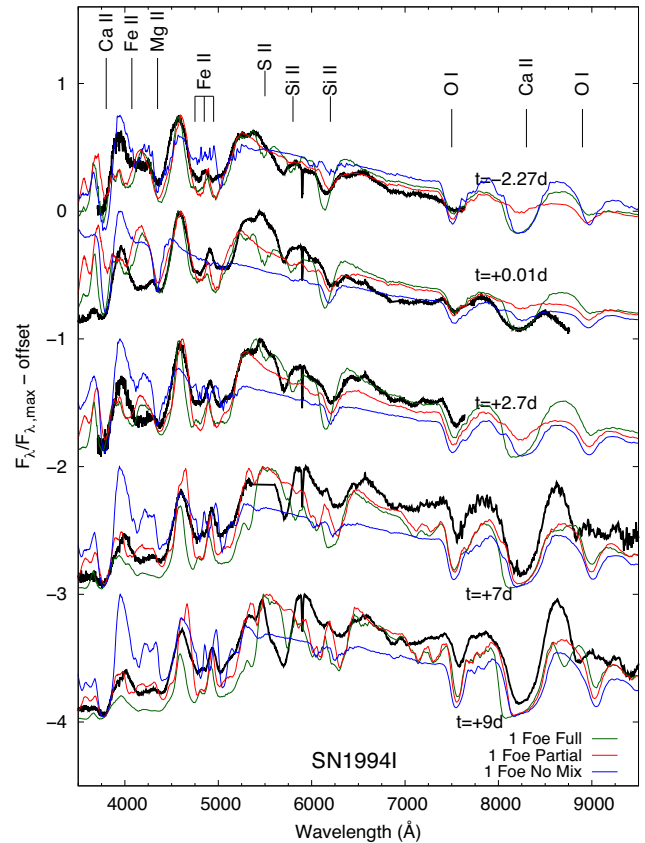


Figure 14. The time-series of spectra of the 1 foe model for all three types of mixing compared to the closest available epochs of SN1994I.

better success. This is also backed by the fitted abundance structure in Mazzali et al. (2017), which shows fairly strong ^{56}Ni and Fe group mixing outside the inner regions. This type of mixing is seen in Fig. 4. Unlike our partial mixing approximation, IME are mixed further out into the ejecta. SN1994I, which is also well studied, also required some mixing of ^{56}Ni and Fe group elements outwards in order to replicate the light curve (Sauer et al. 2006).

The comparison between our model set and observed SNe Ic data gives more evidence that analysing observed SNe requires a combination of spectroscopic and photometric methods to get a solid estimate of the ejecta parameters. The methods in this work are limited as SNe Ic come with a range of M_{ej} , E_k , and M_{Ni} . Additionally, when using scaled spectra one cannot account for luminosity differences between the observed and synthetic spectra. The spectral similarities between the observed and synthetic spectra do give suggestions about the E_k/M_{ej} ratio. For the same ^{56}Ni mass, multiple similar light curves can be generated by changing E_k and M_{ej} while keeping E_k/M_{ej} constant.

Some of the observed light curves in Fig. 17 show a much broader rising phase compared to the unmixed models calculated light curve. The mixed models, however, reproduce this early rise much better. This shows that the width of the light curve alone cannot simply be used to determine M_{ej} and E_k . In this study, M_{ej} was nearly constant for four explosion energies and associated ^{56}Ni masses. The only ‘free’ parameters we had is how we altered the interior density structure and mixed the ^{56}Ni and other elements. Modifying the distribution of ^{56}Ni leads to significant changes in the width of

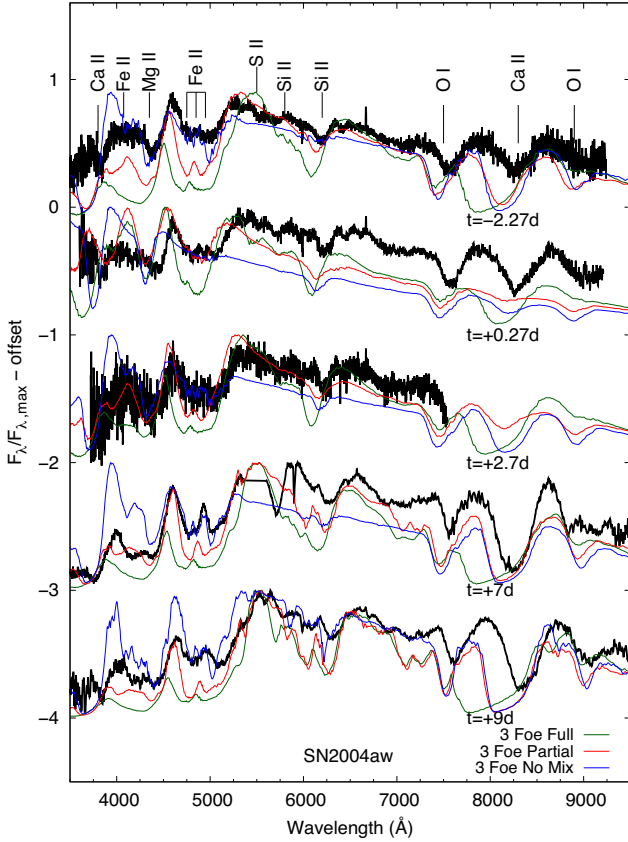


Figure 15. The time-series of spectra of the 3 foe model for all three types of mixing compared to the closest available epochs of SN 2004aw.

the light curve, while M_{ej} and E_k are constant. In mixed models, the presence of ^{56}Ni at higher velocities causes an earlier rise of the luminosity, and thus broadens the light curve. When comparing the mixed to the unmixed models, the broadening in the rise is significant for the same E_k/M_{ej} . This shows that using Arnett’s approximation (which assumes all ^{56}Ni to be centrally located as a point source) without taking into account other factors that influence photon diffusion time, and hence affect the light curve shape, can lead to incorrect estimates of the SN parameters as thoroughly discussed in Mazzali et al. (2017).

Prentice et al. (2019) give rise times for SNe Ib/c in the range from 8.6 ± 3.0^8 to 10.4 ± 1.7^8 d. SNe Ic have shorter rise times than SNe Ib. SESNe with steeply rising light curves, such as those of the 1, 3, and 5 foe models shown in Fig. 6, may be absent from observational studies, since such a rapid rise is difficult to observe. Whether totally unmixed explosions with a structure similar to that of our models do indeed exist is an interesting question. Section 5 shows that both fully and partially mixed models can replicate features much better across multiple epochs for various observed SNe.

Yoon et al. (2019) discuss the effect of ^{56}Ni mixing in the very early phases of the explosion. Their code and work consider phases with respect to peak of -10 to -25 d and include the contribution of breakout emission. Our code does not treat this mechanism or consider phases this early. Both light curves and spectral formation are highly dependent on the explosion models used and the models in our work are quite different from the ones in Yoon et al. (2019). As such we cannot make strong comparisons to their results but we

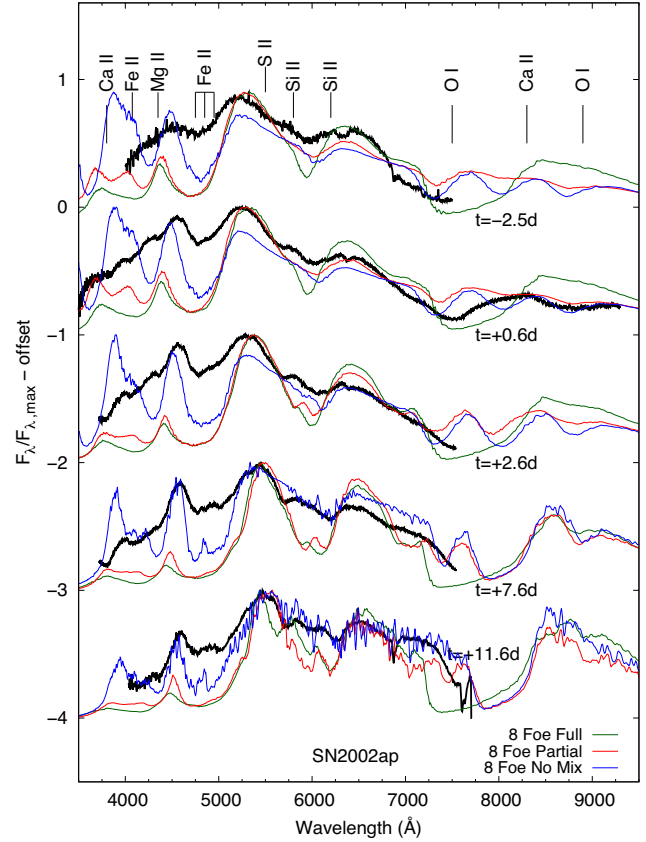


Figure 16. The 8 foe models for all three types of mixing plotted with the closest available epochs of SN2002ap.

will consider a few aspects. They do show that as the mixing of ^{56}Ni increases, the rise time increases, which matches our work. The $B - V$ values in Yoon et al. (2019) show that the least mixed models have a lower $B - V$ at peak and they fully have the highest $B - V$ at peak if we only consider the time range of only -2 to 12 d from peak, similar to the time range in our work. This matches our results in Fig. 10.

Fig. 18 shows the peak bolometric luminosity and the derived M_{Ni} for a set of SNe Ic from Prentice et al. (2016), along with M_{Ni} of our s22 models and their computed peak luminosity. The slight changes in peak luminosity caused by the different degrees of mixing in the models are shown. The fully mixed models have the lowest peak luminosity because the early diffusion of photons reduces the radiative energy available at peak. The peak luminosities of the partially mixed and unmixed models are similar. These two mixing methods keep the bulk of ^{56}Ni in the interior region, although with different densities (Fig. 1). The ^{56}Ni yields are somewhat uncertain in our explosion models as discussed in Section 2.2, but there is likely a correlation between E_k and M_{Ni} , which reproduced observational results. Peak luminosities mostly reflect M_{Ni} , even though M_{ej} changes somewhat for different E_k .

Because of the approximate treatment of nucleosynthesis in the SN simulations, using a 13-species α -network and a 15-species solver for nuclear statistical equilibrium, the exact amount of ^{56}Ni ejected in the explosions is unclear. A considerable fraction of tracer material (X_{56}) and of the α -particles of the neutrino-heated ejecta could also be ^{56}Ni , see the detailed discussion in section 3.3 of Ertl et al. (2019).

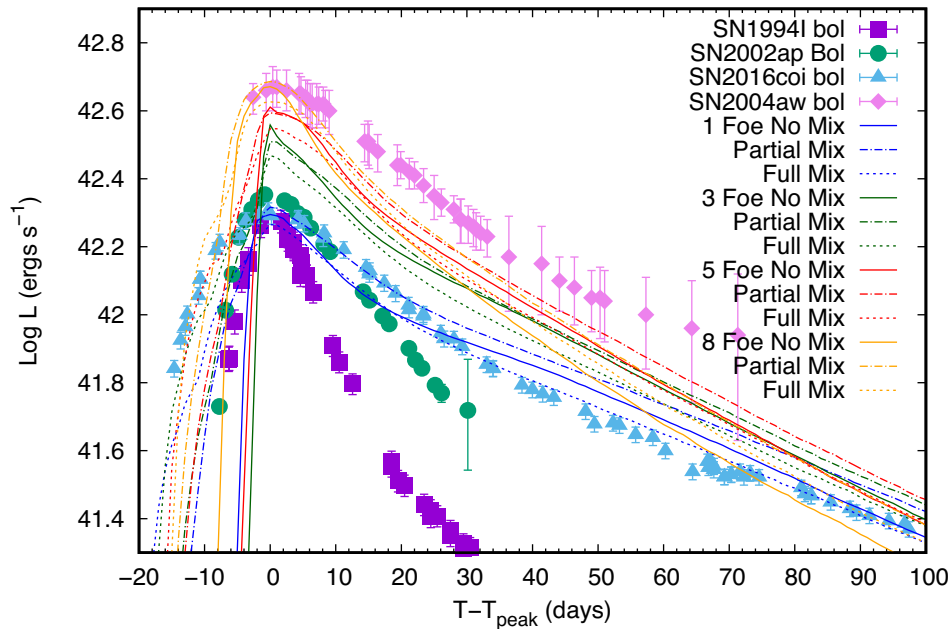


Figure 17. The pseudo-bolometric light curves of SNe 1994I, 2004aw, 2002ap, and 2016coi compared to the bolometric light curves of the models for all four explosion energies and all three mixing approximations.

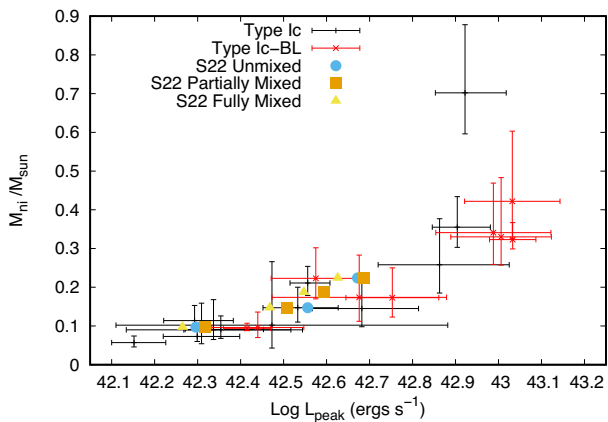


Figure 18. The peak luminosity calculated from a set of fully bolometric light curves taken from Prentice et al. (2016) compared to the measured ^{56}Ni mass using Arnett’s rule. The ^{56}Ni mass in some SNe is a lower limit because the host extinction correction is not available.

Mixing ^{56}Ni and iron to higher velocities produces line blanketing effects in the bluer portion of the spectra, particularly the near-UV. This is shown in the extreme case for the higher E_k fully mixed models, where the region between 2000 and 5000 Å is mostly blanketed. This could suggest that the extent of mixing may be derivable by this region of the spectra, as it has been for SNe Ia (Mazzali et al. 2014), but this region is rarely covered observationally.

With four explosion energies and a single mass model, we tried to cover the likely range of observed E_k/M_{ej} (Table 1). The N -values shown in Table 3 cluster around 5–6 with the 5 and 8 foe models having lower values. As discussed in Prentice & Mazzali (2017), the number of observed SNe for which E_k/M_{ej} is well defined (i.e. it was obtained from detailed modelling) is low, but still a trend appears to exist whereby N increases as E_k/M_{ej} decreases, as simple

considerations also suggest. This is reflected in our models. Mixing has a tendency to favour line blending (the Fe II lines, Ca II IR triplet, and O I 7774) and thus to reduce the value of N .

Fig. 11 shows that fully mixing the ejecta, including the He remaining after α -rich freeze-out, can produce NIR He I lines of varying strengths with respect to E_k , but may not produce a strong enough optical He I line for early or easy classifications to a Type Ib. Observing the 10 830 Å He I line early enough may be necessary for clear differentiation between Type Ib and Ic SNe but this is complicated by the Mg II line in this region. This requires detailed modelling and wider wavelength observations at early and late times if the optical He I lines are weak or hidden.

The lack of E_k/M_{ej} ratios inferred using hydrodynamic models coupled with radiative transfer simulations makes drawing comparisons from that ratio to quantities such as M_{Ni} , M_{ej} , and E_k challenging. Unlike analytic methods, hydrodynamic models coupled with radiative transfer simulations can be time consuming due to the uncertain nature and interconnected behaviours that occur when changing variables. This is where a parameter study can fit in as an extension to available data to determine how variables can affect observable properties (Young 2004). As shown in this work, a single mass with a single E_k but variable mixing can produce SN spectra with a different N -value. Using multiple models, with different M_{ej} , variable E_k , and a range of mixing approximations, can generate a spectral and photometric library that may constrain some parameters. A bulk study of these initial variables combined with physically reasonable and tunable parameters can be used to generate a wide set of possible progenitors that then can be compared to observed photometry and spectra.

Turbulent mixing can be approximated in 1D, but large-scale asymmetries or 3D mixing processes may be underestimated. In this work, a density spike in the original explosion models led to unrealistic light curves and spectra for those models. Therefore, the spike was smoothed out when mixing was applied. However, altering the model in such a way may nullify the predictive power of an evolutionary model. The time and computational cost required to

model turbulence accurately in 2D or 3D simulations limits the ease with which explosion models can be generated to match observed SNe. Implementing the Rayleigh–Taylor instability formulation in 1D (Duffell 2016) may help produce an evolutionary model that can match spectroscopic and photometric SN data.

7 CONCLUSIONS

In this work, we exploded a 22 M_{\odot} progenitor stripped to a bare CO core with E_k of 1, 3, 5, and 8 foe using the 1D explosion code PROMETHEUS-HOTB. For each explosion model, we alternatively do not mix, partially mix, or completely mix the composition of the ejecta and the innermost density. For each combination of E_k and mixing, we generated a light curve and a time-series of spectra. Each model was then classified using the methods from Prentice & Mazzali (2017) and compared to SNe with similar classifications.

We showed that the extent of the mixing of Fe group elements and ^{56}Ni in the ejecta of a SESNe alters both the light curve and the spectra. Hydrodynamic explosion models, with no modification, are characterized by a positive density gradient at the edge of the ^{56}Ni -forming region that can prevent the escape of photons from the deposition of $^{56}\text{Ni}/^{56}\text{Co}$ decay products. Smoothing out the structure of this interior density region and mixing ^{56}Ni outwards into the ejecta produce much broader light curves.

We also show that the combination of mixing the ejecta and increasing E_k leads to SNe with broader lines (Fig. 12). Broad-lined SNe may be the combined result of high E_k , significant mixing, and ejecta mass. SNe Ic-BL are the only ones that correlate with long GRB, which are high-energy events that often include a jet (Woosley & Eastman 1997; Ashall et al. 2019). Jet-driven SNe material likely results in more mixing than found in SNe with smaller E_k .

Future work would expand this analysis towards Type Ib/IIb SNe. The formation of He lines are sensitive to the mass and mixing of the ^{56}Ni in the ejecta (Lucy 1991; Hachinger et al. 2012). Depending on the mass of He in the outer ejecta, the mixing of ^{56}Ni may determine whether or not He is visible during the spectral evolution. This is a partial continuation of work done by Hachinger et al. (2012) in which the mass of He or H present in the outer layers of the star was altered to determine the lower limits of possible H/He masses given some constraints. Continuing this work on SNe Ic, additional grid points with respect to mass will be considered using progenitors with smaller and larger masses. This would expand the parameter space explored, covering most of the measured ejecta masses using for the same grid of explosion energies and mixing approximations.

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