

Practices and Challenges of Active Learning Methods in Mathematics Classes of Upper Primary Schools

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Abstract

The purposes of this study were to explore the nature of the teaching-learning process in line with active learning methods (ALMs) and to identify the major challenges hindering the implementation of these approaches in mathematics classes of upper primary schools. Both qualitative and quantitative methods of data collection were employed. Random sampling technique for students and availability sampling technique for teachers were used. 25 mathematics teachers and 710 students were involved in the study. Questionnaires, lesson observation, and focus groups discussion were the data gathering instruments used. The quantitative data obtained were analyzed using frequency, percentages & mean values. The qualitative data were analyzed by narrating the information obtained from the data. Questioning method, group work, gap lecture, cooperative learning, and individual work were the methods used commonly by the teachers. Large class size; the amount of content to be covered; lack of instructional materials; lack of administrative support; and that it took too much effort from teachers are main challenges that hinder the application of ALMs in the classrooms. Based on the findings, different recommendations are forwarded to address those problems and to improve the use of ALMs in mathematics in the study area.

Keywords: Active learning, challenges of active learning, mathematics, student centered

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1. Introduction

Teaching for understanding is an agenda in educational practice that has been receiving significant interest in international educational communities since the late 1980s (Rutherford and Ahlgren, 1990; Wiske, 1998). In other contexts, it is called 'active learning' (Organization for Economic Co-operation and Development, 1993), 'higher-level cognitive learning' and 'teaching for the twenty-first century' (NCTM 2000). Teaching for understanding (active learning) helps learners to develop their potential as individuals and to make responsible decisions for living and working in the 21st century.

Mathematics helps us think analytically and have better reasoning abilities. Analytical thinking refers to the ability to think critically about the world around us. Analytical and reasoning skills are important because they help us solve problems and look for solutions. Mathematics learning should be about developing conceptual understanding in order to prepare our students for the 21st Century. Successful 21st Century mathematics learning needs to foster 21st Century skills such as communication, collaboration, critical thinking and problem solving.

The overall quality of teaching and learning is improved when students have full opportunities to clarify, question, apply and consolidate new knowledge. In this case, teachers create opportunities for students to engage new material, serving as guides to help them understand and apply information. Student achievement in mathematics increases through mastery of content as a result of active learning techniques. Active learning, at the same time, is a social process that also has recorded multiple benefits for the academic achievements of students on various levels. In the process of solving mathematical problems, such learning can be utilized to attain optimal outcome and build a foundation for the future of students' learning. Students also develop improved problem solving, communication, and higher order thinking skills.

Research has consistently shown that students' attention and concentration during straight lectures tend to drop off dramatically after 15-20 minutes (Penner, 1984; Verner and Dickinson, 1967) even among highly motivated postgraduate students (Stuart and Rutherford, 1978). This is because learning is by its nature an active process which requires engagement and the use of higher order thinking skills such as analyzing, synthesizing and evaluating scientific or mathematical problems and findings.

The teacher-centered method of teaching has a little effect on mathematics learning of students in which the majority of teachers reported that they were not succeeding in teaching concepts of mathematics. (Melaku & Solomon, 2013). Thus, regarding teaching methods, researchers reached on the conclusion that if we want students to become more effective in meaningful learning and thinking, they need to spend more time in active, meaningful learning and thinking, not just sitting and passively receiving information (McKeachie *et al.*, 1986).

Based on this aim in mind, the following basic questions guided this study.

1. What is the status of the implementation practices of active learning methods in upper primary schools of Woliso town?

2. What are the challenges affecting the implementation of active learning methods (ALMs) in upper primary schools of Woliso town?

2. REVIEW OF RELATED LITERATURES

2.1 Conceptual Framework

The active learning framework is a way of thinking about planning for teaching that is purposeful and valuable for primary school students. By including carefully selected intellectual, social, and physical activities into primary school especially, the middle grades classroom, teachers can meet the unique developmental needs of young adolescents while teaching the important content these students need to learn to be empowered to think critically about the world around them (Edwards, 2015). Incorporating all three of these into lessons will not only create a better learning environment and different learning opportunities for students, but it will also bring more pleasure and interest into any primary school classroom.

Instructional strategies centered on active learning include intellectually active learning activities such as problem-solving tasks, questioning, and inquiry. Additionally, social (e.g. discussion methods) and physical (e.g. hands on activities) activities are also important instructional strategies included in this field. The framework for thinking about active learning in middle-grade mathematics classrooms can be expressed by the relationship between intellectual, social and physical activities. Middle grades students respond well to active learning, but there are different ways of thinking about activity in the classroom. Instructional strategies that require students to be intellectually active should certainly be at the heart of any mathematics lesson; however, early adolescents need other types of active learning strategies as well, and mathematical problem solving promotes this activity. The following Venn diagram is purposefully selected to represent the active learning framework in this study.

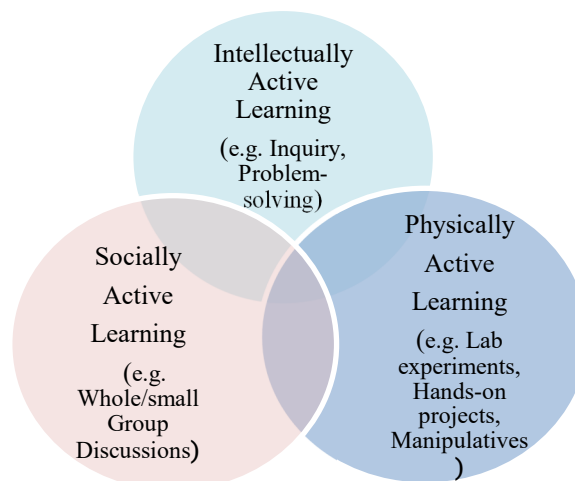


Fig 1: Active learning framework (*Taken & modified from Susan Edwards, 2015*)

2.2 Definitions of Active Learning

All learning is active in a certain sense, but some kinds of learning are more active than others. A formal definition of Meyers and Jones states that Active Learning is learning that allows “students to talk and listen, read, write, and reflect as they approach the course content through problem-solving exercises, small informal groups, simulations, case studies, role-playing, and other activities – all of which require students to apply what they are learning” (Meyers & Jones 1993). Active learning can also be generally defined as any instructional method that engages students in the learning process (Prince 2004). In short, active learning requires students to do meaningful learning activities and think about what they are doing. The core elements of active learning are student activity and engagement in the learning process. Therefore Michael (2006) also described active learning as the process of keeping students mentally, and often physically, active in their learning through activities that involve them in gathering information, thinking, and problem solving.

2.3 Theoretical Bases of Active Learning

Active learning methods are widely-spread nowadays and often associate with constructivism. Although constructivism was not a pedagogical teaching, many of its followers developed practical applications of the theory in learning practice. Constructivist learning theory emphasizes that individuals learn through building their own knowledge, connecting new ideas and experiences to existing knowledge and experiences to form new or enhanced understanding (Bransford *et al.*, 1999).

2.4 Instructional Strategies that Facilitate Active Learning

Active learning instructional strategies include a wide range of activities that share the common element of—involving students in doing things and thinking about the things they are doing (Bonwell & Eison 1991). Active learning instructional strategies can be created and used to engage students in thinking critically or creatively, speaking with a partner, in a small group, or with the entire class, expressing ideas through writing, exploring personal attitudes and values, giving and receiving feedback, and reflecting upon the learning process (Edwards, 2015). Some instructional strategies that facilitate active learning are: using effective questioning strategies to elicit student involvement in class; acknowledging the name of the student who gave a response voluntarily; recording student ideas on the blackboard; occasionally redirecting questions directed at teachers to other students in class by asking for volunteers to answer the question and etc. Some student-centered, active learning approaches which can be applied mostly for science & mathematics subjects from Michael and Modell (2003) are Problem-based or case-based learning, Cooperative/collaborative learning, group work, Think-pair-share or peer instruction, Conceptual change strategies, Inquiry-based learning, Discovery learning and Technology-enhanced learning.

2.5 Effective Strategies for Teaching Elementary Mathematics

Teaching in today's mixed-ability classroom can be a challenge. These days, it's not uncommon to find a wide range of abilities in the one classroom—from students struggling to grasp new concepts, to those who are way ahead of their peers from day one. This factor has contributed to a range of problems for early mathematics learners, including a large achievement gap between students. While individual students do benefit from different learning styles, there are a range of effective strategies which can help all students to succeed. Some effective strategies for teaching elementary mathematics are making it hands-on; using visuals and images; showing and telling new concepts and giving feedback. If we expect students to apply the knowledge they are learning in our classrooms, then we must help them develop the intellectual tools and problem-solving skills necessary to practice doing something with what they are learning (Mischel, 2006).

2.6 Teachers' Interest in Active Learning

Teachers are interested in active learning for several reasons. They are aware that students must be prepared for continual learning throughout their lifetimes. Teachers experience the need for continual learning in their own professional lives, due in part to professional development programs that are provided for them. Teachers are also aware of accumulating research on how people learn. As the constructivist paradigm has come to dominate educational research, educational literature, and teaching in schools of education, it has exerted a strong force on practicing teachers.

2.7 Obstacles to Active Learning in Classrooms

Despite teachers' interest in active learning, they are not always able to arrange for students to do it. One obstacle is that some students find it threatening. They do not want the challenge, or they are more comfortable in a more passive role. Another barrier is the possible conflict with required curriculum and accompanying examinations. Active learning projects take time. They may deepen students' understanding of certain ideas, but teachers may be concerned about sacrificing breadth of coverage. If students' opportunities for further education depend on broad knowledge of material in the required syllabus, there may be little time for active learning. There is a basic contradiction between the goal of developing students' capacity to manage their own learning including the capacity to make good decisions about what to learn and the goal of teaching a predetermined school curriculum. On the other hand, some forms of active learning within the classroom can actually reduce some of the routine tasks teachers have to do, though this may not be evident at first. In co-operative learning, students are sometimes given responsibility for checking and correcting one another's works. This gives the teacher more time to work with students individually.

This leads to another obstacle, which is the necessity for teacher training. It is not sufficient for teachers merely to be told about a different way to teach. They need the opportunity for active learning. This begins by experiencing the new approach from the position of a student, and progresses to trying out the role of a teacher organizing learning processes for others. After supervised practice with the new method, teachers can be ready to use it in their own classrooms, but even then their effectiveness in implementing the new technique was greater if they continue to receive assistance. Teachers of middle school in some countries also mentioned that conditions for teaching (e.g., size of classrooms, number of students, and availability of instructional materials) affected their ability to implement active-learning strategies (Ginsburg M, 2009). As commonly observed in teaching learning mathematics, teachers perceive active learning as if it demands too much effort from them, is additional work load on them and it leads to classroom disturbance are additional factors that hinder the implementation of active learning techniques in classrooms.

Several impediments to active learning have to do with student characteristics. The first student factor

concerns learning conceptions. Students differ in the way they see the fundamentals of learning and the division of tasks between teachers and students. On the one hand there were students who regard learning as copying ideas and information out of books and the heads of teachers into their own heads. These students tend to see teachers as responsible for structuring presentations and assignments.

A second set of impediments to active learning has to do with learning goals. Many students do not think about the goals of learning, they take learning for granted (Saljö, 1979; Thomas and Harri-Augstein, 1985). A related problem concerns students' perceptions of tests and exam demands. Even if teachers value higher level goals, their testing practices are often perceived by students as stressing lower level goals. Motivational, volitional (deliberate intention) and affective factors may also impede active learning. For instance, there are students who are afraid of changing their learning approach. Some students, trying to reduce uncertainty, practice active learning in an unproductive way. Furthermore, students may fail to believe that active learning really "works" (i.e. that you can remember information just by thinking about it). Some students also believe that active learning requires too much effort or energy. Students who do not believe that they are able to learn in active way and reach acceptable or even better results (lack of self-confidence), may not even try to engage in it. A fourth impediment concerns the skill of active learning itself. Students who do not use certain activities will lack the necessary learning skills (elaboration, analyzing, etc.). Many students also lack regulation skills.

Although students in many middle schools had experienced active learning during their mathematics classes, they criticized much of their education. The main reasons for the criticism can be many. Some specific obstacles associated with active learning includes limited class time, the density of the curriculum, the potential difficulty of using active learning in large classes, the lack of materials, equipment or resources, and the conservative attitudes of fellow students who did not like taking part in active learning (Aksit, Niemi, & Nevgi, 2016). In addition to the above challenges, fear of students to participate actively in the classroom, shortage of time because of busy coping notes on the board, and classroom management are other challenges that students face in using active learning methods in the classrooms.

Borkowski and Mutukrishna (1992) described metacognitive models of learning of teachers that form obstacles to active learning. Many teachers believe that learning occurs when students reach a certain task goal by doing what the teacher says. Teachers may hesitate to hand over responsibility to their students because the students are not prepared for it but this keeps the students perpetually unprepared. Larsson (1983) found that some teachers would like to give students more freedom to learn, but do not believe that students are able to handle this freedom. Other obstacles are lack of teaching materials for active learning, and the pressure of exams. Publishers and text books are, generally not suited for active learning. Finally, examination requirements may inhibit active learning. Teachers often believe, rightly or not, that material that will appear on exams must be taught through lectures. This is connected with the fact that many teachers consider themselves in the first place expert in a certain field and only in the second place a professional communicator and educator.

2.8 The classroom conditions

The condition of the classroom is one of the most important factors that should be considered in the teaching-learning process in general and active learning in mathematics education in particular. Burns and Myhill (2004) point out that the physical environment in classrooms can make or break active learning approaches. Thus, to engage students in learning activities the classroom should be well equipped with furniture. There should be a movable desk for every student to use different layouts in the classroom. In another study, Silberman in Zweck (2006) suggested 10 different types of classroom layouts, which facilitate active learning approaches. These layouts include a U-shape, team style, conference table, circle, group on group, work station breakout grouping, traditional classroom, auditorium arrangements etc.

Class size also has its own impact on the teaching-learning process in general and on the implementation of active learning in particular. As the number of students in a class increases like in Woliso town middle primary schools, students face any or all of the following problems: lack of clarity of purpose; knowledge about progress; advice on improvement; lack of opportunity to discussion; inability to support independent study and inability to motivate students (Berhanu, 2010). In contrast to the above, Jarvis (in Slavin, 2005:85-87) suggests that class size is not a significant factor in students' achievement. He found that individual teachers varied in their effectiveness in different class sizes. Some were more effective in large classes than in small ones, while others were less effective in large classes than in small ones. Other researchers have taken middle position. As stated by McKeachie (1999:158-166) whether a large or a small group is appropriate depends on the following factors: learning objective that are to be realized; nature of the subject to be taught; pupil attention and learning resources.

3. MATERIALS AND METHODS

3.1 Research Design

The study was conducted at six governmental upper primary schools (Grade 5 – Grade 8) in Woliso town of Oromia regional state, Ethiopia. These schools were selected by available sampling technique since there are only

six government primary schools in the town in 2018/19 academic year. The design of the research was descriptive survey type. The method involved the survey which describes the status quo and a brief discussion with an individual about a specific topic. Both qualitative and quantitative methods of data collection were employed which is a mixed method research design.

3.1.1 Subjects of the Study

The subjects of the study were students (grades 5- 8) and mathematics teachers of the schools in the academic year of 2018/19. All mathematics teachers in the selected schools were taken as sources of data. On this regard, 25 mathematics teachers participated in the study from the selected schools. By using random sampling technique, from the total populations of 4882 grade 5 – grade 8 students the sample of 733 students were selected from the sample schools.

3.1.2 Data Collection Instruments

In this study, questionnaire, lesson observation (LO) and focus group discussion (FGD) were used as instruments of data collection. Teacher's questionnaire was administered to 25 mathematics teachers teaching in the selected schools and only 21 of them were returned it. Teachers responded to a four point Likert Scale (1=Strongly Disagree, 2=Disagree, 3=Agree, 4= Strongly Agree) questionnaire that focuses on the implementation of ALMs and on the major problems/challenges that hinder them for the implementation of active learning approach in schools. Students' questionnaire was administered to 733 students of which 710 of them were returned and analyzed. The students' also responded to a four point Likert Scale questionnaire (1=Strongly Disagree, 2=Disagree, 3=Agree, 4= Strongly Agree) which was focus on the challenges that hinder to use the techniques in their classrooms and they responded on questionnaires by rating to five point scale (1=never, 2=seldom, 3=sometimes, 4= often, 5=always) which focuses on the use of ALMs. The researcher explained the purpose of the questionnaire and gave detail instruction on how to fill all the items face to face with all the students in the selected schools.

In addition to these, the researcher sat in the participants' class during their regular mathematics period and observed the teaching learning process and recorded it by using an observation checklist prepared earlier. In addition to this, the researcher recorded what he saw, heard, and experienced activities during a teaching session that are not included in the check list (Gay & Airasian 2000). In total 6 lessons (one lesson of 40 minutes from each six sample schools) by six different teachers were observed. Besides one focus group discussion held with voluntarily selected teachers (one mathematics teachers from each schools) and one focus group discussions held with voluntarily selected students (one student from sampled students in each school) were used to study actual classroom teaching and learning of mathematics. It was provided both teachers & students with the opportunity to express their views precisely on challenges of implementing active learning strategies in Mathematics teaching & learning.

Although, both teachers and students questionnaires were adapted from different sources of literature and modified for the current study, before they were utilized for the actual data collection in the schools, the researcher made a pilot study on 40 students at one primary school in other town. The overall Cronbach alpha reliability index was calculated (0.74) and checked for the reliability. The relative specificity of the topics of the discussion and the experiences of the moderators in FGD satisfied the minimum expected reliability of the focus group discussion. Additionally, this instrument was validated in such a way that the participants discussed the questions accordingly during the group discussion. Furthermore, each of the instruments was validated in the other way. Before the actual data collection will start the instruments were given to colleagues so as to get valuable comments and criticisms on the strengths and weaknesses of the items. Based on the comments obtained, necessary modifications were made. Thus, answers to the written questionnaire, records of lesson observation (LO) checklist and FGDs were used to study actual classroom teaching and learning of mathematics.

3.2 Methods of Data Analysis

After collecting all the necessary data on each of the issues, the data was edited, coded, tabulated and processed in a way appropriate to answer the research questions. The quantitative data obtained from mathematics teachers and students through the questionnaires were analyzed by using frequencies, percentages and mean values. Teachers' responses to the questionnaire on their practice of active learning methods were used to answer research question one. The closed ended items were expressed in percentages and averages for the total score calculated and discussed while the open-ended part was expressed and narrated qualitatively. The observation checklist data was analyzed by counting the scores of individual statements for the total of observed lessons and then expressing the counts in percentages. To supplement this result, the first parts of students' responses were described using percentage analysis and conclusion to research question one was reached. Students' responses to the second part of their questionnaire and the data collected from focus group discussion, and teacher's questionnaire on the challenges of implementing ALMs were used to answer the second question of this study. The responses of the questionnaires were described using percentage analysis and reported by merging the favorable continuum (Strongly Agree & Agree) and the unfavorable continuum. The focus group data was read repeatedly and entirely transcribed. Then all the data in the form of transcripts were reviewed and carefully organized to identify the key

themes using the coded key word approach and the results was described qualitatively. Generally, the qualitative data was narrated qualitatively using words, phrases, statements and paragraphs obtained from open-ended questions and FGDS. Hence the qualitative data was used as the complement of quantitative data. Finally, from the results, conclusions were made for each of the research questions and recommendations were forwarded.

4. RESULTS AND DISCUSSIONS

4.1 Analysis of Biographical Data of Teacher Respondents

From the biographical data of teacher respondents, 19% of the teachers were between 30 and 39 and 23.8% of the teachers were between 40 and 49 years old. This implies that there are many teachers in the schools who are productive and young enough to serve in teaching profession. Majority (57.2%) of teacher respondents were greater than 49 years old which implies that they are almost to finish their working service and will left few years to retire. Of the teachers, 62% were male and 38% were female. This study therefore shows that the participation of females as mathematics teachers is medium when compared to the number of male mathematics teachers in the sample schools. Only 9.5% of the teachers have six to ten years of experience and are therefore relatively inexperienced. Also 9.5% of the teachers served eleven to fifteen years, while only 14.3% of the respondents worked for sixteen to twenty years and 66.7% of the teacher respondents taught for more than 20 years and are therefore experienced in the profession. 71.4% of the teachers were qualified in diploma and 28.6% of them have undergraduate degree in mathematics. This implies that hard work is required of the regional or zonal education bureau to develop and capacitate their primary school mathematics teachers. Workload influences teaching style. In this regard the biographical data indicates that only 76.2% of the respondent teachers had a workload of 15 to 20 periods (1 period is 40 minutes long) per week and 23.8% of the teachers have workload that ranges from 21 to 25 periods per week. The implementation of active learning approaches requires a certain amount of time to think about and explore each topic. Such approaches may take more time than a lecture.

The above is complemented by the qualitative data. Lesson observation (LO) also indicated that the classroom seating arrangement does not allow teachers to employ active learning approaches comfortably. During Focus Group discussions (FGDs) some respondents complained that the large class sizes did not allow them to change this type of seating arrangements and it also had a great impact on the implementation of active learning approaches. Most teachers (66.7%) replied that a typical classroom generally has more than 69 students. This was confirmed by lesson observations: the researcher observed 60 to 75 students in any given class.

4.2 Teachers Use of Different Types of Active Learning Methods

Using questionnaires supported by LO and FGs, teacher's provision of students with opportunities to actively participate in the use of active learning methods and the types of active learning methods used by the teachers during their mathematics classroom instruction were described.

Table 1: Analysis of Lesson Observation (LO)

No	Criterion	Yes		No		Remarks
		N	%	N	%	
Methodology						
1	Did the teacher use appropriate methods (e.g. gap-lecture, individual work, questioning & answering) to the contents?	4	66.67	2	33.33	
2	Did group work given to students checked by the teacher carefully?	3	50	3	50	
3	Were the learning activities facilitated effectively?	3	50	3	50	
4	Did the teacher provide clear and constructive feedback	1	16.67	5	83.33	
5	Did the learning activities contribute to promote critical thinking / to develop inquiry skills?	4	66.67	2	33.33	
6	Did the t/r check students' understanding throughout the lesson using d/t assessment techniques?	3	50	3	50	
Student's participation						
7	Did many of the students actively engaged in the given activities both physically and mentally?	2	33.33	4	66.67	
8	Did many of the students respond to posed questions with their own words / from their mind?	4	66.67	2	33.33	
9	Did many of the students ask questions?	2	33.33	4	66.67	
10	Did many of the students connect prior knowledge and experience?	2	33.33	4	66.67	
11	Were the passive students encouraged to take part in the activities?	3	50	3	50	
Teaching and learning aids						
12	Did the teacher use any kind of teaching and learning materials apart from blackboard and chalk?	2	33.33	4	66.67	
13	Did the materials fit with the learning contents of lesson?	2	33.33	4	66.67	
14	Were the materials used in the lesson enhanced student's understandings?	0	0	6	100	
Lesson progression						
15	Were the introductory part motivating students well?	2	33.33	4	66.67	
16	Did t/r allocate sufficient time to each learning activity?	4	66.67	2	33.33	
17	Did t/r make appropriate pacing of lessons for stdnt l/g?	3	50	3	50	
18	Were both the teacher and the students able to conclude what they had learned in a lesson?	3	50	3	50	

From Table 1 above, teaching learning methods such as gap-lecture, individual work, questioning and answering and group work/discussion that seem to be participatory were observed in almost all classrooms, however, when they were examined closely, they were not strong enough. For instance, questioning and answering activities were merely promoting "simple recall" or "comprehension" aspects of the cognitive domain and individual works are done by few students. It was also noted that group works and discussions were not well-structured by teachers even though half of the teachers were tried to check dominant students answers in the group.

From the LOs, again, it was ascertained that half of the teachers were checked students' understanding throughout the lesson using different assessment techniques such as oral questioning, observation of students work and physical response even though only few of them (16.67%) gave constructive feedback for students response. So generally the methodologies used in the class were active but not properly applied because of some challenges such as large class size (teachers FGDs), lack of necessary materials (students & teachers FGDs) and problems of classroom management (LO & TQ). Again the LO results also revealed many of the students in six of the classes observed (66.67%) were not actively engaged in the given activities both physically and mentally. Half of the observed teachers were not encouraging passive students to participate in group work. Even though many of the students responded to posed questions in many (66.67%) classes observed with their own words / from their mind, a small number of students ask questions in many (66.67%) of the observed lessons. On the other hand, in the FGs for students, the sampled students expressed that they would enjoy the subject and learn them better if they had chance to like working on practical activities and real-life related problems. However, according to the students the current classroom teaching learning situation did not promote this, because it had very little practical work because of shortage of time and large class size.

Concerning teacher's use of teaching and learning aids, from the six teachers observed, two teachers used teaching and learning materials apart from blackboard and chalk. The teachers ordered students to use a ruler and protractor to sketch and measure angles, but group dominant students performed the task. The teachers also accepted the correct answer of fast students from the groups but did not check the other students' response for the given activity. The materials used in the lesson enhanced the student's understanding. The progress of the lessons observed in all the classes were very good except the introductory part of many lessons (66.67%) which were not

motivating students well because the teachers went directly to presentation of the day's lesson. Next to this, results from teachers' questionnaire presented and can be analyzed as follows.

Table 2: Data from Teachers' Questionnaire

(key: 1=Strongly Disagree, 2=Disagree, 3=Agree, 4=Strongly Agree)

No.	Category 1: Items	1		2		3		4		Total		Mean
		F	%	f	%	F	%	f	%	N	%	
1	I think that t/rs are the best way to teach s/ts to solve maths problems.	1	4.8	7	33.3	7	33.3	6	28.6	21	100	2.86
2	I consciously facilitate problem solving in the mathematics class.	0	0	7	33.3	9	42.9	5	23.8	21	100	2.9
3	I support the stdnts to discover the desired conceptual knowledge in the l/g process for themselves.	3	14.3	5	23.8	7	33.3	6	28.6	21	100	2.76
4	I encourage students to ask q'ns .	1	4.8	2	9.5	11	52.4	7	33.3	21	100	3.24
5	I think that inquiry learning is effective to actively involve stdts in the maths learning process.	0	0	4	19	11	52.4	6	28.6	21	100	3.1
6	I rarely arrange the students into groups for maths team work.	4	19	9	42.9	6	28.1	2	9.5	21	100	2.29
7	I think that discussions b/n the stdts on a given lesson topic are vital for deep understanding.	1	4.8	3	14.3	9	42.9	8	38.1	21	100	3.14
8	I think cooperative work in groups is good for efficient learning.	1	4.8	5	23.8	8	38.1	7	33.3	21	100	3
9	I prepare a hands-on projects for students to present in the classroom	4	19	9	42.9	6	28.6	2	9.5	21	100	2.29
10	I let my students to use manipulatives to understand mathematical concepts	6	28.1	12	57.1	2	9.5	1	4.8	21	100	3.57

From Table 2 above we can deduce that the practices of active learning methods by the teachers in the classrooms are seen from the conceptual framework described earlier. Therefore, we see that the average value for intellectually active learning activities (Items 1-5) is 71.44% for the favorable continuum (Agree & Strongly Agree) and 28.56% for the unfavorable continuum (disagree & Strongly disagree), for socially active learning activities (Items 6-8) is 63.33% for the favorable continuum (Agree & Strongly Agree) and 36.53% for the unfavorable continuum (disagree & Strongly disagree) and for physically active learning activities (Items number 9 & 10) is 26.2% for the favorable continuum (Agree & Strongly Agree) and 73.8% for the unfavorable continuum (disagree & Strongly disagree). Thus, we can conclude that teachers were practicing more of (71.44%) intellectually active learning activities than socially active learning activities (63.33%) and physically active learning activities (26.2%). The analysis of each item can be done as follows.

Regarding formation of group for team work, an item number six stated: "I rarely arrange the students into groups for mathematics team work." the result shows that 61.9 % of the teachers disagreed and 37.6 % of them agreed with this statement. On item number eight, which states, cooperative work in groups is good for efficient learning, 71.4% teachers also agreed. Accordingly, they responded positively on the item that stated a cooperative learning is needed to help the students understand new concepts. So many teachers (81%) thought that discussions between the students on a given lesson topic are vital for deep understanding. Many students (25%) also stated in their questionnaire that their teacher often facilitated their learning rather than their own teaching in the class. This shows that the teachers realize that lecturing alone is not enough to prepare students to understand their lesson and hence, they support students to work in groups and learn cooperatively in mathematics classes.

For the item number five, if inquiry-learning is effective to actively involve students in the mathematics learning process, 52.4% and 28.6% of teachers agreed or strongly agreed (mean value, 3.1). This is in line with item number two that stated facilitation of problem solving in the mathematics class: about 66.7% of teachers showed their agreement (mean value of 2.9). However, the researcher observed that only fast learners were helped by the teacher to solve problems in the classrooms. This was confirmed by the FGDs that indicated most of the time, fast learners only helped in problem solving and inquiry learning in mathematics classes.

Problem-solving skill is not only helpful in dealing with mathematics problems but also critical to solving the

real-life situations which we encounter in our daily lives (Morgan 2007). Most of the teachers thus seem to realize the importance of active, discovery learning rather than thinking themselves as the best way to teach students to solve mathematics problems. From FGDs of teachers again it was raised that the teachers encourage students to ask questions. This seems to indicate that most teachers believe that lecturing alone is not enough for learning well. Many students (45.28%) also recognized in their questionnaire that their teacher often made them to show their solutions to the whole group and discuss any differences among the solutions (students' questionnaire, item 5). Besides, the majority of the respondent teachers (61.9% and, mean 2.76) indicated that they supported students to discover the desired conceptual knowledge in the learning process for themselves. This result is confirmed by lesson observation as the sample shown by figure 1 below.



Fig 1: Grade 5 Students Measuring in Group the Given Angle Using Protractor

However, observation confirmed that in some of the cases the role of the students was to listen carefully to the teacher's lecture and writing notes from the blackboard. The role of some students was to memorize the facts and rules lectured on and to implement them (one student said in FGD). In addition, few students seemed to prefer to work individually in class. It was observed that in group work there were some students who did not do their share of the work. Students' opinions on the implementation of ALMs can also be analyzed as follows (Appendix B).

According to students response on the item that asks about teachers' ending activities of the lesson, 30.56% of students said their teachers asks them questions like "what was the main point of today's lesson?" sometimes and 32.78% of the students said that their teacher never made them to summarize the answers given by another students. Besides 11.67% of students said that their teacher never posed questions to be worked on in the group that kept groups on task and also do not ask them (18.89%) to go to the blackboard to solve problems. 36.67% of students said their teacher often showed them how to use different strategies when working on a variety of tasks and 9.44% of students blamed their teacher concerning this aspect. Considerable amount of student respondents (23.61%) said they were never provided with multiple opportunities to practice the skills being taught by their mathematics teachers. 62.8% of students replied to the item "Do your teacher connected the topics being covered to your daily life?" positively where as 37.22% of respondents replied negatively to this item.

The results of this study indicate that the teachers implemented active learning/student centered approaches at various stages of the instructional process to some extent (Grand mean 2.83 and 2.9). Generally, from this study, ALMs that were most commonly used and least practiced by the teachers & students are summarized by the table below.

Table 3: Most commonly used and the least practiced active learning methods in mathematics classes

	Teacher's Questionnaire	Lesson Observation	FGD
Most commonly used teaching methods			
1	Questioning/Inquiry Learning	Lecture/ Gap lecture	Lecture
2	Group Discussion	Group discussion/ Group Work	Group discussion
3	Lecture	Questioning	Individual Work
4	Cooperative Learning	Individual Work	
The least practiced teaching methods			
1	Discovery	Problem solving	Presentation of students
2	Practical work	Practical Work	
3	Problem Solving	Cooperative Learning	-

We as teachers have typically suspected - students can often do the mechanical things we ask with certain content/topic but there is not always a high level of understanding behind these computations (Melaku & Solomon 2013). In active learning classrooms, students are engaged in activities like dialogue, debate, writing, discussion and problem solving as well as higher order thinking such as analysis, synthesis and evaluation.

In the teaching learning process, lessons can be divided into: starting phase (summarizing work covered in previous lessons); new content introduction phase, central phase (explanation of the content); activities phase (students work on the content); closing (final feedback) phase. The classroom observations showed that many of the phases, with the exception of central phase, are student-centered approaches. Further, some students in the observed classes were responsible only to listen to lectures, take notes and respond to questions upon request. This is associated with the students' prior experience of active learning, as pointed out by most of teachers in the FGs. Students have no experience to play the active roles expected of them because many come from authoritarian cultural backgrounds and therefore talk only when motivated by someone. Discussion methods help to facilitate active learning/student-centered approaches, as indicated by the work of Baines, Blatchford and Chowne (2007). However, a number of the teachers said that interaction occurred more easily in a relatively small class size (Teacher's FGDs).

Most participants in FGDs also commented on improper use of active learning approaches in their teaching practice. Some said that any transformation from a teacher-centered classroom to an active learning/student-centered classroom, since it involves fundamental change, will meet with resistance. In contrast, a number of teachers noted that it was an approach they already used, had used for a considerable time, or was an implicit part of teaching their mathematics subjects.

4.3 Challenges of Using ALMs and Supports Provided for its Implementation

Using questionnaires supported by classroom observation and FGs, factors that hindered the implementation of active learning approaches in the sample schools (indicated by Table 4 and Table 5) were determined and analyzed as follows.

Table 4: Students' Response on Challenges of Implementing ALMs in the Classroom

(key: 1=Strongly Disagree, 2=Disagree, 3=Agree, 4=Strongly Agree)

No.	Challenges /limiting factors	4		3		2		1		Total		Mean
		F	%	F	%	F	%	F	%	N	%	
1	Shortage of time in the class room.	78	21.7	100	27.7	174	48.3	8	2.22	360	100	2.70
2	Students don't want to talk about the lesson during teaching learning process.	95	26.4	192	53.3	54	15.0	19	5.28	360	100	3.02
3	Teachers' negligence in participating students in the class.	8	2.22	122	33.8	164	45.56	66	18.33	360	100	2.21
4	Teachers didn't control the group learning activities	66	18.3	84	23.3	148	41.1	62	17.22	360	100	2.44
5	Many of the time, our teacher use lecture method in the class.	124	34.4	96	26.7	124	34.4	16	4.44	360	100	2.92
6	Lack of necessary materials (e.g. Papers, diagrams...)	143	39.7	89	24.7	98	27.2	30	8.33	360	100	2.97

Table 4 shows data collected from students' questionnaire on factors hindering the implementation of active

learning approaches. As indicated by the percentages in the Table, the following were mentioned as the major factors: Students don't want to talk about the lesson during teaching learning process (79.72%); Lack of necessary materials (e.g. papers, diagrams...) (64.44%); Many of the time, our teacher use lecture method in the class. (61.11%); Shortage of time in the class room. (49.44%); Teachers didn't control the group learning activities (41.66%); Teachers' negligence in participating students in the class (36.11%).

Table 5: Teachers Response on Challenges of Implementing ALMs in the Classroom

(key: 1=Strongly Disagree, 2=Disagree, 3=Agree, 4=Strongly Agree)

No.	Category Challenges/influencing factors in implementation of ALMs in maths classes.	(1)		(2)		(3)		(4)		Total		Mean
		f	%	f	%	f	%	F	%	N	%	
1	There is a lack of time to actively involve students in my classroom.	2	9.5	2	9.5	12	57.1	5	23.8	21	100	2.95
2	To involve students in active learning will add too much to my work load.	3	14.3	4	19.0	12	57.1	2	9.5	21	100	2.62
3	Active student learning will create problems in my classroom management.	3	14.3	5	23.8	10	47.6	3	14.3	21	100	2.62
4	The amount of content that needs to be covered prevents the use of active learning in the classroom.	4	19.0	4	19.0	8	38.1	5	23.8	21	100	2.67
5	Active learning demands too much effort from teachers.	0	0.0	2	9.5	15	71.4	4	19.0	21	100	3.10

Table 5 shows teachers' responses on factors hindering the implementation of active learning approaches: The result shows that Active learning demands too much effort from teachers (90.48%); there is a lack of time to actively involve students in my classroom teaching (80.95%); to involve students in active learning will add too much to my work load (66.67%); active student learning will create problems in my classroom management (61.9%); the amount of content that needs to be covered prevents the use of active learning in the classroom (61.9%). During the FGs of teachers, teacher participants were asked: *What are the factors/challenges that limit you in applying different active learning methods in teaching mathematics at your school?* Teachers' responses focused on lack of necessary materials, classroom conditions and shortage of time. Examples include:

Theoretically active learning is very useful, but practically difficult to apply for a number of reasons like large class size, work load of teachers, lack of teaching materials, and lack of interest and some complaints of both the teachers and students...

The major challenges identified by the students in using ALMs in mathematics classes were: Students don't want to talk about the lesson during teaching learning process (79.72%); Lack of necessary materials (e.g. papers, diagrams...) (64.44%); Many of the time, teachers use lecture method in the class. (61.11%); Shortage of time in the class room. (49.44%); Teachers didn't control the group learning activities (41.66%). Moreover, during the FGD of students, participants were asked: *What are the factors/challenges that limit you in using different active learning methods in learning mathematics at your school?* Students' responses focused on lack of necessary materials, classroom conditions and ability of students to master the content by them. Examples include:

Most of the time, our teacher explain the lesson and finally give us class work. But only few students do the class work in a given time. Many of students cannot accomplish the task because of no need (fear)of discussing with each other on the question, shortage of time, waiting the teacher to do it, lack of paper to practice & some students disturbance.

The result of teachers' responses to the questionnaire on factors hindering the implementation of active learning approaches are: Active learning demands too much effort from teachers (90.48%); lack of time (80.95%); to involve students in active learning will add too much to my work load (66.67%); active student learning will create problems in my classroom management (61.9%); the wide amount of content that needs to be covered (61.9%). During the FGD of teachers, teacher participants were asked: *What are the factors/challenges that limit you in applying different active learning methods in teaching mathematics at your school?* Teachers' responses focused on lack of necessary materials, classroom conditions and shortage of time. Examples include:

Theoretically active learning is very useful, but practically difficult to apply for a number of reasons like large class size, work load of teachers, lack of teaching materials, and lack of interest and some complaints of both the teachers and students...

4.4 Discussion

In this section the results of the study are discussed regarding teachers' use of active learning/ teaching methods

in class and major factors affecting the implementation of active learning approaches.

4.4.1 Teachers' Use of Active Learning in the Teaching-learning Process

Many educators describe the constructivist approach to learning as a process whereby students work individually or in small groups to explore, investigate and solve authentic problems and become actively engaged in seeking knowledge and information. Everyone does not learn math the same way and regularly implements a variety of strategies (Edwards, 2015). In active learning approaches, students participate actively in their learning and become autonomous learners who actively construct new meaning within the context of their current knowledge, experiences and social environments. Active learning gives students the opportunity to learn through their own efforts and to take full responsibility for their own learning with the teachers as facilitators (Berhanu, 2010).

The results of this study indicate that school teachers implemented active learning approaches at various stages of the instructional process to some extent. It is not only teachers' that affect the implementation of active learning approaches. Students also affect how learning is practiced and how teaching is organized. In the FGDs, some teachers complained that some students had negative attitudes towards active learning approaches. It is known that learning is active when students take the initiative and responsibility for their own learning and this is dependent on students' positive attitudes. This is not the case in the sample schools, where observation indicated that some of the teachers mainly used lectures to teach students to solve mathematics problems and they rarely arranged the students into groups for mathematics team work. This may be caused by large class sizes. It was also shown that majority of the sample teachers (62%) thought that teachers should decide the best way to teach students to solve mathematics problems. However, students build and share their own knowledge with others when they interact with each other and with their teachers (Zweck, 2006). Furthermore, active learning/student-centered approaches such as the inquiry method; problem solving and discovery methods which foster the critical thinking and problem-solving capacity of students were not widely employed. In this regard Balim (2009) emphasizes that students should do more than just listen. They need to read, write, discuss or engage in problem solving activities. In active learning classrooms, students are engaged in activities like dialogue, debate, writing, discussion and problem solving as well as higher order thinking such as analysis, synthesis and evaluation. In the teaching learning process, lessons can be divided into: starting phase (summarizing work covered in previous lessons); new content introduction phase, central phase (explanation of the content); activities phase (students work on the content); closing (final feedback) phase. The lesson observations showed that all the phases, with the exception of central phase which takes more than half of the time, are student-centered approaches. It was also observed that low level order questions were frequently asked by the teachers and only a few students try to answer. This is also supported by the result obtained from the student's FGD by indicating that their teacher asks oral questions many times and even give the answer by himself.

Further, a number of students in the observed classes were responsible only to listen to teachers, take notes and respond to questions upon request. This is associated with the students' prior experience of active learning, as pointed out by most of teachers. Students have no experience to play the active roles expected of them because many come from authoritarian cultural backgrounds and therefore talk only when motivated by someone. Teachers don't take this into consideration when they encourage student participation in instructional processes. This is confirmed by the classroom observation and FGD of teachers. Therefore, all teachers should begin to reform their teaching, employing those particular approaches to fostering active learning that match the needs of our students, our particular courses, and our own teaching styles and personalities. There are plenty of options from which we can choose, so there is no reason not to start. This will mean that we too becomes learners in the classroom.

Discussion methods help to facilitate active learning/student-centered approaches, as indicated by the work of Baines, Blatchford and Chowne (2007:674-676). Discussion can help to develop improved cognitions. Most of the teachers stated that discussion was important. However, a number of the sampled teachers said that interaction occurred more easily in a relatively small class. In summary, in the sample schools instruction/teaching-learning was mixed (both teachers and student centered) instruction. However, research shows that learning is enhanced in contexts where students have supportive relationships, have a sense of ownership and control over the learning process, and can learn with and from each other in safe and trusting learning environments (McCombs, 2003). When we involve students in learning activities that require them to be intellectually, socially, and physically engaged, they will retain the content we want them to remember better (Edwards 2015).

4.4.2 The Major Factors/Challenges Influencing the Implementation of ALMs

According to FGDs, many teachers believed that lack of classroom space and large classes prevented group work. In addition, the following prevented implementation of active learning: lack of time to actively involve students in teaching; the amount of content to be covered; lack of resources; lack of instructional materials; lack of administrative support; and that is took too much effort from teachers. This was confirmed during FGDs of teachers and students.

According to Weimer (2002), for the effective implementation of active learning/student-centered approaches the principals and department heads of the school also need to recognize active learning approaches as building blocks for lifelong learning and provide the support required from them. However, in this study lack of

administrative support and lack of resources inhibited the implementation of active learning in class.

As mentioned, content coverage was a high priority for teachers. Although some teachers indicated that they covered some or most content with active learning approaches, other adopters of active learning approaches indicated that they covered less content than when they lectured exclusively, but that students were learning more. Silberman in Zweck (2006) showed that students in contexts in which teachers paused at intervals and talked six minutes less performed significantly better on the same examination than students in contents where teacher lectured the entire time. Time was an issue. Based on their experience, a large number of teachers thought that active learning would take up more time than the traditional way of teaching. Some teachers believed that due to time constraints, active learning could not be applied in a short period of time. They also believed that the students were passive and that it took a long time to motivate them. The curricular materials and classroom environment were also factors that played a role (FGDs of teachers). For active learning, the materials should include carefully sequenced sets of guiding activities designed to be performed actively by the students. However, as shown by responses from the majority of teachers and as observed, the activities during instruction were not presented in a way to encourage independent, purposive and a reflective way of learning. As mentioned by Feden and Vogel (2003), active learning and teaching materials should contain plenty of exercises and samples of work. They should also be flexible and allow students the time to work at their own pace and using their own methods. But in the present study, teaching materials were filled with large amounts of information to be memorized by the students. Thus, many teachers felt responsible to cover the curriculum in the time provided by a rigid time table. Class size was also a factor. McKeatchie and Svinicki (2005) stated that in a large class, individualization of instruction is limited.

FGDs also indicated that a factor that influences the implementation of the approach is interpersonal relationships or interactions among individuals. Active learning approaches are characterized by “empathic, supportive relationships which free students to discuss their feelings and experiences” so that students are “actively involved in learning through the given opportunities to predict, infer, generalize, and evaluate” (Duffy and Kirkley, 2004). The role of the students in active learning approaches is learning by doing. So as to engage students in learning activities, the classroom should be well equipped with the appropriate furniture and there should be movable desks for every student to use in different layouts in the classroom. From this point of view, the arrangement of desks and tables should allow movement and communication and should be changed whenever necessary. Furthermore, ample teaching resources should be available to implement active learning approaches as required. In this regard, the majority of student respondents (64.4%) replied that they were constrained by lack of adequate resources for using active learning approaches (see Table 6). The data obtained from classroom observation show that some of the classroom seating (the front to back arrangement) does not allow teachers to employ active learning approaches. The desks and tables in most of the classrooms were heavy and could not easily be moved.

5. CONCLUSION

Mathematics teachers of the sample schools encouraged students to ask questions; to deduce general principles from practical exercises and facilitate some problem solving in the mathematics classes. Besides, active learning methods such as the inquiry/questioning method, group work/discussion, cooperative learning, individual work and discovery methods were commonly used by some teachers. The basic active learning activities which were not implemented by most of the observed teachers in the sample schools include physical activities such as hands on projects, manipulative, using cooperative groups for problem solving activities; and facilitating students' curiosity/interest. The inadequate use of the different active learning methods would negatively influence the quality of the teaching-learning process; negatively affect development of self-learning, higher order thinking and problem solving capacities among the students. In this regard the researcher support active learning as pedagogical approach but teachers need to be aware of the constraints that they may face. By incorporating carefully selected intellectual, social, and physical activities into the their classroom, teachers can meet the unique developmental needs of young students while teaching the important content these students need to learn to be empowered to think critically about the world around them.

Active learning helps teachers modify their traditional roles and encourages them to conduct more student-centered applications. If a program is grounded in, or moving toward, a constructivist paradigm, active learning could be a valuable tool for helping teachers construct knowledge about teaching and learning. Teachers should have a more active role as developers of teaching, and they are also seen as being more responsible for the development of their own profession in a larger sense. Teachers' culture should provide more active learning experiences to prepare them to use new methods with their students in schools. Thus, they should be qualified, trained and must be well prepared, especially in improving the quality of education that faces global challenges. Even though large class size; the amount of content to be covered; lack of instructional materials; lack of administrative support; and that it took too much effort from teachers are main challenges identified by respondents all of the teachers participated in this study were able to use ALMs in their classrooms as much as possible. Though

they were trying to select appropriate active learning strategies, they were able to help all students more to involve actively in all activities done in the classrooms intellectually, physically and socially.

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