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Bounded Evaluation: Querying Big Data with Bounded Resources

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Abstract: This work aims to reduce queries on big data to computations on small data, and hence make querying big data possible under bounded resources. A query Q is boundedly evaluable when posed on any big dataset \mathcal{D} , there exists a fraction \mathcal{D}_Q of \mathcal{D} such that $Q(\mathcal{D}) = Q(\mathcal{D}_Q)$, and the cost of identifying \mathcal{D}_Q is independent of the size of \mathcal{D} . It has been shown that with an auxiliary structure known as access schema, many queries in relational algebra (RA) are boundedly evaluable under the set semantics of RA. This paper extends the theory of bounded evaluation to RA_{aggr} , i.e., RA extended with aggregation, under the bag semantics. (1) We extend access schema to bag access schema, to help us identify \mathcal{D}_Q for RA_{aggr} queries Q. (2) While it is undecidable to determine whether an RA_{aggr} query is boundedly evaluable under a bag access schema, we identify special cases that are decidable and practical. (3) In addition, we develop an effective syntax for bounded RA_{aggr} queries, i.e., a core subclass of boundedly evaluable RA_{aggr} queries without sacrificing their expressive power. (4) Based on the effective syntax, we provide efficient algorithms to check the bounded evaluability of RA_{aggr} queries. (5) As proof of concept, we extend PostgreSQL to support bounded evaluation. We experimentally verify that the extended system improves performance by orders of magnitude.

Keywords: Bounded evaluation, resource-bounded query processing, effective syntax, access schema, boundedness.

1 Introduction

Querying big data can be prohibitively costly. As an indicator, it is NP-hard¹ to decide whether a tuple is in the answer $Q(\mathcal{D})$ in a dataset \mathcal{D} to an SPC (select, project, Cartesian product) query Q, and it is PSPACEhard¹ when Q is a query in relational algebra (denoted by RA)^[2]. It takes days to join two tables with 10 million tuples each^[3]. One might be tempted to think that parallel computation could do the job. However, there exist computational problems for which parallel scalability is beyond reach, i.e., no matter how many machines are used, the parallel runtime of algorithms for such problems may not be reduced^[4]. Worse still, small businesses typically have constrained resources and may not afford large-scale parallel computation.

Is querying big data beyond the reach of small companies, or is it just a privilege of big companies? Is it possible to extend DBMS with an immediate capacity to answer common queries over big datasets under constrained resources? One approach to tackling the challenge has recently been studied, based on bounded evaluation^[5, 6]. To answer a query Q on a dataset \mathcal{D} , the idea is to look at only a "bounded" fraction \mathcal{D}_Q of \mathcal{D} that suffices to compute $Q(\mathcal{D})$, instead of at the entire \mathcal{D} . This is doable by using an access schema \mathcal{A} , which is a combination of cardinality constraints and associated indices. Under \mathcal{A} , Q is boundedly evaluable if for all datasets \mathcal{D} that conform to \mathcal{A} , one can identify $\mathcal{D}_Q \subseteq \mathcal{D}$ by reasoning about the cardinality constraints, and fetch \mathcal{D}_Q by using the indices of \mathcal{A} , such that (a) $Q(\mathcal{D}_Q) = Q(\mathcal{D})$ and (b) \mathcal{D}_Q is determined by \mathcal{A} and Q only. In other words, if Q is boundedly evaluable under \mathcal{A} , query Q can then be exactly answered via bounded evaluation, by accessing only D_Q of size bounded by the cardinalities in \mathcal{A} .

The theory has been tested in industry and is found to "improve the performance by orders of magnitude"^[7].

Example 1. Consider query Q_1 from Facebook Graph Search^[8]: Find all my friends who have check-ins in UK². The query is posed on dataset \mathcal{D}_1 with two relations: (a) friend (uid, fid), stating that person fid is a friend of uid, and (b) checkin (uid, loc, cty, date), stating that person uid checked in at location loc in country cty on date. Written as an RA query, Q_1 is as follows (u_0 denotes "me"):

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¹See [1] for more about complexity classes, e.g., NP and PSPACE.

²Facebook users can check-in to locations via "check-ins".

 $Q_1(x) =$ friend $(u_0, x) \bowtie$ checkin(x, loc, ``UK'', date).

Here dataset \mathcal{D}_1 is big, with trillions of friend links and check-ins^[9]. It is costly to compute $Q_1(\mathcal{D}_1)$ directly.

Now consider a set \mathcal{A}_1 of real-life cardinality constraints:

 $\circ \phi_1$: friend(pid \rightarrow fid, 5 000);

 $\circ \phi_2$: checkin(uid \rightarrow country, 193).

Here constraint ϕ_1 specifies a Facebook policy^[10]: a limit of 5000 friends per user; and ϕ_2 states that each user can check-in at most 193 countries. Indices can be built on \mathcal{D}_1 based on ϕ_1 such that given a person, it returns the ids of all her friends by accessing at most 5000 friend tuples; similarly for ϕ_2 . Taken together, these constraints and their associated indices are called access constraints^[5].

Using \mathcal{A}_1 , we can compute $Q_1(\mathcal{D}_1)$ by accessing at most 970000 tuples from \mathcal{D}_1 , instead of trillions. (1) We fetch T_1 of at most 5000 fid's of friend tuples with uid = u_0 , by using ϕ_1 . (2) For each fid f in T_1 , we fetch T_2 of at most 193 country values with ϕ_2 . (3) We return the set of fid's in T_1 with country = UK in T_2 . The plan fetches at most 5000 + 193 × 5000 tuples to compute $Q_1(\mathcal{D}_1)$, no matter how big \mathcal{D}_1 is. Hence, Q_1 is boundedly evaluable under \mathcal{A}_1 .

As shown in Example 1, bounded evaluation answers a query Q over a big dataset by accessing a set \mathcal{D}_Q of data values with bounded size. It does this by retrieving values (i.e., partial tuples) using indices associated with cardinality constraints that correlate attributes. One might think that this can also be carried out by conventional index-only plans for query optimization^[11]. However, the two are different problems as indicated by their complexity bounds: deciding whether an SPC query can be answered with a "bounded" query plan is EX-PSPACE-hard^[5], while it is in PTIME to decide whether it has an index-only plan^[11].

While bounded evaluation is promising, more work has to be done, from theory to systems. Bounded evaluation has only been studied for RA queries under the set semantics^[5, 6]. In the real world, queries are often expressed in RA_{aggr}, i.e., RA extended with aggregation under the bag semantics. RA_{aggr} can express all SQL (structured query language) queries that do not carry arithmetic expressions. This makes bounded evaluation more intriguing.

Example 2. Recall query Q_1 and access schema \mathcal{A}_1 from Example 1. Consider query Q_2 to find the number of UK check-ins from each of my friends. Written in RA_{aggr}, Q_2 is:

 $Q_2 = \text{gpBy}(Q_3, \text{ uid}, \text{ count(cty)}), \text{ where }$

 $Q_3 = \pi_{\text{uid,cty}}(\text{friend}(u_0, x) \Join \text{checkin}(x, \text{loc}, "UK", \text{date}).$

Here $gpBy(Q_3, uid, count(cty))$ groups the results of Q_3 by attribute uid and calculates count(cty) for each group (see Section 2.1 for more details about gpBy operator). In contrast to Q_1 , \mathcal{A}_1 does not help us answer Q_2 .

Using φ_2 , we can fetch a set of distinct countries for each friend x. However, x may have multiple UK check-ins. Access schema no longer suffices for RA_{aggr} under the bag semantics.

For practical use to emerge from the study, it is necessary to extend bounded evaluation from RA to RA_{aggr} (SQL). This gives rise to several questions. How should we extend the access schema of [5, 6] to support the bag semantics? We will see that the problem for checking whether an SQL query is boundedly evaluable is undecidable. Given the negative result, is bounded evaluation beyond reach in practice? More specifically, is there any practical and decidable special case? Is it possible to develop a systematic method that allows us to efficiently check the bounded evaluability of SQL queries? In addition, after determining that an SQL query is boundedly evaluable, how can we generate and optimize a query plan to carry out its bounded evaluation?

Contributions. This paper answers these questions by extending the study to RA_{aggr} , from theory to practice.

(1) Bounded evaluation for SQL. We extend bounded evaluation from RA to RA_{aggr} , i.e., SQL (without arithmetic) to support arbitrarily nested aggregate sub-queries and group-by clauses. We introduce bag access schemas, an extension of the access schema of [5, 6] to support the bag semantics. We also formulate bounded query plans for RA_{aggr} .

(2) Complexity of bounded evaluation. Not surprisingly, bounded evaluability is undecidable for SQL since it is already undecidable for RA^[5]. We identify practical conditions that cover a number of real-life queries, for which the bounded evaluability can be efficiently determined. These conditions tell us what makes queries bounded.

(3) Effective syntax. To accommodate the undecidability, we develop an effective syntax $\mathcal{L}_{\mathcal{B}}$ for boundedly evaluable RA_{aggr} queries. We show that under a bag access schema \mathcal{B} , (a) an RA_{aggr} query Q is boundedly evaluable if and only if it is equivalent to a query $Q' \in \mathcal{L}_{\mathcal{B}}$; and (b) it is in PTIME (polynomial time) to check whether Qis in $\mathcal{L}_{\mathcal{B}}$. That is, $\mathcal{L}_{\mathcal{B}}$ is a core subclass of bounded evaluable RA_{aggr} queries that are syntactically checkable without sacrificing the expressive power. This is along the same lines as how commercial database systems (DBMS) deal with safe relational calculus queries, which are undecidable to decide^[12-14].

(4) Extending DBMS with bounded evaluation. We present a framework, referred to as BEAS (bounded evaluable SQL) to provide commercial DBMS with the capability of bounded evaluation of RA_{aggr} queries. Given an RA_{aggr} query Q and a bag access schema \mathcal{B} , BEAS first checks whether Q is boundedly evaluable under \mathcal{B} . If so, it generates a query plan for Q to compute $Q(\mathcal{D})$ by accessing a bounded small fraction \mathcal{D}_Q of \mathcal{D} using \mathcal{B} . Otherwise, it leverages access schema and generates a partially bounded plan, to bound sub-queries of Q. We develop algorithms underlying BEAS.

(5) Experimental study. As proof of concept, we extend PostgreSQL with bounded evaluation, denoted by BEAS@PG. Using TPCH benchmark^[15] and real-life datasets, we evaluate the performance of BEAS@PG compared to PostgreSQL. We find that BEAS@PG improves PostgreSQL by up to 4 orders of magnitude for boundedly evaluable queries.

Querying big data under bounded resources. This work is a component of a framework for querying big data. As outlined in [16], the framework works as follows: given an SQL query Q posed on a big dataset \mathcal{D} ,

(1) it first checks whether Q is boundedly evaluable;

(2) if so, it computes the exact answer $Q(\mathcal{D})$ by accessing a bounded fraction D_Q of \mathcal{D} via bounded evaluation;

(3) otherwise, it computes approximate answers to Q in \mathcal{D} also by accessing a bounded amount of data, and provides deterministic accuracy ratios^[17].

In the entire process, it only accesses a bounded fraction of data and can be conducted under bounded resources. Hence it is feasible to provide small businesses with a capacity of querying big data despite constrained resources.

To simplify the discussion, we focus on row-oriented DBMS (a.k.a. row stores) in this paper. Nonetheless, as will be seen in Section 2, the model of bounded evaluation subsumes column stores. Moreover, bounded evaluation can be readily extended to parallel and distributed systems^[18].

Organization. The remainder of the paper is organized as follows. Section 2 defines bag access constraints and formulates boundedly evaluable RA_{aggr} queries. Section 3 studies the complexity of bounded evaluation for RA_{aggr} queries. Section 4 proposes effective syntax $\mathcal{L}_{\mathcal{B}}$ for boundedly evaluable RA_{aggr} queries. Section 5 introduces BEAS and develops its underlying algorithms. The experimental study is presented in Section 6. We discuss related work in Section 7, and identifies topics for future work in Section 8.

2 Bounded evaluation of SQL queries

We first define bag access schema (Section 2.1) and then formulate bounded evaluation of RA_{aggr} queries, aggregate or not, under the bag semantics (Section 2.2).

2.1 RA_{aggr} and bag access schema

We start with a review of RA_{aggr} , an extension of RA with a group-by construct and nested aggregate sub-queries.

RA_{aggr} queries. An RA_{aggr} query is an expression defined in terms of RA operators (i.e., select σ_C , project π_Y , Cartesian-product \times or join \bowtie_C , renaming $\rho_{A\to B}$, union \cup and set difference -), and additionally a group-by

aggregate operator

$$\operatorname{gpBy}(Q, X, \operatorname{agg}_1(V_1), \cdots, \operatorname{agg}_m(V_m))$$

where (a) Q is an $\operatorname{RA}_{\operatorname{aggr}}$ query, (b) X is a set of attributes for group-by, (c) agg_i is one of aggregate functions max, min, count, sum, avg, and (d) V_1, \dots, V_m are attributes such that $X \cup \bigcup_{i=1}^m \{\operatorname{agg}_i(V_i)\}$ forms the output relation of Q. We refer to $\operatorname{agg}_i(V_i)$ as an aggregate field on attribute V_i . We write the operator as $\operatorname{gpBy}(Q, X, \operatorname{agg}(V))$ when it is clear from the context. Since Q may include aggregate operators itself, aggregations in an $\operatorname{RA}_{\operatorname{aggr}}$ query may be arbitrarily nested.

In SQL syntax, the operator can be written as

select X, $\operatorname{agg}_1(V_1), \cdots, \operatorname{agg}_m(V_m)$

from ${\cal Q}$

group by X

As a special case, when $X = \emptyset$, $\operatorname{gpBy}(Q, X, \overline{\operatorname{agg}(V)})$ does not have a group-by construct. We write it simply as $\operatorname{agg}(Q)$.

Example 3. Query Q_2 in Example 2 is an RA_{aggr} query.

As another example, an RA_{aggr} query with nested aggregation is Q_4 over relations R(A, B, C) and S(E, F, W):

 $Q_4 = \operatorname{avg}(\pi_z(Q_5(y) \bowtie S(y, 1, z))),$ where

$$Q_5(y) = \operatorname{sum}(\pi_y(R(w, 1, u) \bowtie R(w, x, y))). \square$$

Bag access schema. To support the bag semantics, we extend the access schema of [5, 19] to bag access schema. Over a database schema \mathcal{R} , a bag access schema \mathcal{B} is a set of bag access constraints of the form:

$$\varphi = R\left(X \to Y, N\right)$$

where R is a relation schema in \mathcal{R} , X and Y are sets of attributes of R, and N is a positive integer.

To define the semantics of bag access constraints, we use the following notations. (1) Denote by \mathcal{D} a database of \mathcal{R} , and by D an instance of relation schema R in \mathcal{R} . (2) For an instance D of R, $D_Y(X = \bar{a}) = \{t[Y] \mid t \in D, t[X] = \bar{a}\}$, i.e., $D_Y(X = \bar{a})$ denotes the set of Y values corresponding to X-value \bar{a} . (3) For any XY-value $\bar{a}\bar{b}$ in $D, m(D, \bar{a}\bar{b})$ denotes the cardinality of the bag (multiset) $\{|t \in D \mid t[XY] = \bar{a}\bar{b}|\}$, i.e., the number of occurrences of $\bar{a}\bar{b}$ as XY attributes in D; we refer to $m(D, \bar{a}\bar{b})$ as the multiplicity of $\bar{a}\bar{b}$ in D.

We say that D conforms to ψ , denoted by $D \models \varphi$, if

(1) for any X-value \bar{a} in D, $|D_Y(X = \bar{a})| \leq N$, i.e., there exist at most N distinct associated Y-values in D; and

(2) there exists an index for φ on D such that given any X-value \bar{a} , by accessing at most N tuples, it retrieves (a) all associated distinct Y-values \bar{b} in D, and (b) for each such \bar{b} , the multiplicity $m(D, \bar{ab})$.

Intuitively, $D \models \varphi$ if for any X-value, there exist at

most N distinct corresponding Y values in D. Moreover, these Y-values (partial tuples) and their multiplicities in D are indexed by ψ and can be efficiently retrieved via the index.

Example 4. Extending \mathcal{A}_1 of Example 1, a bag access schema \mathcal{B}_1 consists of the following bag access constraints:

 $\circ \varphi_1 = \text{friend}([\text{pid} \rightarrow \text{fid}, 5000]);$

 $\circ \varphi_2 = \text{checkin}(|\text{uid} \rightarrow \text{country}, 193|).$

Here φ_2 says that (a) for any uid u_1 , there exist at most 193 distinct country values, and (b) there exists an index built on the friend relation that given any uid u_1 , fetches all associated distinct countrys c and for each country c, the multiplicity of (u_1, c) in the friend relation for country c; similarly for φ_2 .

As another example, consider a bag access schema \mathcal{B}_2 for Q_4 of Example 3, which consists of bag access constraints:

- $\circ \varphi_3 = R(A \to B, 1),$
- $\circ \varphi_4 = R(B \to C, 10)$, and

 $\circ \varphi_5 = S(\![EF \to W, 10]\!).$

We will see that Q_4 can be efficiently answered with \mathcal{B}_2 .

A database instance \mathcal{D} of \mathcal{R} conforms to a bag access schema \mathcal{B} , denoted by $\mathcal{D} \models \mathcal{B}$, if $D \models \varphi$ for every $\varphi \in \mathcal{B}$, where $\varphi = R(X \to Y, N)$, and D is the instance of R in \mathcal{D} .

Intuitively, a bag access constraint φ extends an access constraint ψ of [5, 19] by incorporating multiplicity. Similar to ψ , given any X-value \bar{a} in D, φ enforces the cardinality constraint $|D_Y(X = \bar{a})| \leq N$ and returns distinct corresponding Y-values. In contrast to ψ , for each corresponding Y-value \bar{b} , φ also returns the multiplicity of \overline{ab} in D. In other words, access constraints under the set semantics^[5, 6] are a special case of bag access constraints when we only bound the cardinality and retrieve distinct values.

Remark 1. When it is clear from the context, we also simply refer to bag access schema as access schema.

2.2 Bounded evaluation of RA_{aggr} queries

We next define bounded evaluation for RA_{aggr} queries.

Multiplicity relations. From an instance D of a relation schema R, we can use the index of a bag access constraint $R(|X \to Y, N|)$ to retrieve a relation consisting of tuples (t[X, Y], m(t[X, Y])), where t is a tuple in D. It is a set that besides partial tuples t[X, Y] in D, carries multiplicity m(D, t[X, Y]), and is referred to as a multiplicity relation.

The RA_{aggr} operators can be readily extended to multiplicity relations. Take join operator \bowtie_C as an example. Given two multiplicity relations I_1 and I_2 , the result of $I_1 \bowtie_C I_2$, denoted by I_s , is a multiplicity relation as follows: (a) tuples in I_s have the form (t, M), where t is a result tuple of $I_1 \bowtie_C I_2$ using the conventional join semantics (ignoring multiplicity), and (b) $M = m(I_1, t_1) \times$ $m(I_2, t_2)$, where t is joined from $t_1 \in I_1$ and $t_2 \in I_2$, and $m(I_i, t_i)$ denotes the multiplicity of tuple t_i in multiplicity relation $I_i(i \in \{1, 2\})$. Similarly, other RA_{aggr} operators are defined on multiplicity relations.

Bounded RA_{aggr} plans. A bounded RA_{aggr} plan ξ under a bag access schema \mathcal{B} is an algebra tree that extends conventional RA_{aggr} query plans with a new operator fetch (T,φ) , where $\varphi = R(X \to Y, N)$ is a bag access constraint in \mathcal{B} , and T is an intermediate multiplicity relation on attributes R[X] (see Appendix for a formal definition). Over an instance D of R that conforms to φ , fetch (T,φ) retrieves an intermediate relation $S = \bigcup_{\bar{a} \in T} D_{XY}(X = \bar{a})$ by using the index of φ on D, where each tuple t in S is annotated with multiplicity m(D, t) (also retrieved by φ).

Intuitively, a bounded RA_{aggr} plan starts with a set of constants (possibly \emptyset), retrieves data from \mathcal{D} via the fetch operator, and applies RA_{aggr} operators to the fetched data, except that it accesses data by employing the indices of the bag constraints in \mathcal{B} only, and allows group-by aggregate and operates on multiplicity relations.

We denote by $\xi(\mathcal{D})$ the result of applying plan ξ to \mathcal{D} .

Example 5. Recall $\operatorname{RA}_{\operatorname{aggr}}$ query Q_2 from Example 2 and bag access schema \mathcal{B}_1 from Example 4. A bounded plan ξ_{Q_2} for Q_2 under \mathcal{B}_1 , written in algebra expressions, is as follows:

- T_1 (uid,fid) = fetch($\{u_0\}, \varphi_1$),
- T_2 (uid,cty) = fetch($\pi_{\rm fid}T_1, \varphi_2$),
- T_3 (uid, cty) = $\sigma_{\rm ctv} T_2$,
- $T_4 = \text{gpBy}(T_3, \text{uid}, \text{count(cty)}).$

As a more intriguing example, recall query Q_4 from Example 3 and bag access schema \mathcal{B}_2 from Example 4. By the cardinality constraint in φ_3 , for each A-value in any database instance $\mathcal{D} \models \mathcal{B}_2$ for w of Q_4 , there exists at most 1 distinct B-value associated with w. Therefore, $Q_4 \equiv_{\mathcal{B}_2} Q_6$, i.e., Q_4 is equivalent to Q_6 on every database $\mathcal{D} \models \mathcal{B}_2$, where Q_6 is

 $Q_6 = \operatorname{avg}(\pi_z(Q_7(y) \bowtie S(y, 1, z))),$ where

 $Q_7(y)\operatorname{sum}(\pi_y R(w, 1, y)).$

Under \mathcal{B}_2 , Q_6 (hence Q_4) has a bounded query plan ξ_{Q_4} :

 $T_1(B, C) = \text{fetch}(\{1\}, \varphi_4),$ $T_2 = \text{sum}(\pi_C T_1),$ $T_3(E, F, W) = \text{fetch}(T_2 \times \{1\}, \varphi_5),$ $T_4 = \text{avg}(\pi_W T_3).$

Observe that ξ_{Q_4} does not explicitly use φ_3 . However, the correctness of ξ_{Q_4} relies on the cardinality of φ_3 . Moreover, ξ_{Q_4} propagates constants of Q_4 via join and fetch, such that all values and their combinations that are needed for answering Q_4 are fetched from $\mathcal{D} \models \mathcal{B}_2$. In particular, in the presence of nested aggregation, answers to aggregate sub-queries can also be used by fetch, e.g., T_3 .

Boundedly evaluable queries. Under access schema \mathcal{B} , an $\operatorname{RA}_{\operatorname{aggr}} Q$ is boundedly evaluable if it has a

plan ξ such that:

 $\circ \xi$ is a bounded RA_{aggr} plan under \mathcal{B} ;

 \circ constants $\{c\}$ in ξ are from selection conditions of Q;

 \circ moreover, for any database $\mathcal{D} \models \mathcal{B}, \xi(\mathcal{D}) = Q(\mathcal{D}).$

We write $Q \equiv_{\mathcal{B}} \xi$ if Q has such a bounded query plan

ξ.

Here for any multiplicity relation D_1 and a conventional bag (multiset) D_2 , we write $D_1 = D_2$ if D_2 can be obtained from D_1 by including m copies of each tuple $(t,m) \in D_1$.

For example, query Q_2 of Example 2 is boundedly evaluable under \mathcal{B}_1 of Example 4, since it has a bounded plan ξ_{Q_2} given in Example 5. Similarly, Q_4 of Example 3 is also boundedly evaluable under \mathcal{B}_2 of Example 4.

Observe the following about bounded RA_{aggr} plans ξ .

(1) Scale independence. Each fetch operation in ξ retrieves data with a cost that can be quantified by the bag constraint employed. Hence the cost of executing ξ is determined by bag access schema \mathcal{B} and query plan ξ only, not by the size of dataset \mathcal{D} as long as \mathcal{D} conforms to \mathcal{B} . That is, under the bag semantics, bounded RA_{aggr} plans preserve the scale independence of bounded evaluation for RA queries^[5, 6].

(2) Late bag semantics enforcement. Plan ξ fetches and operates on sets since fetch (T, ψ) returns a set. It defers the process of the bag semantics to a stage as late as possible. This reduces performance degradation caused by duplicated values in, e.g., joins, in which duplicates get inflated rapidly.

(3) Subsuming column-stores. Bounded plan ξ can also express query evaluation over column-stores^[20] or columnstore indices^[21]. Indeed, in a column store (or a columnstore index), each column (or column index) on attribute A of a relation schema R is essentially a special case of bag access constraint of the form $R(\emptyset \to A, N)$. Hence, column store and columnstore index are a special case of bag access schema and hence their evaluation plan can be expressed by a bounded plan ξ under such a bag access schema.

Note that the efficiency of column stores mainly comes from its implementation-level optimization, e.g., column compression and vectorization^[20]. While these optimization strategies can also be used to implement the indices of bag access schema, these are not the focus of this paper. We study query evaluation at the logical level, under generic constraints $R([X \to Y, N])$ when X is not necessarily empty. Hence, this paper focuses on row-oriented databases as the underlying platform for implementing bag access schema.

3 Complexity of bounded evaluation

In this section, we study the complexity of bounded evaluability and identify practical decidable cases.

Bounded evaluability. The problem is stated as follows.

 $_{\circ}$ Input: A database schema \mathcal{R} , a bag access schema \mathcal{B} over \mathcal{R} , and an RA_{aggr} query Q over \mathcal{R} .

 $_{\circ}$ Question: Is Q boundedly evaluable under \mathcal{B} ?

This bounded evaluability problem is to decide whether a query can be answered by accessing a bounded amount of data, and is underlying the first step of our framework for querying big data under bounded resources (Section 1).

No matter how important, the problem is hard. To see why it is intriguing, let us consider Example 6.

Example 6. Consider bag access schema \mathcal{B}_3 and SPC query Q_8 defined on relations T(A, B) and U(E, F):

 $\circ \mathcal{B}_3$ consists of the following two access constraints: $\varphi_6 = T(|A \to B, N|),$

 $\varphi_7 = U(|E \to F, 2|);$

 \circ query $Q_8 = Q_9 - Q_{10}$, where

 $Q_9 = \pi_y(T(x, y) \bowtie U(w, 1) \bowtie U(w, x) \bowtie U(w, y)), \text{ and}$ $Q_{10} = \pi_z(T(z, z) \bowtie U(u, 1) \bowtie U(u, z)).$

At a first glance, none of Q_9 and Q_{10} seems boundedly evaluable, and hence neither is Q_8 . Indeed, we cannot retrieve values for any of x, y or z using indices in \mathcal{B}_3 . However, putting together $U(w,1) \bowtie U(w,x) \bowtie U(w,y)$ and φ_7 of \mathcal{B}_3 , one can deduce that x must be equal to either 1 or y in all tuples retrieved from instance of T by any query plan for Q_9 . In other words, under \mathcal{B}_3 , Q_9 reduces to SPCU $Q_9^1 \cup Q_9^2$, where $Q_9^1 = \pi_y(T(1,y) \bowtie$ and $Q_9^2 = \pi_y(T(y, y) \bowtie U(w, 1) \bowtie$ $U(w,1) \bowtie U(w,y)$ U(w, y).Hence, $Q_8 = (Q_9^1 \cup Q_9^2) - Q_{10} = Q_9^1$ since $Q_9^2 \equiv Q_{10}$. It is easy to see that Q_9^1 is boundedly evaluable under \mathcal{B}_3 and as a result, so is Q_8 .

As shown above, it is often necessary to check query equivalence to decide whether a query is bounded. The use of union (\cup) allows us to convert SPC to SPCU under a bag access schema (e.g., Q_4 to $Q_4^1 \cup Q_4^2$), which may further interact with set difference (-) (e.g., Q_3 and Q_4^1).

It is beyond reach in practice to check the equivalence of RA or RA_{aggr} queries. Thus, the bounded evaluability problem is already undecidable for RA, a special case of RA_{aggr} .

Theorem 1.^[5] The bounded evaluability problem is undecidable for RA queries.

Theorem 1 was verified under access schema. As remarked in Section 2, access schema is a special case of bag access schema. Hence, the bounded evaluability problem remains undecidable for RA under a bag access schema. As an immediate corollary, the bounded evaluability problem is undecidable for RA_{aggr} , which subsumes RA.

Decidable cases. We next identify special cases when the bounded evaluability is decidable. The reason is twofold. (1) The special cases cover a large number of RA_{aggr} queries used in practice, e.g., all SPC sub-queries of built-in benchmark queries in TPCH^[15] and TPCDS^[22]. (2) These cases reveal insight about why queries become boundedly evaluable. In Section 4, we will deal with generic RA_{aggr} queries, by devising an effective syntax for boundedly evaluable RA_{aggr} queries.sub> queries.

(I) PTIME cases. The first special case, denoted by $C^{\rm P}$, consists of combinations of SPC queries and bag access schema for which the bounded evaluability can be checked in PTIME, covering all SPC sub-queries of TPCH and TPCDS.

<u>Class \mathcal{C}^{P} </u>. For any bag access schema \mathcal{B} and SPC query Q over the same database schema \mathcal{R} , $(\mathcal{B}, Q) \in \mathcal{C}^{\mathrm{P}}$ if

(a) for each bag constraint $\varphi = R(X \to Y, N),$ N > ||Q||, where ||Q|| is the number of relation atoms in Q; and

(b) Q has no self-join.

Theorem 2. For any bag access schema \mathcal{B} and SPC Q,

(1) it is in PTIME to decide whether (\mathcal{B}, Q) is in $\mathcal{C}^{\mathbf{P}}$; and

(2) it is in PTIME to decide whether Q is boundedly evaluable under \mathcal{B} if (\mathcal{B}, Q) is in $\mathcal{C}^{\mathbf{P}}$.

Proof. Statement (1) apparently holds. Below we prove (2) by giving a PTIME sufficient and necessary condition for checking the bounded evaluability of Q under \mathcal{B} .

The condition needs a notion of covered SPC queries from [6]. It is characterized by a set $cov(Q, \mathcal{B})$, which consists of attributes whose values can be retrieved via fetch operations along with \mathcal{B} , without directly accessing raw data in a database. More specifically, let X_C^Q be the set of attributes A in the constant selection predicates of Q, i.e., $\sigma_{A=c}$ for a constant c. Then $cov(Q, \mathcal{B})$ is inductively defined as:

(a) $X_C^Q \subseteq \operatorname{cov}(Q, \mathcal{B});$

(b) if $A \in \operatorname{cov}(Q, \mathcal{B})$ and $\Sigma_Q \vdash A = B$ (denoting that A = B can be deduced from selection predicates Σ_Q via the transitivity of equality), then $B \in \operatorname{cov}(Q, \mathcal{B})$;

(c) if $X \subseteq cov(Q, \mathcal{B})$ and $R(X \to Y, N) \in \mathcal{B}$, then $Y \subseteq cov(Q, \mathcal{B})$; and

(d) $\operatorname{cov}(Q, \mathcal{B})$ contains nothing else.

Denote by X_R^Q the set of attributes that are either in the selection or join predicates of Q, or are the top-level projection attributes. Then we show the following.

Lemma 3. For any $(\mathcal{B}, Q) \in \mathcal{C}^{\mathbb{P}}$, Q is boundedly evaluable under \mathcal{B} if and only if for each relation R in Q, there is $\varphi = R(X \to Y, N) \in \mathcal{B}$ such that $X_R^Q \subseteq XY \subseteq \operatorname{cov}(Q, \mathcal{B})$.

From Lemma 3, Theorem 2(2) follows since one can simply check the condition of Lemma 3 in PTIME in the sizes of Q and \mathcal{B} . Below we prove Lemma 3.

 (\Rightarrow) Assume that Q is boundedly evaluable under \mathcal{B} . Then there exists a bounded plan ξ for Q under \mathcal{B} . Below we first inductively construct a query Q_{ξ} from ξ such that (a) $\xi \equiv Q_{\xi} \equiv_{\mathcal{B}} Q$, where $Q \equiv_{\mathcal{B}} Q'$ means that $Q(\mathcal{D}) = Q'(\mathcal{D})$ for any database $\mathcal{D} \models \mathcal{B}$, and (b) Q_{ξ} satisfies the condition on Q in Lemma 3. We then show that Q also satisfies the condition when Q_{ξ} satisfies it, and thus Lemma 3 holds. Construction of Q_{ξ} . We construct query Q_{ξ} by induction on the structure of ξ as follows:

• If $\xi = \{c\}$, then $Q_{\xi} = \{c\}$.

 $\circ \quad \text{If } \xi = \sigma_C(\xi') \quad (\text{resp. } \pi_Y(\xi')), \text{ then } Q_{\xi} = \sigma_C(Q_{\xi'}) \\ (\text{resp. } \pi_Y(Q_{\xi'})), \text{ where } Q_{\xi'} \text{ is the query constructed for } \xi'.$

◦ If $\xi = \text{fetch}(\xi', R(X \to Y, N))$, then $Q_{\xi} = \pi_Z(Q_{\xi'} \bowtie_X R(X, Y, Z))$.

• If $\xi = \xi_1 \times \xi_2$, then $Q_{\xi} = Q_{\xi_1} \times Q_{\xi_2}$.

By induction on the structure of ξ , one can readily verify that for each relation R in Q_{ξ} , there exists a bag constraint $\varphi = R(X \to Y, N) \in \mathcal{B}$ such that $X_R^{Q_{\xi}} \subseteq$ $XY \subseteq \operatorname{cov}(Q_{\xi}, \mathcal{B})$, i.e., Q_{ξ} satisfies the condition of Lemma 3.

Query Q satisfies the condition. We next show that Qsatisfies the condition in Lemma 3 when Q_{ξ} does. Since for each bag constraint $\varphi = R(X \to Y, N) \in \mathcal{B}, N > ||Q||,$ from $Q_{\xi} \equiv_{\mathcal{B}} Q$, one can verify that $Q_{\xi} \equiv Q$. Thus there exists a homomorphism ρ from Q_{ξ} to $Q^{[2]}$. Moreover, since Q is self-join free, each relation schema R (i.e., relation atom) has at most one occurrence in Q. Then no relation atom in Q can be removed without changing Q. Thus, Q is minimal (an SPC query is minimal if it has no redundant relation $atoms^{[2]}$). Hence for each relation R in Q, there must exist a relation R' in Q_{ξ} such that $\rho(R') =$ $X_R^Q \subseteq \rho(X_{R'}^{Q_\xi}).$ R,and moreover, Hence $X_{R}^{Q} \subseteq \rho(X_{R'}^{Q_{\xi}}) \subseteq XY \subseteq \rho(\operatorname{cov}(Q_{\xi}, \mathcal{B})) \subseteq \operatorname{cov}(Q, \mathcal{B}).$ That is, Q also satisfies the condition of Lemma 3.

(\Leftarrow) Assume that Q satisfies the condition of Lemma 3. We construct a 3-step bounded query plan ξ under \mathcal{B} for Q:

(a) it has a bounded sub-plan ξ_R for each relation R in Q that fetches all attribute values needed for answering Q;

(b) it combines the attribute values for each relation R in Q via a bounded sub-plan ξ_R^c such that each (partial) tuple fetched and kept for R is guaranteed to draw values from the same tuple in D; and

(c) it finally carries out operations in Q over ξ_R^c for each relation R in Q.

To show such a plan ξ exists for Q under the condition of Lemma 3, we only need to prove the following two properties:

(1) all necessary attribute values for answering Q from each relation R in Q can be retrieved by ξ_R in step (a), and

(2) their combinations can be restored by ξ_R^c in step (b).

Proof of (1). We prove (1) by constructing such a bounded plan $\xi_{R[A]}$ for each attribute $A \in X_R^Q$. Note that only attributes in X_R^Q are needed for answering Q. The plan $\xi_{R[A]}$ is constructed by translating the proof that witnesses $A \in \operatorname{cov}(Q, \mathcal{B})$. More specifically, since the condition of Lemma 3 holds for Q and \mathcal{B} , for any attribute Aof X_R^Q such that $A \in \operatorname{cov}(Q, \mathcal{B})$, there must exist a sequence of applications of rules (a)–(c) that defines $\operatorname{cov}(Q, \mathcal{B})$ such that

$\ell: \operatorname{cov}_0 \xrightarrow{r_1} \operatorname{cov}_1 \xrightarrow{r_2} \cdots \xrightarrow{r_n} \operatorname{cov}_n$

where $\operatorname{cov}_0 = \emptyset$, $A \in \operatorname{cov}_n$, step *i* expands cov_{i-1} by applying rule r_i from one of the rules (a)–(c) for defining $\operatorname{cov}(Q, \mathcal{B})$ given earlier. We translate ℓ into a bounded plan:

$$\xi:\xi_0,\cdots,\xi_n$$

where ξ_0 is empty; ξ_i is derived from ξ_0, \dots, ξ_{i-1} based on step $\operatorname{cov}_{i-1} \stackrel{r_i}{\longmapsto} \operatorname{cov}_i$ as follows:

(i) if r_i is rule (a) for a constant c in X_C^Q , then ξ_i is $\{c\}$;

(ii) if r_i is rule (b) with A = B such that $A \in \operatorname{cov}_{i-1}$, $B \notin \operatorname{cov}_{i-1}$ and $B \in \operatorname{cov}_i$, then $\xi_i = \xi_{i-1}$;

(iii) if r_i is rule (c), then $\xi_i = \text{fetch}(\xi_{j_1} \bowtie \cdots \xi_{j_{|X|}}, \varphi = R(X \rightarrow Y, N))$, where $\xi_{j_1}, \cdots, \xi_{j_{|X|}}$ are the bounded plans that fetch attributes in X $(j_1, \cdots, j_{|X|} < i)$.

By the construction, ξ_i is a bounded plan that fetches all A attribute values for Q. Note that each sub-plan ξ_i is bounded since it does not involve relation scans.

Proof of (2). Plan ξ_R^c is constructed with ξ_A for each $A \in X_R^Q$ by (i) $T_1 = \xi_{A_1} \bowtie \cdots \bowtie \xi_{A_{|X|}}$, where A_i 's $(i \in [1, |X|])$ range over all attributes in X, and X_{A_i} is the plan generated above for fetching A_i values; and (ii) if $X_R^Q \subseteq XY$ for $\varphi = R(|X \to Y, N|) \in \mathcal{B}$, then $\xi_R^c = \text{fetch}(T_1, \varphi)$. Since ξ_A is a bounded plan for each $A \in X_R^Q$, ξ_R^c is bounded under \mathcal{B} .

Hence, when the condition of Lemma 3 holds for Q and \mathcal{B} , ξ constructed above is a bounded plan for Q under \mathcal{B} .

(II) NP cases. One might want to lift the restriction of condition (b) on the queries in C^{P} . This covers all SPC queries, including those with self-joins. However, the bounded evaluability analysis becomes harder unless P = NP.

<u>Class</u> \mathcal{C}^{NP} . Denote by \mathcal{C}^{NP} the set of pairs of bag access schemas \mathcal{B} and SPC queries Q such that for each bag constraint $\varphi = R(X \to Y, N), N > ||Q||$. We have the following.

Theorem 4. For any bag access schema \mathcal{B} and SPC Q,

(a) it is in PTIME to decide whether (\mathcal{B}, Q) is in \mathcal{C}^{NP} ; and

(b) it is NP-complete to decide whether Q is boundedly evaluable under \mathcal{B} if (\mathcal{B}, Q) is in \mathcal{C}^{NP} .

Proof. Statement (a) is immediate. To prove statement (b), we first give a sufficient and necessary condition for query Q to be boundedly evaluable under \mathcal{B} for any $(\mathcal{B}, Q) \in \mathcal{C}^{\text{NP}}$. Based on the characterization, we then show that checking bounded evaluability for \mathcal{C}^{NP} is NP-complete.

Let Q_m be the minimal equivalent query of Q, i.e., the minimized version of Q, which can be obtained by removing all redundant relations (see [2] for details). For an SPC query Q, there exists a unique minimal equivalent query up to isomorphism^[2]. Along the same lines as the proof of Lemma 3, one can verify the following for cases in $\mathcal{C}^{\mathrm{NP}}$.

Lemma 5. For any $(\mathcal{B}, Q) \in \mathcal{C}^{\mathrm{NP}}$, Q is boundedly evaluable under \mathcal{B} if and only if for each relation atom Rin Q_m , there exists $\varphi = R(X \to Y, N) \in \mathcal{B}$ such that $X_R^{Q_m} \subseteq XY \subseteq \operatorname{cov}(Q_m, \mathcal{B}).$

Based on this, we prove that deciding whether Q is boundedly evaluable under \mathcal{B} is NP-complete for (\mathcal{B}, Q) in \mathcal{C}^{NP} .

Upper bound. We give an NP algorithm as follows:

(a) convert Q into its tableau representation $(T_Q, u)^{[2]}$; (b) guess a sub-query Q' = (T, u) of Q such that

 $T' \subseteq T_Q$, and a mapping ρ from T_Q to T;

(c) check (i) whether ρ is a homomorphism from (T_Q, u) to (T, u) and (ii) whether for each relation atom R in Q', there exists $\varphi = R(X \to Y, N) \in \mathcal{B}$ such that $X_R^{Q'} \subseteq XY \subseteq \operatorname{cov}(Q, \mathcal{B})$; return "Yes" if so.

The algorithm is correct since if conditions (i) and (ii) of step (c) hold on Q', they must also hold on the minimal equivalent query Q_m of Q. Indeed, ρ also determines a homomorphism from (T_Q, u) to (T_{Q_m}, u) since Q_m is a minimal equivalent query of Q, i.e., $T_{Q_m} \subseteq T'_Q \subseteq T_Q$; therefore, if condition (ii) holds on Q', by the homomorphism ρ it must also hold on Q_m , i.e., the condition of Lemma 5 applies to Q and \mathcal{B} . Thus, by Lemma 5, Q is boundedly evaluable. The algorithm is in NP since step (a) is in PTIME, and step (c) is in PTIME in $|Q'|, |Q|, |\rho|$, and $|\mathcal{B}|$ while $|Q'| \leq |Q|$ and $\rho = O(|Q|)$. Here |Q| is the size of Q, i.e., the number of attributes and aggregate fields in $Q; |\mathcal{B}|$ is the total length of bag constraints in \mathcal{B} .

Lower bound. To show that the problem is NP-hard, we consider the following problem, denoted by MINCQ.

 $_{\odot}$ Input: A relation schema R and an SPC query Q over R.

 $_{\circ}$ Question: Is Q minimized, i.e., is Q a minimal equivalent query of Q?

It is easy to verify that MINCQ is coNP-complete by reduction from 3-C_{OLORABILITY}, which is NP-complete^[23].

Lemma 6. Problem MINCQ is NP-complete.

We show that the bounded evaluability problem for C^{NP} is NP-hard by reduction from the complement of MINCQ.

Given an instance of MINCQ, i.e., a relation schema $R(A_1, \dots, A_m)$ and an SPC query Q over R, we construct a database schema \mathcal{R}' , an SPC query Q' over \mathcal{R}' and a bag access schema \mathcal{B} . We show that Q is not minimal if and only if Q' is boundedly evaluable under \mathcal{B} .

(1) Database schema \mathcal{R}' consists of a single relation schema $R'(A_1, \dots, A_m, B_1, \dots, B_{\frac{n(n-1)}{2}})$, where *n* is the number of relation atoms that appear in query *Q*.

Intuitively, R' extends R with additional attributes $B_1, \dots, B_{\frac{n(n-1)}{2}}$. As will be shown later, together with Q',

such new attributes will be used as join attributes to pairwisely connect the n relation atoms of Q in Q'.

(2) Query Q' is derived from Q as follows:

o query Q' retains the same number of joins and relation atoms as Q, such that each relation atom R_i (i.e., renaming of relation schema $R \in \mathcal{R}$) is replaced with R_i' (i.e., renaming of relation schema $R' \in \mathcal{R}'$); and

• the selection (join) condition C of query Q' contains all selection predicates of Q, and in addition, the following predicates: for each pair of relations R_i and R_j in Q (i < j), add equality $R'_i[B_p] = R'_j[B_p]$ to C, where $p = n(i-1) - \frac{i(i-1)}{2} + (j-i)$.

Intuitively, C preserves all selection conditions of Q and additionally joins each pair of the n relation atoms on a dedicated attribute $B_i(i \in [1, \frac{n(n-1)}{n}])$: (a) for each B_k , there exist exactly two relation atoms R_i ' and R_j ' such that $R_i'[B_k] = R'_j[B_k]$; and (b) for each R_i' and R_j' , there exists exactly one attribute B_k such that $R_i'[B_k] = R'_j[B_k]$.

(3) The bag access schema \mathcal{B} consists of $\frac{n(n-1)}{2} - 1$ constraints. Let W be the set of all attributes of A_1, \cdots, A_m such that they appear in the selection/join conditions or the top-level projection attributes in Q. Then \mathcal{B} consists of

$$\circ \varphi_1 = R'(\emptyset \to WB_2B_3 \cdots B_{\frac{n(n-1)}{2}}, N)),$$

$$\circ \varphi_2 = R'(\emptyset \to WB_1B_3 \cdots B_{\frac{n(n-1)}{2}}, N)),$$

...

 $\circ \varphi_{\underline{n(n-1)}} = R' (\emptyset \to WB_1B_2 \cdots B_{\underline{n(n-1)}}, N).$

We next show that query Q is not minimal if and only if Q is boundedly evaluable under \mathcal{B} .

 (\Rightarrow) Assume that Q is not minimal. Then none of the n relation atoms in Q' can be removed by minimizing Q'. Hence all $\frac{n(n-1)}{2}$ attributes $B_1, \dots, B_{\frac{n(n-1)}{2}}$, together with W, have to be contained in XY for some $\varphi = R'(X \to Y, N, m)$ in \mathcal{B} by Lemma 5. This yields $|W| + \frac{n(n-1)}{2}$ attributes. This is impossible since for any $\varphi_i \in \mathcal{B}, \varphi_i$ contains $|W| + \frac{n(n-1)}{2} - 1$ attributes only by its definition above.

 $(\Leftarrow) \text{ Assume that } Q' \text{ is boundedly evaluable under } \mathcal{B}.$ Since each $\varphi_i \in \mathcal{B}$ contains $|W| + \frac{n(n-1)}{2} - 1$ attributes, by Lemma 5, $X_{R'_i}^{Q'_m}$ must contain at most $|W| + \frac{n(n-1)}{2} - 1$ attributes for each relation atom R'_i in Q', where Q'_m is the minimal equivalent query of Q'. Since $X_{R'_i}^{Q'}$ contains $|W| + \frac{n(n-1)}{2}$ attributes, query Q' is not minimal. \Box

Remark 2. Despite its intractability, checking the bounded evaluability for C^{NP} is feasible in practice by Lemma 5. Indeed, there have been effective algorithms for minimizing SPC queries, i.e., computing Q_m for $Q^{[2]}$, and the size of Q is typically small. Taking one of these al-

gorithms as an oracle for computing Q_m , one can still efficiently check the bounded evaluability of generic SPC queries: first minimize Q, yielding Q_m , and then check whether Q_m and \mathcal{B} satisfy the condition of Lemma 5 in PTIME in $|Q_m|$ and $|\mathcal{B}|$.

4 Effective syntax

In this section, we propose an effective method to check the bounded evaluability of generic RA_{aggr} queries. We show that while the problem is undecidable (Theorem 1), there exists an effective syntax for boundedly evaluable RA_{aggr} queries, which reduces the problem to syntactic checking (Section 4.1). In addition, we identify two practical subclasses of RA_{aggr} queries and provide their effective syntax. In particular, we give one for RA and show that it covers more bounded queries than the one given in [6] (Section 4.2).

4.1 An effective syntax for RA_{aggr}

Under an access schema \mathcal{B} , an effective syntax for boundedly evaluable queries of \mathbb{L} (\mathbb{L} refers to, e.g., RA or RA_{aggr}) is a subclass $\mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$ of \mathbb{L} such that for any Q in \mathbb{L} ,

(a) if Q is boundedly evaluable, then there exists a query Q' in $\mathcal{L}^{\mathbb{L}}_{\mathcal{B}}$ such that $Q \equiv_{\mathcal{B}} Q'$;

(b) every query Q in $\mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$ is boundedly evaluable; and

(c) it is in PTIME in the size |Q| of query Q and the length $|\mathcal{B}|$ of constraints in \mathcal{B} to check whether $Q \in \mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$.

Here $Q \equiv_{\mathcal{B}} Q'$ if $Q(\mathcal{D}) = Q'(\mathcal{D})$ for all databases $\mathcal{D} \models \mathcal{B}$.

Intuitively, the effective syntax reduces the problem of deciding the bounded evaluability of \mathbb{L} queries to syntactic checking of $\mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$. Indeed, every boundedly evaluable \mathbb{L} query can find an equivalent query in $\mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$ under \mathcal{B} . Hence, we can safely settle with queries in $\mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$, since $\mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$ can express, up to equivalence, all boundedly evaluable \mathbb{L} queries.

Remark 3. To some extent, the development of effective syntax $\mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$ is analogous to the study of range-safe queries for relational calculus. Indeed, the problem for checking the "safety" of relational calculus queries is also undecidable^[2]. Despite this, range-safe queries are supported by commercial DBMS, by making use of an effective syntax of range-safe relational calculus queries. We follow the same approach to dealing with the bounded evaluability of RA_{aggr} queries.

Below we develop such an effective syntax, denoted by $\mathcal{L}_{\mathcal{B}}$, for RA_{aggr} queries that are boundedly evaluable under \mathcal{B} .

<u>The class $\mathcal{L}_{\mathcal{B}}$ </u>. In a nutshell, we characterize $\mathcal{L}_{\mathcal{B}}$ with three sets: BA(Q, \mathcal{B}), BR(Q, \mathcal{B}) and BQ(Q, \mathcal{B}). Informally, under a bag access schema \mathcal{B} , for an RA_{aggr} query Q,

 $\circ BA(Q, \mathcal{B})$ contains attributes (e.g., A) and aggregates (e.g., sum(A)) of Q whose values can be fetched via \mathcal{B} ; $\circ BR(Q, \mathcal{B})$ consists of relations in Q whose partial tuples that are needed to answer Q can be reconstructed from the fetched values for attributes in $BA(Q, \mathcal{B})$; and

 $\circ \mathrm{BQ}(Q,\mathcal{B}) \text{ contains boundedly evaluable sub-queries of } Q.$

An RA_{aggr} query Q is included in $\mathcal{L}_{\mathcal{B}}$ if $Q \in BQ(Q, \mathcal{B})$.

Intuitively, these sets characterize RA_{aggr} queries Q for which the values of all attributes necessary for answering Q can be "deduced" from constants in Q, via joins and fetch under access schema \mathcal{B} . Such attributes participate in RA_{aggr} operations of Q, and are referred as the nontrivial attributes of query Q. The class of such queries makes an effective syntax for boundedly evaluable RA_{aggr} queries.

More specifically, sets BA, BR and BQ are defined in a mutual recursive way using rules given in Fig.1, with

$ \begin{split} &\diamond \mathbf{BA}(Q,\mathcal{B}):\\ &\gamma_1\colon X_Q^c\subseteq BA(Q,\mathcal{B}),\\ &\gamma_2\colon \text{if }A\inBA(Q,\mathcal{B}),\ \Sigma_Q\vdash A=B, \text{ and }B\text{ is an attribute of }Q\text{ (i. e.,}\\ &B\text{ is not an aggregate field, e.g., }sum(R[C])), \text{ then }B\inBA(Q,\mathcal{B})\\ &\gamma_3\colon \text{if }R[X]\subseteqBA(Q,\mathcal{B}),\ R(X\to Y,N)\in\mathcal{B}, \text{ then }R[Y]\subseteqBA(Q,\mathcal{B})\\ &\gamma_4\colon \text{if }Q_s\inBQ(Q,\mathcal{B}), \text{ then }Z_{Q_s}\subseteqBA(Q,\mathcal{B}) \end{split} $
\diamond BR (Q, B): γ_5 : if $R[X] \subseteq$ BA(Q, B), $R([X \to Y, N]) \in B$ and $R[XY]$ contains all nontrivial attributes of Q in R, then $R \in$ BR(Q, B)
\diamond BQ (Q, B): γ ₆ : if all relations R in Q _s of Q are in BR(Q, B), then Q _s ∈ BQ(Q, B)
$\mathcal{L}_{\mathcal{B}}$: RA _{aggr} query Q is in $\mathcal{L}_{\mathcal{B}}$ if $Q \in BQ(Q, \mathcal{B})$

Fig. 1 Effective syntax $\mathcal{L}_{\mathcal{B}}$ for RA_{aggr} queries

Notation	Definition
$\begin{array}{c} A \ (\mathrm{or} \\ R[A]) \end{array}$	An attribute or an aggregate field in ${\cal Q}$
X, Y	Sets of attributes in Q
Q	Number of attributes and aggregate fields in ${\cal Q}$
Q	Number of relation atoms in Q
X_Q	Set of all attributes and aggregate fields in ${\cal Q}$
X_Q^c	Set of attributes A of Q in constant selections $\sigma_{A=c}$
ΣQ^3	Set of equality predicates in selections/joins of ${\cal Q}$
$\Sigma_Q \vdash A = B$	$A=B$ can be deduced from Σ_Q via equality transitivity
Z_Q	Set of attributes and aggregate fields of the output of ${\cal Q}$
nontr. attr.	Attributes participated in algebra operations of ${\cal Q}$
\mathcal{A}/\mathcal{B}	${\rm Access\ schema}/{\rm bag\ access\ schema}$
$ \mathcal{B} $	Total length of bag constraints in ${\cal B}$
$\ \mathcal{B}\ $	The number of bag constraints in ${\cal B}$
ϕ/φ	${\rm Access\ constraint/bag\ access\ constraint}$
$\mathcal{L}_{\mathcal{B}}$	Effective syntax for RA_{aggr} queries bounded. eval. under $\mathcal B$
$\mathcal{L}_{\mathcal{B}}^{\mathbb{L}}$	Effective syntax for $\mathbbm{L}\text{-queries}$ bounded. eval. under $\mathcal B$

Table 1 Notations and definitions

notations explained in Table 1. Intuitively, (1) rule γ_1 of Fig.1 includes constant attributes X_Q^c (see Table 1) in BA(Q, \mathcal{B}); (2) γ_2 propagates value from attributes and aggregate fields to join attributes; (3) γ_3 specifies value propagation via fetch; (4) γ_4 says that if a sub-query is boundedly evaluable, then its output attributes and aggregate fields can also be fetched; (5) γ_5 adds a relation atom R to BR(Q, \mathcal{B}) only when the partial tuples of Rcan be reconstructed from combinations of the fetched values; and (6) γ_6 says that a sub-query is boundedly evaluable if all its relations can be correctly fetched.

As shown in Table 1, Σ_Q denotes the set of equality predicates embedded in the selection or join conditions of Q, and $\Sigma_Q \vdash A = B$ denotes that equality A = B can be deduced from Σ_Q by the transitivity of the equality relation.

Example 7. Recall query Q_2 from Example 2 and bag access schema \mathcal{B}_1 from Example 4. We show that $Q_2 \in \mathcal{L}_{\mathcal{B}_1}$.

(1) Initially, by rule γ_1 , BA(Q_2, \mathcal{B}_1) includes f.uid and c.cty, where f (resp. c) are shorthands for friend (resp. checkin).

(2) By rule γ_3 and φ_1 , BA (Q_2, \mathcal{B}_1) further includes f.fid.

(3) Since $\Sigma_Q \vdash \text{f.fid} = \text{c.uid}$, by f.fid $\in BA(Q_2, \mathcal{B}_1)$, we have that $BA(Q_2, \mathcal{B}_1)$ includes c.uid by rule γ_2 .

(4) By γ_5 , $f \in BR(Q_2, \mathcal{B}_1)$ because both f.uid and f.fid are in $BA(Q_2, \mathcal{B}_1)$ and are attributes of φ_1 . Similarly, $c \in BR(Q_2, \mathcal{B}_1)$ because of φ_2 . Note that only c.uid and c.cty are nontrivial attributes of Q in relation c and they are both in $BA(Q_2, \mathcal{B}_1)$.

(5) By γ_6 , sub-query Q_3 and query Q_2 itself are in $BQ(Q, \mathcal{B})$.

As another example, recall query Q_6 from Example 5 and \mathcal{B}_2 from Example 4. We next show that $Q_6 \in \mathcal{L}_{\mathcal{B}_2}$.

(1) One can readily deduce that $BA(Q_6, \mathcal{B}_2)$ includes B and C by using γ_1 and γ_3 , and that $BR(Q_6, \mathcal{B}_2)$ includes R with γ_5 .

(2) By γ_6 , BQ (Q_6, \mathcal{B}_2) includes sub-query Q_7 of Q_6 .

(3) Hence, further by γ_4 we have that $Z_{Q_7} \in BA(Q_6, \mathcal{B}_2)$, where Z_{Q_7} is the output of Q_7 , i.e., an aggregate field.

(4) By γ_2 , we know that BA(Q_6, \mathcal{B}_2) includes F since $\sigma_{Q_6} \vdash Z_{Q_7} = F$ and F is not an aggregate field.

(5) Thus, by γ_5 and γ_6 , $S \in BR(Q_6, \mathcal{B}_2)$ and $Q_6 \in BQ(Q_6, \mathcal{B}_2)$.

Note that $Q_4 \notin \mathcal{L}_{\mathcal{B}_2}$. However, $Q_4 \equiv_{\mathcal{B}_2} Q_6$, $Q_6 \in \mathcal{L}_{\mathcal{B}_2}$ and Q_6 is boundedly evaluable under \mathcal{B}_2 . Similarly, for Q_8 , Q_9^1 and \mathcal{B}_3 of Example 6, one can verify that $Q_8 \notin \mathcal{L}_{\mathcal{B}_3}$ but $Q_9^1 \in \mathcal{L}_{\mathcal{B}_3}$ and Q_9^1 is boundedly evaluable under \mathcal{B}_3 .

We next show that $\mathcal{L}_{\mathcal{B}}$ is indeed an effective syntax

³To reduce notations, we assume *w.l.o.g.* that selection conditions are conjunctive, i.e., \vee in selection predicates is reduced using \cup .

for boundedly evaluable RA_{aggr} queries under \mathcal{B} .

Theorem 7. Under any bag access schema \mathcal{B} , $\mathcal{L}_{\mathcal{B}}$ is an effective syntax for boundedly evaluable RA_{aggr} queries.

Proof. We show below that $\mathcal{L}_{\mathcal{B}}$ has properties (a) and (b) of an effective syntax, by proving the following lemmas. We will constructively prove property (c) in Section 5.2.

(I) For any bounded plan ξ under \mathcal{B} , there is $Q \equiv_{\mathcal{B}} \xi$ in $\mathcal{L}_{\mathcal{B}}$.

(II) For any $Q \in \mathcal{L}_{\mathcal{B}}$, there is plan $\xi \equiv_{\mathcal{B}} Q$ bounded under \mathcal{B} .

These suffice. Indeed, for any Q that is bounded under \mathcal{B} , by definition there must exist a plan ξ_Q bounded under \mathcal{B} ; hence by (I), there exists $Q' \equiv_{\mathcal{B}} \xi_Q$ in $\mathcal{L}_{\mathcal{B}}$. On the other hand, if $Q \equiv_{\mathcal{B}} Q' \in \mathcal{L}_{\mathcal{B}}$, by (II), Q' has a bounded plan $\xi' \equiv_{\mathcal{B}} Q' \equiv_{\mathcal{B}} Q$, i.e., Q is also boundedly evaluable under \mathcal{B} . Hence, $\mathcal{L}_{\mathcal{B}}$ has properties (a) and (b) of an effective syntax.

We next prove the two lemmas.

<u>Proof of (I)</u>. We prove it by induction on the structure of ξ .

Base case. When ξ is $\{c\}$ or \emptyset , by definition ξ itself is in $\mathcal{L}_{\mathcal{B}}$.

Induction. We consider the structure of ξ .

(i) ξ is $\operatorname{gpBy}(\xi', X, \operatorname{agg}(V))$. By the induction hypothesis, there exists a query $Q' \equiv_{\mathcal{B}} \xi'$ such that $Q' \in \mathcal{L}_{\mathcal{B}}$. Consider $Q = \operatorname{gpBy}(Q', X, \operatorname{agg}(V))$. By the definition of $\mathcal{L}_{\mathcal{B}}$, all relations in Q' are in $\operatorname{BR}(Q', \mathcal{B}) \subseteq \operatorname{BR}(Q, \mathcal{B})$ (since Q and Q' share the same nontrivial attributes). Hence $Q \in \operatorname{BQ}(Q, \mathcal{B})$ by rule γ_6 . That is, $Q \in \mathcal{L}_{\mathcal{B}}$. Obviously, $Q \equiv_{\mathcal{B}} \xi$.

The cases for $\xi = \pi_Y(\xi')$, $\sigma_C(\xi')$, $\xi_1 \times \xi_2$, $\xi_1 \cup \xi_2$, $\xi_1 - \xi_2$ are similar and can be verified along the same lines.

(ii) ξ is fetch (ξ', φ) with $\varphi = R(X \to Y, N)$. By the induction hypothesis, there exists query $Q' \equiv_{\mathcal{B}} \xi'$ such that $Q' \in \mathcal{L}_{\mathcal{B}}$. Consider $Q = \pi_{R[XY]}(Q' \bowtie_{Z_{Q'}=R[X]} R)$. By the semantics of fetch, $Q \equiv_{\mathcal{B}} \xi$. We next show that $Q \in \mathcal{L}_{\mathcal{B}}$. Since $Q' \in \mathcal{L}_{\mathcal{B}}, Q' \in BQ(Q', \mathcal{B})$. Hence by rule $\gamma_4, Q'[X] \subseteq BA(Q', \mathcal{B}) \subseteq BA(Q, \mathcal{B})$. Further by γ_2 , $R[X] \subseteq BA(Q, \mathcal{B})$. By $\gamma_3, R[Y] \subseteq BA(Q, \mathcal{B})$. Hence by γ_5 and $\gamma_6, Q \in BQ(Q, \mathcal{B})$. That is, $\xi \in \mathcal{L}_{\mathcal{B}}$.

<u>Proof of (II)</u>. Since $Q \in \mathcal{L}_{\mathcal{B}}$, by the definition of $\mathcal{L}_{\mathcal{B}}$ there must exist a proof ℓ_Q consisting of applications of rules in Fig.1 that deduces $Q \in BQ(Q, \mathcal{B})$, i.e., a sequence of the form

$$(BA_0, BR_0, BQ_0) \xrightarrow{r_1} \cdots \xrightarrow{r_n} (BA_n, BR_n, BQ_n)$$

where (a) $r_i(i \in [1, n])$ is one of the rules in Fig.1; (b) BA₀ = BR₀ = BQ₀ = \emptyset ; (c) for each step *i*, only one of BA_i, BR_i and BQ_i is changed in BA_{i+1}, BR_{i+1} and BQ_{i+1}, respectively; and (d) r_n is rule γ_6 that deduces $Q \in BQ(Q, \mathcal{B})$. We define the length of ℓ_Q as the number

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n of rules applied in ℓ_Q .

Induction hypothesis. We show that for a proof ℓ of length i,

o if $A \in BA_{i+1}$ but $A \notin BA_i$, values for A that are necessary for answering Q can be fetched via bounded plan under \mathcal{B} ;

◦ if $R \in BR_{i+1}$ but $R \notin BR_i$, then values from R necessary for Q can be fetched via bounded plans under \mathcal{B} ; and

◦ if $q \in BR_{i+1}$ but $q \notin BQ_i$, then the exact answers to sub-query Q of Q can be answered via bounded plans under \mathcal{B} .

Note that for any $Q \in \mathcal{L}_{\mathcal{B}}$, Q must have a proof ℓ_Q ending by including $Q \in BQ(Q, \mathcal{B})$. If the induction hypothesis holds, Q must have a bounded plan under \mathcal{B} , which proves lemma (II).

We next prove it by induction on the length $l(\ell)$ of ℓ .

Base case. When $l(\ell) = 1$, then rule r_1 can only be either (i) γ_1 of Fig. 1, i.e., to include $A \in BA_1$ from selection A = c of Q; or (ii) γ_3 of Fig. 1, i.e., to include R[Y] in BA_1 with $\varphi = R([\emptyset \to Y, N]) \in \mathcal{B}$. For (i), simply let $\xi_A =$ $\{c\}$. Then ξ_A is a bounded plan that fetches all necessary values for A. For (ii), let $\xi_{R[Y]} = \text{fetch}(\emptyset, \varphi)$. Then by the semantics of fetch, all values for R[Y] that are necessary for answering Q are fetched by $\xi_{R[Y]}$ (here we rename Qbeforehand such that there exist no duplicated attribute names).

Induction. Assume that the hypothesis holds for proofs of length at most k. Consider proof ℓ of length k+1. We discuss the last step $(BA_i, BR_i, BQ_i) \xrightarrow{r_{i+1}} (BA_{i+1}, BR_{i+1}, BQ_{i+1})$ of ℓ .

(i) If r_{k+1} is rule γ_1 with attribute A = c, then A can be fetched in exactly the same way as the base case.

(ii) If r_{k+1} is rule γ_2 that includes attribute B in BA_{i+1} with A = B, then attribute A must be included in BA_{i+1} at some steps prior to k+1. By the induction hypothesis, there must exist a bounded plan ξ_A that fetches all necessary values for answering Q except B. Hence $\xi_B = \xi_A$ is also a bounded plan that fetches B for Q by the condition A = B.

(iii) If r_{k+1} is rule γ_3 that includes R[Y] in BA_{i+1} with $R[X] \subseteq BA(Q, \mathcal{B})$ and constraint $\varphi = R(X \to Y, N)$, then there exist steps i_1, \dots, i_p prior to k+1 that include $R[X_1], \dots, R[X_{i_p}]$ in BA such that $R[X_1] \cup \dots \cup R[X_p] = R[X]$. Hence by the induction hypothesis, $R[X_j](j \in [1, p])$ has bounded plan $\xi_{R[X_j]}$. Let $\xi_{R[X]}$ be $\bowtie_{j=1}^p \xi_{R[X_j]}$, then $\xi_{R[X]}$ fetches all values for R[X] that are necessary for answering Q. Hence, further by the semantics of fetch, R[Y] has a plan fetch($\xi_{R[X]}, \varphi$) that retrieves all R[Y]-values needed for answering Q.

(iv) If r_{k+1} is γ_4 that includes Z_{Q_s} in BA_{i+1} from a subquery Q_s of Q that is included in BQ_j at step j < i + 1, then by the induction hypothesis, there exists a plan ξ_{Q_s} for Q_s under \mathcal{B} that exactly answers Q_s . Hence we can get values for its output attributes Z_{Q_s} simply by ξ_{Q_s} . Note that since ξ_{Q_s} is an exact plan for Q_s , the values for Z_{Q_s} are guaranteed correct even when Q_s is an aggregate subquery.

(v) If r_{k+1} is γ_5 that includes R in BR_{i+1} with R[X]and $\varphi = R(X \to Y, N) \in \mathcal{B}$, then by the induction hypothesis, there exist plans $\xi_{R[X_1]}, \dots, \xi_{R[X_p]}$ to fetch all necessary values for $R[X_1], \dots, R[X_p]$ for Q, respectively, such that $R[X_1] \cup \dots \cup R[X_p] = R[X]$. Hence R[X] has a bounded plan $\xi_{R[X]} = \bowtie_{j=1}^p \xi_{R[X_j]}$ that fetches all necessary R[X]-values for Q. Since R[XY] covers all nontrivial attributes of R for Q, by $\xi_{R[XY]} = \operatorname{fetch}(\xi_{R[X]}, \varphi)$, we can fetch all combinations of R[XY]-values that are needed for answering Q.

(vi) If r_{k+1} is γ_6 that includes Q_s in BQ_{i+1} , then all relations R_1, \dots, R_p of Q_s have been included in {BR in prior steps. Hence by the induction hypothesis, there exist $\xi_{R_1}, \dots, \xi_{R_p}$ that fetch all values from R_1, \dots, R_p , respectively, which are necessary for Q. Now construct plan ξ_{Q_s} by replacing each relation $R_i(i \in [1, p])$ in Q_s with ξ_{R_i} . Then ξ_{Q_s} must be a query plan for Q_s of Q since all necessary value combinations can be retrieved from D via $\xi_{R_i}(i \in [1, p])$, and Q_s then filters and combines values exactly the same as on D.

Hence the hypothesis holds for proofs of length k+1. \Box

4.2 Special cases

These are two important sub-classes of RA_{aggr} : (1) RA consists of RA_{aggr} queries without aggregation; and (2) RA_{aggr}^{0} is the class of RA_{aggr} queries in which group-by aggregation, if it exists, only appears at the top-level (final operation). It is common to find RA and RA_{aggr}^{0} in practice.

We provide effective syntax for boundedly evaluable RA and RA^0_{aggr} queries. Denote by $\mathcal{L}_{\mathcal{B}}[RA]$ and $\mathcal{L}_{\mathcal{B}}[RA^0_{agg}]$ the class of RA and the class of RA^0_{aggr} queries that are in $\mathcal{L}_{\mathcal{B}}$, respectively. They yield effective syntax for RA and RA^0_{aggr} .

Corollary 8. For any access schema \mathcal{B} , (1) $\mathcal{L}_{\mathcal{B}}[\text{RA}]$ is an effective syntax for RA queries bounded by \mathcal{B} ; (2) $\mathcal{L}_{\mathcal{B}}[RA_{\text{agg}}^{0}]$ is an effective syntax for $\text{RA}_{\text{aggr}}^{0}$ queries bounded by \mathcal{B} .

Proof. Since it is in PTIME to check whether a query is in $\mathcal{L}_{\mathcal{B}}$ and every query in $\mathcal{L}_{\mathcal{B}}$ has a bounded plan under \mathcal{B} , to show that $\mathcal{L}_{\mathcal{B}}[\text{RA}]$ and $\mathcal{L}_{\mathcal{B}}[\text{RA}_{\text{aggr}}^{0}]$ are effective syntax for boundedly evaluable RA and $\text{RA}_{\text{aggr}}^{0}$ queries, respectively, it suffices to show that for any boundedly evaluable RA Q_1 and $\text{RA}_{\text{aggr}}^{0} Q_2$, there exist $Q'_1 \in \mathcal{L}_{\mathcal{B}}[\text{RA}]$ and $Q'_2 \in \mathcal{L}_{\mathcal{B}}[\text{RA}_{\text{aggr}}^{0}]$ such that $Q_1 \equiv_{\mathcal{B}} Q'_1$ and $Q_2 \equiv_{\mathcal{B}} Q'_2$. This is verified along the same lines as the proof of Lemma (I) for Theorem 7 above, by showing that every bounded RA (resp. $\text{RA}_{\text{aggr}}^{0}$) plan has an equivalent query in $\mathcal{L}_{\mathcal{B}}[\text{RA}]$ (resp. $\mathcal{L}_{\mathcal{B}}[\text{RA}_{\text{aggr}}^{0}]$).

There are close connections between RA^0_{aggr} and RA regarding their effective syntax: any effective syntax for

boundedly evaluable $\operatorname{RA}^{0}_{\operatorname{aggr}}$ queries also gives us an effective syntax for boundedly evaluable RA queries, and vice versa. For any class \mathcal{L} of $\operatorname{RA}^{0}_{\operatorname{aggr}}$ queries $Q = \operatorname{gpBy}(Q', X, \overline{\operatorname{agg}}(V))$, denote by (a) \mathcal{L}^{0} the class of RA queries Q' that are sub-queries embedded in $\operatorname{RA}_{\operatorname{aggr}}$ queries Q in \mathcal{L} ; and (b) $\mathcal{L}[\operatorname{RA}]$ the class of RA queries in \mathcal{L} . Then we have the following.

Lemma 9. Under any bag access schema \mathcal{B} ,

(1) RA is an effective syntax for boundedly evaluable RA if \mathcal{L} is an effective syntax for boundedly evaluable RA_{aggr};

(2) \mathcal{L} is an effective syntax for boundedly evaluable RA_{aggr} if \mathcal{L}^{0} is an effective syntax for boundedly evaluable RA.

Proof. Lemma 9(1) can be verified by the definition of effective syntax. We focus on Lemma 9(2) here (the proof for Lemma 9(1) is simpler). By the definition of boundedly evaluable queries, it is easy to show the following lemma: for any $RA_{aggr} Q = gpBy(Q', X, \overline{agg(V)})$, under \mathcal{B} , Q is boundedly evaluable iff Q' is boundedly evaluable.

We next use the lemma to prove Lemma 9(2). When \mathcal{L}^0 is an effective syntax for boundedly evaluable RA queries under \mathcal{B} , consider the associated class \mathcal{L} of \mathcal{L}^0 . (1) First observe that all queries in \mathcal{L} are also boundedly evaluable since RA queries in \mathcal{L}^0 are. (2) For any RA_{aggr} query $Q = \text{gpBy}(Q_1, X, \overline{\text{agg}}(V))$ that is boundedly evaluable, by the lemma above, Q_1 is also boundedly evaluable under \mathcal{B} . Hence, there exists $Q'_1 \in \mathcal{L}^0$ such that $Q_1 \equiv_{\mathcal{B}} Q'_1$. Hence $Q' = \text{gpBy}(Q'_1, X, \overline{\text{agg}}(V)) \equiv_{\mathcal{B}} Q$ and $Q' \in \mathcal{L}$ (since $Q'_1 \in \mathcal{L}^0$). (3) Moreover, it is in PTIME to check whether a query Q is in \mathcal{L} by checking whether its embedded RA query Q' is in \mathcal{L}^0 , in PTIME. From (1), (2) and (3) above, Lemma 9(2) follows.

By Lemma 9, one can easily extend an effective syntax for boundedly evaluable RA queries, e.g., covered RA in[6], to an effective syntax for boundedly evaluable RA_{ag-gr} queries.

One might think that such an extension is also possible for RA_{aggr} . However, when group-by aggregation is nested with other RA_{aggr} operators, a convenient extension is beyond reach. It is much harder for RA_{aggr} to characterize propagation of values from aggregate subqueries to other relations, or to cover all boundedly evaluable queries up to equivalence.

Nonetheless, $\mathcal{L}_{\mathcal{B}}[RA]$ is more expressive than the class of covered RA of [6], which is also an effective syntax for RA.

Proposition 10. For any bag access schema \mathcal{B} , the set of RA queries covered by \mathcal{B} is properly contained in $\mathcal{L}_{\mathcal{B}}[RA]$.

Proof. One can verify that covered RA queries^[6] can be expressed in $\mathcal{L}_{\mathcal{B}}[\text{RA}]$ without rule γ_4 . Hence it is a subclass of $\mathcal{L}_{\mathcal{B}}$. To see it is a proper subclass, consider an $\mathcal{L}_{\mathcal{B}}[\text{RA}]$ query Q over relations R(A, B) and S(C, D): $Q = \pi_D((\sigma_{A=1}R_1 - \sigma_{B=1}R_2) \bowtie_{A=C} S), \text{ where } R_1 \text{ and } R_2$ rename R. Consider \mathcal{B} consisting of $R([A \to B, N_1]),$ $R([B \to A, N_2]) \text{ and } S([C \to D, N_3]).$ One can verify that Q is not covered by \mathcal{B} since subquery S is not covered (see [6]). However, $Q \in \mathcal{L}_{\mathcal{B}}[\text{RA}].$

5 BEAS for querying big data

In this section, we show how to extend DBMS with the functionality of bounded evaluation. We first present such a framework (Section 5.1). We then provide algorithms underlying the framework, for checking the bounded evaluability (Section 5.2) and generating bounded plans (Section 5.3).

5.1 A Framework of bounded evaluation

The framework, referred to as BEAS, is shown in Fig.2. Given an application that involves queries over instances of a database schema \mathcal{R} , BEAS works as follows.

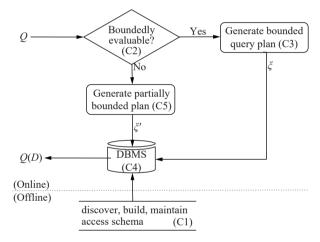


Fig. 2 BEAS: Bounded evaluation on DBMS

<u>Offline preprocessing</u>. As shown in C1 of Fig. 2, as offline preprocessing, BEAS discovers a bag access schema \mathcal{B} from (sample) instances of \mathcal{R} , builds indices of \mathcal{B} on the database \mathcal{D} of \mathcal{R} in use, and maintains \mathcal{B} in response to updates to \mathcal{D} .

<u>Online processing</u>. When a user poses an $\operatorname{RA}_{\operatorname{aggr}}$ query Q on \mathcal{D} , BEAS first checks whether Q is boundedly evaluable under \mathcal{B} (>C2). If so, it generates a bounded query plan ξ for Q under \mathcal{B} (C3), which is interpreted as an SQL query Q_{ξ} and hence can be directly executed by the underlying DBMS on a bounded dataset \mathcal{D}_Q identified by plan ξ (C4). If Q is not boundedly evaluable, it generates a query plan ξ' for Q that is partially bounded, to make maximal use of access constraints in \mathcal{B} (C5). The (partially) bounded plans are optimized and executed by DBMS (C4).

Note that the BEAS framework does not need to change the underlying DBMS. Indeed, it interacts with

the DBMS via SQL only. Hence, BEAS can be built on top of any existing DBMS, providing a bounded evaluation capacity.

BEAS can also compute approximate answers to unbounded queries under constrained resources, and offers deterministic accuracy guarantees under access schema^[17]. We focus on computing exact answers in this paper.

Below we develop algorithms for components C2 and C3 of BEAS in Section 5.2 and Section 5.3, respectively.

5.2 Checking bounded evaluability

We next develop a practical algorithm for component C2 of BEAS. Under a bag access schema \mathcal{B} , given an RA_{aggr} query Q, it decides whether Q is boundedly evaluable.

To do this, we first checks whether Q and \mathcal{B} fall into the two classes of special cases, i.e., \mathcal{C}^{P} or $\mathcal{C}^{\mathrm{NP}}$, in PTIME. If so, their bounded evaluability can be decided efficiently as shown in the proofs of Theorems 2 and 4. Otherwise, we check whether Q is in the effective syntax $\mathcal{L}_{\mathcal{B}}$ for RA_{aggr} (Section 4). Below we give a PTIME algorithm for this.

Algorithm BEChk. The algorithm, denoted by BEChk, is shown in Algorithm 1. It first sets $BA(Q, \mathcal{B})$, $BR(Q, \mathcal{B})$ and $BQ(Q, \mathcal{B})$ to \emptyset . It then iteratively updates $BA(Q, \mathcal{B})$, $BR(Q, \mathcal{B})$ and $BQ(Q, \mathcal{B})$ using the rules in Fig. 1. In each iteration, it

(a) first computes $BA(Q, \mathcal{B})$ using γ_1 , γ_2 and γ_3 (line 3);

(b) then updates $BR(Q, \mathcal{B})$ using γ_4 (line 4); and

(c) it finally updates $BQ(Q, \mathcal{B})$ using γ_5 (line 5).

The iteration continues until $BQ(Q, \mathcal{B})$ can no longer be updated (line 6). It returns "Yes" if $Q \in BQ(Q, \mathcal{B})$ and "No" otherwise (lines 7–8). In each iteration, steps (b) and (c) are straightforward. Below we discuss step (a) in more details.

Algorithm 1. BEChk

Input: Relational schema \mathcal{R} , $\operatorname{RA}_{\operatorname{aggr}} Q$ and bag access schema \mathcal{B} over \mathcal{R} .

Output: "Yes" ("No") if Q is (is not) boundedly evaluable under \mathcal{B} .

- 1 BA $(Q, \mathcal{B}) \leftarrow \emptyset$; BR $(Q, \mathcal{B}) \leftarrow \emptyset$; BQ $(Q, \mathcal{B}) \leftarrow \emptyset$; flag \leftarrow true;
- 2 while flag = true do
- 3 compute $BA(Q, \mathcal{B})$ using $\gamma_1, \gamma_2, \gamma_3 //$ recall γ_i in Table 1
- 4 compute $BR(Q, \mathcal{B})$ using γ_5 ;
- 5 compute $BQ(Q, \mathcal{B})$ using γ_6 ;
- 6 **if** BQ(Q, B) is not changed **then** flag \leftarrow false;
- 7 if $Q \in BQ(Q, \mathcal{B})$ then return "Yes";
- 8 else return "No";

Computing $BA(Q, \mathcal{B})$ (line 3 of Algorithm 1). In each iteration, $BA(Q, \mathcal{B})$ is updated in two steps, as follows.

(1) Building universal relation. We first build a "universal schema" U_Q of Q w.r.t. $BQ(Q, \mathcal{B})$, by mapping attributes and aggregate fields of Q to attributes of U_Q , via a mapping function ρ . For any two attributes R[A] and S[B] of Q, $\rho(R[A]) = \rho(S[B])$ if and only if $\Sigma_Q \vdash R[A] = S[B]$ is in the selection condition of Q. For aggregate field agg(A) and attribute R[B], $agg(A)) = \rho(R[B])$ only when agg(A) is in Z_{Q_s} (recall Table 1) for some $Q_s \in BQ(Q, \mathcal{B})$. Accordingly, bag constraints in \mathcal{B} are also mapped on to U_Q by ρ .

(2) Computing fetch closure. We then reduce the computation of $BA(Q, \mathcal{B})$ to the computation of fetch closures over U_Q with \mathcal{B} w.r.t. ρ . For a set W of attributes of U_Q , its fetch closure, denoted by $W^{\mathcal{B}}$, is a set of attributes of U_Q such that

(i) $W \subseteq W^{\mathcal{B}}$;

(ii) if $X' \subseteq W^{\mathcal{B}}$ and $\varphi = R(X \to Y, N) \in \mathcal{B}$ such that $\rho(R[X]) = X'$ and $\rho(R[Y]) = Y'$, then $Y' \subseteq W^{\mathcal{B}}$; and

(iii) $W^{\mathcal{B}}$ contains nothing else.

Let $W = \rho(X_Q^c) \cup \rho(BA(Q, \mathcal{B})) \cup \bigcup_{Q_s \in BQ(Q, \mathcal{B})} \rho(Z_{Q_s}).$ We set $BA(Q, \mathcal{B}) = \{A \in X_Q \mid \rho(A) \in W^{\mathcal{B}}\}$ (see Z_Q, X_Q in Table 1).

Example 8. Recall Q_2 from Example 2 and bag access schema \mathcal{B}_1 from Example 4. Algorithm BEChk iteratively updates BA, BR and BQ for Q_2 and \mathcal{B}_1 , which are all \emptyset initially.

In the first iteration, BEChk starts by updating $BA(Q_2, \mathcal{B}_1)$ (line 3). To do this, it builds a universal relation $U_{Q_2} = \{ \text{f.uid}, \text{f.fid}, \text{c.cty}, \text{c.date} \}$ via function ρ that maps c.uid to f.fid and keeps all other attributes intact (f and c stand for friend and checkin, respectively). Since $\rho(X_{Q_2}^c) = \{ \text{f.uid, c.cty} \},\$ $\rho(\mathrm{BA}(Q_2,\mathcal{B}_1)) = \emptyset$ and $BQ(Q_2, \mathcal{B}_1) = \emptyset$, BEChk sets W to $\rho(X_{Q_2}^c)$ and computes $W^{\mathcal{B}_1}$ of W, the fetch closure yielding $W^{\mathcal{B}_1} = \{ \text{f.uid}, \text{f.fid}, \text{c.cty} \}$. Hence it updates $BA(Q_2, \mathcal{B}_1)$ to {f.uid, f.fid, c.cty}. It then updates $BR(Q_2, \mathcal{B}_1)$ to {f, c} since all nontrivial attributes of f and c are already in $BA(Q_2, \mathcal{B}_1)$ (line 4). BEChk finally updates $BQ(Q_2, \mathcal{B}_1)$ to $\{Q_3, Q_2\}$ (line 5) and terminates in next iteration and returns "Yes".

It gets more involved for Q_6 from Example 5 and \mathcal{B}_2 from Example 4. In the first iteration, BEChk builds a universal schema $U_{Q_6} = \{A, B, C, E, F, W, F'\}$ via a mapping function ρ that keeps attributes of R and S and maps aggregate field (i.e., the output) sum(y) of Q_7 to F. Note that ρ does not map sum(y) to E although $\Sigma_{Q_6} \vdash \operatorname{sum}(y) = E \quad \text{since} \quad Q_7 \notin \operatorname{BQ}(Q_6, \mathcal{B}_2) = \emptyset \quad \text{yet.}$ BEChk then computes the fetch closure of $X_{Q_6}^C$ over U_{Q_6} and sets $BA(Q_6, \mathcal{B}_2)$ to $\{B, C, F\}$. It then finds that all nontrivial attributes of R are in $BA(Q_6, \mathcal{B}_2)$ and hence updates $BR(Q_6, \mathcal{B}_2)$ to $\{R\}$. Consequently, it sets $BQ(Q_6, \mathcal{B}_2)$ to Q_7 as well. In the second iteration, BEChk builds anupdated universal relation $U_{Q_6} = \{A, B, C, E, F, W\}$ since $Q_7 \in BQ(Q_6, \mathcal{B}_2)$ and $\Sigma_{Q_6} \vdash \operatorname{sum}(y) = E$. It continues to update $\operatorname{BA}(Q_6, \mathcal{B}_2)$ to $\{B, C, E, F, W\}$, BR (Q_6, \mathcal{B}_2) to $\{R, S\}$ and BQ (Q_6, \mathcal{B}_2) to $\{Q_7, Q_6\}$. It terminates after the third iterations and returns "Yes" for Q_6 under \mathcal{B}_2 .

Correctness & Complexity. To see that BEChk correctly checks the effective syntax $\mathcal{L}_{\mathcal{B}}$ of Fig. 1, observe the following. (1) For any fixed BQ (Q, \mathcal{B}) , the corresponding BA (Q, \mathcal{B}) decided by rules $\gamma_1, \dots, \gamma_4$ is exactly the fetch closure $W^{\mathcal{B}}$ (recall the definition of $W^{\mathcal{B}}$ above). (2) The while loop propagates changes from BA to BR and to BQ, and finally to BA again, until reaching a fixed point w.r.t. the rules of Fig. 1.

BEChk can be implemented in $O(p_Q(||Q|||B| + |Q|))$ time, where p_Q is the number of sub-queries in Q, ||Q|| is the number of relation atoms in Q, |Q| is the number of attributes and aggregate fields in the relation atoms and predicates of Q, ||B|| and |B| are the number and total length of bag constraints in B, respectively (see Table 1). Indeed, computing the fetch closure can be implemented in O(||Q|||B||)-time, and hence each while iteration is in O(||Q|||B|| + |Q|) time; there are at most p_Q iterations.

Algorithm BEChk provides a constructive proof for property (c) of the effective syntax $\mathcal{L}_{\mathcal{B}}$ in Theorem 7, i.e., it is in PTIME to check whether $Q \in \mathcal{L}_{\mathcal{B}}$ for an RA_{aggr} query Q.

This also completes the proof of Theorem 7.

5.3 Generating bounded plans

We next provide an algorithm underlying component C3 of BEAS, denoted by BPlan. Given a bag access schema \mathcal{B} and an RA_{aggr} query Q that is determined to be boundedly evaluable under \mathcal{B} by BEChk of Section 5.2, BPlan generates a bounded RA_{aggr} query plan for Q under \mathcal{B} .

Algorithm BPlan. Given a boundedly evaluable $\operatorname{RA}_{\operatorname{aggr}}$ query $Q \in \mathcal{L}_{\mathcal{B}}$ (see Section 4), BPlan generates a bounded plan ξ_Q for Q under \mathcal{B} as follows: (1) fetch a bounded amount of data for each relation R that appears in Q, and (2) carry out operations of Q over fetched data. While step (2) is straightforward, step (1) is rather involved.

To carry out step (1), BPlan generates bounded logical access paths (bLAPs). A bLAP ξ_R for a relation R in Q fetches all values (partial tuples) of R that are necessary for evaluating Q with \mathcal{B} ; moreover, ξ_R is a bounded RA_{aggr} plan under \mathcal{B} . Intuitively, bLAPs play the same role as conventional DBMS access paths. But instead of accessing complete tuples by scan or index, bLAPs fetches values (partial tuples) using \mathcal{B} such that the amount of data accessed is bounded.

More specifically, we give an algorithm, denoted by BAP, as a sub-procedure of BPlan to find a bLAP ξ_R for R under \mathcal{B} . While there may exist exponentially many such bLAPs, BAP aims at computing those with minimum cost.

After BAP computes bLAP ξ_R for every relation R in

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Q, algorithm BPlan generates a bounded plan ξ_Q for Qunder \mathcal{B} , by replacing each R in Q with its bLAP ξ_R , and by carrying out RA_{aggr} operations of Q on the data retrieved by ξ_R .

In the rest of the section, we focus on algorithm BAP.

Parametric cost measures. To evaluate the quality of bLAPs found by BAP, we start with a generic class of cost functions. Conventional access path measures assess the cost of physical table-access methods, e.g., sequential scan and index scan^[11]. These metrics do not apply to bLAPs, which involve, e.g., fetch and joins. Hence, BAP employs a generic cost function $c(\xi_R)$ that takes user specified functions as parameters, to express various cost measures over ξ_R as bLAPs, e.g., output size, data access, etc.

The cost of a bLAP ξ_R for R under \mathcal{B} , denoted by $\boldsymbol{c}(\xi_R)$, is inductively defined in Table 2, with five user configurable parameter functions Γ_{\bowtie} , Γ_U , Γ_- , Γ_{fetch} and Γ_{gpBy} .

Table 2 c() with parameters $\Gamma_{\bowtie/-/\cup/\text{fetch/gpBy}^4}$

bLAP <i>ξR</i>	$oldsymbol{c}(oldsymbol{\xi}_{oldsymbol{R}}) ext{of} oldsymbol{\xi}_{oldsymbol{R}}$
$\{c\}$ or Ø	1
$\sigma_C(\xi')$	$\boldsymbol{c}(\xi') imes \lambda_{\sigma}(C)$
$\xi_1 \Join_C \xi_2$	$\Gamma_{\bowtie}(\boldsymbol{c}(\xi_1), \boldsymbol{c}(\xi_2)) \times \lambda_{\bowtie}(C)$
$\xi_1-\xi_2$	$arGamma(oldsymbol{c}(\xi_1),oldsymbol{c}(\xi_2))$
$\xi_1\cup\xi_2$	$arGamma_\cup(oldsymbol{c}(\xi_1),oldsymbol{c}(\xi_2))$
$\pi_Y(\xi')$	$oldsymbol{c}(\xi')$
$gpBy(\xi', X, \overline{rmagg(V)})$	$\Gamma_{ m gpBy}(oldsymbol{c}(\xi'),\lambda_{\pi}(X))$
$\operatorname{fetch}(\xi',\varphi) \text{with } \varphi = R(X \to Y, N)$	$arGamma_{ ext{fetch}}(oldsymbol{c}(\xi'),N)$

By parameterizing these user configurable functions, we can support various measures for bLAPs. For example, to estimate the worst-case output size of ξ , we simply set (i) $\Gamma_{\bowtie}(c_1, c_2)$ to $c_1 * c_2$, (ii) $\Gamma_{\text{fetch}}(c', N)$ to $c' \times N$, (iii) $\Gamma_{\cup}(c_1, c_2)$ to $c_1 + c_2$, (iv) $\Gamma_{-}(c_1, c_2)$ to c_1 , and (v) $\Gamma_{\text{gpBy}}(c', c)$ to c' if $c \neq 0$ and to 1 otherwise (assume $\lambda_{\pi}(X) = 0$ when $X = \emptyset$).

Algorithm BAP. Algorithm BAP works in two steps:

(1) it reduces bLAPs to proofs of $R \in BR(Q, \mathcal{B})$ and encodes all proofs with a directed graph $\mathcal{G}(Q, \mathcal{B})$ in PTIME; and

(2) it searches $\mathcal{G}(Q, \mathcal{B})$ to find proofs with minimum cost, where a proof corresponds to a subgraph in the search trace.

Here a proof of $R \in BR(Q, \mathcal{B})$ is a sequence of applications of the rules given in Fig.1. Each step of the proof

⁴Following query optimizer in DBMS, $\lambda_{\sigma}(C)$, $\lambda_{\bowtie}(C)$, $\lambda_{\pi}(X)$ are coefficients that can be estimated from database statistics as a priori.

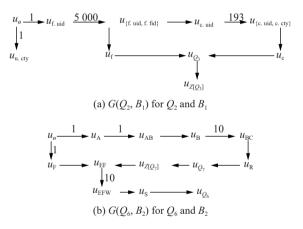
corresponds to one or several operations in a bLAP ξ_R for R.

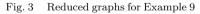
Below we outline BAP (see Appendix for its pseudo code).

(1) Reduction. It reduces the problem of generating bLAPs for R of Q under \mathcal{B} to finding proofs of $R \in BR(Q, \mathcal{B})$. It encodes all proofs of $R \in BR(Q, \mathcal{B})$ (hence all bLAPs for R) in a weighted directed graph $\mathcal{G}(Q, \mathcal{B})$, where nodes encode (a) attributes R[X] and R[XY] in constraints $R(|X \to Y, N|) \in \mathcal{B}$, and (b) relations and sub-queries of Q. Edges encode value propagation among them. It ensures that each proof of $R \in BR(Q, \mathcal{B})$ is encoded by a traversal from a dummy node u_{\emptyset} to node u_R encoding R in $G(Q, \mathcal{B})$. Graph $G(Q, \mathcal{B})$ has at most 2||B|| + |Q| nodes and ||B||(||B|| + |Q|) edges.

We illustrate reduced graphs with the following example, and defer the construction details to Appendix.

Example 9. Recall RA_{aggr} queries Q_2 of Example 2 and Q_6 of Example 5, and bag access schemas \mathcal{B}_1 and \mathcal{B}_2 from Example 4. Graphs $G(Q_2, \mathcal{B}_1)$ and $G(Q_6, \mathcal{B}_2)$ are shown in Fig.3. Here u_{\emptyset} is a dummy node connected to all constant attributes in Q. Edges with numeric weights are to encode deduction steps with rule γ_3 of Fig.1, where the weights are the cardinality N's of the corresponding access constraints.





As will be show below, proofs of a relation $R \in BR(Q, \mathcal{B})$ can be encoded as traversals from u_{\emptyset} to u_R in $G(Q, \mathcal{B})$.

(2) Conditional Dijkstra search. Algorithm BAP then adopts a Dijkstra-like search over $G(Q, \mathcal{B})$, from the dummy node u_{\emptyset} to the relation node u_R encoding R, such that the trace of the search encodes a bLAP (i.e., proof) for R under \mathcal{B} .

It extends Dijkstra algorithm^[24] as follows.

(a) Conditional expansion. Denote by U_u the attribute, relation or sub-query encoded by a node u in $G(Q, \mathcal{B})$. Note that U_u may be deduced from attributes or

sub-queries encoded by multiple predecessors of u as preconditions in the proof of $R \in BR(Q, \mathcal{B})$. To capture this, BAP visits a new node u under the condition that U_u can be obtained from predecessors of u via, e.g., joins or fetch.

With the condition, BAP ensures that for node u encoding relation $R \in BR(Q, \mathcal{B})$, a traversal in $G(Q, \mathcal{B})$ from u_{\emptyset} to u encodes a bLAP for relation atom R in query Q under \mathcal{B} . To illustrate this, let us consider Example 10.

Example 10. A proof of $f \in BR(Q_2, \mathcal{B}_1)$ (here f denotes friend) consists of the deduction steps (1), (2) and (4) in Example 7. It is encoded by the unique path from u_{\emptyset} to u_f in $G(Q_2, \mathcal{B}_1)$; similarly for the proof of $c \in BR(Q_2, \mathcal{B}_1)$.

A more informative example is $S \in BR(Q_6, \mathcal{B}_2)$. Its proof is also described in Example 7. The proof is encoded by the traversal from u_{\emptyset} to u_S , which is $G(Q_6, \mathcal{B}_2)$ without the edge (u_s, u_{Q_6}) as shown in Fig.3. Note that although there are two simple paths from u_{\emptyset} to u_S , none of them is a valid traversal because of the conditional expansion.

The bLAPs encoded by these proofs are exactly subplans of Q_2 and Q_6 given in Example 5. Indeed, the bLAP ξ_c for relation c of Q_2 under \mathcal{B}_1 is (T_1, T_2) of the bounded plan ξ_{Q_2} in Example 5, and the bLAP ξ_f for f is simply T_1 . Similarly, the bLAP ξ_R for R of Q_6 under \mathcal{B}_2 is simply T_1 of ξ_{Q_4} in Example 5; and bLAP ξ_S for S is (T_1, T_2, T_3) of ξ_{Q_4} .

Note that a bLAP may involve multiple relations via fetch and join, e.g., ξ_S for S of Q_6 . Hence its costs cannot be assessed by traditional access path measures since those methods are developed for evaluating the access method of a single relation via, e.g., sequential or index scan.

(b) Search revision. Note that the output of an RA_{ag-gr} sub-query can be used to fetch attributes that have already been deduced, possibly with a smaller cost reduced by $\mathbf{c}(\xi_R)$. To retain the optimality of the search, when visiting a node u that encodes a sub-query of Q, algorithm BAP checks whether this yields a better bLAP by starting a new search from u and marking all nodes as unvisited. It terminates if it cannot further improve the previously searched bLAPs.

Example 11. Continuing with Example 9, assume that we use $c(\xi_R)$ to express the worst-case output size of ξ_R (recall its parameter functions described earlier). Then BAP computes exactly the bLAPs for Q_2 and Q_6 under \mathcal{B}_1 and \mathcal{B}_2 , respectively, as described in Example 10. In particular, $c(\xi_f) = 5\ 000$ and $c(\xi_c) = 5\ 000 \times 193$ for Q_2 under \mathcal{B}_1 ; $c(\xi_R) = 10$ and $c(\xi_S) = 10$ for Q_6 under \mathcal{B}_2 . In this case, when computing ξ_S for relation S of Q_6 under \mathcal{B}_2 , it restarts the search once due to the aggregate subquery Q_7 , which does not improve the bLAPs ξ_R and ξ_S .

Correctness & Complexity. The correctness of algorithm BAP is warranted by the following: (1) each search trace of BAP encodes a proof of $R \in BR(Q, \mathcal{B})$; and (2) a proof of $R \in BR(Q, \mathcal{B})$ encodes a bLAP for Runder \mathcal{B} . BAP can be implemented in $O(|Q||\mathcal{B}|(||\mathcal{B}|| + |Q|\log(|Q| + 2||\mathcal{B}||)))$ -time (ignoring the complexity of parameter functions of $c(\xi_R)$). One can verify that BAP restarts at most N times, where N is the number of nodes in $G(Q, \mathcal{B})$.

Optimality. Algorithm BAP is able to find optimal bLAPs for a large class of parameter functions for $c(\xi_R)$. We defer detailed proofs of this optimality to Appendix.

6 Experimental study

We have developed BEAS@PG by extending PostgreSQL with bounded evaluation. Using a benchmark and two real-life datasets, we conducted four sets of experiments to evaluate (1) the overall performance of BEAS@PG vs PostgreSQL; and the effectiveness of bounded evaluation for (2) bounded queries and (3) unbounded queries.

Experimental setting. We start with the setting.

<u>Bench mark</u>. We used TPCH benchmark^[15]. It uses TPCHdbgen to generate 8 relations with 61 attributes of different scales. It contains 22 built-in benchmark queries.

<u>Real-life datasets</u>. We also used two real-life datasets.

(a) US Air carriers (AIRCA) records flight and statistic data of US air carriers. It consists of Flight On-Time Performance Data^[25] for departure and arrival information, and Carrier Statistic data^[26] for airline market and segment data of the air carriers. It has 3 tables, 200 attributes, and about 16 GB of data with records from 1990 to 1997.

(b) UK MOT data (UKMOT) integrates the anonymised data^[27] that records MOT tests and outcomes, and the roadside survey of vehicle observations^[28] that includes vehicles passing observation points in the UK. It has 3 tables with 42 attributes, about 16 GB of data from 2007 to 2011.

<u>Queries</u>. To test the impact of query structures on the effectiveness of bounded evaluation, we designed a generator to generate queries with different structures over the two real-life datasets. More specifically, we manually created 30 query templates for each of the two datasets (Q1–Q15 are bounded) evaluable and Q16–Q30 are unbounded), with 0 to 4 joins. The generator populates these templates by randomly instantiating parameters in the templates with values from the datasets, yielding 150 queries for each real-life dataset.

<u>Access schema</u>. We built access schemas with 59, 18 and 14 access constraints over TPCH, AIRCA and UK-MOT, respectively. We extended TANE^[29], an algorithm for discovering functional dependencies, to first find candidate constraints $\varphi = R(X \to Y, N)$ on small sample datasets of 100 MB, and ranked them by their cardinalities N's. We then checked whether their N's are insensitive to the size of datasets D, by varying the size of D, e.g., 200 MB and 500 MB. We picked those access constraints with small and size-insensitive N's, such that the total size of the indices is at most 3 times of the size of its D.

<u>Configuration</u>. For DBMS, we used PostgreSQL 9.6 with all optimization enabled (BEAS@PG is built with PostgreSQL 9.6). In favor of PostgreSQL, besides indices for access constraints, we also built the following extra indices for PostgreSQL: (1) for each access constraint $R(X \to Y, N)$, we built a B-tree index on attributes X over R as well; (2) we built all primary key and foreign key indices; and (3) we also built B-tree on numerical attributes. Note that these were only for PostgreSQL, not built for BEAS@PG. We set the cost measure parameters of BEAS@PG as the worst-case output size estimation (recall Section 5.3).

The experiments were conducted on an Amazon EC2 Dense-storage instance m4.xlarge, with 16 GB of memory, 4 Intel Xeon E5-2676 vCPUs, and 500 GB of EBS SSD storage. Both the plan generation time and the execution time of the generated plans are included in evaluation time. All the experiments were run 3 times. The average is reported here.

Experimental results. We next report our findings.

Exp-1: Overall performance. We first report the evaluation time of 22 TPCH queries over 16 GB of TPCH data, and the 60 query templates over the entire AIRCA and UKMOT datasets, where evaluation time of a query template is the average of the evaluation time of its 5 instantiated queries.

(1) Index size. The indices of all the access constraints over TPCH, AIRCA and UKMOT account for 2.98, 0.01 and 0.25 times of the size of the datasets, respectively; the additional indices built only for PostgreSQL (in favor of the conventional DBMS) are of size 2.21, 0.87 and 1.5 times of that of TPCH, AIRCA and UKMOT, respectively.

<u>(2)</u> Query overview. None of the TPCH queries is boundedly evaluable under the access constraints selected. This is because the TPCH data generator scales cardinalities N's of almost all candidate access constraints $R(X \to Y, N)$ due to its simple scaling up strategy. This rules out most of the candidate constraints when we scale up to larger datasets while using a fixed threshold for N. For the 60 query templates over AIRCA and UKMOT, 30 of them are boundedly evaluable under the access constraints used, 15 for each dataset. Note that one could build more access constraints to allow more bounded queries. We will evaluate the performance of BEAS@PG for bounded and unbounded queries in more details in Exp-2 and Exp-3, respectively.

(3) Performance. The results for TPCH, AIRCA and UKMOT are reported in Tables 3–5, respectively.

(a) BEAS@PG outperforms PostgreSQL on each and every query on all the three datasets, when all indices are enabled for PostgreSQL. It is 1.11×10^4 times faster on average.

(b) Even though all TPCH queries are unbounded, over 16 GB of TPCH data, BEAS@PG is up to 40.46 times faster than PostgreSQL, and is on average 7.32 times faster. For unbounded queries over AIRCA and UKMOT, BEAS@PG is on average 1.32×10^3 and 4.61×10^3 times faster than PostgreSQL, respectively, up to 1.48×10^4 and 6.10×10^4 times.

(c) For bounded queries, BEAS@PG is 1.79×10^4 and 3.66×10^4 times faster than PostgreSQL on AIRCA and UKMOT, respectively, up to 3.44×10^4 and 2.52×10^5 times.

The results show that with a modest number (and size) of access constraints, BEAS@PG can speed up PostgreSQL on both bounded queries and unbounded queries, when all relevant indices are enabled for PostgreSQL, including those of access constraints and additional indices tailored for PostgreSQL. This verifies the effectiveness of bounded evaluation for generic queries, bounded or not, while the speedup is much larger for bounded queries, as expected.

Below we report more in-depth evaluation results for BEAS@PG versus PostgreSQL (with additional indices) for bounded queries (Exp-2) and unbounded queries (Exp-3).

Exp-2: Effectiveness for bounded queries. We next evaluated the impact of datasets D and queries Q on the evaluation time of BEAS@PG and PostgreSQL (with indices enabled), when queries Q are boundedly evaluable.

<u>Varying |D|</u>. To evaluate the impact of |D|, we partitioned AIRCA and UKMOT datasets by their date attributes (year and month), yielding subsets of sizes from 1GB to 16GB, consistent with how we scale up TPCH datasets when testing unbounded queries below in Exp-3. We did not use TPCH here since it has no boundedly evaluable queries.

As shown in Figs. 4(a) and 4(b), (a) the evaluation time of BEAS@PG is indifferent to the size of D, as expected for boundedly evaluable queries. (b) Bounded query plans work well with large D. Indeed, BEAS@PG took less than 11.67 ms and 3.94×10^2 ms for all queries over all subsets of AIRCA and UKMOT, respectively, no matter how large the datasets were. In contrast, even on the subsets of AIRCA and UKMOT of size 8 GB, PostgreSQL took 8.45×10^4 ms and 3.88×10^5 ms, respectively, up to 1.58×10^5 ms and 7.80×10^5 ms over the full datasets. That is, PostgreSQL is 1.35×10^4 and 1.98×10^3 slower than BEAS@PG on AIRCA and UKMOT, respectively, even with all relevant indices built. The larger the dataset is, the bigger the gap between PostgreSQL and BEAS@PG is for bounded queries.

<u>Varying Q</u>. To evaluate the impact of queries Q, we varied the complexity of Q, measured as the number #Q of joins in the query templates Q, from 0 to 4, while using the entire AIRCA and UKMOT datasets. Note that for each query template, we instantiated 5 queries by set-

Table 3 TPCH query evaluation time on 16 GB (ms)

Queries	Q1	Q2	Q3	Q4	Q 5	Q6	Q7	Q8	Q9	Q10	Q11
PostgreSQL $t_{\rm P}$	$8.16 imes10^5$	$3.68 imes 10^4$	$1.02 imes 10^5$	$1.56 imes 10^4$	$1.50 imes 10^5$	$2.07 imes 10^4$	$9.53 imes10^4$	$3.71 imes 10^4$	$5.03 imes10^4$	$2.28 imes10^5$	$7.05 imes 10^4$
BEAS@PG $t_{\rm B}$	$5.72 imes 10^4$	$1.67 imes 10^4$	$2.97 imes 10^4$	$1.45 imes 10^4$	$1.43 imes 10^5$	$4.25 imes 10^3$	$7.65 imes 10^4$	$3.43 imes10^4$	$3.24 imes 10^4$	$8.19 imes10^4$	$3.46 imes10^3$
Speedup $t_{\rm P}/t_{\rm B}$	14.28	2.21	3.44	1.07	1.05	4.88	1.24	1.08	1.55	2.79	20.39
Queries	Q12	Q13	Q14	Q15	Q16	Q17	Q18	Q19	Q20	Q21	Q22
$\textbf{PostgreSQL} \ t_{\rm P}$	$6.42 imes 10^4$	$1.79 imes 10^5$	$1.74 imes 10^4$	$5.10 imes10^4$	$4.46 imes 10^4$	$6.04 imes10^3$	$2.83 imes10^5$	$7.27 imes 10^3$	$1.06 imes 10^5$	$2.66 imes10^5$	$7.74 imes10^3$
BEAS@PG $t_{\rm B}$	$8.58 imes10^3$	$1.20 imes 10^5$	$1.10 imes 10^4$	$2.20 imes 10^4$	$3.02 imes 10^4$	$1.49 imes 10^2$	$2.38 imes10^5$	$1.29 imes10^3$	$2.70 imes 10^3$	$1.04 imes 10^5$	$5.70 imes10^3$
${\bf Speedup} t_{\rm P}/t_{\rm B}$	7.48	1.49	1.58	2.32	1.48	40.46	1.19	5.65	39.16	2.55	1.36

Table 4	Average query template evaluation time on AIRCA ((ms)
T able 4	Average query template evaluation time on AntoA	moj

Queries	Q1	Q2	Q3	Q4	Q 5	Q6	Q7	Q8	Q9	Q10
$\textbf{PostgreSQL}t_{\rm P}$	$7.00 imes10^3$	$7.2 imes10^3$	$2.06 imes10^4$	$9.04 imes10^4$	$4.44 imes 10^4$	$9.41 imes 10^4$	$1.36 imes10^5$	$1.44 imes 10^5$	$9.41 imes 10^4$	$1.38 imes10^5$
$\textbf{BEAS@PG} \ t_{\rm B}$	1.22	1.19	0.64	2.63	2.61	6.34	4.28	6.69	6.02	4.98
Speedup $t_{\rm P}/t_{\rm B}$	$5.75 imes 10^3$	$6.04 imes 10^3$	$3.21 imes 10^4$	$3.44 imes 10^4$	$1.70 imes 10^4$	$1.48 imes 10^4$	$3.19 imes10^4$	$2.15 imes 10^4$	$1.57 imes 10^4$	$2.77 imes 10^4$
Queries	Q11	Q12	Q13	Q14	Q15	Q16	Q17	Q18	Q19	Q20
$\textbf{PostgreSQL}t_{\rm P}$	$1.46 imes10^5$	$9.46 imes10^4$	$1.49 imes 10^5$	$1.56 imes10^5$	$10.63 imes 10^4$	$4.46 imes10^4$	$4.65 imes 10^4$	$4.22 imes 10^4$	$4.25 imes 10^4$	$9.29 imes 10^4$
BEAS@PG $t_{\rm B}$	7.24	11.42	6.55	8.5	11.67	24.96	24.3	2.84	$4.63 imes10^2$	$7.26 imes10^2$
${\bf Speedup} t_{\rm P}/t_{\rm B}$	$2.01 imes 10^4$	$8.29 imes10^3$	$2.29 imes10^4$	$1.84 imes 10^4$	$9.11 imes 10^3$	$1.79 imes10^3$	$1.91 imes 10^3$	$1.48 imes 10^4$	91.86	$1.29 imes 10^2$
Queries	Q21	Q22	Q23	Q24	Q25	Q26	Q27	Q28	Q29	Q30
PostgreSQL $t_{\rm P}$	$9.30 imes10^4$	$8.98 imes10^4$	$9.44 imes 10^4$	$9.41 imes 10^4$	$1.39 imes10^5$	$1.47 imes 10^5$	$9.58 imes10^4$	$1.75 imes 10^5$	$1.85 imes 10^5$	$1.31 imes 10^5$
BEAS@PG $t_{\rm B}$	$5.43 imes10^2$	$4.61 imes 10^2$	$7.25 imes 10^2$	$5.23 imes10^2$	$1.4 imes10^3$	$1.74 imes10^3$	$1.36 imes10^3$	$2.67 imes 10^4$	$3.06 imes10^4$	$2.62 imes 10^4$
${\bf Speedup}t_{\rm P}/t_{\rm B}$	$1.71 imes 10^2$	$1.94 imes 10^2$	$1.31 imes 10^2$	$1.80 imes 10^2$	99.52	84.49	70.35	6.54	6.06	5.02

ting its parameters with different values (hence these queries share the same query structure and #Q). The evaluation time of each query template is the average of all its instantiated queries.

The results are reported in Figs.4(c) and 4(d). We find the following. (a) The complexity of Q has impacts on the performance of both BEAS@PG and PostgreSQL, as expected. They both take longer time for queries with more joins (i.e., #Q). However, (b) BEAS@PG scales much better with the number #Q of joins in Q than PostgreSQL (with indices). For instance, on average BEAS@PG found answers for all queries with #Q = 4 within 11.67 ms on full-sized AIRCA, while PostgreSQL takes 1.56×10^5 ms; that is, PostgreSQL is 1.34×10^4 times slower than BEAS@PG for large queries.

<u>Remark</u>. We find that when queries Q incur joins on keys only, PostgreSQL with extra key/foreign key indices built is almost as fast as BEAS@PG (e.g., TPCH Q4). However, as long as Q involves non-key attributes, e.g., many of the AIRCA and UKMOT queries, PostgreSQL performs poorly on big tables, even provided with all indices. Indeed, on average BEAS@PG outperforms PostgreSQL by 8.98×10^3 times and 1.76×10^4 times for all bounded queries over all subsets of AIRCA and UK-MOT, respectively. The gap gets larger when the number of non-key attributes increases.

By looking into PostgreSQL's plan and its E_{XPLAIN} output, we find that this is partially due to the following reason. Given an access constraint $R(X \to Y, N)$, BEAS@PG fetches only distinct values of the relevant XY attributes, but PostgreSQL fetches entire tuples with irrelevant attributes of R, although those attributes are not needed for answering Q at all, no matter what indices are provided. This led to duplicated (X,Y) values when X is not a key, and the duplication got inflated rapidly by joins, e.g., E_{XPLAIN} output shows that PostgreSQL consistently accesses entire tables when there are non-key attributes.

Exp-3: Effectiveness for unbounded queries. In the same setting as in Exp-2, we evaluated the impact of D and Q on the performance of unbounded queries by BEAS@PG and PostgreSQL with indices enabled for PostgreSQL.

<u>Varying |D|</u>. The results on AIRCA, UKMOT and TPCH are in Fig. (4e), (4f) and (4g), respectively. Observe the following.

Table 5 Average query template evaluation time on UKMOT (ms)

Queries	Q1	Q2	Q3	Q4	Q5	Q 6	Q7	Q8	Q9	Q10
PostgreSQL $t_{ m P}$	$1.37 imes 10^5$	$6.47 imes 10^4$	$7.80 imes10^4$	$4.62 imes 10^5$	$4.65 imes 10^5$	$3.86 imes10^5$	$5.8 imes10^5$	$3.91 imes 10^5$	$5.72 imes 10^5$	$5.99 imes 10^5$
$\textbf{BEAS@PG}t_{\rm B}$	0.55	2.73	0.62	16.13	75.2	5.62	$1.50 imes 10^2$	$3.78 imes10^2$	54.79	$1.89 imes 10^2$
Speedup $t_{ m P}/t_{ m B}$	$2.52 imes 10^5$	$2.38 imes10^4$	$1.25 imes 10^5$	$2.86 imes10^4$	$6.18 imes10^3$	$6.88 imes 10^4$	$3.88 imes10^3$	$1.04 imes10^3$	$1.04 imes 10^4$	$3.18 imes10^3$
Queries	Q11	Q12	Q13	Q14	Q15	Q16	Q17	Q18	Q19	Q20
PostgreSQL $t_{\rm P}$	$4.09 imes10^5$	$5.91 imes 10^5$	$7.80 imes10^5$	$5.91 imes10^5$	$7.74 imes10^5$	$1.61 imes 10^5$	$1.59 imes 10^5$	$1.53 imes10^5$	$3.97 imes10^5$	$3.93 imes10^5$
BEAS@PG $t_{\rm B}$	$3.89 imes10^2$	55.42	$1.89 imes10^2$	$3.94 imes10^2$	96.24	30.49	65.09	2.51	$7.4 imes10^3$	$7.41 imes 10^3$
Speedup $t_{ m P}/t_{ m B}$	$1.06 imes10^3$	$1.07 imes 10^4$	$4.13 imes10^3$	$1.49 imes 10^3$	$8.05 imes10^3$	$5.28 imes10^3$	$2.44 imes 10^3$	$6.10 imes10^4$	53.55	53.14
Queries	Q21	Q22	Q23	Q24	Q25	Q26	Q27	Q28	Q29	Q30
PostgreSQL $t_{\rm P}$	$3.93 imes10^5$	$6.01 imes10^5$	$3.94 imes10^5$	$5.98 imes10^5$	$6.26 imes10^5$	$4.13 imes 10^5$	$6.19 imes10^5$	$7.04 imes10^5$	$4.86 imes10^5$	$6.96 imes10^5$
BEAS@PG $t_{\rm B}$	$9.25 imes 10^3$	$7.51 imes 10^3$	$7.72 imes10^3$	$9.34 imes10^3$	$7.62 imes10^3$	$7.82 imes 10^3$	$7.38 imes10^3$	$6.42 imes 10^4$	$7.65 imes 10^4$	$6.26 imes10^4$
Speedup $t_{\rm P}/t_{\rm B}$	42.48	80.07	51.12	64.08	82.14	52.87	83.81	10.95	6.37	11.12

(a) BEAS@PG is able to speed up PostgreSQL even for queries that are not bounded under the available access constraints. On average, BEAS@PG is 7.22×10^2 , 2.29×10^3 and 3.43 times faster than PostgreSQL for unbounded queries on AIRCA, UKMOT and TPCH, respectively. This is because while not all relations in these queries are bounded, bounded evaluation can still speed up their "bounded" subqueries, and hence remains faster than PostgreSQL.

(b) As opposed to evaluating bounded queries, both BEAS@PG and PostgreSQL are sensitive to the size of the datasets when evaluating unbounded queries. However, BEAS@PG scales much better than PostgreSQL, and their performance gap becomes larger when the dataset size increases. For example, when the dataset increases from 1GB to 16GB, the average processing time of BEAS@PG increases from 9.53×10^2 ms, 1.67×10^3 ms and 2.21×10^3 ms to 6.09×10^3 ms, 1.84×10^4 ms and 4.54×10^4 ms on AIRCA, UKMOT and TPCH, respectively. In contrast, PostgreSQL increases from 7.50×10^3 ms, 2.61×10^4 ms and 5.98×10^3 ms to 1.04×10^5 ms, 4.53×10^5 ms and 1.23×10^5 ms, respectively, even with all indices built and enabled.

Note that the speedup for unbounded TPCH queries is not as good as for AIRCA and UKMOT queries. This is because (i) the N's of access constraints $R(X \to Y, N)$ over TPCH scale linearly as the dataset gets larger, while those on AIRCA and UKMOT are more stable and independent of the dataset size; and (ii) joins in TPCH queries are mostly key/foreign key joins, and thus the extra key indices built for PostgreSQL can mimic bounded query plans used by BEAS@PG to some extent, reducing their performance gaps.

<u>Varying Q</u>. Varying the number #Q of joins in the queries, the evaluation time of unbounded queries over

AIRCA and UKMOT is reported in Figs. (4h) and (4i), respectively. The results tell us the following. (a) The processing time of BEAS@PG and PostgreSQL increases when the number of joins increases. However, (b) the gap between BEAS@PG and PostgreSQL becomes larger when #Q increases from 0 to 4. For instance, over AIR-CA, on average BEAS@PG and PostgreSQL take 17.37 ms and 4.43×10^4 ms, respectively, to answer queries with #Q = 0; and the two take 2.78×10^4 ms and 1.64×10^5 ms, respectively, when #Q = 4; the results over UKMOT are similar. Note that for bounded queries, the gap between the two is even larger (Exp-2).

Summary. We find the following. (1) BEAS@PG (PostgreSQL with BEAS built on top) does better than PostgreSQL for each and every query in all cases, even with extra indices built for the latter. On average BEAS@PG improves PostgreSQL by 7.32, 9.58×10^3 and 2.06×10^4 times for TPCH benchmark of 16 GB, AIRCA and UKMOT, respectively, up to 40.46, 3.44×10^4 , and 2.52×10^5 times in the best case. (2) For queries that are boundedly evaluable, BEAS@PG outperforms PostgreSQL by 1.9×10^4 and 3.6×10^4 times on AIRCA and UKMOT, respectively. (3) For queries with complicated joins, e.g., joins on non-key attributes (AIRCA and UK-MOT queries), BEAS@PG is particularly effective, even for unbounded queries. For example, on average BEAS@PG improves PostgreSQL by 5.97×10^2 and 1.90×10^3 times for queries that are not boundedly evaluable over AIRCA and UKMOT, respectively. For cases where conventional DBMS does its best, e.g., table scan/aggregation and key-foreign key joins (most TPCH queries), BEAS@PG still does better than PostgreSQL. (4) The storage cost for indices of access schema is modest, accounting for 2.98, 0.01 and 0.25 times of the size of 16 GB TPCH, AIRCA and UKMOT, respectively.

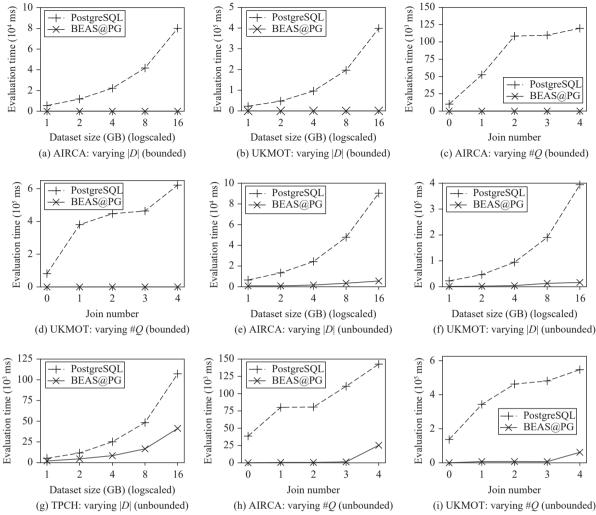


Fig. 4 Effectiveness of bounded evaluation for bounded and unbounded queries

7 Related work

The related work is categorized as follows.

<u>Bounded evaluation</u>. The notion of bounded evaluation was introduced in [5], as an effort to formalize scale independence^[19, 30, 31]. The latter aims to guarantee that a bounded amount of work is required to execute all queries in an application, regardless of the size of the underlying data. Under access schema proposed in [19], Fan et al.^[5] defines boundedly evaluable RA queries. It establishes the complexity of deciding whether a query is boundedly evaluable, for queries in various fragments of RA, ranging from EXPSPACE-hard to undecidable. Bounded evaluation using views was studied in [32], focusing on its complexity bounds.

To cope with the undecidability of the bounded evaluability problem, an effective syntax was given for RA in [6] under the set semantics. Based on the syntax, algorithms were developed^[6] for checking the bounded evaluability of RA queries Q, and if affirmative, generating a bounded query plan for Q. These issues were also studied in [33] for SPC, using a restricted form of query plans. Based on [6], a prototype BEAS for RA queries was developed^[34].

This work extends the prior work in the following. (1) We define bag access schema, an extension of access schema of [5, 19] to support the bag semantics (Section 2). (2) We identify decidable special cases of the bounded evaluability problem that cover a variety of SQL queries commonly used in practice. (3) We develop an effective syntax for boundedly evaluable RA_{aggr} queries under a bag access schema, supporting nested aggregations (Section 4). Moreover, the syntax allows us to make a larger class of RA queries bounded, improving the result of [6] for RA. (4) We extend BEAS^[34] from RA to RA_{aggr}, by seamlessly integrating bounded evaluation with DBMS query optimizers, which is quite different from [6, 34]. These extend DBMS with bounded evaluation, which was not studied in [5, 6, 33, 34].

<u>Query answering with constrained resources</u>. The objective of this work is to make big data analytics accessible to small companies under constrained resources. For queries that are not boundedly evaluable, an approach is to compute approximate answers under available resources. Approximation techniques have been extensively studied, based on synopsis (e.g.,[35–39]) or dynamic sampling (e.g.,[40–42]). We have proposed a data-driven approximation scheme^[17] that computes approximate answers $Q(\mathcal{D}_Q)$ to an RA_{aggr} query Q in a dataset \mathcal{D} , by identifying a fraction \mathcal{D}_Q of \mathcal{D} under an extension of the access schema of [5]. It ensures a deterministic accuracy bound η : (a) for each tuple $s \in Q(\mathcal{D}_Q)$, there exists an exact answer t that is within distance at most η from S, and (b) for each exact answer $t \in Q(\mathcal{D})$, there exists $s \in Q(\mathcal{D}_Q)$ within distance η from t.

This work differs from [17] in that we focus on computing exact answers instead of approximation. The techniques are hence quite different. In particular, a bag access schema carries the multiplicities of tuples to deal with the bag semantics, as opposed to distance bounds in access templates of [17]. This said, this work and [17] are complementary to each other. On one hand, the methods of [17] can be used to compute approximate answers to unbounded queries under constrained resources. On the other hand, the techniques developed in this work can be incorporated into the methods of [17], to improve the accuracy of approximate answers by making use of DBMS optimizers and bounded sub-plans.

<u>Indices</u>. Hash-based or tree-based, DBMS indices are typically defined at the tuple level^[11], to retrieve tuple IDs and fetch full tuples. In contrast, a bag constraint $R(X \to Y, N)$ offers a value-based index. Bounded plans fetch distinct partial tuples (Y-values) for each input Xvalue, and thus reduce duplicated and unnecessary attributes in tuples fetched by DBMS, i.e., reduce data access and intermediate relations. The redundancies get inflated rapidly with joins. Moreover, the cardinality constraints in a bag access schema allow us to determine whether data access is bounded.

Related to bag access schema is a notion of access patterns, which require a relation to be accessed only by providing certain combinations of attributes, e.g., [43–45]. As opposed to access patterns, a bag access schema offers cardinality constraints, tuple multiplicity and indices. Moreover, it is not required to cover all the attributes of a relation and hence, allows us to fetch partial tuples and reduce redundancy. Further, this work studies bounded evaluation of RA_{aggr} queries and its integration with DBMS, which were not considered in the prior work on query answering under access patterns.

<u>Query optimization</u>. There has been a host of work on query optimization in DBMS, including access path selection^[46], join optimization^[47, 48] and recently, machine leaning methods^[49–51]. These focus on access path cost models for, e.g., main-memory concurrent systems^[46], heuristics for join^[47] and group-by^[48] re-ordering, learned indices^[50, 51] or optimizers^[49, 52–54]. Our algorithms and techniques are complementary to the prior work, to incorporate bounded evaluation into DBMS query optimization.

8 Conclusions

We have presented an approach to extending DBMS with bounded evaluation of SQL queries. The novelty of the work consists of (a) a notion of bag access schema to support the bag semantics of nested aggregations; (b) decidable special cases of the bounded evaluability of RA_{aggr} queries; (c) an effective syntax to characterize boundedly evaluable RA_{aggr} queries; and (d) a framework and its underlying algorithms for integrating bounded evaluation with DBMS. Our experimental study has verified that the approach is promising. Together with the approximation scheme of [17], we hope that this work provides small businesses with a capacity for querying big data under constrained resources.

One topic for future work is to develop algorithms for discovering bag access schemas by incorporating machine learning techniques. Another topic is to extend bounded evaluation of SQL queries to column-oriented DBMS.

Appendix

Bounded plans under \mathcal{B} (Section 2)

The set $\Xi_{\mathcal{B}}$ of bounded query plans under a bag access scheme \mathcal{B} is inductively defined in Fig.5.

♦ {	c} and \emptyset are in $\Xi_{\mathcal{B}}$, where c is a constant;
	ξ' is in $\Xi_{\mathcal{B}}$ and has output attributes $X, \ \psi = R(X \to Y, N) \in \mathcal{B},$
	nen $(\xi', fetch(\xi', \psi))$ is in $\Xi_{\mathcal{B}};$
	ξ' is in $\Xi_{\mathcal{B}}$, then $\sigma_C(\xi')$ and $\pi_Y(\xi')$ are in $\Xi_{\mathcal{B}}$;
♦ if	ξ_1 and ξ_2 are in $\Xi_{\mathcal{B}}$, then $\xi_1 \times \xi_2(\xi_1 \bowtie_C \xi_2)$, and $\xi_1 \cup \xi_2, \xi_1 - \xi_2$
are	in $\Xi_{\mathcal{B}}$;
♦ if	ξ is in $\Xi_{\mathcal{B}}$, then $gpBy(\xi, X, \overline{agg(V)})$ is also in $\Xi_{\mathcal{B}}$.

Fig. 5 Bounded plans under \mathcal{B} (set $\Xi_{\mathcal{B}}$)

Details of Algorithm BPlan (Section 5.3)

We provide (1) the construction of weighted directed graph $G(Q, \mathcal{B})$ for generating bLAPs, (2) algorithm BAP, and (3) justification for the optimality of bLAPs found by BAP.

Constructing $G(Q, \mathcal{B})$. Let V and E be the node set and edge set of $G(Q, \mathcal{B})$, respectively. They are constructed as follows: (1) for each access constraint $R(|X \to Y, N|) \in \mathcal{B}$, (a) include $u_{R[X]}$, $u_{R[XY]}$ in V, referred to as BA-node; (b) include $(u_{R[X]}, u_{R[XY]})$ in E, referred to as a fetch-edge; (2) for each relation S, include a node u_S in V, referred to as a BR-node; (3) for each subquery Q_s of Q, include u_{Q_s} in V as a BQ-node and $v_{Z[Q_s]}$ in V as a BA-node, where $Z[Q_s]$ includes the output attributes of Q_s ; (4) for each constant attribute A = c in Q, there is a BA-node u_A in V, and an additional node u_{\emptyset} ; (5) for any two BA-nodes u_X and u_Y , if u_X (resp. u_Y) is not the head (resp. tail) of a fetch-edge, then (u_X, u_Y) is an edge in E if there exist $A \in X$ and $B \in Y$ such that $\Sigma_Q \vdash A = B$; (6) (u_{\emptyset}, u_A) is an edge in E for every constant attribute A in Q; (7) for any BA-node u_X and BRnode u_R , if u_X is the tail of a fetch edge and X contains all nontrivial attributes of R, then (u_X, u_R) is an edge in E; and (8) for any BR-node u_R and BQ-node u_{Q_s} , (u_R, u_{Q_s}) is an edge in E if R is a relation of Q_s .

In graph $G(Q, \mathcal{B})$, fetch-edges carry cardinality N's in their encoded access constraints $R(|X \to Y, N|) \in \mathcal{B}$ as their weights; each edge (u_{\emptyset}, u_A) for constant node u_A has weight 1; and the other edges have no weight. Graph $G(Q, \mathcal{B})$ has at most 2 ||B|| + |Q| nodes and ||B|| (||B|| + |Q|) edges.

Encoding proofs using $G(Q, \mathcal{B})$. Traversing a fetchedge $u_{R[X]}$, $u_{R[XY]}$) encodes fetch $h(\xi_{R[X]}, \varphi)$ for some $\varphi = R(|X \to Y, N|) \in \mathcal{B}$ that fetches values for Y, where ξ_X is the bLAP encoded by the traversal from u_{\emptyset} to $u_{R[X]}$, which retrieves values for R[X] necessary for answering Q; a traversal from a set S of BA-nodes u_{X_1}, \dots, u_{X_m} to a BA-node u_Y encodes a bLAP $\xi_Y = \pi_Y(\xi_{X_1} \bowtie \dots \bowtie \xi_{X_m})$ for Y, where $\xi_{X_i} (i \in [1, m])$ is the bLAP encoded by the traversal from u_{\emptyset} to u_{X_i} that retrieves values for X_i . Other cases are similar.

Algorithm 2. BAP

Input: RA_{aggr} query Q, bounded relation R of Q, bag access schema \mathcal{B} and cost function $\boldsymbol{c}()$. **Output:** A bLAP ξ_R for R under \mathcal{B} . 1 construct graph $G(Q, \mathcal{B})$; 2 $P_Q := \emptyset$; $S_{vt} := \emptyset$; $H := \emptyset$; $D_T[u_{\emptyset}] := 0$; $L_T[u_{\emptyset}] := \emptyset$; $GATE[u_{\emptyset}] := \emptyset;$ 3 for each u in $G(Q, \mathcal{B})$ do 4 if $u \neq u_{\emptyset}$ then $D_T[u] := +\infty;$ $L_T[u] := \emptyset;$ GATE[u] := L[u];5 P_Q .push (u_{\emptyset}) ; //Initialization 6 while: $P_Q \neq \emptyset$ do 7 $u := P_Q.pop(); //P_Q$ pops out u with minimum $D_T[u]$ in P_Q 8 $S_{vt} := S_{vt} \cup \{u\};$ 9 for each neighbor v of u that is not in S_{vt} do $GATE[v] := GATE[v] \setminus L[u];$ 10 11if (u, v) is a fetch-edge and $D_T[v] > \Gamma_{\text{fetch}}(D_T[u])$, w(u, v)) then 12 $P_Q.\operatorname{push}(v);$ 13 $D_T[v] := \Gamma_{\text{fetch}}(D_T[u], w(u, v)); L_T[v] := \{u\}$ 14else if v is a BR-node then 15 $P_Q.\text{push}(v), D_T[v] := D_T[u]; L_T[v] := \{u\}$ else if v is a BQ-node and $GATE[v] = \emptyset$ then 1617 P_Q .push(v); $D_T[v] := \boldsymbol{c}(\xi_v)$; $L_T[v]:=\operatorname{pre}(v) / \xi_v$ is the plan for Q encoded by v, composed from predecessors pre(v) of vfollowing the structure of Q

18 else if
$$GATE[v] = \emptyset$$
 then
//attributes X of v are joined from those of
 $pre(v) \cap S_{vt}$

- 19 $P_Q.\mathrm{push}(v);$
- 20 $(D_T[v], L_T[v], S_{vt}) := \mathrm{SC}(u, \mathrm{pre}(v) \cap S_{vt}, v);$ $d := \Gamma_{\bowtie}(L_T[v]);$
- 21 **if** $L_T[v]$ contains BQ-node u_q and $D_T[v]$ and $u_q \notin H$ **then**
- 22 $D_T[v] := d; S_{vt} := \{u_{\emptyset}, v\}; H := H \cup \{v\}//$ restart the search
- 23 **return** bLAP that is encoded by the traversal from u_{\emptyset} to u_R recorded in L_T [].

Algorithm BAP. BAP is given as Algorithm 2. It uses (a) GATE[u] to record the condition for visiting u, e.g., for the head u_X of a fetch-edge, GATE[u] = X; (b) L[u] to denote the attributes or relations u encoded; (c) $D_T[u]$ to denote the cost of the part of bLAP encoded by the search trace from u_{\emptyset} to u; (d) $L_T[u]$ to store the nodes to be visited before visiting u; (e) a priority queue P_Q for nodes to explore; and (f) sets S_{vt} of visited nodes and H of nodes triggered restarts.

Algorithm BAP starts the search from v_{\emptyset} . It first initializes data structures (lines 2–5). It then iteratively explores nodes in P_Q (lines 6–22). The search extends the Dijkstra search with conditional node expansion controlled by GATE[v] and types of the edges (lines 9–22), using c() to calculate the traversal cost. It restarts the search if the output of a sub-query is used as an input for a fetch (i.e., to visit the head of a fetch-edge; determined by SC given as Algorithm 3) with a reduced cost (lines 21–22). It returns bLAP encoded by the search trace if restarts cannot improve its cost (line 23).

Algorithm 3. SC

Input: visited vertex u and vertex set S_{vt} , and vertex v to be visited. **Output:** $D_T[v]$, $L_T[v]$ and updated S_{vt} . 1 if GATE[v] $\neq \emptyset$ then $D_T[v] := \lambda(D_T[u], w(u, v));$ $L_T[v] := \{u\};$ 2 return $D_T[v]$, $L_T[v]$, S_{vt} $3 W := L[v]; H_v := \emptyset;$ 4 while: $W \neq \emptyset$ do choose $u' \in S_{vt} \cap \operatorname{pre}(v)$ with minimum 5 $\frac{g_v(\{\mathbf{D}_{\mathbf{T}}[v'] \mid v' \in H_v \cup \{u'\}\})}{|W \cap L[u']|};$ 6 $W := W \setminus L[u']; H_v := H_v \cup \{u'\}$ 7 if (u, v) is a fetch-edge and $\lambda(D_T[u], w(u, v)) <$ $g_v(\{D_T[v'] \mid v' \in H_v)$ then 8 $D_T[v] := \lambda(D_T[u], w(u, v)); L_T[v] := \{u\}$ 9 else $D_T[v] := g_v(\{D_T[v'] | v' \in H_v); L_T[v] := H_v;$ 10 11 **if** H_v contains *q*-vertex **then** $S_{vt} := \{v\};$ 12 return $D_T[v], L_T[v], S_{vt}$;

Optimality of BAP. We say that cost $c(\xi_R)$ is regular if (a) all parameter functions are monotonically nondecreasing w.r.t. each of their arguments; and (b) Γ_{\bowtie} , Γ_{-} , Γ_{\cup} , Γ_{gpBy} and Γ_{fetch} are commutative and associative.

Denote $\max_{\varphi=R(|X\to Y,N|)\in\mathcal{B}}|Y|$ by $\#\mathcal{B}$, where |Y| is the

number of attributes in Y. Then we have the following.

Proposition 11. Under any access schema B, BAP finds optimal bLAPs with regular cost functions if $\#B \leq 1$.

Proof sketch. We discuss SPC Q first, followed by RA_{aggr}.

(1) Q is in SPC. We first prove the following lemmas.

(a) For each node $u \in S_{vt}$, $D_T[u]$ is the shortest distance from u_{\emptyset} to u; and for each unvisited node v, $D_T[v]$ is the shortest distance from u_{\emptyset} when traversing nodes in S_{vt} only.

(b) For each $u \in S_{vt}$, the plan encoded by the traversal from u_{\emptyset} to u is of cost $D_T[u]$ when c() is regular and $\#\mathcal{B} = 1$.

For if these hold, then when BAP terminates, the encoded plan from u_{\emptyset} to u_R is an LAP for R with minimum $\mathbf{c}()$.

Lemma (a) can be proved by induction on the number of nodes in S_{vt} , along the same line as Dijkstra's optimality proof, by observing that SC(v, S) always selects the subset $S_0 \subseteq S$ with minimum cost w.r.t. $\mathbf{c}()$ for visiting v when $\#\mathcal{B} = 1$. Lemma (b) can be verified by the same induction with (i) the observation that $D_T[u]$ mimics $\mathbf{c}()$ for the encoded bLAP from u_{\emptyset} to u, and (ii) the correspondence between proofs (traversals in $G(Q, \mathcal{B})$) and bLAPs under \mathcal{B} in the proof of Theorem 7 (part of the proof of Lemma (II)).

(2) Q is in RA_{aggr} . For RA_{aggr} queries, we show that BAP preserves the optimality of SPC with the following lemmas:

(c) Every sub-query Q_s of Q can improve searched LAP once.

(d) The order of sub-queries to restart does not change the final bLAP (up to equivalence).

Both lemmas are proved by induction on the number of -, \cup and gpBy operations in Q, using the condition that Γ_{\times} is associative and commutative and c() is monotonic.

One may expect BAP to find optimal bLAP for more cases while remaining in PTIME. This is, however, beyond reach.

Proposition 12. For each integer k > 1, it is NPhard to decide, given any bag access schema \mathcal{B} with #B = k, RA_{aggr} query $Q \in \mathcal{L}_{\mathcal{B}}$, relation atom R of Q and number R, whether there exists a bLAP ξ_R for R with cost $\mathbf{c}(\xi_R) \leq r$, even when $\mathbf{c}(\xi_R)$ is regular.

Proof. We show the NP-hardness by reduction from V_{ERTEX} C_{OVER} (VC), which is NP-complete^[1]. An instance of VC consists of a graph G(V, E) and an integer n. Given G and n (in binary form), VC is to decide whether there exists a subset $S \subseteq V$ such that (1) S covers G, i.e., for any edge $e \in E$, there exists $u \in S$ on e; and (2) $|S| \leq n$.

Given an instance $G(V = \{v_1, \dots, v_p\}, E = \{e_1, \dots, e_q\})$ and n of VC, we construct a database schema \mathcal{R} , a

bag access schema \mathcal{B} over \mathcal{R} with $\#\mathcal{B} = k$ ($k \geq 2$ is an integer), RA_{aggr} Q over \mathcal{R} , a bounded relation R_B in Q, a real number R, a regular cost function $\mathbf{c}()$ such that there exists a bLAP ξ for R_B under \mathcal{B} with $\mathbf{c}(\xi) \leq r$ if and only if G has a cover S with $|S| \leq n$. More specifically, the reduction is given as follows.

(1) Database schema \mathcal{R} consists of 3 relation schemas $R(A_0, A)$, $S(A_1, \dots, A_q, I)$, and $T(F_1, \dots, F_k)$. Here relation R is to encode the vertices of G, S is to represent edges of G, and T will be used to make \mathcal{B} with #B = k.

(2) Query Q is defined as follows:

 $\pi_{S[I]}(\sigma_{R_1[A_0]=1}(R_1) \bowtie \cdots \bowtie \sigma_{R_p[A_0]=p}(R_p) \bowtie S)$

where the join condition is $R_i[A] = S[A_j]$ if $v_i \in V$ is an end point of $e_j \in E$ in G. Here relation atom $R_i(i \in [1, p])$ is a renaming of relation schema R. Intuitively, the join condition encodes the edge relation of G, and $\pi_{S[I]}$ is to ensure that every attribute in S is nontrivial.

(3) The bag access schema ${\mathcal B}$ consists of 3 access constraints:

$$\begin{split} \varphi_R &= R\left(|A_0 \to A, 2|\right), \\ \varphi_S &= S\left(|\{A_1, \cdots, A_q\} \to I, 1|\right), \text{ and } \end{split}$$

 $\varphi_T = T\left(|\emptyset \to \{F_1, \cdots, F_k\}, 1| \right).$

Here φ_R is to fetch values of attribute R[A] (i.e., vertices of G), and φ_S is to fetch edges encoded by S[I] using $R[A_1, \dots, A_q]$ (i.e., edges of G). Note that $\#\mathcal{B} = k$.

(4) The bounded relation R_B is set to be R. One can easily verify that R is bounded under \mathcal{B} .

(5) We set $r = 2^n$. Note that this is in PTIME since n in the VC instance is in binary.

(6) Function $\boldsymbol{c}()$ is instantiated as follows: (i) $\Gamma_{\times}(\boldsymbol{c}(\xi_1), \boldsymbol{c}(\xi_2)) = c_1 \times c_2$ if $\xi_1 \neq \xi_2$ and is $\max(\boldsymbol{c}(\xi_1), \boldsymbol{c}(\xi_2))$ otherwise. (ii) $\Gamma_{\text{fetch}}(c, N) = c \times N$; and (iii) we simply set all other functions as constants. Note that $\boldsymbol{c}()$ is regular.

We show that G has a vertex cover S of size at most n if and only if R has a bLAP ξ with cost $c(\xi) \leq r$

⇒ Assume that G has a vertex cover S with $|S| \leq n$. We construct a bLAP ξ for R under \mathcal{B} as follows: $\xi = \text{fetch}(\bowtie_{i=1}^{q} \xi_{A_i}, \varphi_S)$, where $\xi_{A_i} = \text{fetch}(\{j\}, \varphi_R)$ if e_i is covered by $v_j \in S$ (when e_i is covered by multiple vertices in S, we pick one of them randomly). By the construction of Q and by that S covers all edges of G, ξ is a bLAP for S under \mathcal{B} . From $|S| \leq n$, we know that $\mathbf{c}(\xi) = \Gamma_{\times}(\bowtie_{i=1}^{q} \xi_{A_i}) \times 1 \leq 2^n = r$.

 $\Leftarrow \text{Assume that } R \text{ has a bLAP } \xi \text{ under } \mathcal{B} \text{ with cost} \\ c(\xi) \leq 2^n. \text{ By the join condition of } Q \text{ and } \varphi_S, \text{ there exist} \\ \text{at most } n \text{ distinct fetch operations for fetching } S[A_1], \cdots, \\ S[A_q], \text{ i.e., } S[A_1], \cdots, S[A_q] \text{ can be fetched from at most } n \\ \text{numbers } 1, 2, \cdots, p \text{ using } \varphi_R. \text{ This gives us a cover } S \text{ of } \\ G \text{ as follows: } S = \{v_i(i \in [1, p]) \mid \exists j \in [1, q], \xi_{A_j} = \text{fetch} \\ (\{i\}, \varphi_R)\}. \text{ By the construction of } Q, S \text{ is a cover of } G \\ \text{with } |S| \leq n.$

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