

Monte Carlo simulation of uncertainty to identify barriers to optimizing blood pressure control

Short title: Simulating uncertainty in hypertension

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Abstract

Objectives: To assess the impact of variable drug response and measurement error on systolic blood pressure (SBP) control.

Methods: We simulated a treat-to-target strategy for populations with different pre-treatment SBP, whereby medications were added sequentially until measured SBP (mSBP) <140mmHg. Monte Carlo simulations determined variability of both drug response ($\text{drug}_{\text{eff}} \pm \sigma_{\text{drug}}$; 10 ± 5 mmHg base case) and measurement error (σ_{meas} ; 10mmHg base case) of true SBP (tSBP). The primary outcome measure was the proportion of individuals who achieved target <140mmHg.

Results: Decision-making based on mSBP resulted in 35.0% of individuals with initial tSBP 150mmHg being either inappropriately given, or inappropriately denied a second drug. When the simulation was run for multiple drug titrations, measurement error limited tSBP control for all populations tested. A strategy of drug titration based on a second measurement for individuals at risk of incorrect decisions (mSBP 120-150mmHg; σ_{meas} 15mmHg) reduced the proportion above target from 40.1 to 30.0% when initial tSBP 160mmHg. When the measurement variability for the second reading was reduced below that usually seen in clinical practice (σ_{meas} 5mmHg), the proportion above target decreased further to 17.4%.

Conclusions: In this simulation, measurement error had the greatest impact on the proportion of individuals achieving their SBP target. Efforts to reduce this error through repeated-measures, alternative measurement techniques or changing thresholds, are promising strategies to reduce cardiovascular morbidity and mortality and should be investigated in clinical trials. Here we have shown that Monte-Carlo simulations are a useful technique to investigate the influence of uncertainty for different hypertension management strategies.

Keywords: Hypertension, Blood Pressure, Monte Carlo Method, Computer Models, Uncertainty, Antihypertensive Agents

Introduction

Current medical management of many common conditions involves initiating or changing treatment based on quantitative, semi-quantitative or qualitative thresholds of some measure of response to treatments. The values that define thresholds commonly represent either a surrogate outcome measure (e.g. blood pressure or spirometry) or elements of a diagnostic or symptomatic metric (e.g. inflammatory markers or a depression score). Typically, the focus is upon the average value of a measurements derived from a clinical encounter without attention on dispersion, yet variation or uncertainty in these values due to measurement error and/or physiological variation has the potential to result in erroneous decisions, with significant implications for efficient and effective healthcare delivery. As the evidence-base for personalised medicine increases, treatments and treatment thresholds are likely to be set according to characteristics of the individual and the impact of measurement error for an individual will increase [1].

Here we present an example of how measurement uncertainty impacts hypertension management, a particularly important example as hypertension is the major cause of death and disability worldwide [2, 3]. Hypertension is particularly amenable to a modeling approach for a number of reasons; (i) there is a strong association between the measured variable (blood pressure; BP) and clinical outcomes [4, 5], (ii) guidelines recommend the initiation of treatment based on a threshold BP and subsequent drug titration to achieve a target BP [6, 7], (iii) both drug response and measurement variability are well-described [8-12], and (iv) most individuals require treatment with two or more drugs, thus providing the potential for measurement error to be compounded [11]. Furthermore, whilst short-, medium- and long-term BP variability has been associated with adverse outcomes, it is unclear to what extent measurement error (and hence over- or undertreatment) may contribute [13].

There is an awareness among clinicians that measurement error can result in incorrect treatment decisions and that approaches to minimize error are important [14-16]. Previous studies have used probabilistic simulations to investigate how

measurement error can impact on the diagnosis of hypertension, with both inadequate device calibration and normal physiological variation contributing to misdiagnosis [17-19]. This study is the first simulation to investigate how measurement error impacts on achieving a blood pressure target for multiple drug titration steps and considers the impact of this on the proportion of individual achieving BP control.

Methods

We used a Monte Carlo simulation to investigate the impact of drug response and measurement variability on treatment outcomes for populations of hypertensive individuals. Monte Carlo simulations are powerful techniques based on mathematical models that describe the behavior of a system over time in response to stochastic (or random) variability of input parameters [20, 21]. Monte Carlo simulations are widely used in Astrophysics and other physical sciences where understanding the uncertainty arising from measurement error plays an important part in interpreting data[22, 23]

Key parameters in our model were the true systolic BP (tSBP; a hypothetical value made without measurement error or physiological variability) and measured SBP (mSBP) which is a value obtained by the observer and includes varying degrees of error. Each mSBP value represented the outcome of a clinical encounter, for example, the mean of multiple office BP readings or ambulatory blood pressure measurement. We focused on SBP due to its predictive validity with outcomes, and recent focus in major treat-to-target studies [3, 24-27].

Observed BP variation arises from the sum of measurement error and physiological variation (characterised by the standard deviation of repeated measurements over time, σ_{meas}), and by the variation in response to a drug (σ_{drug}). Total variance can therefore be described as follows:

$$\sigma_{\text{tot}}^2 = \sigma_{\text{meas}}^2 + \sigma_{\text{drug}}^2$$

Values for these parameters and the mean response to drug treatment (drug_{eff}) were extracted from published literature, with a range input into the simulation to explore

their effects [8-12]. Base case parameters were as follows: σ_{meas} 10 mmHg, drug_{eff} 10 mmHg and σ_{drug} 5 mmHg.

Populations entered the simulation with one of three pre-treatment (initial) tSBPs: 150, 160 or 170 mmHg. Individuals then all received a single drug with response $\text{drug}_{\text{eff}} \pm \sigma_{\text{drug}}$ and underwent BP measurement with variation σ_{meas} . Those with mSBP <140 mmHg then exited the simulation and received no further drugs, as to the observer they appeared to have achieved target. For those with mSBP ≥ 140 mmHg (irrespective of tSBP) they progressed to Step 2 and received another drug. This process of drug titration continued for each individual until their mSBP <140 mmHg. The number of steps for each individual represents the number of drugs received.

The statistical outputs from this simulation were descriptive and considered the proportion of individuals who achieved SBP target (<140 mmHg) according to UK guidelines [27]. Undertreated was defined as tSBP ≥ 140 mmHg, controlled as tSBP 120-139 mmHg, and overtreated as tSBP <120 mmHg.

Results

The typical expected distribution of tSBP and mSBP for our virtual population in response to a single antihypertensive titration is shown in **Figure 1**. In this example, for an initial tSBP 150 mmHg, the use of a drug with drug_{eff} 10 mmHg and σ_{drug} 5 mmHg results in a mean tSBP 140 mmHg. As drug effect is normally distributed in our simulation, the tSBP of the population will be evenly distributed. The mean of mSBP values obtained by an observer will also be 140mmHg and normally distributed. However, the range of mSBP values is much wider than that for tSBP, with approximately 4% appearing to be 'super responders' with mSBP <120 mmHg. In reality, <0.001% of the simulated population have tSBP <120 mmHg. The use of a single mSBP reading to determine response to a single drug titration resulted in 35.0% of the population either being inappropriately given, or inappropriately denied a second drug. Qualitatively similar results were found for other values of initial tSBP.

The relative effects of the input parameters on the proportion of individuals who appear to achieve target (mSBP <140 mmHg) are presented in **Figure 2**. Variation in drug_{eff} had the largest impact on this simulation with the effect greatest at higher initial tSBP. Where initial tSBP was 170 mmHg, mSBP <140 mmHg was achieved in <20% for three drugs when drug response was 5 ± 5 mmHg, compared to >90% when drug response was 15 ± 5 mmHg. Variation in measurement (σ_{meas}) had no effect on the maximal proportion achieving the mSBP target, since this error is not apparent to the observer. With multiple titration steps and at higher initial tSBP, we found an inverse relationship between measurement error and the proportion achieving mSBP <140 mmHg (**Table 1**).

The relative effects of the input parameters on the proportion of individuals who achieved target (tSBP <140 mmHg) are presented in **Figure 3**. Initial tSBP, measurement error and drug response all influenced the proportion of the population who would achieve target should the simulation be run *indefinitum*. Measurement error accounted for a difference of almost 30% (σ_{meas} 5 versus 15 mmHg) at initial tSBP 170 mmHg, compared to <10% at 150 mmHg. When measurement error was reduced to below that achieved in clinical practice (σ_{meas} 5 mmHg) the proportion who failed to achieve tSBP <140 mmHg remained high at approximately 30% for initial tSBP 170 mmHg. The proportion who failed to achieve control on three drugs is shown in **Table 1**.

Drug response influenced both the number of steps required to achieve tSBP <140 mmHg and the maximal proportion of the population who achieved the target. Where drug response was low (drug_{eff} 5 mmHg), for an initial tSBP 170 mmHg approximately 40% achieved target after nine steps (a hypothetical treatment outcome), compared to approximately 75% where drug response was high (drug_{eff} 15 mmHg) (**Figure 3**). Variation in drug response (σ_{drug}) also influenced the proportion reaching tSBP target but accounted for <10% difference for all populations.

Due to the impact of measurement error on achieving target tSBP we next considered how repeated sets of readings might mitigate this. In the first instance we simulated a second, independent measurement at each step when mSBP 120-150 mmHg. The second measurement in this '*at risk population*' was then used to determine the outcome (i.e. addition of another drug or exit simulation) for that individual. **Figure 4** shows that when the first and second measurements had the same error (σ_{meas} 15 mmHg) there was an increase in the proportion of individuals with controlled tSBP (49.9% versus 60.8% for initial tSBP 170 mmHg) and a decrease in individuals with tSBP ≥ 140 mmHg across the range of initial tSBP. When a method of SBP measurement with a lower measurement error was used for the second measurement (σ_{meas} 5 mmHg), the proportion of individuals with controlled tSBP increased further (78.0%) with a corresponding decrease in over- and undertreatment.

Discussion

The results of our simulations indicate that a large proportion of hypertensive individuals in whom SBP is thought to be at target following an initial drug titration, are in fact over- or undertreated. These individuals remain at either an increased risk of cardiovascular events or have an increased risk of side-effects from excessive medication. For example, in individuals with stage two hypertension <65% are controlled to within the target window (tSBP 120-139 mmHg) when clinically relevant base case parameters are input to the model.

The model enabled us to interrogate which parameters have the greatest influence on both the number of drugs required to achieve tSBP control, and the proportion of individuals in whom control is actually achieved. Several important findings have emerged. Firstly, the mean drug response (drug_{eff}) and/or standard deviation of this response (σ_{drug}) principally influences the number of titration steps required to achieve mSBP <140 mmHg, rather than define the upper limit. Where the number of titration steps are unlimited (a hypothetical scenario), all individuals will eventually achieve mSBP <140 mmHg. However, each titration step provides an opportunity for incorrect classification of SBP (mSBP <140 mmHg, despite tSBP ≥ 140 mmHg) and it is

for this reason that the proportion of individuals achieving target was lower when drug_{eff} was reduced.

Secondly, the variation in SBP measurement (σ_{meas}) had no effect on the maximal proportion achieving $\text{mSBP} < 140$ mmHg as the clinician is blinded to measurement error. However, a large effect was observed once tSBP values were analysed, with a lower proportion achieving $\text{tSBP} < 140$ mmHg at higher initial tSBPs . Again, this represents the number of titration steps and thus the number of opportunities for measurement error. In our simulation, it is measurement error that determines most of the misclassification where individuals are thought to be controlled based on mSBP , but tSBP lies outside of the target window.

Thirdly, the proportion of individuals misclassified can be reduced by an independent, second measurement when mSBP lies within a range that is 'at risk' from measurement error. The proportion misclassified was reduced further when the second measurement had lower variation than the first.

The composite of our analyses demonstrate that an individual is most likely to have their SBP misclassified if they have a high initial tSBP , receive drugs of low efficacy (or suboptimal adherence), and have titration decisions based on a single SBP measurement with high variability. The model allows consideration of remedial measures to reduce the number of subjects misclassified. Options to reduce measurement error include the use of single measurement events with increased precision, or repeated measurements that are averaged over longer periods (e.g. oscillometric home BP monitoring or the use of wearable technology). Such an approach could be applied selectively to individuals with measurements close to threshold values to reduce the measurement burden, or to those who exhibit high variability to improve accuracy. Interestingly, the simulation suggests that a small improvement in measurement error (10 versus 15 mmHg) will have negligible impact on misclassification, and that an error level not currently achieved with any clinical technique (5 mmHg) is required.

However even with an accuracy greater than that usually achieved in clinical practice, a substantial proportion of individuals will still be misclassified and receive suboptimal management. An alternative approach would be to recognise that as a high proportion of individuals are undertreated due to misclassification, the target window could be lowered to reduce this number. This would result in fewer individuals with uncontrolled BP but a larger number with relatively low BP. Whether a low BP might be associated with increased morbidity and/or mortality is uncertain and such a strategy would have to be formally tested in clinical trials. The challenge of balancing SBP targets with measurement method can be observed in the varying response by guideline committees to the results from the Systolic Blood Pressure Intervention Trial (SPRINT) [1, 6, 7, 26]. The SBP target selected for this simulation is consistent with UK primary prevention guidelines, but the findings are applicable to alternative targets and healthcare systems [27].

It is important to stress that the simulation exercise presented here is primarily for illustrative purposes since there are several assumptions and simplifications inherent to the model. The simulation is designed to investigate the number of treatment steps required to achieve mSBP <140 mmHg and so does not consider options for antihypertensive de-escalation as a response to either medication side-effects or overtreatment. The limited time horizon does not consider long-term SBP control. However, the proportion of individuals requiring three or more drugs to achieve mSBP <140 mmHg with clinically relevant parameters, corresponds to the prevalence of resistant hypertension both globally and in the UK [28, 29]. The main findings of this study would remain true if a more sophisticated simulation was used whereby drug response varied depending on SBP and the number of titrations [11].

The strength of the present simulation is that it allows the exploration of various management scenarios as a function of the burden of achieving more accurate measurements. Such an approach could inform the best strategies to be tested in clinical trials and provide more accurate data for health economic analyses. A full health economics analysis would require quantification of the relative burden of improving measurement precision and the risk related to poorly controlled

hypertension. Modern technology, such as a wearable wrist monitor, if sufficiently free from systematic bias, could potentially improve estimations of tSBP through the capacity to take high numbers of BP readings which would be sampled from the full range of potential measurement error. Such an approach would place little or no burden on patients or healthcare staff and could have a major impact on hypertension control.

Our approach to simulating uncertainty can also be applied to questions which have either not been fully addressed in clinical trials or for where there remains uncertainty in interpretation of the evidence. One prominent example is the use of initial dual antihypertensive therapy which is recommended by both European and US guidelines [6, 7]. In contrast, the recent UK guidelines were unable to recommend this approach due to a lack of cardiovascular outcome data [27]. By combining simulated tSBP data with a cardiovascular outcome model (in which benefit is proportion to SBP reduction [11]) it may be possible to add clarity to the issue. Furthermore, such an approach could be extended to situations which have not been addressed in cardiovascular outcome studies such as initial triple antihypertensive therapy, decision making based on repeated measures, combinations of half-dose/full-dose antihypertensives or novel polypill formulations.

In conclusion, Monte Carlo simulations have identified measurement error as the major determinant for individuals trying to achieve blood pressure control during initial medication titration. Strategies to reduce measurement error should be tested in pragmatic clinical trials.

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Tables

Table 1: The impact of measurement error (σ_{meas}) on achieving target blood pressure for individuals taking three antihypertensive medications.

	Initial tSBP 150 mmHg		Initial tSBP 160 mmHg		Initial tSBP 170 mmHg	
	mSBP ≥ 140 mmHg	tSBP ≥ 140 mmHg	mSBP ≥ 140 mmHg	tSBP ≥ 140 mmHg	mSBP ≥ 140 mmHg	tSBP ≥ 140 mmHg
5	1.2%	15.1%	13.2%	27.1%	48.3%	56.0%
10	1.8%	20.4%	13.3%	39.6%	42.2%	69.2%
15	2.8%	22.5%	13.0%	46.7%	35.4%	68.5%

Simulation parameters: drug_{eff} 10 mmHg; σ_{drug} 5 mmHg; σ_{meas} 5-15 mmHg.

[mSBP: measured systolic blood pressure; tSBP: true systolic blood pressure]

Captions for Figures

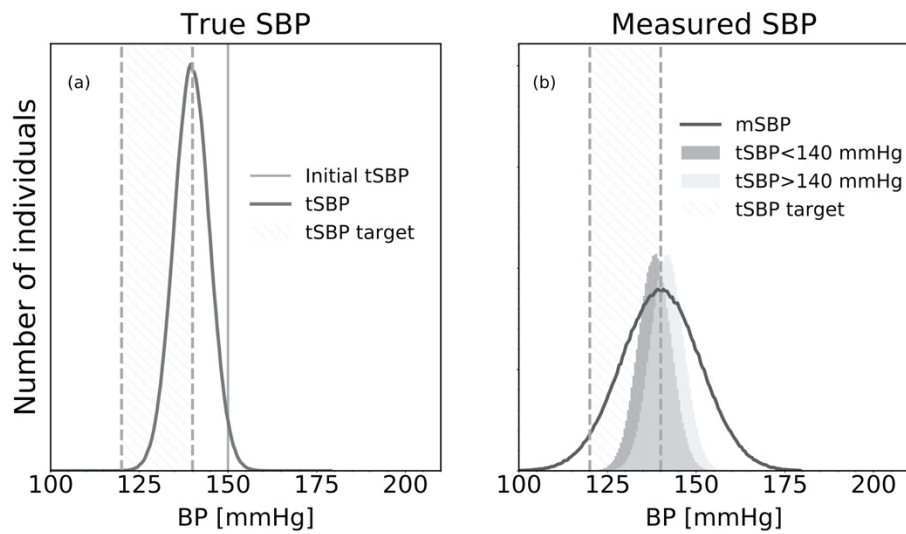


Figure 1: Distribution of (A) true systolic blood pressure (tSBP) and (B) measured systolic blood pressure (mSBP) after a single treatment step. Simulation conducted with an initial tSBP 150 mmHg, drug response ($\text{drug}_{\text{eff}} \pm \sigma_{\text{drug}}$) 10 ± 5 mmHg and standard deviation of measurement (σ_{meas}) 10 mmHg.

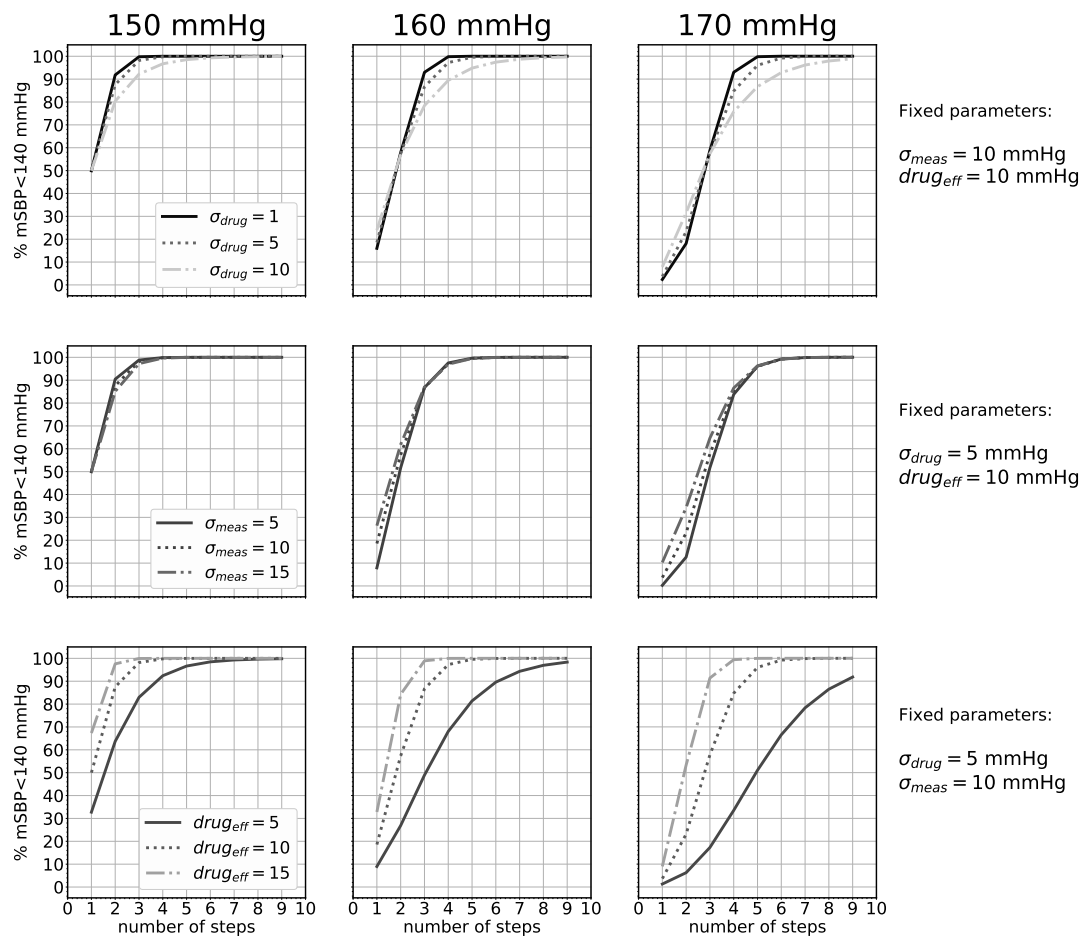


Figure 2: Proportion of individuals achieving a measured systolic blood pressure (mSBP) <140 mmHg with increasing drug titration.

Simulation inputs were varied based on initial true SBP (top of figure), drug response ($drug_{eff} \pm \sigma_{drug}$) and standard deviation of SBP measurement (σ_{meas}).

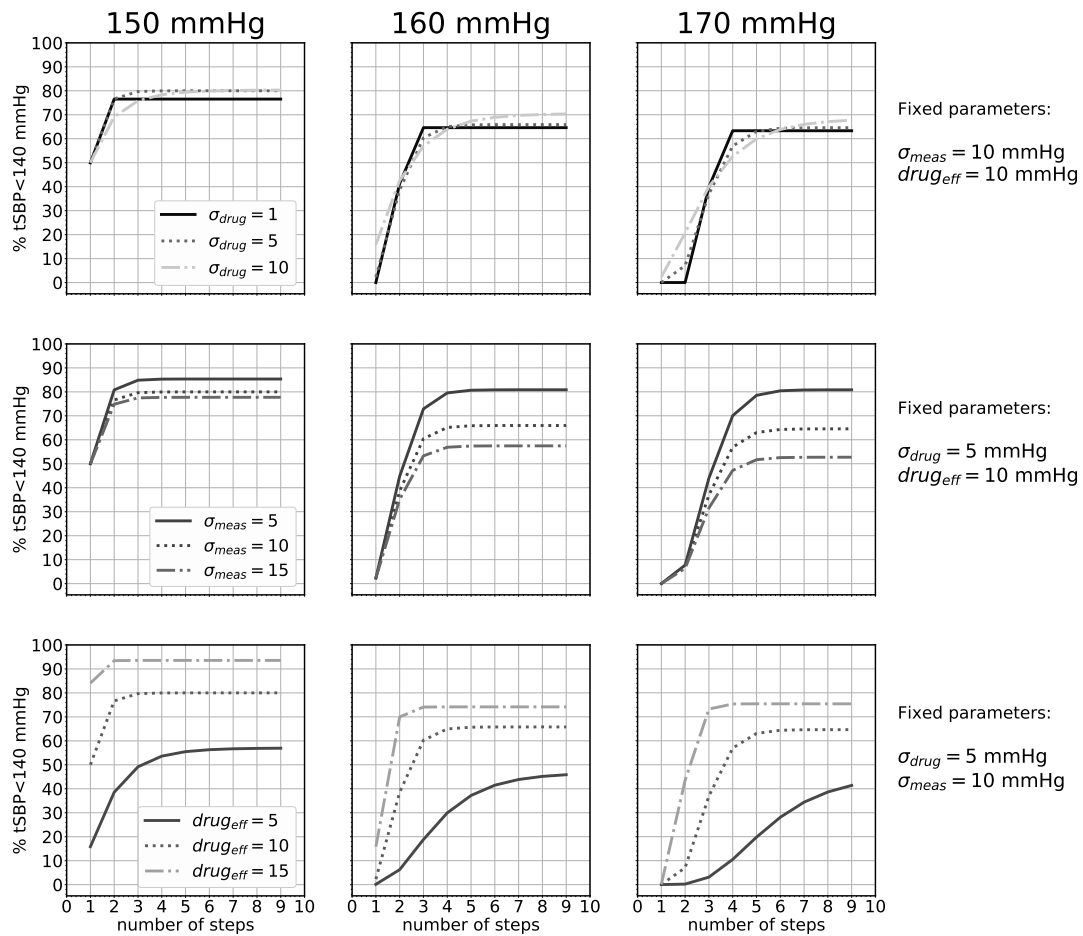


Figure 3: Proportion of individuals achieving a true systolic blood pressure (tSBP) <140 mmHg with increasing drug titration.

tSBP values calculated once mSBP <140 mmHg and subject had exited the simulation. Simulation inputs were varied based on initial t SBP (at top of figure), drug response ($drug_{eff} \pm \sigma_{drug}$) and standard deviation of SBP measurement (σ_{meas}).

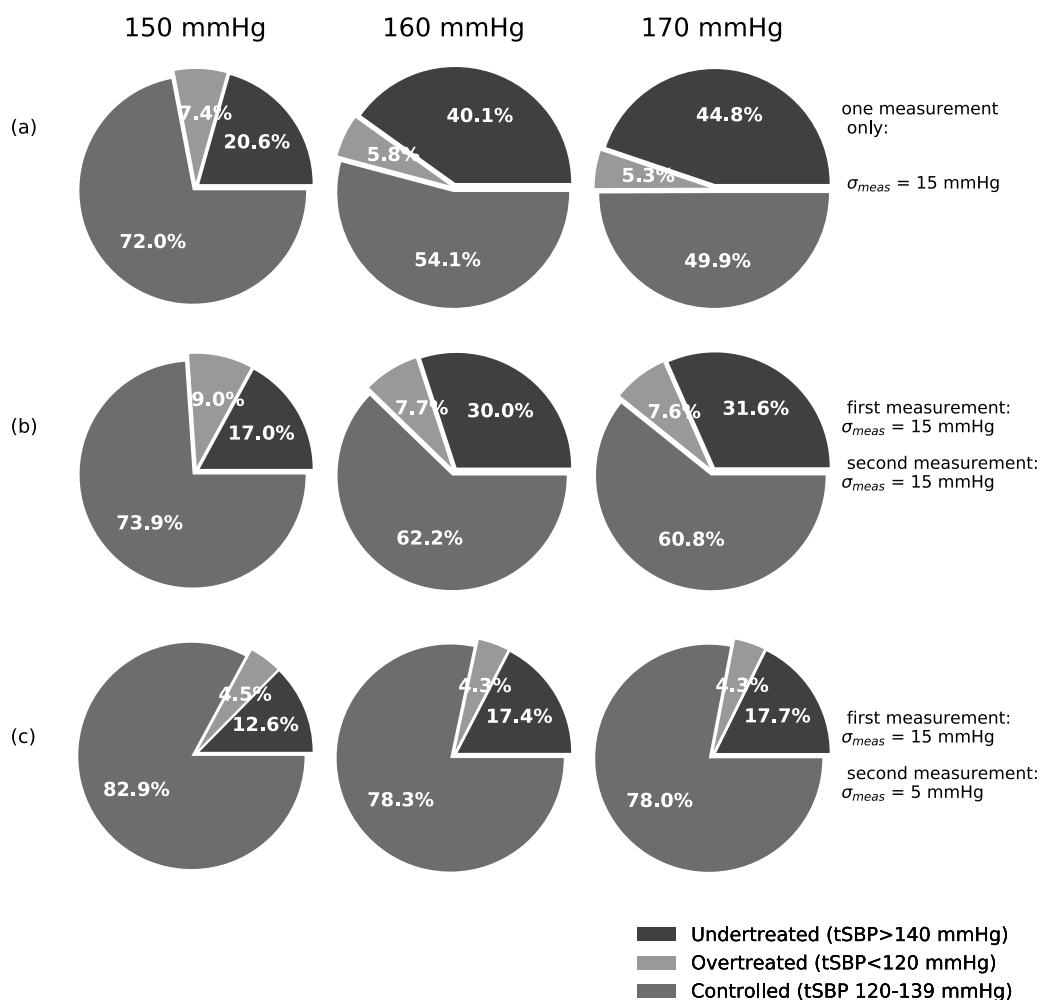


Figure 4: Classification of true systolic blood pressure (tSBP) for individuals exiting the simulation based on (A) single mSBP, (B) repeated measurement when first mSBP 120-150 mmHg, and (C) when second measurement is repeated with greater precision (σ_{meas} 5 mmHg) when first mSBP 120-150 mmHg. Analyses performed for different initial tSBP (top of figure). The response to each titration step was fixed at 10 ± 5 mmHg ($drug_{eff} \pm \sigma_{drug}$).