

1 Title: Attentional coordination in demonstrator-observer dyads facilitates learning and
2 predicts performance in a novel manual task

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8 Abstract:

9 Observational learning is a form of social learning in which a demonstrator performs
10 a target task in the company of an observer, who may as a consequence learn something
11 about it. In this study, we approach social learning in terms of the dynamics of coordination
12 rather than the more common perspective of transmission of information. We hypothesised
13 that observers must continuously adjust their visual attention relative to the demonstrator's
14 time-evolving behaviour to benefit from it. We eye-tracked observers repeatedly watching
15 videos showing a demonstrator solving three manipulative puzzles before attempting at the
16 task. The presence of the demonstrator's face and the availability of his verbal instruction in
17 the videos were manipulated. We then used recurrence quantification analysis to measure the
18 dynamics of coupling between the overt attention of the observers and the demonstrator's
19 manipulative actions. Bayesian regression was applied to examine whether the observers'
20 performance was predicted by such indexes of coordination, how performance changed as
21 they accumulated experience, and if the availability of speech and intentional gaze of the
22 demonstrator mediated it. Results showed that learners better able to coordinate their eye
23 movements with the manipulative actions of the demonstrator had an increasingly higher
24 probability of success in solving the task. The availability of speech was beneficial to
25 learning, whereas the presence of the demonstrator's face was not. We argue that focusing on
26 the dynamics of coordination between individuals may greatly improve understanding of the
27 cognitive processes underlying social learning.

28 Keywords: observational learning; attentional synchronization; eye tracking;
29 recurrence quantification analysis; Bayesian regression

Introduction

30

31 Throughout their lives, humans and nonhuman animals learn to perceive their
32 surroundings and engage more or less skilfully with the different tasks they encounter. Within
33 the behavioural sciences, a common distinction is made between individual (or asocial)
34 learning and social learning (Galef, 1988; Heyes, 1994; Hoppitt & Laland, 2013; Whiten &
35 Ham, 1992; Whiten, Horner, Litchfield, & Marshall-Pescini, 2004). The latter is defined as
36 “learning that is facilitated by observation of, or interaction with, another individual (or its
37 products)” and encompasses a wide range of processes (Hoppitt & Laland, 2013).

38 Here we focus on observational learning (a.k.a. ‘production imitation’), which occurs
39 when an observer acquires an action, or action sequence, after watching another individual
40 perform it (Ashford, Bennett, & Davids, 2006; Carcea & Froemke, 2019; see Hoppitt &
41 Laland, 2013, p. 4 and p. 64 for precise definitions). This type of learning occurs in formal
42 settings such as in schooling, sports training, and apprenticeship, and it usually involves a
43 ‘demonstrator’ (or ‘model’) and a ‘learner’ (or ‘observer’). The demonstrator shows the
44 learner the correct or normative way of performing the target task, either intentionally or
45 unintentionally. The learner observes the demonstration and attempts the task. In this context,
46 the dynamics of joint attention that underlies the execution and observation of the task may
47 facilitate the development of the skills required to complete it effectively, as we argue below.

48 Our perspective is supported by the influential work of Tomasello and collaborators
49 (Carpenter, Nagell, & Tomasello, 1998; Carpenter & Tomasello, 1995; Tomasello 1999,
50 2009; Tomasello, Kruger, & Ratner, 1993), who maintain that joint attention is critical to
51 human social learning and social cognition. These authors suggest that both teaching and
52 collaborative learning are critically reliant on human’s ability to alternate perspective taking
53 and to attend jointly to objects and events with others. Joint attention is thought to underlie
54 the unique aspects of our species’ social cognition skills, differentiating humans from other
55 apes (Carpenter & Tomasello, 1995; Tomasello, 2009), scaffolding language learning and
56 cognitive development (Carpenter, Nagell, Tomasello, Butterworth, & Moore, 1998;
57 Degotardi, 2017; Tomasello, 2003, 2009), and being a key deficit of individuals with autism
58 spectrum disorders (Schertz, Odom, Baggett, & Sideris, 2013).

59 Observational learning has been extensively investigated in the context of motor
60 control to understand, for example, how humans learn novel sequences of existing movement
61 patterns (Bird & Heyes, 2005; Nissen & Bullemer, 1987), rhythmic patterns (Vogt, 1995),

62 interlimb or whole-body coordination patterns (Casile & Giese, 2006; Hodges, Williams,
63 Hayes, & Breslin, 2007), and how to adjust limb movements in novel environments (Mattar
64 & Gribble, 2005). Given its intimate link with learning action sequences, observational
65 learning has received considerable attention in the sport sciences; for example, to assess the
66 effectiveness of demonstrations in facilitating skill acquisition (Horn, Williams, Hayes,
67 Hodges, & Scott, 2007; Horn, Williams, Scott, & Hodges, 2005; Williams & Hodges, 2005).

68 Some of these studies have also examined the role played by overt attention during
69 observational learning. (e.g., Breslin, Hodges, & Williams, 2009; D’Innocenzo, Gonzalez,
70 Williams, & Bishop, 2016; Horn et al., 2005). For example, Breslin and colleagues (2009)
71 examined how attending to different parts of the body of a demonstrator performing a novel
72 cricket bowling action mediates how the action is acquired by the learners. Participants in this
73 study underwent three practice blocks in which they first watched a demonstration video –
74 which consisted of a point-light display film showing either the demonstrator's bowling arm,
75 or his wrists, or his full body – five times and then had ten trials to replicate the action. On
76 the following day, after a retention test, participants practiced another three blocks now
77 watching the full-body point-light display film; and an additional retention test was
78 performed on the third day. Measures of intralimb and interlimb coordination were used to
79 compare the performance of learners with the demonstrator, and eye-tracking was used to
80 examine learners' visual attention to the demonstration videos. When watching the full-body
81 film, participants focused more on the bowling arm than on other body parts (e.g., the legs)
82 suggesting learners prioritize the end effector of the action during observational learning.
83 Most importantly, participants who saw the demonstrator's bowling arm on both days
84 acquired an intralimb coordination profile more similar to the demonstrator compared to
85 participants who saw his bowling arm only on day 2. Despite showing a very interesting
86 relation between overt attention and task performance, this study did not explicitly assess it as
87 the measures of overt attention used were aggregated over the entire trial (e.g., proportion of
88 time spent on each area of interest), and thus they were unable to capture the dynamics of
89 overt attention on a moment-by-moment basis. This aspect is at heart of the current study,
90 which will examine precisely how learners must dynamically adapt their visual attention in
91 order to stay ‘in touch’ (i.e. informationally coupled through active perception) with the
92 relevant aspects of the task as they move in space and change over time; and how this
93 attentional coordination is critically related to their task success.

94 To the best of our knowledge, only few studies have formally examined the
95 association between overt attention and learning outcome, and these do not come from the
96 field of social learning. Eye-movement coordination between speakers and listeners was, for
97 example, found to be positively associated with discourse comprehension (Richardson &
98 Dale, 2005), and emerge as a positive predictor of task success only when interlocutors could
99 engage in a bi-directional conversation (Coco, Dale, & Keller, 2018). Other eye-movement
100 studies have attempted to direct the learners' attention to specific aspects of the task by
101 manipulating the saliency of visual stimuli and examined its effect on learning. Grant and
102 Spivey (2003), for example, found that more learners arrived at the correct solution of a
103 diagram-based insight task when presented with a diagram which highlighted a critical area,
104 compared to a static diagram or a diagram which highlighted a non-critical area.

105 However, intentionally directing the observer's attention towards task-relevant
106 aspects does not always facilitate learning (see van Gog, Jarodzka, Scheiter, Gerjets, & Paas,
107 2009, for counterevidence), which indicates that the relation between attentional coordination
108 and performance may strongly depend on the demands of the task at hand and the specific
109 context of demonstrator-observer interaction. Even if researchers in the field of social
110 learning recognize the importance of joint attention, it is yet to be rigorously demonstrated
111 that the time-evolving dynamics of coordination between demonstrators and learners are
112 indeed predictive of their learning pattern.

113 This approach is in line with the growing body of literature in the cognitive sciences
114 arguing that behaviour and human interaction can be framed as multi-scale, self-organizing
115 and dynamical phenomena (Chemero, 2009; Dale, Fusaroli, Duran, & Richardson, 2013; De
116 Jaegher & Di Paolo, 2007; Haken, Kelso, & Bunz, 1985; Kelso, 1995, 2016; Schoner &
117 Kelso, 1988; Schoner, Zanone, & Kelso, 1992). Important advances in the study of multi-
118 modal coordination have, in fact, been possible through the application of non-linear methods
119 of analysis such as recurrence quantification analysis (*RQA*) which can be used to quantify
120 the temporal dynamics of two or more streams of data underlying human interaction, such as
121 manipulative actions and eye-movement (Coco et al., 2017; Coco & Dale, 2014; Fusaroli,
122 Konvalinka, & Wallot, 2014; Richardson, Dale, & Marsh, 2014; Wallot, Mitkidis, McGraw,
123 & Roepstorff, 2016).

124 In the current study, we take inspiration from dynamical systems theory and borrow
125 some of their methodological tools to examine social learning. We combined eye-tracking,

126 *RQA*, and Bayesian hierarchical logistic regression analysis to investigate how learning rate
127 in a novel manipulative task may depend on the patterns of attentional coordination that arise
128 when learners watch a demonstrator performing task-specific actions. Learners were eye-
129 tracked as they watched videos of a demonstrator showing them how to solve a manipulative
130 construction puzzle (our target task, see Figure 1) and then attempted to solve the same
131 puzzle on their own. Rather than running a single trial, we asked learners to watch the
132 demonstration video and attempt the corresponding puzzle multiple times, so that we might
133 monitor changes in their performance as a function of their accumulated experience.

134 We hypothesised that learners must adjust their overt attention dynamically and
135 synchronously to the demonstrator's unfolding behaviour to benefit from it maximally.
136 Specifically, we expected that if learners systematically time-locked their overt attention to
137 the pieces being manipulated by the demonstrator, they might detect relevant aspects of the
138 demonstration, such as the actions required to orderly and correctly assemble the pieces into
139 the final structure. Thus, we predicted that higher attentional coordination of the learners to
140 the manipulative actions of the demonstrator would result into increasingly better learning
141 outcomes.

142 We acknowledge that the use of pre-recorded demonstrations imply that learners may
143 dynamically adapt their allocation of overt attention to the manipulative actions displayed in
144 the videos, but the demonstrator would always perform the same sequence of actions, and so,
145 there is no dynamical interaction between the demonstrator and the learner. Hence, our use of
146 the expressions `attentional coordination` or `synchronisation` must be interpreted as
147 unidirectional (i.e., only the learner can dynamically adapt to the demonstrator).

148 Another important aspect of an intentional demonstration is gaze following, which is
149 considered central to establishing and sustaining joint attention (e.g., Carpenter et al., 1998;
150 Tomasello, Carpenter, Call, Behne, & Moll, 2005). However, it is also known that people
151 shift their overt attention to objects just before reaching them and tend to look at them until
152 the movement is completed (Johansson, Westling, Backstrom, & Flanagan, 2001; Land &
153 Hayhoe, 2001). Thus, in the context of object manipulation, the objects being looked at may
154 coincide with the objects being manipulated. This suggests that, during a manipulative task,
155 joint attention could be achieved by either following the partner's gaze (the conventional
156 gaze-following route) or the partner's hands (hand-eye coordination route).

157 Yu and Smith (2013), for example, provided eye-tracking evidence for this alternative
158 route to joint attention by examining the attentional coordination of one-year-old children and
159 their parents while playing together with toys. Given that seeing the partner's face might help
160 direct one's own visual attention, and given that learning through (live or recorded)
161 demonstration requires coordinating one's visual attention with the demonstrator, we
162 examined whether the presence of the intentional gaze of the demonstrator helped (or not) to
163 direct the attentional coordination of the learners and, especially, whether it improved (or not)
164 their performance in the construction puzzle task. If gaze following is indeed required to
165 establish joint attention, then we should expect that observers who could see the
166 demonstrator's face (and thus could follow his gaze throughout the demonstration) would
167 learn faster than those that could not (see Figure S1 in the electronic supplementary material
168 for an example of the gaze manipulation and refer to demonstration videos available in the
169 Open Science Framework at <https://osf.io/jhtqb/>). Conversely, if gaze following is not
170 required for joint attention, then we should expect that observers seeing the demonstrator's
171 face would not benefit from it as compared to those that did not see it.

172 The final aspect of an intentional demonstration on which our study focuses is that
173 learners may or may not receive verbal instructions from the demonstrator. Psycholinguistics
174 research has provided compelling evidence that sentence processing is tightly linked with
175 other cognitive modalities such as visual attention: speakers tend to look at those objects that
176 correspond with the words being spoken (Coco & Keller, 2012, 2015; Griffin & Bock, 2000;
177 Meyer, Sleiderink, & Levelt, 1998), and listeners also tend to look at those objects that
178 correspond with the words being heard (Allopenna, Magnuson, & Tanenhaus, 1998; Coco,
179 Keller, & Malcolm, 2016; Knoeferle & Crocker, 2006; Richardson & Dale, 2005). Moreover,
180 systematic links between verbal and non-verbal (e.g., eye movement) behaviour extends to
181 communicative dialogue, where speakers and listeners dynamically adapt their actions and
182 vocalizations to the conversational partner as they go along in the dialogue (Clark & Krych,
183 2004; Fogel, 1993), and may even synchronize their eye-movement behaviour over time
184 (Richardson, Dale, & Kirkham, 2007).

185 This literature clearly shows that listening to verbal communication can have a direct
186 impact on one's visual attention, as well as on task performance. We therefore examined the
187 impact of the demonstrator's verbal instruction on the learners' attentional coordination and
188 on their performance at assembling the puzzle. Given the suggested role of speech in guiding

189 the attention of listeners (e.g., Ingold, 2001; Tomasello, 2003), we predicted that learners
190 who could listen to the demonstrator would learn faster than those ones that could not.

191 **1. Methods**

192 1.1. Design

193 We used a mixed factorial design with the type of demonstration video manipulated
194 as a between-participant variable and with 3 repeated measures of task per participant and 5
195 repeated measures of iteration per task. Specifically, we crossed the visibility of the
196 demonstrator's face (face visible or face blurred) with the availability of the demonstrator's
197 verbal instructions (with audio or no audio), to produce four experimental conditions: face
198 blurred and no audio (noFACE_noAUDIO); face visible and no audio (FACE_noAUDIO);
199 face blurred with audio (noFACE_AUDIO); and face visible with audio (FACE_AUDIO). In
200 addition, to discriminate between 'social' and 'individual' learning we ran two control
201 conditions in which learners only saw a still image of the demonstrator and the puzzle pieces
202 and could therefore not benefit from seeing his manipulative actions. In one condition, the
203 still image was accompanied by the audio of the corresponding demonstration
204 (noVIDEO_AUDIO) and hence learners could only benefit from the demonstrator's verbal
205 instructions. In the other condition, the still image was shown without the audio
206 (noVIDEO_noAUDIO), thus learners could not benefit in any way from the behaviour of the
207 demonstrator. We report these two control conditions in the electronic supplementary
208 material, as they were not central to the main arguments of our study.

209 Participants were randomly allocated to one of the six conditions and performed all
210 three versions of the task (star, egg, and barrel). The order of the puzzles was
211 counterbalanced between participants. At the start of each puzzle, the participants were asked
212 to complete the puzzle without any instruction to obtain a baseline measure. They repeated
213 the puzzle another five times, but each time they first watched the demonstration video before
214 attempting the puzzle. This iterative procedure gives us repeated measures of performance
215 (baseline plus 5), which could be used to construct a learning curve rather than a one-off
216 success/failure outcome (see below for further details about how the data was modelled).

217 1.2. Participants

218 Fifty-three participants (32 female; age: range = [18, 50], median = 21, SD = 5.4)
219 were recruited using the Experimenter Volunteer Panel of the University of Edinburgh. Forty
220 participants did the four experimental conditions explained above and reported in what

221 follows. Thirteen participants instead did the control conditions and, as mentioned, are
222 reported only in the electronic supplementary material. All participants gave informed
223 consent, had normal or corrected-to-normal vision, indicated no known learning disability,
224 and were paid £7 as compensation for their time.

225 In addition, an experienced schoolteacher in Edinburgh (male, 33 years of age) was
226 recruited to perform the role of the demonstrator in the video recordings used as stimuli and
227 received £20 for his time. Prior to data collection, the study was approved by the University
228 of St Andrews Teaching and Research Ethics Committee and by the Psychology Research
229 Ethics Committee of the University of Edinburgh, in accordance with the British
230 Psychological Society guidelines on ethics.

231 1.3. Material

232 The manipulative task was to solve construction puzzles, that is, to assemble sets of
233 wooden pieces to form pre-defined structures. Each participant engaged with three puzzles
234 (star, egg, and barrel, see Figure 1), which differed in the number of pieces (star: six pieces;
235 egg: eight pieces; barrel: twelve pieces) and in the steps required to solve them. In the videos,
236 the demonstrator shows and verbally describes the steps needed to assemble the different
237 structures. The experimenter and the demonstrator scripted the verbal instructions beforehand
238 so that the language used was standardised across the three puzzles (transcriptions of the
239 verbal instructions are available in section 6 of the electronic supplementary material, and
240 examples of the demonstration videos are available in the Open Science Framework page of
241 this project).

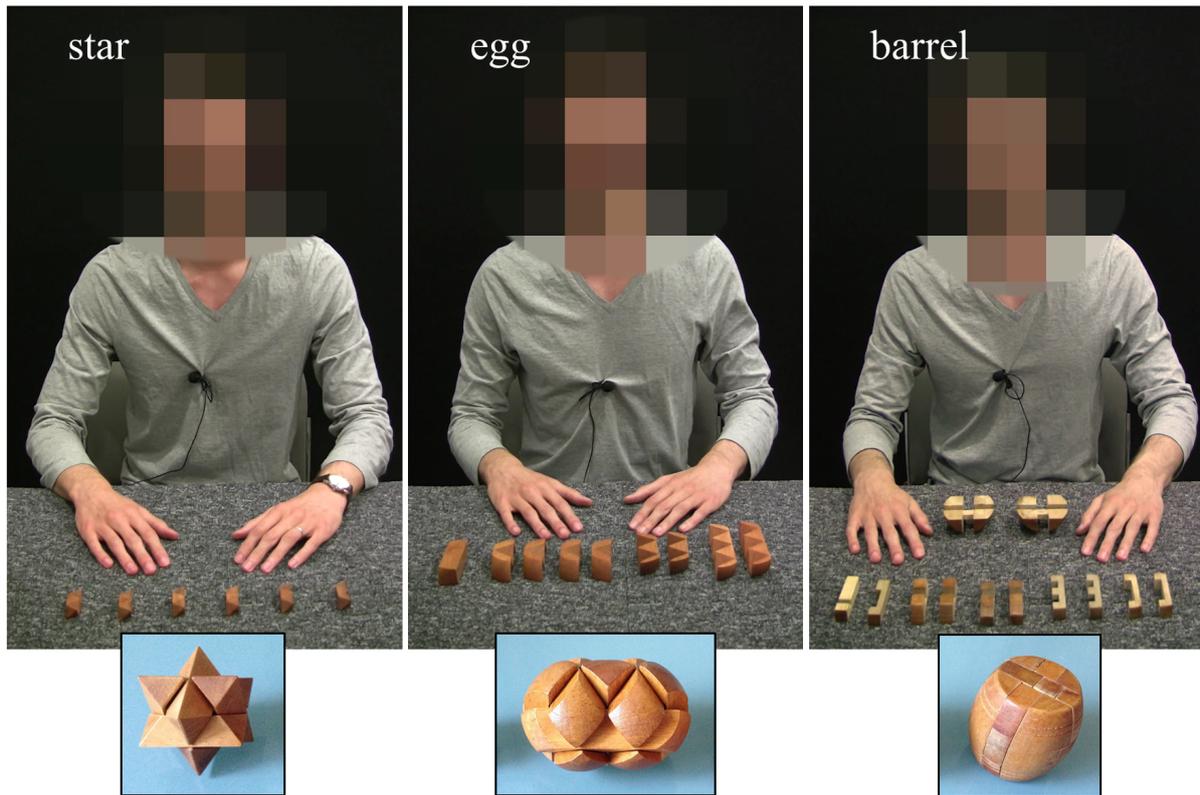
242 A tripod-mounted camera positioned at eye level in front of the demonstrator was
243 used to record the videos. The demonstrator was instructed to act naturally and to look at the
244 camera from time to time, as if he were teaching an imaginary learner in front of him. The
245 videos were captured in the portrait orientation and a lapel microphone was used to record the
246 demonstrator's speech. Because the puzzles differed in the number of pieces, the
247 demonstrations differed in duration (star: 40s, egg: 54s, barrel: 78s). We edited the videos to
248 obtain the versions corresponding to the experimental conditions described above (i.e., face
249 visible/face blurred, with audio/without audio) using the Wondershare Filmora software.

250 1.4. Experimental setup

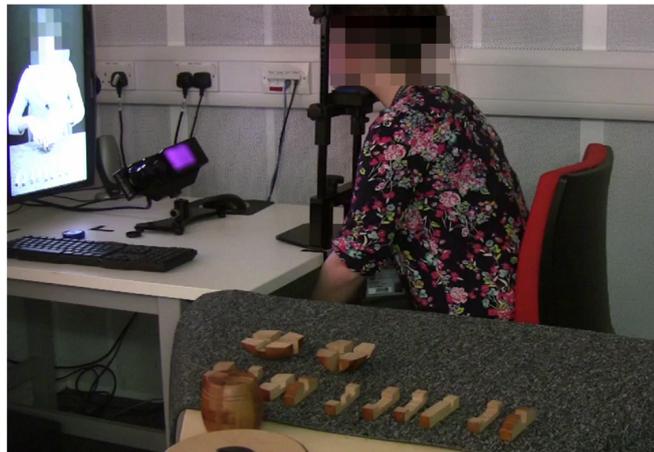
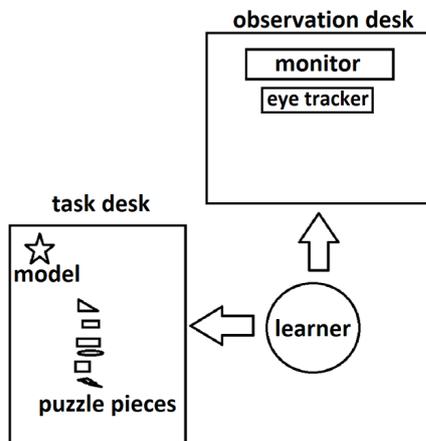
251 Participants watched the videos while being eye-tracked on one desk and assembled
252 the puzzles on another desk (see Figure 1B for a visualization of the workspace). They could
253 easily move between the two desks by rotating 90 degrees on the chair. Videos were
254 displayed on a 21'' monitor in portrait orientation with a resolution of 1050 x 1680 pixels at a
255 refresh rate of 100 Hz and a frame rate of 25 Hz. The audio was played on standard desktop
256 speakers.

257 Eye-movements were tracked using a SR Research EyeLink 1000 with Desktop
258 Mount at a sampling rate of 1000Hz. We only tracked the dominant eye, which was assessed
259 using a parallax test. A forehead-and-chin rest was used to stabilize the participant's head
260 movement. The monitor covered 35 degrees of visual angle vertically and 22 degrees
261 horizontally, and the distance between the headrest and the top of the monitor was 74 cm.
262 Nine-point calibration routines were performed before watching the video for the first time
263 for each puzzle, and a drift check was performed before each subsequent attempt. Experiment
264 Builder (SR Research) was used to implement the experiment. All sessions were also video
265 recorded using two tripod-mounted cameras, but these images were used only to double
266 check the validity of the measures of success manually coded by the experimenter during
267 each session.

A:



B:



268

269 **Figure 1** The experimental setup. **A:** Examples of the starting frames of the demonstration videos for
270 the three puzzle tasks (star, egg, and barrel) in which the demonstrator has his face blurred. The insets
271 show the corresponding solved puzzles. **B:** Plan diagram and photo of the workspace. The learner is at
272 the eye-tracking desk watching the demonstration video and to her left is the task desk with the pieces
273 of a barrel puzzle as well as an assembled model.

274 1.5. Procedure

275 The experimenter told the participants that they would alternate between watching the
276 demonstration videos and attempting the task, and that this procedure would be repeated five
277 times for each of the three puzzles, yielding a total of 15 trials per participant. At the start of
278 each puzzle, the participant was shown all pieces of the puzzle and a correctly finished model
279 and was asked whether she or he had seen it before. If the participant knew the puzzle, the
280 experimenter would skip it and move on to the next (only one participant was familiar with
281 one puzzle). Then, the experimenter asked the participant to produce a copy of the finished
282 model to assess her or his initial ability to solve the puzzle (i.e., before watching the
283 demonstration for the first time) and obtain a baseline score. Participants had a fixed time
284 interval to solve the task (star: 90s, egg: 90s, barrel: 120s) corresponding to twice the time
285 required by the demonstrator to solve it at a comfortable pace. During this period, participants
286 could manipulate their own pieces and visually inspect the finished model but not touch it.
287 The experimenter kept track of the time and interrupted the learner after the time-out,
288 prompting her or him to turn to the eye-tracking desk. After the calibration and validation
289 procedure, the participant watched the demonstration video corresponding to one, out of the
290 four, experimental conditions while being eye-tracked. During this period, the experimenter
291 disassembled the puzzle and re-arranged the pieces on the task desk to prepare for the
292 participant's next attempt. After watching the video for the first time, the participant turned to
293 the task desk and had another attempt at solving the puzzle, thus yielding the first
294 performance measure after the baseline. The participant then turned back to the eye-tracking
295 desk and, after a drift check, watched the demonstration video a second time before the next
296 attempt. This sequence of steps (baseline test plus five iterations of watching the
297 demonstration and attempting the task) was repeated for each of the three puzzles.

298 2. Analysis

299 2.1. Data processing

300 *Demonstrator's manipulation data.* We coded the demonstrator's manipulative
301 actions from the demonstration videos into categorical time series at a sample rate of one
302 observation every 25 milliseconds using the free software Solomon version beta 17.03.22
303 (Péter, 2016). Solving the puzzle requires joining pieces together, thus producing compounds
304 (i.e., the partially-solved puzzle) along the way. In each 25ms temporal window, we used
305 unique categorical labels to code the individual pieces, the compound being manipulated, or
306 to indicate that the demonstrator was not holding any piece. When the demonstrator had a

307 compound in one hand and a piece-to-be-added in the other hand, we used the label for the
308 new piece and, after it was incorporated, the label for the newly-formed compound (see
309 Figure 2A for an illustration of the resulting time series).

310 *Learner's eye-movement data.* Fixations and saccades events were extracted from the
311 raw gaze data using the SR Research Data Viewer software, which performs saccade
312 detection based on velocity and acceleration thresholds of 30°s^{-1} and $9,500^\circ\text{s}^{-2}$, respectively.
313 The eye-movement coordinates were mapped against dynamic Areas Of Interest (AOI),
314 which were defined for each demonstration video using the same labels for pieces and
315 compounds described in the previous paragraph and a label for 'other' to indicate when the
316 participant was looking anywhere else on the screen. We used a customized algorithm written
317 in the R programming language (R Core Team, 2016) to aggregate the eye-movement data
318 into windows of 25ms and assign the label of the AOI that was fixated most of the time
319 within such interval. We therefore obtained categorical time series indicating the sequence of
320 objects fixated by the observers (scan-patterns) in each trial, with length and labels matching
321 the categorical time series indicating the demonstrator's manipulative actions. To avoid very
322 small differences in length that occurred during eye-tracking data collection among
323 participants (star: SD = 6ms, range [1573ms, 1643ms]; egg: SD = 13ms, range [2000ms,
324 2159ms]; barrel: SD = 4ms, range [3078, 3114]), we normalized the length of the scan-
325 patterns and manipulative actions in each puzzle to the same number of bins (star: 1,500 bins,
326 egg: 2,000 bins, barrel: 3,000 bins).

327 *Learner's performance data.* At the end of each trial, the experimenter coded the
328 learners' performance as either a success (i.e. the puzzle was assembled correctly before
329 time-out) or a fail (i.e. the puzzle was not assembled before the time-out), and validated this
330 data by watching the video recordings of the sessions.

331 *Data exclusion.* The initial dataset included 600 trials (40 participants x 3 puzzles x 5
332 iterations). From these, 5 trials were excluded due to one participant knowing the puzzle, 3
333 due to one participant inadvertently moving away from the eye tracker, 2 due to the
334 participant accidentally moving the desk during data collection (perturbing the eye tracking
335 system), and 124 due to the eye tracking data not being acquired properly. The final dataset
336 comprised of 36 participants and 466 trials (condition noFACE_noAUDIO: 10 participants
337 and 131 trials; FACE_noAUDIO: 8 participants and 109 trials; noFACE_AUDIO: 8
338 participants and 100 trials; and FACE_AUDIO: 10 participants and 126 trials).

2.2. Recurrence Quantification Analysis (*RQA*)

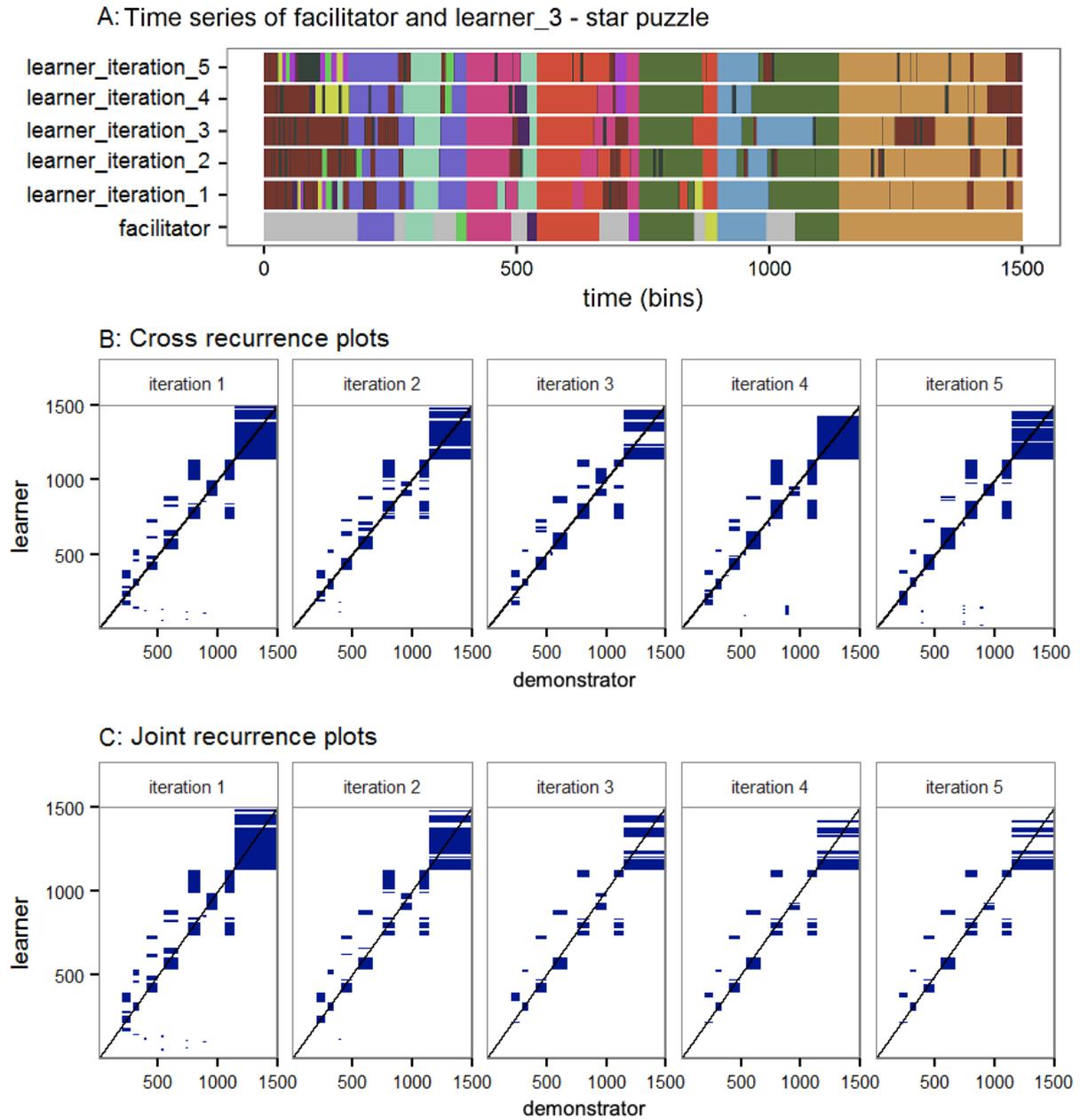
We examined the coordination dynamics between the scan-patterns of the learners (i.e. the sequence of pieces learners looked at while watching the demonstration videos) and the manipulative actions of the demonstrator (i.e. the sequence of pieces the demonstrator manipulated in the demonstration videos) using Recurrence Quantification Analysis or *RQA* (Marwan & Kurths, 2002; Marwan, Romano, Thiel, & Kurths, 2007; Shockley, Butwill, Zbilut, & Webber, 2002; Webber & Zbilut, 2005; Zbilut, Giuliani, & Webber, 1998). In particular, we produced cross-recurrence plots (*CRP*), from which we computed joint-recurrence plots (*JRP*) across the five trials of each puzzle to better capture the iterative process of the task. We used the *crqa* package (version 1.0.9) developed by Coco and Dale (2014) in the *R* software (R Core Team, 2016) to run our analyses using parameter values appropriate for categorical data: *delay* = 1, *embedding* = 1, and *radius* = 0.001.

In Figure 2B and Figure 2C, we illustrate how *CRPs* and *JRPs* were computed for a participant attempting the star puzzle across five iterations after the baseline test. For each trial, we had two time series: one for the manipulative actions of the demonstrator and the other for the scan-pattern of the learner watching the demonstration. Note that the time series for the demonstrator is the same across all five trials (because the demonstration video is the same) but the time series of the learner is different in each trial (because learners are free to move their eyes differently each time).

We produced a *CRP* for each trial by pairing the demonstrator (horizontal axis) with the learner (vertical axis). Conceptually, when the labels of the two time series match in some combination of time-points $[x_i, y_i]$ (i.e., if the puzzle piece being manipulated by the demonstrator at time x_i is the one being looked at by the learner at time y_i), this returns a cross-recurrence point for that entry. When the labels do not match, there is no cross recurrence (see Dale, Warlaumont, & Richardson, 2011, for an extensive explanation of *RQA* applied to categorical time series).

We then obtained joint-recurrence plots (*JRPs*) by simply multiplying the *CRP* of each iteration with all previous iterations on the same puzzle (see Figure 2C). Conceptually, only if all *CRPs* multiplied have a value of 1 in some entry $[x_i, y_i]$ (thus indicating cross-recurrence at that delay in all *CRPs*), then the resulting *JRP* will also have a value of 1 in that same entry, otherwise, the value will be zero. For the first iteration, we just kept the corresponding *CRP*, as there is no previous iteration to multiply it with. For iteration 2, we

371 multiplied the two *CRPs* obtained for iterations 1 and 2. For iteration 3, we multiplied the
 372 three *CRPs* obtained for iterations 1, 2, and 3; and similarly for iterations 4 and 5. Therefore,
 373 the resulting *JRPs* reflect the dynamics of coordination between demonstrator's action and
 374 observer's gaze that is consistently found across the trials with each puzzle.



375

376 **Figure 2. A:** A single time series of the demonstrator manipulating the pieces of the star puzzle and five time
 377 series of one of the learners watching the corresponding video across the five iterations. The colours indicate
 378 either a single piece or the partially assembled puzzle being manipulated/looked at. The grey colour in the
 379 demonstrator's time series represents the moments in which he was not manipulating any piece. **B:** Cross
 380 recurrence plots (*CRP*) of the demonstrator's manipulative actions (horizontal axis) and the learner watching
 381 them (vertical axis). The line of synchrony, i.e., lag 0, is shown in black, and cross recurrence points are shown
 382 in blue. **C:** Joint recurrence plots (*JRP*) produced from the *CRPs* shown in B. For each iteration, the *JRP* is

383 produced by multiplying the *CRP* of that iteration with all previous ones, which leaves in only the recurrence
384 points that consistently occur across iterations.

385 From each *JRP*, we computed three recurrence measures reported in the main
386 analysis. The *recurrence rate (RR)*, which is the proportion of cross-recurrence points in the
387 *JRP*, corresponds mathematically to the cross-correlation sum (Kantz, 1994) and reflects the
388 degree of shared activity or coordination between the two time series. The *determinism*
389 (*DET*), which is the proportion of cross-recurrence points that form continuous diagonal lines
390 (longer than a predefined threshold defined with the parameter *mindiaqline* in the *crqa*
391 package) and reflects the degree of synchronization between the two time series. The *mean*
392 *line length (L)*, which is the average length of the diagonal lines (longer than the threshold),
393 reflects the average time in which the two time series remain synchronized.

394 To compute *DET* and *L* it is necessary to define the threshold parameter (*mindiaqline*
395 in the *crqa* package) because it indicates the minimum length of the diagonal lines in the
396 recurrence plots, i.e. it defines the number of consecutive time-points needed to consider
397 whether the two time series (e.g., the demonstrator and the observer) are in the same state
398 (e.g., manipulating/attending to the same target). In our study, we obtained this threshold
399 empirically by: (1) examining a range of possible threshold values, (2) plotting the resulting
400 *DET* values as a function of the different threshold values examined, (3) visually inspecting
401 these plots and (4) choosing the parameter value that counters ceiling effects (i.e., that leads
402 *DET* values to vary rather than be concentrated at 100%). We obtained a minimum diagonal
403 length threshold value of 30 data-points, which corresponds to a period of 750ms in the raw
404 time series data. In other words, only synchronized attention and manipulative action that was
405 longer than 750ms counted towards the values of *DET* and *L*.

406 Additionally, we computed measures of recurrence across the vertical line structures
407 of the *JRPs*: the laminarity (*LAM*) and the trapping time (*TT*) and obtained largely
408 corroborating results of those observed on the diagonal lines (i.e., *RR*, *DET* and *L*) reported in
409 the main text. These additional analyses are explained and reported in section 6 of the
410 electronic supplementary material.

411 2.3. Statistical analysis

412 *RQA* measures are descriptive in nature and, therefore, comparisons among cases
413 (e.g., conditions, participants, or appropriate baselines) are required to draw inferences and
414 examine specific predictions (Marwan et al., 2007; Shockley et al., 2002). Thus, we

415 examined the relation between the learners' performance, the *RQA* measures of attentional
416 coordination, and the design variables using Bayesian hierarchical logistic regression
417 modelling and the framework of model comparison (Gelman et al., 2014; McElreath, 2016).
418 This allowed us to adequately capture the complexity of our mixed design with repeated
419 measures while improving the estimation of the effects with relatively small samples (e.g.,
420 Baldwin & Fellingham, 2013; Depaoli & van Schoot, 2015). Bayesian regression models
421 were fit in the probabilistic programming language STAN (B. Carpenter et al., 2017) using
422 the *map2stan* function, and compared using the *compare* function, both from the *rethinking*
423 package (McElreath, 2016) in the *R* software. We used Markov Chain Monte Carlo (MCMC)
424 simulation to obtain samples from the posterior distribution of the unknown parameters for
425 which summary statistics were then computed (e.g., mean, credible intervals, differences, or
426 the proportion of positive values). For all models, we used weakly informative priors (i.e.,
427 they were not completely flat but had little influence on the estimated posterior distributions)
428 to obtain a wide range of sensible parameter values and yet avoid unreasonable values
429 (Gelman et al., 2014; McElreath, 2016). We used normal priors with mean 0 and standard
430 deviation of 10 for all non-constrained parameters, and we used half-Cauchy priors with
431 location 0 and shape 5 for the variance parameters.

432 Our core question is whether attentional coordination, operationalized through the
433 independent variables *RR*, *DET*, and *L*, is predictive of learners' performance across trials.
434 We first fitted to the performance data our base model, a hierarchical logistic model (logit
435 link) predicting the probability of task success (Eq. 1). The predictors are the parameters
436 modelling the experimental conditions, i.e. *face* (indicating whether learners could see the
437 demonstrator's face or if it was blurred) and *audio* (indicating whether learners could listen to
438 the demonstrator's verbal instruction or not), *iteration*, and the interaction between condition
439 and *iteration*. Both *face* and *audio* were dummy coded and modelled as between-participant
440 fixed effects, whereas *iteration* was coded numerically from 0 to 4 (i.e., the five trials with
441 each puzzle after the baseline test) and modelled as a within-participant fixed effect. The
442 model also included indicators of the *task* (three levels: star, barrel and egg) and *participant*
443 (36 levels) as varying intercepts (also called fully-crossed random effects). None of the
444 participants solved any of the tasks during the baseline test, therefore we did not include the
445 baseline score as a covariate. This base model captures how performance varies across
446 iterations (i.e. the steepness of the learning curves) for the different experimental conditions

447 and does not include any coordination variable. More formally, the base model can be
 448 represented as:

$$\begin{aligned} \text{logit}(p) = & b_0 + b_1 * \text{face} + b_2 * \text{audio} + b_3 * \text{face} * \text{audio} + (b_4 + b_5 * \text{face} + b_6 * \text{audio} \\ & + b_7 * \text{face} * \text{audio}) * \text{iteration} + I|\text{task} + I|\text{participant} \end{aligned} \quad (1)$$

449 We then fitted three additional models, each including one of the coordination
 450 variables, which were z-scored (i.e. subtracted from the mean and divided by the standard
 451 deviation), as a main (i.e. additive) effect. These models can be represented as:

$$\text{logit}(p) = \text{base_model} + b_8 * RR \quad (2A)$$

$$\text{logit}(p) = \text{base_model} + b_8 * DET \quad (2B)$$

$$\text{logit}(p) = \text{base_model} + b_8 * L \quad (2C)$$

452 Lastly, we fitted three additional models including the interaction between the
 453 experimental condition and the respective coordination variable, thus allowing the effect of
 454 coordination (if there was any) to vary across conditions. These models can be represented
 455 as:

$$\text{logit}(p) = \text{base_model} + (b_8 + b_9 * \text{face} + b_{10} * \text{audio} + b_{11} * \text{face} * \text{audio}) * RR \quad (3A)$$

$$\text{logit}(p) = \text{base_model} + (b_8 + b_9 * \text{face} + b_{10} * \text{audio} + b_{11} * \text{face} * \text{audio}) * DET \quad (3B)$$

$$\text{logit}(p) = \text{base_model} + (b_8 + b_9 * \text{face} + b_{10} * \text{audio} + b_{11} * \text{face} * \text{audio}) * L \quad (3C)$$

456 For each coordination variable, we compared the base model and the two additional
 457 models using the Widely Applicable Information Criterion or WAIC (Gelman et al., 2014;
 458 McElreath, 2016) to examine whether adding the coordination variable, either only as a main
 459 effect or also in interaction with condition, improves model prediction accuracy (the results
 460 of the model comparison are reported in section 4 in the electronic supplementary material).
 461 Lower values of WAIC indicate better predictive accuracy than higher values. We also
 462 examined the Akaike weights, which are rescaled values of WAIC where a total weight of 1
 463 is partitioned among the models under consideration, thus indicating relative predictive
 464 accuracy among them (McElreath, 2016). Including *RR* as a main effect improved model
 465 accuracy but its interaction with the experimental conditions did not improve it further. Thus,
 466 we report model 2A. With respect to *DET* and *L*, including them both as main effect and in

467 interaction with the experimental conditions improved the prediction accuracy over the base
468 model. Thus, we report models 3B and 3C.

469 We ran 2000 iterations (including 1000 warmup iterations) on three chains for each
470 model to ensure the robustness of the results, and report estimates of the posterior
471 distributions from a total of 3,000 samples after warmup. All STAN models converged and
472 mixing of the independent MCMC chains was good, as indicated by inspecting the trace plots
473 and the number of effective sample sizes, and checking the *Rhat* values of the parameters
474 were no higher than 1.01. More details can be found in the Open Science Framework page of
475 this project where we provide a tutorial with the data and scripts to fit and compare the
476 models, as well as to interpret the final models by computing the effects reported in Table 1
477 and replicating Figures 3 and 4. Unless otherwise indicated, we report the mean and 95%
478 central credible interval of the estimated parameters from the fitted models. A strong
479 evidence for an effect is when the 95% credible interval excludes 0, and weak evidence when
480 the 95% credible interval includes 0 but the 90% does not.

481 In section 2 of the electronic supplementary material we report two more models, one
482 examining the performance of the learners across the experimental and the additional control
483 conditions to provide further evidence that learning is indeed facilitated by the demonstrator
484 (in other words, that this is a case of ‘social’ learning), and the other examining the
485 proportion of fixation of the learners to the demonstrator face vs. pieces to obtain clearer
486 insights on the effect of intentional gaze.

487 **3. Results**

488 Table 1 shows the parameter estimates and odds ratios of the three fit logistic models
489 chosen for interpretation (*RR*: model 2A; *DET*: model 3B; *L*: model 3C). Take, for example,
490 the model including *RR* (i.e. the first four rows in Table 1). We observe an odds ratio of 3.17
491 for the effect of iteration in the noFACE_noAUDIO condition, which means the odds of
492 solving the puzzle increases 217% from one iteration to the next. Similarly, we observe an
493 odds ratio of 2.48 for the effect of *RR* across all conditions (as there is no interaction between
494 experimental conditions and *RR* in the model), which means the odds of solving the puzzle
495 increases 148% for each unit increase in *RR*.

496 To help interpretation, we simulated data from the fitted models. To do this, we must
497 decide how to deal with the random effects. We could simulate them too and doing this

498 would increase the variation obtained for the simulated outcome. However, this is unhelpful
499 here as we are not so much interested in the differences among tasks or among participants,
500 but rather in the systematic differences among the experimental conditions. To focus on this
501 aspect, we declared the random effects as zero in the simulations, which corresponds to
502 simulating for an ‘average’ task and ‘average’ participant. Figure 3 shows simulations from
503 the three final models to illustrate the effect of *RR*, *DET*, and *L* on the probability of success
504 across conditions, averaging over the effect of iteration. Figure 4, instead, focuses on model
505 2A (with *RR*) to illustrate also the effect of iteration, and the corresponding figures for *DET*
506 and *L* can be found in the electronic supplementary material, section 5.

507 We will interpret the results of each model in turn and start with model 2A (i.e., *RR*).
508 In line with our main prediction, we found strong evidence that the coordination variable *RR*
509 was positively associated with the probability of success across all experimental conditions
510 (see effect of coordination on Table 1, Figure 3 top row, and Figure 4), which indicates that
511 attentional coordination is beneficial for observational learning. Furthermore, the effect of
512 iteration was positive in all conditions, i.e., learners get progressively better at solving the
513 puzzle.

514 In order to test whether the effect of iteration (i.e. learning rates) differs across
515 conditions, we examined the posterior distribution from the fitted model. For each sample of
516 the posterior distribution, we computed the difference between the effect of iteration
517 estimated for different conditions (say, *FACE_AUDIO* and *FACE_noAUDIO*). This process
518 generates a vector of estimated differences, which we summarised by computing the mean
519 and 95% credible intervals. This summary statistics can be used as evidence (or lack thereof)
520 for a systematic difference between conditions (Gelman et al., 2014). A credible interval
521 crossing zero suggests that the difference between the estimates is not systematic (or, in a
522 frequentist terminology, ‘not significant’). If the credible interval instead does not cross the
523 zero, this suggests that the difference is indeed systematic or ‘significant’. Moreover, a
524 positive difference means the first term of the difference has a higher estimate, and a negative
525 difference means the second term has a higher estimate.

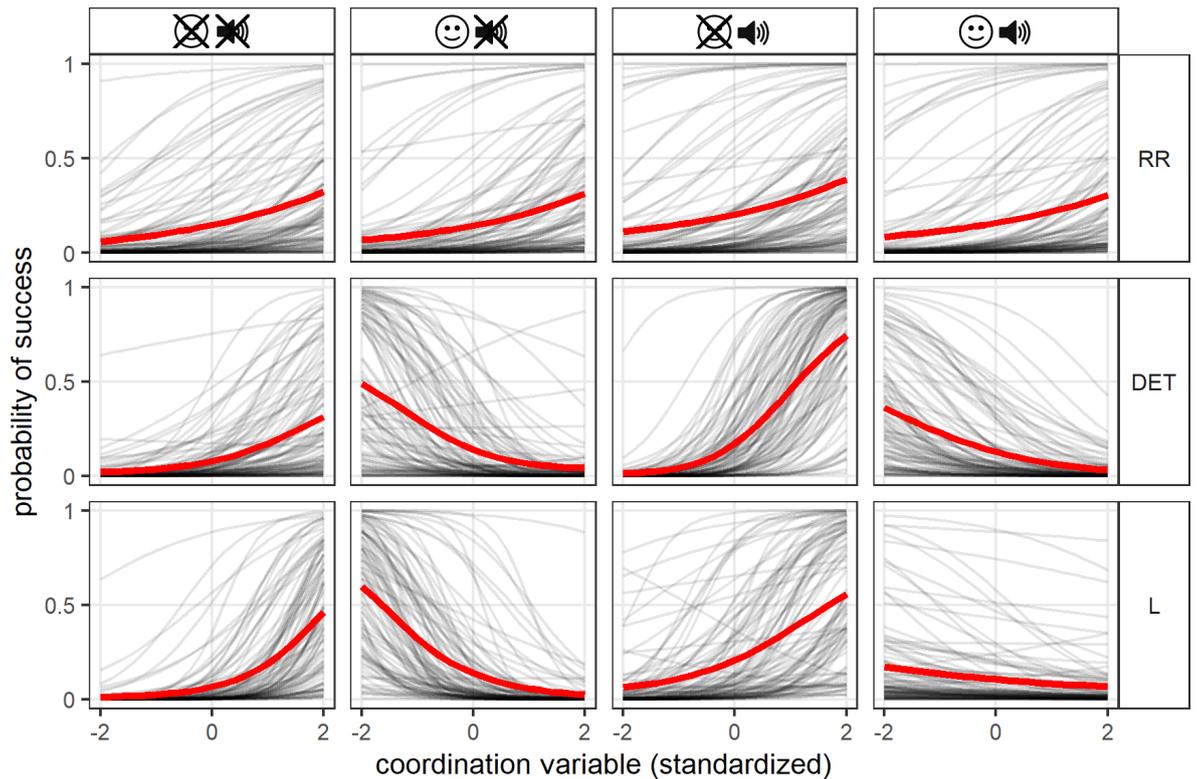
526 We found that the effect of iteration was larger in the condition *FACE_AUDIO* than
527 *FACE_noAUDIO* (difference between the estimates: 1.14 [0.4, 1.97]) and *noFACE_AUDIO*
528 than *noFACE_noAUDIO* (difference between the estimates: 0.88 [0.15, 1.56]). This indicates
529 that learners who could listen to the demonstrator learned faster than those that could not. We

530 found no difference between the effect of iteration for conditions FACE_AUDIO and
 531 noFACE_AUDIO: -0.04 [-0.8, 0.76]; and for conditions FACE_noAUDIO and
 532 noFACE_noAUDIO: -0.3 [-0.97, 0.39]). This result instead indicates that the performance of
 533 learners did not benefit from seeing the demonstrator's face.

534

535 **Table 1** Estimated mean values and a 95% CI (unless a 90% CI is otherwise indicated) for the relative
 536 effects of iteration and coordination on the probability of task success across conditions, computed for
 537 the three final models (one for each coordination variable, *RR*, *DET*, and *L*). Values indicating strong
 538 or weak evidence of an effect are in bold to aid reading.

Coordination variable in the model	Condition	Effect of iteration		Effect of coordination	
		Estimate	Odds ratio	Estimate	Odds ratio
<i>RR</i>		1.11 [0.55, 1.63]	3.04 [1.74, 5.11]	0.91 [0.02, 1.78]	2.48 [1.02, 5.93]
		0.81 [0.26, 1.37]	2.25 [1.30, 3.95]	0.91 [0.02, 1.78]	2.48 [1.02, 5.93]
		2.00 [1.34, 2.67]	7.36 [3.83, 14.41]	0.91 [0.02, 1.78]	2.48 [1.02, 5.93]
		1.95 [1.26, 2.65]	7.04 [3.52, 14.21]	0.91 [0.02, 1.78]	2.48 [1.02, 5.93]
<i>DET</i>		1.39 [0.70, 2.12]	4.03 [2.01, 8.30]	1.14 [0.01, 2.29]	3.13 [1.01, 9.91]
		0.15 [-0.66, 0.91]	1.17 [0.52, 2.47]	-1.32 [-3.03, 0.45]	0.27 [0.05, 1.57]
		2.70 [1.76, 3.68]	14.89 [5.80, 39.70]	2.14 [0.81, 3.68]	8.50 [2.25, 39.49]
		1.44 [0.78, 2.15]	4.23 [2.18, 8.57]	-1.11 [-2.12, -0.17]	0.33 [0.12, 0.85]
<i>L</i>		1.73 [0.98, 2.55]	5.66 [2.67, 12.86]	2.05 [0.82, 3.28]	7.76 [2.28, 26.45]
		0.01 [-0.77, 0.77]	1.01 [0.46, 2.16]	-1.82 90% CI [-3.42, -0.24]	0.16 90% CI [0.03, 0.79]
		2.20 [1.37, 3.07]	9.07 [3.93, 21.63]	1.39 90% CI [0.02, 2.71]	4.00 90% CI [1.02, 14.96]
		1.58 [0.97, 2.28]	4.87 [2.65, 9.79]	-0.41 [-1.11, 0.30]	0.66 [0.33, 1.35]

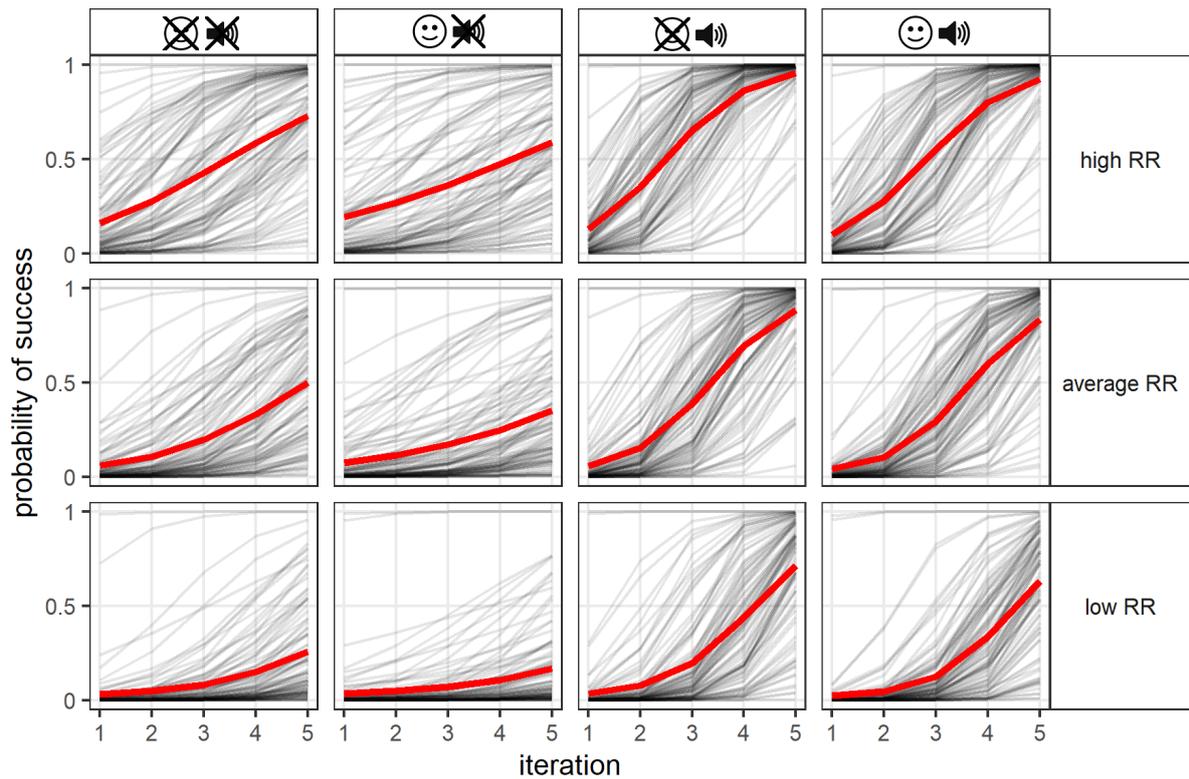


539

540 **Figure 3.** Posterior predictions of the three final logistic models showing the probability of success
 541 (vertical axis) as a function of coordination (horizontal axis) as captured by the *RQA* variables (*RR*,
 542 top row; *DET*, middle row; *L*, bottom row) across the four experimental conditions organized along
 543 the columns. Coordination variables are standardized (z-scored) with -2 corresponding to 2 SD below
 544 the average (low coordination); 0 corresponding to the average value; and 2 corresponding to 2 SD
 545 above the average (high coordination). These simulations are for an average task and average
 546 participant. The shaded black lines represent 100 simulations and the thick red lines represent the
 547 mean of all simulations within each plot.

548 The estimated parameters just discussed reflect the relative effects of iteration and
 549 coordination on the probability of successfully assembling the puzzle. In order to visualize
 550 and interpret their joint contribution, we simulated outcome values (probability of success)
 551 from the fitted model. We fixed the parameter for *RR* at either the average value, a low value
 552 (2 *sd* below the average), or a high value (2 *sd* above the average) and generated 100
 553 predictions for the probability of success for an average task and average participant. The
 554 simulated outcome, reported in Figure 4, clearly shows how the performance of hypothetical
 555 learners (vertical axes) increases as a function of iterations (horizontal axes), varies for the
 556 different experimental conditions (across columns) and is modulated by the degree of
 557 attentional coordination (across rows). A comparison between the three plots within each
 558 column in Figure 4 shows that the learning curves are shifted upwards from low to high
 559 values of attentional coordination. This illustrates that learning is faster among learners who
 560 could coordinate their overt attention with the demonstrator's manipulations more

561 consistently across trials (i.e. those with higher values of coordination computed from the
 562 *JRPs*). In addition, the learning curves are steeper in column 3 compared with those in
 563 column 1, and in column 4 compared to column 2, which confirms that learning was faster
 564 for those individuals who could listen to the verbal instructions as compared to those that
 565 could not. Finally, the learning curves in column 2 are not systematically different from those
 566 in column 1, and those in column 4 are also not different from those in column 3, which
 567 confirms that seeing the demonstrator’s face did not seem to facilitate learning.



568
 569 **Figure 4.** Posterior predictions of the final logistic model with the coordination variable *RR* (model
 570 2A) showing the probability of success (vertical axis) as a function of iterations (horizontal axis)
 571 across conditions (columns), while holding *RR* at either 2 *sd* below the average (low *RR*, bottom row),
 572 at the average value (average *RR*, middle row), or at 2 *sd* above the average (high *RR*, top row). These
 573 simulations are for an average task and average participant. The shaded black lines represent 100
 574 simulations and the thick red lines represent the mean of all simulations within each plot. To see the
 575 effect of the different values of *RR* on performance, the reader should compare the three plots within
 576 each column. To see the effect of seeing the demonstrator’s face compared to face blurred, the reader
 577 should compare the plots in column 1 with those in column 2, and the plots in column 3 with 4. To see
 578 the effect of listening to the demonstrator’s speech compared to no audio, the reader should compare
 579 the plots in column 1 with those in column 3, and the plots in column 2 with 4.

580 Model 3B (i.e., with coordination variable *DET*) and model 3C (with *L*) show similar
 581 patterns, albeit with some interesting differences (Table 1, Figure 3 middle and bottom rows,
 582 see Figures S5 and S6 in the electronic supplementary material for the visualization of
 583 posterior predictions). When the demonstrator’s face was blurred, both *DET* and *L* were

584 positively associated with probability of success, which confirms that learners who
585 synchronized their eye-movement for longer with the demonstrator's actions learned faster
586 than those synchronising for shorter period of time.

587 However, when the demonstrator's face was visible, the probability of success was
588 actually reduced for increasing values of *DET* and *L*. This is illustrated in Figure 3 (middle
589 and bottom rows), which shows that the probability of success declines for higher values of
590 *DET* and *L* in the conditions FACE_noAUDIO and FACE_AUDIO. Accordingly, Figures S5
591 and S6 in the electronic supplementary material show that the learning curves shift downward
592 as we move from low to high values of *DET* and *L*. This suggests that seeing the
593 demonstrator's face, compared to face blurred, was detrimental to learning. This result is
594 confirmed by the strong evidence that iteration has a smaller effect on the probability of
595 success when comparing FACE_noAUDIO with noFACE_noAUDIO for both *DET* and *L*
596 (difference between the estimates for *DET*: -1.24 [-2.31, -0.22]; for *L*: -1.72 [-2.75, -0.63]);
597 and comparing FACE_AUDIO with noFACE_AUDIO for *DET* but not for *L* (difference
598 between the estimates for *DET*: -1.26 [-2.37, -0.14]; for *L*: -0.62 [-1.72, 0.39]).

599 We speculate that the presence of the demonstrator's face attracted the attention of
600 learners to it, distracting them from the actual manipulation task without providing any
601 benefit. Additional analyses reported in the electronic supplementary material (section 3)
602 corroborate this suggestion by confirming that learners looked more at the demonstrator's
603 face when it was visible compared to blurred (difference in the mean estimates of the
604 proportion of fixation time between FACE_noAUDIO and noFACE_noAUDIO: 3.14%
605 [0.5%, 10.3%]), between FACE_AUDIO and noFACE_AUDIO: 5.6% [0.8%, 17.9%]), and
606 even more so when they could listen to his speech (difference between FACE_AUDIO and
607 FACE_noAUDIO: 2.9%, 90% CI [0.2%, 8.0%]).

608 **4. Discussion**

609 Observational learning (or production imitation) is a time-evolving process involving
610 a demonstrator (or model), a learner (or observer), and a target task. In this study, we
611 borrowed the conceptual and analytical framework of dynamical system theory as applied
612 and developed in the cognitive sciences (e.g., Coco et al., 2017; Dale, et, al. 2013; Fusaroli, et
613 al., 2014) to investigate the role of attentional coordination in the 'passing on' or re-
614 construction of knowledge. Researchers in diverse fields have claimed that learning through
615 observation benefits from a constant interaction and tight attentional coupling between the

616 learner and the resources made available by the demonstrator (e.g., M. Carpenter et al., 1998;
617 Mundy & Newell 2009; Tomasello, 2009). However, the experimental support for this claim
618 has lacked both temporal and spatial resolution – for example, because studies used manual
619 annotations of gaze directions from video footage (e.g., M. Carpenter et al 1998), or used
620 eye-tracking measures that aggregate data over time, such as number of fixations, which
621 provides little insight about how attention unfolds over time (e.g., Breslin et al., 2009).

622 In the current study, we combined eye-tracking with sophisticated computational
623 analyses (*RQA* and Bayesian hierarchical regression) and provided evidence that learners
624 better able to coordinate their overt attention with the manipulative actions of the
625 demonstrator had an increasingly higher probability of success in solving a construction
626 puzzle task. Through this dynamical interaction with the demonstrator’s unfolding actions,
627 learners discovered object affordances and the sequence of actions required to successfully
628 complete the task more quickly than if they were learning alone.

629 In this study, we also investigated how the availability of verbal instruction and
630 intentional gaze interacts with attentional coordination and mediate the learning outcomes.
631 Speech and overt attention are known to synchronise strongly during language
632 comprehension, language production, and even dialogue tasks (e.g., Coco & Keller, 2012;
633 Knoeferle & Crocker, 2006; Richardson et al., 2007). We therefore expected that the
634 availability of verbal instruction would improve task performance and be associated with
635 better coordination between overt attention and manipulative actions. Indeed, we found
636 evidence that speech helps cognitive processes to align and plays an important role in the
637 passing on of knowledge, as shown by the stronger improvement of performance compared to
638 when speech was not available.

639 The availability of intentional gaze is considered important to build joint attention
640 (e.g., Tomasello et al., 2005) and we therefore expected that being able to see the
641 demonstrator’s face (as opposed to his blurred face) would improve the learning outcome of
642 our participants in the manipulative task. However, we found that the availability of the
643 demonstrator’s face, and hence of his intentional gaze, were instead detrimental to learning.
644 Learners tended to look more often at the demonstrator’s face when it was visible (compared
645 to blurred) and even more often when they could also hear him speaking. These bouts of
646 attention away from the manipulative actions of the demonstrator and towards his face have
647 likely distracted learners and hence negatively impacted on their learning. We note, however,

648 that our study utilises pre-recorded videos and that, in cases of live interaction, the behaviour
649 of looking at the partner's eyes is likely to play important roles, such as to indicate
650 engagement or request the partner's attention, and hence may be beneficial to learning.
651 Regardless, it is interesting to observe that learners coordinated their visual attention with the
652 demonstrator's actions even when his face was blurred. This result is consistent with the
653 "hand-eye coordination" route to joint attention (Yu & Smith, 2013) rather than the more
654 widely acknowledged gaze-following route and suggests that this alternative route may play
655 an important role in the processes of social learning which has received little attention.

656 Using pre-recorded demonstrations enabled us to achieve greater control when
657 measuring the attentional coordination across learners, because they all watched the same
658 videos. While demonstration videos are commonly used in studies of observational learning,
659 this is arguably one of the main limitations of this design. Most cases of observational
660 learning occur during face-to-face encounters, thus it would be important to examine
661 demonstrator-learner dyads interacting live using the same paradigm. Another important
662 limitation of this study is the relatively small number of participants. The novel manipulative
663 task we conceived was particularly time-consuming, as it not only involved eye-tracking
664 (while participants watched the demonstrations) but also required manual performance (to
665 measure success in every trial) and was iterative (to measure changes in performance across
666 trials, i.e. learning), requiring a total of 15 trials for each participant. To overcome the
667 resulting time constraint, we manipulated the experimental conditions (i.e. type of
668 demonstration video) between participants, which limited the sample size in each. Even
669 though Bayesian statistics is more robust in the context of small sample sizes (see Gelman et
670 al. 2014; van de Schoot et al., 2014) and despite finding systematic differences across
671 conditions, the results must be interpreted as exploratory and might be used as an important
672 foundation for future research interested in similar research questions and deploying a similar
673 methodology. The results from the current study can constitute a solid basis for power
674 analyses estimating effect size statistic in designs aimed at replicating our findings or
675 extending in other ways our innovative experimental approach.

676 This study did not seek to address how the ability to identify and track the relevant
677 aspects of the demonstration develops. Further work might use a similar paradigm to examine
678 dyads from different age groups, and we expect that measures of attentional coordination will
679 be positively correlated with age. In principle, similar methods could be applied to the study

680 of social learning in nonhuman animals, allowing researchers to explore whether coordination
681 is central to social learning more generally, or a species-specific feature of human social
682 learning.

683 One methodological contribution of our study is to show that the combination of eye-
684 tracking methods, *RQA*, and hierarchical modelling, can provide a powerful tool for
685 examining the mechanisms of observational learning with finer granularity. Future research
686 could exploit these methods to further elucidate how and the extent to which the dynamics of
687 attentional coordination may influence social learning by looking, for example, at the stability
688 of the attentional coordination, and the relation between patterns of attentional coordination
689 and learning trajectories, during iterative observational learning. Novel extensions of
690 recurrence quantification analysis to multi-dimensional data might be successfully used to
691 investigate patterns of learning involving larger groups of individuals interacting in real time
692 (see Knight, Kennedy, & McComb, 2016; Wallot, Roepstorff, & Mønster, 2016 for recent
693 developments in this direction).

694 We conclude that viewing social learning from the perspective of moment-to-moment
695 attentional coordination might provide novel theoretical insights to the field, and we hope the
696 present study will motivate further work that embraces the technological and analytical
697 advances deployed here.

698 **Funding:** This work was supported by the University of St Andrews; the Konrad Lorenz
699 Institute for Evolution and Cognition Research [Writing-up Fellowship awarded to MP]; the
700 John Templeton Foundation [grant number 40128 awarded to KNL]; the Leverhulme Trust
701 [grant number ECF-014-205 awarded to MIC]; and the Fundação para a Ciência e Tecnologia
702 [grant number PTDC/PSI-ESP/30958/2017 awarded to MIC]. The funding sources were not
703 involved in the study design; the collection, analysis and interpretation of data; the writing of
704 the report; and the decision to submit the article for publication.

705 **Declarations of interest:** none

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