Influence of He⁺⁺ and shock geometry on interplanetary shocks in the solar wind: 2D Hybrid simulations

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Key Points:

8	•	He++ content modifies the shock profile, temperature anisotropy and distribution
9		functions in the upstream and downstream regions.
10	•	θ_{Bn} and He++ content affects the efficiency with which particles escape to the up-
11		stream region.
12	•	Increase in magnetic fluctuations and He++ content modify regions with higher
13		temperature anisotropy downstream of quasi-perpendicular shocks.

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15 Abstract

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After protons, alpha particles (He⁺⁺) are the most important ion species in the solar wind, constituting 17 typically about 5% of the total ion number density. Due to their different charge-to-mass ratio 18 protons and He⁺⁺ particles are accelerated differently when they cross the electrostatic potential in a 19 collisionless shock. This behavior can produce changes in the velocity distribution function (VDF) for 20 both species generating anisotropy in the temperature which is considered to be the energy source for 21 various phenomena such as ion cyclotron and mirror mode waves. How these changes in temperature 22 anisotropy and shock structure depend on the percentage of He⁺⁺ particles and the geometry of the 23 shock is not completely understood. In this paper we have performed various 2D local hybrid 24 simulations (particle ions, massless fluid electrons) with similar characteristics (e.g., Mach number) 25 to interplanetary shocks for both quasi-parallel and quasi-perpendicular geometries self-consistently 26 including different percentages of He⁺⁺ particles. We have found changes in the shock transition 27 behavior as well as in the temperature anisotropy as functions of both the shock geometry and He⁺⁺ 28 particle abundance: The change of the initial θ_{Bn} leads to variations of the efficiency with which 29 particles can escape to the upstream region facilitating or not the formation of compressive structures 30 in the magnetic field that will produce increments in perpendicular temperature. The regions where 31 both temperature anisotropy and compressive fluctuations appear tend to be more extended and reach 32 higher values as the He⁺⁺ content in the simulations increases. 33

34 1 Introduction

Collisionless shocks are a phenomenon of crucial importance in heliospheric/space plasma 35 physics and astrophysics. Along with solar flares they are the main particle accelerators near the Sun 36 and in the interplanetary (IP) medium. The energy dissipation produced by collisionless shocks is 37 a complex consequence of the interaction between particles and the electric and magnetic fields at 38 the shock interface together with wave-particle interactions in the wave field driven by instabilities 39 at the shock and in the upstream and downstream regions. In addition, due to the lack of collisions, 40 a small fraction of particles can be reflected towards the upstream side of the shocks, reaching high 41 energies [Gosling & Thomsen, 1985; Gosling et al., 1989; Burgess & Scholer, 2015]. 42

⁴³ Depending on the shock normal angle θ_{Bn} , defined as the angle between the upstream magnetic ⁴⁴ field and the shock normal direction, collisionless shocks can be divided in two types: quasi-parallel ⁴⁵ ($\theta_{Bn} < 45^{\circ}$) and quasi-perpendicular ($\theta_{Bn} > 45^{\circ}$). Ion acceleration at the shock can be caused by ⁴⁶ different processes: shock drift acceleration [*Burgess*, 1987a] is usually considered to be the main ⁴⁷ mechanism operating in quasi-perpendicular shocks, while diffusive shock acceleration [*Blanford &* ⁴⁸ *Ostriker*, 1978] works more efficiently in quasi-parallel shocks [see *Burgess & Scholer*, 2015, for a ⁴⁹ detailed description].

In quasi-parallel shocks, the reflected ions can escape back to the upstream side along the 50 magnetic field lines where their interaction with the solar wind (SW) particles can lead to excitation 51 of upstream waves including ultra-low-frequency (ULF) waves which can evolve into shocklets, 52 and other large-amplitude magnetic structures [Russell & Hoppe, 1983; Blanco-Cano et al., 2016; 53 Wilson, L. B. III, 2016]. Consequently, the region upstream of a quasi-parallel shock is intimately 54 linked to the generation of high-energy upstream ions, and is in particular related to the extraction of 55 thermal particles from the upstream side of the shock into the population of energetic ions [Scholer 56 & Burgess, 1992; Burgess et al., 2005; Su et al., 2012a,b; Sundberg et al., 2016]. 57

In quasi-perpendicular shocks, the specularly reflected ions gyrate in the upstream magnetic 58 field generating a foot region, penetrating the shock potential back to the downstream side with 59 high tangential velocities, producing an anisotropic distribution with the perpendicular temperature 60 larger than the parallel one near the shock front. Linear theory and simulations have shown that 61 such an anisotropic distribution can be unstable to ion cyclotron and mirror mode waves [Gary, 62 1993; Lembège & Savoini, 1992; Hada et al., 2003; Yang et al., 2009, 2012]. These waves have 63 been observed in the Earth's magnetosheath behind the quasi-perpendicular bow shock [Anderson & 64 Fuselier, 1993], downstream of shocks associated to stream interaction regions (SIRs) [Blanco-Cano 65

et al., 2016] and also in complex events formed by two or more large-scale solar wind structures which interact in the interplanetary space [*Enriquez-Rivera et al.*, 2010, 2013; *Siu-Tapia et al.*, 2015].

In the solar wind, the shock interface conditions are basically determined by the dynamics of protons, which are the most abundant ion species. However, there are also various kinds of minor ions. Among these, He⁺⁺ is the most important ion species and although it constitutes typically only about 4-5% of the total ion number density [*Neugebauer & Snyder*, 1966; *Ipavich et al.*, 1984; *Wurz*, 2005], its contribution to the upstream mass density and dynamical pressure can be as large as 20%. Therefore, He⁺⁺ effects in shock dynamics should not be ignored as has been pointed previously [*Geiss et al.*, 1970; *Kasper et al.*, 2007; *Gedalin*, 2017].

One of the most interesting features that hybrid simulations of quasi-parallel shocks have 75 revealed is a cyclic behavior [Burgess, 1989a] in their structure above an Alfvénic Mach number 76 of $M_A = V_u/V_A \sim 2$: upstream waves are convected towards the shock, being compressed as they 77 approach producing a gradual shock profile. These arriving waves steepen up at the upstream edge 78 which becomes the newly reformed shock [Burgess, 1989a; Scholer & Terasawa, 1990; Hao et al., 79 2016]. In 1D simulations of quasi-parallel shocks with $\theta_{Bn} \gtrsim 20^\circ$ the low frequency upstream 80 waves evolve to large amplitude pulsations very close to the shock to later interact with the shock, 81 producing an associated increased density of diffuse and/or nearly specularly reflected ions. At 1 AU 82 the observations of interplanetary shocks show different micro-structure even for similar θ_{Bn} values 83 [Blanco-Cano et al., 2016; Kajdič et al., 2012]. This can be attributed to time evolution of the shock 84 front and/or local geometry irregularities, which have been reported and studied at different spatial 85 scales via multispacecraft analysis and hybrid simulations [Aguilar-Rodriguez et al., 2011; Kajdič et 86 al., 2019]. 87

In the past, quasi-parallel hybrid simulations with He⁺⁺as second heavy ion species have been 88 performed [Trattner & Scholer, 1991, 1994], showing that solar wind alpha particles penetrate the 89 shock ramp rather unaffected and gyrate in the downstream magnetic field. In the case of low 90 (~ 0.1) upstream β (ratio of thermal to magnetic pressures) this gyration is in general well behind 91 the shock ramp, and no diffuse alpha particles are generated. However, occasionally the whole 92 distribution is able to gyrate back to the shock ramp and gets accelerated into the upstream region 93 by the electric field in the shock ramp. This leads to the formation of localized backstreaming He⁺⁺ 94 clouds which are the source of diffuse alpha particles. At higher Mach number ($M_A \sim 9$), the 95 gyroradii increase which makes it easier for the beam-like alpha particles behind the shock to reach 96 the shock ramp for a second time. This causes a strong increase of the number of backstreaming alpha 97 particles. Trattner & Scholer (1993) performed 1D hybrid simulations with different alpha particles to proton ratio. Assuming an upstream alpha particle-to-proton temperature ratio (T_{α}/T_{p}) of 4, the 99 downstream temperature ratio of alpha particles to protons was enhanced (\sim 5-7). In a recent work 100 [Caprioli et al., 2017] has studied the thermalization, injection, and acceleration of ions with different 101 mass/charge ratios (A/Z) in non-relativistic collisionless shocks via hybrid simulations finding that 102 in general, ions thermalize to a post-shock temperature proportional to A. When diffusive shock 103 acceleration was efficient, the ions develop a non-thermal tail whose extent scales with Z, so that 104 incompletely-ionized heavy ions are preferentially accelerated. 105

Various works concerning quasi-perpendicular shock hybrid simulations including He⁺⁺ ions 106 [McKean et al., 1995a, 1996] have been carried out in order to study the wave evolution in the 107 downstream region for low and high Mach number (M_A) shocks. These works show how the 108 proton cyclotron and mirror mode waves can be excited near the shock front to be convected further 109 downstream. The energy of the proton cyclotron waves driven by the proton temperature anisotropy 110 $T_{\perp}/T_{\parallel} > 1$ [e.g., Gary et al., 1996] can be absorbed by the He⁺⁺ particles leading to thermalized 111 He⁺⁺ distributions. In these simulated shocks both ion species are decelerated differently due to 112 their different charge-mass ratios when they cross the electrostatic shock potential, producing the 113 formation of a ring-beam distribution of He⁺⁺ downstream of the shock [Fuselier & Schmidt, 1997; 114 Lu & Wang, 2006]. This He⁺⁺ ring-beam distribution can drive helium cyclotron waves, which then 115 scatter He⁺⁺ into a shell-like distribution [Lu & Wang, 2006; Hao et al., 2014]. Geotail spacecraft 116 recent observations have made it possible to identify stable He⁺⁺ ring beams in velocity space 117 perpendicular to the magnetic field generated during a bow shock crossing [Tsubouchi et al., 2016]. 118

In the context of interplanetary shocks a recent work [*Ofman et al.*, 2019] compares the observed magnetic and density structure of different oblique shocks at 1 AU with 2D hybrid simulations to demonstrate the effects of He⁺⁺ on the magnetic and density profiles, the dynamics of the downstream shock oscillations as well as the nonstationarity of the shocks.

Given the presence of He⁺⁺ in the solar wind, in this work we investigate its influence on different 123 interplanetary shock signatures performing a group of 2D hybrid simulations of collisionless shocks 124 [Winske & Leroy, 1985; Burgess, 1987b; Krauss-Varban, 2005]. We use the HYPSI code [Burgess 125 et al., 2015; Gingell et al., 2017; Trotta & Burgess, 2019] varying the He⁺⁺ number density fraction 126 (1, 5 and 10%) and shock geometry ($\theta_{Bn} = 15^\circ, 30^\circ, 50^\circ$ and 65°) for an intermediate Alfvén Mach 127 number ($M_A \sim 4.4$) similar to IP shocks. In this context observational IP shocks with parameters 128 similar to those presented here can be found in the WIND data set (http://ipshocks.fi/) where 129 for instance 48 fast forward IP shocks with Mach numbers $(4 < M_A < 5)$ are listed covering 0.46 130 $<\beta<13.07$ and $8^{\circ}<\theta_{Bn}<88^{\circ}$ as well as in past investigations [Blanco-Cano et al., 2016] and 131 recent case-study works [Enriquez-Rivera et al., 2013; Ofman et al., 2019] where observational He⁺⁺ 132 content is similar to the values in our study. This work is organized as follows: In Section 2, we 133 describe the hybrid simulation model and setup, the simulation results are presented in Section 3, and in Section 4 we discuss and summarize our results. 135

2 Simulation setup

We performed 2D hybrid simulations to investigate the influence of He⁺⁺ on shock dynamics and 137 particle thermalization for different θ_{Bn} initial values and different number content of He⁺⁺ particles. 138 The two dimensional simulations were performed using the hybrid Particle-In-Cell (PIC) code HYPSI 139 [Burgess et al., 2015; Sundberg et al., 2016], that is based on the CAM-CL (see [Matthews, 1994] 140 for details) algorithm. Under this approach protons and He⁺⁺ particles are treated kinetically and 141 advanced using the standard PIC method. Electrons are considered as a charge-neutralizing massless 142 fluid [see A.3 in Burgess & Scholer, 2015]. Electron inertial and kinetic effects are assumed to be 143 negligible. 144

Spatial and temporal scales in the simulation are expressed in units of proton inertial length 145 $d_i = c/\omega_p$ (where ω_p is the proton plasma frecuency and c is the speed of light) and Ω_p^{-1} (where Ω_p 146 is the proton gyro frequency) respectively and velocity is normalized to the simulation Alfvén speed 147 $V_A = B_u / \sqrt{\mu_o n_p m_p}$ that does not change with He⁺⁺ fraction. The proton density $n_p m_p$ and magnetic 148 field B_u used to calculate these parameters are also normalized to the initial upstream values. The 149 number of grid cells for all the runs is $n_x \times n_y = 1000 \times 800$ having cell sizes $\Delta x = \Delta y = 0.5$ c/ ω_p 150 with velocity, magnetic field, and electric field vectors including all three-dimensional components. 151 The time step Δt was chosen so that $\Omega_p \Delta t = 0.005$. In all cases, the plasma is initialised with an 152 inflow speed V_{in} of 3.3 V_A along the x direction and with the magnetic field in the x-y simulation 153 plane. 154

The injection method has been used to create and sustain the shock transition. The plasma flows along the *x* direction at the (super-Alfvénic) speed V_{in} . The right boundary of the simulation acts as a perfectly reflecting wall, and plasma is continuously injected at the left (open) boundary. As a consequence of the interaction between the reflected and injected plasma, a shock is produced, and it propagates in the negative *x* direction. In the simulation frame, the downstream side of the shock is at rest, and the shock normal is antiparallel to the inflow speed. The simulation is periodic in the *y* direction.

We perform different runs varying the initial angle between the upstream B-field direction and the *x*-axis (15°, 30°, 50° and 65°) which also corresponds to the nominal angle θ_{Bn} of the shocks. Alpha particles are included in the simulations self-consistently. For each θ_{Bn} value we vary the relative number density fraction of He⁺⁺ i.e. $n_{\alpha}/n_p = 0.01, 0.05, 0.10$, with n_{α} and n_p being the number density fraction of He⁺⁺ and protons respectively. We thus perform 12 simulation runs (see Figure 1).

A finite resistivity, $\eta = 0.06 \omega_p^{-1}$ is used in the simulations with the upstream ion populations having an isotropic Maxwellian VDF, with an upstream $\beta = 0.5$. In order to keep the statistical noise 168 169 typical of PIC simulations to a minimum, the number of particles per cell for all the simulations is 170 \sim 100 per species (upstream). This is done to correctly model minor species, even if its fraction is small. It should be noted that the different values of θ_{Bn} for each simulation results in slightly 172 different shocks velocities [Caprioli & Spitkovsky, 2014] in the simulation frame (and therefore 173 slightly different M_A) depending on the θ_{Bn} value. We study the shocks once they have reached the 174 same x position (i.e. $x \sim 250 d_i$) in the middle of the box hence due to different shock velocities, the 175 simulation times of the shocks will differ. 176

3 Simulation results

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3.1 Magnetic field

Figure 1 shows the time evolution of the average magnetic field profile obtained by averaging in the y-direction. In the figure the shock θ_{Bn} values increase from left to right from 15°, 30°, 50° to 65°. The He⁺⁺ number density fraction increases from 1% (top panel), 5% (middle) to 10% (bottom).

The color scale has the same range (from 1 to 3.5) in all plots. The shock can be identified by the abrupt jump in the magnetic field magnitude by a factor of ≥ 2 , with the color changing from blue to red. Although the inflow velocity is the same for all the runs, due to the different θ_{Bn} values the shock velocity and thereby the Alfvénic Mach number vary, being higher as the θ_{Bn} increases: $M_A = 4.2, 4.3, 4.5, 4.8$ for $\theta_{Bn} = 15^{\circ}, 30^{\circ}, 50^{\circ}$ and 65° respectively. The He⁺⁺ number density fraction does not seem to influence the Mach number in a significant manner.

¹⁸⁹ Clear differences can be observed in the averaged magnetic field profile time evolution as θ_{Bn} ¹⁹⁰ increases. For the 15° case the magnetic field magnitude exhibits maximum values ≤ 3 in the ¹⁹¹ downstream region (red color) within 25 d_i from shock transition. The width of this plateau tends ¹⁹² to increase as the He⁺⁺ number density fraction increases. Further downstream the magnetic field ¹⁹³ magnitude decreases to ~ 1.5.

In the upstream region the magnetic field fluctuations exhibit amplitudes up to 1.5 near the shock. These upstream fluctuations start to form at the beginning of the simulations very close to the shock, reaching larger distances from the shock as the simulation evolves.

Although not shown here (See Figure S1 in the Supporting Information), the plots of magnetic field magnitude for an horizontal cut in the simulation box at different consecutive times show different compressive waves and whistler wave packets formed upstream of the shock. These waves convect into the shock causing the shock transition to change from a gradual to an abrupt profile contributing to the reformation of the shock as suggested in past works [*Burgess*, 1989a; *Hao et al.*, 2017]. These waves have different characteristics depending on the content of He⁺⁺ particles and will be studied in the future.

In the 30° case the magnetic field magnitude reaches similar maximum values in the downstream region as in the 15° case (< 3) but B values do not decrease as much further downstream, settling at \sim 2. The upstream fluctuations tend to have smaller amplitudes than in the 15° case. They do however behave similarly in the sense that in the beginning they form close to the shock and extend to larger distances from it as the simulation evolves.

For the 50° geometry, the downstream B-field magnitude reaches values of ≤ 3 and there is no clear decrease with distance from the shock in the downstream region. The compressive magnetic fluctuations in the upstream side exhibit considerably smaller amplitudes compared with the previous geometries and begin to appear later in the simulations, after t ~100 Ω^{-1} . Their upstream extensions are much smaller. These upstream increased B-field fluctuations appear later in time as the He⁺⁺ number density fraction increases The onset times are approximately 100, 125 and 170 Ω_p^{-1} for 1, 5 and 10 % of He⁺⁺ respectively. Downstream magnetic field fluctuations decrease their amplitude considerably compared with the less oblique cases and almost no differences are observed in the magnetic signature as the He⁺⁺ percentage changes in the simulations (see also Figure 2).

For the 65° case there are no compressive fluctuations in the upstream region. The shock transition is very abrupt and the B-field increases to values up to ~ 4. A very narrow overshoot is formed immediately behind the shock ramp (see Figure 2) and is followed by a fast decrease to a constant value of ~ 3. The downstream fluctuations for this case have amplitudes similar to those in the 50° case.



Figure 1. Figure matrix showing the time evolution of total magnetic field (averaged over y-axis) for all the runs in this work. θ_{Bn} increases from left to right while the He⁺⁺ number density fraction increases from top to bottom. The change in color from navy to aqua occurs at ~1.25 while the change from green to yellow occurs at ~ 1.5.

Figure 2 shows the average total magnetic field profiles for all the θ_{Bn} values at the time when the shock arrives to ~ 250 d_i . This time has been chosen based on Figure 1 and corresponds to the time when the upstream waves have properly formed. The three profiles plotted in each panel correspond to different He⁺⁺ number density fractions (black: 1%, red: 5%, blue: 10%).

Figure 2 exhibits clear variations of the averaged shock magnetic field profile. Well developed compressive B-field variations in the upstream region can be identified decreasing in amplitude as θ_{Bn} increases except for the 65° geometry where they do not develop. These variations extend farther upstream for the 15° and 30° cases. The averaged shock front becomes steeper as the shock becomes more oblique. As the θ_{Bn} increases, the shock profile changes from a peak-like to a step-like

signature. When $\theta_{Bn} = 65^{\circ}$ a sharp overshoot forms just behind the shock followed by an undershoot. 236 For the quasi-parallel cases ($\theta_{Bn} = 15^{\circ}$ and 30°) the magnetic field fluctuations after the shock 237 decrease more gradually as the content of He⁺⁺ particles increases. The downstream fluctuations 238 tend to have smaller amplitudes as the θ_{Bn} increases. For the more oblique case ($\theta_{Bn} = 65^\circ$) 239 downstream quasi-periodic fluctuations after the undershoot can be observed growing in amplitude 240 as the content of He⁺⁺ particles increases in agreement with a similar recent work [Ofman et al., 241 2019] where simulations of shocks with $\theta_{Bn} = 60^{\circ}$ and different percentages of He⁺⁺ are performed 242 and compared with DSCOVR observations. After ~ $350 d_i$ the downstream compressive fluctuations 243 have almost disappeared, regardless of the He⁺⁺ content. The asymptotic downstream B value is 244 larger as the shock geometry becomes more oblique going from a magnitude of 1.5 for $\theta_{Bn} = 15^{\circ}$ to 245 3 for $\theta_{Bn} = 65^{\circ}$ as expected from the fluid shock conservation (Rankie-Hugoniot) relations. 246



Figure 2. Total magnetic field profile (average over y-axis) for the all the different θ_{Bn} values used in this 247 work when the shock arrives to ~ 250 d_i . The θ_{Bn} angle increases from top to bottom, He⁺⁺ number density 248 fraction is indicated by different colors (black: 1%, red: 5%, blue: 10%). 249

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3.2 Temperature anisotropy

Figure 3 shows the time evolution of proton temperature anisotropy $A_p = (T_{\perp}/T_{\parallel})_p$ averaged 251 over the y-axis for each of our simulations following the same procedure as in Figure 1. The parallel 252 and perpendicular temperatures are calculated from the second velocity moment of the distribution 253 function [see for example Gary, 1993] in each cell. The color bar palette was divided in two colors: 254 dark to aqua-blue color to represent the anisotropy values less than one and yellow to red color for 255 anisotropy values from one to two. Figure 3 shows that there are three types of behavior for A_p 256 which are correlated with shock geometry as follows: 257

• In the case of quasi-parallel shocks with $\theta_{Bn} = 15^{\circ}$ and 30° the upstream region that is 258 filled initially with an isotropic flux $(T_{\parallel} \sim T_{\perp})$ starts to be permeated by backstreaming particles coming from the shock leading to $T_{\parallel} > T_{\perp}$ as can be observed in dark blue color. As the simulation 259 260 evolves and more backstreaming particles interact with the incoming plasma near the shock, upstream 261 regions with $A_p > 1$ begin to develop as a consequence of fluctuations in magnetic field which can 262

²⁶³ be corroborated by examining Figure 1. For $\theta_{Bn} = 15^{\circ}$ these upstream regions where $A_p > 1$ seem ²⁶⁴ more fragmented, also their extension to the upstream side is smaller for the case with 1% of He⁺⁺ in ²⁶⁵ comparison with those with higher He⁺⁺ number density fraction. This behavior is also observed for ²⁶⁶ the $\theta_{Bn} = 30^{\circ}$ case being less fragmented in comparison to the less oblique case. The downstream ²⁶⁷ region for both quasi-parallel cases has $A_p \sim 1$ throughout all the simulation, for the $\theta_{Bn} = 30^{\circ}$ case. ²⁶⁸ Small zones with $A_p > 1$ in the immediate downstream region can be observed at early times in the ²⁶⁹ simulations, being less extended for the case with higher He^{++} number density fraction.

• In the case of the oblique shock with $\theta_{Bn} = 50^{\circ}$ a well defined region with $A_p > 1$ develops 270 very early in the simulation just downstream of the shock, appearing closer to it, being larger in 271 extension as the percentage of He⁺⁺ particles increases. A narrow high anisotropy layer with $A_p \sim 2$ 272 is located exactly at the shock transition reducing its magnitude before upstream regions near the 273 shock with $A_p > 1$ start to appear extending more and more towards the upstream side as the 274 simulation evolves. As for the quasi-parallel cases, the upstream region where the incident plasma 275 flow initially has an isotropic distribution start to be permeated by zones with $T_{\parallel} > T_{\perp}$ (dark blue) due 276 to backstreaming particles aligned to the magnetic field lines. As the simulation continues to evolve 277 upstream regions with $A_p > 1$ appear in the upstream region coinciding with zones with compressive magnetic field fluctuations as discussed in Figure 1. These upstream regions where $A_p > 1$ appear 279 at earlier times $(t < 150\Omega_i^{-1})$ for the simulation with 1% of He⁺⁺ particles in comparison with 280 the 10% case $(t > 150\Omega_i^{-1})$. The upstream transition region from $T_{\parallel} \sim T_{\perp}$ to $T_{\parallel} > T_{\perp}$ is not as 281 sharp as in the quasi parallel cases and the extent of this region lasts longer since the regions with 282 $A_p > 1$ begin to develop at more advanced times for this geometry. Also the region with $T_{\parallel} > T_{\perp}$ 283 appears in the upstream region later in time (t > 100 Ω_i^{-1}) in comparison with its quasi parallel 284 counterpart (t ~ 100 Ω_i^{-1}) which is in agreement with the less efficient parallel transport of particles 285 expected for this quasi-perpendicular geometry. In contrast to the other geometries, for this case the 286 different behavior in the immediate upstream side of the shock after $t \sim 150 \ \Omega^{-1}$ when upstream 287 B-field fluctuations starts to develop allowing the increase in temperature anisotropy that define a 288 characteristic simulation time associated with growth and convection of upstream fluctuations that 289 could not be observed if the simulation had not lasted so long. It must also be mentioned that the 290 "wall effect" observed near the right wall is not physical but a falsely perceived effect due to the high 291 contrast colors near $A_p \sim 1$. 292

• In the case of the shock with $\theta_{Bn} = 65^{\circ}$ the value of A_p is greater than one through all the downstream region reaching the maximum value (> 8) in the region adjacent to the shock transition during the whole time of the simulation. The proton anisotropy value is ~ 1 throughout all the upstream region in agreement with the fact that the rate of backstreaming particles is almost null for this high θ_{Bn} case and no upstream magnetic field fluctuations are present in Figure 1.

Figure 4 shows semi-log plots of T_{\perp}/T_{\parallel} (averaged over y-axis) for protons (blue) and He⁺⁺ (orange) at the time when the shocks arrive to ~ 250 d_i . The shock position is marked with a vertical dashed line while the horizontal dashed line indicates $T_{\perp}/T_{\parallel} = 1$. For clarity only a range from 100 d_i to 300 d_i in the x-axis and from 0.5 to 5 (with minor ticks spaced each 0.25) in the y-axis are plotted. As before, the temperature anisotropy profiles show three distinct behaviors:

• Quasi parallel cases ($\theta_{Bn} = 15^\circ, 30^\circ$): For both geometries the upstream value of $A_p \sim 0.75$ at $x=100 \ d_i$ increases to values ≥ 1 in some *x*-intervals near the shock region that are more extended and reach higher values as the He⁺⁺ number density fraction increases. In general A_p is greater than the He⁺⁺ temperature anisotropy $A_{\alpha} = (T_{\perp}/T_{\parallel})_{\alpha}$ in the upstream region. In the downstream region A_p exhibits a decrement to values less than 1 while A_{α} rises sharply reaching a maximum peak value (~ 1.5 for 15° and ~ 1.75 for 30°) at the shock transition to then decrease to ~ 1. For the case with $\theta_{Bn} = 30^\circ$ the A_{α} peak at the shock transition tends to be wider as the He⁺⁺ percentages increase.

• Oblique case ($\theta_{Bn} = 50^\circ$) : In contrast to the quasi parallel geometries, here A_p at x = 100 d_i becomes increasingly smaller as the He⁺⁺ content grows. x-intervals with $A_p > 1$ that are less extended and reach lower values as the He⁺⁺ number density fraction increases can be observed. Then A_p drops significantly in the upstream region adjacent to the shock. This drop is less pronounced in the case of the 10 % He⁺⁺ run. Unlike for the quasi parallel cases, for this geometry $A_p < A_\alpha$ along



Figure 3. Figure matrix showing the time evolution of temperature anisotropy for protons (averaged over y-axis) for all the runs in this work. θ_{Bn} increases from left to right while the He⁺⁺ number density fraction increases from top to bottom. The color palette is chosen to show anisotropy values less (in blue) and greater (in yellow-red) than 1.

all the upstream side except for the 1 % He⁺⁺ case where a region with $A_p \sim A_\alpha$ at about $x \sim 200$ d_i can be observed. Downstream of the shock A_p decreases to values less than one. The value of A_α rise sharply reaching a peak at the shock transition that increases in value (2.75, 3.75, 4.25) as the He⁺⁺ percentage does and then drops in the downstream region. This fall becomes more abrupt, making the width of the peak thinner as the content of He⁺⁺ particles increases.

• Quasi-perpendicular geometry ($\theta_{Bn} = 65^\circ$): Here the value of A_α is 1 throughout all the 324 upstream region, then rises sharply at the shock transition reaching smaller peak values (8.2, 7.8, 325 7.5) as the He^{++} number density fraction increases, and then decreasing in the downstream region. 326 This drop is not monotonic since downstream oscillations of A_{α} can be observed as a consequence 327 of the coherent gyration of He⁺⁺ particles as pointed in previous works [McKean et al., 1996; Hao et 328 al., 2014] and discussed here in section 3.3. For protons, the upstream values of A_p are just below 329 1, then increase substantially at the shock transition to values that are, in contrast to A_{α} , greater 330 (8.8, 8.9, 9.31) as the He⁺⁺ content increases. Then A_{α} drop to ~ 1.25 in the downstream region. 331 The decrease here does not show downstream oscillations which can be explained in terms of the 332 differences in charge to mass ratios for both species. 333

Additionally, we performed an extra simulation (not shown) with $\theta_{Bn} = 75^{\circ}$ in order to see if there are differences comparing with the $\theta_{Bn} = 65^{\circ}$ case. We did not find significant changes beyond the expected increment in the downstream overshoot magnitude.

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3.3 Velocity distribution functions

We also investigate the behavior of the velocity distribution functions (VDFs) for both ion 338 species in the shock interface zone along the shock surface as well as at different x coordinates 339 for the time when the shock is at x=250 d_i . We show four cases corresponding to $\theta_{Bn} = 15^\circ, 65^\circ$ 340 with 1 and 10% of He⁺⁺ since they exemplify the main VDF characteristics due to variations in the 341 angle θ_{Bn} from quasi-parallel to quasi-perpendicular and the low and high number density fraction 342 in He⁺⁺ particles. It is important to mention that the number density of points in VDFs depends 343 on the number of particles per cell so that the relative fraction of He⁺⁺ to protons is not seen when 344 comparing VDFs for the two species. 345

Figure 5 displays the cases for $\theta_{Bn} = 15^{\circ}$ with 1% and 10% of He⁺⁺. By comparing Figures 5a 346 and 5c we can observe that the downstream region exhibits higher amplitude magnetic fluctuations 347 reaching values (> 3) along a larger range of x in the case of the shock with 10% of He⁺⁺. In 348 panels 5b and 5d where cuts along y=100 d_i (red) and y=250 d_i (blue) are shown, variations in 349 downstream magnetic field are clearly observed. In addition, for the 10% case the variations between 350 both cuts along y-direction are more pronounced compared to the case with lower He⁺⁺ number 351 density fraction. Upstream of the shock whistler precursors are observed in both He⁺⁺ cases for the 352 bottom cut (in red) due to the irregular shock front profile. Whistlers are not found in the top cut (in 353 blue). 354

Figures 5e and 5f show the upstream and downstream VDFs respectively for both species in the regions inside the magenta boxes in Figure 5c corresponding to the case with 10% of He⁺⁺ particles. The proton VDF in the upstream region (V_x - V_y space) has two principal components (Figure 5e): A main beam centered at (V_x , V_y , V_z) = (3.3, 0, 0) V_A corresponding to the inflow particles and a secondary component of backstreaming particles ($V_x < 3.3$). Comparing the upstream VDFs of both species we notice that the secondary component of the VDF corresponding to protons is more populated and reaches higher values in velocity than its He⁺⁺ counterpart.

Although they are qualitatively similar, the differences between VDFs at different vertical locations in the upstream side (not showed) can be attributed to the deformation of the shock front which produces different local geometry (Figures 5a and 5c) that leads to different plasma processing along the shock and inside the collecting boxes as can be corroborated by observing the differences in magnetic profiles in panels 5b and 5d for regions on both sides of the shock.

For the downstream side (Figure 5f) the thermalization of particles through the shock potential produces a spread of the VDF for both species in all directions. Again, the VDF in V_x - V_y space tends to be more isotropic ($T_{\perp}/T_{\parallel} \sim 1$) for protons than for alphas (Figure 5f) which is in agreement with Figure 4. As for the upstream side, there are differences in the VDF's at different y-coordinates in the downstream side but they are not so pronounced, and this can be explained in terms of the differences in the turbulent magnetosheath region as can be observed for both profiles in magnetic field in Figure 5d.

Figure 6 shows the $\theta_{Bn} = 65^{\circ}$ simulation with 1 and 10% of He⁺⁺ particles in the same format 374 as Figure 5. As in the previous case Figures 6a and 6c show that the downstream region is permeated 375 by larger amplitude field fluctuations when the number density fraction of He⁺⁺ is higher. This 376 behavior is corroborated comparing Figures 6b and 6d where the profiles show more turbulence in 377 magnetic field for the case with 10% of He⁺⁺. Also the differences in magnetic field profiles are 378 more pronounced for the case with the highest percentage of helium He⁺⁺. For the upstream side 379 no differences between cases with different He⁺⁺ percentage are found for the magnetic field. In 380 contrast to the quasi parallel cases, here the shock transition is sharp and presents a clear overshoot. 381

Figure 6e for the $\theta_{Bn} = 65^{\circ}$ shows clearly less particles for both species in the upstream side 382 in comparison with the $\theta_{Bn} = 15^{\circ}$ case in Figure 5. The VDF only shows some of the reflected-383 gyrating ions which will eventually end up in the downstream region. In addition, for this case very 384 few backstreaming He⁺⁺ particles can be observed when comparing with protons (lower panels in 6e). This can be explained by the differences of mass for both species that facilitates protons to be 386 more efficiently reflected to the upstream side than their He⁺⁺ counterpart as reported in previous 387 simulation works (See for example [Burgess, 1989b]) and in agreement with [Broll et al., 2018] 388 where data and hybrid simulations of a bow shock observed by the Magnetospheric Multiscale 389 (MMS) mission indicate that the amount of He⁺⁺ that reflects at the shock is smaller than the proton 390 population. 391

Figure 6f shows different behaviors for proton and He⁺⁺ particles in the downstream region. 392 He⁺⁺ particles tend to form a ring-like distribution centered in $(V_x, V_z) = (0, 0)$ in agreement with 393 previous works such as [Hao et al., 2014], who explain this ring as a consequence of differentially 394 deceleration of He⁺⁺ particles compared to protons due to their different charge-to-mass ratio as 395 they cross the shock potential. On V_x - V_y panels in Figure 6f it is possible to see that both species 396 differ mainly in the width of their distributions functions along V_x as expected from the results from Figure 4 where the anisotropy value has a broader and higher peak in the immediate downstream 398 region for He⁺⁺ particles than for protons. Because of the quasi-perpendicular geometry for this 399 case, there are no pronounced irregularities along the shock front as can be observed in Figure 6b 400 and Figure 6d in contrast with the $\theta_{Bn} = 15^{\circ}$ case (panels b and d in Figure 5). Although not showed 401 here (see Figure S2 in the Supporting Information) when compared VDFs between different He⁺⁺ 402 percentages for this quasi perpendicular case it can be observed that the downstream VDFs for both 403 species tend to be more diffuse for the case with higher He⁺⁺ percentage, this can be explained as a 404 consequence of the more perturbed magnetic field on the downstream side of the shock as the He⁺⁺ 405 number density fraction increases as can be observed from the differences between horizontal cuts 406 for both He⁺⁺ cases here (Figures 6b and 6d). 407

The characteristics of VDFs found here are in agreement with previous works [*Motschmann* & *Glassmeier*, 1993] that is, whereas in quasi-parallel configurations the scattering of protons in V_x - V_y space is rather isotropic (Figure 5f) in the quasi-perpendicular case it remains anisotropic (Figure 6f). In the last case the He⁺⁺ distribution in V_x - V_z space is a ring around the magnetic field vector mainly pointed in y direction (Figure 6f).

Figure 7 shows the densities of protons and He++ particles corresponding to the same simulations 413 and times as in Figures 5 and 6. Clear differences can be observed when comparing both geometries. While for the quasi-parallel case (panels a and b) the shock interface is not well defined and 415 presents the typical rippling as well as not coherent fluctuations at both sides of the shock, for 416 the quasi-perpendicular shock (panels c and d) the shock interface is well defined, no upstream 417 density structures can be observed and a wave-like structure is evident behind the shock decreasing 418 in amplitude further in the downstream region. When we analyze the differences for the same 419 geometries taking in account the He⁺⁺ content in the simulations the effect is more evident for the 420 quasi-perpendicular case (panels c and d) where the fluctuations are more defined but with lower 421 amplitudes for the cases with less He⁺⁺ content. This feature is correlated with both the temperature 422 anisotropy and the magnetic field magnitude in the same regions as can be corroborated in Figures 423 4, 5 and 6. This is in agreement with [Ofman et al., 2019] who explain this behavior in terms of 424 the He⁺⁺ "surfing" [Lee et al., 1996] along the shock front evidenced by the strong localized density 425 peaks. 426

427

3.4 Mirror and ion/cyclotron instability analysis

In this section we study the growing of mirror and ion/cyclotron waves [*Gary*, 1993] using instability thresholds related with temperature anisotropy and plasma beta parameters in order to know when these modes can grow. This analysis is valid for cases where the condition $T_{\perp}/T_{\parallel} > 1$ is well fulfilled for protons [*Gary*, 1993; *McKean et al.*, 1995a,b] namely in the downstream region for our $\theta_{Bn} = 65^{\circ}$ cases as can be corroborated in Figure 4 and Figure 6f where the downstream VDFs

are shown. For this purpose in Figure 8 some cuts of proton anisotropy $(T_{\perp}/T_{\parallel})$ and magnetic field at 433 $y = 200 d_i$ and just behind the shock corresponding to the same simulation times of those in Figure 434 7c,d are shown. In addition to T_{\perp}/T_{\parallel} the parameters M = 1 + 1/ β_{\perp} (in red) and IC = 1 + $\beta_{\parallel}^{0.5}$ (in blue) 435 are shown in the same panel. From these it follows that the growing threshold of mirror instability 436 is fulfilled when $T_{\perp}/T_{\parallel} > M$ [Southwood and Kivelson, 1993] while the corresponding condition for 437 the ion/cyclotron instability approximate threshold is $T_{\perp}/T_{\parallel} < \text{IC}$ [Gary et al., 1996; Anderson et al., 438 1996]. As can be observed in Figure 8 for both He⁺⁺ concentrations simulations the ion/cyclotron 439 threshold is fulfilled along the cut. For the mirror instability the threshold is barely fulfilled only 440 at some located intervals near the shock interface. These results are in agreement with [McKean et 441 al., 1995a,b; Hao et al., 2014] who studied with hybrid simulation quasi-perpendicular shocks with 442 similar parameters finding that ion/cyclotron waves can grow in the downstream region by the energy 443 provided by the ion temperature anisotropy. Not many differences are observed when comparing the 444 results for both He⁺⁺ relative abundances except for an increase in the size of the regions where the 445 mirror instability threshold is met for the 10% He⁺⁺ case which leads to a reduction in the size of 446 regions near the shock where the ion/cyclotron threshold is fulfilled. These results could be improved 447 with a full kinetic instability calculation in a future work. 448



Figure 4. Semi-log temperature anisotropy profiles (average over y-axis) for protons (blue) and He⁺⁺ (orange) at the time when the shock arrives to ~ 250 d_i for all the θ_{Bn} values and He⁺⁺ percentages in this work. The vertical dashed line indicates the shock localization and the horizontal dashed line indicates $T_{\perp}/T_{\parallel} = 1$

474 **4 Discussion and Conclusions**

Although the dependence of shock dynamics, temperature anisotropy and VDF evolution with shock geometry (θ_{Bn}) has been widely studied in the past with the help of both, observations and computer simulations, the influence of He⁺⁺ number density fraction on interplanetary shock environments has received less attention. In order to study this influence we have analyzed the results of twelve 2D local hybrid simulations of quasi-parallel ($\theta_{Bn} = 15^\circ$, 30°) and quasi-perpendicular ($\theta_{Bn} = 50^\circ$, 65°) collisionless shocks varying the number density fraction of He⁺⁺ particles (1%, 5%, 10%). Our study shows that both the geometry and the content of He⁺⁺ particles can modify the interplanetary shock profile and the characteristics of the upstream and downstream regions affecting temperature anisotropy, VDF properties and magnetic fluctuations growth.

The variation of initial θ_{Bn} changes the efficiency with which particles can escape to the 484 upstream side of the shock influencing the formation of compressive structures in the magnetic field 485 profile. Quasi-parallel geometries ($\theta_{Bn} = 15^\circ, 30^\circ$) allow particles to be transported efficiently farther in the upstream region along the magnetic field lines. The interaction between these backstreaming 487 particles and the incoming plasma flow results in upstream magnetic field fluctuations. The upstream 488 variations of the averaged B-field profiles tend to have larger amplitudes and extend further to the 489 upstream region for the 15° case. The shock with oblique geometry ($\theta_{Bn} = 50^{\circ}$) takes more 490 time to develop these fluctuations and these reach lower amplitudes and extend less towards the 491 upstream region compared with quasi-parallel cases. For the quasi-perpendicular shock ($\theta_{Bn} = 65^{\circ}$) 492 no upstream magnetic field fluctuations form. In the downstream region such fluctuations tend to 493 decrease in amplitude and length as the θ_{Bn} increase.

The magnetic field profile is also affected by shock geometry. The expected increment of 495 magnetic field in the shock interface tends to be more abrupt as the θ_{Bn} increases. For the quasi-496 parallel geometries ($\theta_{Bn} = 15^\circ$, 30°) the magnetic field magnitude decreases in the downstream 497 side from the shock jump, this decrement is more gradual for the $\theta_{Bn}=30^{\circ}$ case. In contrast, for 498 the oblique geometry ($\theta_{Bn} = 50^\circ$) the magnetic field profile has a step-like shape. For the quasi-499 perpendicular geometry ($\theta_{Bn} = 65^{\circ}$) the same step-like profile is observed with a clear overshoot just 500 after the shock jump followed by a decrement in magnetic field to an almost constant downstream 501 side value. 502

The temperature anisotropy for protons (A_p) is also affected by θ_{Bn} . For the quasi-parallel 503 cases (θ_{Bn} = 15° and 30°) the upstream side starts to be permeated by backstreaming particles since 504 the beginning of the simulation which produce regions with $T_{\parallel} > T_{\perp}$. As the simulation evolves 505 and backstreaming particles interact with the incoming plasma, upstream regions with $A_p > 1$ start 506 to appear due to the fluctuations in magnetic field which can heat and scatter the particles in the 507 perpendicular direction to the magnetic field. For the oblique case ($\theta_{Bn} = 50^\circ$) the upstream zones 508 where $A_p > 1$ are less extended and appear later in time in comparison to the quasi-parallel cases, 509 which is due to the fact that backstreaming particles are less efficiently transported to the upstream 510 region far from the shock as the geometry becomes more oblique. In the quasi-perpendicular shock 511 with $\theta_{Bn} = 65^{\circ}$ there are no zones where $A_p > 1$ in the upstream side which can be explained in terms 512 of the so oblique geometry that does not allow particles to escape beyond the foot-ramp region. 513 In the downstream region $A_p \sim 1$ for the quasi-parallel cases ($\theta_{Bn} = 15^\circ$ and 30°), for the oblique 514 geometry ($\theta_{Bn} = 50^\circ$) a zone with $A_p > 1$ appears, with a size that growths as the simulation evolves. 515 For the quasi-perpendicular shock with $\theta_{Bn} = 65^{\circ}$ the perpendicular temperature presents a sudden 516 increase in the shock transition due to the gyration of reflected particles that are convected into the 517 downstream region increasing its perpendicular velocity. Then they suffer a rapid isotropization in the region downstream of the overshoot that are associated with the fluctuations present in the 519 downstream region. These then diminish in amplitude with increasing distance downstream of the 520 shock as has been observationally reported by [Sckopke et al., 1990]. 521

The temperature anisotropy for both species (A_p, A_α) also shows a dependency on θ_{Bn} . For the quasi-parallel cases $(\theta_{Bn}=15^\circ \text{ and } 30^\circ) A_\alpha < A_p$ in the upstream region and $A_\alpha > A_p$ in the downstream region. For the oblique geometry $(\theta_{Bn}=50^\circ) A_\alpha > A_p$ in general along all the simulation box. In the quasi-perpendicular shock $(\theta_{Bn}=65^\circ) A_\alpha \sim A_p \sim 1$ in the upstream region and then increase suddenly at the shock, decreasing in the downstream region with $A_\alpha > A_p$ and a fluctuating pattern for the He⁺⁺ component. For all the geometries a peak $(A_\alpha > 1)$ is formed at shock transition that tends to be larger as the value of θ_{Bn} increases.

The VDFs for both species are also affected by θ_{Bn} . For the $\theta_{Bn} = 15^{\circ}$ case backstreaming particles of both species can be observed in the immediate upstream region in contrast to the quasi⁵³¹ perpendicular case ($\theta_{Bn} = 65^{\circ}$) where the percentage of particles that do not belong to the inflow ⁵³² beam is much smaller. In contrast to the proton distributions, a ring-like distribution is formed in the ⁵³³ immediate downstream side for He⁺⁺ particles as a consequence of differential acceleration due to ⁵³⁴ the different charge to mass ratio of both species. Also the downstream VDFs for protons are more ⁵³⁵ isotropic and thermalized for the $\theta_{Bn} = 15^{\circ}$ case than for the $\theta_{Bn} = 65^{\circ}$ case.

We find that the content of He⁺⁺ also slightly affects the magnetic field structure at both sides of 536 the shock. In quasi-parallel shocks ($\theta_{Bn} = 15^\circ, 30^\circ$) the compressive magnetic fluctuations on both 537 sides of the shock tend to reach higher amplitudes for the cases with more He⁺⁺ content. In contrast, 538 for the shock with $\theta_{Bn} = 50^{\circ}$ the increment in He⁺⁺ number density fraction does not seem to affect the amplitude of these fluctuations. Although for the quasi-perpendicular case with $\theta_{Bn} = 65^{\circ}$ no 540 upstream compressive fluctuations are observed, in the downstream side these fluctuations tend to 541 reach larger amplitudes for the cases with more He⁺⁺ content due to the increase of the temperature 542 anisotropy in the immediate downstream region as the percentage of He^{++} particles increases (as will 543 be discussed below). 544

The temperature anisotropy for protons (A_p) is also affected by the He⁺⁺ content: The upstream 545 zones where $A_p > 1$ coincide with those where compressive magnetic fluctuations are present as 546 expected because fluctuations in magnetic field can produce heating and scattering of particles in 547 the perpendicular direction relative to the magnetic field. For the quasi-parallel cases ($\theta_{Bn} = 15^\circ$ and 548 30°) the upstream zones where $A_p > 1$ are less fragmented for the simulations where the number 549 density fraction of He⁺⁺ is higher. For the oblique case ($\theta_{Bn} = 50^\circ$) this behavior is repeated while 550 for the downstream region the zone with $A_p > 1$ is closer to the shock zone for the case where the 551 He⁺⁺ number density fraction is larger. When comparing the temperature anisotropy for both species 552 (A_p, A_α) we can observe that although the content of He⁺⁺ particles does not affect significantly 553 the shape of the peak at the shock transition for the quasi-parallel cases, for the oblique case (θ_{Bn} = 554 50°) a clear increment is observed as the number density fraction of He⁺⁺ increases and for the 555 quasi-perpendicular simulations ($\theta_{Bn} = 65^\circ$) the opposite happens, the peak decreases as the number 556 density fraction of He⁺⁺ increases. 557

The fact that for all our simulations, except in the more oblique case ($\theta_{Bn} = 65^\circ$), upstream zones where $T_{\perp} > T_{\parallel}$ coincide with those where compressive magnetic field fluctuations are present is in agreement with recent results of [*Gingell et al.*, 2017] where MMS observations show $T_{\perp} > T_{\parallel}$ in the upstream side of a marginally quasi-parallel bow shock ($\theta_{Bn} \sim 45^\circ$) in regions where compressive fluctuations in the magnetic field occur.

The percentage of He⁺⁺ particles also affects the VDF distributions making them more spread as the percentage of He⁺⁺ increases in both quasi-parallel and quasi-perpendicular cases. This is a consequence of the enhanced fluctuations in magnetic field which occur when the He⁺⁺ content is higher.

Finally, the results obtained in this work are relevant for the study of IP shocks driven by 567 coronal mass ejections in the context of Parker Solar Probe and Solar Orbiter missions which will 568 collect data with high resolution at different helio-distances close to the Sun. This will allow us to 569 directly compare our simulation models with observations for shocks at different stages of evolution. 570 Future work include an in-depth analysis on the evolution of waves and kinetic instabilities at and 571 near the shock for both quasi-parallel and quasi-perpendicular cases, shock reformation and physical 572 mechanisms concerning particle reflection and heating as well as VDF behavior through the upstream 573 region to determine the helium foreshock extension. 574

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587 **References**

- Aguilar-Rodriguez, E., Blanco-Cano, X., Russell, C. T., Luhmann, J. G., Jian, L. K., & Ramirez
 Velez, J. C. (2011), Dual observations of interplanetary shocks associated with stream interaction
 regions, J. Geophys. Res., 116, A12109, doi:10.1029/2011JA016559
- Anderson, B. J., Denton, R. E., Ho, G., Hamilton, D. C., Fuselier, S. A., Strangeway, R. J. (1996).
 Observational test of local proton cyclotron instability in the Earth's magnetosphere. Journal of Geophysical Research 101, 21527.
- Anderson, B. J., & Fuselier S. A. (1993), Magnetic pulsations from 0.1 to 4.0 Hz and associated
 plasma properties in the Earth's subsolardepletion magnetosheath and plasma depletion layer,J.
 Geophys. Res.,98, 1461-1479, doi:10.1029/92JA02197
- ⁵⁹⁷ Blanco-Cano, X., et al. (2016), Interplanetary shocks and foreshocks observed by STEREO during ⁵⁹⁸ 2007-2010,J. Geophys.Res. Space Physics,121, 992-1008
- Blandford, R. D. & Ostriker, J. P. (1978) Particle acceleration by astrophysical shocks. Astrophysical Journal, Part 2 Letters to the Editor, vol. 221, Apr. 1, 1978, p. L29-L32.
- Broll, J. M., Fuselier, S. A., Trattner, K. J., Schwartz, S. J., Burch, J. L., Giles, B. L., & Anderson,
 B. J. (2018). MMS observation of shock-reflected He⁺⁺ at Earth's quasi-perpendicular bow shock.
 Geophysical Research Letters, 45, 49-55.
- Burgess, D., et al. (2005), Quasi-parallel shock structure and processes, Space Sci. Rev., 118, 205-222.
- Burgess, D. (1987a), Shock drift acceleration at low energies. Journal of Geophysical Research, vol.
 92, Feb. 1, 1987, p. 1119-1130.
- Burgess, D. (1987b), Numerical simulation of collisionless shocks, in Proceedings of International
 Conference on Collisionless Shocks, Balatonfured, Hungary, edited by K. Szego, pp. 89-111,
 Central Research Institute for Physics of Hungarian Academy of Sciences, Budapest, 1987
- Burgess, D.(1989a) Cyclical behavior at quasi-parallel collisionless shocks. Geophys. Res. Lett. 16, 345-349
- Burgess, D.(1989b) Alpha particles in field-aligned beams upstream of the bow shock: Simulations.
 Geophys. Res. Lett. 16, 163-166
- Burgess, D. & Scholer, M. (2015), Collisionless Shocks in Space Plasmas, by David Burgess, Manfred Scholer, Cambridge, UK: Cambridge University Press, 2015
- Burgess, D., Hellinger, P., Gingell, I., & Trávnícek, P. M. (2015). Microstructure in two and three-dimensional hybrid simulations of perpendicular collisionless shocks. Journal of Plasma Physics,82, 905820401.
- Caprioli, D. & Spitkovsky, A. (2014). Simulations of Ion Acceleration at Non-relativistic Shocks. I.
 Acceleration Efficiency. The Astrophysical Journal, Volume 783, Issue 2, article id. 91, 17 pp.
- Caprioli, D., Yi, D., Spitkovsky, A. (2017). Chemical Enhancements in Shock-Accelerated Particles:
 Ab initio Simulations. Physical Review Letters, Volume 119, Issue 17, id.171101
- Enriquez-Rivera, O., X. Blanco-Cano, C. T., Russell, L. K., Jian, J. G., & Luhmann (2010) Mirror
 Mode Structures in the Solar Wind: STEREO Observations, AIP Conference Proceedings 1216,
 276 (2010); doi: 10.1063/1.3395854
- Enriquez-Rivera, O., Blanco-Cano, X., Russell, C. T., Jian, L. K., Luhmann, J. G., Simunac, K. D.,
 & Galvin, A. B. (2013), Mirror-mode storms inside stream interaction regions and in the ambient
 solar wind: A kinetic study, J. Geophys. Res. Space Physics, 118, 17-28
- ⁶³⁰ Fuselier, S. A., & Schmidt, W. K. H. (1994), H^+ and He^{2+} heating at the Earth's bow shock, J. ⁶³¹ Geophys. Res., 99, 11,539-11,546, doi:10.1029/94JA00350

632	Fuselier, S. A., & Schmidt, W. K. H. (1997). Solar wind He ²⁺ ring-beam distributions downstream
633	from the Earth's bow shock, J. Geophys. Res., 102, 11,273-11,280, doi:10.1029/97JA00643
634	Gary, S. P. (1993), Theory of Space Plasma microinstabiblities. Cambridge University Press.
635	Gary, S. P., McKean, M. E., & Winske, D. (1996), Proton temperature anisotropy in the magne-
636	tosheath: Hybrid simulations, Geophys. Res. Lett., 23, 2887-2890.
637	Gedalin, M. (2017). Effect of alpha particles on the shock structure. Journal of Geophysical Research:
638	Space Physics, 122, 71-76
639	Geiss, J., Hirt, P., Leutwyler, H. (1970). On Acceleration and Motion of Ions in Corona and Solar
640	Wind. Solar Physics 12, 458.
641	Gingell et al. (2017), MMS Observations and Hybrid Simulations of Surface Ripples at a Marginally
642	Quasi-Parallel Shock. Journal of Geophysical Research: Space Physics, Volume 122, Issue 11,
643	pp. 11,003-11,017
644	Gosling, J. T. & Thomsen, M. F. (1985) Specularly reflected ions, shock foot thicknesses, and
645	shock velocity determinations in space. Journal of Geophysical Research, vol. 90, Oct. 1, 1985, p.
646	9893-9896
647	Gosling, J. T., Thomsen, M. F., Bame, S. J. & Russell, C. T. (1989) Ion reflection and downstream
648	thermalization at the quasi-parallel bow shock. Journal of Geophysical Research, vol. 94, Aug. 1, 1080 p. 10027 10027
649	1969, p. 10027-10057 Hada T. Oonishi M. Lambága B. & Savoini P. (2003). Shock front nonstationarity of supergritical
650 651	perpendicular shocks, J. Geophys. Res., 108(A16), 1233, doi:10.1029/2002JA009339
652	Hao, Y., Lu, Q., Gao, X., Huang, C., Lu, S., Shan, L., & Wang, S. (2014), He ²⁺ dynamics and
653	ion cyclotron waves in the downstream of quasi-perpendicular shocks: 2-D hybrid simulations, J.
654	Geophys. Res. Space Physics, 119, 3225-3236, doi:10.1002/2013JA019717
655	Hao, Y., Lu, Q., Gao, X. & Wang, S. (2016), Ion Dynamics at a Rippled Quasi-parallel Shock: 2D
656	Hybrid Simulations, The Astrophysical Journal, Volume 823, Issue 1, article id. 7, 11 pp.
657	Hao, Y., Gao, X., Lu, Q., Huang, C., Wang, R., & Wang, S. (2017), Reformation of rippled
658	quasi-parallel shocks: 2-D hybrid simulations, J. Geophys. Res. Space Physics, 122, 6385-6396, doi:10.1002/2017IA024234
000	Inavich F M Gosling I T Scholer M (1984) Correlation between the He/H ratios in unstream
661	particle events and in the solar wind. Journal of Geophysical Research, vol. 89. March 1, 1984, p.
662	1501-1507.
663	Kajdič, P., Blanco-Cano, X., Aguilar-Roriguez, E., Russel, C. T., Jian, L. K., & Luhmann, J.
664	G. (2012), Waves upstream and downstream of interplanetary shocks driven by coronal mass
665	ejections, J. Geophys. Res., 117, A06103, doi:10.1029/2011JA017381
666	Kajdič, P., Preisser, L.; Blanco-Cano, X.; Burgess, D. & Trotta, D. (2019), First Observations of
667	Irregular Surface of Interplanetary Shocks at Ion Scales by Cluster, The Astrophysical Journal Letters, Volume 874, Issue 2, article id 113, 11 pp
000	Kasper I C Stevens M I Lazarus A I Steinberg I T Ogilvie K W (2007) Solar Wind
670	Helium Abundance as a Function of Speed and Heliographic Latitude: Variation through a Solar
671	Cycle. The Astrophysical Journal 660, 901.
672	Krauss-Varban, D. (2005). From theoretical foundation to invaluable research tool: Modem hybrid
673	simulations. Proceedings of the 7 th International Symposium for Space Simulations (ISSS-7), pp.
674	15-18, Kyoto Univ.,arXiv:physics/0610133
675	Lee, M. A., Shapiro, V. D., Sagdeev, R. Z. (1996), Pickup ion energization by shock surfing. Journal
676	of Geophysical Research 101, 4777.
677	Lembège, B., & Savoini, P. (1992), Nonstationarity of a two-dimensional quasiperpendic-
678	ular supercritical collisionless shock by self-reformation, Phys. Fluids B, 4, 3533-3548,
679	doi:10.1063/1.860361
680 681	Lu, Q. M., & Wang, S. (2005), Formation of He ²⁺ shell-like distributions downstream of the Earth's bow shock, Geophys. Res. Lett., 32, L03111, doi:10.1029/2004GL021508
682	Lu, O. M., & Wang, S. (2006). Electromagnetic waves downstream of quasi-nerpendicular shocks
683	J. Geophys. Res., 111, A05204, doi:10.1029/2005JA011319
684	Matthews, A. P. (1994), Current Advance Method and Cyclic Leapfrog for 2D Multispecies Hybrid
685	Plasma Simulations, JCoPh, 112, 102

-16-

686	McKean, M. E., Omidi, N., Krauss-Varban, D. & Karimabadi, H. (1995a), Wave and particle evolution downstream of quasi-perpendicular shocks. Adv. Space Res. 15, 319-22
687	McKeen M E Omidi N Krauss Varban D (1005b) Wave and ion evolution downstream of
688 689	quasi-perpendicular bow shocks. Journal of Geophysical Research 100, 3427.
690	McKean, M. E., Omidi, N., & Krauss-Varban, D. (1996), Magnetosheath dynamics downstream of low Mach number shocks. I. Geophys. Res. 101, 20,013, 20,022, doi:10.1029/961A01461
691	Metachmann II & Classificary K (1002). Simulation of heavy ion ring and shall distributions
692 693	downstream of the bow shock, Geophysical Research Letters, vol. 20, no. 10, p. 987-990.
694	Neugebauer, M., Snyder, C. W. (1966.) Mariner 2 Observations of the Solar Wind, 1, Average
695	Properties. J. Geophys. Res. 71, 4469.
696	Ofman, L., Koval, A., Wilson, L., & Szabo, A. (2019). Understanding the Role of α Particles in
697	Oblique Heliospheric Shock Oscillations, J. Geophys. Res. vol. 124, no. 4, p. 2393-2405.
698	Russell, C. T., & Hoppe, M. (1983), Upstream waves and particles, SSRv,34, 155
699 700	Scholer, M., & Burgess, D. (1992), The role of upstream waves in supercritical quasi-parallel shock reformation, J. Geophys. Res., 97,8319-8326, doi:10.1029/92JA00312
701	Scholer M & Terasawa T (1990) Ion reflection and dissipation at quasi-narallel collisionless
702	shocks. Geophys. Res. Lett. 17, 119-122. doi:10.1029/GL017i002p00119
703	Scholer, M., Fujimoto, M., & Kucharek, H. (1993) Two-dimensional simulations of supercritical
704	quasi-parallel shocks: upstream waves, downstream waves, and shock reformation. J. Geophys. Res 98 18971
705	Schonke N Paschmann G Brinca A I Carlson C W & Lühr H (1000) Ion thermalization in
706	auasi-perpendicular shocks involving reflected ions. J. Geophys. Res. Volume 95. Issue A5
708	Siu-Tania, A., Blanco-Cano, X., Kaidič, P., Aguilar-Rodriguez, E., Russell, C. T., Jian, L.
709	K. & Luhmann, J. G. (2015). Low-frequency waves within isolated magnetic clouds and
710	complex structures: STEREO observations, J. Geophys. Res. Space Physics, 120, 2363-2381.
711	doi:10.1002/2014JA020568
712	Southwood, D. J., Kivelson, M. G. (1993). Mirror instability. I-Physical mechanism of linear insta-
713	bility. Journal of Geophysical Research 98, 9181.
714	Sundberg, T., Haynes, C. T., Burgess, D., & Mazelle, C. X. (2016). Ion acceleration at the quasi-
715	parallel bow shock: Decoding the signature of injection. Astrophysical Journal,820, 21
716	Su, Y., Lu, Q., Gao, X., Huang, C., & Wang, S. (2012a), Ion dynamics at supercritical quasi-parallel
717	shocks: Hybrid simulations, Phys. Plasmas, 19, 092108.
718	Su, Y., Lu, Q., Huang, C., Wu, M., Gao, X., & Wang, S. (2012b), Particle acceleration and generation
719	of diffuse superthermal ions at a quasi-parallel collisionless shock: Hybrid simulations, J. Geophys.
720	Res., 117, A08107, doi:10.1029/2012JA017736
721	Trattner, K. J., & Scholer, M. (1991), Diffuse alpha particles upstream of simulated quasi-parallel
722	supercritical collisionless shocks. Geophysical Research Letters, vol. 18, Oct. 1991, p. 1817-1820.
723	Trattner, K. J., & Scholer, M. (1993) Distributions and thermalization of protons and alpha particles
724	at collisionless quasi-parallel shocks. Annales Geophysicae, Vol. 11, No. 9, p. 774-789
725	Trattner, K. J. & Scholer, M. (1994) Diffuse minor ions upstream of simulated quasi-parallel shocks.
726	Journal of Geophysical Research, vol. 99, no. A4, p. 6637-6650
727	Trotta, D. & Burgess, D. (1994) Electron acceleration at quasi-perpendicular shocks in sub and
728	supercritical regimes: 2D and 3D simulations. Monthly Notices of the Royal Astronomical Society,
729	Volume 482, Issue 1, p.1154-1162
730	Tsubouchi, K., Nagai, T., & Shinohara, I. (2016), Stable ring beam of solar wind He ²⁺ in the magnetosheath J. Geophys. Pers Space Physics 121, 1223, 1248, doi:10.1002/201514.021760
731	magnetosneaui, J. Ocophys. Res.space Physics, 121, 1255-1248, doi:10.1002/2015JA021/69
732	Wilson, L. B. III (2010), Low Frequency waves at and Upstream of Collisionless Shocks, in
733	mashington DC American Geophysical Onion Geophysical Monograph Series, Volume 216, pp. 269-291
735	Winske, D., & Leroy, M. M. (1985), Hybrid simulation techniques applied to the Earth's bow shock.

in Computer Simulation of Space Plasmas, edited by H. M. T. Sato, pp. 255-278, Terra Sci., Tokyo,
 Japan.

- Wurz, P. (2005), Solar wind Composition, Proceedings of the 11th European Solar Physics Meeting
 "The Dynamic Sun: Challenges for Theory and Observations" (ESA SP-600). 11-16 September
 2005, Leuven, Belgium. Editors: D. Danesy, S. Poedts, A. De Groof and J. Andries."
- Yang, Z. W., Lu, Q. M., Lembège, B., & Wang, S. (2009), Shock front nonstationarity
- and ion acceleration in supercritical perpendicular shocks, J. Geophys. Res., 114, A03111,
 doi:10.1029/2008JA013785
- Yang, Z. W., Lembège, B., & Lu, Q. M. (2012), Impact of the rippling of a perpendicular shock front
 on ion dynamics, J. Geophys. Res., 117, A07222, doi:10.1029/2011JA017211



Figure 5. Plots corresponding to the simulation with $\theta_{Bn}=15^{\circ}$ at the time when the shock arrives to x=250 d_i : Contour plot of total magnetic field a) and magnetic field b) along two horizontal cuts at the upper (blue line) and lower (red line) dashed lines in panel a) for the case with 1% of He⁺⁺ particles. Panels c) and d) show the same results for the case with 10% of He⁺⁺ particles. The VDF's for both species for the case with 10% of He⁺⁺ particles contained inside the left (upstream side) magenta box on panel c) are shown in panels e). The same results for the right (downstream side) magenta box on panel c) are shown in panels f). The color bar in VDF's indicates the particle counts.



Figure 6. Plots corresponding to the simulation with $\theta_{Bn}=65^{\circ}$ at the time when the shock arrives to x=250 d_i : Contour plot of total magnetic field a) and magnetic field b) along two horizontal cuts at the upper (blue line) and lower (red line) dashed lines in panel a) for the case with 1% of He⁺⁺ particles. Panels c) and d) show the same results for the case with 10% of He⁺⁺ particles. The VDF's for both species for the case with 10% of He⁺⁺ particles contained inside the left (upstream side) magenta box on panel c) are shown in panels e). The same results for the right (downstream side) magenta box on panel c) are shown in panels f). The color bar in VDF's indicates the particle counts.



Figure 7. Contour plots of protons and He⁺⁺ densities corresponding to the simulations with $\theta_{Bn} = 15^{\circ}$ for 1% a) and 10% b) of He⁺⁺ particles and with $\theta_{Bn} = 65^{\circ}$ for 1% c) and 10% d) of He⁺⁺. The time of the plots correspond to those magnetic field magnitude plots in Figures 5 and 6.



Figure 8. Magnetic field and proton temperature anisotropy $(T_{\perp}/T_{\parallel})$ cuts along downstream region at $y = 200 \ d_i$ corresponding to simulations with $\theta_{Bn} = 65^\circ$ for 1% a) and 10% b) of He⁺⁺. Temperature anisotropy as well as the parameters (M = 1 + 1/ β_{\perp}) in red and (IC = 1 + $\beta_{\parallel}^{0.5}$) in blue are shown in the same panels. The condition for the growing of the mirror instability is fulfilled by the threshold $T_{\perp}/T_{\parallel} > M$, the corresponding condition for ion/cyclotron instability is $T_{\perp}/T_{\parallel} < IC$. The time of the plots correspond to those in Figure 7.