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### Phase Noise Can Induce Stochastic Resonance?

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We investigated stochastic resonance (SR) of ac-driven electroconvection (EC) in nematic liquid crystals by employing the phase noise of the ac field. The phase noise smoothly varies the threshold of EC, as the amplitude noise does it. Surprisingly, a kind of phase stochastic resonance (PSR) is discovered in appropriately colored phase noises; thus, it provides nonmonotonic behavior of the threshold in which a peak of the pattern amplitude of EC is found as a function of the phase noise intensity. The colored and white phase noises are discussed for understanding the PSR.

Noise-induced phenomena have been extensively investigated in various fields, in order to understand the role of noise [1-3]. Generally, considering the fluctuations of material and/or control parameters in natural and artificial systems, noise (as the origin of the fluctuations) should be removed or minimized for desirable treatments. However, since Benzi et al. discovered stochastic resonance (SR) [4], noise has been reconsidered as a factor of constructive roles in control of order-disorder and enhancement of the output of various systems [1-3]. In particular, the idea of the enhancement of the output using an optimal noise level (not too small and not too large) has triggered useful applications in neuroscience [5], biophysics [6], photonics [7], mechanics [8], and image processing [9]. The crucial point of these SR phenomena is that a desirable signal can be maximized by controlling noise levels. Contrarily, the minimization of the signal-noise ratio (SNR) was also found in nervous systems [10-14] and nonequilibrium dissipative systems [15]; by analogy with SR, the phenomenon has been called inverse stochastic resonance (ISR) [11-15]. Note that the aforementioned SR and ISR occur in the *amplitude* noise added to the deterministic signal. Recently, Chowdhury et al. discovered random *phase* deviation-induced SR in a nanoelectromechanical membrane system [16], which was named as *phase stochastic resonance* (PSR). In PSR, additional phase noise in a deterministic signal plays a crucial role in the enhancement of the output, instead of the amplitude noise in conventional SR and ISR.

In this study, we address ac-driven electroconvection (EC) in a nematic liquid crystal (NLC). In principle, EC can be induced by applying an ac electric field across a thin layer (typically,  $d = 10-100 \,\mu\text{m}$ ). The basic mechanism of EC was well explained in the earlier studies by Carr [17] and Helfrich [18]. The director fluctuations of an NLC resulting from thermal noise can be reinforced by a material flow via the Coulomb force acting on space charges that are focused by the electric anisotropy of an NLC; when the Coulomb force overcomes the viscoelastic and dielectric restoring forces at a critical threshold voltage  $V_c$ , electrohydrodynamic instability arises in the NLC layer; it provides a regular roll-pattern EC [i.e., so-called Williams domain (WD)] [19,20]. Our question is that how a weak signal below the threshold voltage can induce EC under additional phase noise in the signal.

In this Letter, we present an unexpected PSR found in EC by controlling phase noise; the evolution of EC patterns and

the threshold of EC are examined as a function of a random phase deviation of noise. The reader will find that the PSR appears only in *colored noise* adjusted appropriately (e.g., through low-pass filters of noise generators).

A typical NLC [p-methoxybenzylidene-p'-n-butylaniline (MBBA)] was used in this study; the planarly-aligned NLC sandwiched between two parallel transparent electrodes (indium tin oxide) was characterized by a conductivity of  $\sigma_{\perp} = 2.01 \times 10^{-8} \,\Omega^{-1} \text{m}^{-1}$  and a dielectric constant of  $\varepsilon_{\perp} = 5.14$  (at T = 25 °C). Here,  $\perp$  denotes the orientation perpendicular to the initial director  $n_0$  of the NLC [ $n_0 = (1,0,0)$ ]. The ac voltage V(t) was applied across the thin slab of the NLC having a thickness  $d = 50 \,\mu\text{m}$  and a lateral (active) size  $L_x \times L_y = 1 \times 1 \,\text{cm}$ :

$$V(t) = V_0 \cos\{\omega_0 t + \phi_{N0} \xi(t)\} + A_{N0} \xi(t), \qquad (1)$$

where  $A_{N0}$  indicates the noise intensity for the amplitude deviation of  $V_0$  ( $A_{N0}=0$  in this study). For the phase deviation, a Gaussian-type noise  $[-1 < \xi(t) < 1]$  was externally introduced into a wave generator (WF1974, NF);  $\phi_{N0}$  indicates the magnitude of the random phase deviation, which is a main control parameter in this study ( $0 \le \phi_{N0} \le \pi$ ). Colored noises  $\xi(t)$  characterized by the autocorrelation time  $\tau_N$  [=  $1/(2\pi f_c)$ ] as well as white noise ( $\tau_N \to 0$ :  $f_c \to \infty$ ) were used; the cutoff frequency  $f_c$  of the noise was controlled by the low-pass filters of a synthesizer (7075, Hioki) [15]. The standard shadowgraph method for EC was used for optical observations and measurements [20]; the EC patterns and their dynamics were observed in the xy plane by using a computer-controlled image software system (Scion Image) and an image-capture board (Scion Corp., PCI-VE5) together with a charge-coupled device camera (Sony, XC-75) mounted on a polarizing microscope (Meijitech, ML9300). All measurements were performed at a fixed temperature of T = 25 °C by using an electrothermal control system (TH-99, Japan Hightech) [15].

First, to see the role of the phase noise to EC, the evolution of EC patterns was observed by increasing  $\phi_{N0}$ , as shown in Fig. 1. For fixed values of the ac frequency  $f_0 = 2$  kHz and ac voltage  $V = V_{rms} = 35.6$  V ( $V_0 = 50.3$  V) slightly below  $V_c = 37.3$  V, a rest state is set at  $\phi_{N0} = 0$  [Fig. 1(a)]. By increasing  $\phi_{N0}$ , the rest state evolves into a typical WD at  $\phi_{N0} = 0.873$  rad [Fig. 1(b)], and then into a fluctuating WD (FWD) at  $\phi_{N0} = 1.75$  rad [Fig. 1(c)]. Certainly, owing to the phase noise ( $\phi_{N0} \neq 0$ ), EC occurs in spite of a weak voltage below  $V_c(\phi_{N0} = 0)$ . Furthermore, the FWD reenters a normal WD at  $\phi_{N0} = 2.41$  rad, as shown in Fig. 1(d); then, it successively changes into the rest state at  $\phi_{N0} = 2.62$  rad [Fig. 1(e)]. This novel EC evolution driven by the phase noise has been first found in the present study. In general, a rest state (at  $V < V_c$ ) successively evolves into a WD, an FWD, and a grid pattern, and then finally into a developed turbulent state with the increase of  $V_0$  ( $A_{N0} = 0$  and  $\phi_{N0} = 0$ ) [21], or with the increase of colored amplitude noise  $A_{N0}$  ( $\phi_{N0} = 0$  and a fixed  $V_0$ ) [22]; furthermore, the reverse evolution is found with the decrease of  $V_0$  [21,23], or with the increase of white amplitude noise  $A_{N0}$  ( $\phi_{N0} = 0$  and a fixed  $V_0$ ) [22]. As displayed in the right column of Fig. 1, V(t) applied to each pattern in the left column is modulated by the magnitude of  $\phi_{N0}$ . Note that the optimal phase noise for the most developed EC state [e.g., Fig. 1(c)] exits, and the same rest state [i.e., Fig. 1(a) and 1(e)] or similar WDs [i.e., Fig. 1(b) and 1(d)] appear despite different V(t) modulated by different phase deviations (with a same value of  $V_{rms}$ ). Most importantly of all, this result was obtained by using a colored noise  $\xi(t)$  having an appropriate cutoff frequency (e.g.,  $f_c = 2$  kHz in this study).

Next, to elucidate the evolution of EC mentioned above, we measured the threshold  $V_c$  of EC as a function of  $\phi_{N0}$  (Fig. 2) by using the colored noise ( $f_c = 2$  kHz); additionally, different  $f_c$ -noises  $\xi(t)$  including white noise ( $f_c \to \infty$ ) were also tested. Obviously, the colored phase noise ( $f_c = 2$  kHz) causes nonmonotonic behavior of  $V_c$ ; there exists a minimal  $V_c$  at  $\phi_{N0}^* \sim 1.75$  rad. Accordingly, for the colored noise ( $f_c = 2$  kHz), the WD and FWD [Figs. 1(b)-1(d)] were able to be observed at appropriate values of  $\phi_{N0}$  (0.7 <  $\phi_{N0}$  < 2.45 rad) in spite of the application of low V [<  $V_c(\phi_{N0} = 0) = 37.3$  V]; furthermore,

a rest state was found for  $\phi_{N0} < 0.7$  rad [Fig. 1(a)] and also for  $\phi_{N0} > 2.45$  rad [Fig. 1(e)]. On the other hand, the white phase noise monotonically increases  $V_c$ , whereas an extremely colored noise ( $f_c = 500$  Hz), for which high frequencies (> 500 Hz) is filtered out, monotonically decreases  $V_c$ . Therefore, by increasing  $\phi_{N0}$ , the white noise and the extremely colored noise provide the conventional pattern evolutions; e.g., no reentrance of the WD or rest state is found.

To understand this unusual phenomenon, we examined the power spectra of the voltages  $V(\phi_{N0})$  modulated by the colored noise ( $f_c = 2 \text{ kHz}$ ); Fig. 3(a) shows those of the voltages V(t) displayed in Fig. 1. By increasing  $\phi_{N0}$ , the Fourier frequency components concentrated around the carrier frequency  $f_0$  (at  $\phi_{N0} = 0$ ) become gradually scattered with generating lower and higher frequency ones. The studies of EC under the combined ac fields [24] show that the voltages contribute to destabilizing or stabilizing EC, depending on frequencies lower or higher than a characteristic frequency fcd (~ 2.3 kHz in this study) dividing the conduction and dielectric regimes for EC [20]. Accordingly, in the case of the colored phase noise, the additional low frequency effect may be dominant for small  $\phi_{N0}$  ( $<\phi_{N0}^*$ ), resulting in the decrease of  $V_c$ ; contrastively, the additional high frequency effect may be dominant for large  $\phi_{N0}$  (>  $\phi_{N0}^*$ ), yielding the increase of  $V_c$ . These competitive effects may determine  $V_c$  (Fig. 2) as well as EC states (Fig. 1). Furthermore, the two effects are more clearly revealed in Fig. 3(b); the power sums,  $\Sigma P(f < f_{cd})$  and  $\Sigma P(f > f_{cd})$ , indicate the destabilization and stabilization effects on EC, respectively; the former shows nonmonotonic behavior responsible for the unusual pattern evolution (Fig. 1 and Fig. 2), although  $\phi_{N0}^*$  is slightly larger than that in Fig. 2. On the other hand, the white noise  $(f_c \to \infty)$  and extremely colored noise  $(f_c = 500 \text{ Hz})$ showed, respectively, high frequency-dominant effect and low frequency-dominant one for all ranges of  $\phi_{N0}$ ; e.g., at a fixed  $\phi_{N0} = 1.75$  rad, compare with one another in the voltages and their power spectra having different  $f_c$  (Fig. 4). As a result, the white noise and extremely colored noises give rise to the monotonic increase and decrease of  $V_c$ , respectively (Fig. 2). Therefore, the reason why the different states occur for different  $f_c$  (Fig. 2) can be deduced: e.g., at fixed values of  $\phi_{N0} = 2.41$ rad and V = 37.3 V [i.e, (d) in Fig. 2], a rest state ( $V << V_c$ ) for white ( $f_c \to \infty$ ), a WD ( $V \approx V_c$ ) for  $f_c = 2$  kHz, and turbulence  $(V >> V_c)$  for  $f_c = 500$  Hz. In other words, the appropriately colored noise ( $f_c = 2$  kHz) can give an optimal phase deviation [Fig. 1(c)] from the original phase  $\omega_0 t$  of the carrier signal [Fig. 1(a)] for developing EC. This nonmonotonic behavior of  $V_c(\phi_{N0})$  is similar to the threshold variation in the amplitude noise-induced  $V_c(A_{N0})$  [15,22]; however, the underlain mechanisms are completely different from each other.

Owing to the contribution of high frequencies, chevron patterns characterized for high frequencies around  $f_{cd}$  were observed at  $V_c$ , instead of WDs [20,24,25]: e.g.,  $\phi_{N0} > 2.7$  rad for the colored noise  $f_c = 2$  kHz and  $\phi_{N0} > 1.8$  rad for the white noise; furthermore, owing to the contribution of low frequencies, breathing WDs often found at low frequencies (< 10 Hz) [24] were observed for the extremely colored noise ( $f_c = 500$  Hz): e.g.,  $\phi_{N0} = 2.25$  rad; moreover, more complicated patterns such as defect lattices [26] appeared by the phase noise, which have not been understood in the standard EC theory [17-20].

In addition, to evaluate the phase noise-induced threshold shift as an SR phenomenon, the pattern amplitude of EC was measured as a function of  $\phi_{N0}$ ; a space-time map (STM) [Fig. 5(a)] was constructed by successively placing a one dimensional fixed line (X) arbitrarily selected in two dimensional images [e.g., Fig. 1(b)] with an identical time interval ( $\Delta t = 1$  s in this study). Under the same conditions for Fig. 1 ( $f_0 = 2$  kHz and V = 35.6 V), the present STM was obtained by a successively steplike increase and decrease of  $\phi_{N0}$  ( $\Delta\phi_{N0} = 0.174$  rad for every 10 s), as shown in Fig. 5(a); the one dimensional lines were placed for 10 s at every  $\phi_{N0}$ . By increasing  $\phi_{N0}$  from 0 to  $\pi$ , a pattern evolution appears: a rest state  $\to$  WD  $\to$  WD  $\to$  a rest state; furthermore, by decreasing  $\phi_{N0}$  from  $\pi$  to 0, the same pattern evolution is observed. Accordingly, Fig. 5(b) shows the variation of the pattern amplitude I of EC as a function of  $\phi_{N0}$ ; the normalized intensity I corresponds to the SNR. In Fig. 5(b), one finds a kind of SR (showing a peak of I) with respect to a deterministic signal-induced EC that cannot be induced by the weak intensity of the signal (i.e., below  $V_c$ ); the difference of the magnitude

of *I* between increasing and decreasing  $\phi_{N0}$  depends on the detail of EC [e.g., the optical intensity fluctuation resulting from motion of defects in Fig. 5(a); and see also Fig. 1(c)].

Finally, we have checked the present PSR by simulating the one dimensional Carr-Helfrich equations for EC [17,18,20]:

$$\dot{q} + \frac{q}{\tau} + \sigma_H \frac{V(t)}{d} \psi = 0, \tag{2}$$

$$\dot{\psi} + \lambda \left[ E_0^2 + \left( \frac{V(t)}{d} \right)^2 \right] \psi + \frac{q}{\eta} \frac{V(t)}{d} = 0.$$
 (3)

Here, q and  $\psi$  denote, respectively, the space-charge density and the curvature of the director ( $\psi = \partial \varphi/\partial x$ ) for the angle  $\varphi$  of the director deviation from the x axis (i.e.,  $\varphi = 0$  for  $\mathbf{n}_0$ ); all parameters  $\tau$ ,  $\sigma_H$ ,  $\lambda$ ,  $\eta$ , and  $E_0$  are determined by the detail of the NLC (MBBA in this study). In the numerical simulation of Eqs. (2) and (3) for the linear stability analysis [27], the nonmonotonic threshold behavior is successfully reproduced as a function of  $\phi_{N0}$  ( $f_c = 2$  kHz), as shown in Fig. 5(c).

In conclusion, a kind of PSR has been discovered in the EC system by employing appropriately colored phase noise; thus, it provides nonmonotonic behavior of the threshold of EC. The white phase noise and extremely colored phase noise cause monotonic increase and decrease of the threshold of EC, respectively. In the present PSR, the bell-shaped behavior of the EC pattern amplitude (resulting from the reversed bell-shaped threshold of EC) is found as a function of the phase-noise deviation; this result is originated from appropriate Fourier frequency components generated by the phase noise. In the EC system, competition between destabilization and stabilization effects on EC play a role in the PSR; the former effect occurs through the lower frequencies of noise spectra than a characteristic frequency for EC dividing conduction and dielectric regimes, whereas the latter one does through higher frequencies. The reciprocal effects can be controlled by the phase-noise deviation, and they can induce EC in spite of weak voltages below the threshold one; in particular, note that in colored phase noise adjusted appropriately with respect to the detail of EC, the PSR can be found.

PSR reported in the recent research [16] and the present study may enable various applications such as signal transmission and order-disorder control [3] together with SR [4-9] and ISR [10-15]; furthermore, the mixed phase-amplitude deviations  $[A_{N0} \neq 0 \text{ and } \phi_{N0} \neq 0 \text{ in Eq. (1)}]$  of signals are also expected in future research [16].

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- 27)  $V_c$  was obtained by automatic determination of  $\psi(t) = \psi_0 \exp(\alpha t)$  first going to have a positive growth rate  $(\alpha > 0)$  through steplike increase of V with  $\Delta V = 0.1$  V; i.e., the transition point from the relaxation to the rise of the director.

## **Figure Captions**

- FIG. 1. (Color online) Evolution of EC patterns in the smooth increase of the phase deviation  $\phi_{N0}$  (at fixed values of  $V_0 = 50.3$  V and  $f_0 = 2$  kHz); left column: optical EC patterns for  $\phi_{N0} = 0$  (a), 0.873 (b), 1.75 (c), 2.41 (d), and 2.62 rad (e); right column: applied V(t) for each corresponding EC pattern. A colored noise ( $f_c = 2$  kHz) was used for the random phase deviation  $\phi_N = \phi_{N0}\xi(t)$ . See also Fig. 2.
- FIG. 2. (Color online) Threshold voltage  $V_c$  of EC as a function of the phase deviation  $\phi_{N0}$  of colored ( $f_c = 500$  Hz and 2 kHz) and white ( $f_c \to \infty$ ) noises. The thick arrow indicates increasing  $\phi_{N0}$  (at a fixed V = 35.6 V  $< V_c = 37.3$  V) for the evolution of EC, and (a)-(e) represent ( $\phi_{N0}$ , V) for corresponding patterns in displayed in Fig. 1.
- FIG. 3. (Color online) (a) Power spectra of V(t) modulated by a phase noise ( $f_c = 2 \text{ kHz}$ ) at fixed values of  $V_0 = 50.3 \text{ V}$  and  $f_0 = 2 \text{ kHz}$  for various phase deviations  $\phi_{N0}$ , (b) Power sums  $\Sigma P(f < f_{cd})$  for the destabilization effect on EC and  $\Sigma P(f > f_{cd})$  for the stabilization one ( $f_{cd} = 2300 \text{ Hz}$ ). The solid lines in (b) are a guide for the eye.
- FIG. 4. (a) Applied voltages V(t) modulated by  $\phi_{N0} = 1.75$  rad (at an identical  $V_0 = 50.3$  V) for the noise cutoff frequencies  $f_c = \infty$  (white noise), 2 kHz, and 500 Hz, (b) Power spectra of the corresponding V(t); note the change of Fourier components around the carrier frequency  $f_0 = 2$  kHz. These three kinds of V(t) induce a rest state [Fig. 1(a)], an FWD [Fig. 1(c)], and a turbulent state, respectively.
- FIG. 5. (Color online) (a) Space-time map (STM) for the EC-pattern evolution and (b) optical pattern intensity  $I(\phi_{N0})$  with increasing and decreasing  $\phi_{N0}$  (at fixed values of  $V_0 = 50.3$  V and  $f_0 = 2$  kHz); the STM optically observed was transformed into a normalized intensity I indicating the pattern amplitude of EC after averaging in X and a smoothing process of I(t). (c) Calculated threshold voltage  $V_c$  as a function of  $\phi_{N0}$ . For simulating Eqs. (2) and (3), the MATLAB R2018b was used with the Runge-Kutta method;  $V_c$  was determined at a colored noise ( $f_c = 2$  kHz) provided by a frequency filtering program; compare it with the experimental one provided in Fig.2.

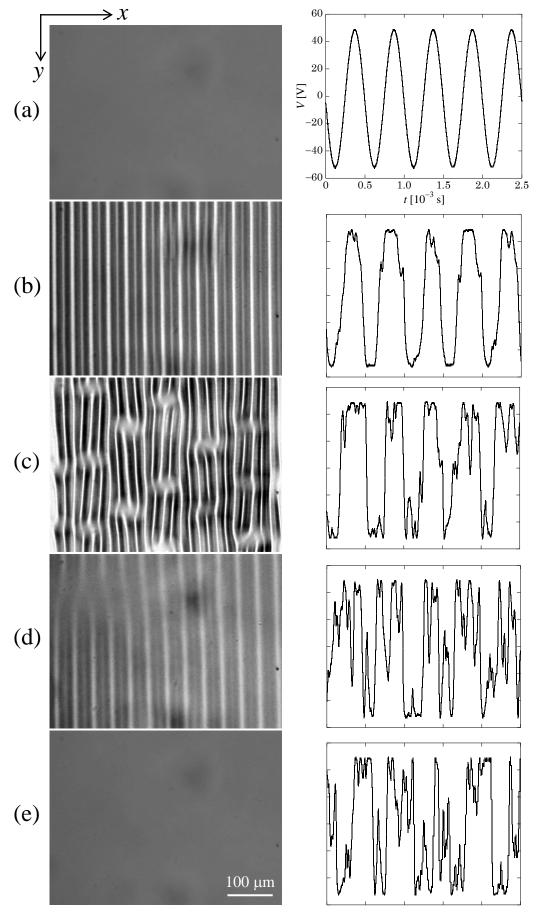


Fig. 1

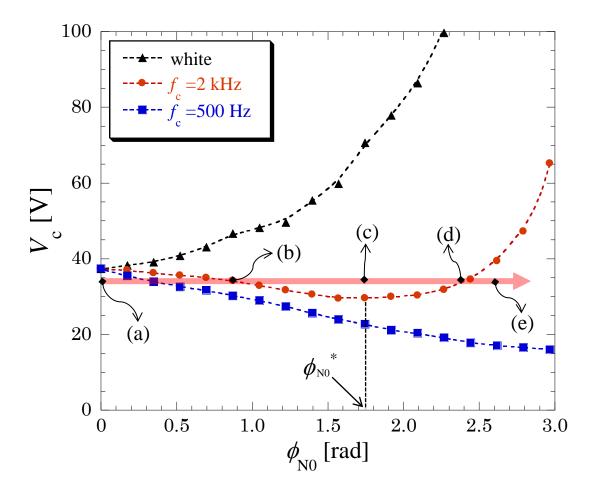


Fig. 2

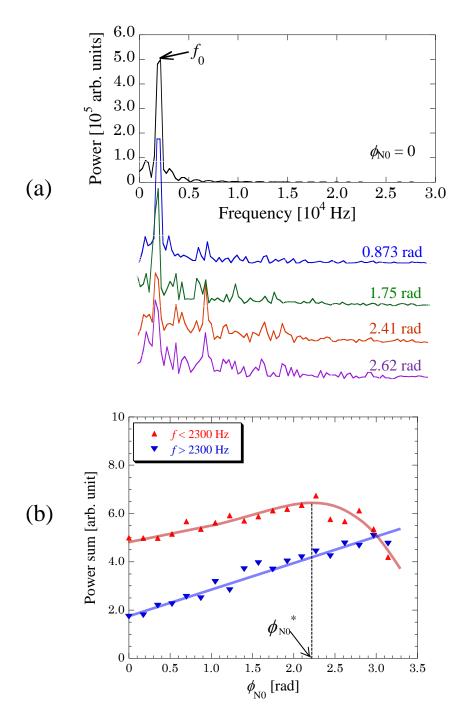


Fig. 3

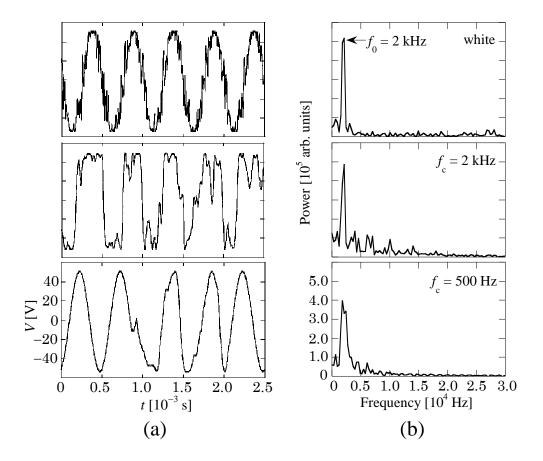


Fig. 4

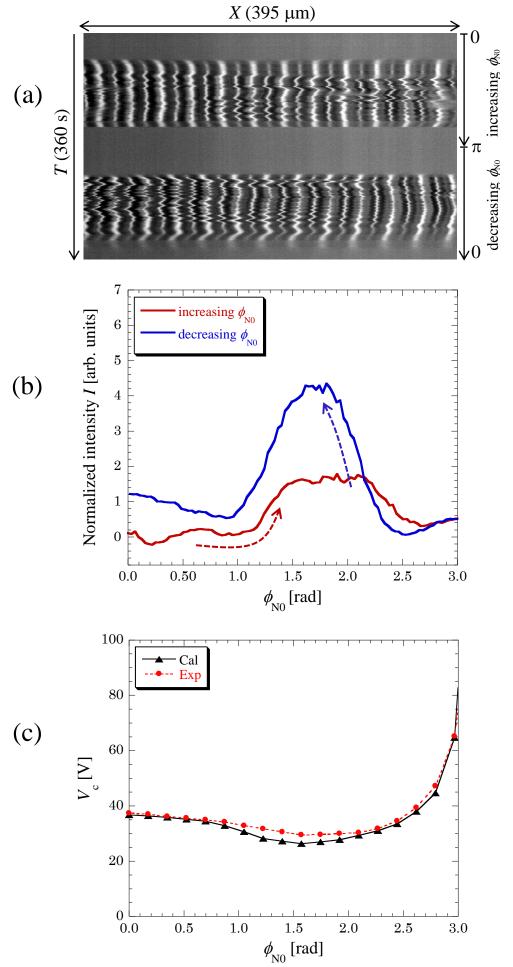


Fig. 5