# **A Revised Computational Neuroanatomy for Motor Control**

| 2  |  | Shlomi Haar <sup>1</sup> , Opher Donchin <sup>2,3</sup>                          |
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| 3  | 1.   | Department of BioEngineering, Imperial College London, UK                        |
| 4  | 2.   | Department of Biomedical Engineering, Ben-Gurion University of the Negev, Israel |
| 5  | 3.   | Zlotowski Center for Neuroscience, Ben-Gurion University of the Negev, Israel    |
| 6  |  |  |
| 7  | Corresponding author: Shlomi Haar (s.haar@imperial.ac.uk)  |  |
| 8  | Imperial College London, London, SW7 2AZ, UK   |  |
| 9  |  |  |
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# 15 Abstract

We discuss a new framework for understanding the structure of motor control. Our approach 16 17 integrates existing models of motor control with the reality of hierarchical cortical processing and the 18 parallel segregated loops that characterize cortical-subcortical connections. We also incorporate the recent 19 claim that cortex functions via predictive representation and optimal information utilization. Our 20 framework assumes each cortical area engaged in motor control generates a predictive model of a different aspect of motor behavior. In maintaining these predictive models, each area interacts with a different part 21 of the cerebellum and basal ganglia. These subcortical areas are thus engaged in domain appropriate 22 system identification and optimization. This refocuses the question of division of function among different 23 24 cortical areas. What are the different aspects of motor behavior that are predictively modelled? We suggest that one fundamental division is between modelling of task and body while another is the model of state 25 and action. Thus, we propose that the posterior parietal cortex, somatosensory cortex, premotor cortex, 26 and motor cortex represent task state, body state, task action, and body action, respectively. In the second 27 part of this review, we demonstrate how this division of labor can better account for many recent findings 28 of movement encoding, especially in the premotor and posterior parietal cortices. 29

## 30 Introduction

Motor control is perhaps one of the most central and complex tasks of the brain. For example, 31 while driving, we must move our arms, legs, and gaze in a coordinated fashion to control the movement 32 33 of our car while also assessing its movement and that of the other cars around us. For that to happen our brain needs to integrate sensory and motor information about our own body's state (joint configuration) 34 and the task state (car direction and speed) in order to plan the required action within the task (like taking 35 36 a sharp turn while staying on the road and avoiding other cars) and the body action to enable it (turning the wheel with the hands and controlling the gas and brake pedals with the foot). This requires predictive 37 coding of the outcome of movements at both the task and body level, accounting for the multiple costs of 38 the task (maintaining the speed limit and proper distance, avoiding rapid acceleration or deceleration) and 39 the body (keeping the arms in comfortable positions while maintaining the ability to respond). As such, 40 the neuroanatomy of motor control involves multiple cortical and subcortical regions across the brain. For 41 decades, theories of the motor functions have failed to address how these different regions simultaneously 42 coordinate the body within the task. We will extend existing theories regarding the roles of the cerebral 43 cortex, the cerebellum and the basal ganglia to address this gap. The historical focus on these three areas 44 (e.g., Kornhuber, 1971; Mogenson et al., 1980) is justified largely because they are tightly interconnected 45 and have been heavily studied in the context of reaching and grasping movements, finger movements, eye 46 47 movements, and locomotion. Of course, other areas - most obviously the spinal cord, red nucleus, and 48 thalamus - play key roles in motor control.

49 Kenji Doya proposed an influential hypothesis that delineated the roles of these different brain structures based on computational principles (Doya, 1999, 2000). Doya suggested that the cerebellum, the 50 basal ganglia, and the cerebral cortex are specialized for different types of learning: supervised learning, 51 reinforcement learning, and unsupervised learning, respectively. Doya addressed the way that these 52 53 different learning rules might shape the roles each motor area played in motor behavior. His view was that 54 the learning rules would lead the cerebellum to form internal models, the basal ganglia to play a role in 55 action selection and the cortex to form representations of state and action. Different versions of this idea of the functions of these different areas have served the field well for many years. However, they were 56 brought together particularly powerfully when they were connected to ideas of optimal feedback control 57 introduced into the field by Emo Todorov and Michael Jordan. The optimal feedback control theory for 58 59 motor coordination (Todorov and Jordan, 2002) suggested a mathematical approach for motor control which formalized the relationship between motor commands, task goals, sensory-motor noise, and sensory 60 feedback. In this formulation, motor commands were chosen to achieve task goals based on an estimate of 61 state that combined sensory feedback with the system's prediction of the current state. The task goals are 62 63 represented as a cost-to-go function. The cost-to-go function ascribes the current state a value that combines how well it leads to achievement of task goals and how much effort will be required to achieve 64 65 them. Reza Shadmehr and John Krakauer (2008) used Todorov's optimal feedback control framework as the basis for a computational neuroanatomy of motor control. In their scheme, primary- and pre-motor cortices generate motor commands, while the basal ganglia evaluate the cost-to-go function, and the cerebellum predicts upcoming state. In recent years, the term computational neuroanatomy mostly refers to algorithm-based quantitative approaches to image processing and 3D reconstruction associated with the study of neuroanatomy. Here we use it in the same sense used by Shadmehr and Krakauer (2008) to describe the identification of distinct motor control processes from computational models and their mapping to different brain regions.

73 In this paper, we try to extend these influential theories in two key ways. First, we suggest that 74 each of the cortical areas involved in motor control may be implementing the model described by Shadmehr and Krakauer (2008), based on anatomical evidence that each cortical region forms its own 75 76 loops with the basal ganglia and the cerebellum. Second, we suggest that these different cortical areas may 77 be interacting in ways that are consistent with existing influential perspectives on the cortical hierarchy, that focus on the cortex's role in representing prediction and optimal information utilization (Clark, 2013; 78 Kanai et al., 2015). These two extensions combine to produce a new, coherent model of the neuroanatomy 79 80 of motor control.

### 81 Multiple cortical loops with the basal ganglia and the cerebellum

Compelling anatomical evidence supports the existence of parallel loops connecting cortical areas 82 with both the basal ganglia and cerebellum. The loops are characterized by a high degree of topographic 83 specificity (Middleton and Strick, 1997, 2001). Most areas of cortex receive input from dedicated, separate 84 regions of the basal ganglia, and the most prominent input to a given region of the basal ganglia derives 85 86 from the same area of cerebral cortex to which it projects. Most cortical areas have a similar loop with 87 cerebellum (Bostan and Strick, 2018; Dum and Strick, 2003; Kelly and Strick, 2003; Middleton and Strick, 1997). Neuroanatomical studies have demonstrated that cerebellar output reaches many areas of the cortex, 88 89 including the posterior parietal cortex and regions of prefrontal cortex (see Bostan et al., 2013, for review). 90 The primary somatosensory cortex has projections to the basal ganglia (Kunzle, 1977) and the cerebellum (Middleton and Strick, 1998). Gerbella et al., (2016) suggested that cortical regions connected one to 91 another (such as specific sectors of the premotor and parietal cortex) also have convergent projections to 92 93 the same striatal sectors. But the figures for individual monkeys suggest that it is a group effect due to 94 inter-subject variability in the projections, and within each monkey there is only partial overlap in the striatal sectors (e.g. case 62, Figures 10 and 11). Neuroimaging is lacking the resolution to address the 95 different pathways, yet, human neuroimaging studies also support the notion that different cortical regions 96 are bidirectionally connected to distinct areas of the cerebellum and the basal ganglia (Buckner et al., 2011; 97 Choi et al., 2012; O'Reilly et al., 2010; Seitzman et al., 2020; Yeo et al., 2011). 98

A model based on this notion of parallel segregated loops of different cortical areas with the basalganglia and the cerebellum was first presented by James Houk, who refers to it as a distributed processing

101 module (DPM) (Houk, 2001, 2005; Houk et al., 2007). According to Houk, a given area of cortex together 102 with its subcortical loop(s) forms a DPM and the different distributed modules communicate with each 103 other through cortico-cortical connections. Cognitive neuroscientist Takashi Hanakawa suggested a model 104 similar to the DPM model to explain how the premotor cortex can serve as a gateway between motor and 105 cognitive networks (Hanakawa, 2011). The Hanakawa model is consistent with the model we present 106 below, although our focus is on the roles of premotor and parietal cortices in task-body integration where 107 the Hanakawa model focuses on motor–cognitive integration.

108 Recent findings of direct connections between the basal ganglia and the cerebellum (Bostan and Strick, 2018; Quartarone et al., 2020) adds complexity to the view of parallel segregated loops. However, 109 one prominent theory proposes that the newly found connections are part of an integrated network which 110 balances the relative influence of the basal ganglia and the cerebellum without changing their respective 111 roles (Bostan and Strick, 2018; Taylor and Ivry, 2014). More controversially, there are recent reports of 112 actual reward processing in the cerebellum (Medina, 2019) based on findings of reward signals in 113 cerebellar climbing fibers (Heffley et al., 2018; Kostadinov et al., 2019). This may challenge the canonical 114 view of the cerebellar role in motor control and learning. However, it is also possible that the reward 115 signals reflect upstream influences of reward on kinematics (Lixenberg et al., 2020). Another suggestion 116 is that some climbing fibers play a homeostatic role and do not affect motor learning (Tang et al., 2017). 117 A final alternative is that reward signals in the cerebellum are found more laterally in the cerebellum and 118 119 thus reflect internal modelling of reward that is not directly connected to movement (Heffley and Hull, 120 2019; Sendhilnathan et al., 2020; Tsutsumi et al., 2019). Considering other recent results showing that 121 climbing fibers provide predictive signals about movement parameters (Streng et al., 2018) the canonical 122 view is still widely accepted (Apps et al., 2018; Sokolov et al., 2017).

123 It is also worth considering recent findings suggesting that basal ganglionic dopamine signals do 124 not necessarily reflect reward prediction error (Cox and Witten, 2019). These findings are in line with an 125 increasingly prominent hypothesis that direct and indirect pathways in the basal ganglia circuit 126 respectively calculate parallel and separate evaluations of action selection and outcome evaluation 127 (Nonomura et al., 2018; Stephenson-Jones et al., 2013, 2016). This would explain why neurons associated the direct pathway would not be sensitive to reward. This hypothesis is consistent with findings that the 128 activity of substantia nigra dopaminergic neurons not associated with reward is strongly associated with 129 130 movement selection and movement vigor (Da Silva et al., 2018).

### **131** Cortical function

The cerebral cortex has a laminar organization, and certain aspects of the laminar organization are preserved across most of cortex. This includes many aspects of the distribution of neurons appearing in each layer; it includes aspects of the structure of interlaminar connections; it also includes the layers producing local and projection efferents (Shipp, 2007). The similarity in the connectivity patterns of the 136 cortical layers, as well as the patterns of input and output from thalamus and other subcortical structures,

- has long been taken to imply that different cortical areas employ similar cortical algorithms (Douglas and
  Martin, 2004; Mumford, 1991, 1992), and that the cerebral cortex, like the cerebellum and basal ganglia,
- is specialized for a particular computation that is applied in different contexts (Doya, 1999).

140 However, recent findings highlighting the heterogeneity across cortical areas mean that the computation performed may vary with the context (Palomero-Gallagher and Zilles, 2019). The variability 141 142 in the neurochemistry of the different cortical areas and the variation in the width of the different cortical 143 layers (Zilles and Amunts, 2010), as well as the variability of the patterns of lateral connectivity (Sirosh 144 et al., 1996) suggest that the cortical algorithm varies in ways that match specific processing demands in each area of cortex (Barbas, 2015). To take a familiar example, the target of thalamic input, layer IV, is 145 unusually thick in visual cortex. This makes sense, since this input brings the visual input to visual cortex. 146 147 In contrast, layer IV is non-existent in the motor cortex. Thalamic input to motor cortex, which represents the output of the basal ganglia and the cerebellum, projects to other layers. Thus, processing in the two 148 areas will be different despite the many similarities between them. 149

150 One traditional view of the cortical structure is that the cortex is essentially a tool for 151 representation: each area of cortex represents different aspects of reality based on the inputs it receives 152 and the sensory-motor receptive fields of its neurons (Penfield and Boldrey, 1937). Thus, information from various sensory receptors flows forward and accumulates progressively to create a full picture of the real-153 world scene (Marr, 1982). A more recent view looks at the brain as a dynamical system. The dynamical 154 155 systems perspective predicts that "the evolution of neural activity should be best captured not in terms of 156 movement parameter evolution, but in terms of the dynamical rules by which the current state causes the 157 next state" (Shenoy et al., 2013). While some find this view to explicitly contrast with a representational 158 view, it can also be viewed as a framework of constraints on neural representations and their dynamics 159 (Churchland et al., 2010). Under this logic, even if we accept the representational view, the representations 160 must be structured so that their dynamics interact meaningfully with the dynamics of the real world being 161 represented (Churchland et al., 2010, 2012; Michaels et al., 2016). Structural and neurochemical variations 162 between cortical regions may reflect differences in the aspects of reality being represented (Palomero-Gallagher and Zilles, 2019). These differences would certainly include differences in the time constants 163 of the dynamics as well as the relative importance of prediction and reliability of new information. It may 164 165 also reflect the dimensionality of the predictive space.

Karl Friston and colleagues have been developing a related approach suggesting that cortical representation is essentially predictive (e.g., Bastos et al., 2012; Clark, 2013; Friston, 2010; Kanai et al., 2015). In this view, cortex mimics the dynamics of the represented world in order to represent future sensory stimulation. In their view, motor commands are characterized as predictive representations of proprioceptive input (Adams et al., 2015). Importantly, parallel segregated loops are a key property of the canonical circuits for predictive coding suggested by Friston and colleagues (Bastos et al., 2012). Incorporating the dynamical and predictive accounts of cortical function and the parallel loops described
above into the Shadmehr and Krakauer (2008) scheme leads to a multi-layer model described in the next
section.

## 175 A revised model for neuroanatomy of motor control

Here we consider the different aspects of reality that might be dynamically represented in different 176 177 cortical areas. We address two orthogonal dissociations: body vs task and state vs action. What the body is actually doing we call body-state. Our motor commands and our active efforts to move the body we call 178 179 body-action. Similarly, task-state and task-action represent the movement within the task space. Let us 180 consider again the example of driving discussed earlier. In this situation, body-state is the configuration of our body (hands resting on the wheel, right foot pressing the gas pedal) while body-action is the movement 181 of our limbs (moving the hands to rotate the steering wheel and changing the pressure applied by the foot 182 to the pedals). Task-state is the configuration of the car within the task (the car is driving 60 mph in the 183 184 right lane), and task-action is the movement of the car within the task (taking a turn, accelerating, or 185 breaking).

In many situations, these different predictive dynamical representations are highly correlated. 186 When we reach to a visual target, task-state encodes origin, target, and cursor position; task-action is the 187 movement of the cursor to the target; body-action is the movement of the hand. In the absence of 188 "experimenter trickery" (such as the well-studied visuomotor perturbations), these naturally represent the 189 190 same direction. Neuronal coding might be quite similar in different cortical areas (e.g. cells with similar directional tuning(Mahan and Georgopoulos, 2013)). This connects to the familiar credit assignment 191 problem (Wolpert and Landy, 2012), as an error can be assigned to different representations of the body 192 and the task. The system relies on various cues, priors and heuristics to resolve the source of its errors 193 194 (Berniker and Kording, 2008; Wei and Körding, 2009), although the computational details are still being explored (Gaffin-Cahn et al., 2019; McDougle et al., 2016; Parvin et al., 2018). 195

The differences between the different 196 197 representations become clearer in the context of a more complex task. For instance, we 198 199 consider pool or billiards (Haar and Faisal, 2020; Haar et al., 2019). In preparing and 200 making a shot (Figure 1), task-state encodes 201 202 ball locations and movement and the pocket 203 into which you want to sink the ball. Task-204 action is defined on the table: how the cue stick 205 hits the white ball and the effect it should have

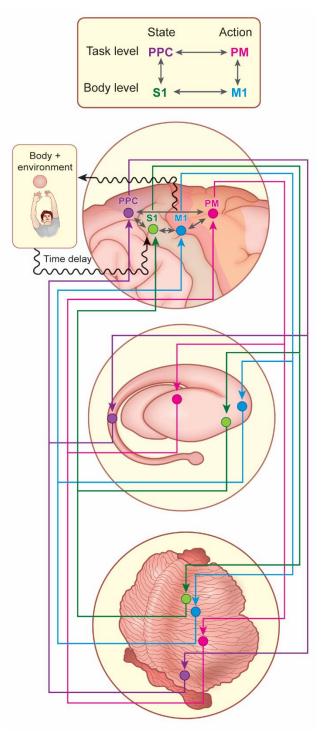


**Figure 1.** A game of billiards as a model for state and action representations. The task-state would encode mostly the locations of the white ball, the red (target) ball, and the pocket which you want to sink the ball to. The task-action would be the action on the table – the cue stick should hit the white ball in a certain position with a certain angle, spin, and speed, and the white ball should hit the target ball and push it towards the pocket. The body-state would be the player's posture and the way he/she holds the cue stick; and the body-action would be the movement that he/she does to move the cue stick.

and how the white ball should hit the target ball to push it towards the pocket. In contrast, body-state
describes your posture and the way you are holding the cue stick while body-action is the movement you
make to take the shot.

209 Our model combines Houk's DPM model 210 with Shadmehr and Krakauer's scheme based on optimal control theory. That is, we propose a 211 multi-layer model where at the center of each 212 213 layer is a cortical region. For each cortical region, activity is affected by a loop through the basal 214 ganglia that incorporates expected costs and 215 rewards into its dynamics. The dynamics of each 216 region is also affected through connections with 217 218 an area of the cerebellum that does predictive 219 error correction: it predicts and corrects persistent 220 errors in the cortical representation of dynamics. 221 This is consistent with the suggestion by Donchin 222 and Frens (2009) that state estimation is actually 223 computed in the deep cerebellar nuclei, and with 224 the findings of Gao et al., (2018) showing that 225 ongoing movement representation in the cortex is dependent on the cerebellum. Together, the 226 227 different cortical regions represent a predictive representation of both state and action (Figure 2). 228

229 This view fits naturally with the proposal 230 that cortex is a tool for predictive estimation and 231 dynamic representation. It elaborates the proposal 232 by suggesting that what distinguishes the different 233 areas of cortex is that they emphasize different 234 parts of reality with different dynamics. For the motor system, we propose that premotor, primary 235 236 motor, somatosensory and posterior parietal 237 cortices all predictively represent the ongoing 238 reality and dynamics of our motor behavior but with different emphases. We hypothesize that 239 240 primary motor cortex (M1) and primary 241 somatosensory cortex (S1) are concerned with the



**Figure 2.** A multi-layer model for motor control. In each layer (marked by different colored dots and arrows), a cortical region is making a loop with a designated area in the basal ganglia for expected costs and rewards, and another loop with an area of the cerebellum for forward modeling and state estimation. Each layer represents different function over the two fundamental divisions of task vs body and state vs action. Bi-directional communication between these different layers takes place in the cortex.

bodily aspects of movement where premotor cortex (PM) and posterior parietal cortex (PPC) emphasize movement inside the construct of our current task. At the same time, the frontal areas (M1 and PM) are associated more strongly with action for both body and task while the parietal areas (S1 and PPC) are concerned with body-state or task-state. The idea that M1, S1, PM and PPC have differential functions in body state and task conditions was suggested before (Cisek and Kalaska, 2010), but using different terms and not in the framework of optimal control.

248 In our model, activity in M1 and PM determines eventual motor output, and the interactions 249 between them creates body-action and task-action chosen in concert. The activity in these areas at any time 250 is determined in part by the ongoing dynamics of task and body actions. However, it is also influenced by the current state of the task and the body, and these are predicted by parietal cortex. All of these dynamics 251 252 must be shaped with the aim of achieving task goals. Parietal cortex must ensure that predictions of body-253 state reflect known dynamics of the body and ongoing sensory input. It must also ensure that predictions 254 are updated in concert with predictions of task-state. Predictions of task-state must reflect known task dynamics. 255

Mathematically, our model is based on that of Shadmehr and Krakauer (2008) but extends its dimensionality. That is, for Shadmehr and Krakauer, there was only one cortical / subcortical loop while our model considers multiple loops. This means that our definitions of state must be expanded to reflect the state in each of the loops simultaneously and the interactions between them. Thus, superficially, the "internal model" of the dynamics as a linear function of motor commands is the same:

$$\hat{x}^{(t+1|t)} = A\hat{x}^{(t|t)} + Bu^{(t)} \tag{1}$$

$$\hat{y}^{(t)} = \hat{H}\hat{x}^{(t)} \tag{2}$$

where  $u^{(t)}$  is the motor command, and  $\hat{y}^{(t)}$  is the expected sensory consequence.  $\hat{x}^{(t|t)}$  represents the predicted state at time t given current and previous sensory feedback. However, in our model the dimensionality of the state vector is increased to include the hypothesized states of the different cortical representations:

$$\hat{x} = \begin{pmatrix} x_{BA} \\ x_{TA} \\ x_{BS} \\ x_{TS} \end{pmatrix} \qquad \begin{array}{l} BA = Body \ Action \\ TA = Task \ Action \\ BS = Body \ State \\ TS = Task \ State \end{array} \tag{3}$$

The body-action and task-action here are not the descending motor command u but the cortical representations of action in the body space and in the task space, which play a role in determining u, but are distinct from it and are also influenced by dynamics of the entire system. Matrix A represents the dynamics of the state. Its block diagonal reflects the dynamics of each cortex separately while the offdiagonal blocks describe the cortico-cortical interactions: This is the author's final version; this article has been accepted for publication in the Journal of Cognitive Neuroscience

$$A = \begin{pmatrix} A_{BA} & D_{BA\leftarrow TA} & D_{BA\leftarrow TS} & 0\\ D_{TA\leftarrow BA} & A_{TA} & 0 & D_{TA\leftarrow TS}\\ D_{BS\leftarrow BA} & 0 & A_{BS} & D_{BS\leftarrow TS}\\ 0 & D_{TS\leftarrow TA} & D_{TS\leftarrow BS} & A_{TS} \end{pmatrix}$$
(4)

270 The single motor command u influences each cortical representation differently and B captures these 271 different effects:

$$B = \begin{pmatrix} B_{BA} \\ B_{TA} \\ B_{BS} \\ B_{TS} \end{pmatrix}$$
(5)

Again, as reality is unified, the state of the different cortical areas must be combined to generate a single sensory vector of sensory predictions,  $\hat{y}$ . For simplicity, we take the sensory feedback to only include proprioceptive and visual components,  $y = \begin{pmatrix} y_p \\ y_v \end{pmatrix}$ , though, in principle it probably also affects other modalities including auditory and haptic. The relative contributions of the different cortices to the prediction of sensory feedback is determined by the matrix H in equation 2:

$$H = \begin{pmatrix} H_{p,BA} & H_{p,TA} & H_{p,BS} & H_{p,TS} \\ H_{\nu,BA} & H_{\nu,TA} & H_{\nu,BS} & H_{\nu,TS} \end{pmatrix}$$
(6)

In addition to equations 1 and 2 above that describe internal representation of state dynamics and input prediction, the model includes a Kalman gain equation, updating the belief state at time t+1, given the acquired sensory information. Here, again, our equation is identical to that of Shadmehr and Krakauer:

$$\hat{x}^{(t+1|t+1)} = \hat{x}^{(t+1|t)} + K^{(t+1)} (y^{(t+1)} - \hat{y}^{(t+1)})$$
(7)

However, in our model the Kalman gain includes separate blocks from the physical dimensions of thesensory consequences to the neural diminutions:

$$K^{(t+1)} = \begin{pmatrix} K_{BA,p} & K_{BA,v} \\ K_{TA,p} & K_{TA,v} \\ K_{BS,p} & K_{BS,v} \\ K_{TS,p} & K_{TS,v} \end{pmatrix}$$
(8)

Also, in the "cost to go" function:

$$u^{(t)} = -G^{(t)}\hat{x}^{(t|t-1)} \tag{9}$$

the matrix G would not be in sensory dimensions (v,p) but in neural dimensions:

$$G^{(t)} = (G_{BA} \quad G_{TA} \quad G_{BS} \quad G_{TS})$$
(10)

284 Importantly, the state vs action dissociation here is not simply sensory vs motor. The state 285 representation of the body  $(x_{BS})$  is more than its sensory state. Even in the absence of any sensory feedback there is a representation of the current state of the body (posture, fatigue, etc.) and the future states the 286 287 body can transition towards. The task-state representation  $(x_{TS})$  is even more distinct from a sensory representation as it accounts for all abstract rules of the task, like driving on the right or the left side of the 288 289 road. Similarly, the body vs task dissociation addressed here is different than the common dissociation of 290 intrinsic vs extrinsic coordinate frames (e.g. Buneo and Andersen, 2006; Haar et al., 2017a; Kalaska et al., 291 1997; Wiestler et al., 2014). In fact, both body and task can be represented in either coordinate frame or 292 in both. Indeed, there is evidence for both intrinsic and extrinsic coordinate frames in the different cortices 293 discussed (e.g. Wu and Hatsopoulos, 2006, 2007). Nevertheless, in the primary sensorimotor cortices those 294 representations, in any coordinate frame, would always be of the body and not the task (e.g., the hands on 295 the steering wheel and not the car on the road). Similarly, in the PM and the PPC those representations, in 296 any coordinate frame, would always be of the task and not the body.

297 The representations of the body's state and action are not at all independent, of course; the extent 298 to which they interact is attested by the strong connectivity between M1 and S1 (equation 4). However, 299 while they are both fundamentally representing the same thing – the position of the body and its movement 300 - they represent different aspects of that same thing. M1 is focused on the world of our possible movements while S1 is focused on what effect our movements and the world around us will have on our body. 301 302 Accordingly, limb perturbation should be processed first in S1 (body-state) and then in M1 (body-action) 303 and PPC (task-state), as the change in the body-state affects both body-action and task-state. Only then 304 will processing pass to PM (task-action), which is affected by body-action and task-state but not directly 305 by body-state (see equation 4). Indeed, an examination of the relative timing of perturbation-related 306 activity across sensory and motor cortices showed this timing gradient (Omrani et al., 2016). Moreover, 307 the authors found that when the same perturbation is applied with and without task context, the earliest 308 and the biggest difference in the neural response is in the PPC, as the task is not experimentally defined 309 and might not be the same in all trials. Thus, the same change in body-state does not induce a consistent 310 change in task-state.

311 In our daily behavior, we do not generally tend to think about or understand our movements in terms of our body and our bodily motor commands. We do not make aware decision which muscle to flex 312 313 and which to extend in order to move our hand. Nearly every movement is part of a motor task and we are 314 controlling our performance in that task in order to achieve certain task goals. While driving, we think 315 about turning the car left, not about the way our hands rotate the steering wheel. In the billiards example, we think about hitting the ball and creating its trajectory. We do not focus on the flexion or abduction of 316 317 our shoulder and elbow. While in many experimental paradigms, body-state and task-state are identical, they are often not identical in real life. In addition to the examples above, one may consider video games, 318 319 riding a bike, driving or typing as situations where body-state and task-state are dissociated. Similarly,

what constitutes a desirable, rewarding body-state may be quite different, on its face, than a desirable
rewarding task-state. I may well bring my body into uncomfortable or unstable positions to achieve task
goals.

323 These fundamental distinctions between body-state and task-state and between body-state and 324 body-action can be extended to similar distinctions between task-action and body-action and between task-325 action and task-state. The essential point is that each of the representations has a different natural dynamics 326 (what is most likely to come after what), a different set of goals and rewards (what is comfortable and 327 what is effortful) and a different collection of complexities and non-linearities that may be hard to capture. One important consequence of this idea of multiple representation of different aspects of the situation is 328 that it emphasizes the importance of bidirectional communication between them (Clark, 2013). A 329 reasonable prediction about task-state is informed by task-actions. That is  $D_{TA \leftarrow TS}$  in Matrix A (Equation 330 4). Task-actions then affect task-state  $(D_{TS \leftarrow TA})$ . Body-actions must, in turn, realize the chosen task-331 actions. However, task-actions cannot be chosen without considering the feasibility of associated body-332 333 actions. Reality itself is multi-level and hierarchical, and, cortex must reflect this underlying structure to successfully model it. The mapping between the different representations cannot be pre-specified but must 334 335 be learned. Thus, in the driving example, a novice driver has no natural map between foot presses and car 336 dynamics. Therefore, driving instructors need an instructor's brake pedal. The novice driver needs to learn 337 the parameters for the task / body dependencies (D parameters in the dynamics matrix in eq. 4).

As discussed, Hanakawa (2011) presented a model, similar to ours, describing the role of premotor cortex in mediating between motor and prefrontal-cognitive cortices. Under the combined framework, we can imagine that prefrontal cortex could represent our ongoing plans, strategies and desires. These should guide the task-action which later guide the body-action. Caminiti et al. (2017) also emphasize the importance of task-related processing in higher level areas but focus on the relationship of the task / body system with higher order processing of reward, motivation, and attention in ways that are reminiscent of Hanakawa's model, but do not focus on the relative role of motor and premotor cortices.

345 In our model, each of the different cortical areas has projections to the basal ganglia to account for the different costs and rewards associated with each type of representation. In essence, it follows the 346 347 model of Nakahara et al., (2001) which suggests that parallel cortico-basal ganglia loops learn different 348 coordinates with different costs and rewards. We suggest those are not coordinates but representations of 349 task vs body and state vs action. For instance, Yeo et al., (2016), discuss the fact that one consequence of 350 movement is its effect on the quality of sensory information. They show the need to account for sensory 351 costs in the framework of optimal feedback control. Following this logic, basal ganglia interactions with 352 sensory cortices may relate to optimizing our behavior to maximize the relevant sensory precision.

353 Inherent in this perspective is an approach to simultaneous representation of state and action. Since 354 each cortical area is representing a particular aspect of reality, inherent in that representation is the implied representation of the dynamics of that aspect of reality. That is, a state representation contains in it, necessarily, an understanding of which states can arise from which other states. In addition, the dynamics of state are influenced by ongoing action so that the pre-central areas must influence the post-central state representations. Similarly, a central part of action representation is the way that one action flows into the next (or leads to the holding of a posture). The dynamics of movement are just as much informed by the ongoing dynamics of state as ongoing state dynamics are informed by knowledge of ongoing actions.

361 Generally speaking, the dynamics of both body and task are high-dimensional, non-linear, and 362 changing over time. Thus, generally speaking, the predictive representations of every cortical area will be fraught with error. In this sense, if the cerebellum engages in error-driven learning, it can serve each of the 363 cortical areas by learning to predict the errors in its predictive representation. This is precisely the 364 interaction between cerebellum and cortex hypothesized by Doya (2000). In this view, the cerebellum will 365 play a different role when it corrects for the errors in different cortical representations. However, although 366 the form of the errors will depend on the domain being represented and the model that has developed, the 367 computations underlying the cerebellar circuitry will be the same. 368

# 369 Task representations

370 The proposed roles of M1 and S1 in representing body-action and body-state, respectively, are 371 straightforward. We use new terminology to describe the commonly accepted roles of these areas. As such, we do not need to take a position on classical debates regarding coordinate systems (muscles versus 372 373 movements). From our perspective, this is a discussion of how body-action is encoded: important in itself 374 but at a level of description that is not our focus. The roles of the posterior parietal cortex and the premotor 375 cortex in task-state and task-action representation, respectively, require further discussion. There is much less clarity about their roles and more work needs to be done to show how our perspective fits in with 376 previous ideas. In the next section, we demonstrate how our perspective helps make sense of the literature. 377

#### 378 Posterior parietal cortex represents task-state

379 There are several schools of thought about the role of posterior parietal cortex. One common view 380 is that the PPC serves as a sensorimotor interface for visually guided movements (e.g. Buneo and 381 Andersen, 2006). As such it is involved mostly in sensory-motor mapping and motor planning (Andersen 382 and Buneo, 2002; Cohen and Andersen, 2002). Perhaps the leading alternative view is that the PPC is a 383 state estimator, as was originally suggested by Daniel Wolpert and colleagues (Wolpert and Ghahramani, 384 2000; Wolpert et al., 1998) and later integrated into the current model of computational neuroanatomy for 385 motor control (Shadmehr and Krakauer, 2008). Other possibilities have also been put forward. They 386 include high-order sensory-motor information integration in support of high-level motor functions (e.g. 387 Fogassi and Luppino, 2005), and conscious motor intentions (e.g. Desmurget and Sirigu, 2012). We

believe that thinking in the abstracted terms of task-state representation will help clarify this extensiveliterature and subsume alternative perspectives within a single framework.

390 Grea et al., (2002) reported that a patient with bilateral posterior parietal cortex damage had no difficulty reaching to targets in their central fixation, but when the target jumped at reach onset the subject 391 392 could not correct for it and continued to reach to the original target location. Desmurget et al., (1999) 393 produce similar results on healthy subjects using a single pulse transcranial magnetic stimulation at reach 394 onset. This phenomenon is a classic example for a deficit in task-state representation. The subject simply 395 could not adjust to the sudden change in the task-state. A study by Funamizu et al., (2016) produced similar 396 results using optogentics in mice. Mice express learning in a task by increased anticipatory licking as they approached their goal, even in the absence of external cues. Thus, the mice are expressing their estimation 397 398 of task-state. The authors showed that silencing of PPC prevented this ability to evaluate task-state. When 399 the PPC is intact, it encodes task-state continuously, for example, it encodes changing target position even 400 while the body is not yet moving (Reid and Dessing, 2018).

It is also possible to point to works where PPC seems to be engaged in behavior that cannot be 401 402 explained as either sensorimotor mapping or state estimation. In these cases, dynamical task-state 403 representation provides a better explanation of PPC function. Fogassi et al., (2005) found that parietal neurons coding a specific behavior, show different activity when this behavior is part of different tasks. 404 405 Gail and Andersen (2006) found that parietal neurons represent the task-rule (pro- or anti-reach) before any specific movement cues, indicating abstract task representation in PPC that goes beyond spatial or 406 407 motor goal representations. This task-rule is a component of task-state. Hwang and Andersen (2012) showed clear differences in PPC LFPs in reaching tasks with direct and symbolic target presentation. They 408 409 saw even more striking differences between visually-guided and memory-guided reaching tasks (Hwang and Andersen, 2011). Bremner and Andersen (2014) found that parietal area 5d switches its coding after 410 411 target presentation so that it always codes the most relevant information for the task. Hawkins et al., (2013) 412 showed that parietal neurons tend to be significantly tuned either during one task or during another but 413 rarely during both. Hawkins and colleagues even interpret their results in terms of task representation 414 suggesting that "the superior parietal lobule plays an important role in processing information about the nonstandard nature of a task". In a recent fMRI study (Heed et al., 2018), a tactile stimulation was applied 415 to the subjects' feet while their legs were either straight or crossed. After a delay, subjects were instructed 416 417 to do pro/anti-pointing towards their feet. The results show that during touch localization S1 encodes the anatomical side of the tactile stimulus while the PPC encodes it in external space. During movement 418 planning only the PPC encodes the task rule (pro vs anti pointing). These results suggest that body and 419 420 task state are dissociated in the parietal cortex.

Explicit visuomotor adaptation is an example where change in task-state can be isolated. In
visuomotor rotation adaptation tasks, visual target and hand target become dissociated. To correct for this,
subjects need to learn to move their hand away from the target, at an angle equal to the rotation angle, in

424 order to get the cursor to the target. Recent studies dissociated explicit and implicit processes in the visuomotor adaptation (e.g. Bromberg et al., 2019; Hegele and Heuer, 2010; Mazzoni and Krakauer, 2006; 425 Taylor and Ivry, 2011; Taylor et al., 2014; Werner et al., 2015). While implicit learning (unaware error 426 427 correction) should change in the task-action representation to be the cursor direction, instead of the hand direction, if the learning is explicit (aware re-aiming, the subject is aware of the perturbation and changes 428 the movement strategy to account for the perturbation), the task-action representation should stay loyal to 429 the hand direction and only the task-state representation and its relation to the task-action should adapt. 430 431 Indeed, we found that directional selectivity in the PPC changes following visuomotor rotation adaptation 432 (Haar et al., 2015), while directional selectivity in the primary-motor, premotor and primarysomatosensory cortex stays loyal to the hand movement direction. The rotation angle in this study was 45° 433 while implicit adaptation to visuomotor rotation tends to be limited to about 15° (e.g. Bond and Taylor, 434 2015; Morehead et al., 2017), suggesting that the adaptation here was mostly explicit. The small 435 436 aftereffects, following the removal of the perturbation, confirm that learning was mostly explicit. 437 Following washout, the task-state is returned to its original representation; as a consequence, the 438 directional selectivity in the PPC also returns to its original pattern. These results were predicted earlier 439 based on theoretical considerations (Tanaka et al., 2009).

440 Task-state representation requires high level effector-invariant components in the neural responses during hand and arm movements for general task properties like the task goal or task rule (e.g., pro- vs. 441 442 anti-reach, or reach vs. grasp). This invariance in the representation of task properties will be matched by 443 a lack of sensitivity to kinematic components that are not related to the task. On the other hand, body-444 action and body-state representations should reflect kinematics. Task-action representations might include 445 both kinematic and effector invariant properties, and kinematic and effector dependent properties. Indeed, effector-invariant representation of reach vs. grasp was found in the PPC and PM but not in M1 and S1 446 447 (Gallivan et al., 2013). At the same time, effector-invariant representation of reaching movement direction (in joint coordinates) was found in M1, S1 and PM, but not in the PPC (Haar et al., 2017a). The study of 448 449 motor variability also supports this framework. In measurements made without feedback, where movement 450 variability is dominated by planning noise (Dhawale et al., 2017), we demonstrated that individual movement variability magnitudes are best predicted by cortical neural variability in the PPC (Haar et al., 451 2017b). Thus, the variability in the PPC is variability in the task-state domain. 452

Since most motor control experimental paradigms involve visual feedback, many of the examples above could also be explained simply as if PPC is representing the visual feedback in the task. Yet, there are examples like Funamizu et al., (2016), where mice are expressing their estimation of task-state in the absence of external cues but silencing of PPC prevented this ability, which support the idea that PPC is involved in task-state estimation, regardless of specific sensory input. The Heed et al., (2018) fMRI study, which was mentioned above, used tactile stimulation (and not visual), and thus provides another support. 459 Another recent review has also managed to incorporate a broad group of approaches to the PPC within a consistent framework (Medendorp and Heed, 2019). They argue that different areas of the PPC 460 show different behavior because they represent the world along two key axes. The first - the rostro-caudal 461 462 axis – separates representation of body from that of the environment. The second – the medio-lateral axis - separates representations of different "action classes." This review, thus, addresses an aspect of PPC 463 function explicitly outside the scope of our review: the functional subdivisions within the PPC; their work 464 is fully complementary to our own. For instance, they emphasize that PPC activity is highly dependent on 465 task and context and represents those aspects of body and environment that are relevant to task 466 467 performance. We suggest a generalization of their approach where rostral PPC reflects the projection of 468 the self into the task – the representation of our ability to have direct effects in the task – rather than an 469 explicit representation of the body which is more properly the role of S1.

#### 470 Premotor cortex represents task-action

471 We propose that the role of the premotor cortex is to represent task-action. Only a few studies in 472 the existing literature can speak to this question. Most often, PM is studied in tasks involving direct reach 473 to target. In these tasks, task-action representation is simple and consistent with both task-state and body-474 action. Nevertheless, some studies show dissociation between body-action representation in M1 and task-475 action representation in PM. For instance, Schwartz et al., (2004) used a motor illusion to separate monkeys' perception of arm movements from their actual movements during figure drawing. Trajectories 476 477 constructed from cortical activity of the monkeys showed that the actual movement (body-action) was represented in M1, whereas the visualized trajectories (task-action) were found in the ventral PM. 478

479 Another example of this dissociation, which also emphasizes the idea of the parallel loops, comes 480 from motor adaptation studies in cerebellar patients (Donchin et al., 2012; Rabe et al., 2009). The results 481 of these studies suggest that patients with pathology in the anterior parts of the arm representation of the 482 cerebellum, apparently connected to M1, failed to adapt to force-field perturbation. This is presumably 483 because force field adaptation requires adapting the relation between task-action and body-action. Patients with a lesion in a more posterior part of the arm area, apparently connected to PM, failed to adapt to 484 visuomotor perturbation. Again, one may presume that this is because visuomotor adaptation requires 485 486 changes in the relation between task-state and task-action. Recent modeling work on neural recordings 487 from M1 and dorsal PM reached a similar conclusion: force-field adaptation changes the relationship 488 between PM and M1; visuomotor adaptation causes changes upstream to M1 (Perich et al., 2018).

In stroke patients performing imitation movements, deficits were found to be associated with PM lesions. Imitations were equally impaired when cued by actor's arm movement or by a cursor, suggesting abstract body-independent movement representation (task-action) in PM (Wong et al., 2019). Further support for this dissociation can be found in the result of a study (Saberi-Moghadam et al., 2016) showing that when target jumps caused a sudden change in motor intention, this led to earlier changes in PM activity than in M1. In this task, information at the task level was driving the change in motor intention so task
level representation changes drive changes at the body level. We predict that tasks where the perturbation
is at the body level and not the task level (for instance, a perturbation of the hand that is not reflected in
the cursor) should drive changes that arise first in M1.

498 More support for task-action representation in the premotor cortex can be found in the results of Pastor-Bernier & Cisek (2011) which shows that directional tuning of neurons in PM modulated following 499 500 changes in rewards associated with targets in the preferred direction of the neuron. This modulated tuning 501 reflects a change in the task-action associated with the same task state. Pearce and Moran (2012) used a 502 complex obstacle-avoidance task and showed that PM activity is modulated both by task demands and by the particular strategy being used. They looked at the activity of the PM neurons during trials differing 503 504 both in the target direction and in the obstacle opening directions and showed that the same neurons show 505 directional selectivity both to the target direction and to the obstacle opening direction. This dual 506 directional selectivity is a good example for task-action representation in the premotor cortex. Finger sequencing is another task were the task and body representations differ: the task-action is the sequence 507 while the body-action is individual finger movements. Indeed, a recent fMRI study by Yokoi et al., (2018) 508 509 found that after intense practice on finger sequences, activity patterns in PM and PPC encoded the task 510 (the different movement sequences), while the activity patterns in M1 and S1 could be fully explained by 511 the body action/state: a linear combination of patterns for the constituent individual finger movements.

Last, a recent study by Martínez-Vázquez and Gail (2018) looked at the LFP directed interaction between PM and PPC during movement planning and execution. They found that during movement planning the direction of the interaction is from the PPC to the PM, and during movement execution there is a flip in the direction of the interaction which flips back after execution. These findings are again consistent with our model. During planning PM receives information from PPC regarding task-state to plan task-action. During execution, PPC receives information from PM regarding ongoing task-action to update task-state.

# 519 Concluding remarks

Shadmehr and Krakauer's proposal for a neuroanatomy for motor control (2008), presented a 520 521 decade ago, highlighted the cortical loops with the basal ganglia and the cerebellum and suggested that 522 they serve for computing costs and for system identification, respectively. We present a new model inspired by that scheme that emphasizes parallel loops connecting different cortical areas with these 523 subcortical regions. This aspect of our model draws inspiration from Houk's DPM model (Houk, 2001) 524 525 and is supported by compelling anatomical evidence (Middleton and Strick, 1997, 2001). In our model, we address the notion that each area of cortex represents reality in a different way with different emphases. 526 527 We suggest that the primary somatosensory and motor cortices represent respectively the state and action 528 of the body, while the PPC and premotor cortex represent the state and action of the task.

While it is largely accepted that the basal ganglia and the cerebellum form parallel segregated loops with different cortical regions, there is an alternative view of a funnel like organization from wide areas of cortex through the sub-cortical regions onto a small area of cortex (Allen and Tsukahara, 1974; Kemp and Powell, 1971). Recent findings suggest caveats to the parallel segregated loops framework (Aoki et al., 2019), but still support it. If this ongoing controversy ultimately shows that the parallel segregated loops are a poor model for basal ganglia and cerebellar connectivity to cortex, our proposed model will be undermined.

Ultimately, we wish to emphasize that this model is only a limited cartoon and makes no attempt to capture the full complexity of the cortical hierarchy in motor control or its subcortical connections. Some of these simplifications have been addressed above. Nevertheless, our model advances the paradigm within which we think about and study the motor cortices. It points the way forward towards a developing understanding of the task / body dimension and the need to distinguish the complex relationships of each cortical area to its subcortical support and develop a fuller understanding of each of the parallel loops.

In models of this sort, precise anatomical definitions of the basal ganglia and cerebellum are left 542 somewhat vague. This is true for the Shadmehr and Krakauer (2008) model, for the models of Houk (2001) 543 544 and Hanakawa (2011), and also for our own model. However, the basic idea is that parallel loops with the 545 basal ganglia will include parallel instantiations of the direct pathway, the indirect pathway, and the hyperdirect pathway (Nambu et al., 2002). Similarly, in the cerebellum, the idea is that the full cerebellar 546 547 microcircuit is involved where cortical input drives mossy fibers originating in the pons as well climbing 548 fiber input originating in the inferior olive, and that the output of the circuit will be from the dentate nucleus 549 via the thalamus (Raymond et al., 1996).

550 Indeed, this class of models further schematizes the motor system because the models generally 551 do not address subdivisions of the premotor and posterior parietal cortices and often leave out other nonprimary motor areas such as supplementary, pre-supplementary and cingulate motor areas. The idea that 552 553 the entire premotor cortex or the entire posterior-parietal cortex performs a unique function is controversial 554 (e.g., Rizzolatti et al., 2014). The models also fail to address recent findings showing direct connections 555 of the basal ganglia to the cerebellum (Bostan and Strick, 2018; Quartarone et al., 2020) and ignores 556 entirely the spinal cord, red nucleus, thalamus, and other subcortical motor areas. These models have, however, helped guide thinking about the inter-relations of parts of the motor system and have been an 557 558 integral part of some of the most inspiring work in our field.

559 One direction for future work would be the one laid out by King et al., (2019). These authors used 560 a battery of motor, sensory and cognitive tasks to produce a detailed map of cerebellar function. However, 561 the tasks they selected do not allow dissociation of task level and body level aspects of the task. As a result, 562 their data cannot be used to directly test our hypothesis. A similar study with specifically designed tasks 563 would be an ideal test of our model. Another possibility for testing the dissociation of task and body This is the author's final version; this article has been accepted for publication in the Journal of Cognitive Neuroscience

representations in PM and M1 would be the use of brain computer interfaces. Using such interfaces, we

565 can define a task that is driven directly by activity in premotor cortex. We predict that we could ask patients

to imagine doing the task with different bodily effectors and, thus, create a situation in which we can see

that premotor activity is directly related to the task while M1 activity is related to the imagined movement

of the body.

### 569 **References**

- Adams, R.A., Friston, K.J., and Bastos, A.M. (2015). Active Inference, Predictive Coding and Cortical Architecture. In Recent
   Advances on the Modular Organization of the Cortex, M.F. Casanova, and I. Opris, eds. (Springer), pp. 97–121.
- Allen, G.I., and Tsukahara, N. (1974). Cerebrocerebellar communication systems. Physiol. Rev. 54, 957–1006.
- 573 Andersen, R.A., and Buneo, C.A. (2002). Intentional maps in posterior parietal cortex. Annu. Rev. Neurosci. 189–220.
- Aoki, S., Smith, J.B., Li, H., Yan, X., Igarashi, M., Coulon, P., Wickens, J.R., Ruigrok, T.J., and Jin, X. (2019). An open cortico-basal ganglia loop allows limbic control over motor output via the nigrothalamic pathway. Elife 8.
- Apps, R., Hawkes, R., Aoki, S., Bengtsson, F., Brown, A.M., Chen, G., Ebner, T.J., Isope, P., Jörntell, H., Lackey, E.P., et al. (2018). Cerebellar Modules and Their Role as Operational Cerebellar Processing Units. Cerebellum *17*, 654–682.
- 578 Barbas, H. (2015). General Cortical and Special Prefrontal Connections: Principles from Structure to Function. Annu. Rev.
   579 Neurosci. 38, 269–289.
- Bastos, A.M., Usrey, W.M., Adams, R.A., Mangun, G.R., Fries, P., and Friston, K.J. (2012). Canonical Microcircuits for
   Predictive Coding. Neuron 76, 695–711.
- Berniker, M., and Kording, K. (2008). Estimating the sources of motor errors for adaptation and generalization. Nat. Neurosci. *11*, 1454.
- Bond, K.M., and Taylor, J. a (2015). Flexible explicit but rigid implicit learning in a visuomotor adaptation task. J.
  Neurophysiol. jn.00009.2015.
- 586 Bostan, A.C., and Strick, P.L. (2018). The basal ganglia and the cerebellum: nodes in an integrated network. Nat. Rev.
  587 Neurosci. *19*, 338–350.
- Bostan, A.C., Dum, R.P., and Strick, P.L. (2013). Cerebellar networks with the cerebral cortex and basal ganglia. Trends Cogn.
  Sci. *17*, 241–254.
- Bremner, L.R., and Andersen, R.A. (2014). Temporal Analysis of Reference Frames in Parietal Cortex Area 5d during Reach
   Planning. J. Neurosci. 34, 5273–5284.
- Bromberg, Z., Donchin, O., and Haar, S. (2019). Eye movements during visuomotor adaptation represent only part of the explicit learning. ENeuro 6, 1–12.
- Buckner, R.L., Krienen, F.M., Castellanos, a., Diaz, J.C., and Yeo, B.T.T. (2011). The organization of the human cerebellum
  estimated by intrinsic functional connectivity. J. Neurophysiol. *106*, 2322–2345.
- Buneo, C.A., and Andersen, R.A. (2006). The posterior parietal cortex: Sensorimotor interface for the planning and online
   control of visually guided movements. Neuropsychologia 44, 2594–2606.
- Caminiti, R., Borra, E., Visco-Comandini, F., Battaglia-Mayer, A., Averbeck, B.B., and Luppino, G. (2017). Computational
   Architecture of the Parieto-Frontal Network Underlying Cognitive-Motor Control in Monkeys. ENeuro 4.
- Choi, E.Y., Yeo, B.T.T., and Buckner, R.L. (2012). The organization of the human striatum estimated by intrinsic functional connectivity. J. Neurophysiol. *108*, 2242–2263.
- Churchland, M.M., Cunningham, J.P., Kaufman, M.T., Ryu, S.I., and Shenoy, K. V. (2010). Cortical Preparatory Activity:
   Representation of Movement or First Cog in a Dynamical Machine? Neuron 68, 387–400.
- Churchland, M.M., Cunningham, J.P., Kaufman, M.T., Foster, J.D., Nuyujukian, P., Ryu, S.I., and Shenoy, K. V (2012). Neural population dynamics during reaching. Nature 487, 51–56.
- Cisek, P., and Kalaska, J.F. (2010). Neural Mechanisms for Interacting with a World Full of Action Choices. Annu. Rev.
   Neurosci. *33*, 269–298.
- Clark, A. (2013). Whatever next? Predictive brains, situated agents, and the future of cognitive science. Behav. Brain Sci. *36*, 181–204.
- Cohen, Y.E., and Andersen, R.A. (2002). A common reference frame for movement plans in the posterior parietal cortex. Nat.
   Rev. Neurosci. *3*, 553–562.
- 612 Cox, J., and Witten, I.B. (2019). Striatal circuits for reward learning and decision-making. Nat. Rev. Neurosci. 20, 482–494.
- 613 Desmurget, M., and Sirigu, A. (2012). Conscious motor intention emerges in the inferior parietal lobule. Curr. Opin. Neurobiol.
- **614** *22*, 1004–1011.

- 615 Desmurget, M., Epstein, C., and Turner, R. (1999). Role of the posterior parietal cortex in updating reaching movements to a 616 visual target. Nat. Neurosci.
- 617 Dhawale, A.K., Smith, M.A., and Ölveczky, B.P. (2017). The Role of Variability in Motor Learning. Annu. Rev. Neurosci. 40,
  618 479–498.
- bonchin, O., Rabe, K., Diedrichsen, J., Lally, N., Schoch, B., Gizewski, E.R., and Timmann, D. (2012). Cerebellar regions
   involved in adaptation to force field and visuomotor perturbation. J. Neurophysiol. *107*, 134–147.
- 621 Douglas, R.J., and Martin, K.A.C. (2004). Neuronal circuits of the neocortex. Annu. Rev. Neurosci. 27, 419–451.
- boya, K. (1999). What are the computations of the cerebellum, the basal ganglia and the cerebral cortex? Neural Networks *12*, 961–974.
- 624 Doya, K. (2000). Complementary roles of basal ganglia and cerebellum in learning and motor control. Curr. Opin. Neurobiol.
   625 10, 732–739.
- Dum, R.P., and Strick, P.L. (2003). An unfolded map of the cerebellar dentate nucleus and its projections to the cerebral cortex.
   J. Neurophysiol. *89*, 634–639.
- 628 Fogassi, L., and Luppino, G. (2005). Motor functions of the parietal lobe. Curr. Opin. Neurobiol. 15, 626–631.
- Fogassi, L., Ferrari, P.F., Gesierich, B., Rozzi, S., Chersi, F., and Rizzolatti, G. (2005). Parietal Lobe: From Action
  Organization to Intention Understanding. Science (80-.). 308, 662–667.
- Frens, M. a, and Donchin, O. (2009). Forward models and state estimation in compensatory eye movements. Front. Cell.
  Neurosci. *3*, 13.
- **633** Friston, K. (2010). The free-energy principle: a unified brain theory? Nat. Rev. Neurosci. *11*, 127–138.
- Funamizu, A., Kuhn, B., and Doya, K. (2016). Neural substrate of dynamic Bayesian inference in the cerebral cortex. Nat.
  Neurosci. *19*, 1682–1689.
- Gaffin-Cahn, E., Hudson, T.E., and Landy, M.S. (2019). Did I do that? Detecting a perturbation to visual feedback in a reaching
   task. J. Vis. *19*.
- Gail, A., and Andersen, R.A. (2006). Neural Dynamics in Monkey Parietal Reach Region Reflect Context-Specific
   Sensorimotor Transformations. J. Neurosci. 26, 9376–9384.
- 640 Gallivan, J.P., McLean, D.A., Flanagan, J.R., and Culham, J.C. (2013). Where One Hand Meets the Other: Limb-Specific and
- Action-Dependent Movement Plans Decoded from Preparatory Signals in Single Human Frontoparietal Brain Areas. J.
   Neurosci. 33, 1991–2008.
- 643 Gao, Z., Davis, C., Thomas, A.M., Economo, M.N., Abrego, A.M., Svoboda, K., De Zeeuw, C.I., and Li, N. (2018). A cortico-644 cerebellar loop for motor planning. Nature *563*, 113–116.
- 645 Gerbella, M., Borra, E., Mangiaracina, C., Rozzi, S., and Luppino, G. (2016). Corticostriate Projections from Areas of the
  "Lateral Grasping Network": Evidence for Multiple Hand-Related Input Channels. Cereb. Cortex 26, 3096–3115.
- 647 Grea, H., Pisella, L., Rossetti, Y., Desmurget, M., Tilikete, C., Grafton, S., Prablanc, C., and Vighetto, A. (2002). A lesion of
  648 the posterior parietal cortex disrupts on-line adjustments during aiming movements. Neuropsychologia *40*, 2471–2480.
- Haar, S., and Faisal, A.A. (2020). Neural biomarkers of multiple motor-learning mechanisms in a real-world task. BioRxiv 2020.03.04.976951.
- Haar, S., Donchin, O., and Dinstein, I. (2015). Dissociating Visual and Motor Directional Selectivity Using Visuomotor
   Adaptation. J. Neurosci. 35, 6813–6821.
- Haar, S., Dinstein, I., Shelef, I., and Donchin, O. (2017a). Effector-Invariant Movement Encoding in the Human Motor System.
  J. Neurosci. *37*, 9054–9063.
- Haar, S., Donchin, O., and Dinstein, I. (2017b). Individual Movement Variability Magnitudes Are Explained by Cortical Neural
   Variability. J. Neurosci. *37*, 9076–9085.
- Haar, S., van Assel, C.M., and Faisal, A.A. (2019). Kinematic signatures of learning that emerge in a real-world motor skill
   task. BioRxiv 612218.
- Hanakawa, T. (2011). Rostral premotor cortex as a gateway between motor and cognitive networks. Neurosci. Res. 70, 144–154.
- 661 Hawkins, K.M., Sayegh, P., Yan, X., Crawford, J.D., and Sergio, L.E. (2013). Neural activity in superior parietal cortex during

- rule-based visual-motor transformations. J. Cogn. Neurosci. 25, 436–454.
- Heed, T., Medendorp, P., and Klautke, J. (2018). Dynamic coding of sensory and motor information during hand movements
   directed to tactile targets. In Program No. 400.01, (San Diego, CA: Society for Neuroscience), p.
- Heffley, W., and Hull, C. (2019). Classical conditioning drives learned reward prediction signals in climbing fibers across the
   lateral cerebellum. Elife 8.
- Heffley, W., Song, E.Y., Xu, Z., Taylor, B.N., Hughes, M.A., McKinney, A., Joshua, M., and Hull, C. (2018). Coordinated
   cerebellar climbing fiber activity signals learned sensorimotor predictions. Nat. Neurosci. 21, 1431–1441.
- Hegele, M., and Heuer, H. (2010). Implicit and explicit components of dual adaptation to visuomotor rotations. Conscious.
   Cogn. 19, 906–917.
- Houk, J.C. (2001). Neurophysiology of Frontal-Subcortical Loops. In Frontal-Subcortical Circuits in Psychiatry and Neurology,
  D.G. Lichter, and J.L. Cummings, eds. (New York: Guilford Press), pp. 92–113.
- 673 Houk, J.C. (2005). Agents of the mind. Biol. Cybern. 92, 427–437.
- Houk, J.C., Bastianen, C., Fansler, D., Fishbach, A., Fraser, D., Reber, P.J., Roy, S.A., and Simo, L.S. (2007). Action selection
   and refinement in subcortical loops through basal ganglia and cerebellum. Philos. Trans. R. Soc. B Biol. Sci. *362*, 1573–1583.
- Hwang, E.J., and Andersen, R.A. (2011). Effects of visual stimulation on LFPs, spikes, and LFP-spike relations in PRR. J.
  Neurophysiol. *105*, 1850–1860.
- Hwang, E.J., and Andersen, R.A. (2012). Spiking and LFP activity in PRR during symbolically instructed reaches. J.
  Neurophysiol. *107*, 836–849.
- Kalaska, J.F., Scott, S.H., Cisek, P., and Sergio, L.E. (1997). Cortical control of reaching movements. Curr. Opin. Neurobiol. 7, 849–859.
- Kanai, R., Komura, Y., Shipp, S., Friston, K., Komura, Y., Shipp, S., and Friston, K. (2015). Cerebral hierarchies : predictive processing , precision and the pulvinar. Philos. Trans. R. Soc. Lond. B. Biol. Sci. *370*, 20140169.
- Kelly, R.M., and Strick, P.L. (2003). Cerebellar loops with motor cortex and prefrontal cortex of a nonhuman primate. J.
  Neurosci. 23, 8432–8444.
- Kemp, J.M., and Powell, T.P.S. (1971). The Connexions of the Striatum and Globus Pallidus: Synthesis and Speculation. Philos.
   Trans. R. Soc. B Biol. Sci. 262, 441–457.
- King, M., Hernandez-Castillo, C.R., Poldrack, R.A., Ivry, R.B., and Diedrichsen, J. (2019). Functional boundaries in the human cerebellum revealed by a multi-domain task battery. Nat. Neurosci. 22, 1371–1378.
- Kornhuber, H.H. (1971). Motor functions of cerebellum and basal ganglia: the cerebellocortical saccadic (ballistic) clock, the
   cerebellonuclear hold regulator, and the basal ganglia ramp (voluntary speed smooth movement) generator. Kybernetik *8*, 157–
   162.
- Kostadinov, D., Beau, M., Pozo, M.B., and Häusser, M. (2019). Predictive and reactive reward signals conveyed by climbing
   fiber inputs to cerebellar Purkinje cells. Nat. Neurosci. 22, 950–962.
- Kunzle, H. (1977). Projections from the primary somatosensory cortex to basal ganglia and thalamus in the monkey. Exp BrainRes *30*, 481-92.
- Lixenberg, A., Yarkoni, M., Botschko, Y., and Joshua, M. (2020). Encoding of eye movements explains reward-related activity
   in cerebellar simple spikes. J. Neurophysiol. *123*, 786–799.
- Mahan, M.Y., and Georgopoulos, A.P. (2013). Motor directional tuning across brain areas: Directional resonance and the role of
   inhibition for directional accuracy. Front. Neural Circuits 7, 1–11.
- 701 Marr, D. (1982). Vision: A computational approach (San Francisco: Freeman & Co).
- Martínez-Vázquez, P., and Gail, A. (2018). Directed Interaction Between Monkey Premotor and Posterior Parietal Cortex
   During Motor-Goal Retrieval from Working Memory. Cereb. Cortex 28, 1866–1881.
- Mazzoni, P., and Krakauer, J. (2006). An Implicit Plan Overrides an Explicit Strategy during Visuomotor Adaptation. J.
   Neurosci. 26, 3642–3645.
- McDougle, S.D., Boggess, M.J., Crossley, M.J., Parvin, D., Ivry, R.B., and Taylor, J.A. (2016). Credit assignment in movement-dependent reinforcement learning. Proc. Natl. Acad. Sci. *113*, 6797–6802.
- 708 Medendorp, W.P., and Heed, T. (2019). State estimation in posterior parietal cortex: Distinct poles of environmental and bodily

- 709 states. Prog. Neurobiol. 183, 101691.
- 710 Medina, J.F. (2019). Teaching the cerebellum about reward. Nat. Neurosci. 22, 846–848.
- Michaels, J.A., Dann, B., and Scherberger, H. (2016). Neural Population Dynamics during Reaching Are Better Explained by a
   Dynamical System than Representational Tuning. PLoS Comput. Biol. 12.
- Middleton, F.A., and Strick, P.L. (1997). Dentate output channels: motor and cognitive components. Prog. Brain Res. 114, 553–566.
- 715 Middleton, F.A., and Strick, P.L. (1998). Cerebellar output: Motor and cognitive channels. Trends Cogn. Sci. 2, 348–355.
- Middleton, F.A., and Strick, P.L. (2001). A Revised Neuroanatomy of Frontal-Subcortical Circuits. In Frontal-Subcortical Circuits in Psychiatry and Neurology, D.G. Lichter, and J.L. Cummings, eds. (New York: Guilford Press), pp. 44–58.
- Mogenson, G.J., Jones, D.L., and Yim, C.Y. (1980). From motivation to action: Functional interface between the limbic system
   and the motor system. Prog. Neurobiol. *14*, 69–97.
- Morehead, J.R., Taylor, J.A., Parvin, D.E., and Ivry, R.B. (2017). Characteristics of Implicit Sensorimotor Adaptation Revealed
   by Task-irrelevant Clamped Feedback. J. Cogn. Neurosci. 29, 1061–1074.
- Mumford, D. (1991). On the computational architecture of the neocortex I. The role of the thalamo-cortical loop. Biol. Cybern.
   65, 135–145.
- Mumford, D. (1992). On the computational architecture of the neocortex II. The role of cortico-cortical loops. Biol. Cybern. 66, 241–251.
- Nakahara, H., Doya, K., and Hikosaka, O. (2001). Parallel Cortico-Basal Ganglia Mechanisms for Acquisition and Execution of
   Visuomotor Sequences—A Computational Approach. J. Cogn. Neurosci. 13, 626–647.
- Nambu, A., Tokuno, H., and Takada, M. (2002). Functional significance of the cortico–subthalamo–pallidal 'hyperdirect' pathway. Neurosci. Res. 43, 111–117.
- Nonomura, S., Nishizawa, K., Sakai, Y., Kawaguchi, Y., Kato, S., Uchigashima, M., Watanabe, M., Yamanaka, K., Enomoto,
- K., Chiken, S., et al. (2018). Monitoring and Updating of Action Selection for Goal-Directed Behavior through the Striatal
   Direct and Indirect Pathways. Neuron *99*, 1302-1314.e5.
- O'Reilly, J.X., Beckmann, C.F., Tomassini, V., Ramnani, N., and Johansen-Berg, H. (2010). Distinct and Overlapping
   Functional Zones in the Cerebellum Defined by Resting State Functional Connectivity. Cereb. Cortex 20, 953–965.
- Omrani, M., Murnaghan, C.D., Pruszynski, J.A., and Scott, S.H. (2016). Distributed task-specific processing of somatosensory feedback for voluntary motor control. Elife 5, e13141.
- Palomero-Gallagher, N., and Zilles, K. (2019). Cortical layers: Cyto-, myelo-, receptor- and synaptic architecture in human cortical areas. Neuroimage *197*, 716–741.
- Parvin, D.E., McDougle, S.D., Taylor, J.A., and Ivry, R.B. (2018). Credit Assignment in a Motor Decision Making Task Is
   Influenced by Agency and Not Sensory Prediction Errors. J. Neurosci. 38, 4521–4530.
- Pastor-Bernier, A., and Cisek, P. (2011). Neural Correlates of Biased Competition in Premotor Cortex. J. Neurosci. 31, 7083–7088.
- Pearce, T.M., and Moran, D.W. (2012). Strategy-Dependent Encoding of Planned Arm Movements in the Dorsal Premotor
  Cortex. Science (80-.). 337, 984–988.
- Penfield, W., and Boldrey, E. (1937). Somatic Motor and Sensory Representation in the Cerebral Cortex of Man as Studies by
   Electrical Stiumlation. Brain 60, 389–443.
- Perich, M.G., Gallego, J.A., and Miller, L.E. (2018). A Neural Population Mechanism for Rapid Learning. Neuron *100*, 964-976.
- Quartarone, A., Cacciola, A., Milardi, D., Ghilardi, M.F., Calamuneri, A., Chillemi, G., Anastasi, G., and Rothwell, J. (2020).
   New insights into cortico-basal-cerebellar connectome: Clinical and physiological considerations. Brain *143*, 396–406.
- Rabe, K., Livne, O., Gizewski, E.R., Aurich, V., Beck, A., Timmann, D., and Donchin, O. (2009). Adaptation to visuomotor
   rotation and force field perturbation is correlated to different brain areas in patients with cerebellar degeneration. J.
- 753 Neurophysiol. *101*, 1961–1971.
- Raymond, J.L., Lisberger, S.G., and Mauk, M.D. (1996). The cerebellum: a neuronal learning machine? Science (80-.). 272, 1126–1131.

- Reid, S.A., and Dessing, J.C. (2018). Non-predictive online spatial coding in the posterior parietal cortex when aiming ahead for catching. Sci. Rep. 8, 7756.
- Rizzolatti, G., Cattaneo, L., Fabbri-Destro, M., and Rozzi, S. (2014). Cortical Mechanisms Underlying the Organization of
   Goal-Directed Actions and Mirror Neuron-Based Action Understanding. Physiol. Rev. *94*, 655–706.
- Saberi-Moghadam, S., Ferrari-Toniolo, S., Ferraina, S., Caminiti, R., and Battaglia-Mayer, A. (2016). Modulation of Neural
   Variability in Premotor, Motor, and Posterior Parietal Cortex during Change of Motor Intention. J. Neurosci. *36*, 4614–4623.
- Schwartz, A.B., Moran, D.W., and Reina, G.A. (2004). Differential Representation of Perception and Action in the Frontal
   Cortex. Science (80-.). 303, 380–383.
- 764 Seitzman, B.A., Gratton, C., Marek, S., Raut, R. V., Dosenbach, N.U.F., Schlaggar, B.L., Petersen, S.E., and Greene, D.J.
- (2020). A set of functionally-defined brain regions with improved representation of the subcortex and cerebellum. Neuroimage 206, 116290.
- Sendhilnathan, N., Ipata, A.E., and Goldberg, M.E. (2020). Neural Correlates of Reinforcement Learning in Mid-lateral
   Cerebellum. Neuron *106*, 188-198.e5.
- 769 Shadmehr, R., and Krakauer, J.W. (2008). A computational neuroanatomy for motor control. Exp. Brain Res. 185, 359–381.
- Shenoy, K. V., Sahani, M., and Churchland, M.M. (2013). Cortical Control of Arm Movements: A Dynamical Systems
   Perspective. Annu. Rev. Neurosci. *36*, 337–359.
- 772 Shipp, S. (2007). Structure and function of the cerebral cortex. Curr. Biol. 17, R443–R449.
- Da Silva, J.A., Tecuapetla, F., Paixão, V., and Costa, R.M. (2018). Dopamine neuron activity before action initiation gates and
   invigorates future movements. Nature 554, 244–248.
- Sirosh, J., Miikkulainen, R., and Choe, Y. (1996). Lateral interactions in the cortex : structure and function (The Utcs Neural Network Research Group).
- Sokolov, A.A., Miall, R.C., and Ivry, R.B. (2017). The Cerebellum: Adaptive Prediction for Movement and Cognition. Trends
   Cogn. Sci. 21, 313–332.
- Stephenson-Jones, M., Kardamakis, A.A., Robertson, B., and Grillner, S. (2013). Independent circuits in the basal ganglia for
   the evaluation and selection of actions. Proc. Natl. Acad. Sci. U. S. A. *110*, E3670–E3679.
- Stephenson-Jones, M., Yu, K., Ahrens, S., Tucciarone, J.M., Van Huijstee, A.N., Mejia, L.A., Penzo, M.A., Tai, L.H.,
  Wilbrecht, L., and Li, B. (2016). A basal ganglia circuit for evaluating action outcomes. Nature *539*, 289–293.
- 783 Streng, M.L., Popa, L.S., and Ebner, T.J. (2018). Complex Spike Wars: a New Hope. Cerebellum 17, 735–746.
- Tanaka, H., Sejnowski, T.J., and Krakauer, J.W. (2009). Adaptation to visuomotor rotation through interaction between
   posterior parietal and motor cortical areas. J. Neurophysiol. *102*, 2921–2932.
- 786 Tang, T., Xiao, J., Suh, C.Y., Burroughs, A., Cerminara, N.L., Jia, L., Marshall, S.P., Wise, A.K., Apps, R., Sugihara, I., et al.
- (2017). Heterogeneity of Purkinje cell simple spike–complex spike interactions: zebrin- and non-zebrin-related variations. J.
   Physiol. 595, 5341–5357.
- 789 Taylor, J.A., and Ivry, R.B. (2011). Flexible cognitive strategies during motor learning. PLoS Comput. Biol. 7.
- Taylor, J.A., and Ivry, R.B. (2014). Cerebellar and Prefrontal Cortex Contributions to Adaptation, Strategies, and
   Reinforcement Learning. In Progress in Brain Research, (Elsevier B.V.), pp. 217–253.
- Taylor, J. a, Krakauer, J.W., and Ivry, R.B. (2014). Explicit and implicit contributions to learning in a sensorimotor adaptation task. J. Neurosci. *34*, 3023–3032.
- 794 Todorov, E., and Jordan, M.I. (2002). Optimal feedback control as a theory of motor coordination. Nat. Neurosci. 5, 1226–1235.
- Tsutsumi, S., Hidaka, N., Isomura, Y., Matsuzaki, M., Sakimura, K., Kano, M., and Kitamura, K. (2019). Modular organization of cerebellar climbing fiber inputs during goal-directed behavior. Elife 8.
- 797 Wei, K., and Körding, K. (2009). Relevance of Error: What Drives Motor Adaptation? J. Neurophysiol. 101, 655–664.
- Werner, S., Van Aken, B.C., Hulst, T., Frens, M.A., Van Der Geest, J.N., Strüder, H.K., and Donchin, O. (2015). Awareness of sensorimotor adaptation to visual rotations of different size. PLoS One *10*, 1–18.
- Wiestler, T., Waters-Metenier, S., and Diedrichsen, J. (2014). Effector-independent motor sequence representations exist in extrinsic and intrinsic reference frames. J. Neurosci. *34*, 5054–5064.
- 802 Wolpert, D.M., and Ghahramani, Z. (2000). Computational principles of movement neuroscience. Nat. Neurosci. 3, 1212–1217.

- 803 Wolpert, D.M., and Landy, M.S. (2012). Motor control is decision-making. Curr. Opin. Neurobiol. 22, 996–1003.
- Wolpert, D.M., Goodbody, S.J., and Husain, M. (1998). Maintaining internal representations : the role of the human superior
   parietal lobe. Nat. Neurosci. 1, 529–533.
- Wong, A.L., Jax, S.A., Smith, L.L., Buxbaum, L.J., and Krakauer, J.W. (2019). Movement Imitation via an Abstract Trajectory
   Representation in Dorsal Premotor Cortex. J. Neurosci. 39, 3320–3331.
- Wu, W., and Hatsopoulos, N. (2006). Evidence against a single coordinate system representation in the motor cortex. Exp. Brain
   Res. 175, 197–210.
- 810 Wu, W., and Hatsopoulos, N. (2007). Coordinate system representations of movement direction in the premotor cortex. Exp.
   811 Brain Res. 176, 652–657.
- 812 Yeo, B.T.T., Krienen, F.M., Sepulcre, J., Sabuncu, M.R., Lashkari, D., Hollinshead, M., Roffman, J.L., Smoller, J.W., Zöllei,
- L., Polimeni, J.R., et al. (2011). The organization of the human cerebral cortex estimated by intrinsic functional connectivity. J.
   Neurophysiol. *106*, 1125–1165.
- Yeo, S.-H., Franklin, D.W., and Wolpert, D.M. (2016). When Optimal Feedback Control Is Not Enough: Feedforward
  Strategies Are Required for Optimal Control with Active Sensing. PLoS Comput. Biol. *12*, e1005190.
- Yokoi, A., Arbuckle, S.A., and Diedrichsen, J. (2018). The role of human primary motor cortex in the production of skilled
  finger sequences. J. Neurosci. *38*, 1430–1442.
- Zilles, K., and Amunts, K. (2010). Centenary of Brodmann's map conception and fate. Nat. Rev. Neurosci. 11, 139–145.

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