

# 1 Assessing Salt-Surfactant Synergistic effects on Interfacial 2 Tension from Molecular Dynamics Simulations

3 Gerard Alonso <sup>a</sup>, Pablo Gamallo <sup>a</sup>, Andrés Mejía <sup>b</sup>, Ramón Sayós <sup>a,\*</sup>

4 <sup>a</sup> *Departament de Ciència de Materials i Química Física & Institut de Química Teòrica i Computacional*  
5 *(IQTCUB), Universitat de Barcelona, C. Martí i Franquès 1, 08028 Barcelona, Spain.*

6 <sup>b</sup> *Departamento de Ingeniería Química, Universidad de Concepción, POB 160-C, Correo 3, Concepción,*  
7 *Chile.*

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9 **Abstract:** In the recent years, many efforts have been carried out trying to comprehend  
10 how surfactants and salts interact among each other at the oil/brine interface to reduce the  
11 interfacial tension (IFT). To that end, the interfacial properties of several combinations  
12 of surfactants, salts and oils have been measured experimentally confirming the existence  
13 of a synergistic effect. Unfortunately, many of the proposed mechanisms for that effect  
14 arise from experimental observations, so this work, based on molecular dynamics  
15 simulations, intends to reproduce and explain this kind of phenomenon from a molecular  
16 point of view. The correct understanding of these phenomena can have application in  
17 many fields, especially in Enhanced Oil Recovery, where reducing IFT can potentially  
18 increase oil production. In this article we evaluate the effect of adding three different salts  
19 (i.e., NaCl, CaCl<sub>2</sub> and MgCl<sub>2</sub>) on the IFT of a water/oil system with different non-ionic  
20 surfactants. We have evaluated the effect that the ions of salt produce to surfactants, as  
21 well as the perturbation that surfactants produce on the ions. From our results, we can  
22 assess that salts (especially NaCl) and surfactants are able to interact with each other,  
23 being both active species in reducing the IFT of the system.

24 **Keywords:** Molecular Dynamics simulations, Interfacial tension, Oil/water interface,  
25 Surfactant, Salt, Synergistic effect

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32 **Corresponding Author**

33 \*E-mail adress: r.sayos@ub.edu (Ramón Sayós)

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## 35 **1. Introduction**

36 The use of surfactants in Enhanced Oil Recovery (EOR) is a common practice to reduce  
37 the interfacial tension (IFT) between crude oil and formation water [1–3]. The IFT  
38 reduction enhances the mobility of the crude oil within the reservoir, weakening the  
39 capillary forces, and ultimately improving oil production. The application of these  
40 compounds is usually expensive, so many studies have been focused on replacing them  
41 with other cheaper compounds. A good example is the low-salinity waterflooding, which  
42 permitted to enhance oil recovery by only controlling the salinity of the injection water  
43 in certain reservoirs [4, 5]. However, the best performance is usually obtained with a  
44 combination of surfactants and other additives (e.g, co-surfactants) to the  
45 oil/water/surfactant mixture [6–8]. Both compounds can act cooperatively to reduce the  
46 IFT to ultralow values and can improve the stability of oil/water microemulsions [9].  
47 Also, similar synergistic interactions were observed experimentally when using salts as  
48 additives [10–23].

49 Species with highly localized charge, such as ions of salts, are capable of interacting with  
50 polar molecules and polar functional groups, changing their microscopical ordering and  
51 affecting their physicochemical properties. For example, water molecules orient their  
52 dipoles towards ions in solution forming highly order solvation shells due to strong  
53 electrostatic interactions. This fact affects the water density, viscosity, surface tension,  
54 melting point, boiling point and vapor pressure [24–26]. Similarly, the ions of salts can  
55 modify the surfactant solubility in water, its Critical Micelle Concentration (CMC) [27–  
56 29] or the IFT of liquid/liquid and vapor/liquid systems. In particular, the equilibrium IFT  
57 (i.e., usually called static IFT) of several water/surfactant + salt mixtures was studied by  
58 different authors, showing reductions of the IFT based on the so-called salt-surfactant  
59 synergistic effect. Some examples are the works of Staszak et al. [22], who studied a  
60 water/zwitterionic surfactant/NaCl system, Koelsch et al. [18], who analyzed different  
61 water/cationic surfactant/potassium halide salt systems or Fainerman et al. [14], who  
62 reported results for different water/anionic surfactant/NaCl+CaCl<sub>2</sub>+MgCl<sub>2</sub> systems,  
63 among others [11–13, 15, 16]. Finally, these synergistic effects were mainly seen at  
64 surfactant concentrations below the CMC [18, 22, 23]. Notice that the static IFT value is  
65 achieved after waiting for all species to diffuse to their equilibrium positions. During this

66 process, which can take several minutes or hours, the IFT is not constant. The variation  
67 of the IFT with time is called dynamic IFT and it converges smoothly to the static IFT.  
68 However, this property is also affected by the salt-surfactant synergistic effect, changing  
69 the dynamic IFT pattern to an abrupt decrease to an IFT minimum (i.e., sometimes even  
70 drops to ultralow values) followed by a smooth increase until it converges with the static  
71 IFT. This behavior was reported by authors such as Liu et al. [20,21], who studied the  
72 dynamic IFT of different water/anionic + non-ionic surfactants/salt systems or  
73 Witthayapanyanon et al. [23], who performed measurements in mixtures containing  
74 water/anionic surfactant/NaCl.

75 The aforementioned experimental evidence served to propose different mechanisms to  
76 explain both the static and the dynamic IFT reduction phenomena. Two mechanisms were  
77 proposed to explain the static IFT reduction: (i) salinity reduces the solubility of  
78 surfactants in water, which forces them to migrate to the interface [30]; (ii) the salt ions  
79 can interact with the surfactant head groups and minimize the electrostatic interaction  
80 among them, which induces a closer packing of surfactants at the interface to allow  
81 additional surfactant molecules to fit at the interface [20, 21]. Alternatively, the dynamic  
82 IFT reduction mechanism proposed assumes that surfactants are soluble in both the oil  
83 and the water phase. Then, the solubility of surfactants in water is lessened upon addition  
84 of salts, which promotes the diffusion of surfactants from the water to the oil phase  
85 through the oil/water interface. The minimum in the dynamic IFT is assumed to occur  
86 when the surfactant molecules that are diffusing to the oil phase, are close to the interface  
87 [31]. Finally, the IFT is increased again when they are at equilibrium in the oil bulk. In  
88 summary, all previous mechanisms were mainly deduced from experimental  
89 measurements, who relate the IFT reduction with an increased number of surfactants at  
90 the interface, based on the Gibbs adsorption isotherm [32]:

$$d\gamma = - \sum_i \Gamma_i \mu_i \quad (1)$$

91 where  $\gamma$  is the IFT of the system and  $\mu_i$  and  $\Gamma_i$  are the chemical potential and the interfacial  
92 excess concentration of species  $i$  at the interface for a given temperature. The ideal  
93 interface, represented by the Gibbs adsorption isotherm, has an infinitesimal volume and  
94 is placed at the Gibbs dividing surface ( $\sigma$ ). For convenience, one should place  $\sigma$  at the  
95 position that makes the  $\Gamma_i$  of a reference component (e.g., water) equal to zero and refer

96 other  $\Gamma_i$  to that component (i.e.,  $\Gamma_i^w$  for water as reference). Finally, Eq. (1) can be  
97 rearranged as:

$$\Gamma_i^w = -\frac{1}{RT} \left( \frac{\partial \gamma}{\partial \ln(a_i)} \right)_{T, a_{j \neq i}} \quad (2)$$

98 Notice that for diluted concentrations the activity  $a_i$  in Eq. (2) can be taken simply as the  
99 concentration. The expression indicates that the interfacial excess of a species  $i$  can be  
100 either negative or positive as a function of the interfacial behavior of this compound. If  
101 this compound accumulates at the interface the value of  $\Gamma_i^w$  is positive and the IFT is  
102 reduced upon addition of this compound to the solution. These types of species are known  
103 as surface active compounds. On the other hand, if a compound depletes from the  
104 interface the value of  $\Gamma_i^w$  becomes negative and the IFT is increased upon addition of this  
105 compound.

106 The need of better understanding the interactions between salts and surfactants, motivated  
107 some simulation studies that combined ionic surfactants and salts [33–35]. From these  
108 works, it was observed that anionic surfactants, which have negatively charged head  
109 groups and usually  $\text{Na}^+$  counterions, are capable of exchanging their  $\text{Na}^+$  by divalent  
110 cations of the salt. This exchange is favored because divalent cations have more charge  
111 and interact more strongly with the charged head groups than  $\text{Na}^+$ . Similarly, cationic  
112 surfactants, which have positively charged head groups and are commonly accompanied  
113 by  $\text{Cl}^-$  counterions, are capable of exchanging their  $\text{Cl}^-$  by divalent anions of the salt. Their  
114 main conclusion was that these ionic exchanges modify the electrostatic interactions at  
115 the interface, which perturb the interfacial molecular distributions. However, none these  
116 works characterized the IFT reduction phenomena due to salt-surfactant synergistic  
117 effects via molecular simulations.

118 To expand the knowledge in salt-surfactant interfacial phenomena, Molecular Dynamics  
119 (MD) simulations on oil/water/surfactant/salt systems are performed, using pure  
120 dodecane as model oil, three different chlorine salts (i.e.,  $\text{NaCl}$ ,  $\text{CaCl}_2$  or  $\text{MgCl}_2$ ) and two  
121 non-ionic surfactants: the Triethyleneglycol 1-dodecyl ether (i.e.,  
122  $\text{CH}_3(\text{CH}_2)_{11}(\text{OCH}_2\text{CH}_2)_3\text{OH}$  also known as  $\text{C}_{12}\text{E}_3$ ), which is a linear surfactant with 12  
123  $\text{CH}_x$  tail groups and a head with three polyoxyethylene units and an alcohol termination,  
124 and triethyleneglycol 6-dodecyl ether (i.e.,  $(\text{CH}_3(\text{CH}_2)_5)(\text{CH}_3(\text{CH}_2)_4)\text{CH}(\text{OCH}_2\text{CH}_2)_3\text{OH}$   
125 alternatively named  $(\text{C}_6\text{C}_5)\text{CE}_3$ ). The latter is a version of the same surfactant but with a

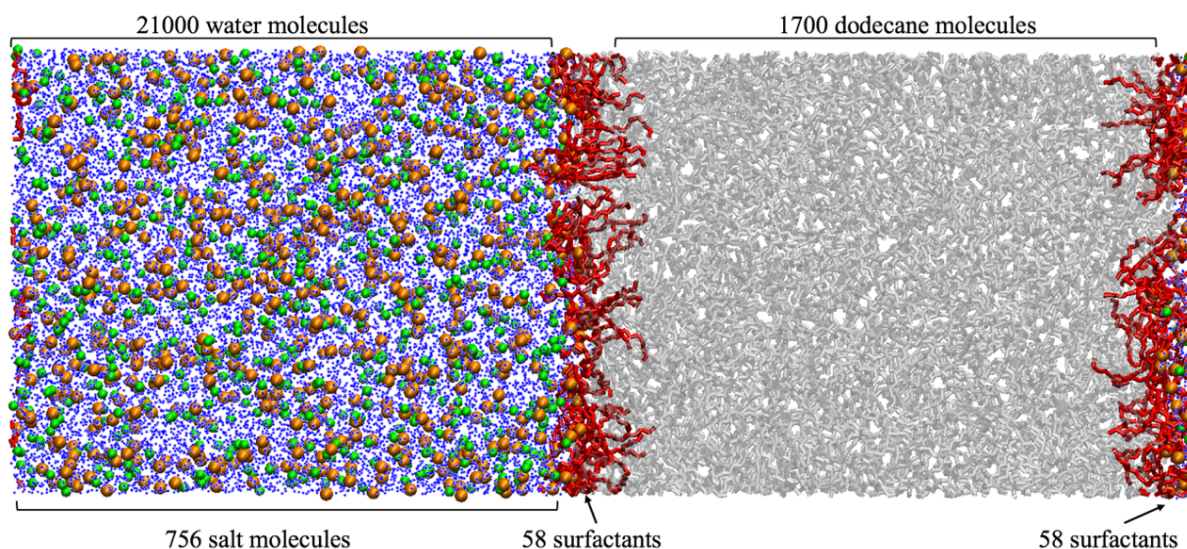
126 ramified tail. Thus  $(C_6C_5)CE_3$  and  $C_{12}E_3$  share the same head group, and both tail groups  
127 have the same molecular weight for the sake of evaluating the effect of the ramification  
128 in the tail group. The purpose of these simulations is to explain the experimental trends  
129 in the static IFT reduction and give an alternative perspective to this phenomenon from a  
130 molecular point of view. Due to the MD simulations yielding equilibrium properties, only  
131 salt-surfactant synergistic effects on the static IFT are evaluated, while the dynamic IFT  
132 processes are not taken into account.

133 Although the correct characterization of the static salt-surfactant synergistic effect has a  
134 significant impact in EOR (i.e., helping to lower the IFT and thus increasing production),  
135 it is only one of the many phenomena involved in the complex process of oil recovery. In  
136 fact, the presence of salts can also activate other mechanisms that hamper the oil  
137 extraction. For example, it is well known that depending on the rock matrix, salt cations  
138 can attach to the mineral surface and attract the negatively charged polar fraction of crude  
139 oils to the rock, which ultimately reduce the wettability of the reservoir [36]. In that  
140 situation, the effectivity of the recovery would be conditioned by the balance between all  
141 the mechanisms activated in presence of salinity. This means that unless the static salt-  
142 surfactant synergistic effect is capable defeating all other processes (i.e., by significantly  
143 reducing the IFT) it might not be directly applicable to EOR. In any case, this effect is  
144 present in any oil recovery process, so understanding it can help to unveil some of the  
145 mechanisms occurring during oil recovery.

146

## 147 **2. Computational methods**

148 MD simulations with classical force fields were performed by means of LAMMPS code  
149 [37]. The initial simulation cell to calculate IFT consists on an orthorhombic box with  
150 dimensions  $L_x = L_y = 80 \text{ \AA}$  and  $L_z = 210 \text{ \AA}$ . Half of the simulation cell was filled with  
151 water molecules at  $\rho = 0.997 \text{ g/cm}^3$  and the other half was filled with dodecane at  $\rho =$   
152  $0.745 \text{ g/cm}^3$ . Both values correspond to the experimental pure liquid densities at  $T = 300$   
153 K and  $P = 1 \text{ atm}$  [38,39]. The three different salts (i.e., NaCl, CaCl<sub>2</sub> or MgCl<sub>2</sub>) were  
154 inserted only in the water phase at a 2.0 molal concentration. Notice that this  
155 concentration is significantly higher than the average seawater salinity (i.e., ~0.6 M)  
156 typically used in waterflooding, or the optimum salinities commonly employed in low-  
157 salinity/surfactant EOR. In fact, low-salinity is favored during oil recovery because it  
158 helps surfactants to achieve ultralow dynamic IFT, and the wettability of the rocks is  
159 increased in absence of salinity. However, in the present work, equilibrium MD  
160 simulations of the liquid/liquid interface were conducted, where neither the dynamic  
161 effects or the interactions with the rock are taken into consideration. Regarding static IFT  
162 reductions, some experimental works seemed to show stronger effects at higher salinity  
163 concentrations up to 2.0 M [16, 20–22]. For this reason, three preliminary calculations  
164 were carried out to find the salinity concentration that maximized the static IFT reduction  
165 effect in the considered oil/water/surfactant systems: (i) no significant change on the  
166 equilibrium IFT was observed at 0.5 molal of NaCl, (ii) a statistically meaningful  
167 reduction effect was detected at 2.0 molal of NaCl and (iii) the IFT was increased when  
168 calculated at 6.0 molal of NaCl. Finally, the surfactants were added directly onto the  
169 water/oil interface to accelerate the equilibration of the system at a concentration below  
170 the CMC. The amount of surfactants simulated represents an interface with an interfacial  
171 excess  $\Gamma_i^w = 1.50 \text{ } \mu\text{mol/m}^2$  (i.e.,  $110 \text{ \AA}^2/\text{molecule}$ ) and it has been chosen in consistency  
172 with the aforementioned experiments performed (i.e., below the CMC) [11–13, 15, 16,  
173 18, 22, 23]. The initial position and orientation of all molecules followed a uniform  
174 random distribution with the only restriction that molecules can only be generated in the  
175 respective regions detailed. Fig. 1 shows a typical simulation cell with a summary of all  
176 species involved in our simulations.



**Fig 1.** Summary of molecules used in the standard  $80 \text{ \AA} \times 80 \text{ \AA} \times 210 \text{ \AA}$  simulation cell with two interfaces. Dodecane and water molecules are represented by grey bonds and blue dots, respectively. Ionic salts are represented by spheres: the cation in orange and the anion in green. Finally, the surfactant molecules are displayed in red bonds accumulated at the interface.

177

178 The simulations were performed in three steps: first, the random creation of particles  
 179 required an initial minimization of the system to avoid molecular overlaps. Second, the  
 180 system was thermalized in the NVT ensemble, using first a Langevin thermostat [40]  
 181 during 20 ps followed by 100 ps with a Nosé-Hoover thermostat [41], a combination of  
 182 thermostats that was very efficient for thermal equilibration. Third, a Berendsen barostat  
 183 [42] was used to equilibrate the pressure during 500 ps, while temperature was still  
 184 controlled by the Nosé-Hoover thermostat. The barostat only couples to the z-direction  
 185 of the simulation cell to keep interfacial area constant (i.e.,  $\text{NAP}_z\text{T}$  ensemble). Finally,  
 186 the Berendsen barostat was changed by a Nosé-Hoover barostat [43] to perform a time  
 187 evolution of 20 ns. The thermostat and barostat constants were 0.2 and 1.0 ps respectively  
 188 and the timestep for all simulation stages was 1 fs.

189 Block averages were extracted each 0.5 ns to monitor the evolution of the total energy  
 190 and interfacial tension of the system. In most simulations the equilibrium was reached  
 191 after 10 ns of evolution, and the range from 10 to 20 ns was used to calculate the  
 192 equilibrium IFT. For those calculations with longer equilibration times, 10 extra ns were  
 193 run to calculate the averages from this additional time. Also, to ensure that calculations  
 194 were fully converged, a single calculation was time evolved during 50 extra ns, obtaining  
 195 an equivalent value of IFT compared to the one calculated up to 20 ns. Finally, the  
 196 molecular distributions were calculated using the final 2 ns of the simulation. Notice that

197 the large interfacial area (i.e., 80 Å x 80 Å) employed in the simulations improve the  
198 statistical significance of the molecular distributions. This means that averaging 2 ns is  
199 enough to yield smooth density profiles as shown in the results section.

200 Intermolecular and intramolecular interactions of organic molecules were represented  
201 with the TraPPE-UA force field [44]. This force field considers that bonds are fixed at  
202 their equilibrium bond lengths, so we followed the standard recommendation of TraPPE  
203 developers and used the spring constants from AMBER force field [45] to allow  
204 molecular vibrations. Water molecules were reproduced using the rigid TIP3P force field  
205 [46], which were constrained to their equilibrium geometry through the SHAKE  
206 algorithm [47]. A validation stage of TraPPE-UA and TIP3P force fields was carried out  
207 to ensure that the models were correctly reproducing the properties of the surfactants and  
208 water. The validation is compiled in the Supplementary Material, where it is seen that the  
209 surfactants are well reproduced by TraPPE-UA. Similarly, the salt-surfactant synergistic  
210 effects identified in this work can also be seen with more sophisticated water models such  
211 as TIP4P/Ew [48]. However, the TIP4P model of water is computationally more  
212 expensive than a standard three-point model such as TIP3P. So, after ensuring that the  
213 latter is capable of capturing the salt-surfactant synergistic effect (see section S1 of the  
214 Supplementary Material), it is selected due to computational efficiency. Finally, the ions  
215 of salts (i.e., Na<sup>+</sup>, Ca<sup>2+</sup>, Mg<sup>2+</sup>, Cl<sup>-</sup>) are compounds hard to simulate by point charge  
216 models, as can be seen by the large amount of force fields developed by many authors on  
217 the last years. To evaluate the effect of the force field on the calculated properties,  
218 simulations with salts were performed with three different non-polarizable sets of  
219 parameters: (i) the force field from Smith and Dang [49], whose parameters are  
220 implemented in CLAYFF; (ii) the force field from Åqvist [50], used in OPLS; and (iii)  
221 the force field from Beglov and Roux [51], found in the CHARMM force field. Crossed  
222 interactions between all species in this work are accounted through the standard Lorentz-  
223 Bethelot mixing rules [52]. All pair interactions were calculated using a spherical cutoff  
224 of 14 Å as recommended by TraPPE. Truncated potentials may induce important  
225 deviations to the calculated IFT values, as shown by several authors [53–57]. However,  
226 these deviations are usually systematic, and the relative trends are maintained, specially  
227 with similar systems. This study focuses on determining the qualitative effects of salt-  
228 surfactant interactions (i.e., the IFT is increased or decreased), so the proper application  
229 of the tail corrections would yield to the same qualitative conclusion. Nevertheless,



230 analytic tail corrections were included to the Lennard-Jones potential as recommended  
 231 by TraPPE [58]. Finally, the long-range coulombic interactions were computed by means  
 232 of the Particle-Particle/Particle-Mesh (PPPM) method [59].

233 IFT was calculated using the pressure tensor method of Kirkwood et al. [60, 61], which  
 234 relates this property with the difference between the normal ( $P_{zz}$ ) and tangential ( $\frac{P_{xx}+P_{yy}}{2}$ )  
 235 components of the pressure tensor (Eq. (3)). In this equation,  $L_z$  corresponds to the length  
 236 of the simulation cell and the factor 1/2 arises since the simulation cell exhibits two  
 237 interfaces. To calculate the statistical uncertainty of the results, three quasi-equivalent  
 238 replicas of the same dodecane/water/surfactant system were built, using the same number  
 239 of molecules, initial distribution, temperature and pressure. Then, all molecules are  
 240 randomly rotated to generate a different initial state of the same system. The standard  
 241 deviation of the three calculated IFT values are used as an estimate of the statistical  
 242 uncertainty. Notice that all oil/water interfaces modelled in this work have a similar IFT,  
 243 so the standard deviation of  $\pm 0.8$  dyn/cm calculated through this procedure is  
 244 transferable to all simulations.

$$\gamma = \frac{L_z}{2} \left( P_{zz} - \frac{P_{xx} + P_{yy}}{2} \right) \quad (3)$$

245 The distribution of molecules along the z-direction of the simulation cell (i.e., the number  
 246 density  $\rho_i(z)$ ), was used to determine the accumulation or depletion of each species at  
 247 the interface. To build them, the simulation cell was divided through the z-direction in  
 248 bins of 1 Å width, and the different number of particles in each bin was averaged over  
 249 the last 2 ns of the simulation. From the z-distributions the interfacial excess was  
 250 calculated using Eq. (4) [32],

$$\Gamma_i^w = \int_a^b \frac{\rho_i(z) - \rho_i^{gibbs}(z)}{A} dz = \int_a^b \frac{\rho_i(z)}{A} dz - \frac{\bar{\rho}_i^w \cdot |\sigma^w - a| + \bar{\rho}_i^o \cdot |b - \sigma^w|}{A} \quad (4)$$

251 where the integration limits  $a$  and  $b$  are the center of the water and oil bulks respectively,  
 252 and  $\sigma^w$  is the position of the Gibbs dividing surface. The position of  $\sigma^w$  was chosen to  
 253 make the interfacial excess of water equal to zero, which was selected as the reference  
 254 component.  $\rho_i^{gibbs}(z)$  corresponds to the density profile of component  $i$  in a system with  
 255 two bulk phases split with an infinitesimally thin interface. In this ideal system the density  
 256 profile in each bulk phase is constant and equal to its the average density within the phase

257 ( $\bar{\rho}_i^w$  for water and  $\bar{\rho}_i^o$  for oil). The water/dodecane reciprocal solubilities as well as the  
258 salt/dodecane solubilities are very low, so the term  $\bar{\rho}_i^o$  can be neglected in our  
259 simulations. Finally, this integral is normalized by the interface unit area  $A$ .

260 To assess how the addition of salts and surfactants affects molecular interactions, Radial  
261 Distribution Functions (RDFs) between different molecular groups were calculated  
262 through VMD code [62]. Also, the orientation of surfactants at the interface was analyzed  
263 from the angle that both, the head and the tail groups, arrange with respect to the  
264 interfacial perpendicular axis (i.e., the z-axis).

265

### 266 3. Results and discussion

#### 267 3.1. IFT calculations and identification of the salt-surfactant synergistic effect

268 We first performed MD simulations on pure water/dodecane systems with and without  
269 addition of salts at 300 K and 1 atm. These calculations were used as a benchmark to test  
270 the accuracy of the methodology and the different force fields in comparison to the  
271 experimental and simulation data available on simple systems. In the case of  
272 water/dodecane system, an equilibrium IFT value of 50.0 dyn/cm was obtained, in good  
273 agreement with reported experimental data (i.e., 51.2 – 52.3 dyn/cm [63, 64]).

274 Salts increase the equilibrium IFT because they stay at the bulk of the water phase  
275 yielding negative surface excess concentrations, which increase IFT according to Eq. (1).  
276 According to IFT results reported in the bibliography on water/oil systems with NaCl  
277 [65–68], CaCl<sub>2</sub> and MgCl<sub>2</sub> [69], IFT increases almost linearly at concentrations up to 2  
278 molal. From the experimental linear trends, we should expect that in the case of NaCl  
279  $\Delta\gamma = \gamma_{salt} - \gamma_{no\_salt}$  values are between 3.0 ~~to~~ and 3.6 dyn/cm at 2 molal. On the other  
280 hand, both divalent salts should increase IFT a similar amount between 6.0 ~~to~~ and 6.5  
281 dyn/cm at the same concentration.

282 Table 1 shows the equilibrium IFT results for the different water/salt/dodecane models  
283 by using different force fields along with their respective  $\Delta\gamma$  values.  $\Delta\gamma_{NaCl}$  is almost  
284 equivalent with the three force fields studied. CLAYFF and CHARMM increase IFT 3.7  
285 dyn/cm and 3.1 dyn/cm, respectively, which is in good agreement with the expected  
286 values [65–69]. On the other hand, OPLS seems to slightly underestimate the NaCl effect  
287 showing a  $\Delta\gamma_{NaCl} = 1.9$  dyn/cm. Although, the difference is small enough to consider  
288 these results comparable, other properties calculated in this work suggest that this  
289 underestimation might be important to reproduce some cross interactions (e.g., like  
290 surfactant-Na<sup>+</sup> interactions). These effects might be caused by a relatively low  $\epsilon$  and high  
291  $\sigma$  values of Na<sup>+</sup> OPLS parameters compared to the other force fields, which makes Na<sup>+</sup>  
292 to be more repulsive and to have less attractive crossed interactions. In the case of divalent  
293 salts, both CLAYFF and OPLS force fields are very similar, but they both give a higher  
294  $\Delta\gamma$  value for CaCl<sub>2</sub> than for MgCl<sub>2</sub> (i.e.,  $\Delta\gamma_{CaCl_2} = 7.1$  dyn/cm and  $\Delta\gamma_{MgCl_2} = 5.6$  dyn/cm  
295 for CLAYFF; and  $\Delta\gamma_{CaCl_2} = 7.2$  dyn/cm and  $\Delta\gamma_{MgCl_2} = 4.6$  dyn/cm for OPLS). On the  
296 other hand, with CHARMM force field the IFT increase is equivalent for the three salts

297 studied (i.e.,  $\Delta\gamma_{\text{NaCl}} = 3.1$  dyn/cm,  $\Delta\gamma_{\text{CaCl}_2} = 2.5$  dyn/cm and  $\Delta\gamma_{\text{MgCl}_2} = 2.5$  dyn/cm).  
 298 From these results we can extract three premises: (i) NaCl is well reproduced with all  
 299 force fields but OPLS might be slightly underestimating the interactions between the Na<sup>+</sup>  
 300 cation and other species; (ii) the divalent salts reproduced with CHARMM parameters  
 301 give IFTs too low when compared to experimental results [69]; and (iii) CLAYFF force  
 302 field seems give the best general representation of the three salts.

**Table 1.**

Equilibrium IFT results (in dyn/cm) for the water/salt/dodecane systems studied at 300 K and 1 atm using the three different force fields for salts. The values between parentheses correspond to the IFT change (i.e.,  $\Delta\gamma = \gamma_{\text{salt}} - \gamma_{\text{no\_salt}}$ ). The estimated uncertainties in these simulations are  $\pm 0.8$  dyn/cm.

	Modelled system	No salt	NaCl	CaCl <sub>2</sub>	MgCl <sub>2</sub>
CLAYFF	Oil/water/salt	50.0	53.7 (3.7)	57.1 (7.1)	55.6 (5.6)
	+ C <sub>12</sub> E <sub>3</sub>	39.0	38.7 (-0.3)	45.4 (6.4)	43.4 (4.4)
	+ (C <sub>6</sub> C <sub>5</sub> )CE <sub>3</sub>	39.0	35.5 (-3.5)	43.6 (4.6)	43.7 (4.7)
OPLS	Oil/water/salt	50.0	51.9 (1.9)	57.2 (7.2)	54.6 (4.6)
	+ C <sub>12</sub> E <sub>3</sub>	39.0	40.9 (1.9)	43.1 (4.1)	44.0 (5.0)
	+ (C <sub>6</sub> C <sub>5</sub> )CE <sub>3</sub>	39.0	40.0 (1.0)	42.4 (3.4)	41.7 (2.7)
CHARMM	Oil/water/salt	50.0	53.1 (3.1)	52.5 (2.5)	52.5 (2.5)
	+ C <sub>12</sub> E <sub>3</sub>	39.0	39.1 (0.1)	43.0 (4.0)	41.7 (2.7)
	+ (C <sub>6</sub> C <sub>5</sub> )CE <sub>3</sub>	39.0	36.9 (-2.1)	41.4 (2.4)	41.0 (2.0)

303

304 We would like to note that, even though force fields for salts do not usually use IFT as a  
 305 target function for fitting, the results obtained with the three force fields are reasonably  
 306 good. Also, the results obtained in our simulations do not state that CLAYFF is a better  
 307 force field than OPLS or CHARMM, but simply that in our system the least deviation  
 308 from the experimental results seems to be obtained by using CLAYFF parameters.  
 309 However, if other properties or systems were assessed, this could no longer be the case.  
 310 For the sake of simplicity, figures will show all the observed effects using only CLAYFF  
 311 parameters for salts, and the discussion among the different force fields will be reduced  
 312 to the minimum. All the information comparing the three force field calculations will be  
 313 available in the Supplementary Material.

314 After this preliminary evaluation, we assessed the effect of salt addition onto a  
 315 water/surfactant/dodecane system using low concentrations of a linear (C<sub>12</sub>E<sub>3</sub>) and a

316 ramified ((C<sub>6</sub>C<sub>5</sub>)CE<sub>3</sub>) non-ionic surfactant. The pure water/dodecane IFT was reduced  
317 from the previous value of 50.0 dyn/cm to 39.0 dyn/cm when adding either the linear or  
318 the ramified surfactant. In these calculations all of the surfactant molecules stay at the  
319 interface with their polar heads facing the water phase and their tail groups oriented  
320 towards the dodecane phase.

321 The addition of salt upon these systems do not show the same trends that the pure  
322 water/dodecane system. When using CLAYFF force field and the linear C<sub>12</sub>E<sub>3</sub> surfactant  
323 is present, the IFT is not increased by NaCl as before, denoting a cooperative effect  
324 between the surfactant and NaCl, which produces a small IFT reduction ( $\Delta\gamma_{\text{NaCl}} = -0.3$   
325 dyn/cm). Additionally, if NaCl is into a system containing the ramified (C<sub>6</sub>C<sub>5</sub>)CE<sub>3</sub>  
326 surfactant, this cooperative effect is enhanced, and shows a larger reduction in the IFT  
327 value ( $\Delta\gamma_{\text{NaCl}} = -3.5$  dyn/cm). On the other hand, the interactions of these surfactants  
328 with divalent cations are weaker, and the calculated  $\Delta\gamma$  does not achieve negative values.  
329 Even though divalent cations do not reduce the IFT, the  $\Delta\gamma$  obtained is lower in presence  
330 of surfactants than in the pure dodecane/water system, which suggests that a weak  
331 interaction is still present on these systems. As an example, CaCl<sub>2</sub> in absence of surfactant  
332 gives a  $\Delta\gamma_{\text{CaCl}_2} = 7.1$  dyn/cm, whereas with the linear surfactant is  $\Delta\gamma_{\text{CaCl}_2} = 6.4$  dyn/cm  
333 and with the ramified surfactant is  $\Delta\gamma_{\text{CaCl}_2} = 4.6$  dyn/cm. The interaction is even weaker  
334 with MgCl<sub>2</sub>, in which all  $\Delta\gamma$  values are relatively similar. As a summary, the results  
335 obtained suggests that salts can interact with surfactants following the order of NaCl >  
336 CaCl<sub>2</sub> > MgCl<sub>2</sub> even when they do not explicitly show an absolute IFT reduction.  
337 Additionally, regardless of the salt used, the values of  $\Delta\gamma$  tend to be ordered from the  
338 lowest to the highest as:  $\Delta\gamma_{\text{ramified}} < \Delta\gamma_{\text{linear}} < \Delta\gamma_{\text{no\_surfact}}$ , which suggest that the  
339 ramified surfactant is the molecule that interacts more strongly with salt ions, followed  
340 by the linear surfactant.

341 The same trends observed without surfactant, regarding IFT, are preserved in these  
342 simulations: the IFT reduction with NaCl is achieved also with CHARMM force field but  
343 not with OPLS, where the salt-surfactant interaction is the weakest. Similarly, divalent  
344 salts modelled with OPLS follow similar trends than CLAYFF, but the salt-surfactant  
345 interactions reproduced with CHARMM are almost inexistent.

346 The previous calculations suggest that the IFT in our system with surfactants is affected  
347 mainly by the presence of NaCl and secondarily by CaCl<sub>2</sub>. The currently proposed

348 mechanisms (explained before) assume that IFT is reduced because, somehow, the  
349 concentration of surfactant is increased at the interface. However, in our setup all  
350 surfactant molecules are already accumulated at the interface before adding the salt, so  
351 the effect must be explained from other molecular rearrangements, orientations, or  
352 microscopical interactions. In this sense, in the following sections we will analyze  
353 different factors that could be affecting the IFT and comparing the effects depending on  
354 the salt used.

355

### 356 3.2. Interfacial excess concentrations and z-distributions:

357 According to Eq. (1), the  $\gamma$  of a system depends on the interfacial excess of each added  
358 species. This magnitude can be positive if the compound accumulates at the interface,  
359 whereas it can be negative if it avoids the interface and stays at the bulk of its phase. We  
360 calculated the interfacial excess of both salt and surfactants from the z-distributions at  
361 equilibrium by means of Eq. (4), using as integration limits the center of each liquid  
362 phase. As all surfactant molecules stay at the interface for the whole simulation time, their  
363 density at the bulk is equal to 0, and the interfacial excess is the same for all calculations  
364 (i.e.,  $\rho_i^{gibbs}(z) = 0$  and  $\Gamma_i^w = 1.50 \mu\text{mol}/\text{m}^2$ ).

365 For the water/salt/dodecane systems (i.e., without surfactants), the interfacial excess of  
366 salts is always negative, which justifies the increase of the IFT. According to our results,  
367 the IFT change with the interfacial excess cannot be directly compared between different  
368 species. For example, with CLAYFF force field (Table 2), both  $\text{Ca}^{2+}$  and  $\text{Cl}^-$  have a  
369 interfacial excess of  $\Gamma_+^w = -0.45 \mu\text{mol}/\text{m}^2$  and  $\Gamma_-^w = -0.89 \mu\text{mol}/\text{m}^2$  respectively, whereas  
370  $\text{Mg}^{2+}$  and  $\text{Cl}^-$  have  $\Gamma_+^w = -0.92 \mu\text{mol}/\text{m}^2$  and  $\Gamma_-^w = -1.83 \mu\text{mol}/\text{m}^2$  respectively. If we only  
371 considered the interfacial excess of  $\text{CaCl}_2$  and  $\text{MgCl}_2$  we would conclude that  $\text{MgCl}_2$  is  
372 farther from the interface than  $\text{CaCl}_2$ , so the change in IFT when adding  $\text{MgCl}_2$  should be  
373 larger. However, with all the checked force fields  $\Delta\gamma_{\text{CaCl}_2} > \Delta\gamma_{\text{MgCl}_2}$ , or at least equal, as  
374 it can be seen in Table 1.

375 The interfacial excess of salts is generally increased by the presence of surfactants  
376 following the order  $\Gamma_{salt}^w(\text{no\_surfact.}) < \Gamma_{salt}^w(\text{C}_{12}\text{E}_3) < \Gamma_{salt}^w(\text{(C}_6\text{C}_5\text{)CE}_3)$ . This  
377 implies that the polar head groups of surfactants are interacting with the ions of salts,  
378 attracting them to the interface. Also, the ramified surfactant is more effective than the

379 linear surfactant as it can be seen with all studied force fields in Table 2. These trends  
 380 correlate with the respective values of  $\Delta\gamma$  obtained in section 3.1, suggesting again that  
 381  $(C_6C_5)CE_3 > C_{12}E_3$  and  $NaCl > CaCl_2 > MgCl_2$  for the salt-surfactant synergistic effects  
 382 in the studied system. Notice from Table 2 that the addition of NaCl onto systems with  
 383 these non-ionic surfactants can even yield positive interfacial excesses. The calculations  
 384 with positive  $\Gamma_i^w$  are the same ones that gave negative or almost zero values of  $\Delta\gamma$ . Finally,  
 385 similar trends regarding the other force fields are shown again, producing weaker effects  
 386 for the NaCl/OPLS and CaCl<sub>2</sub>/MgCl<sub>2</sub>/CHARMM force field combinations.

**Table 2.**

Gibbs interfacial excess concentrations in  $\mu\text{mol}/\text{m}^2$  for the cation ( $\Gamma_+^w$ ) and the anion ( $\Gamma_-^w$ ) of all studied systems at 300 K and 1 atm.

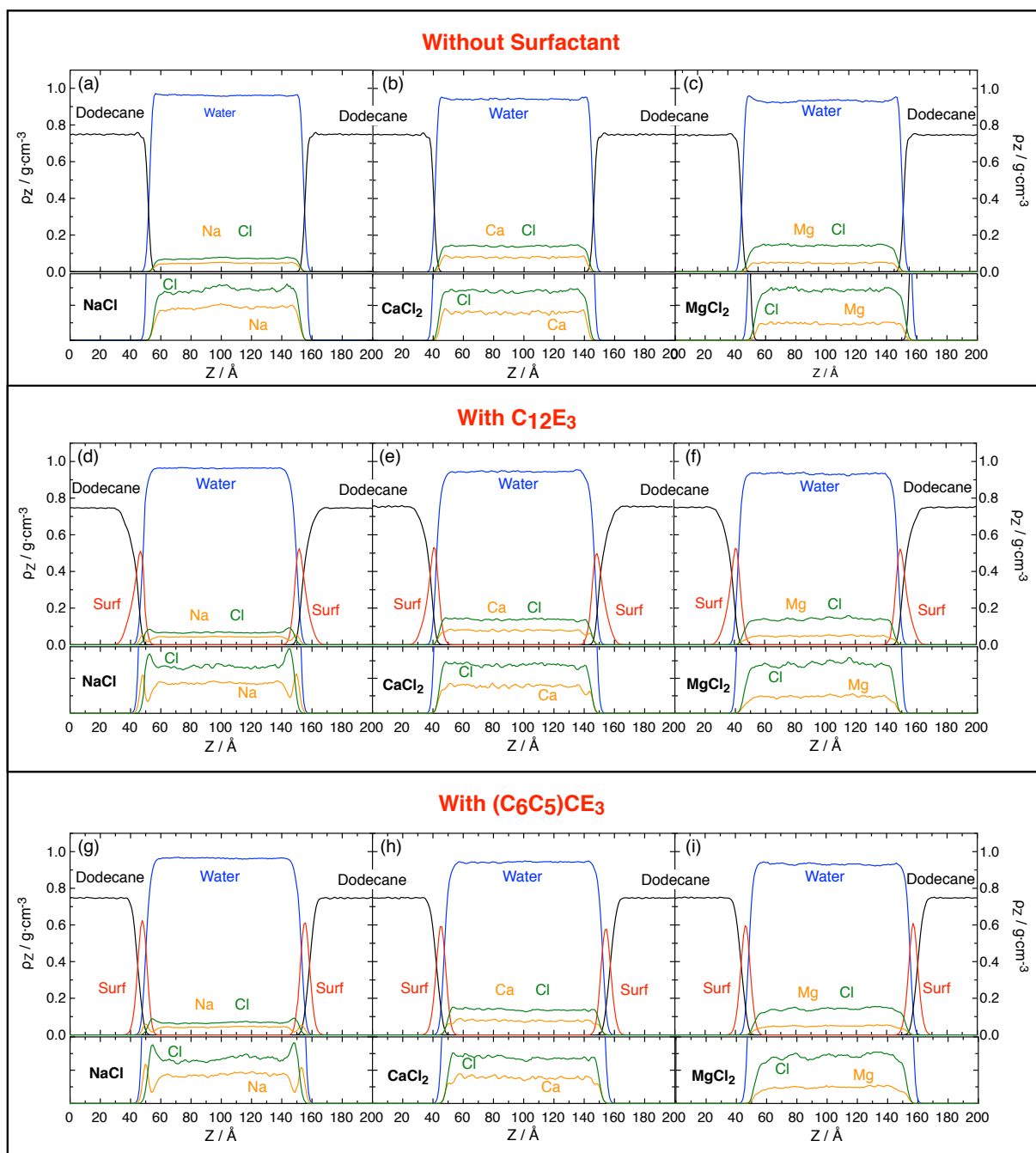
	Modelled system	NaCl		CaCl <sub>2</sub>		MgCl <sub>2</sub>	
		$\Gamma_+^w$	$\Gamma_-^w$	$\Gamma_+^w$	$\Gamma_-^w$	$\Gamma_+^w$	$\Gamma_-^w$
CLAYFF	Oil/water/salt	-0.83	-0.82	-0.45	-0.89	-0.92	-1.83
	+ C <sub>12</sub> E <sub>3</sub>	0.20	0.23	-0.29	-0.57	-0.89	-1.75
	+ (C <sub>6</sub> C <sub>5</sub> )CE <sub>3</sub>	0.22	0.29	-0.19	-0.46	-0.76	-1.51
OPLS	Oil/water/salt	-0.38	-0.40	-0.85	-1.64	-0.99	-1.99
	+ C <sub>12</sub> E <sub>3</sub>	-0.51	-0.54	-0.17	-0.34	-0.61	-1.12
	+ (C <sub>6</sub> C <sub>5</sub> )CE <sub>3</sub>	-0.31	-0.30	-0.14	-0.29	-0.45	-0.95
CHARMM	Oil/water/salt	-0.54	-0.51	-0.54	-1.12	-1.07	-2.11
	+ C <sub>12</sub> E <sub>3</sub>	0.25	0.31	-0.58	-1.19	-1.19	-2.40
	+ (C <sub>6</sub> C <sub>5</sub> )CE <sub>3</sub>	0.47	0.44	-0.66	-1.35	-0.93	-1.87

387

388 In Fig. 2 one can see the z-distributions of all studied systems. In absence of surfactant  
 389 (Fig. 2a-c) the concentration of the three salts in dodecane is zero and then, it starts  
 390 increasing in the water phase until the bulk concentration. In these systems each Na<sup>+</sup>  
 391 cation is paired with a single Cl<sup>-</sup> anion in the whole simulation cell, whereas Ca<sup>2+</sup> and  
 392 Mg<sup>2+</sup> are paired with two Cl<sup>-</sup> due to its divalent charge. However, if we add a non-ionic  
 393 surfactant onto a cell with NaCl (Fig. 2d and Fig. 2g), the salt z-distribution at the  
 394 oil/water interface changes significantly. Two very well-defined peaks (per interface)  
 395 appear in the distribution: the first is a Na<sup>+</sup> peak very close to the interface that suggest  
 396 that the polar head groups of the surfactant are attracting the cation, increasing the  
 397 interfacial excess and reducing the IFT. The second is the most intern Cl<sup>-</sup> peak,

398 approximately 5 Å away from the Na<sup>+</sup> peak, facing the water bulk. This group of ions do  
399 not interact with the surfactants as strongly as Na<sup>+</sup>, so they have been dragged towards  
400 the interface by the coulombic force of its counterions. These differences in interaction  
401 strengths induce a different ionic distribution for Na<sup>+</sup> and for Cl<sup>-</sup> at the interface,  
402 effectively producing an electric double layer, which makes the interface more polar and  
403 probably also affects the IFT (i.e., see the magnifications of Fig. 2d and Fig. 2g). The  
404 excess concentrations of divalent cations are also increased by the presence of surfactant  
405 (Table 2), but their interaction is much weaker, and their distributions do not change  
406 significantly (i.e., no differences can be appreciated in Fig. 2b-c Fig. 2e-f and Fig. 2h-g  
407 due to weaker salt-surfactant interactions).





**Fig. 2.** The  $z$ -distributions of water/salt/dodecane systems, with and without surfactant, at equilibrium. The top row (*i.e.*, (a), (b) and (c)) represents the system only with salt (*i.e.*, NaCl, CaCl<sub>2</sub> and MgCl<sub>2</sub>, respectively and without surfactant); the mid row (*i.e.*, (d), (e) and (f)) shows the distributions of the systems with the linear C<sub>12</sub>E<sub>3</sub> surfactant and the three salts; and the bottom row (*i.e.*, (g), (h) and (i)) contains the equilibrium configurations of systems with the ramified (C<sub>6</sub>C<sub>5</sub>)CE<sub>3</sub> surfactant and the salts. Below each subplot there is a zoom to see more clearly the salt distribution, in which surfactant and dodecane distributions were erased for clarity. In all plots blue lines correspond to water, black lines to dodecane, red lines to the surfactant and orange/green lines to the cation/anion of each salt, respectively. The results shown are calculated with CLAYFF force field for salts at 300 K and 1 atm.

408

409 The obtained results in this section show that cations can interact with the surfactant head  
 410 groups, which affect the distributions of salt ions at the interface. These interactions are

411 stronger in salts that showed the strongest IFT reductions (e.g., the case of Na<sup>+</sup> in Fig. 2d  
412 and Fig. 2g). In these situations, the interface even becomes polarized by an electric  
413 double layer of Na<sup>+</sup> and Cl<sup>-</sup> ions. To conclude, there is a correlation between the  
414 reorganization of interfacial cations and the IFT reduction effect. However, this is not  
415 enough to explain the salt-surfactant synergistic effect. Specifically, the IFT reduction  
416 also depends on the surfactant used, as suggested by the results compiled in Table 1 and  
417 Table 2.

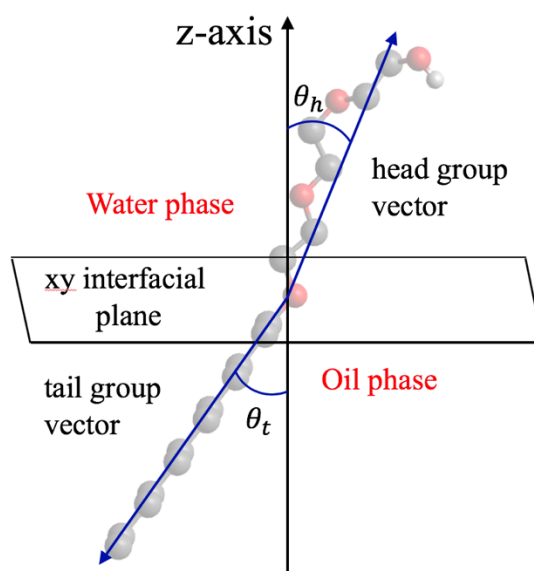
418 This IFT reduction is relatively weak when compared to the required synergistic effects  
419 needed for efficient EOR. However, the effect seen in this work is comparable to some  
420 of the abovementioned studies that use different surfactants and brines and can shed some  
421 light in explaining previously published experiments. Some examples are: Al-Sahhaf et  
422 al. [11] found IFT reductions of 2-3 dyn/cm when adding salt to both a cationic and an  
423 anionic surfactant, or Fainermann et al. [14], who showed that NaCl was capable of  
424 reducing the IFT of an oil/water /surfactant system between 5 dyn/cm and 18 dyn/cm  
425 depending on the surfactant concentration. The synergistic effect with non-ionic  
426 surfactants + NaCl has also been experimentally described close to the CMC by Bera et  
427 al. [12], even achieving resulting IFTs lower than 0.1 dyn/cm.

428

### 429 *3.3 Surfactant orientation at the interface*

430 Normally, the IFT of a system is reduced when compounds accumulate at the interface,  
431 but some works have proven that the orientation of some species can also be an important  
432 aspect to consider. In fact, the orientation of liquid crystals dramatically changes the  
433 interfacial tension (i.e., the reader is redirected to Refs. [70, 71] for a recent review of this  
434 topic). To evaluate the effect that salt ions produce towards surfactant orientation the  
435 angle between the head and the tail groups with respect to the perpendicular of the  
436 interfacial plane (i.e., the z-axis in our simulation cell) was analyzed. Both non-ionic  
437 surfactants have relatively long heads and tails, so the orientation of each group was  
438 determined separately, as it can be seen in Fig. 3. The director vector of the head group  
439 was calculated, from principal component analysis, considering the molecular axis that  
440 goes in the direction from the first oxygen atom (i.e., the closest to the tail group) to the  
441 terminal OH group. Similarly, the tail group vector was chosen as the molecular axis that  
442 follows the direction from the first atom of the tail (i.e., the CH<sub>x</sub> bonded to the first

443 oxygen) to the terminal CH<sub>3</sub> group. For the case of the ramified surfactant, each tail was  
444 considered separately. Moreover, to get information about the conformation of the  
445 surfactants at the interface, we computed the angle formed between the different groups  
446 within the same molecule (i.e., the head-tail angle for both surfactants, and the tail-tail  
447 angle for the ramified surfactant).

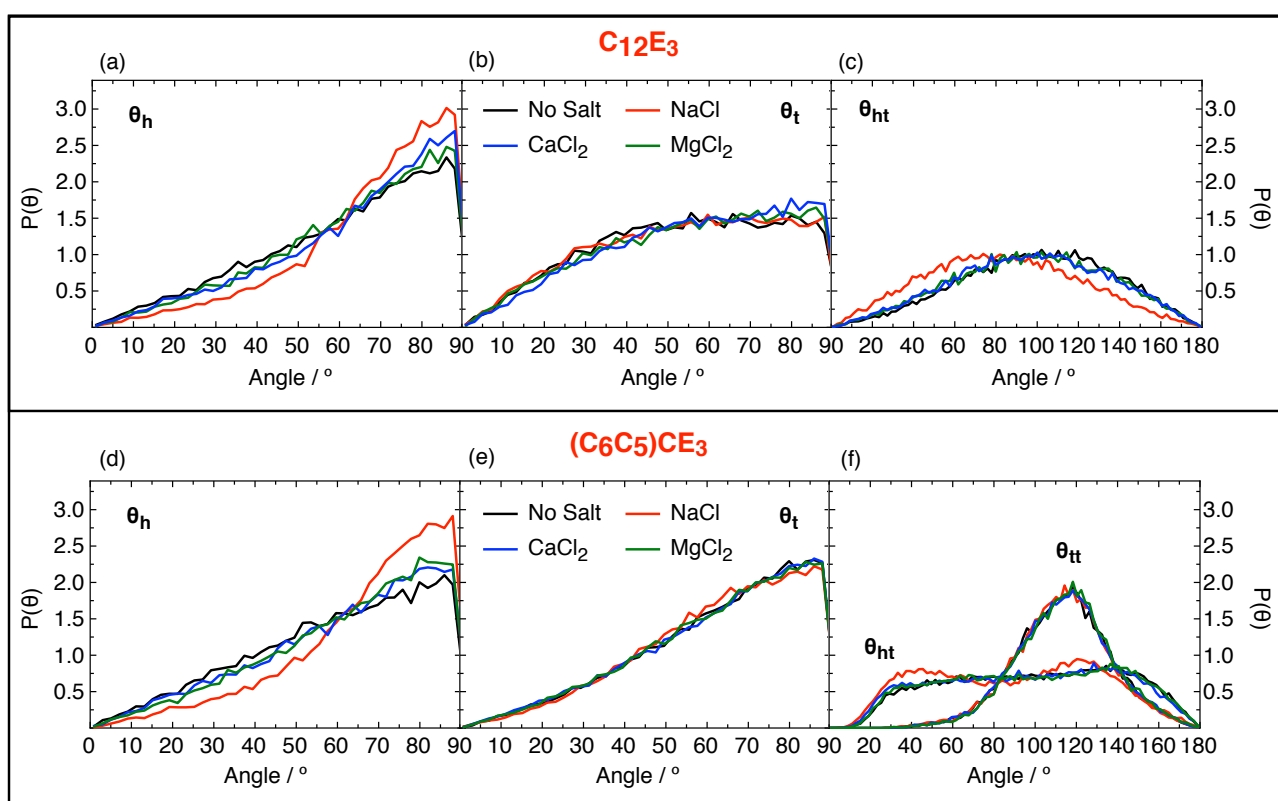


**Fig. 3.** Intramolecular reference framework used for angular distributions of the tail and the head groups of surfactant molecules at the interface.

448

449 Fig. 4 shows the angular distribution of head and tail groups for both the linear surfactant  
450 (Fig. 4a-c) and the ramified surfactant (Fig. 4d-f) in absence and presence of salt. It is  
451 worth noting that in all simulations the head groups are facing the water phase, whereas  
452 the tail groups are facing the oil phase. In absence of salt, the head groups of both  
453 surfactants (Fig. 4a and Fig. 4d) have the highest probability to be oriented almost parallel  
454 to the interfacial plane (i.e., between 70° and 90° with respect to the perpendicular axis).  
455 On the other hand, the tail groups for the linear C<sub>12</sub>E<sub>3</sub> (Fig. 4b) show a uniform random  
456 distribution at angles between 40° and 90° with respect to the z-axis, whereas the tail  
457 groups of the ramified (C<sub>6</sub>C<sub>5</sub>)CE<sub>3</sub> (Fig. 4e) have a large probability to be oriented between  
458 60° and 90°. The obtained results show that both surfactants are positioned relatively  
459 planar with respect to the interface, specially the surfactant head groups and the tail  
460 groups of the ramified surfactant. This means that the ramified surfactant should occupy  
461 more interfacial area than the linear surfactant, because it spreads more through the  
462 interface rather than pointing towards the dodecane bulk. This effect was also observed

463 in the z-distributions of Fig. 2, where the ramified surfactant distribution peak is thinner  
 464 than the one for the linear surfactant. Finally, the angle between the head and the tail  
 465 groups for both  $C_{13}E_3$  (Fig. 4c) forms a very wide distribution with the maximum of  
 466 probability located at values from  $80^\circ$  to  $130^\circ$  approximately, which suggests that the  
 467 surfactant is significantly bent (i.e.,  $180^\circ$  would be completely linear). On the other hand,  
 468  $(C_6C_5)CE_3$  presents an even flatter distribution with similar probabilities between  $30^\circ$  and  
 469  $140^\circ$ . Notice that all distributions shown here are relatively flat because surfactant  
 470 concentration is very low. This fact implies that surfactant molecules are relatively free  
 471 at the interface and their orientation is not restricted by the presence of other surface-  
 472 active molecules.



**Fig. 4.** Probability angular distributions for different groups in the linear surfactant ( $C_{12}E_3$ ) and in the ramified surfactant ( $(C_6C_5)CE_3$ ). The distribution of head groups ( $\theta_h$ ) is shown in (a) and (d), the distribution of tail groups ( $\theta_t$ ) is depicted in (b) and (e) and the head/tail ( $\theta_{ht}$ ) and tail/tail ( $\theta_{tt}$ ) angles are compiled in (c) and (f). The results correspond to the simulations performed with CLAYFF force field for salts at 300 K and 1 atm.

473

474 The addition of salt onto the system with surfactants does not affect the distribution of  
 475 any tail groups (i.e., no effects are seen in Fig. 4b and Fig 4e). However, the peak between  
 476  $70^\circ$  and  $90^\circ$  of the head group distribution is increased in the order  $NaCl > CaCl_2 > MgCl_2$ ,  
 477 as shown in Fig. 4a and Fig. 4d. Namely, this probability is increased around a 30% with

478 both surfactants when adding NaCl. This implies again that cations are able to interact  
479 with the surfactant head groups and, in average, make them become more planar towards  
480 the interface. In general, there is a clear correlation between the amplitude of this effect  
481 and the IFT reduction, which is more noticeable when adding NaCl. Additionally, as the  
482 head group angle is changing, the angle between the head and the tail groups also changes.  
483 In particular, the surfactants become more bent by effect of salts.

484 According to the results shown in this section, the orientations of surfactant head and tail  
485 groups at low interfacial concentration are relatively planar. In fact, the highest  
486 probability in their angular distribution with respect the z-axis for both groups is over 45°.  
487 Also, the ramified surfactant tail occupies more interfacial area than its linear counterpart,  
488 which implies that it should be more effective in covering the water/oil interface and in  
489 reducing the IFT. On the other hand, the distribution of head groups in both surfactants  
490 is affected similarly by salinity. The head groups became more planar with respect to the  
491 interface after the addition of NaCl, but as the ramified surfactant tail occupies more  
492 interfacial area it reduces the IFT more effectively. Finally, tail groups were not affected  
493 by the presence of salt.

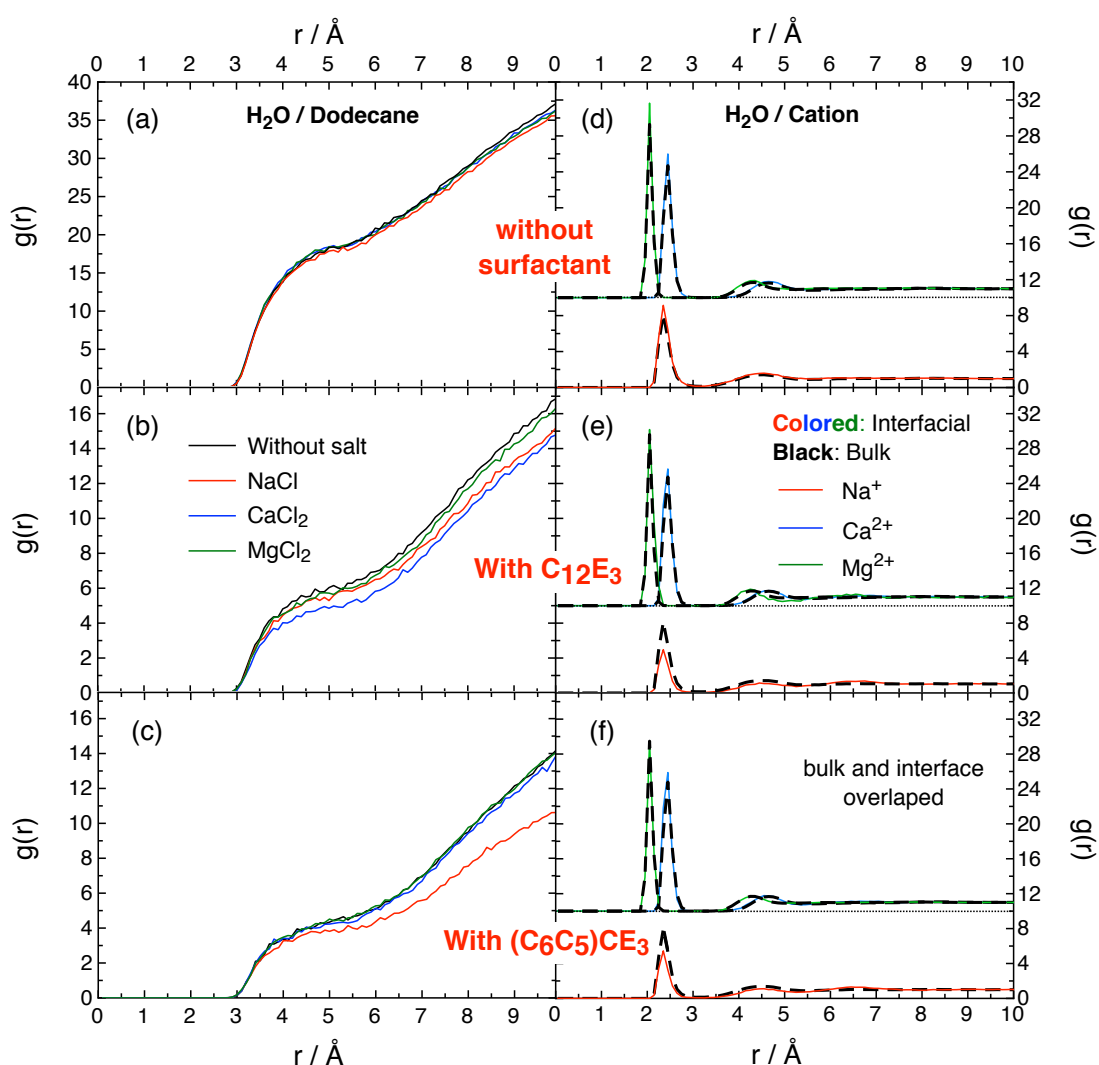
494

### 495 *3.4 Radial distribution functions*

496 We have seen in the previous sections that both, surfactants and salts are forcing each  
497 other to rearrange at the interface. In fact, we have observed a correlation between the  
498 amplitude of the IFT reduction effect in surfactant/NaCl mixtures (Table 1), the formation  
499 of the electric double layer by interfacial Na<sup>+</sup> and Cl<sup>-</sup> ions (Table 2 and Fig. 2) and the  
500 bending of surfactant head groups (Fig. 4). To know more about the interactions that drive  
501 these general patterns we have calculated the RDFs between different molecular groups  
502 (i.e., the water, the salt ions, the dodecane and the surfactant head and tail groups) and  
503 compared their interactions in absence and presence of salt.

504 First, we compared how the RDF between water and dodecane molecules close to the  
505 interface was affected by salinity for systems with and without surfactants. We have  
506 considered all atoms in dodecane and only O atoms for water when building the pair-wise  
507 distributions. The system without surfactant (Fig. 5a) shows an exactly equivalent  
508 distribution regardless of the salt used, which means that salinity does not affect

509 water/dodecane interactions. However, the systems with both the linear (Fig. 5b) and the  
 510 ramified (Fig. 5c) surfactants with NaCl, show a slightly lower RDF. This fact implies  
 511 that dodecane and water are, in average, farther away from each other because surfactants  
 512 occupy more interfacial area. This relegates dodecane and water molecules to their  
 513 respective bulks reducing the RDF. Specifically, the dodecane/water RDFs when  
 514 including surfactants and NaCl are reduced approximately a 15% and a 30% for the linear  
 515 and ramified surfactants, respectively. Notice that  $\text{Ca}^{2+}$  is also able to separate the  
 516 dodecane and water phases with the linear surfactant (Fig. 5b), as well as it was also able  
 517 to affect the orientation of the linear surfactant at the interface (Fig. 4a).

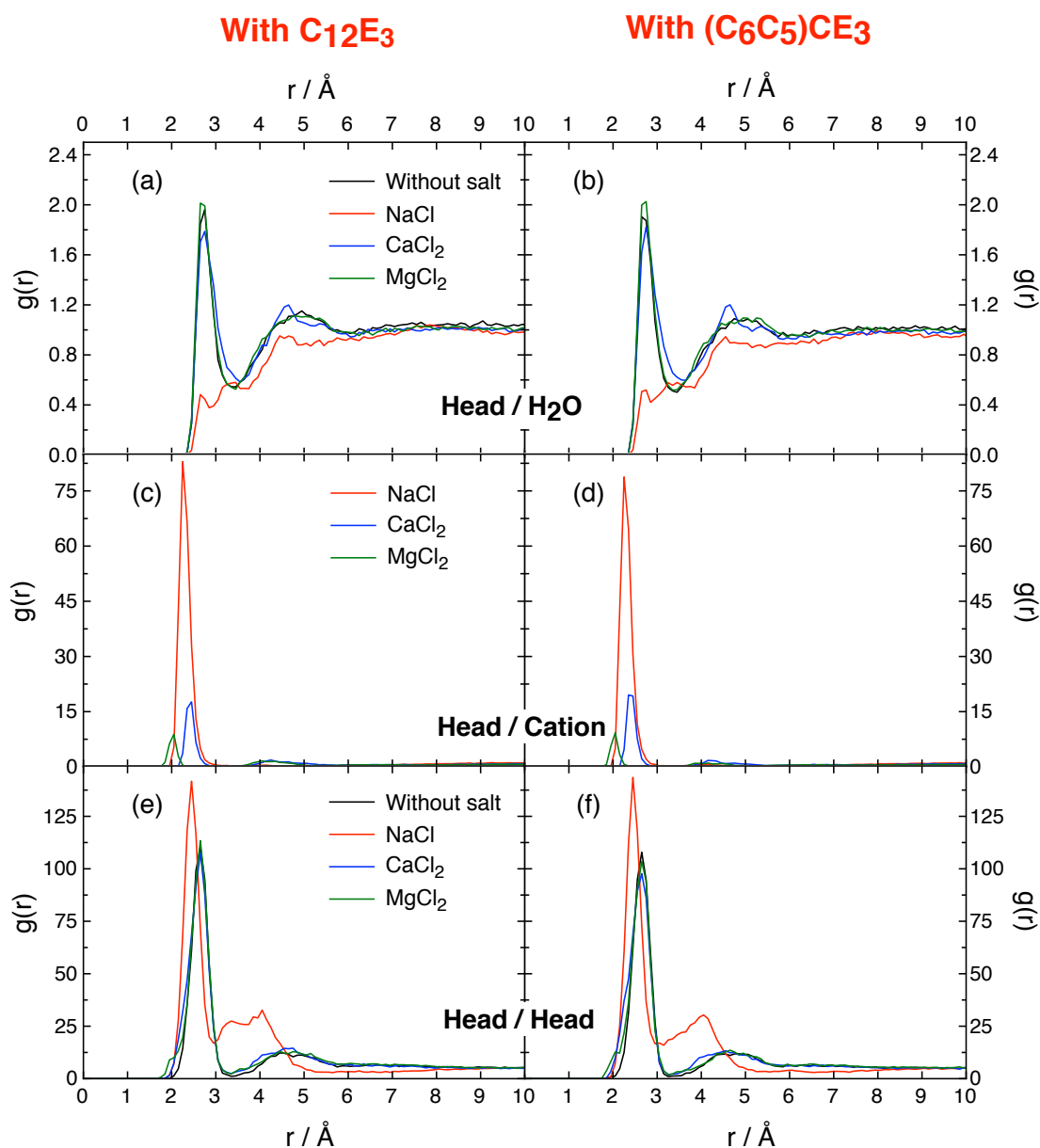


**Fig. 5.** In (a), (b) and (c) water/dodecane RDFs and in (d), (e) and (f) water/cation RDFs for molecules close to the interface in systems with and without surfactants. The black dashed lines in (d), (e) and (f) refer to the RDF of species at bulk. To build the pair-wise distributions for molecular groups, we considered the O atoms for water and the 12  $\text{CH}_x$  groups for dodecane. The results correspond to the simulations performed with CLAYFF force field for salts at 300 K and 1 atm.

518

519 Then, we analyzed how the coordination spheres of interfacial cations were perturbed  
520 with respect the cations at the bulk. To that end, water/cation RDFs were built  
521 differentiating two regions: (i) the water bulk and (ii) the interface. The interface cations  
522 were selected by listing all  $\text{Na}^+$ ,  $\text{Ca}^{2+}$  or  $\text{Mg}^{2+}$  located at less than 15 Å from any dodecane  
523 molecule, which means that are at 15 Å from the oil phase. The rest are considered bulk  
524 cations. In absence of surfactant (Fig. 5d), there is no difference between the coordination  
525 spheres of interfacial or bulk cations. However, in presence of any surfactant (Fig. 5e and  
526 Fig. 5f), the solvation spheres of interfacial  $\text{Na}^+$  are reduced a 40 % with respect bulk  
527  $\text{Na}^+$ . This result suggests that  $\text{Na}^+$  is losing part of its solvation sphere to interact closely  
528 with the surfactant. Notice that this is a necessary process to induce salt-surfactant  
529 synergistic effects because water layers screen the electrostatic charges of ions in  
530 solution, weakening the interactions between salt ions and surfactants. On the other hand,  
531 this effect is not seen with  $\text{Ca}^{2+}$  and  $\text{Mg}^{2+}$  because their interactions with water are too  
532 strong to be broken. Concretely,  $\text{Na}^+$  has a relatively weak hydration sphere with a  
533 hydration enthalpy of -98 kcal/mol [72], whereas  $\text{Ca}^{2+}$  or  $\text{Mg}^{2+}$  have -377 and -459  
534 kcal/mol, respectively [72]. These experimental information of hydration enthalpies  
535 support the conclusion that the surfactant is capable of breaking part of the hydration  
536 sphere of  $\text{Na}^+$  but is not strong enough to separate the divalent cations from their hydration  
537 sphere, as seen by water/cation RDFs.

538 Fig. 6 shows the more relevant changes due to salinity in RDFs of a system with each  
539 surfactant. First, (Fig. 6a and Fig. 6b) show the distributions between water and the  
540 surfactant head groups, where large peaks appear at 2.75 Å, denoting the average  
541 interacting distance between water and the head groups.  $\text{MgCl}_2$  does not affect water-  
542 surfactant interactions (i.e., the distribution is identical to the RDF without salt), which  
543 implies that it interacts very weakly with the head groups, followed by  $\text{CaCl}_2$  (i.e., the  
544 peak in the distribution is slightly lower than with  $\text{MgCl}_2$ ). However, this peak disappears  
545 completely in presence of  $\text{NaCl}$ , which suggest that  $\text{Na}^+$  is sequestering the surfactant  
546 head groups to prevent water/surfactant interactions. Notice that the systems with IFT  
547 reduction effects are also the ones where the cation and the surfactant lose their solvation  
548 sphere to interact with each other.



**Fig. 6.** RDF between surfactant head groups and water (a,b), head groups and the cations (c,d) or head groups with other head groups (e,f). To build the pair-wise distribution for molecular groups, we considered the O atoms for water and the O of the head groups for the surfactant heads. The results correspond to the simulations performed with CLAYFF force field for salts at 300 K and 1 atm.

549

550 Then, if we evaluate the distributions between the head groups and the ions (Fig. 6c and  
 551 Fig. 6d) we confirm the previous affirmation. Na<sup>+</sup> forms a very high and narrow peak at  
 552 2.25 Å, which denotes the strong salt-surfactant interaction. CaCl<sub>2</sub> and MgCl<sub>2</sub> form peaks  
 553 in similar position but significantly lower in height, following the same trend than in Fig.  
 554 6a-b (i.e., Ca<sup>2+</sup> has a stronger interaction with the surfactant head groups than Mg<sup>2+</sup>).  
 555 From these results, we can conclude that the surfactant head group is the responsible  
 556 moiety that interacts with Na<sup>+</sup> and force it to release from its hydration sphere.



557 Finally, salinity also affects how surfactants are arranged among themselves. In Fig. 6e  
558 and Fig. 6f one can see the head-head group distributions that, in absence of salt, form a  
559 high peak at 2.65 Å and a wider lower peak around 4.75 Å. However, in the presence of  
560 NaCl the first peak is displaced to 2.45 Å and the 2<sup>nd</sup> peak to less than 4 Å, increasing  
561 both peaks in height. This result suggests that NaCl not only sequesters the head groups  
562 from water, but also brings surfactants closer to each other (i.e., an enhanced interfacial  
563 packing).

564 Notice that the enhanced packing here validated, was already proposed by  
565 experimentalists to explain IFT reduction through a larger accumulation of surfactants at  
566 the interface [20, 21]. However, in our MD simulations all surfactant molecules are  
567 already at the interface and the IFT is still reduced, which suggests that the salt-surfactant  
568 synergistic effect also includes all phenomena described throughout this work.  
569 Additionally, the change of environment around the surfactant head groups (i.e., less  
570 surfactant/water interactions) does not imply that the surfactant is losing its interfacial  
571 activity, but it just interacts strongly with the cations that form the electric double layer  
572 at the interface.

573 The results obtained in this final section suggest that Na<sup>+</sup> is releasing from its hydration  
574 shell to strongly interact with the surfactant head groups, effectively sequestering them  
575 from water. The new arrangement between surfactants and salt forces the head groups to  
576 be more planar with respect to the interfacial plane, occupying more area and slightly  
577 expelling dodecane molecules from the interface, which increases the efficiency of the  
578 surfactant. Similar effects are seen with Ca<sup>2+</sup> but in a much weaker extent, whereas Mg<sup>2+</sup>  
579 is almost not modifying any salt-surfactant interfacial property, ranking the effects as Na<sup>+</sup>  
580 > Ca<sup>2+</sup> > Mg<sup>2+</sup>. The aforementioned interactions also induce a tighter packing of the  
581 surfactant head groups. This packing could potentially allow additional surfactant  
582 molecules to accumulate at the interface to further reduce the IFT, which is a mechanism  
583 that was already deduced from experimental observations, and is here validated through  
584 molecular dynamics simulations.

585

## 586 4. Conclusion

587 With the aim of explaining the experimentally observed salt-surfactant synergistic effect  
588 from a microscopic point of view we have performed MD simulations to study how  
589 different salts (i.e., NaCl, CaCl<sub>2</sub> and MgCl<sub>2</sub>) affect the interfacial properties of three  
590 different systems: (i) a pure water/dodecane system, (ii) the same system with additional  
591 linear non-ionic surfactants (i.e., water/dodecane/C<sub>12</sub>E<sub>3</sub>) and (iii) the first system with  
592 additional ramified non-ionic surfactants (i.e., water/dodecane/(C<sub>6</sub>C<sub>5</sub>)CE<sub>3</sub>). In this study  
593 we have been able to confirm that salt ions are capable of interacting with the surfactants  
594 changing their interfacial molecular distribution and thus affecting the IFT.

595 In summary, we have observed that cations can potentially release from its hydration  
596 sphere to interact with the surfactant head groups preventing surfactant-water  
597 interactions. These interactions affect the surfactant distributions at the interface,  
598 reducing the distance between surfactant head groups. This mechanism was proposed  
599 experimentally and is validated by the currently MD simulations but is not sufficient to  
600 explain the salt-surfactant synergistic effect on its own. Other processes are involved in  
601 lowering the IFT below the CMC, such as the more planar distribution of surfactants in  
602 presence of salt. Altogether, below the CMC, salinity helps the surfactants to rearrange  
603 and occupy more interfacial area, reducing the water/dodecane interactions and ultimately  
604 decreasing the IFT. The strong attraction felt by cations towards the surfactant molecules  
605 can lead to an increase of the interfacial excess of the salt, even achieving positive values  
606 for the  $\Gamma_{salt}^w$  (i.e., instead of the common negative values). From these results one can  
607 conclude that salt ions could (in certain conditions) accumulate at the interface and  
608 contribute to the IFT reduction as any other surface-active compound. On the other hand,  
609 anions feel less attraction from the surfactants than cations, which generates an electric  
610 double layer that polarizes the interface, being a possible additional cause of IFT  
611 reduction. The effects observed are not equivalent with all cations. Specifically, Na<sup>+</sup>  
612 seems to be the strongest interaction moiety because it can release from its hydration  
613 sphere more easily, whereas Ca<sup>2+</sup> and Mg<sup>2+</sup> present significantly weaker salt-surfactant  
614 interactions because their coulombic interactions become screened by their strongly  
615 bonded solvation water molecules. This ranks the salt-surfactant synergistic effect in this  
616 particular system to be Na<sup>+</sup> > Ca<sup>2+</sup> > Mg<sup>2+</sup>. Finally, the ramified surfactant is more  
617 effective than the linear surfactant in occupying the interface, which makes the salt-  
618 surfactant synergistic effect more noticeable.

619 All of the previously described effects are capable of slightly reducing the IFT of the  
620 system by a relatively small amount and are not capable of achieving ultralow IFT on  
621 their own. For this reason, even though the salt-surfactant effect here described works in  
622 favor of oil recovery, it could be easily overcome by other interactions that hamper oil  
623 extraction in high salinity environments.

624

## 625 **Declaration of Competing Interest**

626 The authors have no competing of interests to declare.

627

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635

## 636 **Appendix A. Supplementary material**

637 Supplementary material to this article can be found online at: \_\_\_\_\_

638

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