

# 1293. Stress arch effect on the productivity of the vertical fractured well

Fanliao Wang<sup>1</sup>, Xiangfang Li<sup>2</sup>, Gary Couples<sup>3</sup>, Donglai Wen<sup>4</sup>, Yuansheng Li<sup>5</sup>, Xiaoliang Chen<sup>6</sup>, Ning Liu<sup>7</sup>, Ling Wu<sup>8</sup>

<sup>1, 2, 5, 6, 7, 8</sup>Key Laboratory of Petroleum Engineering in China University of Petroleum Beijing, 102249, China

<sup>3</sup>Institute of Petroleum Engineering, Heriot-Watt University, Heriot-Watt University Edinburgh, EH14 4AS, UK

<sup>4</sup>Northeast Sichuan Branch, Sinopec Southwest Oil and Gas Company, Nan Chong, 637400, China

<sup>1</sup>Corresponding author

**E-mail:** <sup>1</sup>wangfanliao@163.com, <sup>2</sup>lxfang@263.net, <sup>3</sup>gary.couples@pet.hw.ac.uk, <sup>4</sup>wenxm03@163.com, <sup>5</sup>lys6891@163.com, <sup>6</sup>649447741@qq.com, <sup>7</sup>liuning3939@163.com, <sup>8</sup>wlzc\_2008@126.com

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**Abstract.** Rock permeability impacts by effective stress. Permeability modulus is used to evaluate the level of permeability reduction due to effective stress change. And the permeability modulus is always obtained by the experiment which assumes that the overburden pressure is constant during production. Actually, the overburden pressure reduces during production due to stress arch effect and it is easy to form a stress arch in the overburden when the reservoir is small and soft compared with surrounding's rock. Based on the definition of the permeability modulus, we obtain an expression between permeability modulus  $b_\gamma$  considering stress arch effect and permeability modulus  $b_0$  without stress arch. There lies a linear ship between  $b_\gamma$  and  $b_0$ , which is also proved by the experiment data. Based on the relationship between  $b_\gamma$  and  $b_0$ , a delivery equation for vertical fractured well is established. Compared with the absolute open flow with stress arch ratio of 0, the absolute open flow increases by 2.87 %, 6.79 %, 12.32 %, 20.12 % and 25.44 % for the stress arch ratio of 0.12, 0.28, 0.5, 0.8 and 1, respectively, with permeability modulus  $b_0$  of 0.0397 MPa<sup>-1</sup>. And it increases by 7.31 %, 18.1 %, 34.88 %, 61.02 % and 79.97 % for the stress arch ratio of 0.12, 0.28, 0.5, 0.8 and 1, respectively, when  $b_0 = 1$ . So absolute open flow with high permeability modulus  $b_0$  is more sensitive to stress arch ratio. Stress arch also impacts the optimum fracture half-length. Vertical well has the maximum absolute open flow when it has the optimum fracture half-length. The maximum absolute open flow increases with the increasing of stress arch ratio, while optimum fracture half-length decreases with increasing of stress arch ratio for the same permeability modulus  $b_0$ . Compared with case with no stress arch, the optimum fracture half-length reduces by 2.86 %, 5.7 %, 11.43 %, 17.14 % and 22.86 % for the stress arch ratio of 0.12, 0.28, 0.5, 0.8 and 1 respectively when  $b_0$  equals to 0.0397 MPa<sup>-1</sup>. While the maximum absolute open flow increases by 1.6 %, 3.8 %, 7.16 %, 12.02 % and 15.60 % for the stress arch ratio of 0.12, 0.28, 0.5, 0.8 and 1 respectively. Thus, vertical well considering stress arch needs smaller fracture half-length than that with no stress arch. Meanwhile, the maximum absolute open flow and optimum fracture conductivity both increase as stress arch ratio increases. Compared with the case without stress arch, the optimum fracture conductivity increases by 50 %, while the maximum absolute open flow increases by 21.40 % with stress arch ratio of 0.5 when  $b_0$  equals to 0.0397 MPa<sup>-1</sup>. The stress arch greatly impacts on the stress sensitive permeability, permeability modulus and well performance, which can't be neglected especially in the low and ultra-low permeability reservoir.

**Keywords:** overburden pressure, stress arch effect, stress arching ratio, sulige gas field, permeability modulus, delivery equation.

## 1. Introduction

Rock permeability is sensitive to the effective stress. Permeability modulus is always used to evaluate the permeability reduction due to effective stress change [1]. Permeability modulus can

be obtained by the experiment data and all previous experiments assume that the overburden pressure is constant during production [2-7]. Some authors established the delivery equation considering the stress sensitivity of permeability based on the definition of the permeability modulus [8-9]. And they concluded that production of the low and ultra-low permeability reservoir is significantly affected by the stress sensitivity of permeability.

However, the reservoir, unlike a free body, is attached to the surrounding rocks. Due to the internal driving forces and external constrains, change of overburden pressure may be occurred, which is called stress arch effect [10]. When stress arch generates, part weight of the overburden is supported by the sideburden during reservoir compaction [10-15]. Stress arching ratio is used to describe the value of the overburden pressure drop per unit pore pressure drop and it is related to the reservoir's geometry and rock properties of the reservoir and surrounding's rock [10-14]. When the reservoir is small and soft compared with the surrounding rock, it is easy to form a stress arch in the overburden [13-19]. So, the permeability modulus obtained by the experiment, which assumes that the overburden pressure is constant, can't reflect the permeability change during the production and the delivery equation can't reflect the productivity during the production.

In the previous work, we find that the stress sensitive permeability is significantly impacted by the stress arch effect [20]. In this paper, we begins with the definition of the permeability modulus. A new permeability modulus considering stress arch effect is established, which is proved by experiment data in Sulige gas field. Based on this new permeability modulus, a delivery equation for vertical fractured well is established. Then, we analysis the stress arch influence on productivity, optimum fracture half-length and optimum fracture conductivity.

## 2. Permeability modulus considering stress arch effect

Permeability modulus, which is used to evaluate the change of permeability induced by production, which is defined as [1]:

$$b_0 = \frac{1}{K(p)} \frac{\partial K(p)}{\partial p}, \tag{1}$$

where  $b_0$  is permeability modulus without stress arch,  $\text{MPa}^{-1}$ .  $K(p)$  is permeability measured at the pressure of  $p$ , md. When Biot's coefficient  $\alpha$  equals to 1, the effective stress change can be described as follows:

$$d\sigma = dS_v - dp = -dp, \tag{2}$$

where  $d\sigma$  is effective stress change, MPa.  $dS_v$  means the overburden pressure change, which equals to 0 when there is no stress arch in the overburden. So the permeability modulus can also be expressed as:

$$b_0 = \frac{1}{K(p)} \frac{\partial K(p)}{\partial p} = -\frac{1}{K(\sigma)} \frac{\partial K(\sigma)}{\partial \sigma}. \tag{3}$$

When a stress arch forms in the overburden, the permeability modulus still can be defined as Eq. (4):

$$b_\gamma = \frac{1}{K(p)} \frac{\partial K(p)}{\partial p}, \tag{4}$$

where  $b_\gamma$  is permeability modulus with stress arch. The effective stress considering stress arch effect can be expressed as Eq. (5) when Biot's coefficient  $\alpha$  equals to 1 [10]:

$$d\sigma = dS_v - dp = -(1 - \gamma)dp. \tag{5}$$

Then permeability modulus considering stress arch effect can be described as Eq. (6):

$$b_\gamma = \frac{1}{K(p)} \frac{\partial K(p)}{\partial p} = - \frac{1 - \gamma}{K(\sigma)} \frac{\partial K(\sigma)}{\partial \sigma}, \tag{6}$$

where  $\gamma$  is stress arch ratio, dimensionless. Stress arch ratio is defined as the ratio between stress change and pore pressure change, which varies between 0 and 1. The stress arch ratios can be calculated by the theories of inclusion and inhomogenities, and they are greatly impacted by the reservoir geometry, Poisson's ratio and the shear module ratio between the reservoir and surrounding rocks [10].

Combined Eq. (3) with Eq. (6), there is a linear ship between permeability modulus considering stress arch effect and permeability modulus without stress arch:

$$b_\gamma = b_0(1 - \gamma). \tag{7}$$

When  $\gamma = 0$ , there is no stress arch in the overburden, so  $b_\gamma = b_0$ . When  $\gamma = 1$ , the overburden pressure change equals to pore pressure change and effective stress remains unchanged during production. The permeability change is induced by effective stress change, so there is no permeability stress sensitivity with stress arch ratio of 1 and  $b_\gamma$  equals to 0.

From the definition of the permeability modulus, permeability for different pore pressure can be expressed as Eq. (8):

$$k = k_i \exp[-b_0(1 - \gamma)(p_i - p)]. \tag{8}$$

In the following part, we will used the experiment date to validate Eqs. (7) and (8). Sulige gas field is located at the Ordos basin of China, and covers an area of 20000 km<sup>2</sup>. The field is large sandstone reservoir of braided river system with stratigraphic traps. He 8 and Shan 1 are the main producing formations. Statistics show that 75 % of the effective sand body is isolated, and most of the isolated sand body is produced by one well. The main shape of the reservoirs can be classified as penny shape reservoir and elliptical cylinder reservoir. The penny shape reservoirs are common in the Sulige gas field and they take amount of 70.4 %. The maximum of the stress arch ratios are 0.12 and 0.28 for elliptical cylinder reservoir and penny shape reservoir respectively [20]. The normalized permeability is defined as the ratio of the permeability for current reservoir pressure and initial permeability. The normalized permeabilities are listed as Figs. 1-3 when the stress arch ratios are 0, 0.12 and 0.28 respectively.

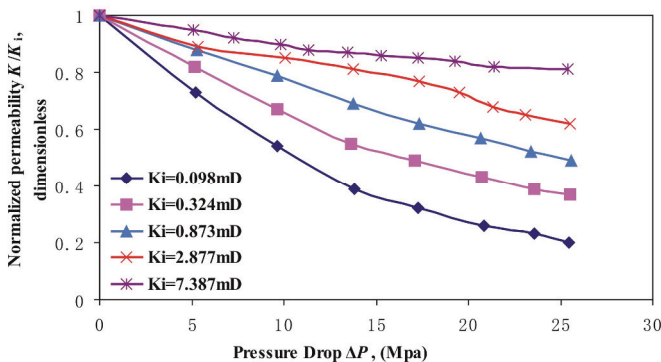


Fig. 1. Normalized permeability  $K/K_i$  versus pressure drop  $\Delta P$  for stress arching ratios  $\gamma$  of 0

There lies in a negative exponential relationship between normalized permeability and

pressure drop. The permeability modulus obtained by the experiment data and predicted by Eq. (7) are listed in Table 1.

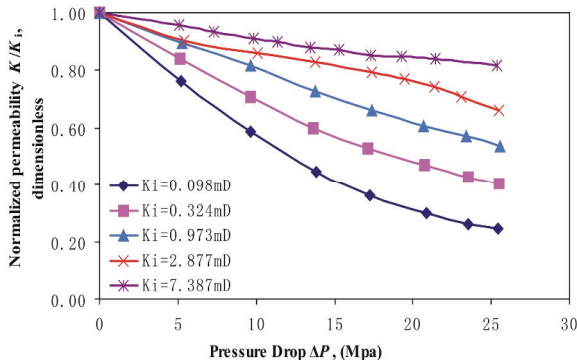


Fig. 2. Normalized permeability  $K/K_i$  versus pressure drop  $\Delta P$  for stress arching ratios  $\gamma$  of 0.12

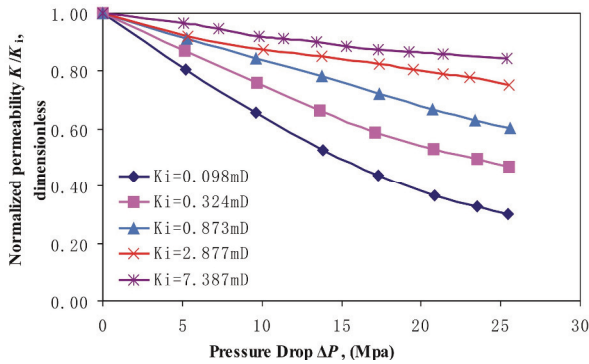


Fig. 3. Normalized permeability  $K/K_i$  versus pressure drop  $\Delta P$  for stress arching ratios  $\gamma$  of 0.28

Table 1. Permeability modulus of permeability for different stress arch ratios

$K_i$ , (mD)	$b_0$	$b_{0.12}$			$b_{0.28}$		
		Tested	Predicted	Error, %	Tested	Predicted	Error, %
0.0987	0.0635	0.057	0.0559	-1.9	0.0483	0.0464	-3.9
0.324	0.0397	0.0361	0.0349	-3.3	0.0304	0.029	-4.6
0.873	0.0283	0.0248	0.0249	0.4	0.0201	0.0207	3.0
2.877	0.018	0.0146	0.0158	8.2	0.0105	0.0131	24.8
7.387	0.0084	0.008	0.0074	-7.5	0.0069	0.0061	-11.6

From Table 1, the predicted values of the permeability modulus are the same as the values obtained by the experiment data. The relative error varies between -1.9 % and 24.8 % and most relative errors are small. So we can use the Eq. (7) to predict the permeability modulus if there is no experiment date for different stress arch ratios. However, this method can't be used if there lies no negative exponential relationship between normalized permeability and pressure drop.

### 3. Delivery equation for vertical fractured well with stress arch

#### 3.1. Idealization and description of the fractured system

Yang, et al. [21] established a fracture system to simplify the calculation of the productivity of the vertical fracture well and they also used the field date to prove that their model could predict the well performance effectively. The relative error of the predict value is 8 %, which is very small.

Guo, et al. [22] also used this fracture system to establish their delivery equation to calculate the absolute open flow, the result was validated by the well test date. The relative error is 2 %. Thus, we still use this fracture system to illustrate stress arch effect on the vertical gas well productivity.

The fracture system in two dimension, illustrated in Fig. 4, has some assumptions as follows.

- 1) The gas producing layer with constant thickness and uniform initial permeability is bounded above and below by impermeable strata.
- 2) After the well is fractured, the cylindrical outer boundary is neither too near nor too far from the fracture.
- 3) The artificial fracture is represented by two parallel planes, which has the limited length  $2X_f$  and fracture conductivity.
- 4) The fracture is bounded by the impermeable matrix above and below the producing layer.
- 5) Gravity effects are neglected, the flow behavior in the reservoir will be independent of the vertical position.
- 6) The reservoir can be divided into two regions, the flow patterns are different in these two regions. In region I, the flow pattern is pseudo radial flow, while it is linear flow in the region II.
- 7) Flow entering the wellbore comes only through the fracture.
- 8) The flow in the reservoir considers the stress sensitivity of permeability, while the flow in the fracture obeys high-velocity non-Darcy flow.
- 9) Neglect the change of the fracture permeability.
- 10) There is no skin near the wellbore.

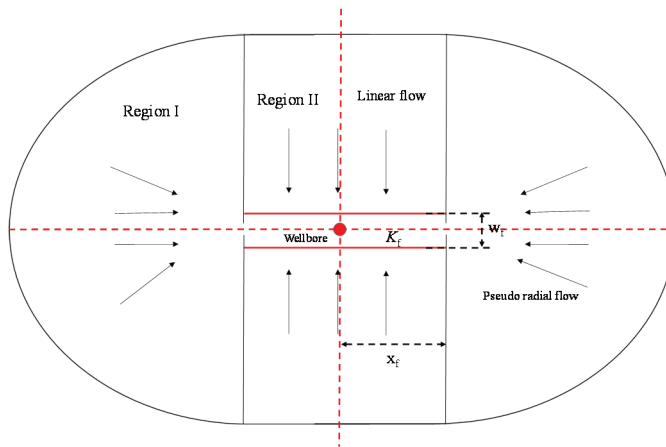


Fig. 4. Schematic diagram of fractured system

### 3.2. Model of delivery equation for the well

In region I, the flow pattern is pseudo radial flow. When the gas flow reaches the fracture, the flow obeys the high-velocity flow through fracture to wellbore. In region II, the flow pattern is linear flow. When it reaches the surface of the fracture, the flow obeys the high-velocity flow through fracture to wellbore.

#### 3.2.1. Pseudo radial flow in region I

For steady state flow condition, Darcy's law for the radial flow of gas can be expressed as:

$$u = \frac{k dp}{\mu dr} \tag{9}$$

where  $u$  is flow velocity, m/s;  $k$  is gas permeability, md;  $\mu$  is gas viscosity, mPa·s;  $p$  is reservoir pressure, MPa;  $r$  is radius at pressure of  $p$ , m.

Substituting Eq. (8) into Eq. (9) gives:

$$\frac{p \exp[-b_0(1-\gamma)(p_i-p)]}{\mu Z} dp = \frac{Q_1 P_{sc} T}{2\pi h Z_{sc} T_{sc} k_i r} dr, \tag{10}$$

where  $Q_1$  is flow rate for pseudo radial flow,  $m^3/s$ ;  $P_{sc}$  is reservoir pressure at standard conditions, MPa;  $h$  is reservoir thickness, m;  $Z$  is compressibility factor, fraction;  $Z_{sc}$  is compressibility factor at standard conditions, fraction;  $T$  is absolute reservoir temperature, K;  $T_{sc}$  is absolute reservoir temperature at standard condition, K.

Let:

$$f(p) = \frac{p \exp[-b_0(1-\gamma)(p_i - p)]}{\mu Z} \quad \text{and} \quad m(p) = \int f(p) dp,$$

Eq. (10) can be written as:

$$m(p_i) - m(p_{wf1}) = \frac{6.455 \times 10^{-4} T Q_{1sc}}{k_i h} \cdot \ln \frac{2r_e}{w_f}, \tag{11}$$

where  $P_{wf1}$  is pressure on both ends of the fracture, MPa;  $Q_{1sc}$  is gas production rate at standard conditions,  $m^3/d$ ;  $r_e$  is the radius of drainage, m;  $w_f$  is the width of the fracture, m.

In region I, the flow in fracture with non-Darcy flow effect can be represented by Forchheimer's equation:

$$-\frac{dp}{dl} = \frac{\mu}{k_f} u_2 + \beta_g \rho_g u_2^2, \tag{12}$$

where gas density  $\rho_g$  and flow velocity  $u_2$  are shown in Eqs. (13) and (14) respectively:

$$\rho_g = \frac{M_a \gamma_g p}{ZRT}, \tag{13}$$

$$u_2 = \frac{ZT p_{sc} Q_1}{2w_f h p Z_{sc} T_{sc}}, \tag{14}$$

where  $k_f$  is fracture permeability, mD;  $u_2$  is flow velocity in fracture, m/s;  $\gamma_g$  is relative density of gas, fraction;  $\rho_g$  is gas density,  $kg/m^3$ ;  $M_a$  is the relative molecular mass of air;  $R$  is universal gas constant;  $\beta_g$  is turbulent factor,  $m^{-1}$ .  $\beta_g = \text{Constant}/k_f^a$ , we commonly use the following equation:

$$\beta_g = \frac{1.21}{k_f^{3.23}}. \tag{15}$$

Substituting Eqs. (13) and (14) into Eq. (12) yields:

$$p_{wf1}^2 - p_w^2 = \frac{4.054 \times 10^{-3} \bar{Z} \bar{\mu} T}{w_f k_f h} (x_f - r_w) Q_{1sc} + \frac{2.788 \times 10^{-20} \beta_g \gamma_g \bar{Z} T}{w_f^2 h^2} (x_f - r_w) Q_{1sc}^2, \tag{16}$$

where  $p_w$  is bottom hole pressure, MPa;  $r_w$  is radius of wellbore, m;  $x_f$  is fracture half-length, m;  $\bar{Z}$  is average gas compressibility factor;  $\bar{\mu}$  is average gas viscosity, mPa.s.  $\bar{Z}$  and  $\bar{\mu}$  are calculated by average pressure, which is the arithmetic mean between initial reservoir pressure and bottom hole pressure.

### 3.2.2. Linear flow in region II

In region II, the flow equation for steady state flow can be expressed as:

$$u = \frac{k_i \exp[-a_0(1 - \gamma)(p_i - p)]}{\mu} \frac{dp}{dr} = \frac{Q_2 P_{sc} Z T}{4 x_f h p Z_{sc} T_{sc}}, \quad (17)$$

where  $Q_2$  is flow rate for linear flow pattern, m<sup>3</sup>/s. Based on the definition of  $m(p)$ , Eq. (17) gives:

$$m(p_i) - m(p_{wf2}) = \frac{1.013 \times 10^{-3} T Q_{2sc}}{k_i x_f h} \left( r_e - \frac{w_f}{2} \right), \quad (18)$$

where  $p_{wf2}$  is the pressure for both side of fracture surface, MPa;  $Q_{2sc}$  is flow rate for linear flow pattern, m<sup>3</sup>/d.

In region II, the flow in fracture with non-Darcy flow effect can be represented by Forchheimer's equation. Then:

$$p_{wf2}^2 - p_w^2 = \frac{4.054 \times 10^{-3} Q_{2sc} \bar{Z} \bar{\mu} T}{w_f k_f h} (x_f - r_w) + \frac{2.788 \times 10^{-20} \beta_g \gamma_g \bar{Z} T Q_{2sc}^2}{w_f^2 h^2} (x_f - r_w). \quad (19)$$

So the total production rate can be expressed as:

$$Q_{sc} = Q_{1sc} + Q_{2sc}, \quad (20)$$

where  $Q_{sc}$  is the total production rate, m<sup>3</sup>/d.

### 3.2.3. Solution method

1) Initial reservoir  $p_i$  and bottom hole pressure  $p_w$  are known. Give initial  $Q_{1sc}(1)$ , so  $p_{wf1}(1)$  can be calculated by Eq. (16).

2) Let:

$$a(1) = m(p_i) - m(p_{wf1}(1)), \quad b(1) = \frac{6.455 \times 10^{-4} T Q_{1sc}(1)}{k_i h} \cdot \ln \frac{2r_e}{w_f}.$$

If the absolute value of the difference between  $a(1)$  and  $b(1)$  is less than 1,  $Q_{1sc} = Q_{1sc}(1)$ ,  $p_{wf1} = p_{wf1}(1)$ . While it is greater than 1, then  $Q_{1sc}(i) = Q_{1sc}(i - 1) + 1$ ,  $p_{wf1}(i)$ ,  $a(i)$  and  $b(i)$  will be calculated until  $|a(i) - b(i)| \leq 1$ , then  $Q_{1sc} = Q_{1sc}(i)$ ,  $p_{wf1} = p_{wf1}(i)$ .

3) Using the same method, we can get  $Q_{2sc}$  and  $p_{wf2}$ .

4) Using Eq. (20) to calculate the total production rate.

## 4. Effect of stress arch on productivity of vertical fractured well

To analyze the stress arch influence on well productivity, the following basic data are needed. Reservoir thickness  $h$  is 10 m; Absolute temperature  $T$  is 395 K; Reservoir initial permeability  $k_i$  is 0.324 mD; Radius of drainage area  $r_e$  is 800 m; Radius of wellbore  $r_w$  is 0.1 m; Fracture half-length  $x_f$  is 200 m; Fracture width  $w_f$  is 0.005 m; Fracture permeability  $k_f$  is 40 D; Relative density of gas  $\gamma_g$  is 0.76; Initial reservoir pressure  $p_i$  is 31.33 MPa; Permeability modulus  $b_0$  is 0.0397 MPa<sup>-1</sup>.

### 4.1. Stress arch effect on IPR curve

Fig. 5 is a series of IPR curves for different stress arch ratio. It is shown that the well production rate increase with the increasing of the stress arch ratio when the permeability modulus  $b_0$  of 0.0397 MPa<sup>-1</sup>. Stress arch greatly impacts on well production rate for large pressure drop. When

$\gamma = 0$ , the absolute open flow is the least one, and the production rate declines quickly as the bottom hole pressure decreases. While,  $\gamma = 1$ , the absolute open flow is the largest one and the production rate declines slowly. Compared with the absolute open flow with stress arching ratio of 0, the absolute flow increases by 2.87 %, 6.79 %, 12.32 %, 20.12 % and 25.44 % for the stress arching ratio of 0.12, 0.28, 0.5, 0.8 and 1 respectively when  $b_0$  equals to 0.0397 MPa<sup>-1</sup>.

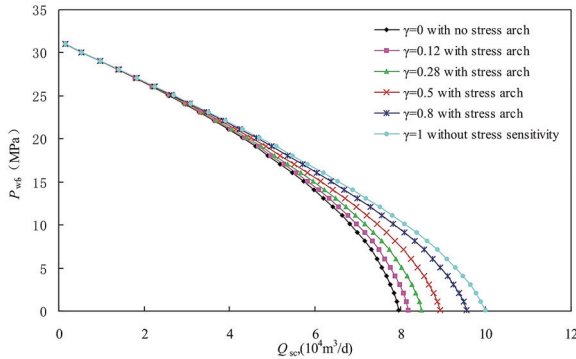


Fig. 5. IPR curve for different stress arching ratio with  $b_0 = 0.0397 \text{ MPa}^{-1}$

For different permeability modulus  $b_0$ , the absolute open flow  $Q_{aof}$  for different stress arching ratio is shown in Fig. 6.

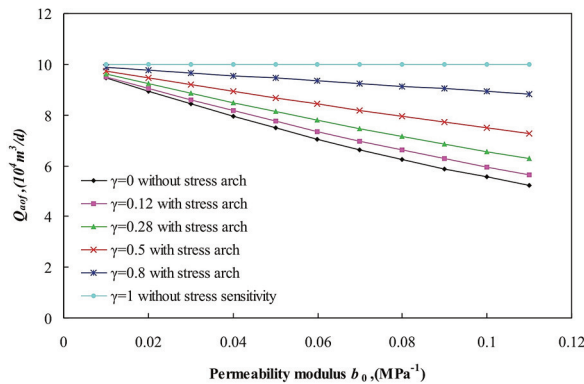


Fig. 6.  $Q_{aof}$  versus permeability modulus  $b_0$  for different stress arching ratio

Fig. 6 shows that absolute open flow  $Q_{aof}$  decreases with the increase in permeability modulus  $b_0$ . Compared with the absolute open flow with no stress arch,  $Q_{aof}$  increases by 0.67 %, 1.56 %, 2.80 %, 4.50 % and 5.63 % for the stress arching ratio of 0.12, 0.28, 0.5, 0.8 and 1 respectively when  $b_0$  equals to 0.01 MPa<sup>-1</sup>. It increases by 7.31 %, 18.1 %, 34.88 %, 61.02 % and 79.97 % for the stress arching ratio of 0.12, 0.28, 0.5, 0.8 and 1 respectively when  $b_0 = 1$ . For the same stress arching ratio, the larger the permeability modulus  $b_0$  is, that is, the larger the permeability reduction is, the larger the increase of the absolute open flow is. It should be noted that the absolute open flow remains unchanged when stress arching ratio equals to 1 because there is no permeability change during the production.

#### 4.2. Stress arch effect on optimum fracture half-length

Fig. 7 shows the correlation between the absolute open flow  $Q_{aof}$  and fracture half-length at a given fracture permeability, say 40 D.  $Q_{aof}$  increases as the fracture half-length increases until it reaches to the maximum value.



If the vertical well has the optimum fracture half-length, the  $Q_{aof}$  is the largest one at the same stress arch ratio. Fig. 8 indicates that the maximum  $Q_{aof}$  increases with the increase in stress arch ratio, while optimum fracture half-length decreases with increasing of stress arch ratio for the same permeability modulus  $b_0$ . Compared with the optimum fracture half-length with no stress arch, it decreases by 2.86 %, 5.7 %, 11.43 %, 17.14 % and 22.86 % for the stress arch ratio of 0.12, 0.28, 0.5, 0.8 and 1 respectively. While the maximum  $Q_{aof}$  increases by 1.6 %, 3.8 %, 7.16 %, 12.02 % and 15.60 % for the stress arch ratio of 0.12, 0.28, 0.5, 0.8 and 1 respectively. It means that vertical well can have large production rate with small fracture half-length and large stress arch ratio.

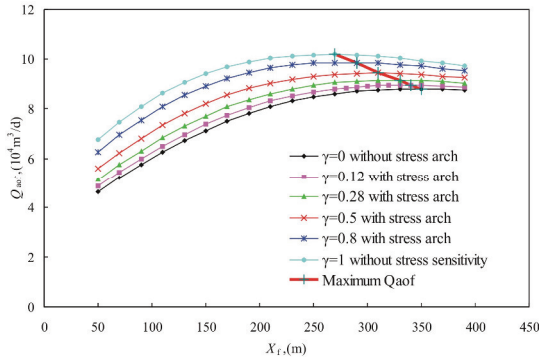


Fig. 7.  $Q_{aof}$  versus fracture half-length for different stress arching ratio with  $b_0$  of  $0.0397 \text{ MPa}^{-1}$

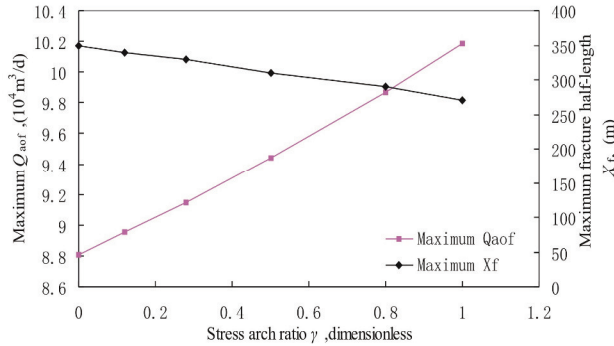


Fig. 8. Maximum  $Q_{aof}$  and maximum fracture half-length versus stress arch ratio with  $b_0$  of  $0.0397 \text{ MPa}^{-1}$

### 4.3. Stress effect on optimum fracture conductivity

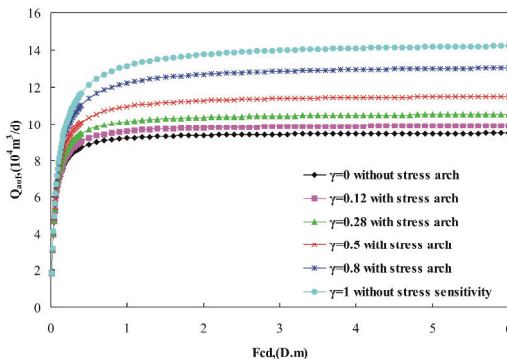


Fig. 9.  $Q_{aof}$  versus  $F_{cd}$  for different stress arching ratio with  $b_0$  of  $0.0397 \text{ MPa}^{-1}$

Fig. 9 shows the correlation between absolute open flow  $Q_{aof}$  and fracture conductivity  $F_{cd}$ . For the same stress arch ratio, the  $Q_{aof}$  increases as  $F_{cd}$  increases until it reaches the maximum value, then it remains nearly unchanged. The vertical well has maximum  $Q_{aof}$  when the fracture has the optimum fracture conductivity. For the same  $F_{cd}$ , the  $Q_{aof}$  increases with the increase in stress arch ratio.

The maximum  $Q_{aof}$  and optimum fracture conductivity both increase with the increasing of stress arch ratio. Compared with the case without stress arch, the maximum fracture conductivity increases by 100 %, while the maximum  $Q_{aof}$  increases by 49.29 % with stress arch ratio of 1.

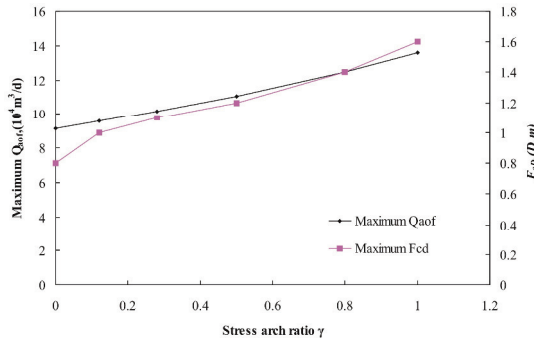


Fig. 10. Maximum  $Q_{aof}$  and maximum  $F_{cd}$  versus stress arch ratio with  $b_0$  of 0.0397 MPa<sup>-1</sup>

### 5. Discussion

Reservoirs are dynamic systems and they continually change during production. As the pore pressure reduces, formation permeability decreases especially for the low permeability and tight gas reservoir. Permeability modulus is used to describe the level of permeability damage. The larger the permeability modulus is, the larger the permeability reduction is. The low permeability or tight gas reservoir has large permeability modulus, which means that the rock with low permeability is more sensitive to effective stress than the rock with high permeability. The permeability modulus is relevant to stress arch ratio. Based on the definition of permeability modulus, we get an expression between permeability modulus  $b_\gamma$  with stress arch and permeability modulus  $b_0$  without stress arch. There lies a linear ship between  $b_\gamma$  and  $b_0$ , which is proved by the experiment data. When stress arch ratio equals to 0, there is no stress arch formed in the overburden, so  $b_\gamma = b_0$ . If  $\gamma = 1$ , there is no stress sensitivity in the reservoir,  $b_\gamma$  equals to 0.

Meanwhile, a delivery equation for vertical fracture well considering stress arch effect is established. It shows that the stress arch greatly impacts on the well productivity, optimum fracture half-length and fracture conductivity. The absolute open flow increases with the increasing of the stress arch ratio for the same  $b_0$ . The stress arch influence on the absolute open flow is also relevant to  $b_0$ . It is more obvious when the rock has the large permeability modulus  $b_0$  than the rock with small one. It means that stress arch has greater effect on the productivity of low permeability reservoir than that of high permeability reservoir.

The absolute open flow  $Q_{aof}$  reaches the maximum value when the vertical well has the optimum fracture half-length for the same fracture permeability. The maximum  $Q_{aof}$  increase with the increase in stress arch ratio, while optimum fracture half-length decreases with increasing of stress arch ratio for the same permeability modulus  $b_0$ . So vertical well has large production rate with small fracture half-length and large stress arch ratio. The vertical well also has maximum  $Q_{aof}$  when the fracture has the optimum fracture conductivity. The maximum  $Q_{aof}$  and optimum fracture conductivity both increase with the increasing of stress arch ratio.

This study emphasizes that stress arch effect on stress sensitivity of permeability and well productivity. We also want to note that the level of permeability damage for low permeability and tight gas reservoir is relevant to stress arch effect. We can't make a conclusion that the low and ultra-low permeability do exist the strongest stress sensitivity. Meanwhile we can't neglect the stress arch effect when we design the oil and gas develop plan for the low and ultra-low permeability reservoir.

It should be noted that if stress sensitive permeability has no exponential relationship with pressure drop or effective stress change, the relationship between  $b_\gamma$  and  $b_0$  may be complicated and need to be proved in the future. For thin reservoir, the horizontal stress arch ratio is larger than vertical stress arch ratio in general. So if the rock is under non hydrostatic stress condition, stress sensitive permeability is a function of stress state and stress arch ratios both in vertical and horizontal directions. And it's more difficult to describe the relationship between  $b_\gamma$  and  $b_0$ , which should also be researched in the future. Meanwhile the delivery equation used here is established on some simple assumption, which should also be improved in the future.

## 6. Conclusion

Based on the definition of the permeability modulus, we obtained an expression between permeability modulus considering stress arch effect ( $b_\gamma$ ) and permeability modulus without stress arch ( $b_0$ ). There lies a linear ship between  $b_\gamma$  and  $b_0$ , which is proved by the experiment data. When stress arch ratio equals to 0, there is no stress arch formed in the overburden, so  $b_\gamma = b_0$ . If  $\gamma = 1$ , there is no stress sensitivity in the reservoir,  $b_\gamma$  equals to 0. The rock with low initial permeability has the larger permeability modulus than that of high initial permeability.

A new delivery equation for vertical fracture well is established, and which is considered the stress arch effect. Compared with the absolute open flow with stress arch ratio of 0, the absolute flow increases by 2.87 %, 6.79 %, 12.32 %, 20.12 % and 25.44 % for the stress arch ratio of 0.12, 0.28, 0.5, 0.8 and 1 respectively when the permeability modulus  $b_0$  equals to 0.0397 MPa<sup>-1</sup>. The increase ratio with larger  $b_0$  is larger than that with small one.

The optimum fracture half-length is also relevant to stress arch ratio. For the same stress arch ratio, the vertical well has the maximum absolute open flow when it has the optimum fracture half-length. The maximum  $Q_{aof}$  increase with the increase in stress arch ratio, while optimum fracture half-length decreases with increasing of stress arch ratio for the same permeability modulus  $b_0$ . Compared with case with no stress arch, the fracture half-length reduces by 11.43 %, while the maximum  $Q_{aof}$  increases by 7.16 % when the stress arch ratio equals to 0.5. Considering stress arch effect, vertical well can have large production rate with small half-length.

The maximum  $Q_{aof}$  and optimum fracture conductivity both increase with the increasing of stress arch ratio. Compared with the case without stress arch, the maximum fracture conductivity increases by 50 %, while the maximum  $Q_{aof}$  increases by 21.40 % with stress arch ratio of 0.5.

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