# Asynchronous Byzantine Consensus with 2f+1 Processes (extended version)

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# Asynchronous Byzantine Consensus with 2f+1 Processes (extended version)<sup>\*</sup>

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# ABSTRACT

Byzantine consensus in asynchronous message-passing systems has been shown to require at least 3f + 1 processes to be solvable in several system models (e.g., with failure detectors, partial synchrony or randomization). Recently a couple of solutions to implement Byzantine fault-tolerant state machine replication using only 2f + 1 replicas have appeared. This reduction from 3f + 1 to 2f + 1 is possible with a hybrid system model, i.e., by extending the system model with trusted/trustworthy components that constrain the power of faulty processes to have certain behaviors. Despite these important results, the problem of solving Byzantine consensus with only 2f + 1 processes is still far from being well understood. In this paper we present a methodology to transform crash consensus algorithms into Byzantine consensus algorithms with different characteristics, with the assistance of a reliable broadcast primitive that requires trusted/trustworthy components to be implemented. We exemplify the methodology with two algorithms, one that uses failure detectors and one that is randomized. We also define a new flavor of consensus and use it to solve atomic broadcast, showing the practical interest of the transformations.

# **Categories and Subject Descriptors**

D.4.7 [**Operating Systems**]: Organization and Design— Distributed Systems

# **General Terms**

Algorithms, Performance

## Keywords

Distributed algorithms, Consensus, Byzantine fault toler-

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## 1. INTRODUCTION

*Consensus* is an important distributed computing problem, both in theoretical and practical terms. The problem consists in making a set of processes to agree on one of the values that each one of them proposes. From a theoretical point of view, consensus has been used to show important impossibility and possibility results, the most well-known of which is probably the Fischer-Lynch-Paterson (FLP) impossibility of solving consensus deterministically in an asynchronous system if one process can fail [14]. From a practical point of view, the problem has been shown to be equivalent to several distributing computing problems [18, 9], so an implementation of a consensus algorithm can be used as a building block of distributed systems [17].

Distributed algorithms depend strongly on the system model considered. A realistic model for many of the current large-scale, open distributed systems is the *asynchronous Byzantine message-passing* system model. The time model is asynchronous in the sense that no bounds are assumed for the communication and processing times. The fault model is Byzantine, meaning that some of the processes can fail arbitrarily, even maliciously. The impossibility of solving consensus deterministically in this system model comes trivially from the FLP impossibility result, but the problem is solvable in several variations of this basic system model.

Consensus in the asynchronous Byzantine message-passing model has been shown to require  $n \ge 3f+1$  processes, where f is the maximum number of faulty processes, to be solvable in several variations of the basic system model, e.g., with failure detectors  $[10, 1]^1$ , partial synchrony [13] or randomization [3]. Reducing the ratio n/f is important theoretically, but also in practice as reducing the number of processes/processors has an impact on the cost of a real system.

Recently a few solutions to implement Byzantine fault-tolerant state machine replication (that requires solving consensus) using only  $n \ge 2f + 1$  replicas have appeared [8, 5]. This reduction from 3f + 1 to 2f + 1 is possible with a hybrid system model, i.e., by extending the asynchronous Byzantine system model with components that can not fail in a Byzan-

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<sup>&</sup>lt;sup>1</sup>Baldoni et al. present a sophisticated algorithm that assumes  $f \leq min(\lfloor (n-1)/2 \rfloor, C)$ , where C is the maximum number of faulty processes allowed by the certification algorithm [1]. However, as they point out, "known certification techniques assume  $n - C = \lceil \frac{2n+1}{3} \rceil$ ." This means that in practice their algorithm also requires  $n \geq 3f + 1$ .

tine way. These trusted/trustworthy components constrain the power of the adversary in the sense that the services they provide can not be corrupted and become faulty. We call these components simply *wormholes* using Verissimo's nomenclature [29]. Systems with wormholes are no longer homogeneous but hybrid: most of the system is still asynchronous Byzantine but the wormhole is trusted/trustworthy by construction.

State machine replication consists in replicating a service in a set of n servers, f of which may be faulty [27]. Correia et al. use a wormhole called trusted timely computing base (TTCB) to help define an order for the execution of the clients' requests with only 2f + 1 servers [8]. The TTCB defines an order for a client's request when f + 1 servers show it that they have the request. More recently, Chun et al. used an attested append-only memory (A2M) abstraction (or wormhole) with the same purpose [5]. A2M forces the servers to commit to a monotonically increasing sequence of operations.

### This paper

Despite these important results, the problem of solving asynchronous Byzantine consensus with only 2f + 1 processes is still far from being well understood. There are several reasons for this: the related works that we cited solve consensus but have the solution for this problem submerged in the complications of a larger problem (state machine replication); they are based on special-purpose components (TTCB, A2M) that researchers are not familiarized with.

The main objective of this paper is to contribute to a better understanding of the problem of consensus with only 2f+1 processes. To reach this objective, the paper presents a methodology to transform asynchronous consensus algorithms that tolerate crash faults and require 2f + 1 processes, into similar algorithms that tolerate Byzantine faults also with 2f + 1 processes. The paper demonstrates the methodology with two previously existing crash fault-tolerant consensus algorithms: an algorithm by Mostefaoui and Raynal that uses failure detectors to circumvent FLP [23] and a probabilistic algorithm by Ben-Or that uses randomization with the same purpose [2]. The methodology to do this modification, which is not necessarily generic, consists in enhancing the algorithm with a set of mechanisms that constrain the power of faulty processes, allowing the algorithm to reach consensus even if there is an adversary that tries to break the algorithm's properties.

The idea of modifying crash into Byzantine fault-tolerant algorithms, or *improving the fault tolerance*, was previously explored by Neiger and Toueg [24], and Coan [6]. The former present two transformations for synchronous systems: one from crash to omission faults and another from omission faults to Byzantine faults. Coan presents a compiler for asynchronous algorithms that transforms crash faulttolerant algorithms into Byzantine fault-tolerant algorithms, just like our methodology, but considers only the case of approximate agreement and does not provide Byzantine faulttolerant algorithms for 2f + 1 processes, which is the main purpose of the present paper.

Like previous works, to solve asynchronous Byzantine consensus with 2f + 1 processes we need trusted / trustworthy components, or wormholes, that provide certain incorruptible services. However, we use the abstraction provided by the wormhole to obtain a communication primitive commonly used in distributed computing: reliable broadcast. This primitive ensures that all processes (i) deliver the same messages and (ii) deliver all messages sent by correct (i.e., non-faulty) processes. More precisely, we present a reliable broadcast algorithm that imposes no bounds on the number of faulty processes, unlike previous existing algorithms that require  $n \ge 3f+1$  [3]. A fortiori, this algorithm also satisfies its properties with  $n \ge 2f+1$  processes.

Using a 2f + 1 reliable broadcast to solve 2f + 1 Byzantine consensus is interesting for two reasons. First, it tackles the difficulty of understanding how a wormhole assists in solving a distributed computing problem, by using it to solve a well-known problem, reliable broadcast. Second, it is important to understand that it is possible to solve 2f + 1 Byzantine consensus by relying only on a 2f + 1 reliable broadcast and no other "unusual" component (e.g., no other component that needs a wormhole to be implemented).

The transformation methodology also requires a *mute*ness failure detector, which detects if a process apparently stopped following the algorithm [11]. The consensus algorithms presented are *indulgent* [16], in the sense that they not violate their safety properties no matter the behavior of the failure detector, which is only needed to ensure termination.

The consensus flavor we consider with the methodology satisfies a weak validity property. Therefore, we introduce a new flavor of consensus, *endorsement consensus*, and use it to solve atomic broadcast with only 2f + 1 processes, thus showing that our consensus algorithms are useful to solve a distributed computing problem with practical interest.

### Contributions

The contributions of the paper are mainly the following:

- from a *theoretical* point of view, it shows that a 2f + 1 reliable broadcast primitive is enough to solve 2f + 1 asynchronous Byzantine consensus, with the assistance of a muteness failure detector;
- from a practical point of view, it presents a methodology to transform asynchronous crash consensus algorithms into asynchronous Byzantine consensus algorithms with different characteristics keeping the number of processes as  $n \ge 2f + 1$ ; this reduces the number of processes needed to tolerate the same number of faulty ones that is n = 3f + 1 in asynchronous Byzantine systems; the paper also presents two 2f + 1 asynchronous Byzantine consensus algorithms.

# 2. PRELIMINARIES

### 2.1 Asynchronous Byzantine System Model

The system is composed by a set of n processes  $\Pi = \{p_1, p_2, ..., p_n\}$ . A process is said to be *correct* if it follows its algorithm, otherwise it is said to be *faulty*. Faulty processes can deviate from the algorithm arbitrarily, i.e., we assume the existence of *Byzantine faults* [21]. However, no more than  $f = \lfloor \frac{n-1}{2} \rfloor$  can be faulty (in the tight case n = 2f + 1).

Processes communicate by message-passing. Every pair of processes is linked by an authenticated reliable channel, which does not allow the creation, modification or dropping of messages. In a malicious environment this involves either physically secure communication channels or the use of cryptographic mechanisms, which requires the additional assumption of a computationally bounded adversary.

The system is asynchronous, which means that there are no bounds on the processing times or communication delays. However, we assume the existence of failure detector modules in each of the processes. Failure detectors (FDs) give hints about faulty processes. The original FDs were used to suspect that processes crashed [4]. In this paper we consider *muteness failure detectors*, which suspect that a process is *mute*, either because it crashed or is Byzantine and stopped sending messages according to the algorithm [11]. Unlike crash FDs, muteness FDs depend on the algorithm,  $\mathcal{A}$ .

We consider a class of muteness FDs that is inspired in Chandra and Toueg's eventually perfect FD, which we call eventually perfect muteness FD,  $\Diamond \mathcal{MP}_{\mathcal{A}}$ . Failure detectors of this class satisfy the following properties:

- Mute strong A-completeness. Eventually every process that is mute to any correct process p is permanently suspected by p.
- Eventual strong A-accuracy. There is a time after which correct processes are not suspected by any correct process.

This FD is stronger than FDs used in previous Byzantine consensus algorithms [11, 1], but the two properties are satisfied in partition-free partially synchronous systems [13]. Doudou et al. provide an implementation  $\mathcal{I}_{\mathcal{D}}$  of the muteness failure detector  $\Diamond \mathcal{M}_{\mathcal{A}}$  that they introduce [11]. Although that FD satisfies only eventual weak  $\mathcal{A}$ -accuracy, it is simple to show that  $\mathcal{I}_{\mathcal{D}}$  is also an implementation of  $\Diamond \mathcal{MP}_{\mathcal{A}}$  in the same system model.

### 2.2 Reliable Broadcast

The basic system model of the previous section is extended with a reliable broadcast primitive. The reliable broadcast problem consists essentially in making all correct processes *deliver* the same messages [3]. Furthermore, if the process that *broadcasts* the message is correct, then all correct processes deliver the message, and no two messages with the same identifier are delivered by any correct process. Formally, a reliable broadcast algorithm can be defined in terms of the following properties [18] (we consider that the sender also delivers the messages it broadcasts):

- *RB1 Validity.* If a correct process broadcasts a message *m*, then some correct process eventually delivers *m*.
- *RB2 Agreement*. If a correct process delivers a message *m*, then all correct processes eventually deliver *m*.
- RB3 Integrity. For any identifier id and sender p, every correct process q delivers at most one message m with identifier id from sender p, and if p is correct then m was previously broadcast by p.

Bracha presented a reliable broadcast algorithm that needs  $n \ge 3f+1$  processes [3]. A proof that 3f+1 is the minimum number of processes was provided by Toueg [28].

### Wormhole

Consider that there is a set of trusted/trustworthy wormholes  $\Upsilon = \{w_1, w_2, ..., w_n\}$  and that process  $p_j$  has access exclusively to wormhole  $w_j$ . Each wormhole  $w_j$  has a publicprivate key pair  $(K_{uj}, K_{rj})$ . The private key  $K_{rj}$  is known only by  $w_j$  and is used to produce digital signatures. Every correct process knows the correct public key  $K_{uj}$  of every wormhole  $w_j$ . The wormholes provide a single service that can be abstracted as a function that is called by the processes (for wormhole  $w_j$ ):  $\sigma \leftarrow sign_j(id, msg)$ . The function takes as parameters a message identifier id and a message msg. It returns either the signature  $\sigma \in S$  of (id, msg) or  $\perp \notin S$ , where S is the set of possible signatures. The signature is returned if id > id', where id' is the identifier given as parameter in the previous call to the function; otherwise  $\perp$  is returned.

This service is simple but it precludes a faulty process from obtaining two different messages with the same identifier correctly signed. Algorithm 1 uses this service to solve Byzantine fault-tolerant reliable broadcast with any number of faulty processes. The wormhole can be implemented inside a secure coprocessor, a smartcard or another hardware board. Further discussion on the implementation of wormholes can be found in papers on the topic, e.g., [8, 5].

### The algorithm

The proposed reliable broadcast algorithm is similar to the classical crash fault-tolerant reliable broadcast algorithm [18] In relation to Bracha's algorithm, it has one less communication step due to the use of the wormhole and requires no bounds on the number of faulty processes. The algorithm is requested to *broadcast* a message by calling RELIABLE\_BROADCAST(*id*, *msg*) (first line) and a message is *delivered* when DELIVER(*j*, *id*, *msg*) is called by the algorithm (lines 3, 6). Basically the sender sends the message to all processes and all processes send an ECHO message also to all processes. The wormhole is used to prevent a faulty sender from sending two different messages with the same identifier as explained above. Function  $verify(id, msg, \sigma, K_{uj})$  verifies if the signature  $\sigma$  was obtained with message (*id*, *msg*) and key  $K_{rj}$  (line 4).

A proof of correctness of the algorithm is provided in the appendix.

### 3. METHODOLOGY AND CONSENSUS

Informally, consensus is the problem of making a set of processes to agree on a value. A process p is said to propose a value  $v \in \mathcal{V}$  for an execution of the consensus algorithm when it calls \*\_2FBC\_CONSENSUS(v) (with \* equal to MR or BO). The process is said to decide a value v when the algorithm calls DECIDE(v). There are several definitions of Byzantine consensus in the literature. In this section we consider the following definition, which is the most common for crash consensus [18, 23, 15]<sup>2</sup>, and is also much used for Byzantine consensus [10, 1]. Byzantine asynchronous multi-valued consensus is defined in terms of the following properties:

• *MVC1 Validity*. If a correct process decides v, then v was proposed by some process.

 $<sup>^{2}</sup>$ Crash consensus is also often defined in terms of *uniform* properties, which make statements about what is decided by faulty processes. These properties are not enforceable in the Byzantine fault model in which faulty processes can have an arbitrary behavior.

### **Algorithm 1** Reliable broadcast algorithm (at process $p_i$ )

### **Function** RELIABLE\_BROADCAST(*id*, *msq*)

### Task T1:

1:  $\sigma \leftarrow sign_i(id, msg)$ 

2:  $\forall j \neq i$ : SEND INITIAL $(i, id, msg)_{\sigma}$  to  $p_j$ 

 $\overline{3}$ : Deliver(i, id, msg)

Task T2: {execute only once per message broadcast}

4: when (message INITIAL  $(j, id, msq)_{\sigma}$  or ECHO $(j, id, msq, \sigma)$  is received) and (verify $(id, msq, \sigma, K_{uj})$ ) do

 $\forall k \neq j : \text{SEND ECHO}(j, id, msg, \sigma) \text{ to } p_k$ 5:

DELIVER(j, id, msg)6:

- 7: end when
  - MVC2 Agreement. No two correct processes decide differently.
  - MVC3 Termination. Every correct process eventually decides.

This section presents the methodology to transform crash consensus algorithms into Byzantine consensus algorithms. The section starts by introducing the methodology with a concrete example, the transformation of the Mostefaoui and Raynal's crash fault-tolerant consensus algorithm (MR\_Consensus broadcast primitive (messages PHASE1 and PHASE2) or by for short) [23] into a Byzantine fault-tolerant algorithm. Then, it presents the methodology itself (Section 3.2) and applies it to Ben-Or's algorithm (Section 3.3).

#### 3.1 Mostefaoui and Raynal's Algorithm

Algorithm 2 is the modified algorithm, MR\_2FBC, Like the original algorithm, MR\_Consensus  $[23]^3$ , it is based on a rotating coordinator. Each round (lines 3-13), one of the processes is selected to be the coordinator (line 4) and tries to impose its estimate as the decision (line 5). Each round has two phases. In the first (lines 5-7), the coordinator disseminates a PHASE1 message with its estimate of the value to be decided. In the second phase (lines 8-12), each process disseminates a PHASE2 message with the estimate of the coordinator or  $\perp \notin \mathcal{V}$ . If a correct process receives n-f PHASE2 messages with the same value, it decides this value and disseminates this decision using a DECISION message (line 11).

Some of the modifications to MR\_Consensus are clear: reliable channels are substituted by authenticated reliable channels and message disseminations are substituted by the reliable broadcast primitive (lines 5, 8). Notice that the identifier (id) of a message disseminated is composed by the message type (e.g., PHASE1) and the round number.

Another modification is that we use the message validation mechanism introduced by Bracha [3] to prevent some of the attacks that might be done by faulty processes. In several places the algorithm only takes into account messages that are valid (lines 7, 9, 10, 14). Informally, a message is said to be valid if it is justified by the messages previously received by the process. For instance, line 14 seems to be wrong since the process  $p_i$  should require DECISION messages from f + 1 processes, for at least one to be sent by a correct process, before deciding in line 15. However, the validation

mechanism ensures that the condition in that line is true only if the DECISION message might have been sent by a correct process, i.e., if  $p_i$  received n - f PHASE2 messages with the same estimate est (lines 9-11).

The definition of *valid* message is identical to Bracha's. Each step k of the algorithm has the following basic format: the process disseminates a message to all other processes, waits for a set S of messages from the other processes, and obtains the content of the next message using a protocol function F(k, S). A message that is delivered by the reliable a reliable channel (messages DECISION) at step k is called a k-message. Each process  $p_i$  maintains a set of messages  $VALID_i$  such that:

- $VALID_i^1 = \{ \text{ delivered } 1\text{-}messages \}$
- for  $k > 1, m_j^k \in VALID_i^k$  if there exist n f (k-1)-messages  $m_1, ..., m_{n-f}$  such that  $m_j^k = F(k, \{m_1, ..., m_{n-f}\})$

The main difference from MR\_2FBC to MR\_Consensus is line 9. In MR\_Consensus, processes wait until they receive messages from n - f processes (line 8 of Fig. 1 at [15]). Clearly it is not possible to block waiting for more messages as f processes can be faulty. However, there is an important difference between the crash and the Byzantine fault models: while in the crash fault model (thus in MR\_Consensus) all of those n - f messages are sent by processes that follow the algorithm, in the Byzantine fault model (thus in MR\_2FBC) f of those messages can be sent by faulty processes. In the worst case, with n = 2f + 1 and f Byzantine processes, in every round that set of n - f messages contains f + 1 messages, f of which sent by Byzantine processes<sup>4</sup>. The behavior of these f faulty processes is constrained by the message validation mechanism, but they can do a simple attack that is undistinguishable from correct behavior: to send always  $\perp$  as their estimate, pretending that their FD modules suspect of the coordinator (lines 6-8).

To deal with this problem, line 9 must "know about" all processes before continuing. More precisely, line 9 waits for messages from n - f processes, but also either for messages or to suspect of the rest of the processes. This ensures that eventually  $p_i$  receives messages from all correct processes, as there is a time after which correct processes are not suspected by any correct process (eventual strong  $\mathcal{A}$ -accuracy). This is also the reason why we need a stronger FD than previous Byzantine consensus algorithms, that require only eventual weak A-accuracy [11, 1]. While those algorithms

 $<sup>^{3}\</sup>mathrm{We}$  consider two simplifications introduced by Friedman and the same authors in [15]: the relation between f and n is given by  $f = \lfloor \frac{n-1}{2} \rfloor$  (instead of  $n \ge 2f + 1$ ); and we consider only the case of eventually strong failure detector  $\Diamond S$  (they consider also strong failure detectors).

<sup>&</sup>lt;sup>4</sup>This is not the case with 3f + 1 Byzantine consensus algorithms as they wait for 2f+1 messages, a majority of which must come from correct processes.

**Algorithm 2** MR\_2FBC Byzantine consensus algorithm (code for process  $p_i$ )

### **Function** MR\_2FBC\_CONSENSUS $(v_i)$

Task T1:

1:  $r_i \leftarrow 0$  {round number} 2:  $est_i \leftarrow v_i$  {current estimate of the value to be decided} 3: while true do 4:  $c_i \leftarrow (r_i \mod n) + 1; \quad r_i \leftarrow r_i + 1 \quad \{c_i = \text{coordinator}\}$ phase 1: coordinator to all -5:if  $(c_i = i)$  then RELIABLE\_BROADCAST PHASE1 $(r_i, est_i)$  end if 6:wait until (message PHASE1 $(r_i, -)$  is received from  $p_{c_i}$  or  $p_{c_i}$  is suspected by  $p_i$ 's FD module) 7: if  $(valid \text{ message PHASE1}(r_i, v) \text{ received from } p_{c_i})$  then  $aux_i \leftarrow v$  else  $aux_i \leftarrow \bot$  end if phase 2: all to all --} RELIABLE\_BROADCAST PHASE2 $(r_i, aux_i)$ 8. 9: wait until (valid message PHASE2( $r_i$ , -) are received from at least n-f processes) and ( $\forall j$ : valid message PHASE2( $r_i$ , -) is received from  $p_j$  or  $p_j$  is suspected by  $p_i$ 's FD module) 10:  $\forall j : \mathbf{if} (valid \text{ message PHASE2}(r_i, v) \text{ received}) \mathbf{then} R_i[j] \leftarrow v \mathbf{else} R_i[j] \leftarrow \bot \mathbf{end} \mathbf{if}$  $\exists v \neq \perp : \#_v(R_i) \geq n-f)$  then  $est_i \leftarrow v; \forall j \neq i : \text{SEND DECISION}(r_i, est_i)$  to  $p_j; \text{DECIDE}(est_i)$  else if  $(\exists v \neq \perp : \#_v(R_i) \geq n-2f)$  then  $est_i \leftarrow v$  end if end if if 11: $12 \cdot$ 13: end while Task T2: 14: when valid message DECISION(r, est) is received do {no need of f + 1 messages due to the validation mechanism} 15:  $\forall j \neq i$ : SEND DECISION(r, est) to  $p_j$ ; DECIDE(est)16: end when

require only that the coordinator is eventually not suspected, MR\_2FBC requires that eventually no correct process is suspected, i.e., eventual *strong* A-accuracy.

Recall that the protocol function F(k, S) is the function used to obtain the next message to be sent. The function comes trivially from the algorithm pseudo-code. The notion of step used to define the protocol function in this case is a phase. The formal specification of the function can be found in the pseudo-code itself, but informally the function is the following (for process  $p_i$  in round r):

- to obtain a PHASE1 message: if  $p_i$  is the coordinator, the function returns  $p_i$ 's estimate; otherwise, it does not return anything (the message is not defined, the function is not called);
- to obtain a PHASE2 message: if  $p_i$  received a valid PHASE1 $(r_i, v)$  message from the coordinator in round r then the function returns v, otherwise it returns  $\perp$ ;
- to obtain a DECISION message: if  $p_i$  received n f valid PHASE2 messages with the same estimate v, then return v; otherwise, it does not return anything (the message is not defined, the function is not called).

A proof of correctness of the algorithm is provided in the appendix.

### **3.2** The Methodology

The transformation of Mostefaoui and Raynal's algorithm into a 2f + 1 Byzantine consensus algorithm illustrates the application of the methodology for increasing the fault tolerance of crash algorithms. The methodology consists in doing the following modifications, then prove the correctness of the resulting algorithm:

1. Communication channels: communication channels are substituted by *authenticated reliable channels*. These channels constrain the power of the adversary in the network in the sense that these channels do not allow the creation, modification or dropping of messages.

- 2. Broadcast communication: broadcasts are substituted by reliable broadcasts. This mechanism constrains the power of the adversary by preventing it from delivering different messages with the same identifiers to different processes. This requires the reliable broadcast algorithm of Section 2.2.
- 3. Message validation: message receptions are enhanced with message validations, i.e., when a message is received it is only considered if it is valid as defined in Section 3.1. The objective is to force the adversary to conform to the algorithm.
- 4. Reception quorum: receptions of messages from quorums of n f processes are substituted by: reception of messages from at least n f processes plus the FD suspicion of all other processes (line 9 in Algorithm 2). This requires an eventually perfect muteness FD,  $\Diamond \mathcal{MP}_{\mathcal{A}}$ .

The process of applying the methodology is straightforward as shown in the next section.

## 3.3 Ben-Or's Algorithm

The objective of this section is to show how to apply the methodology, now that it was introduced. This section presents a transformation of Ben-Or's asynchronous crashtolerant binary randomized consensus algorithm  $[2]^5$  into an asynchronous Byzantine binary randomized consensus algorithm, BO\_2FBC.

The application of the methodology consisted of picking the original algorithm and modifying it following the list above. Then, we simply proved that the resulting algorithm satisfies the properties of Byzantine consensus.

The result can be found in Algorithm 3. Notice that Ben-Or's consensus is a binary consensus, i.e.,  $\mathcal{V} = \{0, 1\}$ . Notice also that the consensus is randomized so there is a random

 $<sup>^5 \</sup>mathrm{Ben-Or's}$  paper also presents a Byzantine consensus algorithm, but we are interested only in the crash consensus algorithm.

action (line 13). The definition provided for multi-valued consensus in Section 3 is still valid, except for the termination that becomes probabilistic with probability 1.

The BO\_2FBC algorithm is straightforward and uses a notation similar to the previous one (although we retained some of Ben-Or's notation also), so we skip a detailed textual description of how it works. The original algorithm was randomized so it had no failure detectors, but BO\_2FBC uses  $\Diamond \mathcal{MP}_{\mathcal{A}}$  due to the methodology of transformation (lines 4) and 10). A proof of correctness of the algorithm is provided in the appendix.

#### Discussion 3.4

Although we present two transformations, we do not claim that the methodology can be applied successfully to any asynchronous crash-tolerant consensus algorithm. However, the two algorithms use two common communication patterns, something that suggests that the methodology can be used in many cases. The pattern of MR\_Consensus is based on a rotating coordinator that tries to impose a decision in the first phase, which is vouched or not in the second phase. The pattern of Ben-Or's algorithm has essentially two phases: in the first all processes exchange estimates, then pick one and try to reach agreement in the second phase. Algorithms like Chandra and Toueg's [4], Hurfin and Raynal's [19] or Schiper's [26] use the first pattern, while algorithms like Dwork et al.'s [13] and Pedone et al.'s [25] use the second, so the methodology seems to be usable with all of them.

### 4. 2F + 1 ATOMIC BROADCAST

The previous section shows that it is possible to solve asynchronous Byzantine consensus problems with 2f+1 processes, using a reliable broadcast algorithm that needs 2f+1(or less) processes and an eventually perfect muteness FD  $(\Diamond \mathcal{MP}_A)$ . The flavor of multi-valued consensus solved in Section 3.1 is often used to show that a certain combination of mechanisms can be used to solve consensus [12, 10, 1], but it is particularly weak and not very useful to solve other distributed computing problems. This section introduces a novel flavor of consensus that can be solved with 2f + 1processes, and shows how it can be used to solve atomic broadcast. Atomic broadcast is a problem with practical interest, e.g., because it is the core of state machine replication, a generic solution to implement fault-tolerant services [27].

The Validity property MVC1 states that the value that is decided is one of the values proposed (Section 3). However, it does not say if that process is correct. Suppose we want to solve some problem that involves solving several multivalued consensuses: it is perfectly possible that all values decided in those consensus are proposed by faulty processes, turning them useless. The solution to this difficulty is to use another flavor of consensus with a different validity property (the other properties, MVC2/MVC3 remain the same). There are two definitions that are much used, but that are problematic with only 2f + 1 processes:

- Validity' [13, 22, 20]: If all correct processes propose the same value v, then any correct process that decides, decides v.
- Vector validity [12]: Every correct process that decides, decides on a vector V of size n such that: for

all processes  $p_i$ , if  $p_i$  is correct, then either V/i is the value proposed by  $p_i$  or  $\perp$ ; and at least (f+1) elements of V were proposed by correct processes.

The problem of consensus with Validity' is that a process can never know for sure if it received messages from all correct processes, so this flavor is not implementable with 2f+1processes. The problem of consensus with Vector validity is that with 2f + 1 processes it ensures only that the vector decided contains f + 1 values, the majority of which can be proposed by faulty processes (f).

The three flavors of consensus mentioned so far seem to be problematic with 2f + 1 processes, so we introduce a new form of consensus, endorsement consensus, and present an algorithm that solves the problem using only 2f + 1 processes. The idea behind endorsement consensus is to consider that a correct process can have a notion about which values are adequate decisions for the consensus. More formally, each process  $p_i$  has a set  $E_i$  of values that it *endorses*, i.e., that it considers to be adequate decisions for the consensus<sup>6</sup>. The problem is defined in terms of MVC2, MVC3 and the following property:

• EC1 Validity. If a correct process decides v, then vwas endorsed by some correct process.

The problem *assumes* that the endorsement sets satisfy the following properties:

- Initial endorsement. For any correct process  $p_i$ ,  $E_i$ contains always at least the value proposed by  $p_i(v_{0_i})$ .
- Increasing endorsement. For any correct process  $p_i$ , for any two instants of time during the execution of the algorithm  $t_1, t_2$ , if  $t_2 > t_1$  then  $E_{i_2} \supseteq E_{i_1}$ , where  $E_{i_1}$  and  $E_{i_2}$  are the values of  $E_i$  at the two instants.
- Eventual endorsement. For any pair of correct processes  $p_i$  and  $p_j$ , eventually  $v_{0_i} \in E_j$ .

This last property means that all proposals of correct processes are eventually endorsed by all correct processes. Notice that this is not something that is guaranteed by an algorithm that solves the problem, but something that has to be satisfied for the algorithm to solve the problem, i.e., an assumption. This is precisely what happens with the atomic broadcast algorithm that we see next.

An algorithm that solves this flavor of consensus is Algorithm 2 with a single modification, substituting line 7 by:

7

7: if (valid PHASE1
$$(r_i, v)$$
 received from  $p_{c_i}$  and  $v \in E_i$ )  
then  $aux_i \leftarrow v$  else  $aux_i \leftarrow \bot$  end if

We call this algorithm MR\_2FBEC. The idea is that correct processes  $p_i$  only disseminate a message PHASE2 if the estimate of the coordinator (v) is in  $E_i$ , besides the message being valid as already in Algorithm 2. A proof of correctness of the algorithm is provided in the appendix.

Byzantine atomic broadcast can be defined similarly to reliable broadcast (properties RB1-3 above) plus an additional order property:

<sup>&</sup>lt;sup>6</sup>The problem is related to the Byzantine generals with alternative plans problem, in which processes have sets of good values and bad values [7].

**Algorithm 3** BO<sub>2</sub>FBC Byzantine consensus algorithm (code for process  $p_i$ )

**Function** BO\_2FBC\_CONSENSUS $(v_i)$ 

1:  $est_i \leftarrow v_i$  {current estimate of the value to be decided} 2: step 0:  $r_i \leftarrow 1 \quad \{\text{round number}\}$ 3: step 1: RELIABLE\_BROADCAST PHASE1 $(r_i, est_i)$ 4: step 2: wait until (valid message PHASE1( $r_i$ , -) are received from at least n - f processes) and ( $\forall j : valid$  message PHASE1( $r_i$ , -) is received from  $p_j$  or  $p_j$  is suspected by  $p_i$ 's FD module) 5: if (more than n/2 messages have the same value v) then 6: RELIABLE\_BROADCAST PHASE2 $(r_i, v, decision)$ 7: else 8: RELIABLE BROADCAST PHASE  $2(r_i, \perp)$ 9: end if 10: step 3: wait until (valid messages PHASE2( $r_i$ , -) are received from at least n - f processes) and ( $\forall j : valid$  message PHASE2( $r_i$ , -) is received from  $p_j$  or  $p_j$  is suspected by  $p_i$ 's FD module) 11: if (there is one decision message PHASE2 $(r_i, v, decision)$ ) then  $est_i \leftarrow v$ else if (there are n - f decision messages PHASE2 $(r_i, v, decision)$ ) then DECIDE(v)

- 12. else if (there are n j accision messages PHASE2 $(r_i, v, aecision)$ ) then been 13: else  $est_i \leftarrow 1$  or 0 each with probability 1/2
- 14: step 4:  $r_i \leftarrow r_i + 1$ ; go to step 1
  - AB4 Total order: If two correct processes deliver two messages  $M_1$  and  $M_2$  then both processes deliver the two messages in the same order.

This problem has been shown to be equivalent to consensus in several system models [18, 9]. A transformation from consensus into Byzantine atomic broadcast with only 2f + 1 processes, which we designate by HT\_2FBAB, is provided by a combination of:

- 1. the transformation of consensus and reliable broadcast into atomic broadcast presented in [18];
- 2. algorithm MR\_2FBEC, which substitutes the consensus used in the transformation;
- 3. in every process  $p_i$ , the set  $E_i \equiv R_{-}$  delivered.

The transformation provided in [18] (Section 7.2.2) is for crash faults. The idea is the following. When the algorithm is requested to do atomic broadcast of a message, it does reliable broadcast of that message. When a process receives such a message, it inserts it in the  $R_{-}$  delivered set. When there are messages in that set that have still not been ordered, each process proposes the set of those messages to a consensus. Consensuses are done in an ordered fashion and messages within a consensus can be trivially ordered (e.g., in lexicographical order), so this provides a total order of messages.

In Hadzilacos and Toueg's transformation the consensus always decides a value proposed by a process that is not Byzantine, because there are no malicious processes in the crash system model. In our case we have to deal with that case, which is where the endorsement consensus comes in: it only lets values endorsed by correct processes to be decided by the consensus, thus ordered by the atomic broadcast algorithm. More precisely, given a set  $S_i$  of messages pending to be ordered, proposed by some process  $p_i$ , this set is only decided if at least once correct process endorses this set, i.e., if it receives these messages from the reliable broadcast algorithm (remember that  $E_i \equiv R_delivered$ ). We skip the proof of correctness of HT\_2FBAB.

### 5. FINAL REMARKS

The paper shows that it is possible to implement 2f + 1 asynchronous Byzantine consensus algorithms using a reliable broadcast algorithm (that requires trusted/trustworthy)

components to be implemented), and an eventually perfect muteness failure detector  $\Diamond \mathcal{MP}_{\mathcal{A}}$ . The paper also shows that it is possible to transform 2f + 1 crash consensus algorithms, both based on failure detectors and randomized, into 2f + 1 Byzantine consensus algorithms by applying a set of mechanisms to constrain the power of faulty processes. The paper bridges the gap between previous state machine replication systems that require only 2f + 1 replicas and consensus, a distributed computing problem of known theoretical and practical importance.

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# APPENDIX

# A. CORRECTNESS PROOFS

## A.1 Reliable broadcast algorithm

THEOREM 1. Algorithm 1 solves the reliable broadcast problem as defined by properties RB1, RB2 and RB3.

**Proof** (sketch): RB1 Validity. If a correct process  $p_i$  broadcasts (id, msg) then it sends a message INITIAL $(i, id, msg)_{\sigma}$ with a correct signature  $\sigma$  (line 2) that is received by all correct processes due to the properties of the authenticated reliable channels (line 4), and those processes deliver the message (line 6).

*RB2 Agreement.* If a correct process  $p_j$  delivers a message (id, msg) (line 6) then it first sends ECHO $(i, id, msg, \sigma)$  to all processes (line 5). Therefore, all correct processes eventually receive this ECHO message (line 4) and deliver (id, msg) (line 6).

*RB3 Integrity.* The definition of the wormhole service and an inspection of the algorithm show that the property is always satisfied.  $\Box$ 

Notice that the proofs do not depend on quorums (subsets) of processes of certain sizes, so the algorithm tolerates any number of faulty processes.

# A.2 MR\_2FBC algorithm

LEMMA 1. If a correct process decides v in round r, then no correct process decides  $v' \neq v$  in a round  $r' \geq r$ .

Proof (sketch): A correct process can only decide in lines 11 or 15.

Decision in line 11: A correct process p decides v in round r in line 11 iff it receives n - f valid messages PHASE2(r, v) (lines 9-11). Any other correct process p' falls in one of two cases: (1) it also receives n - f of those messages, therefore it also decides v in round r; (2) it receives less that n - f of those messages.

In the second case, the fact that p receives n-f PHASE2(r, v)messages implies that p' receives at least n-2f PHASE2(r, v)messages (the messages are reliable broadcast so there are at most n messages from different processes). The other messages must contain  $(r, \perp)$  to be valid (this is the only value that is consistent with the value disseminated by the coordinator in phase 1). Therefore, p' sets its estimate  $est_i$  to v (line 12).

Now consider round r + 1. There are three cases, corresponding to p' receiving from the coordinator a message: (2.1) PHASE1(r+1, v); (2.2) PHASE1 $(r+1, \bot)$ ; or (2.3) PHASE1(r+1, v'), with  $v' \neq v$ . In case (2.1), the process p' (and all correct processes) would broadcast a message PHASE2(r + 1, v) in line 5, we would fall again in cases (1) or (2), and messages with different values would never become valid.

Cases (2.2) and (2.3) can never happen: for p' to consider that message valid it would have to receive n - f messages PHASE2 $(r, \perp)$ , something that can not happen because there are n - f messages PHASE2(r, v) and there can be no more than n messages PHASE2(r, \*) (where \* can be v or  $\perp$ ) due to the properties of the reliable broadcast primitive.

Decision in line 15: A correct process p decides in line 15 if it receives a valid DECISION(r, est), thus the protocol function F requires it to have received n - f PHASE2(r, v) messages. If that is the case, all correct processes received at least n - 2f of those messages and we fall in the case of line 11 above.  $\Box$ 

### LEMMA 2. Every correct process eventually decides.

*Proof (sketch):* First we have to prove that the algorithm does not block indefinitely at some line. The only lines where a process blocks are those where it waits for messages, i.e., lines 6 and 9. The properties of the failure detector guarantee that the algorithm does not block at those lines.

Now let us prove that one correct process eventually decides. The eventual strong  $\mathcal{A}$ -accuracy property of the failure detector ensures that eventually there will be a round r in which no correct process is suspected. In that case, all correct processes receive messages from all other correct processes in line 9 and decide in line 10.

In this latter situation all processes decide in the same round but that is not mandatory. For instance, if FD modules in some correct processes suspect some of the other processes, then it is possible that one of the correct processes p decides in a round r, but not the others. In that case, no correct process decides a different value (Lemma 1). Furthermore, every other correct process p' decides the same value when it eventually receives the DECIDE message sent by p (lines 11 and 14-16). Notice that this message must be valid as it is valid iff process p' receives n - f valid PHASE2(r, v) messages, which it must have received since these are the messages that made p to decide (lines 9-11) and the reliable broadcast ensures that all correct processes receive the same PHASE2 messages (property RB2 Agreement).

THEOREM 2. Algorithm 2 solves the Byzantine consensus problem as defined by properties MVC1, MVC2 and MVC3.

*Proof (sketch):* Property MVC1 Validity comes from inspection of the algorithm. MVC2 Agreement is an immediate consequence of Lemma 1. Property MVC3 Termination is given by Lemma 2. □

# A.3 BO\_2FBC algorithm

LEMMA 3. If a correct process decides v in round r then no correct process decides  $v' \neq v$  in round  $r' \geq r$ .

*Proof (sketch):* A correct process p decides value v in round r in line 12 if and only if it receives n - f valid decision

messages PHASE2 $(r_i, v, decision)$ . Any other correct process p' falls in one of two cases: (1) it also receives n - f decision messages, therefore it also decides v in round r; (2) it receives less that n - f of those messages.

In the second case, the fact that process p receives n - f PHASE2 $(r_i, v, decision)$  messages implies that p' receives at least n - 2f PHASE2 $(r_i, v, decision)$  messages (the messages are reliable broadcast so there are at most n messages from different processes). Therefore, p' sets its estimate to v (line 11). Now consider round r+1. There are two cases (lines 5-9): (2.1) p' receives more than n/2 messages with the same value v; (2.2) the contrary.

Case 2.2 can never happen for the following reason. For that to be possible p' would have to receive and consider valid at least one message with PHASE1(r+1, v'), with  $v' \neq v$ . A faulty process can send such message but the validation mechanism at p' does not consider it valid because it contradicts the existence of n-f messages PHASE2 $(r_i, v, decision)$ .

This leaves us with case 2.1, i.e., any correct process falls in that case and executes line 6. Therefore, any correct process either falls in cases 1 or 2 above. Therefore, no correct process ever decides a value  $v' \neq v$  in round  $r' \geq r$ .  $\Box$ 

LEMMA 4. Every correct process eventually decides.

*Proof (sketch):* An inspection of the algorithm shows that it never blocks in any line, so we have only to prove that it does progress and eventually terminates. The eventual strong  $\mathcal{A}$ accuracy property of the failure detector states that there is a time after which correct processes are not suspected by any correct process. Let us consider that that time passed, so no correct processes suspect of correct processes. This has the practical implication of all correct processes receiving all messages from each other in lines 4 and 10. If not before, eventually there is a round r in which all correct processes set est to the same value v either in line 13 or in lines 11 and 13. When that happens, in round r+1 all correct processes broadcast v in line 3, all receive at least n - f PHASE1 messages with that value (since there are at least that number of correct processes), all broadcast PHASE2(r+1, v, decision)messages, all receive each other PHASE2 messages in line 10, and all decide in line 12. 

THEOREM 3. Algorithm 3 solves the Byzantine consensus problem as defined by properties MVC1, MVC2 and MVC3.

Proof (sketch): Property MVC1 (Validity) comes from inspection of the algorithm (recall that  $\mathcal{V} = \{0, 1\}$ ). Property MVC2 (Agreement) is a consequence of Lemma 3. Property MVC3 (Termination) comes from Lemma 4.

# A.4 MR\_2FBEC algorithm

THEOREM 4. Algorithm  $MR_2FBEC$  solves the Byzantine endorsement consensus problem as defined by properties EC1, MVC2 and MVC3.

*Proof (sketch):* Property EC1 Validity is intuitive from inspection of the algorithm: one correct process must endorse the value that is decided (line 7) or it would never be decided. MVC2 Agreement is an immediate consequence of Lemma 1, which also applies to this algorithm. Property MVC3 Termination is given by Lemma 2, taking into account that the eventual endorsement property ensures that eventually the predicate  $v \in E_i$  in line 7 becomes forever true.