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**Modelling of the anaerobic semi-continuous co-digestion of
sewage sludge and wine distillery wastewater**

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Water Impact Statement

The proposed process can be worldwide used as an eco-friendly way of wine-making wastewater valorization.

The kinetic study of this process is necessary for a correct design of any WWTPs aimed to incorporate other residues for improving energy generation.

The incorporation of agro-industrial wastewater as WDW to any WWTPs overcome the limitation problems derived from the first stages in AD.

1 **Modelling of the anaerobic semi-continuous co-digestion of sewage sludge and**
2 **wine distillery wastewater.**

3

4 Vanessa Ripoll^{a, b}

5 Cristina Agabo^a

6 Rosario Solera^a

7 Montserrat Perez^{a, *}

8 ***Author to whom correspondence will be addressed**

9

10 **Affiliation**

11 ^a Department of Environmental Technologies, University of Cadiz, Campus de Puerto
12 Real, 11500 Puerto Real, Cadiz, Spain.

13 ^b Current affiliation: Facultad de Ciencias Experimentales, Universidad Francisco de
14 Vitoria (UFV), Ctra. Pozuelo-Majadahonda km 1.800, 28223 Pozuelo de Alarcón,
15 Madrid, Spain

16

17 **E-mail addresses**

18 vanessa.ripoll@ufv.es (V. Ripoll)

19 cristina.agabo@uca.es (C. Agabo)

20 rosario.solera@uca.es (R. Solera)

21 montserrat.perez@uca.es (M. Perez)

22

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24 ABSTRACT

25 The semi-continuous mesophilic anaerobic co-digestion of sewage sludge and wine
26 distillery wastewater was investigated. In this sense, the effects of reducing hydraulic
27 retention time (HRT, from 20 d to 8 d) on the degradation of organic matter and
28 methane production were determined. The experimental results showed that anaerobic
29 co-digestion enhanced the biodegradability of the mixture in terms of VS and CODt (7-
30 8% higher) for HRT = 8 d. The methane productivity at HRT = 8 d ($18.0 \text{ L}_{\text{CH}_4}/\text{kg}_{\text{VS}}\cdot\text{d}$),
31 was also enhanced (30% higher) than those obtained in the control experiment. In
32 addition, a mathematical kinetic model was proposed to determine the rate-limiting step
33 of the process. Stoichiometric parameters obtained for SS:WDW ($0.115 \text{ kg}_{\text{CH}_4}/\text{kg}_{\text{COD}}$)
34 was higher than SS ($0.094 \text{ kg}_{\text{CH}_4}/\text{kg}_{\text{COD}}$), which means that co-digestion increased the
35 rate of consumption because more amount of biodegradable compounds. Kinetic study
36 showed that anaerobic co-digestion favoured methane production rate enhancing the
37 acetate consumption step and making methanogenesis the rate-limiting step in this
38 process.

39 **Keywords:** *anaerobic co-digestion; wine distillery wastewater; sewage sludge; organic*
40 *loading rate (OLR); kinetic modelling.*

41

42 1 Introduction

43 The cost of sewage sludge management in urban wastewater treatments plants (WWTP)
44 is over 50% of the overall operating costs taking into account the land value, the
45 transportation, landfilling operation and leachate treatment, and maintenance for a
46 correct pollution control¹. Therefore, anaerobic digestion (AD) has been widely
47 implemented as an effective technology at an industrial scale in WWTP². AD is a

48 renewable energy technology in which microorganisms break down biodegradable
49 material in an oxygen-free environment to produce a solid digestate along with biogas.
50 Biogas production has social advantages, such as the economical production of
51 electricity or heat. In addition, AD process achieves the reduction and stabilization of
52 rotting organic matter and partial inactivation of pathogenic agents³⁻⁵. However, sewage
53 sludge (SS) organic load values undergo high variations and are often not sufficient for
54 an economically effective operation¹. Given that many of the anaerobic digesters
55 installed in WWTP are oversized, the scientific community is paying close attention to
56 simultaneous anaerobic co-digestion (ACoD) of SS and other types of waste aimed to
57 promote the biodegradability of the feedstock and hence to enhance biogas production⁶⁻
58 ⁷. The main advantages of ACoD include: shared treatment facilities, reduced
59 investment and operating costs, buffering of the variations in the composition of the
60 waste over time and the diluting of toxic compounds and cytotoxic inhibitors. Several
61 published studies have already focused on the employment of agro-industrial wastes,
62 which contain easily degradable substrates⁸⁻¹¹. Among different residues, wine distillery
63 wastewater (WDW) is one of the main types of waste generated in the viticulture
64 industry and its disposal constitutes an environmental concern. In addition, the disposal
65 costs. This waste has a strongly acidic pH and contains a high organic pollutant load
66 (around 40 gCOD/L) including various phenolic compounds such as gallic acid, p-
67 coumaric acid and gentisic acid¹². In this sense, the AD of sole WDW at semi-continuous
68 mode has been previously studied (including kinetic evaluation) as a successful
69 biological treatment for producing biomethane: in fixed-film reactors¹³; thermophilic
70 high rate reactors ¹⁴ and after different pre-treatments¹⁵. However, semi-continuous
71 ACoD of SS:WDW only has been previously studied to produce biohydrogen at
72 thermophilic conditions in continuous stirred tank reactor technology (CSTR)¹⁶. In

73 addition, the ACoD of SS:WDW has been previously studied at batch mode without any
74 pretreatment¹⁷. So, in the present work it was studied its biomethane potential as co-
75 substrate for continuous biomethane production in CSTR technology and the kinetic
76 parameters, complementing the recently research published about ACoD of SS:WDW at
77 batch mode. This information will be useful for determining operational conditions in
78 scaling-up process in regions with high volume of WDW production in order to use
79 them in WWTP in wine-producing areas¹⁷.

80

81 In this sense, process modelling is a useful tool for describing and predicting the
82 performance of anaerobic digestion systems. Monod type kinetic models have been
83 widely used to describe the process kinetics of anaerobic digesters¹⁸. Although there has
84 been some success in applying Monod type kinetics to the anaerobic process, some
85 research workers found it difficult to apply them for their systems¹⁹⁻²⁰. In the equation
86 proposed by Contois (1959)²¹, the specific growth rate was considered as a function of
87 the growth-limiting nutrient in both input and effluent substrate concentration by using
88 an empirical constant, which was related to microbial concentration. On this basis, Chen
89 and Hashimoto (1980)²² developed kinetic models for substrate utilisation and methane
90 production and suggested that the Contois type kinetic models would be more suitable
91 than the Monod type kinetic models to predict digester performance. Both consider that
92 the AD takes place throughout a single stage of biological reaction that combines a
93 complex biological reaction network. In this paper, a novel kinetic model is proposed
94 based on the methane production results to describe the step rates involved in the
95 anaerobic process. An unstructured non-segregated kinetic model is proposed to
96 describe the anaerobic digestion considering two steps: the hydrolysis of the particulate
97 substrate (COD_P) to obtain accessible or soluble substrate (COD_S) for the

98 microorganisms and the consumption of this accessible substrate to produce methane.
99 Moreover, there is not much published information available for the process kinetics of
100 anaerobic co-digestion treating sewage sludge and wine distillery wastewater.

101

102 The aim of this paper was focused, therefore, on the experimental and kinetic
103 description of the anaerobic semi-continuous co-digestion of SS and WDW within the
104 mesophilic temperature range, studying the influence of the organic loading rate (OLR)
105 on the overall process: the efficiency of organic matter removal, biogas production and
106 kinetic analysis. In order to achieve this goal, several hydraulic retention times (HRT)
107 were employed ranging from 20 to 8 d, corresponding to different OLR ranges (2.26 –
108 5.38 kgCOD/m³·d). An anaerobic digestion trial using only sewage sludge as feedstock
109 was also carried out as a control experiment to determine whether adding WDW to the
110 WWTP anaerobic digester enhances the degradation of organic matter and/or methane
111 production. The semi-continuous control experiment was carried out under the same
112 HRT conditions (from 20 to 8 d), involving an OLR range from 3.43 to 6.99
113 kgCOD/m³·d. Finally, a comparison of different kinetic parameters obtained after
114 modelling was made to determine the rate-limiting step in each case.

115

116 **2 Materials and methods**

117 The experimental protocol was designed to study the influence of increasing OLR on
118 the efficiency of an anaerobic digestion treatment within the mesophilic temperature
119 range employing a 1:1 (v/v) ratio of SS:WDW, as well as SS alone (as a control
120 experiment).

121

122 The methods and materials used are briefly described in this section. Each trial was
123 carried out in duplicate and all the reported results correspond to the average values of
124 the last data obtained.

125 **2.1 Feedstock and inoculum**

126 The substrates used in the experimental stage were collected directly from two real
127 industrial facilities. SS corresponds to the activated sludge from the secondary treatment
128 employed at Guadalete municipal WWTP (located in Cadiz, Spain). WDW was
129 obtained from Gonzalez-Byass, an ethanol producing wine-distillery plant located in
130 Jerez de la Frontera (Cadiz, Spain). All the samples were characterized on reception at
131 the laboratory and were stored at 4 °C for a maximum of one month before being used
132 in the experiments in order to prevent their degradation.

133

134 The experimental work was carried out over a period of 6 months. During the
135 experiments, waste samples had to be collected several times. Parameters related to
136 organic material content, such as total solids (TS), volatile solids (VS) and chemical
137 oxygen demand (COD), were determined.

138

139 The inoculum was obtained from a 5-L laboratory scale anaerobic digester operating
140 under stable conditions at 20 d HRT within the mesophilic temperature range (35 °C).
141 available in the Research Group and fed with SS coming from secondary decanter of
142 WWTP from Jerez (Cádiz-Spain). The characteristics of the inoculum are shown in
143 Table 1.

144

Table 1. Characteristics of inoculum

Parameters	Inoculum
pH	7.60 ± 0.02
CODt (kg/m ³)	20.1 ± 0.5
CODs (kg/m ³)	10.1 ± 0.4
TS (g/L)	32.0 ± 2.5
VS (g/L)	23.4 ± 2.0

145

146 **2.2** *Experimental equipment*

147 A 3-L semi-continuous stirred tank reactor with a working volume of 2-L was used
148 (MiniReactor, Trallero and Schee®) in this study. The digester was sealed with a lid
149 provided with several openings for different purposes (biogas output, pH probe,
150 temperature probe, stirring system). The stirring speed was set at 20 rpm. The
151 temperature was maintained within the mesophilic range (35 ± 1 °C) by means of an
152 electric heater. The produced biogas was collected in 5-L Tedlar® bags, employing a
153 special syringe to sample the gases.

154

155 **2.3** *Operating conditions*

156 In the present study, the influence of the OLR on the anaerobic co-digestion of a 1:1
157 (v/v) mixture of SS and WDW was analysed in semi-continuous operating mode within
158 the mesophilic temperature range (35 °C). These results were compared with the
159 behaviour of an anaerobic digester using only SS working under similar operating
160 conditions (OLR and temperature range). Initially, both digesters were loaded with a
161 mixture of inoculum and substrate at a ratio of 1:2.5 (v/v), which is considered optimal
162 for biogas production^{17, 23}. The start-up of the reactors took place at 20 d HRT. The

163 subsequent series of HRT were set at 15, 10 and 8 days, which involved progressive
 164 increases in feed flow rates (from 0.10 to 0.15, 0.2 and 0.25 L/d, respectively). These
 165 operating conditions were selected on the basis of the previous experience of our
 166 research group ^{8,10} and ²⁴⁻²⁵. At least 3 trials employing the corresponding HRT (20, 15,
 167 10 and 8 d, respectively) were conducted under each operating condition in order to
 168 ensure the steady state. The reactors were fed once a day with SS:WDW (1:1 (v/v)) and
 169 SS without the addition of nutrients in order to establish the semi-continuous process.
 170 Each HRT was maintained at least 3 times to ensure that steady-state conditions were
 171 reached. The composition of the industrial wastes employed varied during the
 172 experimental period. Therefore, the OLR was determined for each condition in terms of
 173 feed VS (OLR_{VS}) and feed COD (OLR_{COD}). The main characteristics of the feedstocks
 174 are shown in Table 2 (a, b).

Table 2. Main characteristic of the feedstock (a) 1:1 SS:WDW and (b) SS.

(a)

HRT (d)	TS (kg_{TS}/m^3)	VS (kg_{VS}/m^3)	COD _t (kg_{COD}/m^3)	COD _s (kg_{COD}/m^3)	OLR ($kg_{VS}/m^3 \cdot d$)	OLR ($kg_{COD}/m^3 \cdot d$)
20	30.6 ± 1.6	23.4 ± 0.8	45.2 ± 2.4	24.9 ± 1.7	1.17 ± 0.04	2.26 ± 0.12
15	31.7 ± 1.9	25.3 ± 1.1	43.0 ± 1.9	22.4 ± 1.3	1.90 ± 0.08	3.23 ± 0.14
10	31.8 ± 0.3	24.7 ± 0.4	41.9 ± 1.9	20.6 ± 2.2	2.47 ± 0.04	4.19 ± 0.19
8	34.7 ± 0.3	25.6 ± 0.4	43.0 ± 1.9	22.4 ± 1.3	3.20 ± 0.05	5.38 ± 0.24

175

(b)

HRT (d)	TS (kg_{TS}/m^3)	VS (kg_{VS}/m^3)	COD _t (kg_{COD}/m^3)	COD _s (kg_{COD}/m^3)	OLR ($kg_{VS}/m^3 \cdot d$)	OLR ($kg_{COD}/m^3 \cdot d$)
20	52.8 ± 2.0	43.2 ± 1.7	68.5 ± 3.3	15.9 ± 3.2	2.16 ± 0.09	3.43 ± 0.17
15	52.4 ± 0.4	42.6 ± 0.3	68.5 ± 2.0	10.4 ± 2.5	3.20 ± 0.02	4.57 ± 0.15
10	54.8 ± 0.3	42.9 ± 0.2	65.8 ± 3.3	9.9 ± 1.6	4.29 ± 0.02	6.58 ± 0.33

8 44.4 ± 0.5 37.8 ± 1.2 65.9 ± 0.8 10.4 ± 1.1 4.66 ± 0.15 6.99 ± 0.10

176

177 **2.4 *Analytical methods***

178 Analytical characterization of the feedstock and the digestate were carried out twice a
179 week during the experimental stage. The main parameters (total solids (TS), volatile
180 solids (VS) and chemical oxygen demand (COD)) were determined in accordance with
181 the Standard Methods²⁶. In order to better understand the system behaviour, the total
182 and soluble COD (COD_T and COD_s, respectively) of both the feedstock and effluent
183 were determined. Volatile fatty acids (VFA) (acetic, propionic, iso-butyric, butyric, iso-
184 valeric, valeric, iso-caproic, caproic and heptanoic acids) were determined on a gas
185 chromatograph (GC-2010 Plus Shimadzu) employing a Nukol® capillary column and a
186 FID detector. Total acidity was calculated by the addition of the individual fatty acids in
187 terms of acetic acid concentration equivalent. Gas composition was determined
188 employing a gas chromatographic technique (GC-2010 Shimadzu). The analysed gases
189 (H₂, CH₄, CO₂, O₂ and N₂) were measured by means of a thermal conductivity detector
190 (TCD) at 250 °C using a Supelco Carboxen 1010 PLOT column. The oven temperature
191 was programmed between 35 and 200 °C. Manual injection was carried out using a
192 sample volume of 250 µL. The carrier gas employed was nitrogen at a pressure of 35
193 kPa. The biogas volume was collected daily in Tedlar bags. Volumes were directly
194 determined employing a gas flow meter (Ritter Wet Drum TG 0.1 mbar). The pH was
195 measured using a Crison 20 BASIC pHmeter.

196

197 **2.5 *Process efficiency***

198 Process efficiency was related to the percent removal efficiency obtained by anaerobic
 199 digestion in terms of VS removal and CODt removal. In order to evaluate biogas
 200 production, two parameters related to specific methane production (SMP) (Eq. 1 and 2)
 201 and methane productivity (MP) (Eq. 3 and 4) were defined.

$$203 \quad SMP_{VS} \left(L_{CH_4} / kg_{VS} \right) = \frac{V_{CH_4}}{OLR_{VS}} \quad (1)$$

$$205 \quad SMP_{COD} \left(L_{CH_4} / kg_{COD} \right) = \frac{V_{CH_4}}{OLR_{COD}} \quad (2)$$

$$207 \quad MP_{VS} \left(L_{CH_4} / kg_{VS} \cdot d \right) = \frac{V_{CH_4}}{V_{Digester} \cdot VS_{INLET}} \quad (3)$$

$$209 \quad MP_{COD} \left(L_{CH_4} / kg_{COD} \cdot d \right) = \frac{V_{CH_4}}{V_{Digester} \cdot COD_{INLET}} \quad (4)$$

211 3 Results and discussion

213 3.1 Process stability: pH evolution and VFA

214 The evolution of pH inside the digesters throughout the experiments are shown in
 215 Figure 1-A (i, ii). The optimal pH range for the activity of methanogenic
 216 microorganisms (7.5–8.5) in mesophilic anaerobic digestion is well known²⁷⁻²⁹.

217

218 Thus, the monitoring of the physicochemical parameter provides useful information
219 with respect to the anaerobic digestion steps that are taking place. The pH values
220 remained within the 7.3–8.2 range in both the ACoD digester and the control
221 digester for months. The pH was maintained constant due to two causes: (i) daily
222 adjustment of substrate before feeding in the case of co-digestion (due to low values
223 of pH of WDW) and (ii) the microbial consortia activity. So, the pH was
224 maintained at optimal range and the volatile fatty acids, which are being formed
225 during hydrolytic-acidogenesis pathways, are neutralized avoiding acidification of
226 the reactor and allowing the normal activity of acetogenic and methanogenic
227 bacteria.

228

229 3.2 *Organic matter removal*

230 The organic matter content in the feedstock and effluent was determined by measuring
231 VS and COD_T in both streams. The evolution of these two key parameters during AD at
232 each tested HRT are shown in Figures 1-B (i, ii) and 1-C (i, ii) and the average of these
233 parameters after reaching steady state is showed in Table 2. As it can be seen in Figures
234 1B-C, the start-up of the process (20 d HRT) showed a proper acclimation of the
235 inoculum to the waste. The present study was conducted employing real industrial
236 wastes as feedstock. Thus, the characteristics of the initial feedstock varied over the six
237 months of experimental work. Nevertheless, the organic matter determined in the outlet
238 stream remained stable (Figure 1 B-C) regardless of the changes in feedstock, as it was
239 concluded in other previous studies employing different types of wastes¹⁰. On average,
240 VS and COD_T removal in all the cases was 44.6 and 49.9% for SS and 52.7 and 56.7%
241 for SS:WDW for OLR ≤ 3.2 (kg_{VS}/m³·d).

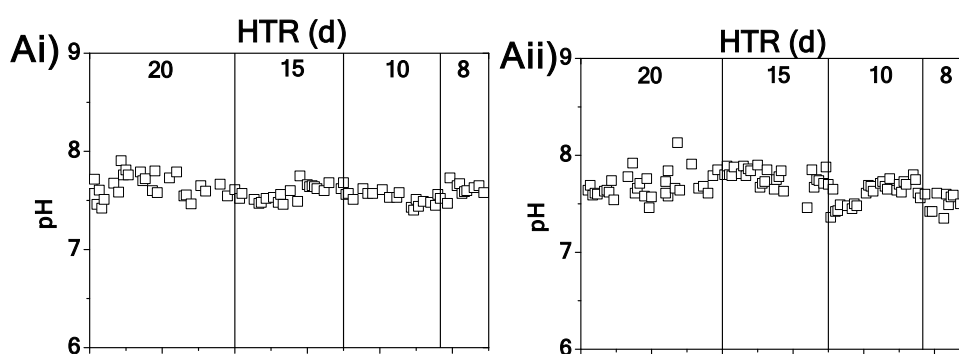
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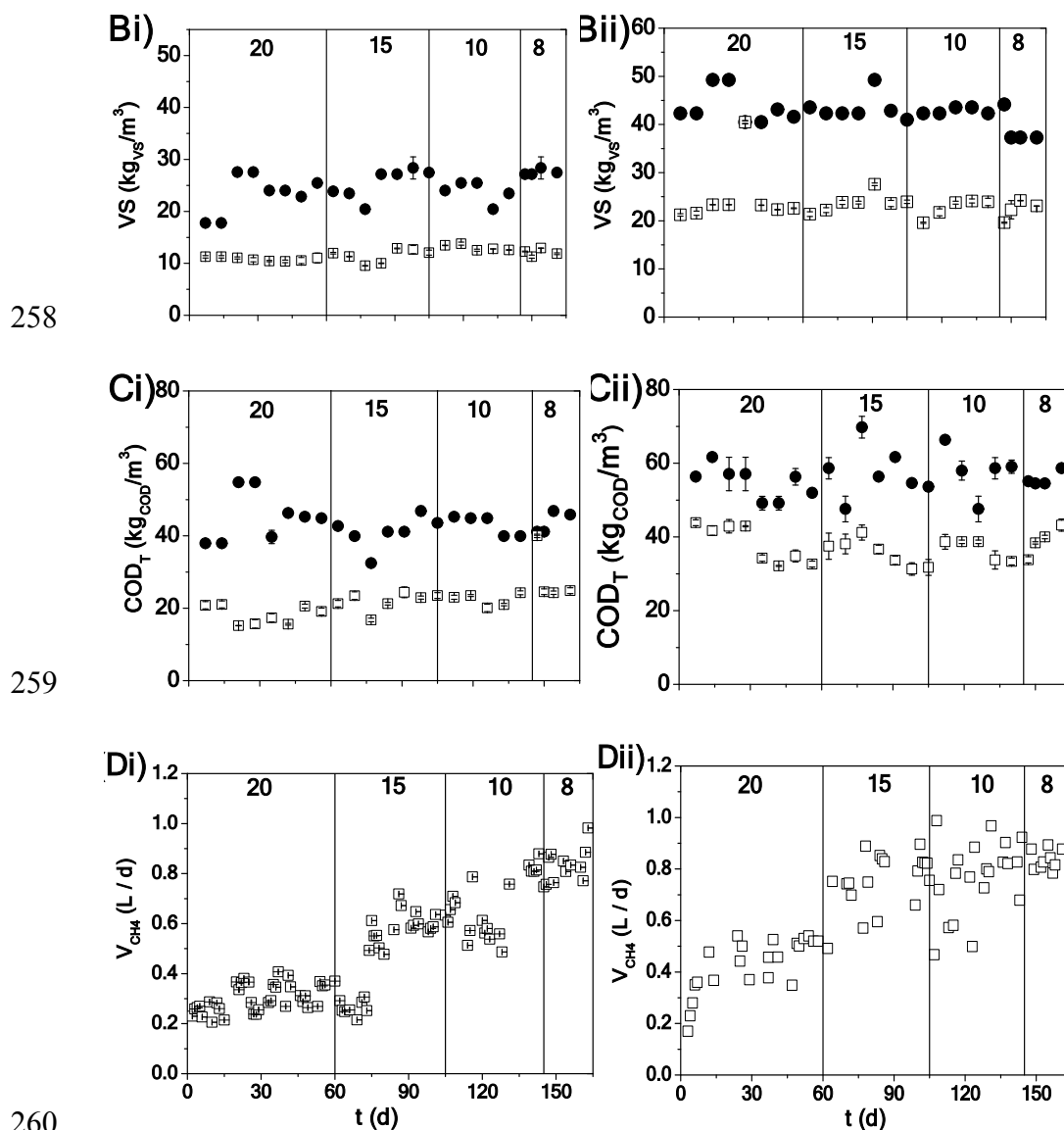
243 Total VFA (mgAc/L) at the steady state is also shown in Table 2. There is a slight
 244 increase between 20 and 8 d HRT of the total VFA concentration, being higher in co-
 245 digestion digesters than in those fed only with SS. Taking into account that initial VFA
 246 were very high (4424 ± 122 mg Ac/L and 6827 ± 135 mg/L Ac/L for WDW:SS and SS,
 247 respectively) the VFAs were used almost fully: between 76-90% and 90-96% for
 248 WDW:SS and SS, respectively. It should be pointed out that this parameter had no
 249 effect on pH, which remained stable during the tests. According to these results, the co-
 250 digestion system has proven to be stable under the operating conditions studied here.

251

252 In Table3, VS/TS ratios are also shown, obtaining on average $61.4\% \pm 2.0$ and $71.2 \pm$
 253 1.3% for SS:WDW and SS, respectively. Regarding energy efficiency (EE) as the
 254 energy cost of recovering usable energy from the sludge, according to Li and Feng
 255 (2018)³⁰ when AD is operating at $VS/TS \geq 60\%$, the system was more than twice
 256 efficient than the

257





261 **Figure 1.** Evolution of (A) pH inside the digesters, (B) VS of the feedstock and the
 262 effluent, (C) COD of the feedstock and the effluent, and (D) daily methane volume in
 263 the semi-continuous anaerobic digesters of (i) SS:WDW (1:1 (v/v)), and (ii) SS. Key
 264 ●feeding □effluent.

system working at VS/TS = 70%. Then, the ACoD system proposed not only will be an eco-friendly way of wine making residue valorization but also an energetically efficient process.

Table 3. Main characteristic of the effluents and daily methane production at the steady

state: (a) 1:1, SS:WDW and (b) SS.

HTR (d)	VS (kg _{VS} / m ³)	VS/TS (%)	COD _t (kg _{COD} / m ³)	COD _s (kg _{COD} / m ³)	VFAs (mg _{ac} /L)	V _{CH₄} (L/d)	X _{CH₄} (%)
20	10.6 ± 0.1	59.9	15.2 ± 0.9	8.5 ± 0.5	418 ± 87	0.47 ± 0.03	68.1 ± 1.6
15	11.3 ± 0.7	60.4	16.8 ± 1.4	8.8 ± 0.9	721 ± 60	0.63 ± 0.03	66.8 ± 1.1
10	12.7 ± 0.1	64.8	20.6 ± 0.1	9.6 ± 0.8	1018 ± 103	0.75 ± 0.06	68.0 ± 1.4
8	12.2 ± 0.5	60.4	22.4 ± 5.2	10.5 ± 2.3	1608 ± 189	0.92 ± 0.01	69.4 ± 1.6

265

266

(a)

HTR (d)	VS (kg _{VS} / m ³)	VS/TS (%)	COD _t (kg _{COD} / m ³)	COD _s (kg _{COD} / m ³)	VFAs (mg _{ac} /L)	V _{CH₄} (L/d)	X _{CH₄} (%)
20	22.7 ± 0.4	70.5	28.9 ± 1.9	17.3 ± 0.9	271 ± 69	0.54 ± 0.03	68.8 ± 2.4
15	23.1 ± 0.4	70.2	31.5 ± 1.8	14.7 ± 0.5	398 ± 90	0.82 ± 0.02	68.3 ± 1.5
10	23.2 ± 0.7	70.5	36.1 ± 1.5	15.0 ± 2.6	446 ± 76	0.89 ± 0.01	68.0 ± 2.9
8	23.3 ± 0.4	73.5	38.2 ± 1.6	14.0 ± 0.5	658 ± 102	0.93 ± 0.01	67.7 ± 1.2

267

268

(b)

269

270

271 3.3 Biogas production

272 Figure 1-D (i, ii) shows the evolution of daily methane production. In response to
 273 changing OLR conditions, an acclimation stage is observed before to reaching the
 274 steady state. The lower the HRT (which means the higher the OLR), the higher the
 275 biogas production. The average methane production under each condition is

276 summarized in Table 2. The maximum value obtained was 0.92 ± 0.2 L/d at 8 d HRT,
277 regardless of substrate used. Table 2 also shows the percentage of methane contained in
278 the biogas (X_{CH_4}), near of 70% in both trials, similar than previous reported by ACoD of
279 these both substrates¹⁷.

280 The influence of OLR on specific methane production (SMP) in terms of VS and COD
281 are shown in Figure 2 (A, B). Increasing OLR lead to a linear increase in SMP,
282 regardless of the waste employed (SS:WDW or SS). However, as it can be seen in
283 Figure 2 (C, D) the influence of OLR on MP shows a different trend. ACoD of
284 SS:WDW significantly enhances MP with respect to AD of SS alone in terms of both
285 VS and COD, because initial SS had more VS and COD than SS:WDW (Table 1) . The
286 explanation of this result lies in the favourable characteristics of WDW (high dissolved
287 organic matter content and biodegradability) improving methane production rate. The
288 reduced effectiveness of the system is also reflected in the higher accumulation on VFA
289 intermediate compounds in the AD (Table 2). Based on these results, employing HRT
290 below 8 d could entail the destabilization of the digester and the breakdown of
291 efficiency. The best methane productivity was obtained when ACoD of SS:WDW was
292 operated at HRT = 8d (OLR = $3.2 \text{ kg}_{VS}/\text{m}^3 \cdot \text{d}$), obtaining $18.0 \text{ L}_{CH_4}/\text{kg}_{VS} \cdot \text{d}$ and 10.7
293 $\text{L}_{CH_4}/\text{kg}_{COD} \cdot \text{d}$, being 30% higher than those observed in the AD of SS alone. Other
294 researchers have obtained similar MP increases on mono-digestion of SS by addition of
295 agri-food residues. Donoso-Bravo et al.,³¹ studied the effect of ACoD of SS with two
296 co-substrates: (i) beverage wastewater and (ii) thermally pretrated biological sludge.
297 Results obtained improved values of MP in 21.4% and 16.2% by using 10% v/v of co-
298 substrates and 90% of SS. Montañés et al.,³² obtained 33.6% higher MP in terms of
299 $\text{m}^3\text{CH}_4/\text{kg COD}_{\text{removal}}$ by using 10% v/v of lixiviation of sugar beep pulp as co-substrate at

300 OLR = 3.55 kg_{VS}/m³·d. Pitk et al.,³³ obtained an increase of 37.7% at OLR ~ 3
 301 kg_{VS}/m³·d using 7.5% of slaughterhouse residues.

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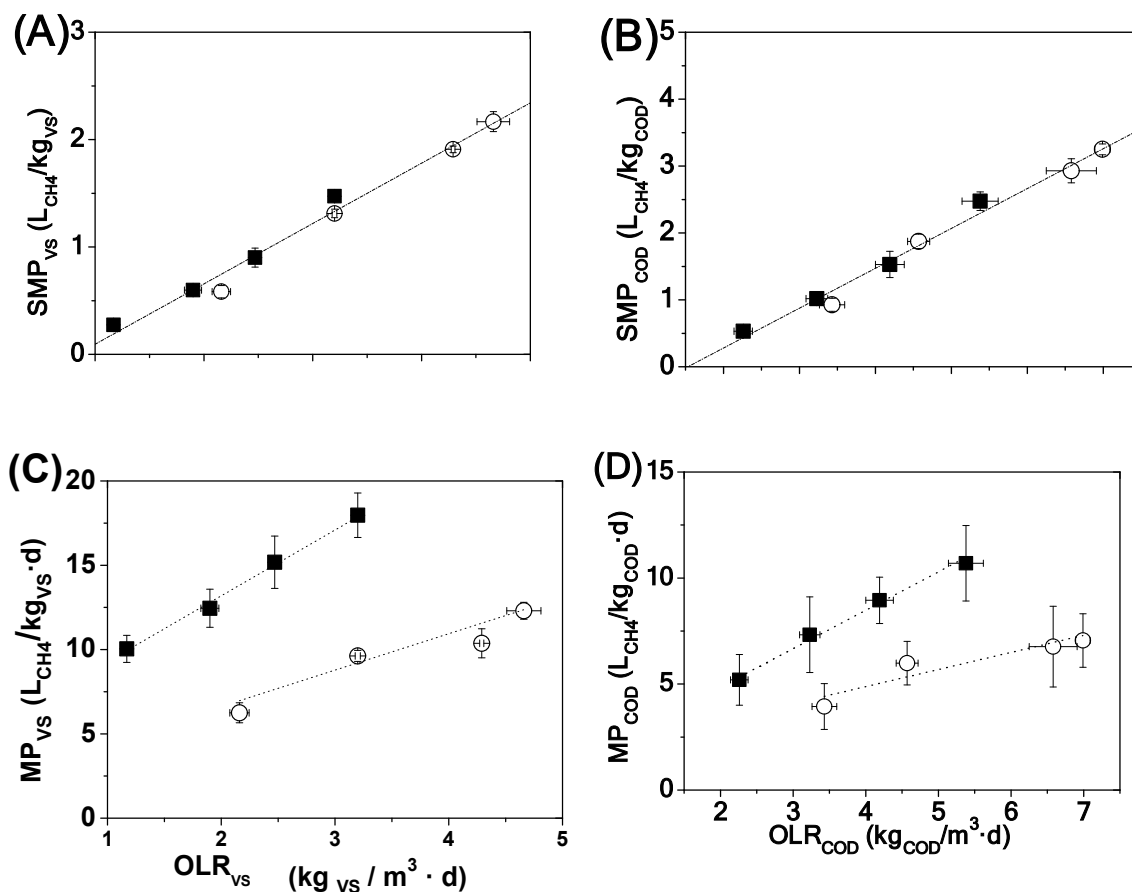


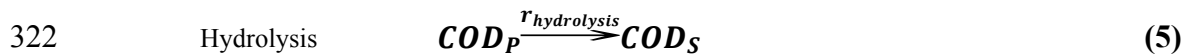
Figure 2 Influence of OLR on (A) SMP in terms of VS, (B) SMP in terms of COD, (C) MP in terms of VS and (D) MP in terms of COD. Key: ■SS:WDW (1:1) ○SS.

303 3.4 Kinetic modelling

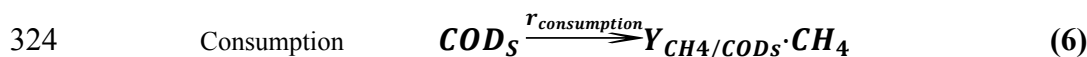
304 A kinetic model is proposed based on the MP results to describe the step rates involved
 305 in both the ACoD of SS:WDW and the AD of SS alone. AD takes places via a complex
 306 biological reaction network. An unstructured non-segregated kinetic model is proposed
 307 here to describe the anaerobic digestion of WDW and SS at the macroscopic scale. The
 308 two reactions considered are: hydrolysis of the solid substrate (COD_p) to obtain

309 accessible substrate (COD_S) for the microorganisms (Eq. 5), and consumption of this
 310 accessible substrate to produce methane (Eq. 6). The Eq. 5 simplify the equations
 311 produced during the hydrolysis because the exo-enzymes activity of microbes. In this
 312 sense, the organic matter particulate (measured as COD_P) is converted to organic matter
 313 soluble (COD_S). On the other hand, the Eq. 6 simplify in a unique reaction the organic
 314 matter consumption reactions that produce biomethane. This reaction schematically
 315 represents all the processes that occur when biodegradable organic matter (which
 316 indirectly is measured by COD_S) is converted to biomethane (CH_4). It is necessary to
 317 establish a relationship between both parameters with the stoichiometric coefficient.
 318 This parameter is analogue to biomethane yield. As it is known, that this complex
 319 process does not occur in a unique step, this yield involves the stoichiometry in
 320 macroscopic terms.

321



323



325

326 The proposed kinetic equations depend on the substrate concentration via a first-order
 327 reaction (Eq. 7 and 8), in line with previously published papers by other authors³⁴⁻³⁶.

328

329 Hydrolysis $r_{hydrolysis} \left(\frac{kg_{COD}}{m^3 \cdot d} \right) = k_{hydrolysis} \cdot COD_P$ (7)

330

331 Consumption $r_{consumption} \left(\frac{kg_{COD}}{m^3 \cdot d} \right) = k_{consumption} \cdot COD_S$ (8)

332

333 Considering the mass balance in the digester and assuming that the digester behaves as
 334 an ideal complete mixed tank bioreactor, the hydrolysis and consumption rates are
 335 related to properties of the feedstock and effluent at the steady state, and the HRT
 336 condition. Therefore, both rates can be calculated using inlet and outlet biodegradability
 337 parameters (Table 2) at the steady state for each HRT condition (Eq. 9 and 10).
 338 According to Eq. 9 $r_{\text{hydrolysis}}$ is calculated by difference of inlet and outlet COD_P referred
 339 to HRT which represent the soluble matter that is formed inside the reactor. However,
 340 in Eq.10 the consumption rate shows the difference between CODs in the reactor
 341 (CODs that enter with feeding plus the CODs that already is inside the reactor as a
 342 consequence of hydrolysis step) and the CODs that exit from reactor.

343

$$344 \quad \text{Hydrolysis} \quad r_{\text{hydrolysis}} = \frac{1}{\text{HRT}} \cdot (\text{COD}_P^{\text{Inlet}} - \text{COD}_P^{\text{Outlet}}) \quad (9)$$

345

$$346 \quad \text{Consumption} \quad r_{\text{consumption}} = \frac{1}{\text{HRT}} \cdot (\text{COD}_S^{\text{inside reactor}} + \text{COD}_S^{\text{inlet}}) - \text{COD}_S^{\text{Outlet}} \quad (10)$$

347

348

349 Based on these equations, the kinetic parameters of the model ($k_{\text{hydrolysis}}$ and $k_{\text{consumption}}$)
 350 and the pseudo-stoichiometric parameter ($Y_{\text{CH}_4/\text{COD}}$) can be estimated (Table 3) by
 351 fitting the experimental data (Figure 3) to linear regression.

352

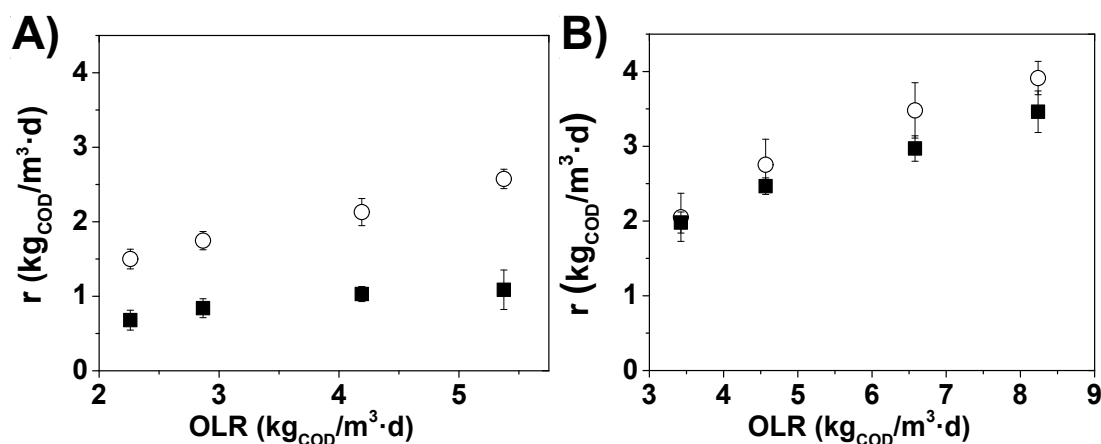
353 In Figure 3 it is shown the evolution of reaction rate in each step (Hydrolysis and
 354 consumption) at each condition: mono-digestion of SS and co-digestion of SS:WDW. In
 355 the case of SS condition (Figure 3-B) the hydrolysis and consumption rate are very
 356 similar. This occur because the hydrolysis rate was the limiting-step since the SS
 357 contain high number of complex structures that must be hydrolyzed before the rest of

358 the process and hence the consumption step depends on hydrolysis. Taking into account
359 the consumption rate calculation (Eq. 9), three effects occurred in mono-digestion of
360 SS: (1) CODs inlet was low because low content of easily hydrolyzable compounds in
361 SS so $K_{\text{hydrolysis}}$ must be high for transforming the major number of complex structures
362 to simple ones (2) acetogenesis is quicker than hydrolytic-acidogenesis³⁷ so: in spite of
363 high activity of hydrolysis transforming CODp into CODs, the consumption of CODs is
364 higher than the production. So, in the calculation of $K_{\text{consumption}}$ it is important to take
365 into account that the majority of CODs formed (CODs inside the reactor, Eq.10) is
366 assimilated. And hence, its concentration measured in the reactor is very low (only
367 0.04-1% of substrate CODs, Table 2) and the sum with the inlet CODs is lower than
368 CODs outlet obtaining a negative $K_{\text{consumption}}$ (Table 4).

369

370 However, in the case of co-digestion of SS:WDW (Figure 3-A) , the hydrolysis rate
371 was higher than consumption one, due to the high amount of easily biodegradable
372 compounds supply by WDW co-substrate. So in this case, the hydrolysis was not the
373 limiting-step (as it usually happens in AD) because the WDW contribute directly with
374 easily hydrolyzable organic matter compounds (inlet CODs, in Eq. 10). In addition, the
375 higher amount of TVS in WDW enhance the nutrients matter transfer to
376 microorganisms³⁷. Other authors have previously identified the degradation of acetate
377 (an intermediate compound in the metabolic pathway) as the rate-limiting step in co-
378 digestion processes³⁸⁻³⁹. As acetate assimilation is one of the reactions that occur during
379 consumption process, in this case, the rate-limiting step can be the consumption step
380 and $K_{\text{hydrolysis}}$ was higher than $K_{\text{consumption}}$ (Table 4).

381



382

383

384 **Figure 3** Influence of OLR on the hydrolysis and consumption reactions rate in the
 385 AcoD digester of SS:WDW (1:1 (v/v)) and in the control digester: **(A)** SS:WDW (1:1
 386 (v/v)). and **(B)** SS. Key: \circ hydrolysis \blacksquare consumption.

387

Table 4 Values of the kinetic and stoichiometric parameters obtained by regression using the first kinetic model, Eq. (5-8).

Feedstock	Parameter	Value	r^2	SSR
Co-digestion (1:1; SS:WDW)	$k_{hydrolysis}$ (d^{-1})	$5.22 \cdot 10^{-1}$	0.996	0.0102
	$k_{consumption}$ (d^{-1})	$9.57 \cdot 10^{-2}$	0.962	0.0044
	$Y_{CH_4/COD}$ (kg_{CH_4}/kg_{COD})	$1.15 \cdot 10^{-1}$	0.966	0.0004
Digestion (SS)	$k_{hydrolysis}$ (d^{-1})	$1.65 \cdot 10^{-1}$	0.997	0.0250
	$k_{consumption}$ (d^{-1})	$-4.98 \cdot 10^{-1}$	0.833	0.0346
	$Y_{CH_4/COD}$ (kg_{CH_4}/kg_{COD})	$0.95 \cdot 10^{-1}$	0.999	0.0020

388

389 Comparing both conditions, in spite of having a $k_{hydrolysis}$ in the same order in both
 390 conditions, the high $k_{consumption}$ in the case of co-digestion increase the global rate of the
 391 process obtaining a higher stoichiometric parameter for SS:WDW ($0.165 \text{ kg}_{\text{CH}_4}/\text{kg}_{\text{COD}}$)
 392 than that for SS ($0.094 \text{ kg}_{\text{CH}_4}/\text{kg}_{\text{COD}}$). Then, ACoD of SS:WDW improved the

393 biomethane potential and hence also the methane production efficiency of the systems
 394 removing the limiting effect of hydrolysis step.

395 Finally, the available organic matter consumption (elimination of COD_p) and
 396 production (production of COD_s) were calculated by Eq. 11 and 12, respectively; and
 397 the methane production by Eq. 13; taking into account its roles in the net of reactions
 398 proposed in the kinetic model as well as the kinetic values of constant (k) at the steady
 399 state in the semi-continuous anaerobic digesters. The results were drawn-up in Figure 4,
 400 evaluating the influence of HRT on each of them.

401

$$402 \quad \text{Solid substrate consumption} \quad (-R_{CODp}) = r_{hydrolysis} \quad (11)$$

403

$$404 \quad \text{Soluble substrate consumption} \quad (-R_{CODs}) = r_{hydrolysis} - r_{consumption} \quad (12)$$

405

$$406 \quad \text{Methane production} \quad R_{CH4} = Y_{CH4/CODs} \cdot r_{consumption} \quad (13)$$

407

408 As it was explained before, the ACoD of SS:WDW (1:1 v/v) avoid the limiting effect of
 409 hydrolysis step and as it was expected, the solid substrate consumption rate was much
 410 higher than the soluble substrate consumption being the consumption the rate-limiting
 411 step. In short, adding WDW to the feedstock involves a switch in the rate-limiting step
 412 in the process due to the high dissolved organic matter contained in this waste. Then, for
 413 ACoD of SS:WDW (1:1 v/v) the methane production rate depend on the consumption
 414 rate mainly because acetate degradation limiting effect.

415

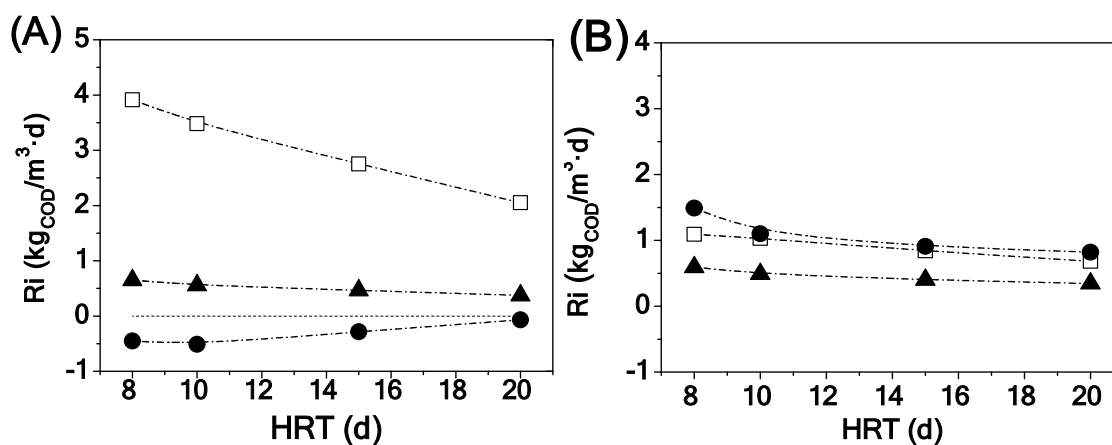
416 When sole SS was used as substrate, the COD_p and COD_s were very similar and it was
 417 reduced with the increasing of HRT (Figure 4-A). However, in this case of the methane

418 production obtained lower values than hydrolysis or solid/soluble substrate
 419 consumption. This means that not only hydrolysis but also methanogenesis is the rate-
 420 limiting step in this process. This occur because the high sensibility of the *Archaea*
 421 microorganisms to changes in the environment as well as the diffusional limitations of
 422 biomethane in the liquid medium ⁴⁰⁻⁴². Therefore, the control of the biomethane
 423 production in SS mono-digestion was due to the hydrolysis and methanogenesis steps.

424

425 In spite of being hydrolysis step the rate-limiting step in SS mono-digestion, in both
 426 conditions, the highest rates of methane production were reached at minimum OLR
 427 (Figure 3) and at maximum HRT = 8d (Figure 4) because the augmentation of new
 428 organic compounds used for microbial population.

429



430

431 **Figure 4** Influence of HRT on consumption rates in the semi-continuous anaerobic
 432 digesters of (A) SS:WDW (1:1 (v/v)), and (B) SS. Key: □COD_P ●COD_S ▲CH₄.

433

434 4 Conclusions

435 The proposed ACoD system promotes efficiently wine-making industry water
 436 sustainability by its use in WWTP as a co-substrate with sewage sludge. When

437 SS:WDW was anaerobically digested, biodegradability of the mixture in terms of VS
438 and CODT was 7-8% higher (52.7 and 56.7%, respectively for $OLR \leq 3.2$ ($\text{kg}_{\text{VS}}/\text{m}^3 \cdot \text{d}$))
439 and methane production was 30% higher than when SS was used as sole substrate. It
440 was reflected in kinetic study results that co-digestion improved biomethane potential
441 and methane production efficiency by switching the rate-limiting step. In this sense,
442 methane production related to the amount of organic matter was higher in the AcoD
443 SS:WDW (0.165 kgCH_4 / kgCOD) than in AD of SS alone (0.096 kgCH_4 / kgCOD).
444 These results open a new path in optimization studies of WWTP design and operation
445 by using new agro-industrial residues in an eco-friendly way.

446

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449 specifically [grant number CTM2015-64810R] entitled *Hydrogen-methane production*
450 *from biosolids and vinasses anaerobic co-digestion*, financed by the European Regional
451 Development Fund (ERDF).

452 **Nomenclature**

453	AD	Anaerobic digestion
454	COD	Chemical oxygen demand (kg/m^3)
455	COD _p	Particulate chemical oxygen demand (kg/m^3)
456	COD _s	Soluble chemical oxygen demand (kg/m^3)
457	COD _T	Total chemical oxygen demand (kg/m^3)
458	EE	Energy efficiency
459	HRT	Hydraulic retention time (d)
460	k	Kinetic constant (d^{-1})
461	MP	Methane productivity ($\text{L}/\text{kg}\cdot\text{d}$)
462	OLR	Organic loading rate ($\text{kg}/\text{m}^3\cdot\text{d}$)
463	r	Reaction rate ($\text{kg}/\text{m}^3\cdot\text{d}$)
464	R	Production rate ($\text{kg}/\text{m}^3\cdot\text{d}$)
465	SMP	Specific methane production (L/kg)
466	SS	Sewage sludge
467	TS	Total solids (kg/m^3)
468	V	Volume (L)
469	VFA	Volatile fatty acids (mg/L)
470	VS	Volatile solids (kg/m^3)
471	WDW	Wine distillery wastewater
472	WWTP	Wastewater treatment plant
473	X _{CH₄}	Percentage of methane in the biogas (%)
474	Y	Stoichiometric parameter
475	Subscript	
476	COD	Relating to chemical oxygen demand

477	<i>Consumption</i>	Relating to the consumption reaction
478	CH ₄	Relating to methane
479	Digester	Relating to the operating volume
480	<i>Hydrolysis</i>	Relating to the hydrolysis reaction
481	i	Relating to compound i
482	<i>Inlet</i>	Relating to the feed stream
483	<i>Outlet</i>	Relating to the effluent stream
484	VS	Relating to volatile solids
485		

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617 regression using the first kinetic model, Eq. (5-8).

618

619

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621 **Figure 1** Evolution of (A) pH inside the digester, (B) VS of the feed and the
622 effluent, (C) COD of the feed and the effluent, and (D) daily methane
623 volume in the semi-continuous anaerobic digesters of (i) SS:WDW (1:1
624 (v/v)), and (ii) SS.

625 **Figure 2** Influence of OLR on (A) SMP in terms of VS, (B) SMP in terms of
626 COD, (C) MP in terms of VS, and (D) MP in terms of COD.

627 **Figure 3** Influence of OLR on the hydrolysis and consumption reactions rate in the
628 AcoD digester of SS:WDW (1:1 (v/v)) and in the control digester: **(A)**
629 SS:WDW (1:1 (v/v)), and **(B)** SS. Key: ■ *consumption*. ○ *hydrolysis*

630 **Figure 4** Influence of HRT on production rates in the semi-continuous anaerobic
631 digesters of **(A)** SS:WDW (1:1 v/v) and **(B)** SS.

632 **Figure Captions**

633 **Figure 1** Key ● *feed* ■ *effluent*.

634 **Figure 2** Key: ■ *SS:WDW (1:1)* ○ *SS*.

635 **Figure 3** Key: ○ *hydrolysis* ■ *consumption*

636 **Figure 4** Key: □ COD_P ● COD_S ▲ CH_4 .

