1 Performance comparison of sampling designs for quality and safety

2 control of raw materials in bulk: a simulation study based on NIR

3 spectral data and geostatistical analysis

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# 13 ABSTRACT

14 This study exploits the potential of near infrared (NIR) spectroscopy to deliver a measurement 15 for each sampling point. Furthermore, it provides a protocol for the modelling of the spatial 16 pattern of analytical constituents. On the basis of these two aspects, the methodology proposed 17 in this work offers an opportunity to provide a real-time monitoring system to evaluate raw 18 materials, easing and optimising the existing procedures for sampling and analysing products 19 transported in bulk. In this paper, Processed Animal Proteins (PAPs) were selected as case 20 study, and two types of quality/safety issues were tested in PAP lots —induced by moisture and 21 cross-contamination. A simulation study, based on geostatistical analysis and the use of a set of 22 sampling protocols, made a qualitative analysis possible to compare the representation of the 23 spatial surfaces produced by each design. Moreover, the Root Mean Square Error of Prediction 24 (RMSEP), calculated from the differences between the analytical values and the geostatistical 25 predictions at unsampled locations, was used to measure the performance in each case. Results 26 show the high sensitivity of the process to the sampling plan used — understood as the 27 sampling design plus the sampling intensity. In general, a gradual decrease in the performance 28 can be observed as the sampling intensity decreases, so that unlike for higher intensities, the too 29 low ones resulted in oversmoothed surfaces which did not manage to represent the actual 30 distribution. Overall, Stratified and Simple Random samplings achieved the best results in most 31 cases. This indicated that an optimal balance between the design and the intensity of the 32 sampling plan is imperative to perform this methodology.

Keywords: Near infrared spectroscopy; Geostatistics; Kriging; real-time evaluation; in situ
 monitoring; spatial analysis

#### 35 1 Introduction

36 The European policy on quality and safety assurance of foods and feeds is stringent and

37 extensive. Strengthening monitoring schemes and management systems is therefore a strategic

38 goal for public bodies and food/feed operators, which need to develop alert systems and good

39 manufacturing practices to improve traceability, obtain safe products and ensure quality

40 standards. In this context, the existing legislation as regards animal by-products (ABPs) and, in

41 particular, processed animal proteins (PAPs), goes in line with the above framework [1–3].

42 For PAPs, which are valued as a major component of pet foods, a number of ingredients are

43 available in their manufacturing process (sheep, poultry, pig, bones, feathers, etc.), and the

44 effect of varying their proportions may lead to significant differences in the chemical

45 composition and nutritional value of the final product [4]. This case is evidence of the key role

that the industry plays in the agri-food chain. In this respect, the vision of a shared responsibility

47 for food/feed safety and the need to take steps towards closer interaction between operators and

48 authorities has already been expressed [5–8].

49 Bearing the above background in mind, all participants involved in the food chain

50 (manufacturers, authorities, laboratories, etc), along with the scientific community, have made

51 substantial efforts in response to the challenging task of implementing methodologies to assess

52 raw materials. On the one hand, the importance of the design of private and official food/feed

53 sampling plans should be emphasised. First, sampling of bulk raw materials must be done so

54 that representative sample can be obtained, which is crucial for accurately determining quality

and safety parameters. In fact, Kuiper and Paoletti [9] argue that representative sampling is a

56 must, so it needs to be considered as "a prerequisite equally important as the analytical

57 methodology to ensure reliability of final results".

58 Bulk food/feed sampling is typically described as a multistep process. First, a set of incremental

samples are taken from the lot. These are combined to form an aggregate sample, which is then

60 mass-reduced (possibly in several steps) to obtain the final analytical aliquot intended for

61 laboratory analysis [10,11]. The minimisation of all errors that may arise during this process is

of great relevance, and the Theory of Sampling (TOS) provides a fundamental framework to

63 categorise and either eliminate or minimise these errors, thus ensuring sampling

64 representativeness. To this end, a number of scientific studies addressing TOS and TOS-

65 compliant standards are available in the literature [12–15]. Nonetheless, there is still much to be

66 done to prevent sampling procedures of raw materials in bulk from being held back by financial

67 factors, required resources or time constraints. In fact, they usually lead to over-simplistic

68 solutions (e.g. grab sampling), excessive reduction of the sample volume (from several tons -lot;

to a few grams -lab aliquot), with the risks that this entails for the lot-sample representativity,

10 loss of spatial information and sampling procedures that are not tied in with the nature of the 11 product. Thus, improved and cost-effective methods and monitoring tools are needed, which

- 71 product. Thus, improved and cost-effective methods and monitoring tools are needed, which
- would enable the development of more efficient sampling plans. Moreover, the implementation

73 of fit-for-purpose protocols and real-time decision support systems are still lacking.

74 From an analytical point of view, Near-infrared spectroscopy (NIRS) can be a crucial asset for 75 the design of food/feed quality assurance systems. NIRS has experienced a strong development 76 over the last few years. Currently, it allows reliable analytical measurements to be made at 77 different steps of the production process. The acceleration of technological innovation has also 78 led to improved instrumentation, which has contributed to the use of NIRS for different 79 purposes (from at-line to in-situ applications) [16]. In the light of this, published research has 80 grown exponentially demonstrating NIRS abilities for analysing a wide variety of foods and 81 feeds, including heterogeneous materials, under diverse conditions. Considering its potential 82 impact, a number of industries have already integrated NIR-based quality-control schemes into 83 their manufacturing processes successfully, mostly in the form of at-line applications [17].

84 This notwithstanding, the analysis of raw materials in bulk directly from the load of a transport 85 vehicle has not been explored in depth yet. However, NIRS features a range of valuable 86 qualities that can make it ideal for this task. Unlike traditional wet chemistry methods, this 87 technique is capable of performing quantitative and qualitative analysis of intact sample within 88 seconds, thus allowing the volume of sample analysed to be significantly increased. The 89 application of NIRS to this task could resolve some of the constraints of the existing 90 methodologies by performing rapid and cost-effective analysis. On this basis, research was 91 recently initiated to implement a real-time NIRS-based monitoring system for the in-situ 92 characterization of raw materials at delivery points of production plants [18]. The methodology 93 proposed by the authors relies on using NIRS optical probes to sample loads of transport units 94 of products in bulk. A subsequent geostatistical analysis of the observations succeeded in 95 mapping the spatial distribution of key properties of PAPs. Despite this, the study did not fully 96 investigate the sampling stage of the evaluation process, as well as its impact on the 97 representation of the spatial surfaces of the PAP quality/safety attributes. 98 On the basis of this methodology, this paper aims at making a performance comparison of a set 99 of sampling schemes through carrying out a simulation study. A further goal is to evaluate these

plans concerning their ability to spatially characterize the quality and safety issues tested in PAP

- 101 lots.
- 102

#### 103 2 Materials and Methods

# 104 2.1 Samples and experimental design

A set of 8 lots of PAPs coming from a rendering plant was selected for this work from the ones
used by Adame-Siles et al [18]. The set consisted of the following lots: Lot 1 (100% Poultry),
Lot 2 (58% Poultry, 42% Pig), Lot 3 (64% Poultry, 36% Pig), Lot 4 (100% Poultry), Lot 5 (50%
Poultry, 50% Pig), Lot 7 (100% Poultry), Lot 8 (100% Poultry) and Lot 10 (23% Poultry, 60%
Pig, 11% Cattle, 6% Sheep). These captured the variability of the available batches in terms of
species composition.

111 Two sorts of quality and safety issues were simulated, on one hand the presence of high 112 moisture content areas (issue A), which may act as indicators as they could lead to fungal 113 growth or bacteriological problems, and on the other, adulteration or cross-contamination 114 between products of different nature or category (issue B). A glass container was used to place 115 and analyse each lot and type of issue (Figure 1). Issue A was induced in five lots in different 116 ways. In each case, two layers at different depths were measured and a methacrylate sheet with 117 10 x 14 sampling points facilitated the positioning of the probe for analysis (first at layer A, and 118 then the probe was inserted deeper into the sample at each point to reach layer B). Lots 1 119 (Figure 1B), 2 (Figure 1E), 3 (Figure 1F), 4 (Figure 1G) and 7 (Figure 1A) formed part of this 120 particular case study, in which distribution and quantity of water were the two sources of 121 variability among tests. Water was poured 1 day prior to analysis according to the distribution 122 and amount of water that Figure 1 shows for each test. On the other hand, three further tests, 123 involving Lots 1, 5, 8 and 10, addressed the evaluation of issue B. For this evaluation, tests were 124 carried out making three different mixtures between lots, two of them between Lot 1 and Lot 5, 125 varying their distribution (Figure 1C and Figure 1D), and the third one between Lot 8 and Lot 126 10 (Figure 1H). Measurements were taken for layer A in these tests. Moreover, it is important to 127 point out that the tests performed aimed at exploring the limits of the methodology, which is 128 why both issues were induced in localized areas.

## 129 2.2 Instrumentation and data analysis

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130 2.2.1 Near-infrared Spectroscopy analysis
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131 A reflection probe (Turbido, Solvias AG) (Figure 1) was interfaced to a Matrix-F FT-NIR

132 instrument (834.2–2502.4 nm) to measure reflectance spectra in PAP lots according to the

experimental design described above. The probe features a stainless-steel body of 12 mm in

134 diameter with an insertable length of 300 mm, and its end has a sapphire window that is capable

135 of illuminating a 1.5 mm diameter spot. The probe is composed of two optical fibers: one for

- illumination and one for detection (each one of 600 µm core); while two fiber cables of 100 min length connect the probe to the instrument.
- 138 In every test, a measurement was taken for each probe insertion point of the designed grid, and
- each spectrum was an average of 32 scans with a scanner velocity of 10 kHz and a resolution of
- 140 16 cm<sup>-1</sup>. White reference measures were taken with a probe-specific Spectralon every set of 42
- 141 measurements (every 25-30 minutes approximately).
- 142 Within the context of a preliminary study [18], first, the noise level of the signal was evaluated
- along the spectral range by applying to the log 1/R data a first derivative pre-treatment, with a
- single-unit gap and five data-point smoothing. After visual examination, noisy regions were
- 145 found at the beginning and at the end of the spectral range, leading to the selection of the
- optimum wavelength range 1386-2033 nm. Subsequently, a standardization methodology was
- 147 initiated to transfer a database of 346 samples of PAPs, from which calibration equations had
- 148 been developed using a different analysis mode (the same instrument was used but coupled to a
- 149 detection head for contactless measurements). Finally, after a recalibration procedure,
- 150 calibration equations (whose most relevant statistics are shown in Table 1) were obtained so that
- an analytical result for both moisture (issue A) and crude protein (issue B) constituents could be
- 152 got at every sampling unit using the NIR reflection probe.
- Software OPUS v7.0 (Bruker Optik) was used for spectral acquisition. WinISI v.1.50 (Infrasoft
  International), Matlab R2018a (The MathWorks Inc.) and PLS Toolbox (Eigenvector Research)
  were used for applying the NIRS prediction models.
- 156 2.2.2 Geostatistical analysis
- The geostatistical study addressed the analysis of the spatial distributions of moisture (issue A)
  and crude protein (issue B). The methodology used provides for a two-stage assessment process
  for each test: (a) structural analysis; and (b) spatial estimation.
- 160 First, the structural analysis comprised both the exploratory data analysis and the variographic
- 161 analysis. The spatial correlation analysis, which aims at describing the relationships between
- sampled points, was carried out following two steps: the estimation of the semi-variogram and
- 163 its subsequent modelling. The semi-variogram measures the average dissimilarity between data
- separated by distance **h**, a vector commonly known as the lag distance or lag, and it is calculated
- as half the average squared difference between the components of data pairs [19]. The
- 166 experimental variograms were computed for each test, obtaining omnidirectional and directional
- 167 variograms (defined by 0, 45, 90 and 135°), in order to analyse the autocorrelation structure and
- 168 the spatial pattern of the considered constituent in each case. The spherical and linear models
- 169 were used for the fitting of the experimental variograms, hence obtaining continuous functions

that provide a model of spatial dependence, which is needed to compute a variogram value atunobserved locations [20].

172 The spatial estimation of the variables under consideration was addressed by using Kriging as 173 the interpolation technique. This family of generalized least squares linear regression 174 algorithms, characterized by being highly accurate and robust, manages to use the combination 175 of weights and values at known locations (from the structural analysis) to estimate the value at 176 unsampled locations, achieving reliable results. The regionalized variable of interest,  $Z(\mathbf{u})$ , is 177 considered a random function, generically decomposed into a trend component, m(u), and a 178 residual component, R(u). There exist different kinds of kriging estimators, which mainly differ 179 in their treatments of the trend component. Ordinary kriging (OK) was used to interpolate the 180 NIRS predictions for the parameters of interest in this paper. OK, which is one of the most 181 commonly used variants of kriging, is based on the assumption that the mean is unknown and 182 limits its stationarity to the local neighbourhood of the location **u** being estimated. Further 183 details on the implementation of the geostatistical approach in PAPs and on OK theory and 184 practice may be found in [18,21–25].

All geostatistical analyses were carried out in the R environment (version 3.4.3), including the
exploratory data analysis, the variographic analysis, and the mapping of spatial estimations. The
R package gstat was used to develop the methodology [26].

#### 188 2.3 Simulation study

#### 189 2.3.1 General procedure

NIRS measurements were taken once for every sampling location, i.e. obtaining a grid of 10x14
points for each test performed, which were used as analytical reference for this simulation study.
Considering this population of N=140 units, the data were then sub-sampled by several
procedures to give different sample sizes and distributions and evaluate the loss of information
in each case.

- A set of four different sampling intensities were tried (i=30, 20, 10 and 5% of the population)
- 196 for every sampling design (defined in section 2.3.2), making a total of 16 sampling plans
- 197 (Figure 2). These intensities were chosen so as to facilitate comparison by ensuring that all
- 198 sampling designs achieved the same sample size n(i).
- 199 Moreover, after performing each sampling plan (defined by the sampling design and the
- sampling intensity), the resulting data sets were all assessed and treated for geostatistical
- 201 analysis, so that both variographic analysis and subsequent kriging with the sub-sampled data
- 202 were performed according to the procedure described before. Therefore, this led to obtaining

- (for each sampling plan) spatial predictions from the geostatistical models that could becompared with the reference data.
- All the sampling plans include some randomness, so in order to carry out a performance
- 206 comparison of the methodology among sampling plans, a total of R=1000 simulation
- 207 replications were computed for each one.
- 208 2.3.2 Sampling designs
- Simple random sampling (SRS)
- 210 Most standards, guidelines and regulations dealing with the control of loose feeds consider
- simple random sampling (SRS) as the selection process of incremental samples when samplingfrom bulk [10,27].
- In this paper, different sets of n(i) units, from the sampled grid (N = 140 points, all having an
  analytical result available), were randomly selected according to every sampling intensity tried,
- 215 i (Figure 3A).
- Stratified random sampling (StRS)

The study area was partitioned into 7 regions (Figure 3B). These areas were distributed so that the corners, the centre and the lateral walls of the container represent different strata. Therefore, this resulted in a total of 4 corner strata each composed of a grid of 5x4 sampling points, two lateral strata with a grid of 3x6 units respectively, and a central stratum with a grid of 4x6

- sampling locations.
- The sampling design within each stratum was SRS, with the selections in the different strata being made independently. Furthermore, the same number of units was selected from each stratum to form the final sample size n(i).
- Cluster sampling (Clu)
- In this work, clusters were conceived to be formed of two sampling units adjacent on the
  vertical axis (Figure 3C). Consequently, an arrangement of 70 clusters over the study area was
  available.
- A number of clusters,  $k \le n(i)/2 \in \aleph$ , were randomly selected according to each sampling intensity i, so that the final sample size n(i) contained the same number of sampling units as the rest of the sampling designs; except for i=5%, in which 3 clusters were selected and therefore n(5%) was made of 6 units, one less than in all other cases.

#### • Systematic sampling (Sys)

Among the possible realizations of this type of sampling scheme, it was decided to simulate one in particular due to its high potential and efficiency to run multiple iterations within the study area. In this case, the approach was to simulate that the NIR fiber-optic probe would follow the moves of a knight over a PAP lot as if it were a chessboard.

238 Many methods tackle the issue of the knight's tour problem, trying to discover those possible

239 paths or sequence of moves such that every square is only visited once. As a consequence, a

number of algorithms and solutions have been found to that problem (brute-force approach,

241 neural network computing, etc.). This paper implements an algorithm based on the Warnsdorff's

rule. The algorithm starts by randomly selecting 1 unit of the available sampling grid (N=140),

and then proceeds to the adjacent, unvisited unit with the least degree from which the probe will

have the fewest onward moves, and so on (Figure 3D). As a stopping rule, the algorithm uses

the sampling intensity considered, i.

## 246 2.3.3 Performance evaluation

As a measure to compare the performance of the different sampling plans, the Root Mean

248 Square Error of Prediction (RMSEP) statistic was used in this paper:

$$RMSEP = \sqrt{\frac{\sum_{j=1}^{N} (y_{j,krig} - y_{j,NIR})^2}{N}}$$
(1)

where  $y_{j,krig}$  are the predictions obtained for N by applying kriging from the sample selected by each sampling plan and  $y_{i,NIR}$  are the NIR analytical values obtained for the sampled grid N.

Both the mean and the standard deviation (SD) of this statistic were calculated for the
 R=1000 simulations performed:

$$\mu = \frac{1}{R} \sum_{i=1}^{R} RMSEP_i$$
(2)

$$\sigma = \sqrt{\frac{\sum_{i=1}^{R} (RMSEP_i - \mu)^2}{R - 1}}$$
(3)

- 253 In addition, two-way analysis of variance (ANOVA) was performed for every test to examine
- whether significant differences in log values of the mean RMSEP were found among samplingintensities and sampling designs.
- All algorithms to carry out the simulations of the different sampling plans, together with the calculation of those statistics involved in the performance assessment, were developed in RStudio (v 1.1.1463).
- 259

#### 260 **3 Results and Discussion**

#### 261 3.1 Data preparation and analysis

Once all the experimental tests were performed, analysing each case with the reflection probe, the NIRS calibration equations were applied to every unit of the sampling grid (hereinafter referred to as "100% sampling", i.e. N=140 points) of each test. Hence, this made it possible to obtain a NIRS prediction for the parameter of interest, either moisture (issue A) or crude protein (issue B), at each sampling location of the case being analysed.

267 The first stage of the geostatistical study was then tackled to find the model that best describes 268 the spatial pattern of the constituent in each test. A comprehensive description of the spatial 269 behaviour of these parameters in tests with PAPs can be found in [18]. Overall, the results of the 270 variographic analysis of the tests presented in this paper are in line with those reported in [18]. 271 Thus, the semivariograms, computed from the "100% sampling" data sets in each case study, 272 show differences between the spatial variation of both constituents. On the one hand, crude 273 protein semivariograms generally result in plots with a steady increase in the semivariance with 274 distance, as well as a discontinuity at the origin. In contrast, semivariograms for tests involving 275 moisture adulteration display curves with lower semivariances than crude protein, which show a 276 zero, or close to zero, intercept and rise until they reach a plateau. To infer spatial estimations at 277 unobserved locations from the spatial autocorrelation analysis, theoretical functions are needed 278 for the fitting of the semivariograms. For this purpose, linear and spherical models were 279 generally used for crude protein and moisture constituents, respectively, as they were the 280 mathematical models that provided the best fit in each case.

Based both on the NIRS predictions and the results of the variographic analyses, the simulation study proceeded to perform the different sampling plans, which were implemented based upon the arrangement of the intensities and designs described in the methodology. For each sampling strategy, corresponding to a specific sampling intensity together with the sampling design in question, a routine was run comprising a total of 1000 simulations. The specific sample data set resulting from every simulation of each test was used as an input for spatial interpolation by
ordinary kriging, thus producing a map based on the sample and interpolated values at all 140
points for use in equation (1).

### 289 3.2 Spatial distributions

290 Figure 4 and Figure 5 illustrate representative examples of the two kinds of issues in lots of 291 PAPs tested in this work. While the former shows the spatial distributions for moisture of one 292 test associated with issue A (Lot 1-layer B, Figure 1B), the latter displays crude protein spatial 293 surfaces obtained for one of the tests related to issue B (Mixture of lots 1+5(2), Figure 1D). In 294 both scenarios, the results are derived from the geostatistical study and application of ordinary 295 kriging to the dataset composed of the NIRS predictions (for the constituent under study) at the 296 sampled locations (defined by each sampling plan). Both figures present one random iteration 297 for each sampling plan.

Figure 4 (top of picture) shows first the original distribution achieved by applying OK to the 100% sampling dataset, with the goal of allowing for comparison with the rest of sampling plans. In this plot, the moisture distribution reveals that higher values are concentrated in the corners and the central region of the investigated area, which in fact corresponds to the accumulation of water induced in this test (Figure 1B).

One of the clearest results that can be observed from the maps obtained, taking into account the range of sampling intensities tested, is that in general there is a decrease in the accuracy of mapping risk areas by moisture accumulation with sampling intensity. In this way, while sampling intensities of 30% and 20% frequently manage to portray most of the critical areas, both 10% and 5% intensities give rise to a significant loss of at least one or several of these regions in most cases.

309 On the other hand, when it comes to sampling designs, simple random sampling and stratified 310 sampling achieve the best spatial surfaces, if the actual moisture distribution in the test 311 performed is considered. Both sampling strategies succeed in depicting more faithfully the 312 moisture concentration profile, if compared to 100% sampling, even when a 10% sampling 313 intensity is applied. Conversely, neither cluster sampling nor systematic sampling were able to 314 find accurate distributions, the former failing to reach reasonable results particularly at 10% and 315 5% of sampling intensity, whilst the latter did so at 20% and less.

316 As in the previous case, the crude protein distribution for the 100% sampling dataset of the test

317 appears on the top of Figure 5. This map for the crude protein parameter pictures two distinct

318 areas showing a different pattern from the rest, which is consistent with the composition of the

319 mixture of lots performed in this test (Figure 1D).

- 320 The resulting spatial maps are also shown for this case according to the sampling plan used.
- 321 Their analysis and discussion are analogous to the one previously made. As the sampling
- 322 intensity decreases, there is a clear fall in the performance regardless of the sampling design,

323 with 30% and 20% sampling intensities achieving better results than 10% and 5%.

324 Once again, comparing all the maps at a given sampling intensity, both simple random sampling

325 and stratified sampling manage to represent most efficiently the actual crude protein

326 distribution. This notwithstanding, cluster sampling remains close to them here at all cases but

327 5%, whereas systematic sampling fails again particularly at 10% and 5%.

328 In interpreting of these results, it should be taken into consideration that kriging techniques tend 329 to overestimate small values and underestimate large values under certain circumstances, i.e. its 330 estimates are less variable than the true values. Moreover, the larger the kriging variance of the 331 estimates on average, the more apparent this smoothing effect becomes [22]. One reason for a 332 larger kriging variance is because sample sites might be too sparse. This may have led to the 333 highly smoothed representations observed when sampling intensities of 10% and 5% were used. 334 A clear effect of this is a significant decrease in their ability to faithfully represent the actual 335 scenario and, thereby, the spatial patterns eventually end up providing misleading information 336 in these cases.

#### 337 3.3 Spatial prediction

Following the qualitative analysis of the spatial distributions, the calculation of the RMSEP for all the tests performed, whose results are reported in Appendix A (Tables A1-A4), aimed at allowing a quantitative examination of the estimation error values. These tables show the mean and the SD of the RMSEP for every sampling protocol of each test, computed from the 1000 iterations carried out. All these errors were obtained comparing, in each point of the 100% sampling grid, constituent values estimated by OK and the true analytical value (NIRS prediction).

345 In order to facilitate a performance comparison, figures 6 and 7 graphically summarize the mean 346 and the SD (showed as error bars) values of the RMSEP for the different case studies tested, 347 categorizing the results by groups both according to the sampling strategy used and the 348 sampling intensity in each case (layer A statistics for both issues A and B are shown in Figure 6, 349 while results from layer B, i.e. only for issue A, appear in Figure 7). First, they illustrate how 350 there is a clear negative correlation between the sampling intensity and the observed error of the 351 estimates. This may be explained by considering the nature of kriging. As anticipated, this 352 geostatistical technique consists of a multistep process, which is dependent upon the statistical 353 relationships among the measured points. In this way, kriging not only considers the distance

- between the observed locations and the prediction point but also the overall spatial arrangement
- 355 of the sampled points, to finally derive a prediction. To this aim, the task of uncovering the
- 356 model of statistical dependence, i.e. the spatial autocorrelation model, to be fitted to the
- 357 observed points is therefore crucial. Consequently, bearing in mind both the distributions and
- 358 the error values obtained, the aggregate effect of a smaller sample size and sparser sample sites
- 359 (linked to lower sampling intensities) along with the aforementioned smoothing effect of
- 360 kriging might have had a critical impact on the spatial dependence model, hindering its
- 361 representativeness in these cases and leading to the loss of performance observed.
- Overall, it can be noticed that stratified sampling outperforms the rest of the sampling protocols
  in most cases. In fact, if sampling intensities of 10% and 5% are considered, it is the sampling
  design accomplishing the lowest estimation error in all the tests performed. For higher
- intensities, however, stratified sampling along with systematic sampling prevail over the rest
- 366 with the lowest value of RMSEP. It should also be noted that simple random sampling remains
- 367 close to the performance of stratified sampling in general. Unlike the other designs, cluster
- 368 sampling did not succeed in being as appropriate for the purpose of inferring the spatial369 distributions.
- 370 The ANOVA results (Table 2) showed that there was significant variation in RMSEP values 371 among sampling intensities in all cases (P < 0.05). This variation suggests the important role of 372 the sampling intensity in the results. On the other hand, significant differences were also found 373 in most tests among sampling designs. Nonetheless, the results revealed a few exceptions in this 374 case. No statistically significant difference could be determined for moisture tests involving Lot 375 7 (layer A and B) and Lot 4 (layer A), along with the protein test from the mixture Lot 1+5. As 376 can be noted from the tables provided, in all these cases, systematic sampling outperforms other 377 designs at intensities of 30% and 20%, whilst stratified sampling does the same at 10% and 5%. 378 Thus, as regards efficiency of the sampling design, no clear evidence was found in these cases
- to help decide one design over the other.

380 Based on these results, it should be underlined the importance of carrying out a preliminary 381 thorough analysis of the raw material properties (heterogeneity, risk tolerance limits, etc.), as 382 well as a profound study both of the Total Analytical Error (TAE) and the Total Sampling Error 383 (TSE), which is deeply addressed by the Theory of Sampling (TOS), to draw conclusions from 384 the implementation of the methodology. Thus, it is strongly encouraged to be careful, not only 385 when modelling the spatial autocorrelation present in the lot, but also when interpreting the 386 maps as a result of the representation of the kriged estimates. As can be appreciated from the 387 results, a precise balance between an optimal sampling intensity (taking into account that lower 388 intensities might prove to be insufficient to ensure reliable results) and a fit-for-purpose

- 389 sampling design is a necessary requirement to represent as faithfully as possible the spatial390 distribution of the constituents, avoiding misleading pictures.
- 391

#### 392 4 Conclusions

393 NIR spectroscopy was used to perform sampling and analysis (as a single step) over a set of 394 tests simulating two quality/safety issues. The results show that spatializing critical parameters 395 of PAPs can provide decision makers with a useful, low-cost reference tool to identify patterns 396 and risk areas non-compliant with quality and safety criteria. As a consequence, this might 397 benefit the supplier-purchaser relationship by improving efficiency and transparency along the 398 process.

399 The spatial analysis of reference constituents, and the estimation in non-sampled locations by 400 geostatistical inferential methods allowed the mapping of crucial analytical constituents for the 401 evaluation of lots of PAPs. This study has shown that the combination of NIRS and 402 geostatistical analysis can be a powerful tool. Nevertheless, the results reveal that the accuracy 403 of the distributions depends to a great extent on the sampling plan performed, i.e. both on the 404 design and the level of intensity. Among the sampling designs tested, stratified sampling 405 achieved the best results in most cases in both qualitative and quantitative terms, followed by 406 simple random sampling and systematic sampling. In addition, sampling intensities of 10% and 407 5% of the total sampling grid tested proved to be mostly inefficient to represent the actual 408 distributions.

- It should be highlighted that the prediction results highly depend on the quality of the availableobservations and their spatial relationship. Therefore, the adoption of this methodology must
- 411 necessarily rely on robust NIRS models together with an optimal sampling plan (striking a
- 412 balance between strategy and intensity), to finally achieve reliable results. In this regard, further
- 413 research should be carried out, for instance, to explore more efficient and fit-for-purpose
- 414 sampling plans, as well as to perform validation tests in real conditions for evaluating products
- 415 in bulk directly over the transport unit (trucks, trailers, containers, etc.)
- 416

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- 426

## 427 **References**

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## 516 Tables

Constituent	Pre-processing	Mean	SECV	R <sup>2</sup>	RPD
Moisture	1,5,5,1	3.78	0.36	0.77	2.1
Crude Protein	1,5,5,1	57.7	2.45	0.86	2.7

517 Table 1. Calibration statistics for predicting moisture and crude protein content (%) in PAP lots.

- 518 SECV: standard error of cross-validation (%); R<sup>2</sup>: coefficient of determination; RPD: Residual
- 519 Predictive Deviation.

Table 2. Two-way ANOVA results (P values) for the sampling designs (SRS, Str, Clu, Sys) and
 intensities (i=30%, 20%, 15%, 5%) tested in Moisture (M) and Crude Protein (CP) tests.

Layer	Sampling	Lot 1 (M)	Lot 2 (M)	Lot 3 (M)	Lot 4 (M)
	Intensities	4.16x10 <sup>-6</sup>	1.62x10 <sup>-6</sup>	3.63x10 <sup>-9</sup>	2.14x10 <sup>-5</sup>
A	Designs	0.022	0	0.001	0.6
D	Intensities	9.18x10-9	2.52x10-5	1.18x10 <sup>-8</sup>	3.93x10-7
D	Designs	0.015	0.001	0.017	0.01
Layer	Sampling	Lot 7 (M)	Lot 1+5 (CP)	Lot 1+5(2) (CP)	Lot 8+10 (CP)
	Intensities	4.19x10 <sup>-5</sup>	2.02x10 <sup>-6</sup>	1.9x10 <sup>-9</sup>	3.49x10 <sup>-11</sup>
A	Designs	0.097	0.38	0.001	0.013
D	Intensities	2.19x10 <sup>-6</sup>	-	-	-
В	Designs	0.08	-	-	-

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535	Figures Caption
536 537	<b>Figure 1.</b> Experimental design: Glass container and Reflection Probe. (A) Lot 7. (B) Lot 1. (C) Lot 1+5. (D) Lot 1+5(2). (E) Lot 2. (F) Lot 3. (G) Lot 4. (H) Lot 8+10.
538	Figure 2. Procedure to perform the simulation study.
539 540	<b>Figure 3.</b> Sampling designs. (A) Simple Random, i=10% example. (B) Stratified. (C) Cluster. (D) Systematic, i= 20% example.
541	Figure 4. Spatial distributions Lot 1b (Moisture): 100%; Simple Random (1-4); Stratified (5-8);
542	Cluster (9-12); Systematic (13-16).
543 544	<b>Figure 5.</b> Spatial distributions Lot 1+5(2) (Crude Protein): 100%; Simple Random (1-4); Stratified (5-8); Cluster (9-12); Systematic (13-16).
545	Figure 6. Estimation error values (mean and SD of RMSEP; layer A) for the Moisture (M) and
546	Crude Protein (CP) case studies and the different sampling plans. Protocols: Cluster Sampling
547	(Clu), Simple Random Sampling (SRS), Stratified Sampling (Str) and Systematic Sampling
548	(Sys). Intensities: 5% (S05), 10% (S10), 20% (S20) and 30% (S30).
549	Figure 7. Estimation error values (mean and SD of RMSEP; layer B) for Moisture (M) case
550	studies and the different sampling plans. Protocols: Cluster Sampling (Clu), Simple Random
551	Sampling (SRS), Stratified Sampling (Str) and Systematic Sampling (Sys). Intensities: 5%
552	(S05), 10% (S10), 20% (S20) and 30% (S30).
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- 562 APPENDIX A
- **Table A.1.** Estimation error values (RMSEP Mean and Standard Deviation). Simple Random
- 565 Sampling (SRS).

SPS	Sampling	Lot 1		Lot 7		Lot 2		Lot 3		Lot 4		Lot 1+5		Lot 1	+5(2)	Lot 8+10	
SKS	Intensity (%)	Mean	Std	Mean	Std	Mean	Std	Mean	Std								
Layer A	30	0.149	0.016	0.230	0.025	0.098	0.006	0.122	0.010	0.131	0.011	1.456	0.104	1.585	0.081	1.524	0.074
	20	0.174	0.019	0.266	0.031	0.109	0.008	0.136	0.009	0.144	0.010	1.593	0.099	1.736	0.103	1.660	0.083
	10	0.220	0.032	0.327	0.044	0.125	0.013	0.155	0.014	0.161	0.011	1.809	0.151	1.958	0.147	1.818	0.105
	5	0.262	0.042	0.377	0.057	0.142	0.017	0.174	0.021	0.174	0.015	1.994	0.244	2.171	0.239	1.956	0.169
	30	0.271	0.026	0.230	0.037	0.093	0.006	0.095	0.011	0.101	0.008						
Layer B	20	0.315	0.031	0.277	0.046	0.103	0.008	0.110	0.014	0.113	0.009						
	10	0.370	0.037	0.362	0.054	0.118	0.012	0.139	0.019	0.130	0.010						
	5	0.415	0.045	0.423	0.054	0.132	0.016	0.167	0.026	0.144	0.014						

- **Table A.2.** Estimation error values (RMSEP Mean and Standard Deviation). Stratified
- 568 Sampling (Str).

Str	Sampling	Lot 1		Lot 7		Lot 2		Lot 3		Lc	ot 4	Lot 1+5		Lot 1	+5(2)	Lot 8+10	
Str	Intensity																
	(%)	Mean	Std	Mean	Std	Mean	Std	Mean	Std								
	30	0.145	0.013	0.227	0.023	0.098	0.006	0.121	0.010	0.130	0.009	1.442	0.105	1.575	0.078	1.516	0.072
Layer A	20	0.169	0.016	0.261	0.023	0.108	0.007	0.135	0.009	0.143	0.010	1.585	0.088	1.723	0.091	1.650	0.072
	10	0.210	0.026	0.312	0.029	0.123	0.012	0.153	0.012	0.160	0.010	1.769	0.104	1.921	0.138	1.806	0.096
	5	0.246	0.034	0.358	0.048	0.137	0.016	0.169	0.018	0.172	0.015	1.941	0.191	2.127	0.202	1.929	0.151
	30	0.269	0.021	0.223	0.029	0.093	0.006	0.093	0.010	0.099	0.008						
Layer B	20	0.309	0.028	0.268	0.038	0.102	0.008	0.107	0.013	0.112	0.009						
	10	0.368	0.034	0.347	0.047	0.116	0.011	0.129	0.014	0.127	0.010						
	5	0.410	0.042	0.414	0.050	0.128	0.014	0.152	0.015	0.143	0.013						

# **Table A.3.** Estimation error values (RMSEP Mean and Standard Deviation). Cluster Sampling

571 (Clu).

	Sampling	Lo	ot 1	Lot 7		Lot 2		Lot 3		Lot 4		Lot 1+5		Lot 1	+5(2)	Lot 8+10		
Clu	Intensity (%)	Mean	Std	Mean	Std	Mean	Std	Mean	Std									
	30	0.170	0.023	0.260	0.034	0.100	0.008	0.124	0.011	0.133	0.011	1.468	0.121	1.606	0.099	1.533	0.077	
Layer A	20	0.201	0.033	0.301	0.044	0.113	0.010	0.138	0.011	0.147	0.011	1.633	0.126	1.770	0.123	1.674	0.083	
	10	0.249	0.042	0.362	0.059	0.133	0.016	0.162	0.019	0.165	0.012	1.873	0.200	2.022	0.168	1.847	0.118	
	5	0.308	0.052	0.437	0.072	0.156	0.023	0.191	0.029	0.184	0.023	2.121	0.282	2.292	0.274	1.998	0.194	
	30	0.290	0.034	0.259	0.049	0.096	0.008	0.103	0.016	0.105	0.009							
Layer B	20	0.334	0.038	0.317	0.058	0.107	0.010	0.121	0.018	0.118	0.010							
	10	0.391	0.039	0.398	0.057	0.124	0.014	0.156	0.025	0.136	0.012							
	5	0.443	0.055	0.480	0.073	0.144	0.021	0.185	0.032	0.156	0.023							

# **Table A.4.** Estimation error values (RMSEP Mean and Standard Deviation). Systematic

574 Sampling (Sys).

Sys	Sampling	Lo	Lot 1		Lot 7		Lot 2		Lot 3		Lot 4		Lot 1+5		+5(2)	Lot 8+10	
Sys	Intensity (%)	Mean	Std	Mean	Std	Mean	Std										
	30	0.153	0.014	0.189	0.013	0.121	0.017	0.113	0.007	0.136	0.010	1.347	0.131	1.655	0.134	1.484	0.051
Layer A	20	0.170	0.015	0.219	0.018	0.135	0.013	0.123	0.008	0.149	0.008	1.580	0.075	1.774	0.140	1.631	0.062
	10	0.255	0.079	0.338	0.086	0.146	0.015	0.157	0.026	0.176	0.022	1.952	0.142	2.079	0.217	1.817	0.102
	5	0.356	0.107	0.444	0.112	0.156	0.016	0.209	0.040	0.187	0.030	2.188	0.377	2.372	0.422	1.967	0.214
	30	0.270	0.020	0.200	0.016	0.119	0.014	0.095	0.006	0.101	0.005						
Layer B	20	0.310	0.024	0.241	0.030	0.129	0.012	0.106	0.007	0.108	0.006						
	10	0.395	0.063	0.391	0.087	0.136	0.013	0.162	0.036	0.136	0.015						
	5	0.455	0.088	0.494	0.118	0.141	0.015	0.189	0.035	0.152	0.016						





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(1) SRS | 30%

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(6) Str | 20%

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(7) Str | 10%



(4) SRS | 5%

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(1) SRS | 30%

(2) SRS | 20%

(3) SRS | 10%

(4) SRS | 5%



























