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DEEP LEARNING AND POLAR TRANSFORMATION TO ACHIEVE A NOVEL ADAPTIVE AUTOMATIC MODULATION CLASSIFICATION FRAMEWORK

by

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A THESIS

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DEEP LEARNING AND POLAR TRANSFORMATION TO ACHIEVE A NOVEL ADAPTIVE AUTOMATIC MODULATION CLASSIFICATION FRAMEWORK

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University of Nebraska, 2020

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Automatic modulation classification (AMC) is an approach that can be leveraged to identify an observed signal's most likely employed modulation scheme without any a priori knowledge of the intercepted signal. Of the three primary approaches proposed in literature, which are likelihood-based, distribution test-based, and feature-based (FB), the latter is considered to be the most promising approach for real-world implementations due to its favorable computational complexity and classification accuracy. FB AMC is comprised of two stages: feature extraction and labeling. In this thesis, we enhance the FB approach in both stages. In the feature extraction stage, we propose a new architecture in which it first removes the bias issue for the estimator of fourth-order cumulants, then extracts polar-transformed information of the received IQ waveform's samples, and finally forms a unique dataset to be used in the labeling stage. The labeling stage utilizes a deep learning architecture. Furthermore, we propose a new approach to increasing the classification accuracy in low signal-to-noise ratio conditions by employing a deep belief network platform in addition to the spiking neural network platform to overcome computational complexity concerns associated with deep learning architecture. In the process of evaluating the contributions, we first study each individual FB AMC classifier to derive the respective upper and lower performance bounds. We then propose an adaptive framework that is built upon and developed around these findings. This framework aims to efficiently classify the received signal's modulation scheme by intelligently switching between these different FB classifiers to achieve an optimal balance between classification accuracy and computational complexity for any observed channel conditions derived from the main receiver's equalizer. This

framework also provides flexibility in deploying FB AMC classifiers in various environments. We conduct a performance analysis using this framework in which we employ the standard RadioML dataset to achieve a realistic evaluation. Numerical results indicate a notably higher classification accuracy by 16.02% on average when the deep belief network is employed, whereas the spiking neural network requires significantly less computational complexity by 34.31% to label the modulation scheme compared to the other platforms. Moreover, the analysis of employing framework exhibits higher efficiency versus employing an individual FB AMC classifier.

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To my mother, Jinus.

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|--|
|--|

List of Acronyms

| AMC | Automatic modulation classification |
|------|-------------------------------------|
| IMD | Intelligent modem design |
| DSA | Dynamic spectrum access |
| SC | Spectrum congestion |
| EW | Electronic warfare |
| ES | Electronic support |
| EA | Electronic attack |
| EP | Electronic protect |
| LB | Likelihood-based |
| PDF | Probability density function |
| ML | Maximum likelihood |
| ALRT | Average likelihood ratio test |
| GLRT | Generalized likelihood ratio test |
| SNR | Signal-to-noise ratio |
| HLRT | Hybrid likelihood ratio test |

| DLRT | Discrete likelihood ratio test |
|------------------------------------|--|
| MDLF | Minimum distance likelihood function |
| NPLF | Non-parametric likelihood function |
| DT | Distribution test-based |
| GoF | Goodness of fit |
| KS | Kolmogorov-Smirnov |
| CDF | Cumulative distribution function |
| OKS | One-sample Kolmogorov–Smirnov |
| TKS | Two-sample Kolmogorov–Smirnov |
| CVM | Cramer–Von Mises |
| | |
| AD | Anderson–Darling |
| AD FB | Anderson–Darling Feature-based |
| | - |
| FB | Feature-based |
| FB ML | Feature-based Machine learning |
| FB ML SS | Feature-based Machine learning Signal spectral-based |
| FB ML SS PSD | Feature-based Machine learning Signal spectral-based Power spectral density |
| FB ML SS PSD WT | Feature-based Machine learning Signal spectral-based Power spectral density Wavelet transform-based |
| FB ML SS PSD WT HoS | Feature-based Machine learning Signal spectral-based Power spectral density Wavelet transform-based High-order statistics-based |

- **DL** Dictionary learning
- ANN/NN Artificial neural network
- **DNN** Deep neural network
- **CNN** Convolutional neural network
- **RNN** Recurrent neural network
- **ResNN** Residual neural network
- **CR** Cognitive radio
- **SDR** Software defined radio
- **CSI** Channel state information
- **QoS** Quality of service
- **QoE** Quality of experience
- *P_{CC}* Probability of correct classification
- M-ASK M-amplitude shift keying
- **M-PSK** M-phase shift keying
- M-FSK M-frequency shift keying
- M-QAM M-quadrature amplitude modulation
- **CWT** Continuous wavelet transform
- AWGN Additive white Gaussian noise
- LSTM Long short-term memory
- **DBN** Deep belief network

- **RBM** Restricted boltzmann machine
- **SNN** Spiking neural network
- FCN Fully-connected network
- **ADAM** Adaptive moment estimation algorithm
- **SGD** Stochastic gradient descent
- **EPSP** Excitatory postsynaptic potential
- **IPSP** Inhibitory postsynaptic potential
- MLP Multilayer perceptrons
- **ReLU** rectified linear units
- **ODE** Ordinary differential equation
- **IF** Integrate-and-fire
- LIF Leaky-integrateand-fire
- **STDP** Spike-timing-dependent-plasticity
- **GP** Genetic programming

List of Symbols

| Ymax | Normalized and centred maximum instantaneous amplitude value of the intercepted signal's spectral power density |
|--|---|
| σ_{iap} | Non-linear component absolute value's standard deviation of the instantaneous phase |
| σ_{ip} | Non-linear component direct value's standard deviation of the instantaneous phase |
| λ | Evaluation of the spectrum symmetry around the carrier frequency |
| σ_{ias} | Normalized and centered of absolute value of instantaneous amplitude of signal's symbols' standard deviation |
| σ_{if} | Normalized and centered of absolute value of instantaneous frequency's standard deviation |
| σ_{ia} | Normalized and centered instantaneous amplitude's standard deviation |
| <i>K</i> ^{<i>a</i>} ₄₂ | Normalized and centered instantaneous amplitude's Kurtosis |
| K_{42}^{f} | Normalized and centered instantaneous frequency's Kurtosis |
| I | Real part of the received symbol |
| Q | Imaginary part of the received symbol |

| r | Radius of the polar transformed symbol |
|---|---|
| θ | Angle of the polar transformed symbol |
| X | Random variable |
| $E\{X\}$ | Expected value of random variable <i>X</i> |
| <i>x</i> _i | i^{th} sample of random variable X |
| \overline{X} | Mean of random variable <i>X</i> |
| \overline{m}_i | i^{th} partition's mean of X |
| L | Number of a random variable's samples |
| M_n^i | n^{th} order of central moment of i^{th} partition of X |
| $\Delta_{\mathcal{BR}}$ | Mean difference of portions \mathcal{A} and \mathcal{B} of X |
| | |
| l_i | Length of i^{th} partition of X |
| l_i $\sigma(.)$ | Length of <i>i</i> th partition of <i>X</i> Sigmoid function |
| · | |
| $\sigma(.)$ | Sigmoid function |
| σ(.) T | Sigmoid function Time steps in LSTM layer |
| $\sigma(.)$ T W $_{\alpha}$ | Sigmoid function Time steps in LSTM layer Shared time-distributed NN weight matrix |
| σ(.) T Wα ζα | Sigmoid function Time steps in LSTM layer Shared time-distributed NN weight matrix Shared time-distributed NN bias matrix |
| σ(.) $ T $ $ Wα $ $ ζα $ $ αt$ | Sigmoid function Time steps in LSTM layer Shared time-distributed NN weight matrix Shared time-distributed NN bias matrix t th attention weight |
| σ(.) T $ W_{\alpha} $ $ ζ_{\alpha} $ $ α_t $ $ y_t $ | Sigmoid function Time steps in LSTM layer Shared time-distributed NN weight matrix Shared time-distributed NN bias matrix t th attention weight t th output of LSTM layers |

| E | Energy function |
|---------------------------|--|
| V | Vectors of units in visible layers |
| h | Vectors of units in hidden layers |
| Z(.) | Partition function |
| a _i | Visible layers' biases |
| b_i | Hidden layers' biases |
| $\mathcal V$ | Moving average |
| g | Gradient on current mini-batch |
| eta_i | New introduced hyperparameter to ADAM algorithm |
| η | Step size |
| $ ho_i$ | Binary inputs to neurons |
| λ | Predefined learning rate |
| С | Membrane capacitance |
| R | Membrane resistance |
| I(t) | Total input current to the neuron at time <i>t</i> |
| v(t) | Membrane potential |
| $I_{ext}(t)$ | External current |
| S_i | Spike train |
| $\overline{\mathbf{S}}$: | Low-pass filtered versions of spike train |

 $\overline{S_i}$ Low-pass filtered versions of spike train

CHAPTER 1

Introduction

Automatic modulation classification (AMC) refers to a signal processing mechanism through which the intercepted signal's modulation scheme can be classified with minimal information on the signal's configurations. This process is exclusively operated at the receiver side of a communication, as illustrated in Fig 1.1 [1].

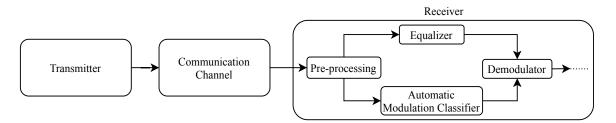


Figure 1.1: Overview of an AMC operation in a communication system.

The modulation scheme's information will then be used in the demodulator for further processing. The term "*automatic*" is used to oppose the initial implementations of fixed modulation classification procedures, where signals are modulated by electronic processors capable of operating one fixed modulation scheme. AMC essentially gained importance when link adjustment methods that use adaptive modulation and coding were introduced. These methods created an adaptive selection of modulation schemes in which a pool of multiple modulation schemes are employed by the system [2]. In this manner, the communication system further enabled an optimization process through which the transmission reliability

and data rate are investigated to lead to the adaptive selection of the modulation scheme according to communication channel conditions. While the transmitter has the freedom to choose the most reliable modulation scheme, the receiver must know the modulation scheme in order to demodulate the received signal so that the transmission can be successful. An easy way to inform the receiver about changes in the modulation scheme at the transmitter is to include the modulation scheme's information in each transmitted signal frame [3]. However, this solution affects the spectrum efficiency due to the extra information that is included in each signal frame. In the current era of wireless communication, where the wireless spectrum is extremely limited and valuable, this solution is not considered to be efficiently sufficient. For this reason, AMC is an attractive solution to the problem of notifying the receiver of the transmitted signal's modulation scheme.

Additionally, AMC also has other applications, which are briefly discussed below.

1.1 AMC Applications

AMC applications can be generally categorized into two groups: civilian applications and military applications.

1.1.1 Civilian AMC Applications

In this category, AMC mainly targets applications for intelligent modem designs (IMDs), spectrum sensing, safety monitoring in open or working areas, interference cancellation, dynamic spectrum access (DSA), link-adjustment to data rate and channel capacity, and signal protection [4]. In general, AMC's primary contribution to these applications can be summarized into three aspects. Below, we highlight these three aspects and describe them in more detail.

• Signal Cancellation:

With the near ubiquitous presence of wireless devices, we face a significant problem

of spectrum congestion (SC). At any given moment, a receiver faces the challenge of observing multiple radio signals, and has to filter out all but the intended transmitter's signal. The intended transmitter's signal may not be of favorable strength or quality, which results in the receiver cancelling out competing signals. One option to determine unfavorable signals is to deploy AMC at the receiver to find the signal's modulation scheme. After the modulation scheme is determined, the receiver then can filter out any signals that do not match the modulation schemes of the targeted transmitter [5].

• Spectrum Surveillance:

By deploying AMC at the receiver and then conducting a sweep of all supported frequencies, the receiver can then easily conduct a survey of mapping modulation schemes used at each particular frequency. This knowledge provides the primary tool to either eavesdrop or jam a signal in the area.

• Removing Overhead in the receiver:

In many communication systems, the transmitter changes the modulation scheme during the connection. This can be caused by any number of reasons, such as adjusting transmission parameters with channel rates. When the transmitter changes the modulation scheme, it typically notifies the receiver by sending information to the receiver. This overhead can be removed by deploying AMC in the receiver.

1.1.2 Military AMC Applications

AMC can assist with three tasks in electronic warfare (EW). These tasks are electronic support (ES), electronic attack (EA), and electronic protect (EP) [6]. The main duty in ES is to collect communication information on the battlefield, especially concerning hostile units. Frequency bands used by hostile units are examples of essential information. These frequency bands can be determined by utilizing AMC in friendly units to monitor modulation schemes and their corresponding frequency bands which are being employed

on the battlefield. This assists friendly units in differentiating among known (friendly) and unknown (hostile) modulation schemes and their frequency bands. As a result, friendly units can obtain two pieces of information from battlefield communications: frequency bands and modulation schemes used by hostile units. In EA, after capturing hostile communication information, jamming these hostile transmissions is a relatively easy task that can be accomplished by transmitting a signal with a higher power in the same frequency band to override the hostile transmission. In EP, if friendly communications are cut off by the same EA mechanism done by hostile units, the friendly frequency bands can be changed to those that are free and safe. The primary means by which these tasks can be accomplished is to gain information on the hostile communications' modulation schemes. Moreover, all the information gathered through this process can be leveraged to eavesdrop on hostile communications.

We will next briefly introduce proposed AMC approaches in literature.

1.2 AMC Approaches

AMC can fundamentally be organized into three primary widely discussed approaches in the literature: likelihood-based, distribution test-based, and feature-based. In the following subsections, we not only introduce these approaches, but also discuss their working principles.

1.2.1 Likelihood-based AMC

In the likelihood-based (LB) approach, it is believed that the probability density function (PDF) of the intercepted signal conditioned over an observed embedded modulated waveform consists of all required information for the modulation classification process. The LB classification process is generally accomplished in three following steps at the receiver:

1. Establishing a likelihood evaluation process in addition to an optimizing process for

threshold determination.

- Performing likelihood evaluation between the calculated pool of modulation schemes' PDF and the observed signal's PDF for each observed received frame while updating the threshold through a predefined optimization process.
- 3. Determining which likelihood evaluation reaches the optimized threshold to make the final decision.

This operation can be seen in Fig 1.2.

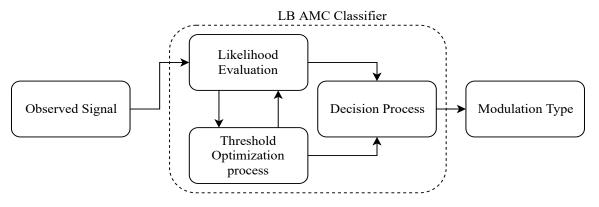


Figure 1.2: LB approach operation structure.

It is evident that all three steps are highly expensive computational processes for the receiver to simultaneously execute along with other processes at receiver such as equalizing. Furthermore, this procedure is also dependent on the channel's parameters since likelihood evaluation is conditioned over them. There is no way to exclude the effects of channel parameters since likelihood evaluation cannot handle any missing parameter. This also creates more computational complexity and requires the receiver to have some knowledge of the channel's parameters as conditional variables of PDF. Having perfect knowledge of channel parameters does not occur in real-world scenarios. Therefore, there is a theoretical classifier that uses a known channel's parameters, in addition to executing all aforementioned steps in a precise manner, called *Maximum likelihood (ML) classifier*. This classifier reaches the highest classification accuracy in comparison with all other classifiers. LB AMC was

then developed to make this approach more practical in real-world scenarios where there is no available information on channel parameters at the receiver, which resulted in proposing three other classifiers in this approach [7]. These classifiers attempt to estimate the channel's parameters along with executing AMC likelihood evaluation. They also ease the above three likelihood evaluation steps by calculating an approximation of likelihood evaluation, and performing a comparison scenario rather than optimizing the decision threshold to determine the intercepted signal's modulation scheme. Hence, the channel parameters' calculation mechanism, in addition to the degree of likelihood evaluation approximation and the comparison process, determines the classification accuracy and computational complexity of these three classifiers. The first of these classifiers is called average likelihood ratio test (ALRT) classifier. This classifier handles the channel's parameters that are unknown to it as random variables with certain PDFs that very well fit with the mathematical definition of the properties of the channel's parameters. Essentially, the most likely value of the channel parameters is computed by considering the integration of all possible values in the likelihood evaluation. The classifier consequently calculates the likelihood evaluation for each observed signal's PDF conditioned on channel parameters, while forming and updating a likelihood ratio test as part of the decision making process. This procedure, which forms the ALRT classifier, produces the highest computational complexity of all other non-theoretical classifiers. It attempts to precisely obtain the channel parameters in addition to the typical procedure of LB AMC, which is to calculate the likelihood evaluation for each observed waveform, and makes decisions based on an updated ratio. Despite this disadvantage, the classifier reaches the highest classification accuracy of all other nontheoretical classifiers. Consequently, ALRT can be called the optimal AMC classifier [8]. In order to ease computational complexity of this classifier, another alternative classifier was proposed called generalized likelihood ratio test (GLRT) classifier. This classifier handles a channel's parameters as unknown deterministics. Hence, in order to estimate the values of the channel's parameters, likelihood evaluation can be done over a specific

range of values, not over all possible values such as in ALRT. This approximation reduces the computational complexity of this classifier in addition to its classification accuracy, especially in lower signal-to-noise ratio (SNR) conditions where it is extremely difficult to determine the aforementioned range for nested modulation schemes. To solve this problem, the hybrid likelihood ratio test (HLRT) classifier was proposed, which is fundamentally built upon the signal carrier phase. Then this classifier acquires the values of the channel's parameters by performing discrete likelihood evaluation. In other words, this classifier finds the most likely values within a few number of candidates. This mechanism of approximation notably reduces computational complexity while slightly overcoming the lower SNR issue with GLRT. On the other hand, it makes the average classification accuracy of HLRT to be lower than both the ALRT and GLRT classifiers. In the sequence of reducing this approach's computational complexity, we can point to a few other classifiers such as discrete likelihood ratio test (DLRT) and look-up table classifier, minimum distance likelihood function (MDLF) classifier and non-parametric likelihood function (NPLF) classifier. These classifiers reduce the LB approach's computational complexity by applying various channel parameters' estimation methods as well as approximation of likelihood evaluation. These classifiers still have high enough computational complexity, which hinders their real-world implementation due to creating delays in further processes at the receiver. It can be concluded that this approach's classifiers obtain the highest classification accuracy on average, and have the highest computational complexity of all other approaches' classifiers due to the mathematical perspective of this approach. Therefore, another mathematical perspective is needed to overcome the computational complexity and cost issues.

1.2.2 Distribution Test-based AMC

The distribution test-based (DT) approach is built upon a mathematical definition called *goodness of fit* (GoF), which in this domain represents the difference of two signals' distributions [9]. Thus, in order to build a classifier upon this definition, the calculated distribution

of the intercepted signal of adequate length, compared with the empirical one of different modulated signals, should be used in the GoF test. The modulation scheme that has the closest empirical distribution to the calculated one from the intercepted signal will be selected as the signal's modulation scheme. This process can be seen in Fig 1.3.

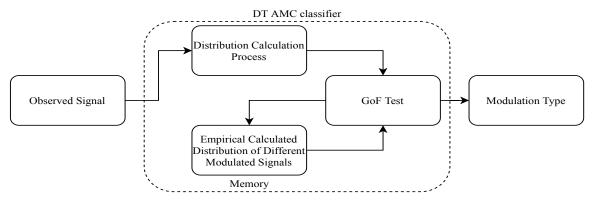


Figure 1.3: DT approach operation structure.

There are many proposed different distribution tests for GoF, but only a few are appropriate for our modulation classification purposes. The first one is the *Kolmogorov–Smirnov (KS) test.* In this test, the cumulative distribution function (CDF) is used for distribution calculations. This test was originally selected for AMC because of its notable lower computational complexity compared to the LB approach. Comparing these two approaches in this test creates two classifiers: the *One-sample KS (OKS) test classifier* and the *Two-sample KS (TKS) test classifier* [10]. These two classifiers have different implementable applications. TKS should be used when the channel is in a harsh condition, which results in the need for precisely reconstructing the CDF of an actual transmitted signal's CDF. In other words, TKS performs higher in lower SNR scenarios, and also has a higher computational complexity than OKS. Two alternatives to the KS test, which have their own comparison mechanisms between empirical CDF and a reconstructed CDF, are called the *Cramer–Von Mises (CVM) test* and the *Anderson–Darling (AD) test*. The difference between these two tests lies in their sensitivity to the changes in the tail of the signal's distributions. The AD test shows less sensitivity than CVM to sudden changes in the tail of the distribution.

less computationally complex than both KS and CVM. Moreover, this also results in lower performance than both KS and CVM classifiers on average [11]. There are other tests that have attempted to do various models of approximation to ease the computational complexity issue to make this approach operational in real-time. In summary, the DT approach performs less accurately than the LB approach on average, especially in lower SNRs, while having less computational complexity as well. But this approach's performance highly depends on the surroundings where transceivers are deployed, because that determines the SNR condition. Additionally, the computational complexity of the DT approach can vary based on the selected test for the mechanism of GoF. Therefore, this approach cannot provide a global solution for AMC.

1.2.3 Feature-based AMC

The feature-based (FB) approach gained importance when machine learning (ML) algorithms became popular in classification applications. Machine learning algorithms are important in real-world applications when there are no patterns of changes in the data structures. This perspective can well connect with the disorderly changes caused by channel parameters over transmitted signals [12]. Thus, machine learning algorithms can assist with assessing and analyzing these negative effects and eventually lead to modulation classification. This approach involves two stages. In the first stage, an instantaneous signal's feature is extracted and then used in the second stage, which is also called labeling stage. The features that are utilized in the first stage relate mostly to a signal's characteristics. They can be categorized as follows:

- Signal spectral-based (SS) features, which also include:
 - The normalized and centered maximum instantaneous amplitude values of the intercepted signal's power spectral density (PSD) (γ_{max})
 - The non-linear component absolute value's standard deviation of the instanta-

neous phase (σ_{iap})

- The non-linear component direct value's standard deviation of the instantaneous phase (σ_{ip})
- Evaluation of the spectrum symmetry around the carrier frequency (λ)
- The normalized and centered absolute values of the instantaneous amplitude of the standard deviations of a signal's symbols.(σ_{ias})
- The normalized and centered absolute values of instantaneous frequency's standard deviations (σ_{if})
- The normalized and centered instantaneous amplitude's standard deviations (σ_{ia})
- The normalized and centered instantaneous amplitude's Kurtosis (K_{42}^a)
- The normalized and centered instantaneous frequency's Kurtosis (K_{42}^f)
- Wavelet transform-based (WT) features
- High-order statistics-based (HoS) features, which include:
 - Moment-based features
 - Cumulant-based features
- Cyclostationary analysis-based (CA) features

In the second stage, machine learning algorithms execute the labeling procedure [13]. Machine learning algorithms that have been utilized in literature are:

- K-nearest neighbor (KNN)
- Genetic programming (GP)
- Support vector machine (SVM)
- Dictionary learning (DL)

- Artificial neural network (ANN/NN), which also includes:
 - Deep neural network (DNN)
 - Convolutional neural network (CNN)
 - Recurrent neural network (RNN)
 - Residual neural network (ResNN)

An overview of this approach can be seen in Fig 1.4.

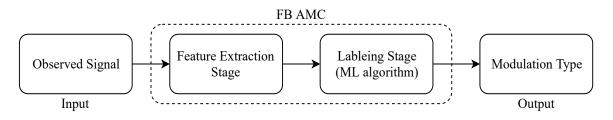


Figure 1.4: FB AMC overview structure.

As it can easily be observed, a combination of various feature extraction techniques and labeling procedures can create different AMC classification mechanisms with different levels of computational complexity and classification accuracy. One important factor in the computational complexity and cost of ML algorithms is the environment where the AMC classifier is intended to be deployed. The impact of this parameter and other elements will be further investigated in detail in Chapter 3 and 4. It can be concluded that this approach can be targeted for more real-world applications of AMC while its computational complexity and classification accuracy are related to the environment, feature extraction techniques and the labeling stage (ML algorithm) that form the FB AMC classifier; which are mostly under control of the AMC classifier designer.

1.3 AMC Implementation

The implementation of AMC was widely regarded as an impossible task before the introduction of cognitive radio (CR) and software-defined radio (SDR) technologies. Historically, transceiver designs were very limited in the number of modulation schemes they could implement for transmission and reception for a variety of reasons, including hardware component and size limits, computation limitations, energy considerations, band limits, and more. Even today, with all the developments in modern technologies, it is still not possible to have a transmitter modulate a signal with all available types of modulation schemes. It only became feasible with the advent of CR and SDR [14]. CR transmitters are capable of sensing their environments and changing transmission parameters based on the obtained results from the environment. One of these parameters could be the employed signal's modulation scheme. SDR technology, on the other hand, enables transceivers to avoid being locked into fixed functionality sets. On the other hand, it makes the transmitter capable of employing virtually any type of modulation schemes simply through software upgrades. This entire process can be seen in Fig 1.5.

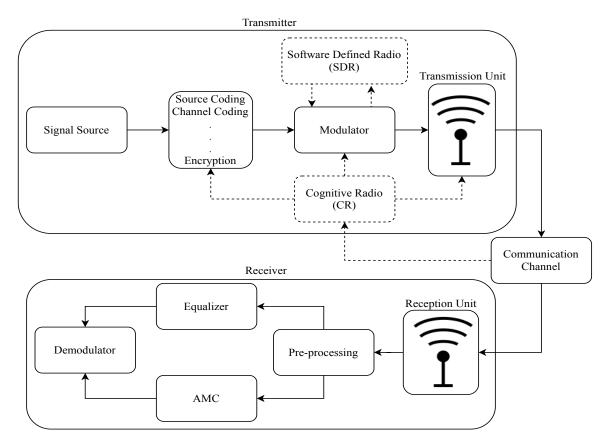


Figure 1.5: Required components in transmitter to necessitate inclusion of AMC in the receiver.

But CR and SDR only help in providing the necessary functionality for AMC. It does not mandate inclusion of AMC, as AMC inherently suffers from high computational complexity. This problem stems from the need for multi-dimensional computations to extract features and estimate a channel's unknown parameters, such as the signal and carrier frequency offset, signal and carrier phase offset, channel state information (CSI), and so on. And yet, the expectation is that AMC needs to operate in real-time with minimal latency. Once the signal is received and sampled, it is expected to immediately go through demodulating and decoding processes. Hence, AMC information is also needed virtually immediately in order to control the demodulation process. Latency stemming from computational complexity can cause delays in this process. Therefore, the continued presence of the excessive computational complexity prevents AMC from being employed in current transceiver systems [15]. However, the reduction in computational complexity through the use of low complex algorithms results in a significant degradation in classification accuracy. As a result, there is a trade-off between computational complexity and classification accuracy. Depending on which application AMC is being deployed, this trade-off needs to be resolved either in favor of lower latency or higher classification accuracy. It should be noted that for most military applications that consider AMC, real-time low-latency operation is vital. On the other hand, for civilian applications, a somewhat higher latency may still be acceptable, as long as it does not negatively impact either quality of service (QoS) or Quality of Experience (QoE). In order to further investigate AMC implementation, related works will be discussed and analyzed in this thesis.

1.4 Summary of AMC Approaches

After providing an introduction and background of different AMC approaches and reviewing various aspects of AMC, we can conclude that the theoretical aspects of AMC have reached a point that it can classify the intercepted signal's modulation scheme with the highest

potential probability of correct classification (P_{CC}) at a given SNR condition with the LB AMC approach. Even though the DT approach reduces the computational complexity of the LB approach, its performance is notably degraded in lower SNR conditions. The proportional degradation in classification accuracy over reduction of computational complexity is not considered efficient compared to what the FB approach can offer. On the other hand, in feature-based AMC, there is still research that needs to be done to improve its classification accuracy performance as well as decreasing its corresponding computational complexity to make it an efficient and flexible real-world implementable approach.

1.5 Thesis Organization

The rest of the thesis is organized as follows. Chapter 2 presents the problem statement of this thesis specially concerning FB AMC appraoch. Chapter 3 provides a literature review of prominent works in this domain. Chapter 4 presents the proposed solutions to the problem statement, which their corresponding findings finally form the novel framework. Chapter 5 presents the numerical results, analysis and discussion of the proposed solutions and the novel framework. And finally, Chapter 6 concludes the thesis.

CHAPTER 2

Problem Statement

In this thesis, we deeply focus on addressing the problem of increasing the classification accuracy for high-order modulation schemes in harsh channel conditions (low SNR values). Moreover, the computational complexity of the AMC architecture is also taken into consideration in order to make the AMC classifier operate simultaneously alongside other components in the receiver. Reducing computational complexity should be accomplished while not sacrificing classification accuracy as much as computational complexity is decreased. We focus on featuring the AMC classifier with flexibility, where it can freely switch between various architectures to obtain an efficient balance between computational complexity and classification accuracy in different environments.

To accomplish the above objectives, we select feature-based automatic modulation classification as the potential real-world implementable approach with advancements in computational power of next communication systems, especially the receiver. The proposed next generation of communication systems that involve machine learning algorithms for different tasks make this approach even more promising. In addition to these advantages, the feature-based approach also provides the following properties when designing the AMC classifier:

1. A combination of various methods in both stages of the FB AMC classifier that can create myriad methods with different levels of computational complexity and classification accuracy can help the designer easily deal with particular applications, which require certain computational complexity and classification accuracy.

- 2. The designer has control over the FB AMC classifier's computational complexity and classification accuracy by deigning a complex or non-complex architecture.
- 3. The FB AMC approach provides flexibility for various applications in different environments since computational complexity and classification accuracy of this approach can be designed by application's requirements and environment's condition.

As mentioned in the previous chapter, this approach consists of two stages. Each stage suffers from a number of problems that can eventually affect the performance of the FB AMC classifier. We investigate each stage's issues below.

2.1 Feature Extraction Stage

There are several methods that can be utilized to extract the intercepted signal's features. All of these methods have their own advantages and disadvantages, although they represent some information about a signal's modulation scheme. Our goal is to investigate which one is capable of providing more correlative in-depth information to finally help address our problem statement of increasing classification accuracy of high-order modulation schemes with low SNR values.

• Signal Spectral-based Features: Spectral-based features provide frequency-domain metrics on the intercepted signal. These metrics can target various aspects of the frequency domain of the intercepted signal. These aspects can include functions that use the zeroth and first power of the intercepted signal's samples, i.e., spectral power, absolute or direct instantaneous phase, absolute or normalized or centered instantaneous amplitude, normalized or centered instantaneous carrier frequency. The functions that use the second order of the intercepted signal's samples can include

features such as the normalized or centered amplitude's and frequency's Kurtosis. These features provide generic information about changes in density of the modulation parameters such as amplitude and phase density.

- Advantages: These features can be used to generally group the intercepted signal's modulation scheme into one of the M-amplitude shift keying (M-ASK), M-phase shift keying (M-PSK), M-frequency shift keying (M-FSK), or M-quadrature amplitude modulation (M-QAM) groups without specifying the order of modulation scheme (M). These features are also resilient against destructive environmental effects over transmitted signals. When this feature extraction technique is used, a simple tree classification can be sufficient for executing the labeling procedure. Hence, if no detailed information of the intercepted signal's modulation scheme is of interest, then this technique is considered to possess efficient computational complexity as well. The simplicity of this method, in addition to its labeling stage, can be seen in Fig 2.1.

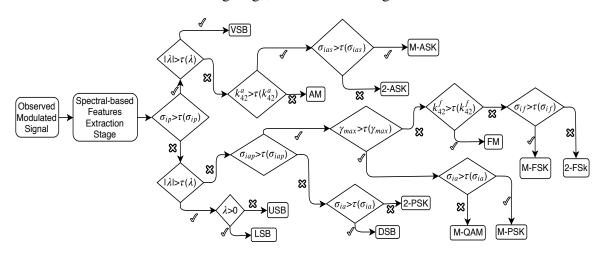


Figure 2.1: Spectral-based features tree classification procedure.

- Disadvantages: These features do not provide any in-depth information about determining the order of the intercepted signal's modulation scheme. Hence, they cannot be used to extract features from the intercepted signal when the environment is characterized with a high SNR value since in such environments, high-order modulation schemes are deployed to transmit and receive more data. This problem is intensified nowadays when the communication protocols tend to increase the bandwidth of transmitted and received data.

- Wavelet Transform-based Features: These features form series that represent a square-integrable (real- or complex-valued) function by a certain orthonormal series generated by a wavelet. In other words, functions that use the third power of the intercepted signal's samples can form such features. In literature, three mother wavelet functions, namely Morlet, Haar and Shannon, are involved in calculating the continuous wavelet transform (CWT) to extract the intercepted signal's features.
 - Advantages: Each mother wavelet function is capable of providing a different level of correlation between received signal's symbols. This provides more in-depth information regarding symbols' patterns that can finally enable the labeling stage to also classify low-order modulation schemes in addition to the aforementioned general groups.
 - Disadvantages: Deploying the mother wavelet function, which provides more correlative information about received signal's symbols, can increase the computational complexity. This is because it requires computationally expensive procedures to extract the features and longer waveforms to enable feature extraction stage to form these relations. On the other hand, the classification accuracy of higher-order modulation schemes does not satisfactorily increase compared to the increase in computational complexity.
- Cyclostationary Analysis-based Features: These features represent statistical properties of the received signal that vary cyclically with time. In literature, there are two ways to treat these features: probabilistic approaches and deterministic approaches. A deterministic approach views the measurements of the intercepted signal as a single time series, from which a probability distribution for a sample associated with the

time series can be defined as the fraction of time. This entire process occurs over the samples' lifetime of the time series. In both approaches, the process or time series is considered to be cyclostationary if and only if its associated probability distributions vary periodically with time.

- Advantages: As this method measures the intercepted signal samples over time, it can provide precise information about amplitude and phase changes happening in signal over time if the sampling rate adheres to the Nyquist rate. Hence, enough in-depth information can be obtained from this method to enable the FB AMC classifier to also classify higher modulation schemes as well as lower-order ones.
- Disadvantages: This method's principal working element is time, and it also needs multiple waveforms to extract enough in-depth features of the intercepted signal. Hence, this method cannot operate in real time alongside other components in the receiver because the extracted features are also used in the labeling stage for training and classifying. Moreover, literature shows that as environmental conditions become harsh, this method significantly loses its precision in extracting features.
- **Higher-order Statistics-based Features:** Higher-order statistics-based features, which are also known as statistics moments, refer to utilizing functions with a third or higher power of the intercepted signal's sample. Whereas, conventional methods utilize low powers such as constant, linear and quadratic terms in their calculations. These calculations involve with zeroth, first and second powers, respectively. HoS features are used in estimation of shape parameters, which indicate the changing behavior of a sample.
 - Advantages: Estimating the properties of shape parameters can not only reveal the disorderly changes in a signal's symbols, but also provide enough in-depth

information on the correlation between the received signal's symbols. This can easily enable the labeling stage to achieve higher classification accuracy on higher-order modulation schemes. Moreover, these features follow a simple recursive mathematical procedure that does not impose any expensive computational complexity on the entire operation of the FB AMC classifier. Additionally, these features have a special property. That is, if the received signal is degraded by noise, which follows the additive white Gaussian noise (AWGN) distribution, calculating these features with any order greater than 2 will automatically result in cancelling out the effects of the AWGN noise in output. Hence, no matter how harsh the environment becomes, this method can compensate for AWGN degradation. This is one the reasons why they are widely used for AMC purposes.

Disadvantage) The estimator function of a signal's moments is proven to be biased. In other words, the extracted features by a signal's moment estimator is not accurate. That's because the true value of the features being estimated is different than the estimator's expected value. Further, this provides an inaccurate or mirage correlation among received symbols. As the order of modulation scheme increases, this inaccuracy intensifies due to a decrease in spatial distance among symbols in the signal's constellation. We also should take into consideration the environmental effect on the received signal's constellation. It is clear that as the environmental conditions become harsh, the received signal's constellation's shape becomes even more disorderly, which makes the AMC task more difficult.

Among feature extraction methods, HoS features exhibit higher effectiveness in providing more in-depth correlative information about the received signal's constellation. Hence, HoS features are considered effective enough for implementation in the feature extraction stage. Although, HoS features hold many advantages, they provide inaccurate quantitative features in the labelling stage as the environmental conditions become more harsh, or the order of the modulation scheme increases. To improve the performance of the FB AMC classifier in lower SNR conditions when high-order modulation schemes are classified, we should address the bias issue of the HoS method's estimator function in the feature extraction stage. We next explore the classification stage problem statement.

2.2 Classification Stage

As mentioned in the introduction, machine learning algorithms execute classification procedures in the labeling stage of FB AMC classifiers. Each machine learning algorithm has various factors measuring its performance. Two of these factors that are critical in the AMC domain are classification accuracy and computational complexity. These two factors affect a FB AMC classifier's performance based on the provided features of the received signal. We next investigate the problem statement for each of these factors.

2.2.1 Classification Accuracy

Classification accuracy measures the precision of a machine learning algorithm in the classification of an intercepted signal's modulation scheme. In other words, to specifically explain this factor in the AMC domain, it corresponds to a fraction whose numerator is the number of waveforms with correctly classified modulation schemes, and its denominator represents all analyzed waveforms.

The environment in which the FB AMC classifier is deployed is one of the major elements that can affect the FB AMC classifier's classification accuracy. As environmental conditions degrade in terms of scattering elements, e.g., densely developed urban environments representing a multipath propagation case, it is more difficult for an AMC classifier to classify the intercepted signal's modulation scheme with a high degree of accuracy. This mostly happens to nested modulation schemes with higher orders such as 128-QAM and 256-QAM. Therefore, there should be a mechanism that can resolve this issue in lower SNR values. This finds its application in situations where classification accuracy is of crucial importance, such as military applications.

2.2.2 Computational complexity

A machine learning algorithm's computational complexity refers to the required time for executing training, validation, and classification steps. Among these steps, training requires the longest time, since it needs to find hidden patterns in data changes. A classification step, on the other hand, can be done in a short amount of time. There are two methods to measure computational complexity of a machine learning algorithm.

- 1. Theoretically, where it involves the process of Big O notation to describe the limiting behavior of a machine learning algorithm when its running time tends towards a particular value or infinity in the defined space of an experiment.
- 2. Experimentally, where the specifications of a platform in which the machine learning algorithm runs are given, and then the required time to do training, validation, and classification are normalized based on the platform's timing unit.

These methods are of importance in the AMC domain because we need to simulate the theoretical performance of the FB AMC classifier while considering its real-world implementation. Implementing a real-time FB AMC classifier in receivers has been historically considered to be an impossible task, since it inherently suffers from high computational complexity. This problem stems from the need for multi-dimensional computations to estimate unknown pattern changes in the intercepted signal to finally extract information of sufficient fidelity regarding the signal's modulation scheme. However, FB AMC must operate in real time while imposing minimal latency on other receiver components. Hence, FB AMC information is needed virtually immediately in order to control the demodulation process. Latency stemming from computational complexity can cause delays in this process.

Therefore, the continued presence of this excessive computational complexity prevents AMC from being implemented in most current receivers.

In a very concise comparison between the computational complexity of these steps and the feature extraction stage, we can easily observe that the computational complexity of the labeling stage is much higher than the feature extraction stage. Hence, we mainly focus on reducing the labelling stage's computational complexity to provide for the possibility that the FB AMC classifier can operate real time. However, when employing low computational complexity algorithms to achieve a reduction in computational complexity, the achievable results show a significant degradation in classification accuracy. As a result, there is a trade-off between computational complexity and classification accuracy. Depending on which application FB AMC is being utilized for, this trade-off needs to be resolved either in favor of lower latency or higher classification accuracy. For most military applications that consider AMC deployment, real-time operation is vital. On the other hand, for civilian applications, a somewhat higher latency may still be acceptable as long as it does not negatively impact quality of service and experience.

CHAPTER 3

Literature Review

In this chapter, we briefly investigate some of the prominent works in the FB AMC domain to see how they have attempted to address the aforementioned problems.

Yu and *Miao* in [16] proposed a deep learning-based method combining two CNNs with different structures trained on different datasets with their samples composed of inphase and quadrature component signals, otherwise known as in-phase and quadrature samples, to distinguish modulation modes. They also adopted a dropout instead of a pooling operation. Their entire system design is based on constellation diagrams for 16QAM and 64QAM modulation schemes. Combining two machine learning platforms with different learning structures creates a powerful FB AMC classifier capable of learning more hidden patterns of the received signal's constellation shape when, in particular, the focus is on classifying M-QAM modulation schemes. This easily increases the classification accuracy for constellation-based modulation schemes, their FB AMC classifier is not capable of classifying M-FSK and M-PSK modulation groups as well as M-QAM. Moreover, combining two NN platforms notably increases computational complexity. This makes their FB AMC classifier difficult to implement in the real world.

Fan and *Peng* in [17] proposed a CNN-based deep learning structure where the labeling stage is trained in two steps. After the first training step is done, the learned characteristics

are transferred to the second step of training. Through this two-step training structure, not only are features from the long symbol-rate observation sequence extracted, but the environmental condition is also estimated. Their classifier can also dimensionally accommodate varying inputs. Two-step training can increase the robustness of the labeling stage in the presence of carrier phase offset under most environmental conditions. This can also provide independence for the FB AMC classifier form receiver's main equalizer in providing the SNR value. Moreover, their deep learning structure is flexible over the input data's dimension, which makes the FB AMC classifier capable of operating on different waveform lengths. Two-step training significantly increase the computational complexity of the labeling stage, which makes the FB AMC classifier incapable of operating the AMC task real-time. Additionally, having a CNN-based platform does not create a robust FB AMC classifier for the M-FSK and M-PSK groups of modulation schemes.

Chieh-Fang and *Ching-chun* in [18] proposed a CNN-based deep learning platform in which a mechanism to estimate channel state information is created. In such a mechanism, the FB AMC classifier is enabled to compensate for the destructive channel's effect on the received signal. CNN-based platform dimensions were increased to a two-dimensional platform, which is capable of being trained not only over I - Q, but also over $r - \theta$ samples. It is obvious that equalizing the channel's effect over signal, and reconstructing the estimated transmitted signal, will significantly increase classification accuracy. Additionally, providing extra information ($r - \theta$ samples) to the labeling stage will lead to a more accurate training process of the CNN-based platform, which can eventually increase the classification accuracy. Having the mechanism to estimate channel state information is inherently a computationally expensive task since it requires multiple iterations to obtain channel parameters. Hence, adding such mechanism to a deep learning platform will result in a significant increase in computational complexity of a proposed FB AMC classifier. Moreover, providing another dataset to the deep learning structure in order to increase classification accuracy will result in increasing the computational complexity of the training stage.

Zhe and Yong in [19] proposed a novel pre-processing stage that eliminates the effect of a multipath channel coefficient over the intercepted signal. They utilized an estimation mechanism to achieve channel state information parameters. They furthermore utilized a logarithmic functional fitting method to classify received modulated signals. Their proposed FB AMC classifier increases the classification accuracy of low-order modulation schemes under harsh environmental conditions. Utilizing the logarithmic functional fitting method can decrease the computational complexity of the labeling stage due to its simple classification mechanism. The authors attempted to compensate for the increase in computational complexity of their proposed FB AMC classifier due to utilizing the channel state information estimation method by selecting a simple labeling mechanism. Adding another stage such as pre-processing to a typical FB AMC classifier's components will increase its total computational complexity, which hinders its practical implementation. Moreover, estimating channel state information when receiving a high-order modulated signal is a very computationally expensive task, since it requires several iterations of the modulated signal's waveforms. Deploying a simple mechanism in the labeling stage can decrease the accuracy of detecting hidden patterns in data, which can finally result in lower classification accuracy for high-order modulation schemes.

Shengliang and *Hanyu* in [20] mainly focused on decreasing the labeling stage's computational complexity. To accomplish this, they employed two CNN platforms built by Google called AlexNet and GoogLeNet, which are capable of parallel computation over various partitioned data. It is obvious that parallel computation, especially in the training stage, will significantly decrease the required time to execute each step of the labeling stage. This idea can be leveraged for real-world implementation where faster classification of an intercepted signal's modulation scheme is of importance. Partitioning the data, received samples of an intercepted signal, can result in losing the correlation between partitioned data considering the fact that each partitioned data will separately be processed by the ML platforms. This can finally lead to a less accurate training process of the ML algorithm that can negatively impact classification accuracy, especially with high-order modulation schemes. Additionally, since AlexNet and GoogLeNet are CNN-based, they are not capable of exhibiting high performance when M-FSK and M-PSK modulation schemes groups participate in classification.

Sudhan and Rahul in [21] proposed a new architecture of a feature extraction stage that combines two feature extraction methods, namely elementary cumulants and cyclic cumulants. This method can easily detect if the intercepted signal's modulation scheme is within a real, circular or rectangular class (group of the modulation scheme). Moreover, they used cyclic cumulants that describe positions of non-zero cyclic frequencies to classify the order of the modulation scheme. Utilizing two feature extraction methods in the feature extraction stage can not only provide more in-depth information to the labeling stage, leading to a more accurate training process, but also can enable the FB AMC classifier to blindly make a final decision without knowing the channel state information. Utilizing non-zero cyclic frequency features can be beneficial in increasing the classification accuracy of M-FSK modulation schemes. Having two feature extraction methods increases the computational complexity of the FB AMC classifier. Although more in-depth information is provided to the labeling stage by extracting two different features from the intercepted signal, their proposed classifier can robustly classify the general group of modulation schemes in addition to low-order ones. In order for high-order modulation schemes to be robustly classified, more correlative information that cannot be provided by elementary cumulants and cyclic cumulants is needed.

Sreeraj and *Wannes* in [22] attempted to enhance the training process of the labeling stage by adding a long short-term memory (LSTM) layer to conventional deep learning structures. In the training process, LSTM layers are characterized by executing several iterations over the data to lead the LSTM layer to memorize the features of the intercepted signal. This property will become useful later to balance the links weights of NNs. Memorizing extracted features of intercepted signal and helping to balance the links weights of NN will result in increasing classification accuracy regardless of the group of an intercepted signal's modulation scheme. Utilizing the LSTM layer also provides more robustness to the classification process in various environments. All these advantages together can make this FB AMC classifier more suitable for those applications where classification accuracy is of crucial importance. LSTM layers are considered computationally expensive due to several iterations performed to memorize features. Therefore, the FB AMC classifier in which LSTM layers are utilized is not recommended for selection for real-time practical applications.

Yahia and *Octavia* in [23] conducted an experiment to classify phase shift-keying modulated signals based on the graph representation of the Fourier transform of the second and fourth powers of these signals. This experiment shows the capability of classifying low-order of phase shift-keying signals with high accuracy. For high-order of phase shift-keying signals, the experiment is not as successful as for low-order signal classification. Graph representation of the Fourier transform of the second and fourth powers of the intercepted signal does not provide in-depth enough information for high-order modulation schemes to be robustly classified.

Muhammad and *Zhechen* in [24] proposed a FB AMC classifier where this classifier combines genetic programming and K-nearest neighbor in labeling stage. In this work, K-nearest neighbor has been used to evaluate the fitness of GP individuals during the training step. Additionally, in the testing step, K-nearest neighbor has been used for deducing the classification performance of the best individual produced by GP. The classification step has been divided into two phases for improving the classification accuracy. In feature extraction stage, cumulants have been user as input feature for GP. They tested their classifier's performance with four modulation schemes: BPSK, QPSK, 16QAM and 64QAM. Utilizing two machine learning algorithms in labeling stage can increase the classification accuracy. This increase in classification accuracy is built upon the fact that K-nearest neighbor oversees the performance of GP to deduce the classification performance of the best individual

produced by GP. This feedback operation helps classifier to more deeply find hidden patterns in symbol changes. On the other hand, this entire procedure is highly computationally expensive because the feedback operation in this classifier is built on top of K-nearest neighbor algorithm, which itself is based on several nested loops. Hence, although the classification accuracy is increased, computational complexity of this classifier is considered to be much higher than other ones on this domain.

Lei and Hong in [25] proposed a classifier where it uses a distributed AMC scheme based on compressive sensing by taking advantage of the sparse property of cyclic feature mapping. Thus, they introduced a novel method based on compressive sensing principle for capturing the prominent peaks of the feature mapping. This method is capable to acceptably perform AMC task at sub-Nyquit rate of sampling. Additionally, they proposed a novel neural network fusion strategy for better cooperation with compressive sensing principle. Using a classifier that can operate at sub-Nyquit rate can be extremely helpful for situations where there is no knowledge of transmitted signal such as in battlefields. Moreover, since a compressive sensing method is used, the training step of neural network in labeling stage is considered to be accomplished in shorter time, which implies the decrease in computational complexity. This work has shown that their classifier strongly performs with low-order modulation schemes. On the other hand, using a compressive sensing method in addition to operating at sub-Nyquist sampling rate can decrease the probability of correct classification for higher-order modulation schemes.

Octavia and *Ali* in [26] proposed a classifier where it employs higher-order cyclic cumulants to discriminate linear or low-order digital modulation schemes under various channel conditions. In order to more deeply investigate the performance of this classifier, they not only test its performance in single-antenna mode, but they also consider a multiple-antenna case to assess the effect of spatial diversity. Additionally, they derived analytical closed-form expressions for the cyclic cumulant polyspectra of linearly digitally modulated signals affected by fading, carrier frequency and timing offsets, and additive Gaussian noise.

Their proposed classifier significantly increase the classification accuracy for low-order modulation schemes especially in multiple-antenna scenario due to taking the advantage of spatial diversity to eliminate the fading effect over received signal. On the other hand, their classifier is also capable to address the problem of increasing the classification accuracy for high-order modulation schemes in low SNR conditions while its computational complexity is notably increases. This increase is due to the fact that higher-order cyclic cumulants requires several waveforms to be able to establish the relationships between received signal's moment and cumulants. It also should be noted that the increase in computational complexity is much more than the increase in average classification accuracy for higher-order modulation schemes.

After reviewing the literature, we can conclude:

- 1. No study, to the best of our knowledge, has considered the impact of the estimator's bias in the feature extraction stage when a signal's moment is to be extracted.
- Literature contributions that aim to increase classification accuracy have thus far not achieved acceptable performance at lower SNR values for high-order modulation schemes.
- Computational complexity of deep learning architecture in the labeling stage has not been effectively reduced up to a point of operating real-time.
- 4. Thus, to date, no efficient and adaptive framework has been presented in literature to provide flexibility in controlling computational complexity and classification accuracy.

The problems statement and our findings from reviewing the scientific literature on the topic of AMC have led us to conduct research that aims to address these challenges. Our contributions and the resulting novel framework structure are presented in the next chapter.

CHAPTER 4

Proposed Solution

This thesis aims to address the aforementioned prominent problem statements in both stages of the FB AMC classifier. Providing an overview of contributions in below can strongly help the reader understand our procedure to address these problems.

4.1 Solutions Structure

The following subsections will provide an overview of proposed solutions to solve the stated problems of both forming stages of the FB AMC classifier.

4.1.1 Feature Extraction Stage

Feature extraction stage procedures in literature have not been promising in providing in-depth enough correlative information of received signal to labeling stage, specially for high-order modulation schemes. Therefore, we propose a new architecture for the feature extraction stage. This architecture is comprised of two components. The first component extracts the fourth-order cumulants from the received signal's I - Q symbols. For this process, we also address the problem of biased estimators for fourth-order cumulants for two different cases: when the received signal's symbols are 1) real values, and 2) complex values. The second component extracts polar coordinates $r - \theta$ from the received I - Q symbols

to provide more in-depth information to the labeling stage of a signal's constellation. This solution will be explored in detail in this chapter in section 4.2.

4.1.2 Labeling Stage

Contrary to other efforts in the literature that aim to modify conventional machine learning algorithms or deep learning structures that were proposed for AMC, we instead introduce the idea of using two entirely different machine learning algorithms in a deep learning structure for AMC. These algorithms will specifically address the stated problems traditionally associated with this stage that can be generally categorized as classification accuracy and computational complexity.

4.1.2.1 Classification Accuracy

We introduce a deep belief network (DBN) platform to be utilized in AMC for the first time, to the best of our knowledge. There are two motivations to employ DBN in AMC that can eventually improve the performance of the FB AMC classifier under low SNR conditions.

- 1. In any ANN platform, there is a problem called vanishing gradient that spreads throughout the network and imbalances the link weights as the training cycles are executed. This results in an inaccurate training process, and furthermore increases the misclassification error. The proposed solution is to use a gradient-based learning method combined with back-propagation. This solution involves a Restricted Boltzmann Machine (RBM) which automatically finds hidden patterns in the data by reconstructing the input. This property enables DBN to not only be trained like conventional NNs, but to tag the important portion of data with higher probability. A DBN is created by stacking RBM layers. Hence, vanishing gradients are removed in DBNs. This leads to a more accurate training process of DBN.
- 2. A DBN benefits from reconstructing the input in a back-propagation loop. This

finally results in a high capability of learning how to probabilistically reconstruct the input. This allows DBNs to recognize the influential portion of the input with high probability. Then by focusing the training process onto this portion of the input it can be more accurately trained.

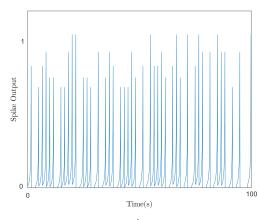
These two properties allow a DBN to be capable of finding deeper hidden patterns in the input data while removing the vanishing gradient problem. Hence, this platform exhibits superior capabilities in classifying high-order modulation schemes in lower SNR conditions. This solution will be explored in detail in this chapter in section 4.4.

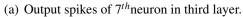
4.1.2.2 Computational Complexity

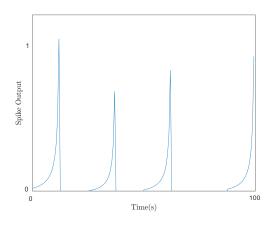
We also introduce the use of a spiking neural network (SNN) platform for AMC. Spiking neural networks are a close mathematical approximation of natural neurons' operations. In their operations, not only the neuron's state are applied, but time is also incorporated into the synaptic property of the neurons. This leads to the main motivation to introduce the use of this type of neural network platform in AMC: Neurons in SNNs fire only when they have reached a specific value by accumulating the spikes' values from neurons in former layer. This results in two important SNNs' characteristics.

- All neurons forming a layer do not participate in classification operation. This is a direct consequence of SNN's property where not all neurons fire at each propagation cycle, but rather fire only when a membrane potential – an intrinsic quality of the neuron related to its membrane electrical charge – reaches a specific value. This eliminates notable required computations in each layer. Therefore, in layer-wise comparison with other platforms introduced in AMC, SNNs are characterized by lower computational cost.
- 2. The aforementioned process of neurons not participating in classification and eliminating computations of each layer intensifies as the data moves forward in a network's

layers. In other words, let's assume that the fifth layer in an SNN requires significantly less computations than the third layer in the same network due to the notably lower produced number of spikes in the fifth layer. The computational cost of an SNN corresponds to the neurons' involvement in producing spikes. Therefore, not only is the computational cost decreased layer-wise, but the entire network also requires notably less computational cost. This can be better understood with the intuition provided in Fig 4.1 for the proposed SNN-based model that will be explored in detail in chapter 4.







(b) Output spikes of 12^{th} neuron in fifth layer.

Figure 4.1: Output spikes of neurons in third and fifth for the proposed SNN-based model.

Overall, this platform, by its inherent design, requires less computational cost in all steps

of training, validation and classification. As a result, this FB AMC classifier will have a high likelihood of achieving real-time operation for most AMC applications in classification step. This solution will be explored in detail in this chapter in section 4.5.

4.1.3 The Proposed Novel Framework Structure

We propose an adaptive framework that efficiently switches between the two aforementioned labeling platforms based on each platform's specific characteristics, i.e., computational complexity and classification accuracy. In other words, this framework attempts to automatically adapt between classification accuracy and computational complexity for any derived SNR from the main receiver's equalizer. In this way, this framework can be flexible in implementation in different environments. We describe the principal functionality of this novel framework and investigate it in detail in section 4.6.

4.2 New Feature Extraction Stage Architecture

In this section, we present our design of a new architecture for this stage, which takes in the received signal and extracts from it a stream of feature descriptors that are then used in the labeling stage. This new architecture is comprised of two components that operate in parallel. The output of these components will be appended to the original received signal to create an augmented signal data stream. This architecture can be seen in Fig 4.2.

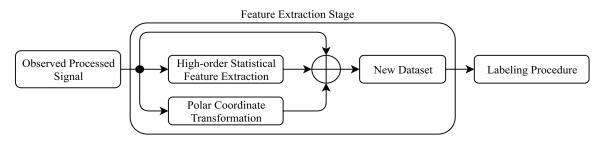


Figure 4.2: Architecture of the new feature extraction stage.

The resulting 3D high-order statistical polar-based dataset is built upon the idea that

the more in-depth correlative information that can be provided to the labeling stage, the more precisely the training and validating steps of labeling procedure will be executed. Consequently, the system will be able to achieve a higher classification accuracy. Adding the polar coordinate transform component does not increase the computational complexity of the feature extraction stage since 1) it does not require any recursive computation compared to the high-order statistical feature extraction component, and 2) the polar coordinate transform component. It should be mentioned that due to the high-order statistical feature extraction component. It should be mentioned that due to the high-order statistical feature extraction's recursive nature, its computational complexity is longer than the polar coordinate transform. These components will be explored in more detail in the next subsections.

4.2.1 High-Order Statistical Feature Extraction Component

High-order statistics refers to applying functions with third-order or higher powers over sample data. Cumulants are one of these functions used in the literature for AMC. The definition of cumulants is simply the formal relation between the coefficients in the Taylor expansion of function M_n with $\overline{m} = 1$, and the coefficients in the Taylor expansion of log M_n . They have beneficial properties such as their symmetric and additive operation over input arguments and their homogeneous behavior over partitions. The most important property of cumulants is that if the input arguments follow a Gaussian distribution, then their cumulants of any order higher than two equate to zero. By taking advantage of this property, the negative effect of noise that is typically observed with Gaussian distributions will be automatically eliminated from the labeling stage. Moreover, these useful properties enable cumulants to estimate shape parameters, which indicate the changing behavior of sample data. This helps significantly in producing enough in-depth correlative information about the high-order modulation schemes. However, the estimator for any order of cumulants greater than two has been proven to be biased [27], which produces inaccurate values that can, in turn, result in the labeling stage producing misclassified results, especially at lower SNRs for high-order modulation schemes such as 128QAM and 256QAM. Therefore, in our framework, we address the problem of removing the bias of fourth-order cumulants for the scenarios when the received signal's symbols are 1) real values for low-order modulation schemes, and 2) complex values for high-order modulation schemes. For a random variable of *X*, M_n is defined as:

$$M_n \triangleq E\{(X - E[X])^n\}$$
(4.1)

For finite and equiprobable samples $x_i \in X$, M_n can be written as:

$$M_n = \frac{1}{L} \sum_{i=1}^{L} (x_i - \overline{m}), \qquad (4.2)$$

where

$$\overline{m} = \frac{1}{L} \sum_{i=1}^{L} x_i \tag{4.3}$$

If we do not consider the estimator's bias issue, referring to the difference between the estimator's expected value and the true value of the parameter being estimated, then Equation (4.6) can provide cumulants of nth order. However, the clear advantage to addressing the bias issue is to provide accurate correlative quantitative features to the labeling stage. The more accurate these quantitative features are, the more accurately the training, validation and classification steps of the labeling stage are executed. Hence, we can accomplish it using two algorithms called *one-pass* and *two-pass* for the case where the received symbols are real-valued.

4.2.1.1 One-Pass Algorithm

Through using the binomial theorem and expanding the term of $(x_i - \overline{m})^n$ to explicit powers of x_i and \overline{m} in binomial theorem, Equation (4.2) can thus be rewritten as:

$$M_n = \sum_{k=0}^n \binom{n}{k} (\frac{1}{L} \sum_{i=1}^L x_i^{n-k}) (-\overline{m})^k$$
(4.4)

This algorithm thus attempts to remove any estimation bias by considering the probability of whether estimation bias has happened.

4.2.1.2 **Two-Pass Algorithm**

As an alternative to the one-pass algorithm's approach, the *two-pass* algorithm attempts to solve this issue statistically, by using the following statistical procedure. It first divides the received signal symbols into two partitions, \mathcal{A} and \mathcal{B} ; where $l_{\mathcal{A}}$ and $l_{\mathcal{B}}$ are respectively the length of partitions \mathcal{A} and \mathcal{B} . Moreover, $\overline{m}_{\mathcal{A}}$ and $\overline{m}_{\mathcal{B}}$ represent the mean of each partition. After that, Equation (4.2) can be rewritten as shown in Equation (4.4) for any order equal or greater than 2. In Equation (4.4), $M_n^{\mathcal{A}}$ and $M_n^{\mathcal{B}}$ are moments of order *n* over each \mathcal{A} and \mathcal{B} portions. $\Delta_{\mathcal{B}\mathcal{A}}$ also equates with $\overline{m}_{\mathcal{B}} - \overline{m}_{\mathcal{A}}$, where each term stands for the mean of their corresponding signal's portion.

$$M_{n} = M_{n}^{\mathcal{A}} + M_{n}^{\mathcal{B}} + l_{\mathcal{A}} \left(\frac{-l_{\mathcal{B}} \Delta_{\mathcal{B}\mathcal{A}}}{L}\right)^{n} + l_{\mathcal{B}} \left(\frac{l_{\mathcal{A}} \Delta_{\mathcal{B}\mathcal{A}}}{L}\right)^{n} + \sum_{k=1}^{n-2} \binom{n}{k} \Delta_{\mathcal{B}\mathcal{A}}^{k} [M_{n-k}^{\mathcal{A}} \left(\frac{-l_{\mathcal{B}}}{L}\right)^{k} + M_{n-k}^{\mathcal{B}} \left(\frac{l_{\mathcal{A}}}{L}\right)^{k}]$$
(4.5)

The *Two-Pass* algorithm removes the estimator's bias more accurately compared to the *One-Pass* algorithm. On the other hand, this algorithm also requires more computational resources. After addressing the discrete moment estimator's bias issue, the cumulants of the

received signal can be recursively calculated from the discrete moment of the signal as:

$$C_n = M_n - \sum_{i=1}^{n-1} \frac{(n-1)!}{(i-1)!(n-i)!} C_i M_{n-i}$$
(4.6)

If the received signal has complex-valued symbols, then joint cumulants of the symbols need to be calculated. This applies to modulated signals with high-order modulation schemes. We derive the fourth-order cumulants over the intercepted signal (X) in Equation (4.7).

$$C_{4}(X) = \frac{L^{2}}{L^{3} - 6L^{2} + 13L - 12} [(L+1)\overline{X^{4}} - 4(L+1)\overline{X^{3}}\,\overline{X} - 3(L-1)\overline{X^{2}}\,\overline{X^{2}} + 12L(\overline{X^{2}}\,\overline{X}\,\overline{X}) - 6L\overline{X}^{4}]$$
(4.7)

The derivation process is presented below.

The generic format of an estimator for nth-order cumulants of a random events vector $X = \{X_1, X_2, \dots, X_n\}$ is defined as:

$$C_n(X_1, X_2, \cdots, X_n) = \frac{\partial^n}{\partial k_1 \cdots \partial k_n} K_X(k)$$
(4.8)

with the following generating function at k = 0.

$$K_X(k) = ln\{E[\exp(k \cdot X)]\}$$
(4.9)

This leads to the biased fourth-order multivariate cumulants estimator in terms of products

of higher order moments.

$$C_{4}(X_{1}, X_{2}, X_{3}, X_{4}) = E[X_{1}X_{2}X_{3}X_{4}] - E[X_{1}X_{2}X_{3}]E[X_{4}] - E[X_{1}X_{2}X_{4}]E[X_{4}] - E[X_{1}X_{3}X_{4}]E[X_{2}]$$

$$- E[X_{2}X_{3}X_{4}]E[X_{1}] - E[X_{1}X_{2}]E[X_{3}X_{4}] - E[X_{1}X_{3}]E[X_{2}X_{4}] - E[X_{1}X_{4}]E[X_{2}X_{3}]$$

$$+ 2\{E[X_{1}X_{2}]E[X_{3}]E[X_{4}] + E[X_{1}X_{3}]E[X_{2}]E[X_{4}] + E[X_{1}X_{4}]E[X_{2}]E[X_{3}]$$

$$+ E[X_{2}X_{3}]E[X_{1}]E[X_{4}] + E[X_{2}X_{4}]E[X_{1}]E[X_{3}] + E[X_{3}X_{4}]E[X_{1}]E[X_{2}]\}$$

$$- 6E[X_{1}]E[X_{2}]E[X_{3}]E[X_{4}]$$
(4.10)

The procedure for obtaining the derivation of the unbiased fourth-order multivariate cumulants is as follows. We can easily observe that $E[\overline{X_1 X_2 X_3 X_4}] = E[X_1 X_2 X_3 X_4]$. Hence, different multiplicity structures of $\{X_1, X_2, X_3, X_4\}$ can be calculated based on the expressions below. Expressions $E[\overline{X_1 X_2 X_4 X_3}]$, $E[\overline{X_1 X_3 X_4 X_2}]$, $E[\overline{X_2 X_3 X_4 X_1}]$ and $E[\overline{X_1 X_2 X_3 X_4}]$ can also be calculated through equation (4.11).

$$E[\overline{X_1 X_2 X_3} \overline{X_4}] = \frac{1}{L^2} \sum_{i,j}^{L} E[X_{1_i} X_{2_i} X_{3_j} X_{4_j}]$$
(4.11)

where i, j are realizations of multiplicities. This leads to:

$$L^{2}E[\overline{X_{1} X_{2} X_{3}} \overline{X_{4}}] = \{L(L-1)E[X_{1} X_{2} X_{3}]E[X_{4}] + LE[X_{1} X_{2} X_{3} X_{4}]\}$$
(4.12)

Expressions $E[\overline{X_1 X_3 X_2 X_4}]$, $E[\overline{X_1 X_4 X_2 X_3}]$, $E[\overline{X_2 X_3 X_1 X_4}]$, $E[\overline{X_2 X_4 X_1 X_3}]$ and $E[\overline{X_3 X_4 X_1 X_2}]$ can also be calculated based on:

$$E[\overline{X_1 X_2} \,\overline{X_3} \,\overline{X_4}] = \frac{1}{L^3} \sum_{i,j,k}^{L} E[X_{1_i} X_{2_i} X_{3_j}, X_{4_k}]$$
(4.13)

that results in:

$$L^{3}E[\overline{X_{1} X_{2}} \overline{X_{3}} \overline{X_{4}}] =$$

$$L(L-1)(L-2)E[X_{1} X_{2}]E[X_{3}]E[X_{4}]$$

$$+L(L-1)\{E[X_{1} X_{2} X_{3}]E[X_{4}] + E[X_{1} X_{2} X_{4}]E[X_{3}]\}$$

$$+L(L-1)E[X_{1} X_{2}]E[X_{3} X_{4}] + LE[X_{1} X_{2} X_{3} X_{4}]$$
(4.14)

Eventually, the expression $E[\overline{X_1} \ \overline{X_2} \ \overline{X_3} \ \overline{X_4}]$ can be calculated as:

$$E[\overline{X_1} \ \overline{X_2} \ \overline{X_3} \ \overline{X_4}] = \frac{1}{L^4} \sum_{i,j,k,l}^{L} E[X_{1_i} X_{2_j}, X_{3_k} X_{4_l}]$$
(4.15)

which can be explicitly stated as:

$$L^{4}E[\overline{X_{1}} \ \overline{X_{2}} \ \overline{X_{3}} \ \overline{X_{4}}] =$$

$$L(L-1)(L-2)(L-3)E[X_{1}]E[X_{2}]E[X_{3}]E[X_{4}]$$

$$+L(L-1)(L-2)\{E[X_{1}X_{2}]E[X_{3}]E[X_{4}] + 5 \ o.p.\}$$

$$+L(L-1)\{E[X_{1}X_{2}X_{3}]E[X_{4}] + 3 \ o.p.\}$$

$$+L(L-1)\{E[X_{1}X_{2}]E[X_{3}X_{4}] + 2 \ o.p.\} + LE[X_{1}X_{2}X_{3}X_{4}]$$
(4.16)

where 'o.p.' means other permutations of the variables in e.g. $E[\overline{X_1X_2}] E[\overline{X_3}] E[\overline{X_4}]$ that give rise to (non-identical) terms like $E[\overline{X_1X_3}] E[\overline{X_2}] E[\overline{X_4}]$. Then, the $C_4(X_1, X_2, X_3, X_4)$ can be derived for equation (4.10) as:

$$C_{4}(X_{1}, X_{2}, X_{3}, X_{4}) = \frac{L^{2}}{L^{3} - 6L^{2} + 13L - 12} \times \{(L+1)\overline{X_{1} X_{2} X_{3} X_{4}} - (L+1)(\overline{X_{1} X_{2} X_{3} \overline{X_{4}}} + 3 o.p.) - (L-1)(\overline{X_{1} X_{2} \overline{X_{3} X_{4}}} + 2 o.p.) + 2L(\overline{X_{1} X_{2} \overline{X_{3} X_{4}}} + 5 o.p.) - 6L\overline{X_{1} \overline{X_{2} \overline{X_{3} X_{4}}}}\}$$
(4.17)

For the special case if $X_1 = X_2 = X_3 = X_4$, we obtain the equation (4.7).

4.2.2 Polar Coordinate Transformation

Mapping I - Q values of the received signal's symbols in I - Q plane to polar coordinates can be easily conducted through establishing the relationship between I - Q and $r - \theta$ values as $\mathbf{r} = \sqrt{\mathbf{I}^2 + \mathbf{Q}^2}$ and $\theta = \arctan(\mathbf{Q}/\mathbf{I})$ where \mathbf{I} and \mathbf{Q} indicate the real and imaginary parts of the received complex symbols, and \mathbf{r} and θ represent the radius and angle of the polar transformed coordinates. As can be seen from the simple mathematical process of polar coordinate transformation, this component does not increase the computational complexity of the feature extraction stage since 1) it does not require any recursive computation compared to the high-order statistical feature extraction component, and 2) the polar coordinate transform component operates in parallel with high-order statistical feature extraction's recursive nature, its computational complexity is longer than the polar coordinate transform. On the other hand, this transformation provides more in-depth information on the symbols' placements within the constellation for the subsequent labeling stage.

4.3 **Proposed Deep Learning Structure for Labeling Stage**

NNs contain hidden layers consisting of some number of neurons. Each single neuron in each middle hidden layer is connected to all neurons in the previous and subsequent hidden layer through links, each with associated weights, which determine the overall value for a neuron's output. There are different functions, also known as activation functions, to calculate the link weights. The selected numbers for hidden layers and neurons, as well as the activation function computing the links' weights, influence the accuracy and computational cost of the FB AMC classifier. If we select more than 2 hidden layers, then the neural network is called a deep neural network. DNN classifiers generally are capable of faster classification

operations and more accurate learning of non-linear patterns than SVM. Although DNN performs on average higher than SVM, its performance is not appreciably higher than that of SVM, especially in lower SNR values. Thus, a recurrent neural network was proposed to be used in AMC to overcome this issue. We will next investigate a specific NN architecture, RNN-LSTM, coupled with DNN that has been recently proposed in AMC applications. A recurrent neural network is an architecture that aims to address the issue of ML algorithms' learning process having to restart from scratch. In practice, this task is done by creating loops over the ML algorithm's learning process to be frequently trained over different portions (*m* number) of a cross-validated training set, as shown in Fig 4.3.

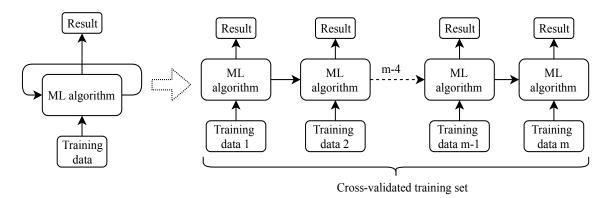


Figure 4.3: RNN training process over m portion of cross-validated training set.

This procedure trains the ML algorithm *m* times which, for an ML algorithm, results in learning and discerning the relationship in a much more accurate manner between various parameters' values in a dataset by not being trained only once as in conventional techniques. In other words, RNN architecture is capable of connecting and relating previously learned information to the present learning process. Although it is correct that RNN architecture builds a stronger learning procedure, it might not be necessary for the ML algorithm to learn previous information and correlate it with the new one. In order to address this issue in the RNN architecture, long-short term memory as an architecture derived from RNN was proposed. LSTM is explicitly designed to avoid the long-term dependency problem. In all RNN architectures, there exists the form of a chain of repeating modules of a neural

network. In standard RNNs, this repeating module will have a very simple structure, such as a single *tanh* layer. LSTMs also follow the same chain-like structure, but the repeating module has a different procedure. This module follows the procedure in the block shown in Fig 4.4 where it is replaced with ML algorithm blocks in Fig 4.3.

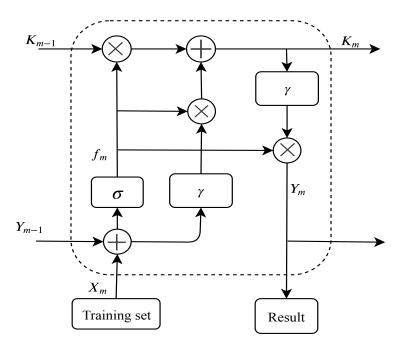


Figure 4.4: LSTM module in each RNN architecture training iteration.

In this module, the σ block, also known as sigmoid, is responsible for producing a binary value indicating what information from a previous training iteration will be neglected and vice versa. The γ block, on the other hand, creates a vector of new candidate values that will be added to the previous training iteration's results if the output of sigmoid block is 1. The outputs of LSTM module are as follows:

$$K_m = \{K_{m-1} \cdot f_m\} + \{f_m \cdot \gamma(Y_{m-1} + X_m)\}$$
(4.18)

$$Y_m = f_m \cdot \gamma(K_m) \tag{4.19}$$

where $f_m = \sigma (Y_{m-1} + X_m)$. The performance of an FB AMC classifier using LSTM layers is expected to be much higher than a conventional DNN in terms of final classification accuracy (P_{CC}), since it first follows RNN architecture and then selects more correlated information to be transferred to the next iteration of training. To summarize, utilizing these layers can benefit the FB AMC classifier by 1) extracting temporal information of the received signal, 2) distinguishing more accurately among different signal samples, and 3) requiring less optimization of hyperparameters due to its property of weight sharing across time steps. Hence, we use two stacked-LSTM layers in our deep learning architecture. The output of these LSTM layers follows the *temporal attention mechanism* in order to: 1) save parts of the derived information, and 2) avoid overfitting. This mechanism also benefits the deep learning architecture by adaptively deriving the final output of an LSTM layer using the outputs of all time steps. This mechanism works as follows. The output of the LSTM layer $\{\mathbf{y}_t\}_{t=0}^{T-1}$ through processing of a shared time-distributed neural network layer that is characterized with weight \mathbf{W}_{α} and bias ζ_{α} matrices results in the calculation of attention weights $\alpha = \{\alpha_t\}_{t=0}^{T-1}$ based on a softmax activation function as in (4.20).

$$\alpha_{t} = \frac{\sigma(\mathbf{y}_{t} \cdot \mathbf{W}_{\alpha} + \zeta_{\alpha})}{\sum_{t=0}^{T-1} \sigma(\mathbf{y}_{t} \cdot \mathbf{W}_{\alpha} + \zeta_{\alpha})}$$
(4.20)

It should be noted that $\sum_{t=0}^{T-1} \alpha_t = 1$ while $\alpha_t \ge 0$. Then the final output is calculated as:

$$\mathbf{y} = \sum_{t=0}^{T-1} \alpha_t \mathbf{y}_t \tag{4.21}$$

This output is then provided to a fully-connected network (FCN), which we will introduce in the following sections. At the end, a softmax activation function is also employed to provide the final result. The Deep Learning architecture for our labeling stage can be seen in Fig 4.5.

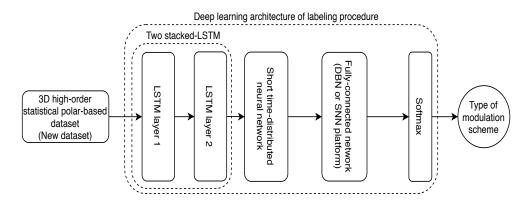


Figure 4.5: Deep Learning architecture of the labeling stage.

4.4 Deep Belief Network as Fully-Connected Network in Deep Learning Structure

The main idea behind proposing the use of DBN for AMC applications is to address the vanishing gradient problem in training the artificial neural network with gradient-based learning methods and back-propagation that have already been used for AMC. The solution to this problem is comprised of two parts [28]. The first involves a restricted boltzmann machine (RBM). This is a method that can automatically find patterns in our data by reconstructing the input. An RBM is a shallow two-layer network shown in Fig 4.6; the first layer is known as the visible layer and the second is called the hidden layer.

Each node in the visible layer (V_i) is connected to every node in the hidden layer (h_j) . An RBM is considered restricted because no two nodes in the same layer share a connection [29]. An RBM is the mathematical equivalent of a two-way translator, where its energy function can be defined as the following based on parameters in Fig 4.6 in one layer of an RBM network:

$$\mathcal{E}(\mathbf{V},\mathbf{h}) = -\sum_{i} a_{i}V_{i} - \sum_{j} b_{j}h_{j} - \sum_{i,j} V_{i}h_{j}w_{ij}$$
(4.22)

where V and h are respectively the vectors of units in the visible and hidden layers. In the forward pass, an RBM takes the inputs and translates them into a set of numbers that

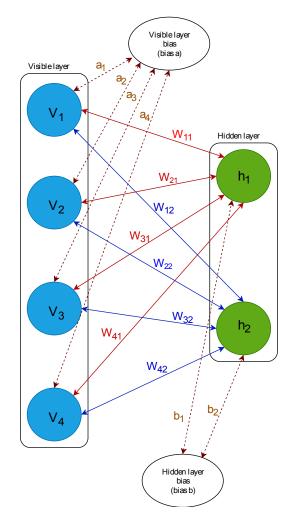


Figure 4.6: An example *RBM* structure with 4 visible and 2 hidden units in their corresponding layers in which the effect of biases on visible and hidden layers units can be observed.

encode the inputs. In the backward pass, it takes this set of numbers and translates them back to form the re-constructed inputs [29]. A well-trained network will be able to perform the backwards translation with a high degree of accuracy. In both steps, the weights and biases have a very important role. In each certain state, an RBM assigns probabilities rather than discrete values to each link. This makes RBMs probabilistic. Accordingly, the joint distribution of each certain state is defined as [29]:

$$p(\mathbf{V}, \mathbf{h}) = \frac{1}{\mathbf{Z}} exp(-E(\mathbf{V}, \mathbf{h}))$$
(4.23)

Where Z is called partition function.

$$\mathbf{Z} = \sum_{\mathbf{V},\mathbf{h}} exp(-E(\mathbf{V},\mathbf{h}))$$
(4.24)

It should be noted that it is a difficult process to calculate the above joint probability due to the large number of possible combinations of V and h in the partition function Z. On the other hand, conditional probabilities of V given h, and h given V are much easier to calculate.

$$p(\mathbf{V}|\mathbf{h}) = \prod_{i} p(v_i|\mathbf{h})$$
(4.25)

$$p(\mathbf{h}|\mathbf{V}) = \prod_{j} p(h_{j}|\mathbf{V})$$
(4.26)

Breaking down the above conditional probabilities while considering that each unit can only exist in a binary state of 0 or 1 will lead us to:

$$p(v_i = 1 | \mathbf{h}) = \sigma(a_i + \sum_j W_{ij} h_j))$$
(4.27)

And analogously,

$$p(h_j = 1 | \mathbf{V}) = \boldsymbol{\sigma}(b_j + \sum_i W_{ij} V_i))$$
(4.28)

where $\sigma(.)$ is the sigmoid function with $\sigma(x) = \frac{1}{1+exp(-x)}$ as its definition. The entire procedure above helps the RBM in deciding which input features are the most important when detecting patterns. Through several forward and backward passes, an RBM is trained to reconstruct the input data. Three steps are repeated iteratively through the training process [29]:

- 1. With a forward pass, every input is combined with an individual weight and one overall bias, and the result is passed to the hidden layer which may or may not activate.
- 2. Next, in a backward pass, each activation is combined with an individual weight and an overall bias, and the result is passed to the visible layer for reconstruction.
- 3. At the visible layer, the reconstruction is compared against the original input to determine the quality of the result.

Steps 1 through 3 are repeated with varying weights and biases until the input and the re-construction are as close as possible [29]. In other words, the update matrix for new weights is: $\mathbf{W}_{new} = \mathbf{W}_{old} + \Delta \mathbf{W}$, where $\Delta \mathbf{W} = \mathbf{V}_0 \otimes p(\mathbf{h}_0 | \mathbf{V}_0) - \sum_{ij} \mathbf{V}_i \otimes p(\mathbf{h}_j | \mathbf{V}_i)$. An interesting aspect of an RBM is that the data does not need to be labelled. This turns out to be very important for real-world data sets such as over-the-air received signals. An RBM automatically sorts through the data, and by properly adjusting the weights and biases an RBM is able to extract the important features and reconstruct the input[7]. An important note is that an RBM is actually making decisions about which input features are important and how they should be combined to form patterns[30]. In other words, an RBM is part of a family of feature extraction neural networks that are all designed to recognize inherent patterns in data. These networks are also called *auto-encoders*, because in a way they have to encode their own structure[8]. For the second part of the solution, we obtain a powerful new model that finally solves the problem by combining RBMs together and introducing a carefully chosen training method. A Deep Belief Network (DBN) can be viewed as a stack of RBMs, where the hidden layer of one RBM is the visible layer of the one above it within the DBN. Therefore, the joint distribution of DBN of *l* layers is as follows [30]:

$$p(\{h_1, h_2, \dots, h_l\}) = (\prod_{k=0}^{l-2} p(h_k | h_{k+1})) p(h_{l-1}, h_l)$$
(4.29)

where $\mathbf{h} = \{h_1, h_2, \dots, h_l\}$ is the vector of all layers in the DBN. A DBN is trained as follows:

- The first RBM is trained to re-construct its input as accurately as possible.
- The hidden layer of the first RBM is treated as the visible layer for the second and the second RBM is trained using the outputs from the first RBM.
- This process is repeated until every layer in the network is trained.

An important note about DBNs is that each RBM layer learns the entire input. In other kinds of models, such as convolutional networks, early layers detect simple patterns and later layers recombine them [30]. A DBN, on the other hand, works globally by fine-tuning the entire input in succession as the model slowly improves. The reason that a DBN works so well is that a stack of RBMs will outperform a single unit [29]. After this initial training, the RBMs create a model that can detect inherent patterns in the data [30]. But we still don't know exactly what the patterns are called [29]. To finish training, we need to introduce labels to the patterns and fine-tune the network with supervised learning [29]. To do this, we need a very small set of labeled samples so that the features and patterns can be associated with a name. The weights and biases are altered slightly, resulting in a small change in the network's perception of the patterns, and often a small increase in the total accuracy [29]. Fortunately, the set of labelled data can be small relative to the original data set, which as we've discussed is extremely helpful in real-world applications [30]. As mentioned before, a DBN only needs a small labelled dataset, which is important for real-world applications. The training process can also be completed in a reasonable amount of time through the use of GPUs. And best of all, the resulting network will be very accurate compared to a shallow network.

Learning parameters, also known as hyperparameters, play a very important role in the accuracy of the training process. Hence, setting optimized hyperparameters can finally result in an increase in classification accuracy. Optimizing the hyperparameters when DBN is deployed as FCN in a deep learning structure can be done by two methods.

1. Manually, by several trials to evaluate the training process's performance. This method

is not only inefficient, but it also exhibits lower effectiveness in enhancing the training process.

 Optimizing algorithms specifically designed for such a purpose, like gradient-based optimization.

We select the adaptive moment estimation (Adam) algorithm to optimize the hyperparameters of the learning process in a deep learning structure when DBN is employed.

4.4.1 Adaptive Moment Estimation

Adaptive moment estimation algorithm can be looked at as a combination of RMSprop and stochastic gradient descent (SGD) with momentum. It uses the squared gradients to scale the learning rate like RMSprop and it takes advantage of momentum by using the moving average of the gradient instead of the gradient itself like SGD with momentum. Adam is an adaptive learning rate method, which means it computes individual learning rates for different parameters. Its name is derived from adaptive moment estimation, and the reason it's called that is because Adam uses estimations of first and second moments of gradient to adapt the learning rate for each weight of the neural network. nth moment of a random variable is defined as the expected value of that variable to the power of n. This relation can be seen below.

$$M_n = E[X^n] \tag{4.30}$$

Note that the gradient of the cost function of a neural network can be considered a random variable, since it is usually evaluated on some small random batch of data. The first moment is mean, and the second moment is uncentered variance. In other words, there is no need to subtract the mean during variance calculation. To estimate the moments, Adam utilizes

exponentially moving averages, computed on the gradient evaluated on a current mini-batch:

$$M_t = \beta_1 M_{t-1} + (1 - \beta_1) g_t \tag{4.31}$$

$$\mathcal{V}_t = \beta_2 \mathcal{V}_{t-1} + (1 - \beta_2) g_t^2 \tag{4.32}$$

where *M* and \mathcal{V} are moving averages, *g* is the gradient on the current mini-batch, and β_i is new introduced hyper-parameters of the algorithm. They have very good default values of 0.9 and 0.999, respectively. Almost no designer ever changes these values. The vectors of moving averages are initialized with zeros at the first iteration. These values correlate with the moment, defined as in (4.30). Since *M* and V are estimates of first and second moments, the following property should be held for all iterations:

$$E[M_t] = E[g_t] \tag{4.33}$$

$$E[\mathcal{V}_t] = E[g_t^2] \tag{4.34}$$

Expected values of the estimators should equal the parameter we are trying to estimate. Fortunately, the parameter in our case is also the expected value. If these properties held true, that would mean that we have unbiased estimators. Now, we will see that these do not hold true for our moving averages. Because the process is an initialized averages with zeros, the estimators are biased towards zero. We can prove that for M. It should be noted that the proof for \mathcal{V} would be analogous to prove that we need the formula for M to the very first gradient. By feeding some values of M, we can see the direction the pattern follows.

$$M_0 = 0$$
 (4.35)

$$M_1 = \beta_1 M_0 + (1 - \beta_1) \tag{4.36}$$

$$M_2 = \beta_1 M_1 + (1 - 1)g_2 \tag{4.37}$$

$$M_3 = \beta_1 M_2 + (1 - \beta_1)g_3 \tag{4.38}$$

As can be seen, the further this process expands the value of *M*, the less the first values of the gradients contribute to the overall value, as they get multiplied by smaller and smaller β_i . Capturing this pattern, we can rewrite the formula for our moving average as:

$$M_t = (1 - \beta_1) \sum_{i=0}^t \beta_1^{t-i} g_i$$
(4.39)

In order to remove the discrepancy of two expected values of M, we can relate it to the true first moment:

$$E[M_t] = E[(1 - \beta_1) \sum_{i=0}^t \beta_1^{t-i} g_i]$$
(4.40)

$$E[M_t] = E[g_i](1 - \beta_1) \sum_{i=0}^t \beta_1^{t-i} + K$$
(4.41)

$$E[M_t] = E[g_i](1 - \beta_1^t) + K$$
(4.42)

In the first row, the new formula is used for the moving average to expand M. Next, by approximating g_i with g_t , we can take it out of the sum, since it does not now depend on i. Because the approximation is taking place, the error K emerges in the formula. In the last line, we just use the formula for the sum of a finite geometric series. There are two things we should note from that equation.

- 1. We have a biased estimator. This is not just true for Adam only; the same holds for algorithms, using moving averages (SGD with momentum, RMSprop, etc.).
- 2. It won't have much effect because the value β to the power of t is quickly going towards zero.

Now we need to correct the estimator, so that the expected value is the accurate one. This step is usually referred to as bias correction. The final formulas for our estimator will be as

follows:

$$\hat{M}_t = \frac{M_t}{1 - \beta_1^t} \tag{4.43}$$

$$\hat{\mathcal{V}}_t = \frac{\mathcal{V}_t}{1 - \beta_2^t} \tag{4.44}$$

(4.45)

The only step left to do in this algorithm is to use those moving averages to scale the learning rate individually for each parameter. The way it is done in Adam is by performing a weight update as follows:

$$W_t = W_{t-1} - \eta \frac{\hat{M}_t}{\sqrt{\hat{\mathcal{V}}_t} + \varepsilon}$$
(4.46)

where *W* is model weights, and η is the step size.

Algorithm 1 summarizes aforementioned description of Adam algorithm.

Algorithm 1 Adam algorithm to optimize DBN hyperparameters.

Require: η **Require:** f(W) (Stochastic objective function) **Require:** initializing W_0 $t \leftarrow 0$ $M_{t=0} \leftarrow 0$ $\psi_{t=0} \leftarrow 0$ **while** W_t not converged **do** $t \leftarrow t+1$ $g_t \leftarrow \Delta_W f_t(W_{t-1})$ (Obtaining gradients with respect to objective at timestep t) $M_t \leftarrow \beta_1 M_{t-1} + (1 - \beta_1) g_t$ $\psi_t \leftarrow \beta_2 \psi_{t-1} + (1 - \beta_2) g_t^2$ $\hat{M}_t \leftarrow \frac{M_t}{(1 - \beta_1)}$ $\hat{\psi}_t \leftarrow \frac{V_t}{(1 - \beta_2)}$ $W_t \leftarrow W_{t-1} - \eta \frac{\hat{M}_t}{\sqrt{\hat{\psi}_t + \varepsilon}}$ **end while return** W_t

In general, we can list the three main Adam properties below.

- The actual step size taken by the Adam in each iteration is approximately bounded by the step size hyperparameter. This property adds intuitive understanding to our previous unintuitive learning rate hyperparameter.
- 2. The step size of the Adam update rule is invariant to the magnitude of the gradient, which helps a lot when going through areas with tiny gradients (such as saddle points or ravines). In these areas, SGD struggles to quickly navigate through them.
- 3. Adam was designed to combine the advantages of Adagrad, which works well with sparse gradients, and RMSprop, which works well in online settings. Having both of these enables us to use Adam for a broader range of tasks. Adam can also be looked at as the combination of RMSprop and SGD with momentum.

Chapter 4 presents the optimized hyperparameters by Adam when DBN is used as FCN.

4.5 Spiking Neural Network as a Fully-Connected Network in a Deep Learning Structure

In order to fully understand how SNNs work, we first need to go through two other basic model networks.

4.5.1 Threshold Unit Networks

The first generation of neural network models is based on McCulloch-Pitts neurons or logical threshold units. Such neurons from the rst generation are Boolean, that is, they can output either a zero or a one. This is of course motivated by the observation that biological neurons either re or not, i.e., a spike is transmitted along the axon if and only if the membrane potential surpasses a certain threshold value (provided the cell is not in the absolutely refractory phase shortly after a spike, when no new action potential can

be initiated). Binary encoding of neural activity therefore seems very plausible at rst. So neurons of the first generation receive binary inputs (ρ_i) from other neurons which, depending on the corresponding synaptic weights (w_i), can cause either a excitatory or inhibitory postsynaptic potential (EPSP and IPSP respectively). All stimuli are added up, and if their sum is large enough (corresponding to sufficient depolarization of the membrane at the axon hillhock), a spike is transmitted to the next neurons, i.e., the output is 1. The dynamics of such a threshold unit can thus be summarized as:

$$y = \begin{cases} 1 & \text{, if } h = \sum_{i} \rho_{i} w_{i} > u \\ 0 & \text{, Otherwise} \end{cases}$$
(4.47)

While the threshold *u* was taken to be zero in the first models, non-zero thresholds (biases) were introduced in later models for more flexibility. Models of the first generation include, among others, multilayer perceptrons (MLPs). Due to the binary nature of threshold unit neurons resembling spiking activity, the appropriate learning algorithm for such networks is Hebbian learning. In the case of threshold unit networks, this translates to a weight update rule of the form:

$$\Delta w_i = \lambda \rho_i y \tag{4.48}$$

where λ is a predefined learning rate. In other words, when input i's firing is involved in a neuron's firing, the connection is strengthened. Neural networks of the first generation have been shown to be universal for digital, i.e., logical, computation. The proof is relatively simple: it can be shown that by choosing appropriate weights, a McCulloch-Pitts neuron can compute the logical AND, OR and NOT operators; since any Boolean function can be expressed as a composition of these three logical operators, any such function can be computed by an MLP with a single hidden layer. However, the restriction to binary outputs is also a considerable limitation in an analog world. Moreover, the first generation models do not include a notion of time, but instead assume synchronous updates of units.

4.5.2 Continuous Neural Networks

The second generation of neural networks arise as a very natural extension of the previous generation by allowing real numbers as inputs and outputs, thereby facilitating analog computation. This is achieved by simply replacing the thresholding after summing up the weighted stimuli by a continuous activation function g (note that the step function is discontinuous at the threshold value). The dynamics of a single unit from the second generation can then (except in very special cases) be summarized as:

$$y = g(\sum_{i} w_i \rho_i - b) \tag{4.49}$$

where *b* is the previously mentioned bias term. The standard choice for *g* used to be a sigmoid function, e.g., the logistic or hyperbolic tangent function; however, other simpler functions such as rectified linear units (ReLUs) have become very popular recently in the context of deep learning. Almost all modern NNs such as sigmoid feed-forward, radial basis function, or recurrent neural networks, e.g., the popular and powerful LSTMs. While the binary outputs of McCulloch-Pitts neurons have a very intuitive interpretation as spikes, it is not straightforward to motivate the real valued outputs of artificial neurons of the second generation. Yet, a biological motivation exists also in this case. Instead of coding spikes, these units encode the firing rates of neurons, i.e., frequencies of spikes averaged over some time window. This is biologically justified by observations that neurons often react to stimulus not with a single spike, but instead fire bursts of many spikes within a very short time, and they can fire at a range of intermediate frequencies between their maximal and minimal firing rates. Such an information coding scheme is known as (firing-) rate coding, and it is one of the most prominent coding schemes in neuroscience. However, its applicability is very likely limited. In contrast, Hebbian learning is no longer directly

applicable to the second generation networks since units are computing rates instead of spikes. One of the key advantages of continuous output activation functions is that such models are receptive for the large class of gradient-based optimization techniques from mathematics. The standard learning algorithm for second generation networks is therefore gradient-descent, usually in combination with the backpropagation algorithm, which allows us to propagate error signals (in the case of supervised learning) backwards through the topological ordering of the network. This enables the training of networks with many layers of artificial neurons, so-called deep networks, and is one of the key ingredients of modern deep learning approaches. Hence, neural networks from the second generation introduce an implicit notion of time into the model by computing with firing rates instead of spikes, which makes them biologically more plausible than their predecessors. This was achieved by adapting the previous model to incorporate some new findings from neuroscience. Moreover, networks of the second generation are also universal for digital computation (applying thresholding to the real valued output), and can in fact compute certain Boolean functions with fewer units than threshold units from the first generation. In this sense, second generation networks are computationally more powerful than first generation networks. Furthermore, in a result known as the universal approximation theorem, it has been proven that a network from the second generation with a single hidden layer can approximate any continuous function arbitrarily well.

4.5.3 Spiking Neural Networks

The major difference between SNNs and the other neural networks described above is that SNNs model time explicitly. This is based on the central paradigm of spiking networks in that it is the exact timing of individual spikes, rather than their firing rate averaged over some time window, which carries information in biological brains. SNNs are thus dynamic systems which are usually formulated as systems of ordinary differential equations (ODEs). The central object of SNN models is the membrane potential v(t) of a neuron,

which represents its internal state at time *t*. Since the membrane potential determines the spiking activity, it is necessary to model its time evolution in order to work with exact timing of spikes. Many different models for spiking neurons exist, and a common framework for different models is still largely lacking - an issue that will be discussed in more detail later. These common characteristics are shared by almost all such models:

- 1. Neurons receive multiple continuous-time inputs from their synapses with other neurons in form of spikes, which are usually modelled as Dirac delta functions.
- 2. Such synaptic stimuli can be either excitatory, i.e., increasing the membrane potential and thereby the probability of firing, or inhibitory, i.e., decreasing the membrane potential.
- They produce a single output spike whenever their membrane potential reaches a certain threshold value.

Probably the first and simplest SNN models are the Integrate-and-fire (IF) model and a slightly improved version thereof called the Leaky-integrate-and-fire (LIF) model, whose dynamics are given by:

$$C\frac{dv}{dt}(t) = I(t) - \frac{v(t)}{R}$$
(4.50)

$$C\frac{dv}{dt}(t) = I_{ext}(t) + \sum_{j} w_{j}I_{j}(t) - \frac{v(t)}{R}$$

$$(4.51)$$

where *C* is the membrane capacitance, *R* the membrane resistance, and I(t) the total input current to the neuron at time *t*, which can be decomposed as external current and a sum over all currents transmitted from neurons *j* with synaptic weights w_j . The last term (v(t)) was introduced in the LIF model to account for an exponential decay of the membrane potential to its resting state in lack of new stimuli not accounted for in the earlier IF model. The external current, $I_{ext}(t)$, in the LIF ODE is only relevant for the subset of input neurons in the case of artificial SNNs, and can be ignored for the remaining network dynamics. The resulting equation looks somewhat similar to the inner term of the activation function for second generation models, also containing a summation over inputs multiplied by their synaptic weights. The key difference here is that inputs are spikes in time rather than rates. The exponential decay term might be loosely interpreted as a biased term over time: if no new spikes arrive timely enough to cause an action potential, the membrane returns to its resting state.

Whereas it is relatively easy to understand why SNNs are more biologically plausible than standard ANNs, the issue regarding their computational power is less clear. However, various theoretical results about the computational power of artificial SNNs have been published. In these works, it was shown that any function which can be computed by a network of the first two generations can also be computed by an artificial SNN. In particular, this includes the universal approximation property for SNNs, stating that any continuous function $F : [0,1]^n \rightarrow [0,1]^k$ can be approximated arbitrarily closely (with regard to uniform convergence) by one hidden layer network of spiking neurons with simple piece-wise linear response- (shape of the EPSPs and IPSPs for non-linear responses) and threshold functions (regulating firing threshold and absolutely refractory period). Moreover, it was demonstrated that certain functions can in fact be computed by SNNs with much fewer units than those required by networks of the first and second generation. For example, the Boolean function $CD_n : \{0,1\}^{2n} \rightarrow \{0,1\}$

$$CD_n(x_1, \cdots, x_n, y_1, \cdots, y_n) = \begin{cases} 1 & \text{, if } \rho_i = y_i & \text{for some}i \\ 0 & \text{, Otherwise} \end{cases}$$
(4.52)

can be computed by a single spiking neuron with appropriately chosen weights and delays, whereas a threshold gate network from the first generation computing CD_n has at least $\frac{n}{log(n+1)}$ units, and a continuous neural network from the second generation computing CD_n has at least $n^{1/4}$ units asymptotically. Note that CD_n is not just any arbitrary function, but has a biological interpretation as pattern matching or coincidence detection from two sources x_i and y_i , and is therefore likely to be computed by biological brains as well.

In summary, in contrast to other NNs, SNNs include time explicitly in the model. The output and input of individual neurons in SNNs (except for the case of input units which receive external currents) are completely determined by the firing times of other neurons *j*. However, computing the output firing times requires us to explicitly model the membrane potential as an ODE. The structure of SNNs is a directed graph, identical to other NNs.

Training SNNs has been historically a difficult task. SNNs have been originally destined to be unsupervisedly trained.

4.5.4 Unsupervised Learning-Hebbian Learning

Similar to the first generation of neural networks, modelling the firing of neurons explicitly in SNNs has the advantage that Hebbian learning is applicable. However, Hebbian's rule does not explicitly mention the timing of spikes, but instead just refers to neurons firing together. While this issue does not arise for threshold gates, which are assumed to be synchronized and therefore always either fire together or do not fire together. For lack of better understanding, the units' activities in Hebbian's rule have traditionally been interpreted as firing rates and used in this context for continuous neural networks. A study in which the timing of presynaptic stimulus and postsynaptic action potential was systematically varied finally found a convincing correlation between the timing of pre- and postsynaptic spikes and the synaptic changes affected thereby. Generally speaking, presynaptic spikes occurring shortly before postsynaptic activity resulted in strengthening of the synaptic connection (potentiation), whereas presynaptic spiked arriving shortly after the postsynaptic spike weakened the connection (depression). This process has been termed Spike-timingdependent-plasticity (STDP) and can be seen as an extension of Hebbian learning by exact spike timing. Interestingly, a similar but opposite process to STDP has also been observed in some synapses, i.e., presynaptic spiked following postsynaptic ones resulted in potentiation and vice versa for depression, and was termed anti-STDP. A rule for applying STDP-like

unsupervised learning in SNN models derived from these experimental findings can be formulated as:

$$\frac{d}{dt}w_{ji}(t) = a_0 + a_1 S_i(t) + a_2 S_j(t) + a_3 S_i(t) \overline{S_j}(t) + a_4 \overline{S_i}(t) S_j(t)$$
(4.53)

where S_i and S_j are the spike trains. $\overline{S_i}$ and $\overline{S_j}$ are low pass filtered versions thereof, i.e. with exponential decay instead of a single pulse, and ai are constants governing the synaptic changes. Hence, different choices of the hyperparameters (considering w_{ji} as the main parameters) a_i can account for, e.g., STDP or anti-STDP.

The obtained hyperparameters associated with our deep learning structure are presented in Chapter 4.

4.6 **Proposed Novel Framework Structure**

Our literature review illustrates the fact that there is no framework available for AMC that provides flexibility and efficiency in terms of classification accuracy and computational complexity. Therefore, we address this shortcoming by proposing our adaptive framework that follows the deep learning architecture proposed in this research. This framework is built upon the fact that the AMC component in the receiver has to be trained for both ML platforms (DBN- and SNN-based models) before deployment. After the training processes are completed, the average classification accuracy for each platform for all modulation schemes at a particular SNR is recorded together with the number of timing units that are required for classification. In this manner, the FB AMC classifier, before deployment, has knowledge over required computational complexity and the likelihood of maximum classification accuracy of both ML platforms. Table 4.1 illustrates the required information to be recorded alongside with their notations, which will be further used in forming the decision ratio.

In this framework, the main equalizer of the receiver leverages the SNR value of

| Values | Notation |
|--|-------------|
| Average DBN-based model's classification accuracy of all modulation schemes at each SNR | DBN-ACA-SNR |
| Average SNN-based model's classification accuracy of all modulation schemes at each SNR | SNN-ACA-SNR |
| Timing units required to perform DBN classification | DBN-t |
| Timing units required to perform SNN classification | SNN-t |

Table 4.1: Values to be collected

the intercepted signal, and provides it to the AMC component, which then calculates the following ratio to determine the quantified trade-off of classification accuracy versus computational complexity. The obtained value represents the preferability of using the DBN-based model versus the SNN-based model at that SNR.

$$\frac{\left(\frac{DBN-ACA-SNR}{SNN-ACA-SNR}\right)}{\left(\frac{DBN-t}{SNN-t}\right)} \leqslant 1 \tag{4.54}$$

If this ratio is less than 1, favorability indicates the use of the SNN-based model to be employed for classification. If the ratio is above 1, then DBN is the better choice. This is due to the fact that the SNN-based model is capable of performing the classification with significantly less required number of timing units while maintaining classification accuracy comparable to what the DBN-based model offers. Therefore, this ratio creates an efficient trade-off between classification accuracy and computational complexity between the two models. This provides the flexibility to the AMC classifier to adapt to changing conditions, instead of being compelled to follow a fixed design. An overview of this framework's principal operation can be seen in Fig 4.7.

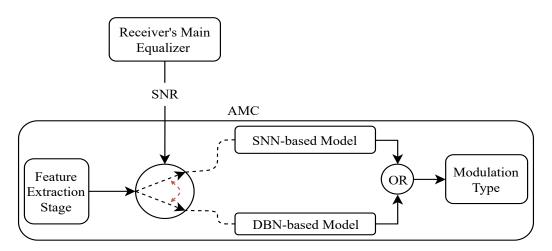


Figure 4.7: The proposed novel framework's principal working.

CHAPTER 5

Results, Analysis and Discussion

In this chapter, we will present the numerical results when each individual FB AMC classifier, DBN- and SNN-based, is implemented for classification. Afterwards, the novel framework will be analyzed.

In order to conduct the evaluation of our proposed platforms and our overall framework, we first obtain the lower and upper performance bounds for each introduced platform by selecting two of the lowest-order (BPSK and QPSK) and highest-order (128QAM and 256QAM) digital modulation schemes from the RadioML dataset [31]. Further, we compare their performance with other works from the scientific literature, specifically [32], [33], which represent two recent efforts that modified the structures of CNN and RNN in order to achieve higher classification accuracy. Details of this evaluation can be found in Appendix A.

We first present the RadioML dataset that is used as the signal reference for experiments of this thesis.

5.1 RadioML2018.01A Dataset

The RadioML dataset is widely used as a reference modulation dataset, and has been generated and recorded over the air by utilizing GNU Radio. The RadioML2018.01A dataset,

specifically, contains two categories of modulated signals with a total of 24 modulation schemes:

- Normal group: OOK, 4ASK, BPSK, QPSK, 8PSK, 16QAM, AM-SSB-SC, AM-DSB-SC, FM, GMSK, OQPSK.
- Difficult group: 8ASK, 16PSK, 32PSK, 16APSK, 32APSK, 64APSK, 128APSK, 32QAM, 64QAM, 128QAM, 256QAM, AM-SSB-WC, AM-DSB-WC.

The dataset's SNR covers a range of -20 dB to +30 dB in increments of 2dB, thus totalling 26 SNR values. There are 4096 signal waveforms for each modulation scheme at a particular SNR. Therefore, in this dataset, there are 106,496 signal waveforms for each modulation scheme for the entire SNR range. Each signal waveform includes 1024 separate complex IQ samples (2×1024). This creates a dataset of 2,555,904 vectors of modulated signal waveforms, with each vector having 1024 IQ samples. In our experiment, we split the dataset into 60% for training and validation, and 40% for testing processes. Table 5.1 investigates the dimensions of the input data for ML algorithms.

| Data Type | Dimensions |
|--------------------|--------------------------------|
| RadioML Dataset | $2\times1024\times2,555,904$ |
| Training Dataset | $2\times1024\times1,277,952$ |
| Validation Dataset | $2 \times 1024 \times 255,590$ |
| Testing Dataset | $2\times1024\times1,022,361$ |

Table 5.1: Input data dimensions.

In order to apply different wireless channels, or environmental effects, all modulated signals were exposed to real-world effects, such as additive white Gaussian noise, multipath fading, frequency offset and phase offset, in order to represent dynamic channel effects. The order of applying real-world effects has been selected to begin from most destructive one while continuing towards less destructive one. It also should be noted that in a given environment, the transmitted signal is not exposed to all of these real-world affects. In other

words, the RadioML dataset is created upon the assumption of having the most destructive environmental effects applied to signal. This process can be seen in Fig 5.1.

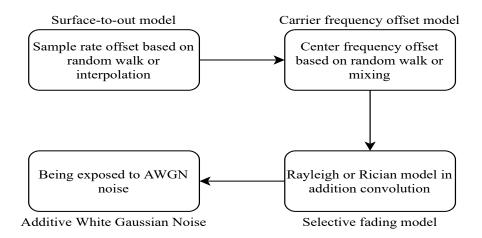
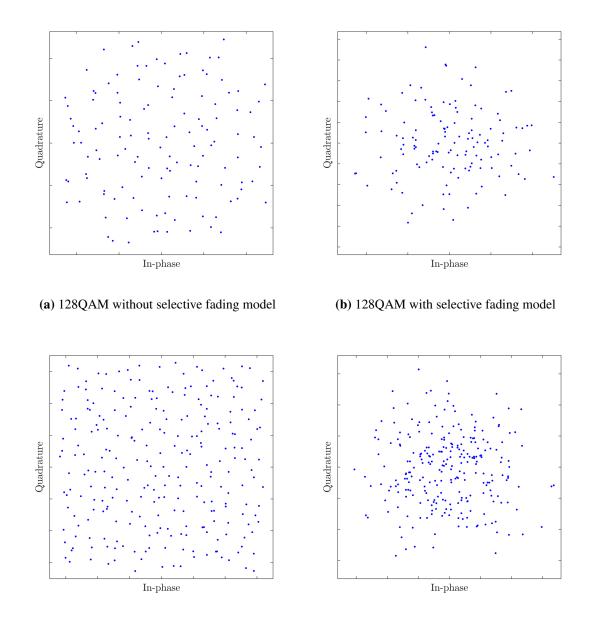


Figure 5.1: Process of applying channel effects to the transmitted signal

The order of applying aforementioned destructive environmental effects has been designed based on likely real-world scenario where the first effect has the highest likeliness of being occurred. But, as can be seen in Fig 5.1, AWGN effect is designed to be the last destructive effect although this effect is considered as first destructive ones in any environment. This is because authors in [31] have attempted to create a worst-case scenario. In such a manner, AWGN effect has to be applied to signal in last step.

From among the effects that the signal is exposed to, the selective fading model has the most destructive impact on higher-order modulation schemes, primarily due to the phase shift offset resulting from this model. Fig 5.2 shows the constellation of a received signal from this dataset for 128QAM and 256QAM at an SNR of 5 dB, both with and without the selective fading model applied. Therefore, in order to achieve higher classification accuracy, information on the properties impacted by the selective fading model, such as phase shift offset, should be extracted during the feature extraction stage, and provided to the labeling stage. This can be achieved through the use of polar coordinate transforms.

Furthermore, in order to provide intuitive understanding of how polar coordinates can provide another domain of information for labeling stage, we plot the output of this



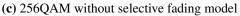
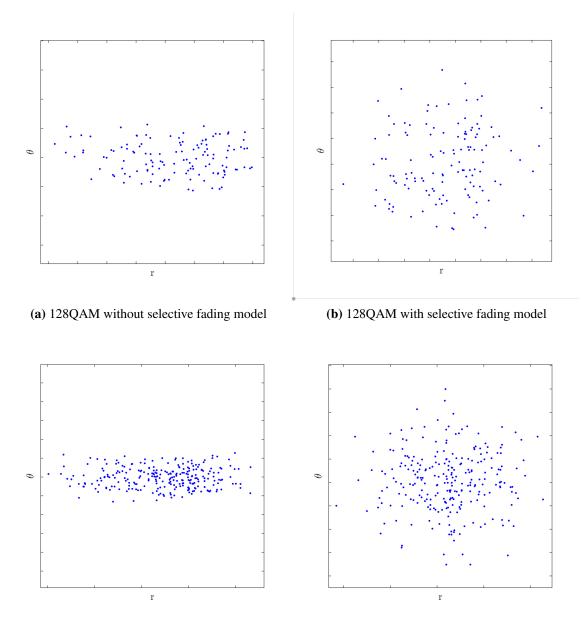
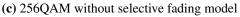




Figure 5.2: The destructive effect of the selective fading model over the constellation of 128QAM and 256QAM from RadioML dataset at $SNR = 5 \, dB$.

component in feature extraction stage. Moreover, we also investigate the effect of selective fading model over polar coordinates. Fig 5.3 shows the polar-based constellation of a received signal from this dataset for 128QAM and 256QAM at an SNR of 5 dB, both with and without the selective fading model applied.





(d) 256QAM with selective fading model

Figure 5.3: Polar-based constellation of 128QAM and 256QAM from RadioML dataset at SNR = 5 dB with and without destructive effect of the selective fading model.

After the RadioML dataset has gone through the new architecture of feature extraction stage, the operation results in *3D high-order statistical polar-based* dataset, for which Table 5.2 shows the corresponding dimensions.

| Data Type | Dimensions |
|--------------------|----------------------------------|
| New Dataset | $4 \times 1025 \times 2,555,904$ |
| Training Dataset | $4 \times 1025 \times 1,277,952$ |
| Validation Dataset | $4 \times 1025 \times 255,590$ |
| Testing Dataset | $4 \times 1025 \times 1,022,361$ |

Table 5.2: 3D high-order statistical polar-based dataset dimensions.

5.2 DBN-based FB AMC Classifier Analysis

In order to start analyzing the performance of this classifier, we first need to build its architecture including setting its hyperparameters.

5.2.1 DBN Architecture and Employment

Designing the architecture of DBN and deployment involves setting its hyperparameters and defining the environment in which it will be simulated.

The input and output layers of our DBN will, respectively, include 24 and 4 units to represent the 24 modulation schemes in the RadioML dataset, and 4 modulation schemes in this research's evaluation. In order to achieve an optimized DBN model, we have selected the adaptive moment estimation (Adam) algorithm [34], [35]. This resulted in optimized hyperparameters and other configurations of DBN presented in Table 5.3.

| Hyperparameters | Values |
|---|---------|
| Number of hidden layers | 6 |
| Number of units in each hidden layer | 18 |
| Activation function of the first 5 layers | ReLU |
| Activation function of the last layer | Softmax |
| Batch size | 256 |
| Number of maximum training epoch | 250 |
| Learning rate | 0.0005 |
| Number of times where contrastive divergence is run (k) | 12 |

Table 5.3: Optimized hyperparameters and configurations of DBN.

From an RBM architecture perspective, this implies that there are 3 visible and 3 shallow layers, each including 18 units. Our training, validating and testing environments are

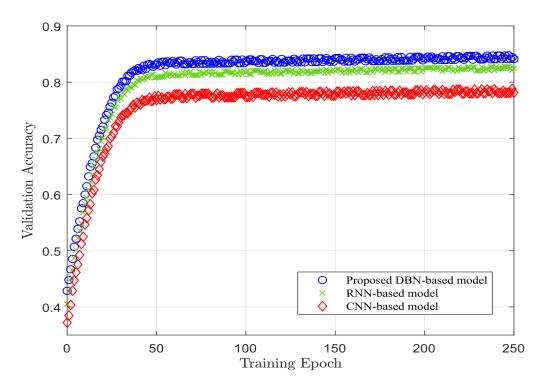


Figure 5.4: Validation accuracy of DBN-based model in training stage.

implemented using the deep learning library Keras running on top of TensorFlow executed in our university's supercomputing infrastructure, HCC Crane JupyterHub [36]. Fig 5.4 and Fig 5.5 respectively show the training performance of the presented DBN-based model in terms of the number of training epochs versus validation accuracy and training loss in addition to a comparison with deep RNN- and CNN-based models. To have a fair representation of validation accuracy and training loss, parameters such as batch size and learning rate are set to be the same for all three models.

The proposed DBN-based model shows higher rising and declining slopes in both evaluations. This points to the fact that DBN-based models are capable of a more accurate training process compared to the other two models. Next, we will present the AMC numerical results and discuss them.

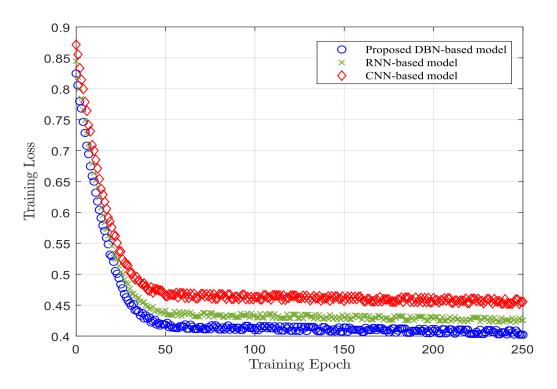


Figure 5.5: Training loss of DBN-based model in training stage.

5.2.2 AMC Results and Discussion

We herein present our results from evaluating the AMC classification performance using our framework, and obtain the lower and upper bounds of the proposed DBN-based model as well as a comparison with RNN- and CNN-based models. Due to the performance plateau of classifiers below -10 dB, we selected the range of SNR to be between -10 and +30 dB for the upper-bound performance analysis. We similarly selected the range of SNR between -10 and +10dB for the lower-bound performance evaluation. Fig 5.6 and Fig 5.7 in next subsections show the aforementioned performances for lower and upper bounds, respectively. Final results are achieved by interpolating between each two consecutive available SNR's probability of correct classification (P_{CC}). The results show the proposed DBN-based model performance compared to RNN- and CNN-based models to obtain lowerand upper-bounds of performance when {BPSK, QPSK} and {128QAM, 256QAM} are classified, respectively. We will separately discuss the numerical results for the lower- and upper-bounds performance.

5.2.2.1 Lower-bound Discussion

As can be observed from Fig **??**, where modulations {BPSK and QPSK} are classified, the proposed DBN-based model outperforms the other two models over the entire range of SNR. This higher performance is notably observable in lower SNRs.

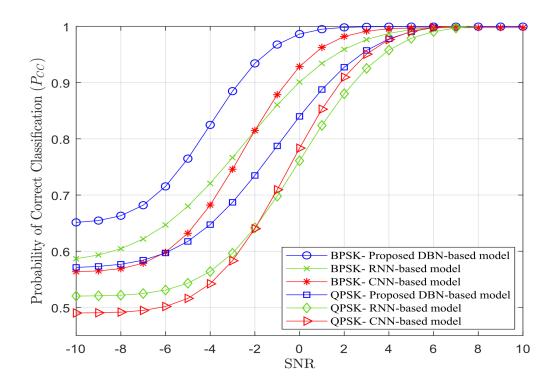


Figure 5.6: Proposed DBN-based lower-bound performance compared to RNN and CNN

The performance of the proposed DBN-based model is on average 21.8% and 16.2% higher than the average performance of the other two models when classifying BPSK and QPSK, respectively. It also should be noted that there is a performance advantage of CNN for lower SNRs over that of RNN. However, the RNN-based model performs better than the CNN-based model in SNRs below -3 dB. That is due to CNN operating based on the constellation shape of the intercepted signal's modulation scheme. And a signal's

constellation shape becomes less apparent as the SNR value decreases.

5.2.2.2 Upper-bound Discussion

Similarly to the discussion of the lower-bound performance, we can observe in Fig 5.7 that the DBN-based model shows a higher capability for correct classification over the entire range of SNR, especially in lower SNR cases. The proposed DBN-based model performs 14.7% and 11.4% on average better than RNN and CNN when 128QAM and 256QAM are classified, respectively.

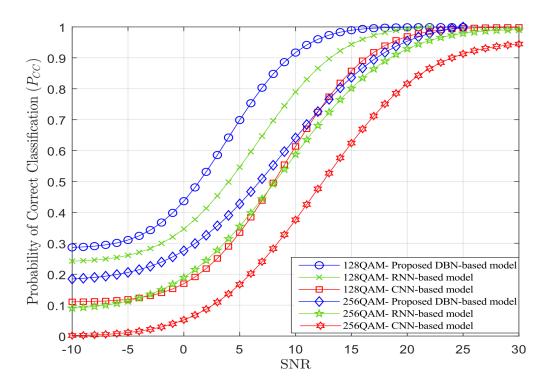


Figure 5.7: Proposed DBN-based upper-bound performance compared to RNN and CNN

As can be seen, while classifying 256QAM, the performance of the proposed DBN- and RNN-based models tends to merge at higher SNRs since the training process of RNN-based model becomes more accurate as SNR increases. This even can be seen in classifying QPSK for the lower-bound performance. Since the CNN-based model depends on the constellation shape to extract the signal's information, its performance generally is degraded as the order

of modulation scheme increases. This degradation in performance is easily noticeable from comparing lower- and upper-bound performances.

Another aspect of DBN performance is that the set of labelled data can be small relative to the original dataset, which is extremely helpful in real-world applications where low latency is of importance [37].

5.2.2.3 Number of Training Samples Discussion

One of the important factors to consider in the AMC domain is how to train the classifier as quickly as possible, and subsequently test it in real-time. One way to accomplish this task is to reduce the sample size while not sacrificing the classification accuracy. DBNs are capable of achieving this goal [38]. Therefore, we herein investigate this property and compare it to the other two models when classifying 32QAM modulation scheme in two scenarios where 1) the full size of and 2) half of the *3D high-order polar-based* dataset is to be used for training, validation and testing with the same aforementioned proportionality. As

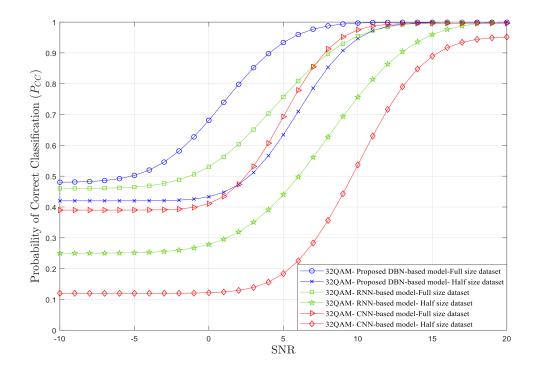


Figure 5.8: Number of training sample impact on classification accuracy.

can be seen from Fig 5.8, when the size of the input sample is reduced to half, the average performance of the proposed DBN-based model drops much less than that of the other two models. At lower SNRs, the proposed DBN-based model's performance trained with half the size of the dataset is even higher than the CNN-based model when trained with the full dataset. Additionally, over higher SNRs, the proposed DBN-based model trained on half of the dataset achieves maximum classification accuracy at approximately the same SNR than the RNN-based model after utilizing the full dataset training size. The main reason behind this key benefit is DBN's capability of probabilistic reconstruction of the input samples, as explained earlier. Additionally, DBN platforms are more resilient than other platforms against the overfitting problem [39].

5.2.3 Computational Complexity Analysis

Computational complexity of any AMC classifier is of high importance in order to measure its capability of operating real-time [40]. Hence, time has been traditionally a metric to measure an AMC classifier's computational complexity. Thus, to analyze computational complexity of the proposed DBN-based model, we take into consideration the time required to perform the classification on this model, and compare it with the other two models in the simulation environment mentioned before. But, in order to exclude the effect of computing power of simulation platform, we define a parameter τ representing the timing unit in this evaluation. Note that τ is scalable based on the simulation platform's computing power. Table 5.4 shows details of this analysis.

| | Proposed DBN- | RNN-based | CNN-based |
|----------------------|---------------|------------------|------------------|
| | based model | model | model |
| Each batch | 0.0022τ | 0.0021τ | 0.0020τ |
| Each epoch | 22.4716τ | 21.826τ | 20.6637τ |
| Total classification | 5056.11τ | 4910.86τ | 4649.35τ |

Table 5.4: Computational complexity of the proposed DBN-based model.

As can be observed from results, the computational complexity of the proposed DBN-

based model is slightly higher than the RNN-based model, by 2.9%, although the average classification accuracy of the proposed DBN-based model is notably higher than the other two models, especially at low SNRs by on average 16.02%. Therefore, we can state in general that the achievable significant increase in classification accuracy easily offsets the slight increase in computational complexity.

5.2.4 Model Conclusion

The proposed DBN-based model increases the average classification accuracy for lowerbound evaluation by 19%, and 13.05% for higher-bound evaluation. This results in a total average increase of 16.02% over the four modulation schemes chosen for this evaluation. This significant increase can be seen over all ranges of SNR, but especially so for lower SNR cases. As a result, the slight increase in computational complexity by 2.9% compared to RNN-based model is acceptable and often negligible. But the proportionality of this increase in classification accuracy compared to that of the increase in computational complexity (5.52) shows the efficiency of this proposed model to be employed for lower SNR cases.

5.3 SNN-based FB AMC Classifier Analysis

Similarly to DBN-based classifier's analysis, we first build the architecture of SNN-based model and then proceed to analyze it.

In order to have a fair evaluation of a DBN-based model, we follow the architecture of the DBN-based model with minimal modifications specifically needed to accommodate SNN, including its training process.

The input and output layers will respectively include 24 and 4 neurons based on the same reasoning as in the previous section. The training algorithm for SNN is selected to be Hebbian learning, which strongly involves the spike-timing-dependent plasticity (STDP) rule in unsupervised learning [41]. Hence, we need to not only set typical hyperparameters

of a neural network, but we are also required to predetermine other parameters regarding Hebbian learning [42]. We set SNN's typical hyperparameters as shown for the proposed DBN-based model, to once again ensure a fair comparison. Table 5.5 indicates these hyperparameters.

| Hyperparameters | Values |
|---------------------------------------|---------|
| Number of hidden layers | 6 |
| Number of units in each hidden layer | 18 |
| Activation function of the last layer | Softmax |
| Batch size | 256 |
| Number of maximum training epoch | 250 |
| Learning rate | 0.0005 |
| Discharge | 0.1 |
| Long term potentiation (LTP) | 1.5 |
| inhLTP | 1.5 |
| Long term depression (LTD) | 0.1 |

Table 5.5: SNN hyperparameters' architecture.

Here, inhLTP represents the fact that if a pre-synaptic neuron is inhibitory, the weight always increases if the pair of neurons fire within a certain time-window, irrespective of the order of firing (inhLTP) [41]–[43]. Building an SNN model as FCN in the proposed deep learning architecture is shown in Fig 5.9 and Fig 5.10 in terms of training validation and loss process measurements, respectively.

The training process measurements mainly include the performance of the number of training epochs versus validation accuracy and training loss. Both Fig 5.9 and Fig 5.10 also include the other three models' performances for comparison purposes. As can be seen from Fig 5.9 and Fig 5.10, SNN's training performance is notably similar to that of the RNN-based model, even overlapping in some epochs, but it is always lower than the proposed DBN-based model and always higher than the CNN-based model. This implies that although SNN benefits from eliminating neurons having no apparent impact on classification from computations [44], classification accuracy suffers as a result of that same property [45]. The simulation environment is the same as explained in the previous section [36], [46].

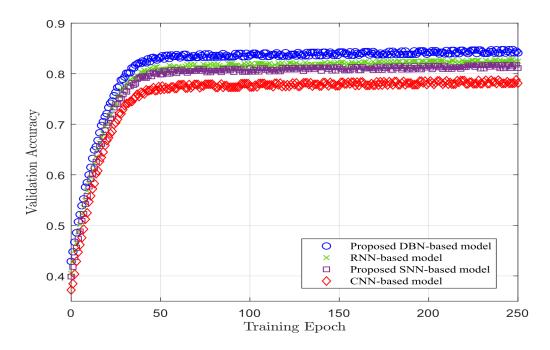


Figure 5.9: Proposed SNN-based model performance of number of training epochs versus validation accuracy.

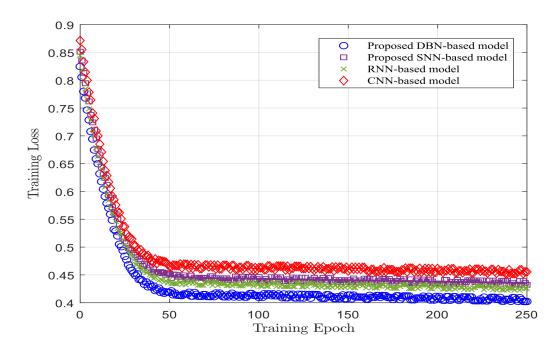


Figure 5.10: Proposed SNN-based model performance of number of training epochs versus training loss.

5.3.1 Results and Discussion

Implementing SNN as FCN in the proposed deep learning architecture results in Fig 5.11 and Fig 5.12, in order to obtain the lower- and upper-bounds performance of the proposed SNN-based model where {BPSK and QPSK} and {128QAM and 256QAM} are respectively classified.

Similar to the proposed DBN-based model discussion, we separately investigate the upper and lower performance bounds for the proposed SNN-based model.

5.3.1.1 Lower-bound performance

Observing Fig 5.11 shows that the proposed SNN-based model significantly outperforms the CNN-based model by an average of 17.1% and 9.8% when classifying 128QAM and 256QAM, respectively.

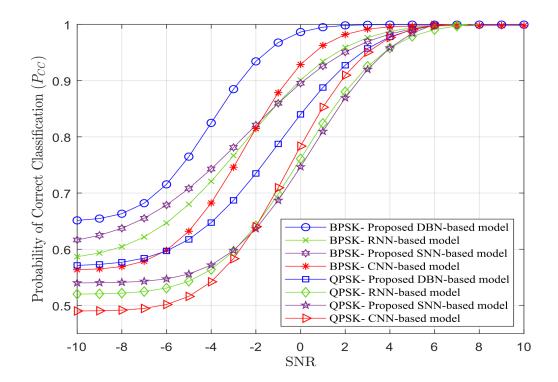


Figure 5.11: Proposed SNN-based model lower-bound performance compared to proposed DBN-, RNN- and CNN-based models.

On the other hand, the proposed SNN-based model also exhibits modestly higher

performance compared to the RNN-based model at higher SNRs. Overall, it can be stated that the proposed SNN-based model performs on average 14.3% and 7.8% higher than CNN-and RNN-based models when classifying 128QAM and 256QAM, respectively.

5.3.1.2 Upper-bound Performance

As can be seen from Fig 5.12, the proposed SNN-based model outperforms the RNN- and CNN-based models at SNRs lower than -2 dB by 9.2%.

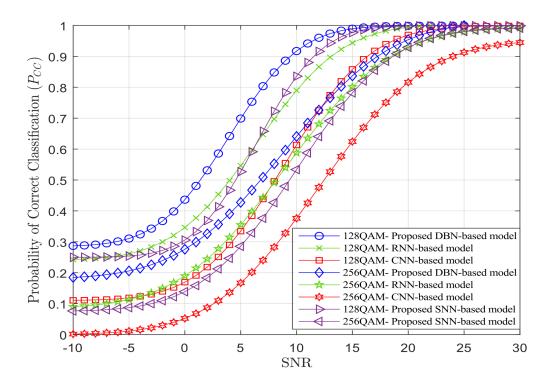


Figure 5.12: Proposed SNN-based model upper-bound performance compared to proposed DBN-, RNN- and CNN-based models.

This is a consequence of the neurons' behavior of not firing when they have no constructive effect on the classification [47]. This can be seen in lower SNR cases, where involving misled neurons can degrade the classification process. On the other hand, the training process of the proposed DBN-based model is significantly more accurate and outperforms the proposed SNN-based model over the entire SNR range. Overall, the proposed SNN-based model performs on average 5.7% and 2.9% higher than CNN- and RNN-based models over the entire SNR range. However, the CNN-based model has a higher performance at SNRs above -2 dB due to the higher orderly constellation shape of the received signal.

5.3.2 Computational Complexity Analysis

Similar to the analysis provided in the previous section, we now investigate the computational complexity of the proposed SNN-based model, based on analyzing the timing unit required to achieve classification. For this model, Table 5.6 indicates the obtained computational complexity measurements.

| Proposed SNN-based model's architecture parameters | Elapsed timing units | |
|--|----------------------|--|
| Each batch | 0.00158τ | |
| Each epoch | 15.84 τ | |
| Total classification | 3565.32 τ | |

 Table 5.6: Proposed SNN-based model computational complexity measurement.

This analysis clearly shows a significant decrease in the required number of timing units to train, validate and classify for the SNN-based model. The number of timing units required by the proposed SNN-model is 1084τ lower than that of the CNN-based model, which has the lowest computational complexity among the proposed DBN- and RNN-based models. This implies that the proposed SNN-based model is 23.31% faster than CNN-based model. Additionally, the proposed SNN-based model performs the AMC operation 41.81% and 34.31% faster when compared to the proposed DBN- and RNN-based models.

5.3.3 Model Conclusion

Although the main purpose behind the proposal to use SNN-based models was to reduce computational complexity, its classification accuracy performance in obtaining both lower and upper bounds indicates that it is very competitive compared to the average classification accuracy of the other models investigated during our research. The proposed SNN-based model reduces computational complexity by an average of 33.14% compared to the three other models, while it outperforms CNN- and RNN-based models by on average 4.3% and 11% in obtaining lower and upper bounds, respectively.

5.4 Proposed Novel Framework Analysis

Applying the presented ratio for framework (4.54) provides us with the answer to which ML approach to use for different channel conditions, as shown in Table 5.7. SNN is clearly the

| SNR dB | Model | SNR dB | Model |
|--------|-------|--------|-------|
| -20 | DBN | 6 | SNN |
| -18 | DBN | 8 | SNN |
| -16 | DBN | 10 | SNN |
| -14 | DBN | 12 | SNN |
| -12 | DBN | 14 | SNN |
| -10 | DBN | 16 | SNN |
| -8 | DBN | 18 | SNN |
| -6 | DBN | 20 | SNN |
| -4 | DBN | 22 | SNN |
| -2 | SNN | 24 | SNN |
| 0 | SNN | 26 | SNN |
| 2 | SNN | 28 | SNN |
| 4 | SNN | 30 | SNN |

 Table 5.7: Tradeoff-driven model selection for classification at each SNR.

preferred choice over a significant portion of the evaluated SNR range. This would indicate that SNN is also the overall better choice for non-adaptive AMC implementation. However, having an FB-AMC classifier that can adapt according to Table 5.7 reduces computational complexity by 39.2% compared to the case where the proposed DBN-based model is utilized for classification over all SNR ranges. Additionally, such a classifier only sacrifices on average 5.8% in classification accuracy for SNRs lower than -2 dB.

CHAPTER 6

Conclusion and Future Work

In this thesis, in the area of automatic modulation classification, we achieved significant performance improvements in both stages of the feature-based AMC approach. We contributed to the feature extraction stage by designing a new architecture that enables the retrieval of unbiased fourth-order cumulants, and leverages polar coordinates of the intercepted signal for improved accuracy. This resulted in a new 3D high-order statisti*cal polar-based* dataset to be used in the labeling stage. Here, through a deep learning architecture design, we introduced the platforms of deep belief network and spiking neural network in order to increase classification accuracy, specifically at lower SNR values, and decrease computational complexity of the classifier, respectively. In our evaluation, we obtained the lower- and upper-bounds performance of the proposed classifiers while classifying the lowest- (BPSK, QPSK) and highest-order modulation schemes (128QAM, 256QAM) utilizing the signals from the RadioML dataset. We not only provided numerical results of the proposed classifiers, but we also compared them with two recent modified classifiers based on convolutional- and recurrent-based neural networks. The comparison showed a significant increase in classification accuracy by an average of 16.02% when a deep belief network was employed. Specifically, for lower SNR values, we obtained both lower-bound performance improvements of 19% and upper-bound improvements of 13.05%. Additionally, we showed that the spiking neural network's performance remained

competitive compared to recurrent-based neural networks while performing classification on average 34.31% faster. We showed that the proposed spiking neural network achieved notable higher classification accuracy compared to the convolutional-based neural network while also performing AMC 23.31% faster. Finally, we developed an efficient and flexible framework based on the proposed platforms' characteristics, computational complexity and classification accuracy. It can adapt between these ML approaches based on the currently observed SNR obtained from the receiver's equalizer component. This framework achieved a 36.2% higher efficiency in terms of required computational cost while sacrificing only 5.8% in classification accuracy for SNRs lower than -2 dB.

Our future research direction involves both DBN and SNN models. For DBN platform, it is necessary to decrease the computational complexity of the DBN-based model without sacrificing notable classification accuracy. This requires modification in inherent design of DBN-based model to be specifically adapted for AMC applications. In this manner, we will be able to decrease the computational complexity of DBN-based model while classification accuracy of such platform does not decrease as much as computational complexity. The very optimistic scenario occurs when we decrease the DBN-based model's computational complexity without sacrificing any of classification accuracy. We can have such a same direction for SNN-based model.

For SNN platform, the goal should be to increase the classification accuracy without increasing the computational complexity. To do this task again, we need to apply some modification in inherent design of SNN platform to specially adjust its operation for AMC applications. In this direction, the very optimistic path is to increase the classification accuracy while computational complexity is decreased.

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APPENDIX A

Deep Learning Models Participating in Comparing Results

We herein investigate two of the most studied ANN platforms, CNN and RNN, in the AMC domain. We built a comparison mechanism by modeling two of the most recently proposed deep CNN- and RNN-based models that significantly improve the performance of the FB-AMC classifier.

A.1 Deep CNN-based Model

The authors of [32] proposed an end-to-end trainable deep CNN-based model that is capable of automatically learning a signal's features without going through feature extraction. They also proposed a two-step training approach that includes pre-training and fine-tuning steps for the proposed CNN-based model. Their model also divides the input data into unit sizes for parallel computation. Then, a maximum *a posteriori* probability (MAP) criterion classifies the modulation schemes. Eliminating the feature extraction stage and parallel computation simplified their system design, but they had to remove some decision processes to keep their system's computational complexity low. Their system model also requires SNR to be known for the classifier to work. We implemented their system in order to compare this model with our proposed classifiers. The general view of their network architecture can be seen in Fig A.1.

The structure dimensions of this network are described in Table A.1 where 'n.a.' represents not-applied.

| Layers | Kernel Number | Kernel Size | Stride | Window Size |
|-----------------|------------------|-------------|--------|----------------|
| Convolutional A | 12 | 3 | 1 | n.a. |
| Convolutional B | 24 | 3 | 1 | n.a. |
| Convolutional C | 32 | 3 | 1 | n.a. |
| AveragePool | n.a. | n.a. | 1 | 2 |

Table A.1: CNN-based model structure dimensions.

The output vectors of the last AveragePool layer are compacted into a vector by the flattened layer. Then, the dense layer encodes this vector into a 256-dimensional vector that

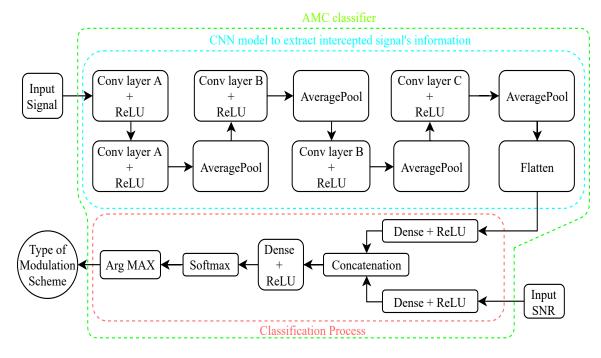


Figure A.1: The deep CNN-based classifier's structure.

carries high-level extracted information from the intercepted signal. Pre-training executes the following steps: 1) generating and sampling training data, 2) randomly setting system model parameters, and 3) training the model and storing the updated parameters with minimal validation loss. Fine-tuning steps are: 1) producing training data, 2) randomly initializing the top layer of system model after its replacement with updated parameters from pre-training, and finally 3) training the model and storing the updated parameters with minimal validation loss. More details of this model can be found in [32]. In order to fit this model with our experiment, we do not execute the first steps of pre-training and fine-tuning. Moreover, note that the input data dimension in the RadioML dataset is 2×1024 for the received symbols. On the other hand, their input data dimension is 2×1000 .

A.2 RNN-based Model

We also implemented the deep RNN-based system model proposed in [33]. In this model, a pre-processing stage is first used to re-order the structure of the received samples based on their phases. Then, a deep RNN-based model is built upon a long short-term memory (LSTM) network that can properly learn long-term dependencies of the received samples. Finally, a MAP criterion is used for modulation classification. The deep RNN-based model can be seen in Fig A.2.

This model consists of three stacked-LSTM layers that are later connected to a four-layer fully-connected network. In each layer of the fully-connected network, the number of units is set to 11 because of using of RadioML2016.10a, which contains a total of 11 modulated signals. Hence, in order to fit this model into our experiment, we needed to increase the

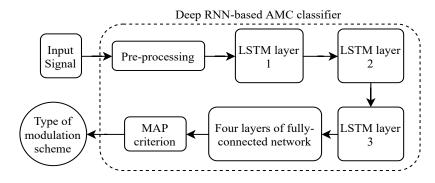


Figure A.2: The deep RNN-based classifier's structure.

number of units in the input layer to 24 and decrease the output layer's units to 4. All other steps remained the same as shown in [33], which also contains more details for the interested reader.

APPENDIX **B**

Spiking Neural Network-Based Platform Utilized in This Research

We herein provide the code written¹ by author to create the environment and simulate the spiking neural network in Python language based on PyTorch simulator, especially adapted to AMC applications. We group the codes that relate to one another in following sections in order to operate.

B.1 Initialization and Refactored Conversion Module

```
1 from pathlib import Path
3 from . import (
      utils,
4
      network,
5
      models,
6
      analysis,
7
      preprocessing,
8
      datasets,
9
      encoding,
10
      pipeline,
11
      learning,
12
13
      evaluation,
      environment,
14
      conversion,
15
16 )
17
18 ROOT_DIR = Path(__file__).parents[0].parents[0]
                               Listing B.1: Initialization
1 import math
```

2 import torch 3 import numpy as np

¹The structure and flow of following SNN code were inspired and followed based on bindsnet 0.2.7 package [48].

```
4
5 from torch import Tensor
6 import torch.nn.functional as F
7 from numpy import ndarray
8 from typing import Tuple, Union
9 from torch.nn.modules.utils import _pair
10
11
12 def im2col_indices(
13
      x: Tensor,
      kernel_height: int,
14
      kernel_width: int,
15
      padding: Tuple[int, int] = (0, 0),
16
      stride: Tuple[int, int] = (1, 1),
17
18) -> Tensor:
      # language=rst
19
      0.0.0
20
      im2col is a special case of unfold which is implemented inside
21
     of Pytorch.
22
     :param x: Input image tensor to be reshaped to column-wise
     format.
     :param kernel_height: Height of the convolutional kernel in
24
     pixels.
      :param kernel_width: Width of the convolutional kernel in pixels
      :param padding: Amount of zero padding on the input image.
26
      :param stride: Amount to stride over image by per convolution.
27
      :return: Input tensor reshaped to column-wise format.
28
      .....
29
      return F.unfold(x, (kernel_height, kernel_width), padding=
30
     padding, stride=stride)
31
32
33 def col2im_indices(
34
      cols: Tensor,
      x_shape: Tuple[int, int, int, int],
35
      kernel_height: int,
36
      kernel_width: int,
37
      padding: Tuple[int, int] = (0, 0),
38
      stride: Tuple[int, int] = (1, 1),
39
40 ) -> Tensor:
      # language=rst
41
      0.0.0
42
      col2im is a special case of fold which is implemented inside of
43
     Pytorch.
44
      :param cols: Image tensor in column-wise format.
45
      :param x_shape: Shape of original image tensor.
46
      :param kernel_height: Height of the convolutional kernel in
47
     pixels.
      :param kernel_width: Width of the convolutional kernel in pixels
48
     :param padding: Amount of zero padding on the input image.
49
```

```
:param stride: Amount to stride over image by per convolution.
50
      :return: Image tensor in original image shape.
51
      0.0.0
52
53
      return F.fold(
          cols, x_shape, (kernel_height, kernel_width), padding=
54
     padding, stride=stride
      )
55
56
57
58 def get_square_weights(
      weights: Tensor, n_sqrt: int, side: Union[int, Tuple[int, int]]
59
_{60}) -> Tensor:
      # language=rst
61
      0.0.0
62
      Return a grid of a number of filters 'sqrt ** 2' with side
63
     lengths ''side''.
64
      :param weights: Two-dimensional tensor of weights for two-
65
     dimensional data.
      :param n_sqrt: Square root of no. of filters.
66
      :param side: Side length(s) of filter.
67
      :return: Reshaped weights to square matrix of filters.
68
      0.0.0
69
      if isinstance(side, int):
70
          side = (side, side)
71
72
      square_weights = torch.zeros(side[0] * n_sqrt, side[1] * n_sqrt)
73
      for i in range(n_sqrt):
74
          for j in range(n_sqrt):
75
               n = i * n_sqrt + j
76
               if not n < weights.size(1):</pre>
78
                   break
79
80
               x = i * side[0]
81
               y = (j \% n_sqrt) * side[1]
82
               filter_ = weights[:, n].contiguous().view(*side)
83
               square_weights[x : x + side[0], y : y + side[1]] =
84
     filter_
85
      return square_weights
86
87
88
89 def get_square_assignments(assignments: Tensor, n_sqrt: int) ->
     Tensor:
      # language=rst
90
      .....
91
      Return a grid of assignments.
92
93
     :param assignments: Vector of integers corresponding to class
94
     labels.
      :param n_sqrt: Square root of no. of assignments.
95
      :return: Reshaped square matrix of assignments.
96
      0.0.0
97
```

```
square_assignments = torch.mul(torch.ones(n_sqrt, n_sqrt), -1.0)
98
      for i in range(n_sqrt):
99
           for j in range(n_sqrt):
100
101
               n = i * n_sqrt + j
102
               if not n < assignments.size(0):</pre>
103
                   break
104
105
106
               square_assignments[
                   i : (i + 1), (j % n_sqrt) : ((j % n_sqrt) + 1)
107
               ] = assignments[n]
108
109
      return square_assignments
110
113 def reshape_locally_connected_weights(
      w: Tensor,
114
      n_filters: int,
      kernel_size: Union[int, Tuple[int, int]],
116
      conv_size: Union[int, Tuple[int, int]],
      locations: Tensor,
118
      input_sqrt: Union[int, Tuple[int, int]],
119
    -> Tensor:
120)
      # language=rst
      .....
      Get the weights from a locally connected layer and reshape them
      to be two-dimensional and square.
124
      :param w: Weights from a locally connected layer.
      :param n_filters: No. of neuron filters.
126
      :param kernel_size: Side length(s) of convolutional kernel.
       :param conv_size: Side length(s) of convolution population.
128
      :param locations: Binary mask indicating receptive fields of
129
      convolution population neurons.
      :param input_sqrt: Sides length(s) of input neurons.
130
      :return: Locally connected weights reshaped as a collection of
      spatially ordered square grids.
       .....
132
      kernel_size = _pair(kernel_size)
      conv_size = _pair(conv_size)
134
      input_sqrt = _pair(input_sqrt)
135
136
      k1, k2 = kernel_size
      c1, c2 = conv_size
138
      i1, i2 = input_sqrt
139
      clsqrt, c2sqrt = int(math.ceil(math.sqrt(c1))), int(math.ceil(
140
      math.sqrt(c2)))
      fs = int(math.ceil(math.sqrt(n_filters)))
141
142
      w_{-} = torch.zeros((n_filters * k1, k2 * c1 * c2))
143
144
      for n1 in range(c1):
145
           for n2 in range(c2):
146
               for feature in range(n_filters):
147
```

```
n = n1 * c2 + n2
148
                                                 filter_ = w[
149
                                                           locations[:, n],
150
                                                           feature * (c1 * c2) + (n // c2sqrt) * c2sqrt + (
151
              n % c2sqrt),
                                                 ].view(k1, k2)
152
                                                 w_{feature * k1 : (feature + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * k1, n * k2 : (n + 1) * (n + 1) 
153
               1) * k2] = filter_
154
                if c1 == 1 and c2 == 1:
155
                            square = torch.zeros((i1 * fs, i2 * fs))
156
157
                           for n in range(n_filters):
158
                                      square[
                                                 (n // fs) * i1 : ((n // fs) + 1) * i2,
160
                                                 (n % fs) * i2 : ((n % fs) + 1) * i2,
161
                                      ] = w_{n} * i1 : (n + 1) * i2
162
163
                           return square
164
                 else:
165
                           square = torch.zeros((k1 * fs * c1, k2 * fs * c2))
166
167
                           for n1 in range(c1):
168
                                      for n2 in range(c2):
169
                                                 for f1 in range(fs):
170
                                                           for f2 in range(fs):
                                                                      if f1 * fs + f2 < n_filters:</pre>
172
                                                                                 square[
173
                                                                                           k1 * (n1 * fs + f1) : k1 * (n1 * fs
174
              + f1 + 1),
                                                                                           k2 * (n2 * fs + f2) : k2 * (n2 * fs
              + f2 + 1),
                                                                                 ] = w_{[}
176
                                                                                            (f1 * fs + f2) * k1 : (f1 * fs + f2)
177
              + 1) * k1,
                                                                                            (n1 * c2 + n2) * k2 : (n1 * c2 + n2)
178
              + 1) * k2,
                                                                                ٦
179
180
                           return square
181
182
183
      def reshape_conv2d_weights(weights: torch.Tensor) -> torch.Tensor:
184
                # language=rst
185
                 .....
186
                Flattens a connection weight matrix of a Conv2dConnection
187
188
                :param weights: Weight matrix of Conv2dConnection object.
189
                 :param wmin: Minimum allowed weight value.
190
                 :param wmax: Maximum allowed weight value.
191
                 0.0.0
192
                sqrt1 = int(np.ceil(np.sqrt(weights.size(0))))
193
                sqrt2 = int(np.ceil(np.sqrt(weights.size(1))))
194
                height, width = weights.size(2), weights.size(3)
195
```

```
reshaped = torch.zeros(
196
           sqrt1 * sqrt2 * weights.size(2), sqrt1 * sqrt2 * weights.
197
      size(3)
198
      )
199
       for i in range(sqrt1):
200
           for j in range(sqrt1):
201
                for k in range(sqrt2):
202
                    for l in range(sqrt2):
203
                        if i * sqrt1 + j < weights.size(0) and k * sqrt2</pre>
204
       + l < weights.size(
                             1
205
                        ):
206
                             fltr = weights[i * sqrt1 + j, k * sqrt2 + 1
207
      ].view(height, width)
                             reshaped[
208
                                 i * height
209
                                 + k * height * sqrt1 : (i + 1) * height
                                 + k * height * sqrt1,
                                  (j % sqrt1) * width
                                 + (1 % sqrt2) * width * sqrt1 : ((j %
      sqrt1) + 1) * width
                                 + (1 % sqrt2) * width * sqrt1,
214
                             ] = fltr
216
      return reshaped
217
```

Listing B.2: Refactored conversion module

B.2 Environment and its Initialization

```
1 from .environment import Environment, GymEnvironment
                              Listing B.3: Initialization
1 from abc import ABC, abstractmethod
2 from typing import Tuple, Dict, Any
4 import gym
5 import numpy as np
6 import torch
8 from ...datasets.preprocess import subsample, gray_scale,
     binary_image, crop
9 from .. encoding import Encoder, NullEncoder
10
11
12 class Environment(ABC):
      # language=rst
13
      .....
14
      Abstract environment class.
15
      0.0.0
16
17
      @abstractmethod
18
```

```
def step(self, a: int) -> Tuple[Any, ...]:
19
           # language=rst
20
           ......
           Abstract method head for ''step()''.
22
           :param a: Integer action to take in environment.
24
           0.0.0
25
           pass
26
27
      @abstractmethod
28
      def reset(self) -> None:
29
           # language=rst
30
           0.0.0
31
           Abstract method header for ''reset()''.
32
           0.0.0
33
           pass
34
35
      @abstractmethod
36
      def render(self) -> None:
37
           # language=rst
38
           0.0.0
39
           Abstract method header for ''render()''.
40
           0.0.0
41
           pass
42
43
      @abstractmethod
44
      def close(self) -> None:
45
           # language=rst
46
           0.0.0
47
           Abstract method header for '`close()''.
48
           0.0.0
49
           pass
50
51
      @abstractmethod
52
      def preprocess(self) -> None:
53
           # language=rst
54
           0.0.0
55
           Abstract method header for ''preprocess()''.
56
           0.0.0
57
           pass
58
59
60
61 class GymEnvironment(Environment):
      # language=rst
62
      0.0.0
63
      A wrapper around the OpenAI ''gym'' environments.
64
       0.0.0
65
66
      def __init__(self, name: str, encoder: Encoder = NullEncoder(),
67
     **kwargs) -> None:
           # language=rst
68
           0.0.0
69
           Initializes the environment wrapper. This class makes the
70
           assumption that the OpenAI ''gym'' environment will provide
71
```

an image of format HxW or CxHxW as an observation (we will add the C dimension to HxW tensors) or a 1D observation in which case no dimensions will be added. 74 75 :param name: The name of an OpenAI ''gym'' environment. 76 :param encoder: Function to encode observations into spike 77 trains. 78 Keyword arguments: 79 80 :param float max_prob: Maximum spiking probability. 81 :param bool clip_rewards: Whether or not to use ''np.sign'' 82 of rewards. 83 :param int history: Number of observations to keep track of. 84 :param int delta: Step size to save observations in history. 85 :param bool add_channel_dim: Allows for the adding of the 86 channel dimension in 2D inputs. 87 88 self.name = name 89 self.env = gym.make(name) 90 self.action_space = self.env.action_space 91 92 self.encoder = encoder 93 94 # Keyword arguments. 95 self.max_prob = kwargs.get("max_prob", 1.0) 96 self.clip_rewards = kwargs.get("clip_rewards", True) 97 98 self.history_length = kwargs.get("history_length", None) 99 self.delta = kwargs.get("delta", 1) 100 self.add_channel_dim = kwargs.get("add_channel_dim", True) 101 102 if self.history_length is not None and self.delta is not 103 None: self.history = { 104 i: torch.Tensor() 105 for i in range(1, self.history_length * self.delta + 106 1, self.delta) } 107 else: 108 self.history = {} 109 110 self.episode_step_count = 0 self.history_index = 1 self.obs = None 114 self.reward = None 116 assert (0.0 < self.max_prob <= 1.0 118

), "Maximum spiking probability must be in (0, 1]." 119 120 def step(self, a: int) -> Tuple[torch.Tensor, float, bool, Dict[121 Any, Any]]: # language=rst 122 0.0.0 123 Wrapper around the OpenAI 'gym' environment 'step()' 124 function. 125 :param a: Action to take in the environment. 126 :return: Observation, reward, done flag, and information dictionary. 0.0.0 128 # Call gym's environment step function. 129 self.obs, self.reward, self.done, info = self.env.step(a) 130 if self.clip_rewards: self.reward = np.sign(self.reward) 134 self.preprocess() 136 # Add the raw observation from the gym environment into the info # for debugging and display. 138 info["gym_obs"] = self.obs 139 140 # Store frame of history and encode the inputs. 141 if len(self.history) > 0: 142 self.update_history() 143 self.update_index() 144 # Add the delta observation into the info for debugging 145 and display. info["delta_obs"] = self.obs 146 147 # The new standard for images is BxTxCxHxW. 148 # The gym environment doesn't follow exactly the same 149 protocol. 150 # # 1D observations will be left as is before the encoder and 151 will become BxTxL. # 2D observations are assumed to be mono images will become 152 BxTx1xHxW # 3D observations will become BxTxCxHxW 153 if self.obs.dim() == 2 and self.add_channel_dim: 154 # We want CxHxW, it is currently HxW. 155 self.obs = self.obs.unsqueeze(0) 156 157 # The encoder will add time - now Tx... 158 if self.encoder is not None: 159 self.obs = self.encoder(self.obs) 160 161 # Add the batch - now BxTx... 162 self.obs = self.obs.unsqueeze(0) 163 164

```
self.episode_step_count += 1
165
166
           # Return converted observations and other information.
167
           return self.obs, self.reward, self.done, info
168
169
       def reset(self) -> torch.Tensor:
170
           # language=rst
           0.0.0
           Wrapper around the OpenAI 'gym'' environment 'reset()''
      function.
174
           :return: Observation from the environment.
175
           0.0.0
176
           # Call gym's environment reset function.
           self.obs = self.env.reset()
178
           self.preprocess()
179
180
           self.history = {i: torch.Tensor() for i in self.history}
181
182
           self.episode_step_count = 0
183
184
           return self.obs
185
186
       def render(self) -> None:
187
           # language=rst
188
           0.0.0
189
           Wrapper around the OpenAI 'gym'' environment 'render()''
190
      function.
           0.0.0
191
           self.env.render()
192
193
       def close(self) -> None:
194
           # language=rst
195
           0.0.0
196
           Wrapper around the OpenAI ''gym'' environment ''close()''
197
      function.
           ......
198
           self.env.close()
199
200
       def preprocess(self) -> None:
201
           # language=rst
202
           .....
203
           Pre-processing step for an observation from a ''gym''
204
      environment.
           .....
205
           if self.name == "SpaceInvaders-v0":
206
                self.obs = subsample(gray_scale(self.obs), 84, 110)
207
                self.obs = self.obs[26:104, :]
208
                self.obs = binary_image(self.obs)
209
           elif self.name == "BreakoutDeterministic-v4":
                self.obs = subsample(gray_scale(crop(self.obs, 34, 194,
      0, 160)), 80, 80)
                self.obs = binary_image(self.obs)
           else: # Default pre-processing step.
```

```
pass
214
           self.obs = torch.from_numpy(self.obs).float()
216
217
      def update_history(self) -> None:
218
           # language=rst
219
           .....
220
           Updates the observations inside history by performing
      subtraction from most
222
           recent observation and the sum of previous observations. If
      there are not enough
           observations to take a difference from, simply store the
223
      observation without any
           differencing.
224
           0.0.0
           # Recording initial observations.
226
           if self.episode_step_count < len(self.history) * self.delta:</pre>
               # Store observation based on delta value.
228
               if self.episode_step_count % self.delta == 0:
229
                    self.history[self.history_index] = self.obs
230
           else:
               # Take difference between stored frames and current
      frame.
               temp = torch.clamp(self.obs - sum(self.history.values())
      , 0, 1)
234
               # Store observation based on delta value.
               if self.episode_step_count % self.delta == 0:
236
                    self.history[self.history_index] = self.obs
238
               assert (
                    len(self.history) == self.history_length
240
               ), "History size is out of bounds"
241
               self.obs = temp
242
243
244
       def update_index(self) -> None:
           # language=rst
245
           .....
246
           Updates the index to keep track of history. For example: "
247
      history = 4 '',
           ''delta = 3'' will produce ''self.history = {1, 4, 7, 10}''
248
      \texttt{and}
           "self.history_index" will be updated according to "self.
249
      delta '' and will wrap
           around the history dictionary.
250
           0.0.0
251
           if self.episode_step_count % self.delta == 0:
252
               if self.history_index != max(self.history.keys()):
253
                    self.history_index += self.delta
254
               else:
255
                    # Wrap around the history.
256
                    self.history_index = (self.history_index % max(self.
257
```

```
history.keys())) + 1
```

Listing B.4: Environment

B.3 Network

```
1 from .network import Network, load
2 from . import nodes, topology, monitors
```

Listing B.5: Initialization

```
1 import tempfile
2 from typing import Dict, Optional, Type, Iterable
4 import torch
5
6 from .monitors import AbstractMonitor
7 from .nodes import Nodes
8 from .topology import AbstractConnection
9 from ..learning.reward import AbstractReward
10
11
12 def load(file_name: str, map_location: str = "cpu", learning: bool =
      None) -> "Network":
13
      # language=rst
      0.0.0
14
      Loads serialized network object from disk.
15
16
      :param file_name: Path to serialized network object on disk.
17
      :param map_location: One of '' cpu"' or '' cuda"'. Defaults to
18
      · · " cpu" · · ·.
      :param learning: Whether to load with learning enabled. Default
19
     loads value from
          disk.
20
      .....
21
      network = torch.load(open(file_name, "rb"), map_location=
22
     map_location)
      if learning is not None and "learning" in vars(network):
23
          network.learning = learning
24
25
      return network
26
27
28
29 class Network(torch.nn.Module):
      # language=rst
30
      0.0.0
31
      Central object of the "'bindsnet'' package. Responsible for the
32
     simulation and
      interaction of nodes and connections.
33
34
      **Example:**
35
36
      .. code-block:: python
37
38
```

```
import torch
39
          import matplotlib.pyplot as plt
40
41
42
          from bindsnet
                                  import encoding
          from bindsnet.network import Network, nodes, topology,
43
     monitors
44
          network = Network(dt=1.0) # Instantiates network.
45
46
          X = nodes.Input(100) # Input layer.
47
          Y = nodes.LIFNodes(100) # Layer of LIF neurons.
48
          C = topology.Connection(source=X, target=Y, w=torch.rand(X.n
49
     , Y.n)) # Connection from X to Y.
50
          # Spike monitor objects.
51
          M1 = monitors.Monitor(obj=X, state_vars=['s'])
52
          M2 = monitors.Monitor(obj=Y, state_vars=['s'])
53
54
          # Add everything to the network object.
55
          network.add_layer(layer=X, name='X')
56
          network.add_layer(layer=Y, name='Y')
57
          network.add_connection(connection=C, source='X', target='Y')
58
          network.add_monitor(monitor=M1, name='X')
59
          network.add_monitor(monitor=M2, name='Y')
60
61
          # Create Poisson-distributed spike train inputs.
62
          data = 15 * torch.rand(100) # Generate random Poisson rates
63
      for 100 input neurons.
          train = encoding.poisson(datum=data, time=5000) # Encode
64
     input as 5000ms Poisson spike trains.
65
          # Simulate network on generated spike trains.
66
          inputs = {'X' : train} # Create inputs mapping.
67
          network.run(inputs=inputs, time=5000) # Run network
68
     simulation.
69
          # Plot spikes of input and output layers.
70
          spikes = {'X' : M1.get('s'), 'Y' : M2.get('s')}
71
          fig, axes = plt.subplots(2, 1, figsize=(12, 7))
73
          for i, layer in enumerate(spikes):
74
              axes[i].matshow(spikes[layer], cmap='binary')
75
              axes[i].set_title('%s spikes' % layer)
76
              axes[i].set_xlabel('Time'); axes[i].set_ylabel('Index of
77
      neuron')
              axes[i].set_xticks(()); axes[i].set_yticks(())
78
              axes[i].set_aspect('auto')
79
80
          plt.tight_layout(); plt.show()
81
      .....
82
83
      def __init__(
84
          self,
85
          dt: float = 1.0,
```

86

```
batch_size: int = 1,
87
           learning: bool = True,
88
           reward_fn: Optional[Type[AbstractReward]] = None,
89
90
       ) \rightarrow None:
           # language=rst
91
           0.0.0
92
           Initializes network object.
93
94
           :param dt: Simulation timestep.
95
           :param batch_size: Mini-batch size.
96
           :param learning: Whether to allow connection updates. True
97
      by default.
            :param reward_fn: Optional class allowing for modification
98
      of reward in case of
               reward-modulated learning.
99
           .....
100
           super().__init__()
101
102
           self.dt = dt
103
           self.batch_size = batch_size
104
105
           self.layers = {}
106
           self.connections = {}
107
           self.monitors = {}
108
109
           self.train(learning)
110
           if reward_fn is not None:
                self.reward_fn = reward_fn()
114
           else:
                self.reward_fn = None
116
       def add_layer(self, layer: Nodes, name: str) -> None:
117
           # language=rst
118
           0.0.0
119
           Adds a layer of nodes to the network.
120
121
           :param layer: A subclass of the "Nodes" object.
           :param name: Logical name of layer.
           0.0.0
124
           self.layers[name] = layer
           self.add_module(name, layer)
126
           layer.train(self.learning)
128
           layer.compute_decays(self.dt)
129
           layer.set_batch_size(self.batch_size)
130
       def add_connection(
           self, connection: AbstractConnection, source: str, target:
133
      str
       ) \rightarrow None:
134
           # language=rst
           0.0.0
136
           Adds a connection between layers of nodes to the network.
```

```
138
           :param connection: An instance of class ''Connection''.
139
           :param source: Logical name of the connection's source layer
140
           :param target: Logical name of the connection's target layer
141
           .....
142
           self.connections[(source, target)] = connection
143
           self.add_module(source + "_to_" + target, connection)
144
145
           connection.dt = self.dt
146
           connection.train(self.learning)
147
148
       def add_monitor(self, monitor: AbstractMonitor, name: str) ->
149
      None:
           # language=rst
150
           0.0.0
151
           Adds a monitor on a network object to the network.
152
153
           :param monitor: An instance of class ''Monitor''.
154
           :param name: Logical name of monitor object.
155
           .....
156
           self.monitors[name] = monitor
157
           monitor.network = self
158
           monitor.dt = self.dt
159
160
       def save(self, file_name: str) -> None:
161
           # language=rst
162
           .....
163
           Serializes the network object to disk.
164
165
           :param file_name: Path to store serialized network object on
166
       disk.
167
           **Example:**
168
169
           .. code-block:: python
                import torch
                import matplotlib.pyplot as plt
173
174
               from pathlib
                                        import Path
175
               from bindsnet.network import *
176
               from bindsnet.network import topology
178
               # Build simple network.
179
               network = Network(dt=1.0)
180
181
               X = nodes.Input(100) # Input layer.
182
               Y = nodes.LIFNodes(100) # Layer of LIF neurons.
183
               C = topology.Connection(source=X, target=Y, w=torch.rand
184
      (X.n, Y.n)) # Connection from X to Y.
185
               # Add everything to the network object.
186
```

```
network.add_layer(layer=X, name='X')
187
                network.add_layer(layer=Y, name='Y')
188
               network.add_connection(connection=C, source='X', target
189
      = 'Y')
190
               # Save the network to disk.
191
               network.save(str(Path.home()) + '/network.pt')
192
           .....
193
           torch.save(self, open(file_name, "wb"))
194
195
       def clone(self) -> "Network":
196
           # language=rst
197
           0.0.0
198
           Returns a cloned network object.
199
200
           :return: A copy of this network.
201
           0.0.0
202
           virtual_file = tempfile.SpooledTemporaryFile()
203
           torch.save(self, virtual_file)
204
           virtual_file.seek(0)
205
           return torch.load(virtual_file)
206
207
       def _get_inputs(self, layers: Iterable = None) -> Dict[str,
208
      torch.Tensor]:
           # language=rst
209
           ......
210
           Fetches outputs from network layers to use as input to
211
      downstream layers.
           :param layers: Layers to update inputs for. Defaults to all
      network layers.
           :return: Inputs to all layers for the current iteration.
214
           .....
           inputs = {}
216
218
           if layers is None:
                layers = self.layers
219
220
           # Loop over network connections.
           for c in self.connections:
222
               if c[1] in layers:
                    # Fetch source and target populations.
224
                    source = self.connections[c].source
                    target = self.connections[c].target
226
                    if not c[1] in inputs:
228
                         inputs[c[1]] = torch.zeros(
229
                             self.batch_size, *target.shape, device=
230
      target.s.device
                        )
231
                    # Add to input: source's spikes multiplied by
      connection weights.
                    inputs[c[1]] += self.connections[c].compute(source.s
234
```

```
)
235
          return inputs
236
      def run(
238
           self, inputs: Dict[str, torch.Tensor], time: int, one_step=
239
      False, **kwargs
      ) -> None:
240
           # language=rst
241
           .....
242
           Simulate network for given inputs and time.
243
244
           :param inputs: Dictionary of 'Tensor''s of shape ''[time, *
245
      input_shape]'' or
                          ''[time, batch_size, *input_shape]''.
246
           :param time: Simulation time.
247
           :param one_step: Whether to run the network in "feed-forward
248
      " mode, where inputs
               propagate all the way through the network in a single
249
      simulation time step.
               Layers are updated in the order they are added to the
250
      network.
251
           Keyword arguments:
252
253
254
           :param Dict[str, torch.Tensor] clamp: Mapping of layer names
       to boolean masks if
               neurons should be clamped to spiking. The "Tensor"s
255
      have shape
               ``[n_neurons]'` or '`[time, n_neurons]'`.
256
           :param Dict[str, torch.Tensor] unclamp: Mapping of layer
257
      names to boolean masks
               if neurons should be clamped to not spiking. The ''
258
      Tensor''s should have
               shape ''[n_neurons]'' or ''[time, n_neurons]''.
259
           :param Dict[str, torch.Tensor] injects_v: Mapping of layer
260
      names to boolean
               masks if neurons should be added voltage. The "Tensor"
261
      s should have shape
               ''[n_neurons]'' or ''[time, n_neurons]''.
262
           :param Union[float, torch.Tensor] reward: Scalar value used
263
      in reward-modulated
               learning.
264
           :param Dict[Tuple[str], torch.Tensor] masks: Mapping of
265
      connection names to
               boolean masks determining which weights to clamp to zero
266
267
           **Example:**
268
269
           .. code-block:: python
270
               import torch
272
               import matplotlib.pyplot as plt
```

```
from bindsnet.network import Network
         from bindsnet.network.nodes import Input
         from bindsnet.network.monitors import Monitor
         # Build simple network.
         network = Network()
         network.add_layer(Input(500), name='I')
         network.add_monitor(Monitor(network.layers['I'],
state_vars=['s']), 'I')
         # Generate spikes by running Bernoulli trials on Uniform
(0, 0.5) samples.
         spikes = torch.bernoulli(0.5 * torch.rand(500, 500))
         # Run network simulation.
         network.run(inputs={'I' : spikes}, time=500)
         # Look at input spiking activity.
         spikes = network.monitors['I'].get('s')
         plt.matshow(spikes, cmap='binary')
        plt.xticks(()); plt.yticks(());
        plt.xlabel('Time'); plt.ylabel('Neuron index')
        plt.title('Input spiking')
         plt.show()
     ......
    # Parse keyword arguments.
     clamps = kwargs.get("clamp", {})
    unclamps = kwargs.get("unclamp", {})
    masks = kwargs.get("masks", {})
    injects_v = kwargs.get("injects_v", {})
    # Compute reward.
    if self.reward_fn is not None:
         kwargs["reward"] = self.reward_fn.compute(**kwargs)
    # Dynamic setting of batch size.
    if inputs != {}:
         for key in inputs:
             # goal shape is [time, batch, n_0, ...]
             if len(inputs[key].size()) == 1:
                 # current shape is [n_0, ...]
                 # unsqueeze twice to make [1, 1, n_0, ...]
                 inputs[key] = inputs[key].unsqueeze(0).unsqueeze
(0)
             elif len(inputs[key].size()) == 2:
                 # current shape is [time, n_0, ...]
                 # unsqueeze dim 1 so that we have
                 # [time, 1, n_0, ...]
```

inputs[key] = inputs[key].unsqueeze(1)

size

274

275

276 277

278

279

280

281

282

283

284

285 286

287

288 289

290

291

292

293

294

295

296

297

298

299

300

301

302 303

304

305

306 307

308

309

311

312

313

314

315

317

318

319

320

322

if inputs[key].size(1) != self.batch_size: 324 self.batch_size = inputs[key].size(1) 326 327 for l in self.layers: self.layers[1].set_batch_size(self. 328 batch_size) 329 for m in self.monitors: 330 self.monitors[m].reset_state_variables() 331 332 break 334 # Effective number of timesteps. timesteps = int(time / self.dt) 336 # Simulate network activity for 'time' timesteps. 338 for t in range(timesteps): 339 # Get input to all layers (synchronous mode). 340 current_inputs = {} 341 if not one_step: 342 current_inputs.update(self._get_inputs()) 343 3/1/ for l in self.layers: 345 # Update each layer of nodes. 346 if l in inputs: 347 if l in current_inputs: 348 current_inputs[l] += inputs[l][t] 349 350 else: current_inputs[l] = inputs[l][t] 351 352 if one_step: 353 # Get input to this layer (one-step mode). 354 current_inputs.update(self._get_inputs(layers=[1 355])) 356 self.layers[1].forward(x=current_inputs[1]) 357 358 # Clamp neurons to spike. 359 clamp = clamps.get(1, None) 360 if clamp is not None: 361 if clamp.ndimension() == 1: 362 self.layers[l].s[:, clamp] = 1 363 else: 364 self.layers[l].s[:, clamp[t]] = 1 365 366 # Clamp neurons not to spike. 367 unclamp = unclamps.get(1, None) 368 if unclamp is not None: 369 if unclamp.ndimension() == 1: 370 self.layers[1].s[unclamp] = 0 371 else: 372 self.layers[1].s[unclamp[t]] = 0 373 374 # Inject voltage to neurons.

```
inject_v = injects_v.get(1, None)
376
                    if inject_v is not None:
377
                         if inject_v.ndimension() == 1:
378
379
                              self.layers[1].v += inject_v
                         else:
380
                              self.layers[1].v += inject_v[t]
381
382
                # Run synapse updates.
383
                for c in self.connections:
384
                    self.connections[c].update(
385
                         mask=masks.get(c, None), learning=self.learning,
386
       **kwargs
                    )
387
388
                # Get input to all layers.
389
                current_inputs.update(self._get_inputs())
390
391
                # Record state variables of interest.
392
                for m in self.monitors:
393
                    self.monitors[m].record()
394
395
           # Re-normalize connections.
396
           for c in self.connections:
397
                self.connections[c].normalize()
398
399
       def reset_state_variables(self) -> None:
400
           # language=rst
401
           0.0.0
402
           Reset state variables of objects in network.
403
           0.0.0
404
           for layer in self.layers:
405
                self.layers[layer].reset_state_variables()
406
407
           for connection in self.connections:
408
                self.connections[connection].reset_state_variables()
409
410
           for monitor in self.monitors:
411
                self.monitors[monitor].reset_state_variables()
412
413
       def train(self, mode: bool = True) -> "torch.nn.Module":
414
           # language=rst
415
           .....
416
           Sets the node in training mode.
417
418
           :param mode: Turn training on or off.
419
420
           :return: ''self'' as specified in ''torch.nn.Module''.
421
           ......
422
           self.learning = mode
423
           return super().train(mode)
424
```

Listing B.6: Network

from abc import ABC, abstractmethod

```
2 from functools import reduce
3 from operator import mul
4 from typing import Iterable, Optional, Union
6 import torch
8
9 class Nodes(torch.nn.Module):
      # language=rst
10
      ......
11
      Abstract base class for groups of neurons.
      0.0.0
13
14
      def __init__(
15
          self,
16
          n: Optional[int] = None,
17
          shape: Optional[Iterable[int]] = None,
18
          traces: bool = False,
19
          traces_additive: bool = False,
20
          tc_trace: Union[float, torch.Tensor] = 20.0,
          trace_scale: Union[float, torch.Tensor] = 1.0,
22
          sum_input: bool = False,
23
          learning: bool = True,
24
          **kwargs,
25
      ) \rightarrow None:
26
          # language=rst
27
          0.0.0
28
          Abstract base class constructor.
29
30
          :param n: The number of neurons in the layer.
31
           :param shape: The dimensionality of the layer.
32
           :param traces: Whether to record decaying spike traces.
33
           :param traces_additive: Whether to record spike traces
34
     additively.
          :param tc_trace: Time constant of spike trace decay.
35
           :param trace_scale: Scaling factor for spike trace.
36
          :param sum_input: Whether to sum all inputs.
37
          :param learning: Whether to be in learning or testing.
38
          0.0.0
39
          super().__init__()
40
41
          assert (
42
              n is not None or shape is not None
43
          ), "Must provide either no. of neurons or shape of layer"
44
45
          if n is None:
46
               self.n = reduce(mul, shape) # No. of neurons product of
47
      shape.
          else:
48
               self.n = n # No. of neurons provided.
49
50
          if shape is None:
51
               self.shape = [self.n] # Shape is equal to the size of
52
     the layer.
```

```
else:
53
               self.shape = shape # Shape is passed in as an argument.
54
55
           assert self.n == reduce(
56
               mul, self.shape
57
           ), "No. of neurons and shape do not match"
58
59
           self.traces = traces # Whether to record synaptic traces.
60
           self.traces_additive = (
61
               traces_additive
62
           ) # Whether to record spike traces additively.
63
           self.register_buffer("s", torch.ByteTensor()) # Spike
64
      occurrences.
65
           self.sum_input = sum_input # Whether to sum all inputs.
66
67
           if self.traces:
68
               self.register_buffer("x", torch.Tensor())  # Firing
69
      traces.
               self.register_buffer(
70
                    "tc_trace", torch.tensor(tc_trace)
71
                  # Time constant of spike trace decay.
               )
               if self.traces_additive:
73
                    self.register_buffer(
74
                        "trace_scale", torch.tensor(trace_scale)
75
                   ) # Scaling factor for spike trace.
76
               self.register_buffer(
77
                    "trace_decay", torch.empty_like(self.tc_trace)
78
                 # Set in compute_decays.
               )
79
80
           if self.sum_input:
81
               self.register_buffer("summed", torch.FloatTensor()) #
82
      Summed inputs.
83
           self.dt = None
84
           self.batch_size = None
85
           self.trace_decay = None
86
           self.learning = learning
87
88
       @abstractmethod
89
      def forward(self, x: torch.Tensor) -> None:
90
           # language=rst
91
           .....
92
           Abstract base class method for a single simulation step.
93
94
           :param x: Inputs to the layer.
95
           .....
96
           if self.traces:
97
               # Decay and set spike traces.
98
               self.x *= self.trace_decay
99
100
               if self.traces_additive:
101
                   self.x += self.trace_scale * self.s.float()
102
               else:
103
```

```
self.x.masked_fill_(self.s != 0, 1)
104
105
           if self.sum_input:
106
107
                # Add current input to running sum.
                self.summed += x.float()
108
109
       def reset_state_variables(self) -> None:
110
           # language=rst
111
           0.0.0
           Abstract base class method for resetting state variables.
           0.0.0
114
           self.s.zero_()
116
           if self.traces:
               self.x.zero_()
                                # Spike traces.
118
119
           if self.sum_input:
120
                self.summed.zero_() # Summed inputs.
121
       def compute_decays(self, dt) -> None:
123
           # language=rst
124
           .....
           Abstract base class method for setting decays.
126
           0.0.0
           self.dt = dt
128
           if self.traces:
129
                self.trace_decay = torch.exp(
130
                    -self.dt / self.tc_trace
131
                   # Spike trace decay (per timestep).
                )
       def set_batch_size(self, batch_size) -> None:
134
           # language=rst
135
           136
           Sets mini-batch size. Called when layer is added to a
      network.
138
           :param batch_size: Mini-batch size.
139
           .....
140
           self.batch_size = batch_size
141
           self.s = torch.zeros(batch_size, *self.shape, device=self.s.
142
      device)
143
           if self.traces:
144
                self.x = torch.zeros(batch_size, *self.shape, device=
145
      self.x.device)
146
           if self.sum_input:
147
                self.summed = torch.zeros(
148
                    batch_size, *self.shape, device=self.summed.device
149
                )
150
151
       def train(self, mode: bool = True) -> "Nodes":
152
           # language=rst
153
           0.0.0
154
```

```
Sets the layer in training mode.
156
           :param bool mode: Turn training on or off
157
           :return: self as specified in 'torch.nn.Module'
158
           0.0.0
159
           self.learning = mode
160
           return super().train(mode)
161
162
163
  class AbstractInput(ABC):
164
       # language=rst
165
       0.0.0
166
       Abstract base class for groups of input neurons.
167
       0.0.0
168
169
170
  class Input(Nodes, AbstractInput):
171
       # language=rst
       .....
       Layer of nodes with user-specified spiking behavior.
174
       0.0.0
176
       def __init__(
177
           self,
178
           n: Optional[int] = None,
179
           shape: Optional[Iterable[int]] = None,
180
           traces: bool = False,
181
           traces_additive: bool = False,
182
           tc_trace: Union[float, torch.Tensor] = 20.0,
183
           trace_scale: Union[float, torch.Tensor] = 1.0,
184
           sum_input: bool = False,
185
           **kwargs,
186
       ) -> None:
187
           # language=rst
188
           0.0.0
189
           Instantiates a layer of input neurons.
190
191
           :param n: The number of neurons in the layer.
192
           :param shape: The dimensionality of the layer.
193
           :param traces: Whether to record decaying spike traces.
194
           :param traces_additive: Whether to record spike traces
195
      additively.
           :param tc_trace: Time constant of spike trace decay.
196
           :param trace_scale: Scaling factor for spike trace.
197
           :param sum_input: Whether to sum all inputs.
198
           0.0.0
199
           super().__init__(
200
                n=n,
201
                shape=shape,
202
                traces=traces,
203
                traces_additive=traces_additive,
204
                tc_trace=tc_trace,
205
                trace_scale=trace_scale,
206
                sum_input=sum_input,
207
```

```
)
208
209
       def forward(self, x: torch.Tensor) -> None:
211
           # language=rst
           0.0.0
           On each simulation step, set the spikes of the population
      equal to the inputs.
214
           :param x: Inputs to the layer.
215
           0.0.0
216
           # Set spike occurrences to input values.
           self.s = x
218
219
           super().forward(x)
       def reset_state_variables(self) -> None:
222
           # language=rst
           0.0.0
224
           Resets relevant state variables.
           0.0.0
226
           super().reset_state_variables()
227
228
229
  class McCullochPitts(Nodes):
230
       # language=rst
231
       .....
       Layer of 'McCulloch-Pitts neurons
233
       <http://wwwold.ece.utep.edu/research/webfuzzy/docs/kk-thesis/kk-
234
      thesis-html/node12.html>'_.
       . . . .
236
       def __init__(
           self.
238
           n: Optional[int] = None,
239
           shape: Optional[Iterable[int]] = None,
240
           traces: bool = False,
241
           traces_additive: bool = False,
242
           tc_trace: Union[float, torch.Tensor] = 20.0,
243
           trace_scale: Union[float, torch.Tensor] = 1.0,
244
           sum_input: bool = False,
245
           thresh: Union[float, torch.Tensor] = 1.0,
246
           **kwargs,
247
       ) -> None:
248
           # language=rst
249
           0.0.0
250
           Instantiates a McCulloch-Pitts layer of neurons.
251
252
           :param n: The number of neurons in the layer.
253
           :param shape: The dimensionality of the layer.
254
           :param traces: Whether to record spike traces.
255
           :param traces_additive: Whether to record spike traces
256
      additively.
           :param tc_trace: Time constant of spike trace decay.
257
           :param trace_scale: Scaling factor for spike trace.
258
```

```
:param sum_input: Whether to sum all inputs.
259
            :param thresh: Spike threshold voltage.
260
            .....
261
262
            super().__init__(
                n=n,
263
                shape=shape,
264
                traces = traces ,
265
                traces_additive=traces_additive,
266
267
                tc_trace=tc_trace,
                trace_scale=trace_scale,
268
                sum_input=sum_input,
269
           )
270
            self.register_buffer(
                "thresh", torch.tensor(thresh, dtype=torch.float)
            )
               # Spike threshold voltage.
274
            self.register_buffer("v", torch.FloatTensor()) # Neuron
275
      voltages.
276
       def forward(self, x: torch.Tensor) -> None:
            # language=rst
278
            .....
279
           Runs a single simulation step.
280
281
            :param x: Inputs to the layer.
282
            0.0.0
283
            self.v = x # Voltages are equal to the inputs.
284
            self.s = self.v >= self.thresh # Check for spiking neurons.
285
286
            super().forward(x)
287
288
       def reset_state_variables(self) -> None:
289
            # language=rst
290
            ......
291
            Resets relevant state variables.
292
            .....
293
            super().reset_state_variables()
294
295
       def set_batch_size(self, batch_size) -> None:
296
            # language=rst
297
            0.0.0
298
            Sets mini-batch size. Called when layer is added to a
299
      network.
300
            :param batch_size: Mini-batch size.
301
            0.0.0
302
            super().set_batch_size(batch_size=batch_size)
303
            self.v = torch.zeros(batch_size, *self.shape, device=self.v.
304
      device)
305
306
307 class IFNodes(Nodes):
       # language=rst
308
       \mathbf{H} = \mathbf{H}
309
```

```
Layer of 'integrate-and-fire (IF) neurons <http://
      neuronaldynamics.epfl.ch/online/Ch1.S3.html>'_.
       .....
311
312
       def __init__(
313
           self,
314
           n: Optional[int] = None,
315
           shape: Optional[Iterable[int]] = None,
316
           traces: bool = False,
317
           traces_additive: bool = False,
318
           tc_trace: Union[float, torch.Tensor] = 20.0,
319
           trace_scale: Union[float, torch.Tensor] = 1.0,
           sum_input: bool = False,
           thresh: Union[float, torch.Tensor] = -52.0,
           reset: Union[float, torch.Tensor] = -65.0,
           refrac: Union[int, torch.Tensor] = 5,
324
           lbound: float = None,
           **kwargs,
326
       ) \rightarrow None:
327
           # language=rst
328
           .....
329
           Instantiates a layer of IF neurons.
330
331
           :param n: The number of neurons in the layer.
           :param shape: The dimensionality of the layer.
333
334
           :param traces: Whether to record spike traces.
           :param traces_additive: Whether to record spike traces
335
      additively.
           :param tc_trace: Time constant of spike trace decay.
336
           :param trace_scale: Scaling factor for spike trace.
337
           :param sum_input: Whether to sum all inputs.
338
           :param thresh: Spike threshold voltage.
339
           :param reset: Post-spike reset voltage.
340
           :param refrac: Refractory (non-firing) period of the neuron.
341
           :param lbound: Lower bound of the voltage.
342
           0.0.0
343
           super().__init__(
344
345
               n=n,
               shape=shape,
346
                traces=traces,
347
348
                traces_additive=traces_additive,
                tc_trace=tc_trace,
349
                trace_scale=trace_scale,
350
                sum_input=sum_input,
351
           )
352
           self.register_buffer(
354
               "reset", torch.tensor(reset, dtype=torch.float)
           ) # Post-spike reset voltage.
356
           self.register_buffer(
357
                "thresh", torch.tensor(thresh, dtype=torch.float)
358
              # Spike threshold voltage.
           )
359
           self.register_buffer(
360
                "refrac", torch.tensor(refrac)
361
```

```
) # Post-spike refractory period.
362
           self.register_buffer("v", torch.FloatTensor())
                                                                 # Neuron
363
      voltages.
364
           self.register_buffer(
                "refrac_count", torch.FloatTensor()
365
              # Refractory period counters.
           )
366
367
           self.lbound = lbound # Lower bound of voltage.
368
369
       def forward(self, x: torch.Tensor) -> None:
           # language=rst
371
           0.0.0
372
           Runs a single simulation step.
373
374
           :param x: Inputs to the layer.
375
           0.0.0
376
           # Integrate input voltages.
377
           self.v += (self.refrac_count == 0).float() * x
378
379
           # Decrement refractory counters.
380
           self.refrac_count = (self.refrac_count > 0).float() * (
381
                self.refrac_count - self.dt
382
           )
383
384
           # Check for spiking neurons.
385
           self.s = self.v >= self.thresh
386
387
           # Refractoriness and voltage reset.
388
           self.refrac_count.masked_fill_(self.s, self.refrac)
389
           self.v.masked_fill_(self.s, self.reset)
390
391
           # Voltage clipping to lower bound.
392
           if self.lbound is not None:
393
                self.v.masked_fill_(self.v < self.lbound, self.lbound)</pre>
394
395
           super().forward(x)
396
397
       def reset_state_variables(self) -> None:
398
           # language=rst
300
           .....
400
           Resets relevant state variables.
401
           .....
402
           super().reset_state_variables()
403
           self.v.fill_(self.reset) # Neuron voltages.
404
           self.refrac_count.zero_() # Refractory period counters.
405
406
       def set_batch_size(self, batch_size) -> None:
407
           # language=rst
408
           0.0.0
409
           Sets mini-batch size. Called when layer is added to a
410
      network.
411
           :param batch_size: Mini-batch size.
412
           0.0.0
413
```

```
super().set_batch_size(batch_size=batch_size)
414
           self.v = self.reset * torch.ones(batch_size, *self.shape,
415
      device=self.v.device)
416
           self.refrac_count = torch.zeros_like(self.v, device=self.
      refrac_count.device)
417
418
  class LIFNodes(Nodes):
419
      # language=rst
420
       .....
421
      Layer of 'leaky integrate-and-fire (LIF) neurons
422
      <http://icwww.epfl.ch/~gerstner/SPNM/node26.html#</pre>
423
      0.0.0
424
425
      def __init__(
426
           self,
427
           n: Optional[int] = None,
428
           shape: Optional[Iterable[int]] = None,
429
           traces: bool = False,
430
           traces_additive: bool = False,
431
           tc_trace: Union[float, torch.Tensor] = 20.0,
432
           trace_scale: Union[float, torch.Tensor] = 1.0,
433
           sum_input: bool = False,
434
           thresh: Union[float, torch.Tensor] = -52.0,
435
           rest: Union[float, torch.Tensor] = -65.0,
436
           reset: Union[float, torch.Tensor] = -65.0,
437
           refrac: Union[int, torch.Tensor] = 5,
438
           tc_decay: Union[float, torch.Tensor] = 100.0,
439
           lbound: float = None,
440
           **kwargs,
441
      ) -> None:
442
           # language=rst
443
           0.0.0
444
           Instantiates a layer of LIF neurons.
445
446
           :param n: The number of neurons in the layer.
447
           :param shape: The dimensionality of the layer.
448
           :param traces: Whether to record spike traces.
110
           :param traces_additive: Whether to record spike traces
450
      additively.
           :param tc_trace: Time constant of spike trace decay.
451
           :param trace_scale: Scaling factor for spike trace.
452
           :param sum_input: Whether to sum all inputs.
453
           :param thresh: Spike threshold voltage.
454
           :param rest: Resting membrane voltage.
455
           :param reset: Post-spike reset voltage.
456
           :param refrac: Refractory (non-firing) period of the neuron.
457
           :param tc_decay: Time constant of neuron voltage decay.
458
           :param lbound: Lower bound of the voltage.
459
           0.0.0
460
           super().__init__(
461
               n=n,
462
               shape=shape,
463
```

```
traces=traces,
464
                traces_additive=traces_additive,
465
                tc_trace=tc_trace,
466
467
                trace_scale=trace_scale,
                sum_input=sum_input,
468
           )
469
470
           self.register_buffer(
471
                "rest", torch.tensor(rest, dtype=torch.float)
472
              # Rest voltage.
           )
473
           self.register_buffer(
474
                "reset", torch.tensor(reset, dtype=torch.float)
475
           )
              # Post-spike reset voltage.
476
           self.register_buffer(
477
                "thresh", torch.tensor(thresh, dtype=torch.float)
478
           )
              # Spike threshold voltage.
479
           self.register_buffer(
480
                "refrac", torch.tensor(refrac)
481
           ) # Post-spike refractory period.
482
           self.register_buffer(
483
                "tc_decay", torch.tensor(tc_decay)
484
              # Time constant of neuron voltage decay.
           )
185
           self.register_buffer(
486
                "decay", torch.zeros(*self.shape)
487
           )
              # Set in compute_decays.
488
           self.register_buffer("v", torch.FloatTensor())
                                                                # Neuron
489
      voltages.
           self.register_buffer(
490
                "refrac_count", torch.FloatTensor()
491
492
           )
               # Refractory period counters.
493
           self.lbound = lbound # Lower bound of voltage.
494
495
       def forward(self, x: torch.Tensor) -> None:
496
           # language=rst
497
           .....
498
           Runs a single simulation step.
499
500
           :param x: Inputs to the layer.
501
           0.0.0
502
           # Decay voltages.
503
           self.v = self.decay * (self.v - self.rest) + self.rest
504
505
           # Integrate inputs.
506
           self.v += (self.refrac_count == 0).float() * x
507
508
           # Decrement refractory counters.
509
           self.refrac_count = (self.refrac_count > 0).float() * (
510
                self.refrac_count - self.dt
511
           )
512
513
           # Check for spiking neurons.
514
           self.s = self.v >= self.thresh
515
516
```

```
# Refractoriness and voltage reset.
517
           self.refrac_count.masked_fill_(self.s, self.refrac)
518
           self.v.masked_fill_(self.s, self.reset)
519
520
           # Voltage clipping to lower bound.
521
           if self.lbound is not None:
522
               self.v.masked_fill_(self.v < self.lbound, self.lbound)</pre>
523
524
           super().forward(x)
525
526
      def reset_state_variables(self) -> None:
527
           # language=rst
528
           0.0.0
529
           Resets relevant state variables.
530
           0.0.0
531
           super().reset_state_variables()
532
           self.v.fill_(self.rest) # Neuron voltages.
533
           self.refrac_count.zero_() # Refractory period counters.
534
535
      def compute_decays(self, dt) -> None:
536
           # language=rst
537
           0.0.0
538
           Sets the relevant decays.
539
           0.0.0
540
           super().compute_decays(dt=dt)
541
           self.decay = torch.exp(
542
               -self.dt / self.tc_decay
543
           )
              # Neuron voltage decay (per timestep).
544
545
      def set_batch_size(self, batch_size) -> None:
546
           # language=rst
547
           0.0.0
548
           Sets mini-batch size. Called when layer is added to a
549
      network.
550
551
           :param batch_size: Mini-batch size.
           .....
552
           super().set_batch_size(batch_size=batch_size)
553
           self.v = self.rest * torch.ones(batch_size, *self.shape,
554
      device=self.v.device)
           self.refrac_count = torch.zeros_like(self.v, device=self.
555
      refrac_count.device)
556
557
  class CurrentLIFNodes(Nodes):
558
      # language=rst
559
       .....
560
      Layer of 'current-based leaky integrate-and-fire (LIF) neurons
561
      <http://icwww.epfl.ch/~gerstner/SPNM/node26.html#
562
      Total synaptic input current is modeled as a decaying memory of
563
      input spikes multiplied by synaptic strengths.
       .....
564
565
```

```
def __init__(
566
           self,
567
           n: Optional[int] = None,
568
569
           shape: Optional[Iterable[int]] = None,
           traces: bool = False,
570
           traces_additive: bool = False,
571
           tc_trace: Union[float, torch.Tensor] = 20.0,
572
           trace_scale: Union[float, torch.Tensor] = 1.0,
573
           sum_input: bool = False,
574
           thresh: Union[float, torch.Tensor] = -52.0,
575
           rest: Union[float, torch.Tensor] = -65.0,
576
           reset: Union[float, torch.Tensor] = -65.0,
577
           refrac: Union[int, torch.Tensor] = 5,
578
           tc_decay: Union[float, torch.Tensor] = 100.0,
579
           tc_i_decay: Union[float, torch.Tensor] = 2.0,
580
           lbound: float = None,
581
           **kwargs,
582
       ) \rightarrow None:
583
           # language=rst
584
           0.0.0
585
           Instantiates a layer of synaptic input current-based LIF
586
      neurons.
           :param n: The number of neurons in the layer.
587
           :param shape: The dimensionality of the layer.
588
           :param traces: Whether to record spike traces.
589
           :param traces_additive: Whether to record spike traces
590
      additively.
           :param tc_trace: Time constant of spike trace decay.
591
           :param trace_scale: Scaling factor for spike trace.
592
           :param sum_input: Whether to sum all inputs.
593
           :param thresh: Spike threshold voltage.
594
           :param rest: Resting membrane voltage.
595
           :param reset: Post-spike reset voltage.
596
           :param refrac: Refractory (non-firing) period of the neuron.
597
           :param tc_decay: Time constant of neuron voltage decay.
598
           :param tc_i_decay: Time constant of synaptic input current
599
      decay.
           :param lbound: Lower bound of the voltage.
600
           0.0.0
601
           super().__init__(
602
603
               n=n,
               shape=shape,
604
               traces=traces,
605
               traces_additive=traces_additive,
606
               tc_trace=tc_trace,
607
               trace_scale=trace_scale,
608
               sum_input=sum_input,
609
           )
610
611
                                                                  # Rest
           self.register_buffer("rest", torch.tensor(rest))
612
      voltage.
           self.register_buffer("reset", torch.tensor(reset))
                                                                    # Post-
613
      spike reset voltage.
           self.register_buffer("thresh", torch.tensor(thresh))
                                                                      #
614
```

```
Spike threshold voltage.
           self.register_buffer(
615
                "refrac", torch.tensor(refrac)
616
617
           ) # Post-spike refractory period.
           self.register_buffer(
618
                "tc_decay", torch.tensor(tc_decay)
619
              # Time constant of neuron voltage decay.
           )
620
           self.register_buffer(
621
               "decay", torch.empty_like(self.tc_decay)
622
           )
              # Set in compute_decays.
623
           self.register_buffer(
624
               "tc_i_decay", torch.tensor(tc_i_decay)
625
           )
              # Time constant of synaptic input current decay.
626
           self.register_buffer(
627
               "i_decay", torch.empty_like(self.tc_i_decay)
628
           )
              # Set in compute_decays.
629
630
           self.register_buffer("v", torch.FloatTensor())
                                                                # Neuron
631
      voltages.
           self.register_buffer("i", torch.FloatTensor())
                                                                # Synaptic
632
      input currents.
           self.register_buffer(
633
                "refrac_count", torch.FloatTensor()
634
           )
              # Refractory period counters.
635
636
           self.lbound = lbound # Lower bound of voltage.
637
638
       def forward(self, x: torch.Tensor) -> None:
639
           # language=rst
640
           0.0.0
641
           Runs a single simulation step.
642
643
           :param x: Inputs to the layer.
644
           0.0.0
645
           # Decay voltages and current.
646
           self.v = self.decay * (self.v - self.rest) + self.rest
647
           self.i *= self.i_decay
648
649
           # Decrement refractory counters.
650
           self.refrac_count = (self.refrac_count > 0).float() * (
651
                self.refrac_count - self.dt
652
           )
653
654
           # Integrate inputs.
655
           self.i += x
656
           self.v += (self.refrac_count == 0).float() * self.i
657
658
           # Check for spiking neurons.
659
           self.s = self.v >= self.thresh
660
661
           # Refractoriness and voltage reset.
662
           self.refrac_count.masked_fill_(self.s, self.refrac)
663
           self.v.masked_fill_(self.s, self.reset)
664
665
```

```
# Voltage clipping to lower bound.
666
           if self.lbound is not None:
667
                self.v.masked_fill_(self.v < self.lbound, self.lbound)</pre>
668
669
           super().forward(x)
670
671
       def reset_state_variables(self) -> None:
672
           # language=rst
673
           0.0.0
674
           Resets relevant state variables.
675
           0.0.0
676
           super().reset_state_variables()
677
           self.v.fill_(self.rest) # Neuron voltages.
678
           self.i.zero_() # Synaptic input currents.
679
           self.refrac_count.zero_() # Refractory period counters.
680
681
       def compute_decays(self, dt) -> None:
682
           # language=rst
683
           .....
684
           Sets the relevant decays.
685
           0.0.0
686
           super().compute_decays(dt=dt)
687
           self.decay = torch.exp(
688
                -self.dt / self.tc_decay
689
           )
              # Neuron voltage decay (per timestep).
690
           self.i_decay = torch.exp(
691
                -self.dt / self.tc_i_decay
692
           )
              # Synaptic input current decay (per timestep).
693
694
       def set_batch_size(self, batch_size) -> None:
695
           # language=rst
696
           0.0.0
697
           Sets mini-batch size. Called when layer is added to a
698
      network.
699
700
           :param batch_size: Mini-batch size.
           .....
701
           super().set_batch_size(batch_size=batch_size)
702
           self.v = self.rest * torch.ones(batch_size, *self.shape,
703
      device=self.v.device)
           self.i = torch.zeros_like(self.v, device=self.i.device)
704
           self.refrac_count = torch.zeros_like(self.v, device=self.
705
      refrac_count.device)
706
707
  class AdaptiveLIFNodes(Nodes):
708
       # language=rst
709
       .....
      Layer of leaky integrate-and-fire (LIF) neurons with adaptive
      thresholds. A neuron's voltage threshold is increased
      by some constant each time it spikes; otherwise, it is decaying
      back to its default value.
       .....
714
```

```
def __init__(
           self,
716
           n: Optional[int] = None,
718
           shape: Optional[Iterable[int]] = None,
           traces: bool = False,
719
           traces_additive: bool = False,
           tc_trace: Union[float, torch.Tensor] = 20.0,
721
           trace_scale: Union[float, torch.Tensor] = 1.0,
722
           sum_input: bool = False,
           rest: Union[float, torch.Tensor] = -65.0,
724
           reset: Union[float, torch.Tensor] = -65.0,
           thresh: Union[float, torch.Tensor] = -52.0,
726
           refrac: Union[int, torch.Tensor] = 5,
           tc_decay: Union[float, torch.Tensor] = 100.0,
728
           theta_plus: Union[float, torch.Tensor] = 0.05,
729
           tc_theta_decay: Union[float, torch.Tensor] = 1e7,
730
           lbound: float = None,
           **kwargs,
      ) \rightarrow None:
           # language=rst
734
           0.0.0
           Instantiates a layer of LIF neurons with adaptive firing
736
      thresholds.
           :param n: The number of neurons in the layer.
738
           :param shape: The dimensionality of the layer.
739
           :param traces: Whether to record spike traces.
740
           :param traces_additive: Whether to record spike traces
741
      additively.
           :param tc_trace: Time constant of spike trace decay.
742
           :param trace_scale: Scaling factor for spike trace.
743
           :param sum_input: Whether to sum all inputs.
744
           :param rest: Resting membrane voltage.
745
           :param reset: Post-spike reset voltage.
746
           :param thresh: Spike threshold voltage.
747
           :param refrac: Refractory (non-firing) period of the neuron.
748
           :param tc_decay: Time constant of neuron voltage decay.
749
           :param theta_plus: Voltage increase of threshold after
750
      spiking.
           :param tc_theta_decay: Time constant of adaptive threshold
751
      decay.
           :param lbound: Lower bound of the voltage.
752
           0.0.0
753
           super().__init__(
754
               n=n,
755
               shape=shape,
756
               traces=traces,
757
               traces_additive=traces_additive,
758
               tc_trace=tc_trace,
759
               trace_scale=trace_scale,
760
               sum_input=sum_input,
761
           )
762
763
           self.register_buffer("rest", torch.tensor(rest)) # Rest
764
```

```
voltage.
           self.register_buffer("reset", torch.tensor(reset))
                                                                    # Post-
765
      spike reset voltage.
           self.register_buffer("thresh", torch.tensor(thresh))
                                                                      #
766
      Spike threshold voltage.
           self.register_buffer(
767
               "refrac", torch.tensor(refrac)
768
           )
              # Post-spike refractory period.
769
           self.register_buffer(
770
               "tc_decay", torch.tensor(tc_decay)
           )
             # Time constant of neuron voltage decay.
772
           self.register_buffer(
               "decay", torch.empty_like(self.tc_decay)
774
           )
             # Set in compute_decays.
           self.register_buffer(
776
               "theta_plus", torch.tensor(theta_plus)
           )
             # Constant threshold increase on spike.
778
           self.register_buffer(
779
               "tc_theta_decay", torch.tensor(tc_theta_decay)
780
             # Time constant of adaptive threshold decay.
           )
781
           self.register_buffer(
782
               "theta_decay", torch.empty_like(self.tc_theta_decay)
783
              # Set in compute_decays.
           )
784
785
           self.register_buffer("v", torch.FloatTensor())
                                                                # Neuron
786
      voltages.
           self.register_buffer("theta", torch.zeros(*self.shape))
                                                                         #
787
      Adaptive thresholds.
           self.register_buffer(
788
               "refrac_count", torch.FloatTensor()
789
           )
             # Refractory period counters.
790
           self.lbound = lbound # Lower bound of voltage.
791
792
      def forward(self, x: torch.Tensor) -> None:
793
           # language=rst
794
           .....
795
           Runs a single simulation step.
796
797
           :param x: Inputs to the layer.
798
           0.0.0
799
           # Decay voltages and adaptive thresholds.
800
           self.v = self.decay * (self.v - self.rest) + self.rest
801
           if self.learning:
802
               self.theta *= self.theta_decay
803
804
           # Integrate inputs.
805
           self.v += (self.refrac_count == 0).float() * x
806
807
           # Decrement refractory counters.
808
           self.refrac_count = (self.refrac_count > 0).float() * (
809
               self.refrac_count - self.dt
810
           )
811
812
           # Check for spiking neurons.
813
```

```
self.s = self.v >= self.thresh + self.theta
814
815
           # Refractoriness, voltage reset, and adaptive thresholds.
816
817
           self.refrac_count.masked_fill_(self.s, self.refrac)
           self.v.masked_fill_(self.s, self.reset)
818
           if self.learning:
819
                self.theta += self.theta_plus * self.s.float().sum(0)
820
821
           # voltage clipping to lowerbound
822
           if self.lbound is not None:
823
                self.v.masked_fill_(self.v < self.lbound, self.lbound)</pre>
824
825
           super().forward(x)
826
827
       def reset_state_variables(self) -> None:
828
           # language=rst
829
           0.0.0
830
           Resets relevant state variables.
831
           .....
832
           super().reset_state_variables()
833
           self.v.fill_(self.rest) # Neuron voltages.
834
           self.refrac_count.zero_() # Refractory period counters.
835
836
       def compute_decays(self, dt) -> None:
837
           # language=rst
838
           839
           Sets the relevant decays.
840
           0.0.0
841
           super().compute_decays(dt=dt)
842
           self.decay = torch.exp(
843
                -self.dt / self.tc_decay
844
           )
              # Neuron voltage decay (per timestep).
845
           self.theta_decay = torch.exp(
846
                -self.dt / self.tc_theta_decay
847
           )
              # Adaptive threshold decay (per timestep).
848
849
       def set_batch_size(self, batch_size) -> None:
850
           # language=rst
851
           0.0.0
852
           Sets mini-batch size. Called when layer is added to a
853
      network.
854
           :param batch_size: Mini-batch size.
855
           0.0.0
856
857
           super().set_batch_size(batch_size=batch_size)
           self.v = self.rest * torch.ones(batch_size, *self.shape,
858
      device=self.v.device)
           self.refrac_count = torch.zeros_like(self.v, device=self.
859
      refrac_count.device)
860
861
862 class DiehlAndCookNodes(Nodes):
       # language=rst
863
       \mathbf{H} = \mathbf{H}
864
```

```
Layer of leaky integrate-and-fire (LIF) neurons with adaptive
865
      thresholds (modified for Diehl & Cook 2015
      replication).
866
       0.0.0
867
868
       def __init__(
869
           self,
870
           n: Optional[int] = None,
871
           shape: Optional[Iterable[int]] = None,
872
           traces: bool = False,
873
           traces_additive: bool = False,
874
           tc_trace: Union[float, torch.Tensor] = 20.0,
875
           trace_scale: Union[float, torch.Tensor] = 1.0,
876
           sum_input: bool = False,
877
           thresh: Union[float, torch.Tensor] = -52.0,
878
           rest: Union[float, torch.Tensor] = -65.0,
879
           reset: Union[float, torch.Tensor] = -65.0,
880
           refrac: Union[int, torch.Tensor] = 5,
881
           tc_decay: Union[float, torch.Tensor] = 100.0,
882
           theta_plus: Union[float, torch.Tensor] = 0.05,
883
           tc_theta_decay: Union[float, torch.Tensor] = 1e7,
884
           lbound: float = None,
885
           one_spike: bool = True,
886
           **kwargs,
887
       ) -> None:
           # language=rst
889
           0.0.0
890
           Instantiates a layer of Diehl & Cook 2015 neurons.
891
892
           :param n: The number of neurons in the layer.
893
           :param shape: The dimensionality of the layer.
894
           :param traces: Whether to record spike traces.
895
           :param traces_additive: Whether to record spike traces
896
      additively.
           :param tc_trace: Time constant of spike trace decay.
897
           :param trace_scale: Scaling factor for spike trace.
898
           :param sum_input: Whether to sum all inputs.
899
           :param thresh: Spike threshold voltage.
900
           :param rest: Resting membrane voltage.
901
           :param reset: Post-spike reset voltage.
902
           :param refrac: Refractory (non-firing) period of the neuron.
903
           :param tc_decay: Time constant of neuron voltage decay.
904
           :param theta_plus: Voltage increase of threshold after
905
      spiking.
           :param tc_theta_decay: Time constant of adaptive threshold
906
      decay.
           :param lbound: Lower bound of the voltage.
907
           :param one_spike: Whether to allow only one spike per
908
      timestep.
           0.0.0
909
           super().__init__(
910
911
               n=n,
               shape=shape,
912
               traces=traces,
913
```

```
traces_additive=traces_additive,
914
               tc_trace=tc_trace,
915
               trace_scale=trace_scale,
916
917
               sum_input=sum_input,
           )
918
919
           self.register_buffer("rest", torch.tensor(rest)) # Rest
920
      voltage.
           self.register_buffer("reset", torch.tensor(reset))
                                                                    # Post-
921
      spike reset voltage.
           self.register_buffer("thresh", torch.tensor(thresh))
                                                                      #
922
      Spike threshold voltage.
           self.register_buffer(
923
               "refrac", torch.tensor(refrac)
924
           )
              # Post-spike refractory period.
925
           self.register_buffer(
926
               "tc_decay", torch.tensor(tc_decay)
927
           )
              # Time constant of neuron voltage decay.
928
           self.register_buffer(
929
               "decay", torch.empty_like(self.tc_decay)
930
           )
             # Set in compute_decays.
931
           self.register_buffer(
932
               "theta_plus", torch.tensor(theta_plus)
933
             # Constant threshold increase on spike.
           )
934
           self.register_buffer(
935
               "tc_theta_decay", torch.tensor(tc_theta_decay)
936
           ) # Time constant of adaptive threshold decay.
937
           self.register_buffer(
938
               "theta_decay", torch.empty_like(self.tc_theta_decay)
939
940
           )
              # Set in compute_decays.
           self.register_buffer("v", torch.FloatTensor())
                                                                # Neuron
941
      voltages.
           self.register_buffer("theta", torch.zeros(*self.shape)) #
942
      Adaptive thresholds.
           self.register_buffer(
943
               "refrac_count", torch.FloatTensor()
944
           )
              # Refractory period counters.
945
946
           self.lbound = lbound # Lower bound of voltage.
0/17
           self.one_spike = one_spike # One spike per timestep.
948
949
       def forward(self, x: torch.Tensor) -> None:
950
           # language=rst
951
           0.0.0
952
           Runs a single simulation step.
953
954
           :param x: Inputs to the layer.
955
           0.0.0
956
           # Decay voltages and adaptive thresholds.
957
           self.v = self.decay * (self.v - self.rest) + self.rest
958
           if self.learning:
959
               self.theta *= self.theta_decay
960
961
           # Integrate inputs.
962
```

```
self.v += (self.refrac_count == 0).float() * x
963
964
            # Decrement refractory counters.
965
966
            self.refrac_count = (self.refrac_count > 0).float() * (
                self.refrac_count - self.dt
967
            )
968
969
            # Check for spiking neurons.
970
            self.s = self.v >= self.thresh + self.theta
971
972
            # Refractoriness, voltage reset, and adaptive thresholds.
973
            self.refrac_count.masked_fill_(self.s, self.refrac)
974
            self.v.masked_fill_(self.s, self.reset)
975
            if self.learning:
976
                self.theta += self.theta_plus * self.s.float().sum(0)
977
978
            # Choose only a single neuron to spike.
979
            if self.one_spike:
980
                if self.s.any():
981
                     _any = self.s.view(self.batch_size, -1).any(1)
982
                     ind = torch.multinomial(
983
                         self.s.float().view(self.batch_size, -1)[_any],
984
      1
                     )
985
                     _any = _any.nonzero()
986
                     self.s.zero_()
987
                     self.s.view(self.batch_size, -1)[_any, ind] = 1
988
989
            # Voltage clipping to lower bound.
990
            if self.lbound is not None:
991
                self.v.masked_fill_(self.v < self.lbound, self.lbound)</pre>
992
993
            super().forward(x)
994
995
       def reset_state_variables(self) -> None:
996
            # language=rst
997
            0.0.0
998
            Resets relevant state variables.
999
            0.0.0
1000
            super().reset_state_variables()
1001
            self.v.fill_(self.rest) # Neuron voltages.
1002
            self.refrac_count.zero_() # Refractory period counters.
1003
1004
       def compute_decays(self, dt) -> None:
1005
            # language=rst
1006
            0.0.0
1007
            Sets the relevant decays.
1008
            0.0.0
1009
            super().compute_decays(dt=dt)
1010
            self.decay = torch.exp(
1011
                -self.dt / self.tc_decay
1012
               # Neuron voltage decay (per timestep).
            )
1013
            self.theta_decay = torch.exp(
1014
                -self.dt / self.tc_theta_decay
1015
```

```
) # Adaptive threshold decay (per timestep).
1016
1017
       def set_batch_size(self, batch_size) -> None:
1018
1019
            # language=rst
            0.0.0
1020
            Sets mini-batch size. Called when layer is added to a
1021
      network.
1022
1023
            :param batch_size: Mini-batch size.
            0.0.0
1024
            super().set_batch_size(batch_size=batch_size)
1025
            self.v = self.rest * torch.ones(batch_size, *self.shape,
1026
      device=self.v.device)
            self.refrac_count = torch.zeros_like(self.v, device=self.
1027
      refrac_count.device)
1028
1029
   class IzhikevichNodes(Nodes):
1030
       # language=rst
1031
       0.0.0
1032
       Layer of Izhikevich neurons.
1033
       .....
1034
1035
       def __init__(
1036
            self,
1037
            n: Optional[int] = None,
1038
            shape: Optional[Iterable[int]] = None,
1039
            traces: bool = False,
1040
            traces_additive: bool = False,
1041
            tc_trace: Union[float, torch.Tensor] = 20.0,
1042
            trace_scale: Union[float, torch.Tensor] = 1.0,
1043
            sum_input: bool = False,
1044
            excitatory: float = 1,
1045
            thresh: Union[float, torch.Tensor] = 45.0,
1046
            rest: Union[float, torch.Tensor] = -65.0,
1047
1048
            lbound: float = None,
            **kwargs,
1049
       ) \rightarrow None:
1050
            # language=rst
1051
            0.0.0
1052
            Instantiates a layer of Izhikevich neurons.
1053
1054
            :param n: The number of neurons in the layer.
1055
            :param shape: The dimensionality of the layer.
1056
            :param traces: Whether to record spike traces.
1057
            :param traces_additive: Whether to record spike traces
1058
      additively.
            :param tc_trace: Time constant of spike trace decay.
1059
            :param trace_scale: Scaling factor for spike trace.
1060
            :param sum_input: Whether to sum all inputs.
1061
            :param excitatory: Percent of excitatory (vs. inhibitory)
1062
      neurons in the layer; in range ''[0, 1]''.
            :param thresh: Spike threshold voltage.
1063
            :param rest: Resting membrane voltage.
1064
```

```
:param lbound: Lower bound of the voltage.
1065
            ......
1066
            super().__init__(
1067
1068
                 n=n,
                 shape=shape,
1069
                 traces=traces,
1070
                 traces_additive=traces_additive,
1071
                 tc_trace=tc_trace,
1072
1073
                 trace_scale=trace_scale,
                 sum_input=sum_input,
1074
            )
1075
1076
            self.register_buffer("rest", torch.tensor(rest))
                                                                      # Rest
1077
       voltage.
            self.register_buffer("thresh", torch.tensor(thresh))
                                                                          #
1078
       Spike threshold voltage.
            self.lbound = lbound
1079
1080
            self.register_buffer("r", None)
1081
            self.register_buffer("a", None)
1082
            self.register_buffer("b", None)
1083
            self.register_buffer("c", None)
1084
            self.register_buffer("d", None)
1085
            self.register_buffer("S", None)
1086
            self.register_buffer("excitatory", None)
1087
1088
            if excitatory > 1:
1089
                 excitatory = 1
1090
            elif excitatory < 0:</pre>
1091
                 excitatory = 0
1092
1093
            if excitatory == 1:
1094
                 self.r = torch.rand(n)
1095
                 self.a = 0.02 * torch.ones(n)
1096
                 self.b = 0.2 * torch.ones(n)
1097
                 self.c = -65.0 + 15 * (self.r ** 2)
1098
                 self.d = 8 - 6 * (self.r ** 2)
1099
                 self.S = 0.5 * torch.rand(n, n)
1100
                 self.excitatory = torch.ones(n).byte()
1101
1102
            elif excitatory == 0:
1103
1104
                 self.r = torch.rand(n)
                 self.a = 0.02 + 0.08 * self.r
1105
                 self.b = 0.25 - 0.05 * self.r
1106
                 self.c = -65.0 * torch.ones(n)
1107
                 self.d = 2 * torch.ones(n)
1108
                 self.S = -torch.rand(n, n)
1109
                 self.excitatory = torch.zeros(n).byte()
1111
1112
            else:
1113
                 self.excitatory = torch.zeros(n).byte()
1114
1115
                 ex = int(n * excitatory)
```

```
inh = n - ex
1117
1118
                # init
1119
1120
                self.r = torch.zeros(n)
                self.a = torch.zeros(n)
1121
                self.b = torch.zeros(n)
1122
                self.c = torch.zeros(n)
                self.d = torch.zeros(n)
1124
                self.S = torch.zeros(n, n)
1126
                # excitatory
1127
                self.r[:ex] = torch.rand(ex)
1128
                self.a[:ex] = 0.02 * torch.ones(ex)
1129
                self.b[:ex] = 0.2 * torch.ones(ex)
1130
                self.c[:ex] = -65.0 + 15 * self.r[:ex] ** 2
1131
                self.d[:ex] = 8 - 6 * self.r[:ex] ** 2
1132
                self.S[:, :ex] = 0.5 * torch.rand(n, ex)
1133
                self.excitatory[:ex] = 1
1134
1135
                # inhibitory
1136
                self.r[ex:] = torch.rand(inh)
1137
                self.a[ex:] = 0.02 + 0.08 * self.r[ex:]
1138
                self.b[ex:] = 0.25 - 0.05 * self.r[ex:]
1139
                self.c[ex:] = -65.0 * torch.ones(inh)
1140
                self.d[ex:] = 2 * torch.ones(inh)
1141
                self.S[:, ex:] = -torch.rand(n, inh)
1142
                self.excitatory[ex:] = 0
1143
1144
            self.register_buffer("v", self.rest * torch.ones(n))
                                                                         #
1145
      Neuron voltages.
            self.register_buffer("u", self.b * self.v) # Neuron
1146
      recovery.
1147
       def forward(self, x: torch.Tensor) -> None:
1148
            # language=rst
1149
            .....
1150
            Runs a single simulation step.
1151
1152
            :param x: Inputs to the layer.
1153
            0.0.0
1154
            # Check for spiking neurons.
1156
            self.s = self.v >= self.thresh
1157
            # Voltage and recovery reset.
1158
            self.v = torch.where(self.s, self.c, self.v)
1159
            self.u = torch.where(self.s, self.u + self.d, self.u)
1160
1161
            # Add inter-columnar input.
1162
            if self.s.any():
1163
                x += torch.cat(
1164
                     [self.S[:, self.s[i]].sum(dim=1)[None] for i in
1165
      range(self.s.shape[0])],
                     dim=0,
1166
                )
1167
```

```
1168
            # Apply v and u updates.
1169
            self.v += self.dt * 0.5 * (0.04 * self.v ** 2 + 5 * self.v +
        140 - self.u + x)
1171
            self.v += self.dt * 0.5 * (0.04 * self.v ** 2 + 5 * self.v +
        140 - self.u + x)
            self.u += self.dt * self.a * (self.b * self.v - self.u)
1173
            # Voltage clipping to lower bound.
1174
            if self.lbound is not None:
                self.v.masked_fill_(self.v < self.lbound, self.lbound)</pre>
1176
            super().forward(x)
1178
1179
       def reset_state_variables(self) -> None:
1180
            # language=rst
1181
            0.0.0
1182
            Resets relevant state variables.
1183
            .....
1184
            super().reset_state_variables()
1185
            self.v.fill_(self.rest) # Neuron voltages.
1186
            self.u = self.b * self.v # Neuron recovery.
1187
1188
       def set_batch_size(self, batch_size) -> None:
1189
1190
            # language=rst
            .....
1191
            Sets mini-batch size. Called when layer is added to a
1192
      network.
1194
            :param batch_size: Mini-batch size.
            0.0.0
1195
            super().set_batch_size(batch_size=batch_size)
1196
            self.v = self.rest * torch.ones(batch_size, *self.shape,
1197
      device=self.v.device)
            self.u = self.b * self.v
1198
1199
1200
   class SRMONodes(Nodes):
1201
       # language=rst
1202
        .....
1203
       Layer of simplified spike response model (SRMO) neurons with
1204
      stochastic threshold (escape noise). Adapted from
        '(Vasilaki et al., 2009) <https://intranet.physio.unibe.ch/
1205
      Publikationen/Dokumente/Vasilaki2009PloSComputBio_1.pdf>'_.
        .....
1206
1207
       def __init__(
1208
            self,
1209
            n: Optional[int] = None,
1210
            shape: Optional[Iterable[int]] = None,
1211
            traces: bool = False,
            traces_additive: bool = False,
1213
            tc_trace: Union[float, torch.Tensor] = 20.0,
1214
            trace_scale: Union[float, torch.Tensor] = 1.0,
1215
```

```
sum_input: bool = False,
           thresh: Union[float, torch.Tensor] = -50.0,
1217
           rest: Union[float, torch.Tensor] = -70.0,
1218
1219
           reset: Union[float, torch.Tensor] = -70.0,
           refrac: Union[int, torch.Tensor] = 5,
           tc_decay: Union[float, torch.Tensor] = 10.0,
1221
           lbound: float = None,
           eps_0: Union[float, torch.Tensor] = 1.0,
           rho_0: Union[float, torch.Tensor] = 1.0,
           d_thresh: Union[float, torch.Tensor] = 5.0,
1225
           **kwargs,
1226
       ) \rightarrow None:
            # language=rst
1228
            0.0.0
           Instantiates a layer of SRMO neurons.
1230
            :param n: The number of neurons in the layer.
           :param shape: The dimensionality of the layer.
            :param traces: Whether to record spike traces.
1234
            :param traces_additive: Whether to record spike traces
      additively.
            :param tc_trace: Time constant of spike trace decay.
1236
            :param trace_scale: Scaling factor for spike trace.
1237
            :param sum_input: Whether to sum all inputs.
1238
            :param thresh: Spike threshold voltage.
            :param rest: Resting membrane voltage.
1240
            :param reset: Post-spike reset voltage.
1241
            :param refrac: Refractory (non-firing) period of the neuron.
1242
            :param tc_decay: Time constant of neuron voltage decay.
1243
            :param lbound: Lower bound of the voltage.
1244
            :param eps_0: Scaling factor for pre-synaptic spike
1245
      contributions.
            :param rho_0: Stochastic intensity at threshold.
1246
            :param d_thresh: Width of the threshold region.
1247
           0.0.0
1248
1249
            super().__init__(
                n=n,
1250
1251
                shape=shape,
                traces=traces,
1252
                traces_additive=traces_additive,
1253
                tc_trace=tc_trace,
1254
                trace_scale=trace_scale,
1255
                sum_input=sum_input,
1256
           )
1257
1258
           self.register_buffer("rest", torch.tensor(rest))
                                                                  # Rest
1259
      voltage.
           self.register_buffer("reset", torch.tensor(reset))
                                                                    # Post-
1260
      spike reset voltage.
           self.register_buffer("thresh", torch.tensor(thresh))
                                                                       #
1261
      Spike threshold voltage.
           self.register_buffer(
1262
                "refrac", torch.tensor(refrac)
1263
           ) # Post-spike refractory period.
1264
```

```
self.register_buffer(
1265
                "tc_decay", torch.tensor(tc_decay)
1266
            )
              # Time constant of neuron voltage decay.
1267
1268
            self.register_buffer("decay", torch.tensor(tc_decay))
                                                                        # Set
       in compute_decays.
            self.register_buffer(
1269
                "eps_0", torch.tensor(eps_0)
1270
              # Scaling factor for pre-synaptic spike contributions.
            )
            self.register_buffer(
                "rho_0", torch.tensor(rho_0)
1273
            )
              # Stochastic intensity at threshold.
1274
            self.register_buffer(
1275
                "d_thresh", torch.tensor(d_thresh)
1276
            )
              # Width of the threshold region.
            self.register_buffer("v", torch.FloatTensor())
                                                                 # Neuron
1278
      voltages.
            self.register_buffer(
1279
                "refrac_count", torch.FloatTensor()
1280
           )
               # Refractory period counters.
1281
1282
            self.lbound = lbound # Lower bound of voltage.
1283
1284
       def forward(self, x: torch.Tensor) -> None:
1285
            # language=rst
1286
            .....
1287
            Runs a single simulation step.
1288
1289
            :param x: Inputs to the layer.
1290
            0.0.0
1291
            # Decay voltages.
1292
            self.v = self.decay * (self.v - self.rest) + self.rest
1293
1294
            # Integrate inputs.
1295
            self.v += (self.refrac_count == 0).float() * self.eps_0 * x
1296
1297
            # Compute (instantaneous) probabilities of spiking, clamp
1298
      between 0 and 1 using exponentials.
            # Also known as 'escape noise', this simulates nearby
1299
      neurons.
            self.rho = self.rho_0 * torch.exp((self.v - self.thresh) /
1300
      self.d_thresh)
            self.s_prob = 1.0 - torch.exp(-self.rho * self.dt)
1301
1302
            # Decrement refractory counters.
1303
            self.refrac_count = (self.refrac_count > 0).float() * (
1304
                self.refrac_count - self.dt
1305
            )
1306
1307
            # Check for spiking neurons (spike when probability > some
1308
      random number).
            self.s = torch.rand_like(self.s_prob) < self.s_prob</pre>
1309
            # Refractoriness and voltage reset.
1311
            self.refrac_count.masked_fill_(self.s, self.refrac)
1312
```

```
self.v.masked_fill_(self.s, self.reset)
1314
            # Voltage clipping to lower bound.
1315
1316
            if self.lbound is not None:
                self.v.masked_fill_(self.v < self.lbound, self.lbound)</pre>
1317
1318
            super().forward(x)
1319
1320
       def reset_state_variables(self) -> None:
1321
            # language=rst
            0.0.0
1323
            Resets relevant state variables.
1324
            0.0.0
            super().reset_state_variables()
1326
            self.v.fill_(self.rest) # Neuron voltages.
1327
            self.refrac_count.zero_() # Refractory period counters.
1328
1329
       def compute_decays(self, dt) -> None:
1330
            # language=rst
1331
            0.0.0
            Sets the relevant decays.
            0.0.0
1334
            super().compute_decays(dt=dt)
1335
            self.decay = torch.exp(
1336
                -self.dt / self.tc_decay
            ) # Neuron voltage decay (per timestep).
1338
1339
       def set_batch_size(self, batch_size) -> None:
1340
            # language=rst
1341
            0.0.0
1342
            Sets mini-batch size. Called when layer is added to a
1343
      network.
1344
            :param batch_size: Mini-batch size.
1345
            0.0.0
1346
1347
            super().set_batch_size(batch_size=batch_size)
            self.v = self.rest * torch.ones(batch_size, *self.shape,
1348
      device=self.v.device)
            self.refrac_count = torch.zeros_like(self.v, device=self.
1349
      refrac_count.device)
```

```
Listing B.7: Nodes
```

```
1 from abc import ABC, abstractmethod
2 from typing import Union, Tuple, Optional, Sequence
3
4 import numpy as np
5 import torch
6 from torch.nn import Module, Parameter
7 import torch.nn.functional as F
8 from torch.nn.modules.utils import _pair
9
10 from .nodes import Nodes
11
```

```
12
13 class AbstractConnection(ABC, Module):
      # language=rst
14
      0.0.0
15
      Abstract base method for connections between "Nodes".
16
      .....
17
18
      def __init__(
19
          self,
20
          source: Nodes,
21
          target: Nodes,
22
          nu: Optional[Union[float, Sequence[float]]] = None,
          reduction: Optional[callable] = None,
24
          weight_decay: float = 0.0,
          **kwargs
26
      ) \rightarrow None:
27
          # language=rst
28
          0.0.0
29
          Constructor for abstract base class for connection objects.
30
31
           :param source: A layer of nodes from which the connection
32
     originates.
          :param target: A layer of nodes to which the connection
     connects.
          :param nu: Learning rate for both pre- and post-synaptic
34
     events.
          :param reduction: Method for reducing parameter updates
35
     along the minibatch
               dimension.
36
          :param weight_decay: Constant multiple to decay weights by
37
     on each iteration.
38
          Keyword arguments:
39
40
          :param LearningRule update_rule: Modifies connection
41
     parameters according to
               some rule.
42
          :param float wmin: The minimum value on the connection
43
     weights.
          :param float wmax: The maximum value on the connection
44
     weights.
           :param float norm: Total weight per target neuron
45
     normalization.
          ......
46
          super().__init__()
47
48
          assert isinstance(source, Nodes), "Source is not a Nodes
49
     object"
          assert isinstance(target, Nodes), "Target is not a Nodes
50
     object"
51
          self.source = source
52
          self.target = target
53
54
```

```
self.nu = nu
55
           self.weight_decay = weight_decay
56
           self.reduction = reduction
57
58
           from ..learning import NoOp
59
60
           self.update_rule = kwargs.get("update_rule", NoOp)
61
           self.wmin = kwargs.get("wmin", -np.inf)
62
           self.wmax = kwargs.get("wmax", np.inf)
63
           self.norm = kwargs.get("norm", None)
64
           self.decay = kwargs.get("decay", None)
65
66
           if self.update_rule is None:
67
                self.update_rule = NoOp
68
69
           self.update_rule = self.update_rule(
70
                connection=self,
71
               nu=nu,
                reduction=reduction,
                weight_decay=weight_decay,
74
                **kwargs
75
           )
76
77
       @abstractmethod
78
       def compute(self, s: torch.Tensor) -> None:
79
           # language=rst
80
           .....
81
           Compute pre-activations of downstream neurons given spikes
82
      of upstream neurons.
83
           :param s: Incoming spikes.
84
           0.0.0
85
           pass
86
87
       @abstractmethod
88
       def update(self, **kwargs) -> None:
89
           # language=rst
90
           0.0.0
91
           Compute connection's update rule.
92
93
           Keyword arguments:
94
95
           :param bool learning: Whether to allow connection updates.
96
           :param ByteTensor mask: Boolean mask determining which
97
      weights to clamp to zero.
           0.0.0
98
           learning = kwargs.get("learning", True)
99
100
           if learning:
101
                self.update_rule.update(**kwargs)
102
103
           mask = kwargs.get("mask", None)
104
           if mask is not None:
105
                self.w.masked_fill_(mask, 0)
106
```

```
107
       @abstractmethod
108
      def reset_state_variables(self) -> None:
109
110
           # language=rst
           0.0.0
111
           Contains resetting logic for the connection.
112
           .....
114
           pass
115
116
117 class Connection(AbstractConnection):
      # language=rst
118
       .....
119
       Specifies synapses between one or two populations of neurons.
122
      def __init__(
           self,
124
           source: Nodes,
           target: Nodes,
126
           nu: Optional[Union[float, Sequence[float]]] = None,
           reduction: Optional[callable] = None,
128
           weight_decay: float = 0.0,
129
           **kwargs
130
      ) -> None:
           # language=rst
132
           0.0.0
           Instantiates a :code: 'Connection' object.
134
           :param source: A layer of nodes from which the connection
136
      originates.
           :param target: A layer of nodes to which the connection
137
      connects.
           :param nu: Learning rate for both pre- and post-synaptic
138
      events.
           :param reduction: Method for reducing parameter updates
139
      along the minibatch
               dimension.
140
           :param weight_decay: Constant multiple to decay weights by
141
      on each iteration.
142
143
           Keyword arguments:
144
           :param LearningRule update_rule: Modifies connection
145
      parameters according to
               some rule.
146
           :param torch.Tensor w: Strengths of synapses.
147
           :param torch.Tensor b: Target population bias.
148
           :param float wmin: Minimum allowed value on the connection
149
      weights.
           :param float wmax: Maximum allowed value on the connection
150
      weights.
           :param float norm: Total weight per target neuron
151
      normalization constant.
```

```
0.0.0
152
           super().__init__(source, target, nu, reduction, weight_decay
153
      , **kwargs)
154
           w = kwargs.get("w", None)
155
           if w is None:
156
                if self.wmin == -np.inf or self.wmax == np.inf:
157
                    w = torch.clamp(torch.rand(source.n, target.n), self
158
      .wmin, self.wmax)
                else:
159
                    w = self.wmin + torch.rand(source.n, target.n) * (
160
      self.wmax - self.wmin)
           else:
161
                if self.wmin != -np.inf or self.wmax != np.inf:
162
                    w = torch.clamp(w, self.wmin, self.wmax)
163
164
           self.w = Parameter(w, requires_grad=False)
165
           self.b = Parameter(kwargs.get("b", torch.zeros(target.n)),
166
      requires_grad=False)
167
       def compute(self, s: torch.Tensor) -> torch.Tensor:
168
           # language=rst
169
           0.0.0
170
           Compute pre-activations given spikes using connection
      weights.
172
           :param s: Incoming spikes.
173
           :return: Incoming spikes multiplied by synaptic weights (
174
      with or without
                     decaying spike activation).
175
           .....
176
           # Compute multiplication of spike activations by weights and
       add bias.
           post = s.float().view(s.size(0), -1) @ self.w + self.b
178
           return post.view(s.size(0), *self.target.shape)
179
180
       def update(self, **kwargs) -> None:
181
           # language=rst
182
           0.0.0
183
           Compute connection's update rule.
184
           0.0.0
185
           super().update(**kwargs)
186
187
       def normalize(self) -> None:
188
           # language=rst
189
           0.0.0
190
           Normalize weights so each target neuron has sum of
191
      connection weights equal to
           ''self.norm''.
192
           0.0.0
193
           if self.norm is not None:
194
                w_abs_sum = self.w.abs().sum(0).unsqueeze(0)
195
                w_abs_sum[w_abs_sum == 0] = 1.0
196
               self.w *= self.norm / w_abs_sum
197
```

```
def reset_state_variables(self) -> None:
        Contains resetting logic for the connection.
        super().reset_state_variables()
class Conv2dConnection(AbstractConnection):
    Specifies convolutional synapses between one or two populations
        kernel_size: Union[int, Tuple[int, int]],
        stride: Union[int, Tuple[int, int]] = 1,
        padding: Union[int, Tuple[int, int]] = 0,
```

```
dilation: Union[int, Tuple[int, int]] = 1,
    nu: Optional[Union[float, Sequence[float]]] = None,
    reduction: Optional[callable] = None,
    weight_decay: float = 0.0,
    **kwargs
) -> None:
    # language=rst
    0.0.0
    Instantiates a ''Conv2dConnection'' object.
    :param source: A layer of nodes from which the connection
originates.
     :param target: A layer of nodes to which the connection
connects.
    :param kernel_size: Horizontal and vertical size of
convolutional kernels.
    :param stride: Horizontal and vertical stride for
convolution.
    :param padding: Horizontal and vertical padding for
convolution.
     :param dilation: Horizontal and vertical dilation for
convolution.
    :param nu: Learning rate for both pre- and post-synaptic
events.
    :param reduction: Method for reducing parameter updates
along the minibatch
         dimension.
```

```
:param weight_decay: Constant multiple to decay weights by
239
     on each iteration.
```

240 241

198

199

200

201

202

203 204

205 206 207

208

209

210

212

214

217

218

219

220

223

224

225 226

228 229

230

233

234

236

238

language=rst

0.0.0

0.0.0

language=rst

def __init__(self,

> source: Nodes, target: Nodes,

of neurons.

0.0.0

.....

```
242
           :param LearningRule update_rule: Modifies connection
243
      parameters according to
244
               some rule.
           :param torch.Tensor w: Strengths of synapses.
245
           :param torch.Tensor b: Target population bias.
246
           :param float wmin: Minimum allowed value on the connection
247
      weights.
           :param float wmax: Maximum allowed value on the connection
248
      weights.
           :param float norm: Total weight per target neuron
249
      normalization constant.
           .....
250
           super().__init__(source, target, nu, reduction, weight_decay
251
      , **kwargs)
252
           self.kernel_size = _pair(kernel_size)
253
           self.stride = _pair(stride)
254
           self.padding = _pair(padding)
255
           self.dilation = _pair(dilation)
256
257
           self.in_channels, input_height, input_width = (
258
               source.shape[0],
259
                source.shape[1],
260
                source.shape[2],
261
           )
262
           self.out_channels, output_height, output_width = (
263
                target.shape[0],
264
                target.shape[1],
265
266
                target.shape[2],
           )
267
268
           width = (
269
                input_height - self.kernel_size[0] + 2 * self.padding[0]
270
           ) / self.stride[0] + 1
271
           height = (
                input_width - self.kernel_size[1] + 2 * self.padding[1]
273
           ) / self.stride[1] + 1
274
           shape = (self.in_channels, self.out_channels, int(width),
275
      int(height))
276
           error = (
277
                "Target dimensionality must be (out_channels, ?,"
278
                "(input_height - filter_height + 2 * padding_height) /
279
      stride_height + 1,"
                "(input_width - filter_width + 2 * padding_width) /
280
      stride_width + 1"
           )
281
282
           assert (
283
                target.shape[0] == shape[1]
284
               and target.shape[1] == shape[2]
285
               and target.shape[2] == shape[3]
286
           ), error
287
```

```
288
           w = kwargs.get("w", None)
289
           if w is None:
290
                if self.wmin == -np.inf or self.wmax == np.inf:
291
                    w = torch.clamp(
292
                         torch.rand(self.out_channels, self.in_channels,
293
      *self.kernel_size),
                         self.wmin,
294
                         self.wmax,
295
                    )
296
                else:
297
                    w = (self.wmax - self.wmin) * torch.rand(
298
                         self.out_channels, self.in_channels, *self.
299
      kernel_size
                    )
300
                    w += self.wmin
301
           else:
302
                if self.wmin != -np.inf or self.wmax != np.inf:
303
                    w = torch.clamp(w, self.wmin, self.wmax)
304
305
           self.w = Parameter(w, requires_grad=False)
306
           self.b = Parameter(
307
                kwargs.get("b", torch.zeros(self.out_channels)),
308
      requires_grad=False
309
           )
310
       def compute(self, s: torch.Tensor) -> torch.Tensor:
311
           # language=rst
312
           .....
313
           Compute convolutional pre-activations given spikes using
314
      layer weights.
315
           :param s: Incoming spikes.
316
           :return: Incoming spikes multiplied by synaptic weights (
317
      with or without
                decaying spike activation).
318
           319
           return F.conv2d(
320
                s.float(),
321
                self.w,
322
                self.b,
323
                stride=self.stride,
324
                padding=self.padding,
                dilation=self.dilation,
326
           )
327
328
       def update(self, **kwargs) -> None:
329
           # language=rst
330
           0.0.0
           Compute connection's update rule.
332
           0.0.0
333
           super().update(**kwargs)
334
335
       def normalize(self) -> None:
336
```

```
# language=rst
337
           .....
338
           Normalize weights along the first axis according to total
339
      weight per target
           neuron.
340
           0.0.0
341
           if self.norm is not None:
342
                # get a view and modify in place
343
                w = self.w.view(
344
345
                    self.w.size(0) * self.w.size(1), self.w.size(2) *
      self.w.size(3)
                )
346
347
                for fltr in range(w.size(0)):
348
                    w[fltr] *= self.norm / w[fltr].sum(0)
349
350
       def reset_state_variables(self) -> None:
351
           # language=rst
352
           .....
353
           Contains resetting logic for the connection.
354
           0.0.0
355
           super().reset_state_variables()
356
357
358
  class MaxPool2dConnection(AbstractConnection):
359
       # language=rst
360
       0.0.0
361
       Specifies max-pooling synapses between one or two populations of
362
       neurons by keeping
       online estimates of maximally firing neurons.
363
       .....
364
365
       def __init__(
366
           self,
367
           source: Nodes,
368
369
           target: Nodes,
           kernel_size: Union[int, Tuple[int, int]],
           stride: Union[int, Tuple[int, int]] = 1,
371
           padding: Union[int, Tuple[int, int]] = 0,
372
           dilation: Union[int, Tuple[int, int]] = 1,
373
           **kwargs
374
       ) -> None:
375
           # language=rst
376
           .....
377
           Instantiates a ''MaxPool2dConnection'' object.
378
379
           :param source: A layer of nodes from which the connection
380
      originates.
           :param target: A layer of nodes to which the connection
381
      connects.
           :param kernel_size: Horizontal and vertical size of
382
      convolutional kernels.
           :param stride: Horizontal and vertical stride for
383
      convolution.
```

```
:param padding: Horizontal and vertical padding for
384
      convolution.
           :param dilation: Horizontal and vertical dilation for
385
      convolution.
386
           Keyword arguments:
387
388
           :param decay: Decay rate of online estimates of average
389
      firing activity.
           .....
390
           super().__init__(source, target, None, None, 0.0, **kwargs)
391
392
           self.kernel_size = _pair(kernel_size)
393
           self.stride = _pair(stride)
394
           self.padding = _pair(padding)
395
           self.dilation = _pair(dilation)
396
397
           self.register_buffer("firing_rates", torch.ones(source.shape
398
      ))
399
       def compute(self, s: torch.Tensor) -> torch.Tensor:
400
           # language=rst
401
           0.0.0
402
           Compute max-pool pre-activations given spikes using online
403
      firing rate
           estimates.
404
405
           :param s: Incoming spikes.
406
           :return: Incoming spikes multiplied by synaptic weights (
407
      with or without
                decaying spike activation).
408
           .....
409
           self.firing_rates -= self.decay * self.firing_rates
410
           self.firing_rates += s.float()
411
412
           _, indices = F.max_pool2d(
413
                self.firing_rates,
414
                kernel_size=self.kernel_size,
415
                stride=self.stride,
416
                padding=self.padding,
417
                dilation=self.dilation,
418
                return_indices=True,
419
           )
420
421
           return s.take(indices).float()
422
423
       def update(self, **kwargs) -> None:
424
           # language=rst
425
           0.0.0
426
           Compute connection's update rule.
427
           0.0.0
428
           super().update(**kwargs)
429
430
       def normalize(self) -> None:
431
```

```
# language=rst
432
           .....
433
           No weights -> no normalization.
434
           0.0.0
435
           pass
436
437
       def reset_state_variables(self) -> None:
438
           # language=rst
439
           0.0.0
440
           Contains resetting logic for the connection.
441
           0.0.0
442
           super().reset_state_variables()
443
444
           self.firing_rates = torch.zeros(self.source.shape)
445
446
  class LocalConnection(AbstractConnection):
447
       # language=rst
448
       ......
449
       Specifies a locally connected connection between one or two
450
      populations of neurons.
       0.0.0
451
452
       def __init__(
453
           self,
454
           source: Nodes,
455
           target: Nodes,
456
           kernel_size: Union[int, Tuple[int, int]],
457
           stride: Union[int, Tuple[int, int]],
458
           n_filters: int,
459
           nu: Optional[Union[float, Sequence[float]]] = None,
460
           reduction: Optional[callable] = None,
461
           weight_decay: float = 0.0,
462
           **kwargs
463
       ) \rightarrow None:
464
           # language=rst
465
           .....
466
           Instantiates a ''LocalConnection'' object. Source population
467
       should be
           two-dimensional.
468
469
           Neurons in the post-synaptic population are ordered by
470
      receptive field; that is,
           if there are "'n_conv' neurons in each post-synaptic patch,
471
       then the first
           "n_conv" neurons in the post-synaptic population
472
      correspond to the first
           receptive field, the second "'n_conv" to the second
473
      receptive field, and so on.
474
           :param source: A layer of nodes from which the connection
475
      originates.
           :param target: A layer of nodes to which the connection
476
      connects.
           :param kernel_size: Horizontal and vertical size of
477
```

```
convolutional kernels.
           :param stride: Horizontal and vertical stride for
478
      convolution.
479
           :param n_filters: Number of locally connected filters per
      pre-synaptic region.
           :param nu: Learning rate for both pre- and post-synaptic
480
      events.
           :param reduction: Method for reducing parameter updates
481
      along the minibatch
               dimension.
482
           :param weight_decay: Constant multiple to decay weights by
483
      on each iteration.
484
           Keyword arguments:
485
486
           :param LearningRule update_rule: Modifies connection
487
      parameters according to
               some rule.
488
           :param torch.Tensor w: Strengths of synapses.
489
           :param torch.Tensor b: Target population bias.
490
           :param float wmin: Minimum allowed value on the connection
491
      weights.
           :param float wmax: Maximum allowed value on the connection
492
      weights.
           :param float norm: Total weight per target neuron
493
      normalization constant.
           :param Tuple[int, int] input_shape: Shape of input
494
      population if it's not
               ''[sqrt, sqrt]''.
495
           .....
496
           super().__init__(source, target, nu, reduction, weight_decay
497
      , **kwargs)
498
           kernel_size = _pair(kernel_size)
499
           stride = _pair(stride)
500
501
           self.kernel_size = kernel_size
502
           self.stride = stride
503
           self.n_filters = n_filters
504
505
           shape = kwargs.get("input_shape", None)
506
           if shape is None:
507
               sqrt = int(np.sqrt(source.n))
508
               shape = _pair(sqrt)
509
510
           if kernel_size == shape:
511
               conv_size = [1, 1]
512
           else:
513
               conv_size = (
514
                    int((shape[0] - kernel_size[0]) / stride[0]) + 1,
515
                    int((shape[1] - kernel_size[1]) / stride[1]) + 1,
516
               )
517
518
           self.conv_size = conv_size
519
```

```
520
           conv_prod = int(np.prod(conv_size))
521
           kernel_prod = int(np.prod(kernel_size))
522
523
           assert (
524
               target.n == n_filters * conv_prod
525
           ), "Target layer size must be n_filters * (kernel_size ** 2)
526
      . "
527
           locations = torch.zeros(
528
                kernel_size[0], kernel_size[1], conv_size[0], conv_size
529
      [1]
           ).long()
530
           for c1 in range(conv_size[0]):
531
                for c2 in range(conv_size[1]):
532
                    for k1 in range(kernel_size[0]):
533
                         for k2 in range(kernel_size[1]):
534
                             location = (
535
                                  c1 * stride[0] * shape[1]
536
                                 + c2 * stride[1]
537
                                 + k1 * shape[0]
538
                                 + k2
539
                             )
540
                             locations[k1, k2, c1, c2] = location
541
542
           self.register_buffer("locations", locations.view(kernel_prod
543
      , conv_prod))
           w = kwargs.get("w", None)
544
545
           if w is None:
546
                w = torch.zeros(source.n, target.n)
547
               for f in range(n_filters):
548
                    for c in range(conv_prod):
549
                         for k in range(kernel_prod):
550
                             if self.wmin == -np.inf or self.wmax == np.
551
      inf:
                                  w[self.locations[k, c], f * conv_prod +
552
      c] = np.clip(
                                      np.random.rand(), self.wmin, self.
553
      wmax
                                  )
554
                             else:
555
                                  w [
556
                                      self.locations[k, c], f * conv_prod
557
      + c
                                 ] = self.wmin + np.random.rand() * (self
558
      .wmax - self.wmin)
           else:
559
                if self.wmin != -np.inf or self.wmax != np.inf:
560
                    w = torch.clamp(w, self.wmin, self.wmax)
561
562
           self.w = Parameter(w, requires_grad=False)
563
564
           self.register_buffer("mask", self.w == 0)
565
```

```
566
           self.b = Parameter(kwargs.get("b", torch.zeros(target.n)),
567
      requires_grad=False)
568
           if self.norm is not None:
569
                self.norm *= kernel_prod
570
571
       def compute(self, s: torch.Tensor) -> torch.Tensor:
572
           # language=rst
573
           .....
574
           Compute pre-activations given spikes using layer weights.
575
576
           :param s: Incoming spikes.
577
           :return: Incoming spikes multiplied by synaptic weights (
578
      with or without
                decaying spike activation).
579
           .....
580
           # Compute multiplication of pre-activations by connection
581
      weights.
           if self.w.shape[0] == self.source.n and self.w.shape[1] ==
582
      self.target.n:
                return s.float().view(s.size(0), -1) @ self.w + self.b
583
           else:
584
                a_post = (
585
                    s.float().view(s.size(0), -1)
586
                    @ self.w.view(self.source.n, self.target.n)
587
                    + self.b
588
                )
589
                return a_post.view(*self.target.shape)
590
591
       def update(self, **kwargs) -> None:
592
           # language=rst
593
           .....
594
           Compute connection's update rule.
595
596
           Keyword arguments:
597
598
           :param ByteTensor mask: Boolean mask determining which
599
      weights to clamp to zero.
           ......
600
           if kwargs["mask"] is None:
601
                kwargs["mask"] = self.mask
602
603
           super().update(**kwargs)
604
605
       def normalize(self) -> None:
606
           # language=rst
607
           ......
608
           Normalize weights so each target neuron has sum of
609
      connection weights equal to
           ''self.norm''.
610
           .....
611
           if self.norm is not None:
612
                w = self.w.view(self.source.n, self.target.n)
613
```

```
w *= self.norm / self.w.sum(0).view(1, -1)
614
615
       def reset_state_variables(self) -> None:
616
617
           # language=rst
           0.0.0
618
           Contains resetting logic for the connection.
619
           0.0.0
620
           super().reset_state_variables()
621
622
623
  class MeanFieldConnection(AbstractConnection):
624
       # language=rst
625
       0.0.0
626
       A connection between one or two populations of neurons which
627
      computes a summary of
       the pre-synaptic population to use as weighted input to the post
628
      -synaptic
       population.
629
       0.0.0
630
631
       def __init__(
632
633
           self,
           source: Nodes,
634
           target: Nodes,
635
           nu: Optional[Union[float, Sequence[float]]] = None,
636
           weight_decay: float = 0.0,
637
           **kwargs
638
       ) -> None:
639
           # language=rst
640
           .....
641
           Instantiates a :code: 'MeanFieldConnection' object.
642
           :param source: A layer of nodes from which the connection
643
      originates.
           :param target: A layer of nodes to which the connection
644
      connects.
           :param nu: Learning rate for both pre- and post-synaptic
645
      events.
           :param weight_decay: Constant multiple to decay weights by
646
      on each iteration.
           Keyword arguments:
647
           :param LearningRule update_rule: Modifies connection
648
      parameters according to
                some rule.
649
           :param torch.Tensor w: Strengths of synapses.
650
           :param float wmin: Minimum allowed value on the connection
651
      weights.
           :param float wmax: Maximum allowed value on the connection
652
      weights.
           :param float norm: Total weight per target neuron
653
      normalization constant.
           0.0.0
654
           super().__init__(source, target, nu, weight_decay, **kwargs)
655
656
           w = kwargs.get("w", None)
657
```

```
if w is None:
658
                if self.wmin == -np.inf or self.wmax == np.inf:
659
                    w = torch.clamp((torch.randn(1)[0] + 1) / 10, self.
660
      wmin, self.wmax)
                else:
661
                    w = self.wmin + ((torch.randn(1)[0] + 1) / 10) * (
662
      self.wmax - self.wmin)
           else:
663
                if self.wmin != -np.inf or self.wmax != np.inf:
664
                    w = torch.clamp(w, self.wmin, self.wmax)
665
666
           self.w = Parameter(w, requires_grad=False)
667
668
       def compute(self, s: torch.Tensor) -> torch.Tensor:
669
           # language=rst
670
           0.0.0
671
           Compute pre-activations given spikes using layer weights.
672
           :param s: Incoming spikes.
673
           :return: Incoming spikes multiplied by synaptic weights (
674
      with or without
                decaying spike activation).
675
           ......
676
           # Compute multiplication of mean-field pre-activation by
677
      connection weights.
           return s.float().mean() * self.w
678
679
       def update(self, **kwargs) -> None:
680
           # language=rst
681
           ......
682
           Compute connection's update rule.
683
           684
           super().update(**kwargs)
685
686
       def normalize(self) -> None:
687
           # language=rst
688
           .....
689
           Normalize weights so each target neuron has sum of
690
      connection weights equal to
           ''self.norm''.
691
           0.0.0
692
           if self.norm is not None:
693
                self.w = self.w.view(1, self.target.n)
694
                self.w *= self.norm / self.w.sum()
695
                self.w = self.w.view(1, *self.target.shape)
696
697
       def reset_state_variables(self) -> None:
698
           # language=rst
699
           0.0.0
700
           Contains resetting logic for the connection.
701
           0.0.0
702
           super().reset_state_variables()
703
704
705
706 class SparseConnection(AbstractConnection):
```

```
# language=rst
707
       .....
708
      Specifies sparse synapses between one or two populations of
709
      neurons.
       .....
710
      def __init__(
712
           self,
713
           source: Nodes,
714
           target: Nodes,
715
           nu: Optional[Union[float, Sequence[float]]] = None,
716
           reduction: Optional[callable] = None,
717
           weight_decay: float = None,
718
           **kwargs
719
      ) \rightarrow None:
720
           # language=rst
           0.0.0
           Instantiates a :code: 'Connection' object with sparse weights
724
           :param source: A layer of nodes from which the connection
      originates.
           :param target: A layer of nodes to which the connection
726
      connects.
           :param nu: Learning rate for both pre- and post-synaptic
727
      events.
           :param reduction: Method for reducing parameter updates
728
      along the minibatch
               dimension.
729
           :param weight_decay: Constant multiple to decay weights by
730
      on each iteration.
           Keyword arguments:
           :param torch.Tensor w: Strengths of synapses.
734
           :param float sparsity: Fraction of sparse connections to use
735
           :param LearningRule update_rule: Modifies connection
736
      parameters according to
               some rule.
737
           :param float wmin: Minimum allowed value on the connection
738
      weights.
           :param float wmax: Maximum allowed value on the connection
739
      weights.
           :param float norm: Total weight per target neuron
740
      normalization constant.
           0.0.0
741
           super().__init__(source, target, nu, reduction, weight_decay
742
      , **kwargs)
743
           w = kwargs.get("w", None)
744
           self.sparsity = kwargs.get("sparsity", None)
745
746
           assert (
747
```

w is not None 748 and self.sparsity is None 749 or w is None 750 751 and self.sparsity is not None), 'Only one of "weights" or "sparsity" must be specified' 752 753 if w is None and self.sparsity is not None: 754 i = torch.bernoulli(755 1 - self.sparsity * torch.ones(*source.shape, * 756 target.shape)) 757 if self.wmin == -np.inf or self.wmax == np.inf: 758 v = torch.clamp(759 torch.rand(*source.shape, *target.shape)[i.byte 760 ()], self.wmin, 761 self.wmax, 762) 763 else: 764 v = self.wmin + torch.rand(*source.shape, *target. 765 shape)[i.byte()] * (self.wmax - self.wmin 766) 767 w = torch.sparse.FloatTensor(i.nonzero().t(), v) 768 elif w is not None and self.sparsity is None: 769 assert w.is_sparse, "Weight matrix is not sparse (see 770 torch.sparse module)" if self.wmin != -np.inf or self.wmax != np.inf: 771 w = torch.clamp(w, self.wmin, self.wmax) 772 773 self.w = Parameter(w, requires_grad=False) 774 def compute(self, s: torch.Tensor) -> torch.Tensor: 776 # language=rst 777 0.0.0 778 Compute convolutional pre-activations given spikes using 779 layer weights. 780 :param s: Incoming spikes. 781 :return: Incoming spikes multiplied by synaptic weights (782 with or without decaying spike activation). 783 784 return torch.mm(self.w, s.unsqueeze(-1).float()).squeeze(-1) 785 786 def update(self, **kwargs) -> None: 787 # language=rst 788 0.0.0 789 Compute connection's update rule. 790 0.0.0 791 pass 792 793 def normalize(self) -> None: 794 # language=rst 795

```
0.0.0
796
            Normalize weights along the first axis according to total
797
      weight per target
798
            neuron.
            0.0.0
799
            pass
800
801
       def reset_state_variables(self) -> None:
802
            # language=rst
803
            .....
804
            Contains resetting logic for the connection.
805
            0.0.0
806
            super().reset_state_variables()
807
```

Listing B.8: Topology

```
1 import os
2 import torch
3 import numpy as np
1
5 from abc import ABC
6 from typing import Union, Optional, Iterable, Dict
8 from .nodes import Nodes
9 from .topology import AbstractConnection
10
11
12 class AbstractMonitor(ABC):
      # language=rst
13
      ......
14
      Abstract base class for state variable monitors.
15
      ......
16
17
18
19 class Monitor(AbstractMonitor):
      # language=rst
20
      0.0.0
21
      Records state variables of interest.
      .....
23
24
      def __init__(
25
           self,
26
          obj: Union[Nodes, AbstractConnection],
27
           state_vars: Iterable[str],
28
           time: Optional[int] = None,
29
          batch_size: int = 1,
30
      ):
31
          # language=rst
32
           .....
33
          Constructs a "Monitor" object.
34
35
           :param obj: An object to record state variables from during
36
     network simulation.
          :param state_vars: Iterable of strings indicating names of
37
```

```
state variables to
               record.
38
           :param time: If not ''None'', pre-allocate memory for state
39
     variable recording.
           0.0.0
40
           super().__init__()
41
42
           self.obj = obj
43
           self.state_vars = state_vars
44
           self.time = time
45
           self.batch_size = batch_size
46
47
           # Deal with time later, the same underlying list is used
48
           self.recording = {v: [] for v in self.state_vars}
49
50
      def get(self, var: str) -> torch.Tensor:
51
           # language=rst
52
           .......
53
           Return recording to user.
54
55
           :param var: State variable recording to return.
56
           :return: Tensor of shape ''[time, n_1, ..., n_k]'', where
57
      ``[n_1, ..., n_k]`` is
               the shape of the recorded state variable.
58
           .....
59
           return torch.cat(self.recording[var], 0)
60
61
      def record(self) -> None:
62
           # language=rst
63
           .....
64
           Appends the current value of the recorded state variables to
65
      the recording.
           .....
66
           for v in self.state_vars:
67
                data = getattr(self.obj, v).unsqueeze(0)
68
                self.recording[v].append(data.detach().clone())
69
70
           # remove the oldest element (first in the list)
71
           if self.time is not None:
                for v in self.state_vars:
73
                    if len(self.recording[v]) > self.time:
74
75
                         self.recording[v].pop(0)
76
      def reset_state_variables(self) -> None:
77
           # language=rst
78
           0.0.0
79
           Resets recordings to empty ''torch.Tensor''s.
80
           0.0.0
81
           self.recording = {v: [] for v in self.state_vars}
82
83
84
85 class NetworkMonitor(AbstractMonitor):
      # language=rst
86
      \mathbf{H}_{\mathbf{H}} = \mathbf{H}_{\mathbf{H}}
87
```

```
Record state variables of all layers and connections.
88
       .....
89
90
91
      def __init__(
           self,
92
           network: "Network",
93
           layers: Optional[Iterable[str]] = None,
94
           connections: Optional[Iterable[str]] = None,
95
           state_vars: Optional[Iterable[str]] = None,
96
           time: Optional[int] = None,
97
      ):
98
           # language=rst
99
           .....
100
           Constructs a ''NetworkMonitor'' object.
101
102
           :param network: Network to record state variables from.
103
           :param layers: Layers to record state variables from.
104
           :param connections: Connections to record state variables
105
      from.
           :param state_vars: List of strings indicating names of state
106
       variables to
               record.
107
           :param time: If not ''None'', pre-allocate memory for state
108
      variable recording.
           0.0.0
109
           super().__init__()
110
111
           self.network = network
112
           self.layers = layers if layers is not None else list(self.
      network.layers.keys())
           self.connections = (
114
               connections
115
               if connections is not None
116
               else list(self.network.connections.keys())
           )
118
           self.state_vars = state_vars if state_vars is not None else
119
      ("v", "s", "w")
           self.time = time
120
           if self.time is not None:
               self.i = 0
123
124
           # Initialize empty recording.
125
           self.recording = {k: {} for k in self.layers + self.
126
      connections}
127
           # If no simulation time is specified, specify 0-dimensional
128
      recordings.
           if self.time is None:
129
               for v in self.state_vars:
130
                    for l in self.layers:
                        if hasattr(self.network.layers[1], v):
                             self.recording[1][v] = torch.Tensor()
134
```

for c in self.connections: if hasattr(self.network.connections[c], v): 136 self.recording[c][v] = torch.Tensor() 138 # If simulation time is specified, pre-allocate recordings 139 in memory for speed. else: 140 for v in self.state_vars: 141 for l in self.layers: 142 143 if hasattr(self.network.layers[1], v): self.recording[1][v] = torch.zeros(144 self.time, *getattr(self.network.layers[145 1], v).size()) 146 147 for c in self.connections: 148 if hasattr(self.network.connections[c], v): 149 self.recording[c][v] = torch.zeros(150 self.time, *getattr(self.network. connections[c], v).size()) 152 153 def get(self) -> Dict[str, Dict[str, Union[Nodes, 154 AbstractConnection]]]: # language=rst 155 156 Return entire recording to user. 157 158 :return: Dictionary of dictionary of all layers' and connections' recorded state variables. 160 0.0.0 161 return self.recording 162 163 def record(self) -> None: 164 165 # language=rst 166 Appends the current value of the recorded state variables to 167 the recording. 168 if self.time is None: 169 for v in self.state_vars: 170 for l in self.layers: if hasattr(self.network.layers[1], v): 172 data = getattr(self.network.layers[1], v). 173 unsqueeze(0).float() self.recording[1][v] = torch.cat(174 (self.recording[1][v], data), 0) 176 177 for c in self.connections: 178 if hasattr(self.network.connections[c], v): 179 data = getattr(self.network.connections[c], 180 v).unsqueeze(0)

self.recording[c][v] = torch.cat(181 (self.recording[c][v], data), 0 182) 183 184 else: 185 for v in self.state_vars: 186 for l in self.layers: 187 if hasattr(self.network.layers[1], v): 188 data = getattr(self.network.layers[1], v). 189 float().unsqueeze(0) self.recording[1][v] = torch.cat(190 (self.recording[1][v][1:].type(data.type 191 ()), data), 0) 192 193 for c in self.connections: 194 if hasattr(self.network.connections[c], v): 195 data = getattr(self.network.connections[c], 196 v).unsqueeze(0) self.recording[c][v] = torch.cat(197 (self.recording[c][v][1:].type(data.type 198 ()), data), 0) 199 200 self.i += 1201 202 def save(self, path: str, fmt: str = "npz") -> None: 203 # language=rst 204 205 Write the recording dictionary out to file. 206 207 :param path: The directory to which to write the monitor's 208 recording. :param fmt: Type of file to write to disk. One of '' pickle 209 "'' or '''npz"''. 210 if not os.path.exists(os.path.dirname(path)): os.makedirs(os.path.dirname(path)) if fmt == "npz": 214 # Build a list of arrays to write to disk. $\operatorname{arrays} = \{\}$ 216 for o in self.recording: if type(o) == tuple: 218 arrays.update(219 { 220 "_".join(["-".join(o), v]): self. recording[o][v] for v in self.recording[o] } 223) 224 elif type(o) == str: 225 arrays.update(226 {

"_".join([o, v]): self.recording[o][v] 228 for v in self.recording[o] 229 } 230) 231 np.savez_compressed(path, **arrays) 234 elif fmt == "pickle": with open(path, "wb") as f: 236 torch.save(self.recording, f) 238 def reset_state_variables(self) -> None: 239 # language=rst 240 0.0.0 241 Resets recordings to empty 'torch.Tensors''. 242 0.0.0 243 # Reset to empty recordings 244 self.recording = {k: {} for k in self.layers + self. 245 connections} 246 if self.time is not None: 247 self.i = 0248 249 # If no simulation time is specified, specify O-dimensional 250 recordings. if self.time is None: 251 for v in self.state_vars: 252 for l in self.layers: 253 if hasattr(self.network.layers[1], v): 254 self.recording[1][v] = torch.Tensor() 255 256 for c in self.connections: 257 if hasattr(self.network.connections[c], v): 258 self.recording[c][v] = torch.Tensor() 259 260 # If simulation time is specified, pre-allocate recordings 261 in memory for speed. else: 262 for v in self.state_vars: 263 for l in self.layers: 264 if hasattr(self.network.layers[1], v): 265 self.recording[1][v] = torch.zeros(266 self.time, *getattr(self.network.layers[267 1], v).size()) 268 269 for c in self.connections: 270 if hasattr(self.network.connections[c], v): self.recording[c][v] = torch.zeros(272 self.time, *getattr(self.network.layers[273 c], v).size()) 274

Listing B.9: Monitors

B.4 Pipeline

```
1 from .environment_pipeline import EnvironmentPipeline
2 from .base_pipeline import BasePipeline
3 from .dataloader_pipeline import DataLoaderPipeline,
        TorchVisionDatasetPipeline
4 from . import action
```

Listing B.10: Initialization

```
1 import itertools
2 from typing import Callable, Optional, Tuple, Dict
4 import torch
6 from .base_pipeline import BasePipeline
7 from ... analysis.pipeline_analysis import MatplotlibAnalyzer
8 from .. environment import Environment
9 from .. network import Network
10 from ...network.nodes import AbstractInput
11 from ...network.monitors import Monitor
12
13
14 class EnvironmentPipeline(BasePipeline):
     # language=rst
15
      0.0.0
16
      Abstracts the interaction between "Network", "Environment",
17
     and environment
     feedback action.
18
      ......
19
20
      def __init__(
          self,
          network: Network,
          environment: Environment,
24
          action_function: Optional[Callable] = None,
25
          **kwargs,
26
      ):
27
          # language=rst
28
          .....
29
          Initializes the pipeline.
30
31
          :param network: Arbitrary network object.
32
33
          :param environment: Arbitrary environment.
          :param action_function: Function to convert network outputs
34
     into environment
              inputs.
35
36
          Keyword arguments:
37
38
          :param int num_episodes: Number of episodes to train for.
39
     Defaults to 100.
          :param str output: String name of the layer from which to
40
     take output.
```

```
:param int render_interval: Interval to render the
41
     environment.
          :param int reward_delay: How many iterations to delay
42
     delivery of reward.
          :param int time: Time for which to run the network. Defaults
43
      to the network's
               timestep.
44
          .....
45
          super().__init__(network, **kwargs)
46
47
          self.episode = 0
48
49
          self.env = environment
50
          self.action_function = action_function
51
52
          self.accumulated_reward = 0.0
53
          self.reward_list = []
54
55
          # Setting kwargs.
56
          self.num_episodes = kwargs.get("num_episodes", 100)
57
          self.output = kwargs.get("output", None)
58
          self.render_interval = kwargs.get("render_interval", None)
59
          self.reward_delay = kwargs.get("reward_delay", None)
60
          self.time = kwargs.get("time", int(network.dt))
61
62
          if self.reward_delay is not None:
63
               assert self.reward_delay > 0
64
               self.rewards = torch.zeros(self.reward_delay)
65
66
          # Set up for multiple layers of input layers.
67
          self.inputs = [
68
               name
69
               for name, layer in network.layers.items()
70
               if isinstance(layer, AbstractInput)
71
          ٦
          self.action = None
74
75
          self.voltage_record = None
76
          self.threshold_value = None
77
          self.reward_plot = None
78
79
          self.first = True
80
          self.analyzer = MatplotlibAnalyzer(**self.plot_config)
81
82
          if self.output is not None:
83
               self.network.add_monitor(
84
                   Monitor(self.network.layers[self.output], ["s"]),
85
     self.output
               )
86
87
               self.spike_record = {
88
                   self.output: torch.zeros((self.time, self.env.
89
     action_space.n))
```

```
}
90
91
       def init_fn(self) -> None:
92
93
           pass
94
       def train(self, **kwargs) -> None:
95
           # language=rst
96
           .....
97
           Trains for the specified number of episodes. Each episode
98
      can be of arbitrary
           length.
99
           0.0.0
100
           while self.episode < self.num_episodes:</pre>
101
                self.reset_state_variables()
102
103
                for _ in itertools.count():
104
                    obs, reward, done, info = self.env_step()
105
106
                    self.step((obs, reward, done, info), **kwargs)
107
108
                    if done:
109
                        break
110
111
                print(
                    f"Episode: {self.episode} - "
                    f"accumulated reward: {self.accumulated_reward:.2f}"
114
                )
                self.episode += 1
116
       def env_step(self) -> Tuple[torch.Tensor, float, bool, Dict]:
118
           # language=rst
119
           0.0.0
120
           Single step of the environment which includes rendering,
121
      getting and performing
           the action, and accumulating/delaying rewards.
122
           :return: An OpenAI 'gym'' compatible tuple with modified
124
      reward and info.
           0.0.0
125
           # Render game.
126
           if (
                self.render_interval is not None
128
                and self.step_count % self.render_interval == 0
129
           ):
130
                self.env.render()
131
           # Choose action based on output neuron spiking.
           if self.action_function is not None:
134
                self.action = self.action_function(self, output=self.
135
      output)
136
           # Run a step of the environment.
           obs, reward, done, info = self.env.step(self.action)
138
139
```

```
# Set reward in case of delay.
140
           if self.reward_delay is not None:
141
                self.rewards = torch.tensor([reward, *self.rewards[1:]])
142
      .float()
                reward = self.rewards[-1]
143
144
           # Accumulate reward.
145
           self.accumulated_reward += reward
146
147
           info["accumulated_reward"] = self.accumulated_reward
148
149
           return obs, reward, done, info
150
151
       def step_(
           self, gym_batch: Tuple[torch.Tensor, float, bool, Dict], **
      kwargs
       ) \rightarrow None:
154
           # language=rst
           .....
156
           Run a single iteration of the network and update it and the
157
      reward list when
           done.
158
159
           :param gym_batch: An OpenAI ''gym'' compatible tuple.
160
           .....
161
           obs, reward, done, info = gym_batch
162
163
           # Place the observations into the inputs.
164
           obs_shape = [1] * len(obs.shape[1:])
165
           inputs = {k: obs.repeat(self.time, *obs_shape) for k in self
166
      .inputs}
167
           # Run the network on the spike train-encoded inputs.
168
           self.network.run(inputs=inputs, time=self.time, reward=
169
      reward, **kwargs)
170
           if self.output is not None:
                self.spike_record[self.output] = (
                    self.network.monitors[self.output].get("s").float()
                )
174
175
           if done:
176
                if self.network.reward_fn is not None:
                    self.network.reward_fn.update(
178
                         accumulated_reward=self.accumulated_reward,
179
                        steps=self.step_count,
180
                        **kwargs,
181
                    )
182
                self.reward_list.append(self.accumulated_reward)
183
184
       def reset_state_variables(self) -> None:
185
           # language=rst
186
           .....
187
```

Reset the pipeline.

```
0.0.0
189
           self.env.reset()
190
           self.network.reset_state_variables()
191
192
           self.accumulated_reward = 0.0
           self.step_count = 0
193
194
      def plots(self, gym_batch: Tuple[torch.Tensor, float, bool, Dict
195
      ], *args) -> None:
           # language=rst
196
           .....
197
           Plot the encoded input, layer spikes, and layer voltages.
198
199
           :param gym_batch: An OpenAI ''gym'' compatible tuple.
200
           0.0.0
201
           obs, reward, done, info = gym_batch
202
203
           for key, item in self.plot_config.items():
204
               if key == "obs_step" and item is not None:
205
                    if self.step_count % item == 0:
206
                        self.analyzer.plot_obs(obs[0, ...].sum(0))
207
               elif key == "data_step" and item is not None:
208
                    if self.step_count % item == 0:
209
                        self.analyzer.plot_spikes(self.get_spike_data())
210
                        self.analyzer.plot_voltages(*self.
      get_voltage_data())
               elif key == "reward_eps" and item is not None:
                    if self.episode % item == 0 and done:
213
                        self.analyzer.plot_reward(self.reward_list)
214
           self.analyzer.finalize_step()
216
```

Listing B.11: Environmental pipeline

```
1 import time
2 from typing import Tuple, Dict, Any
4 import torch
5 from torch._six import container_abcs, string_classes
6
7 from ...network import Network
8 from ...network.monitors import Monitor
9
10
11 def recursive_to(item, device):
      # language=rst
12
      0.0.0
14
      Recursively transfers everything contained in item to the target
      device.
15
16
      :param item: An individual tensor or container of tensors.
17
      :param device: ''torch.device'' pointing to ''"cuda"'' or ''"cpu
18
     11 C C
19
      :return: A version of the item that has been sent to a device.
20
```

```
elif isinstance(item, (string_classes, int, float, bool)):
```

```
25
          return item
26
      elif isinstance(item, container_abcs.Mapping):
27
          return {key: recursive_to(item[key], device) for key in item
28
     }
      elif isinstance(item, tuple) and hasattr(item, "_fields"):
29
          return type(item)(*(recursive_to(i, device) for i in item))
30
      elif isinstance(item, container_abcs.Sequence):
31
          return [recursive_to(i, device) for i in item]
      else:
33
          raise NotImplementedError(f"Target type {type(item)} not
34
     supported.")
35
36
37 class BasePipeline:
      # language=rst
38
      .....
39
      A generic pipeline that handles high level functionality.
40
      0.0.0
41
42
      def __init__(self, network: Network, **kwargs) -> None:
43
          # language=rst
44
          0.0.0
45
          Initializes the pipeline.
46
47
          :param network: Arbitrary network object, will be managed by
48
      the
               "BasePipeline" class.
49
50
          Keyword arguments:
51
52
          :param int save_interval: How often to save the network to
53
     disk.
          :param str save_dir: Directory to save network object to.
54
          :param Dict[str, Any] plot_config: Dict containing the plot
55
     configuration.
              Includes length, type (''color"'' or ''line"''), and
56
     interval per plot
               type.
57
          :param int print_interval: Interval to print text output.
58
          :param bool allow_gpu: Allows automatic transfer to the GPU.
59
          0.0.0
60
          self.network = network
61
62
          # Network saving handles caching of intermediate results.
63
          self.save_dir = kwargs.get("save_dir", "network.pt")
64
          self.save_interval = kwargs.get("save_interval", None)
65
66
          # Handles plotting of all layer spikes and voltages.
67
          # This constructs monitors at every level.
68
```

0.0.0

if isinstance(item, torch.Tensor):

return item.to(device)

21

```
self.plot_config = kwargs.get(
69
                "plot_config", {"data_step": None, "data_length": 10}
70
           )
72
           if self.plot_config["data_step"] is not None:
               for l in self.network.layers:
74
                    self.network.add_monitor(
75
                        Monitor(
76
                             self.network.layers[1], "s", self.
77
      plot_config["data_length"]
                        ),
78
                        name=f"{1}_spikes",
79
                    )
80
                    if hasattr(self.network.layers[1], "v"):
81
                        self.network.add_monitor(
82
                             Monitor(
83
                                 self.network.layers[1], "v", self.
84
      plot_config["data_length"]
                             ),
85
                             name=f"{1}_voltages",
86
                        )
87
88
           self.print_interval = kwargs.get("print_interval", None)
89
           self.test_interval = kwargs.get("test_interval", None)
90
           self.step_count = 0
91
           self.init_fn()
92
           self.clock = time.time()
93
           self.allow_gpu = kwargs.get("allow_gpu", True)
94
95
           if torch.cuda.is_available() and self.allow_gpu:
96
               self.device = torch.device("cuda")
97
           else:
98
                self.device = torch.device("cpu")
99
100
           self.network.to(self.device)
101
102
       def reset_state_variables(self) -> None:
103
           # language=rst
104
           0.0.0
105
           Reset the pipeline.
106
           ......
107
           self.network.reset_state_variables()
108
           self.step_count = 0
109
110
       def step(self, batch: Any, **kwargs) -> Any:
111
           # language=rst
           ......
           Single step of any pipeline at a high level.
114
115
           :param batch: A batch of inputs to be handed to the ''step_
116
      () '' function.
                           Standard in subclasses of ''BasePipeline''.
           :return: The output from the subclass's 'step_()' method,
118
      which could be
```

```
anything. Passed to plotting to accommodate this.
119
           .....
120
           self.step_count += 1
121
122
           batch = recursive_to(batch, self.device)
123
           step_out = self.step_(batch, **kwargs)
124
125
           if (
126
                self.print_interval is not None
                and self.step_count % self.print_interval == 0
128
           ):
129
                print(
130
                    f"Iteration: {self.step_count} (Time: {time.time() -
       self.clock:.4f})"
                )
                self.clock = time.time()
134
           self.plots(batch, step_out)
136
           if self.save_interval is not None and self.step_count % self
      .save_interval == 0:
                self.network.save(self.save_dir)
138
139
           if self.test_interval is not None and self.step_count % self
140
      .test_interval == 0:
                self.test()
141
142
           return step_out
143
144
       def get_spike_data(self) -> Dict[str, torch.Tensor]:
145
           # language=rst
146
           0.0.0
147
           Get the spike data from all layers in the pipeline's network
148
149
           :return: A dictionary containing all spike monitors from the
150
       network.
           .....
151
           return {
152
                1: self.network.monitors[f"{1}_spikes"].get("s")
153
                for l in self.network.layers
154
           }
155
156
       def get_voltage_data(
157
           self
158
       ) -> Tuple[Dict[str, torch.Tensor], Dict[str, torch.Tensor]]:
159
           # language=rst
160
           0.0.0
161
           Get the voltage data and threshold value from all applicable
162
       layers in the
           pipeline's network.
163
164
           :return: Two dictionaries containing the voltage data and
165
      threshold values from
```

```
the network.
166
           .....
167
           voltage_record = {}
168
169
           threshold_value = {}
           for l in self.network.layers:
170
                if hasattr(self.network.layers[1], "v"):
171
                    voltage_record[1] = self.network.monitors[f"{1}
172
      _voltages"].get("v")
               if hasattr(self.network.layers[1], "thresh"):
173
                    threshold_value[1] = self.network.layers[1].thresh
174
175
           return voltage_record, threshold_value
176
       def step_(self, batch: Any, **kwargs) -> Any:
178
           # language=rst
179
           0.0.0
180
           Perform a pass of the network given the input batch.
181
182
           :param batch: The current batch. This could be anything as
183
      long as the subclass
                agrees upon the format in some way.
184
           :return: Any output that is need for recording purposes.
185
           0.0.0
186
           raise NotImplementedError("You need to provide a step_
187
      method.")
188
       def train(self) -> None:
189
           # language=rst
190
           0.0.0
191
           A fully self-contained training loop.
192
           193
           raise NotImplementedError("You need to provide a train
194
      method.")
195
       def test(self) -> None:
196
197
           # language=rst
           0.0.0
198
           A fully self contained test function.
199
           0.0.0
200
           raise NotImplementedError("You need to provide a test method
201
      .")
202
       def init_fn(self) -> None:
203
           # language=rst
204
           0.0.0
205
           Placeholder function for subclass-specific actions that need
206
       to
           happen during the construction of the "BasePipeline".
207
208
           raise NotImplementedError("You need to provide an init_fn
209
      method.")
       def plots(self, batch: Any, step_out: Any) -> None:
           # language=rst
```

213 """ Create any plots and logs for a step given the input batch and step output.
215
216 :param batch: The current batch. This could be anything as long as the subclass
217 agrees upon the format in some way.
218 :param step_out: The output from the ''step_()'' method.
219 raise NotImplementedError("You need to provide a plots method.")

Listing B.12: Base pipeline

```
1 from typing import Optional, Dict
2
3 import torch
4 from torch.utils.data import Dataset
5 from tqdm import tqdm
6
7 from ...network import Network
8 from .base_pipeline import BasePipeline
9 from ..analysis.pipeline_analysis import PipelineAnalyzer
10 from ...datasets import DataLoader
11
12
13 class DataLoaderPipeline(BasePipeline):
14
     # language=rst
      0.0.0
15
      A generic 'DataLoader'' pipeline that leverages the ''torch.
16
     utils.data'' setup.
     This still needs to be subclassed for specific implementations
17
     for functions given
      the dataset that will be used. An example can be seen in
18
      ' TorchVisionDatasetPipeline ' '.
19
      0.0.0
20
21
      def __init__(
22
23
          self,
          network: Network,
24
          train_ds: Dataset,
25
          test_ds: Optional[Dataset] = None,
26
          **kwargs
27
      ) \rightarrow None:
28
          # language=rst
29
          .....
30
31
          Initializes the pipeline.
32
          :param network: Arbitrary ''network'' object.
33
          :param train_ds: Arbitrary ''torch.utils.data.Dataset''
34
     object.
           :param test_ds: Arbitrary ''torch.utils.data.Dataset''
35
     object.
          0.0.0
36
```

```
super().__init__(network, **kwargs)
37
38
          self.train_ds = train_ds
39
40
          self.test_ds = test_ds
41
          self.num_epochs = kwargs.get("num_epochs", 10)
42
          self.batch_size = kwargs.get("batch_size", 1)
43
          self.num_workers = kwargs.get("num_workers", 0)
44
          self.pin_memory = kwargs.get("pin_memory", True)
45
          self.shuffle = kwargs.get("shuffle", True)
46
47
      def train(self) -> None:
48
          # language=rst
49
          0.0.0
50
          Training loop that runs for the set number of epochs and
51
     creates a new
          "DataLoader" at each epoch.
52
          0.0.0
53
          for epoch in range(self.num_epochs):
54
               train_dataloader = DataLoader(
55
                   self.train_ds,
56
                   batch_size=self.batch_size,
57
                   num_workers=self.num_workers,
58
                   pin_memory=self.pin_memory,
59
                   shuffle=self.shuffle,
60
               )
61
62
               for step, batch in enumerate(
63
                   tqdm(
64
65
                       train_dataloader,
                       desc="Epoch %d/%d" % (epoch + 1, self.num_epochs
66
     ),
                       total=len(self.train_ds) // self.batch_size,
67
                   )
68
               ):
69
                   self.step(batch)
70
      def test(self) -> None:
          raise NotImplementedError("You need to provide a test
     function.")
74
75
 class TorchVisionDatasetPipeline(DataLoaderPipeline):
76
      # language=rst
77
      .....
78
      An example implementation of 'DataLoaderPipeline' that runs
79
     all of the datasets
      inside of ''bindsnet.datasets'' that inherit from an instance of
80
      а
      'torchvision.datasets'. These are documented in 'bindsnet/
81
     datasets/README.md''.
      This specific class just runs an unsupervised network.
82
      .....
83
```

```
def __init__(
85
           self,
86
           network: Network,
87
88
           train_ds: Dataset,
           pipeline_analyzer: Optional[PipelineAnalyzer] = None,
89
           **kwargs
90
      ) -> None:
91
           # language=rst
92
           0.0.0
93
           Initializes the pipeline.
94
95
           :param network: Arbitrary ''network'' object.
96
           :param train_ds: A ''torchvision.datasets'' wrapper dataset
97
      from
                ''bindsnet.datasets''.
98
99
           Keyword arguments:
100
101
           :param str input_layer: Layer of the network that receives
102
      input.
           .....
103
           super().__init__(network, train_ds, None, **kwargs)
104
105
           self.input_layer = kwargs.get("input_layer", "X")
106
           self.pipeline_analyzer = pipeline_analyzer
107
108
      def step_(self, batch: Dict[str, torch.Tensor], **kwargs) ->
109
      None:
           # language=rst
110
           .....
111
           Perform a pass of the network given the input batch.
      Unsupervised training
           (implying everything is stored inside of the ''network''
      object, therefore
           returns ''None''.
114
           :param batch: A dictionary of the current batch. Includes
116
      image, label and
               encoded versions.
117
           .....
118
           self.network.reset_state_variables()
119
           inputs = {self.input_layer: batch["encoded_image"]}
120
           self.network.run(inputs, time=batch["encoded_image"].shape
121
      [0])
      def init_fn(self) -> None:
           pass
124
      def plots(self, batch: Dict[str, torch.Tensor], *args) -> None:
126
           # language=rst
127
           0.0.0
128
           Create any plots and logs for a step given the input batch.
129
130
           :param batch: A dictionary of the current batch. Includes
131
```

```
image, label and
                encoded versions.
           .....
133
           if self.pipeline_analyzer is not None:
134
                self.pipeline_analyzer.plot_obs(
135
                    batch["encoded_image"][0, ...].sum(0), step=self.
136
      step_count
                )
138
                self.pipeline_analyzer.plot_spikes(
139
                    self.get_spike_data(), step=self.step_count
140
                )
141
142
                vr, tv = self.get_voltage_data()
143
                self.pipeline_analyzer.plot_voltages(vr, tv, step=self.
144
      step_count)
145
                self.pipeline_analyzer.finalize_step()
146
147
       def test_step(self):
148
           pass
149
```

Listing B.13: Data-loader pipeline

```
1 import torch
2 import numpy as np
3
4 from . import EnvironmentPipeline
6
7 def select_multinomial(pipeline: EnvironmentPipeline, **kwargs) ->
     int:
      # language=rst
8
      ......
9
      Selects an action probabilistically based on spiking activity
10
     from a network layer.
11
      :param pipeline: EnvironmentPipeline with environment that has
12
     an integer action
          space.
13
      :return: Action sampled from multinomial over activity of
14
     similarly-sized output
          layer.
15
16
      Keyword arguments:
17
18
      :param str output: Name of output layer whose activity to base
19
     action selection on.
      0.0.0
20
      try:
21
          output = kwargs["output"]
22
      except KeyError:
23
          raise KeyError('select_multinomial() requires an "output"
24
     layer argument.')
```

```
25
      output = pipeline.network.layers[output]
26
      action_space = pipeline.env.action_space
28
      assert (
29
          output.n % action_space.n == 0
30
      ), f"Output layer size of {output.n} is not divisible by action
31
     space size of {action_space.n}."
32
      pop_size = int(output.n / action_space.n)
33
      spikes = output.s
34
      _sum = spikes.sum().float()
35
36
      # Choose action based on population's spiking.
      if _sum == 0:
38
          action = np.random.choice(pipeline.env.action_space.n)
39
      else:
40
          pop_spikes = torch.tensor(
41
               Γ
42
                   spikes[(i * pop_size) : (i * pop_size) + pop_size].
43
     sum()
                   for i in range(action_space.n)
44
              ]
45
          )
46
          action = torch.multinomial((pop_spikes.float() / _sum).view
47
     (-1), 1)[0].item()
48
      return action
49
50
51
s2 def select_softmax(pipeline: EnvironmentPipeline, **kwargs) -> int:
      # language=rst
53
      0.0.0
54
      Selects an action using softmax function based on spiking from a
55
      network layer.
56
      :param pipeline: EnvironmentPipeline with environment that has
57
     an integer action
          space and :code:'spike_record' set.
58
      :return: Action sampled from softmax over activity of similarly-
59
     sized output layer.
60
      Keyword arguments:
61
62
      :param str output: Name of output layer whose activity to base
63
     action selection on.
      0.0.0
64
      try:
65
          output = kwargs["output"]
66
      except KeyError:
67
          raise KeyError('select_softmax() requires an "output" layer
68
     argument.')
69
      assert (
```

70

```
pipeline.network.layers[output].n == pipeline.env.
71
     action_space.n
      ), "Output layer size is not equal to the size of the action
     space."
      assert hasattr(
74
          pipeline, "spike_record"
75
      ), "EnvironmentPipeline is missing the attribute: spike_record."
76
77
      spikes = torch.sum(pipeline.spike_record[output], dim=0)
78
      probabilities = torch.softmax(spikes, dim=0)
79
      return torch.multinomial(probabilities, num_samples=1).item()
80
81
82
83 def select_random(pipeline: EnvironmentPipeline, **kwargs) -> int:
      # language=rst
84
      0.0.0
85
      Selects an action randomly from the action space.
86
87
     :param pipeline: EnvironmentPipeline with environment that has
88
     an integer action
          space.
89
      :return: Action randomly sampled over size of pipeline's action
90
     space.
      0.0.0
91
      # Choose action randomly from the action space.
92
      return np.random.choice(pipeline.env.action_space.n)
93
```

Listing B.14: Action

B.5 Encoding

```
1 from .encodings import single, repeat, bernoulli, poisson,
     rank_order
2 from .loaders import bernoulli_loader, poisson_loader,
     rank_order_loader
3 from .encoders import (
     Encoder,
4
      NullEncoder,
5
      SingleEncoder,
6
      RepeatEncoder,
7
      BernoulliEncoder,
8
      PoissonEncoder,
9
      RankOrderEncoder,
10
11 )
```

Listing B.15: Initialization

```
1 from typing import Optional, Union, Iterable, Iterator
2
3 import torch
4
5 from .encodings import bernoulli, poisson, rank_order
6
```

```
7
8 def bernoulli_loader(
      data: Union[torch.Tensor, Iterable[torch.Tensor]],
9
10
      time: Optional[int] = None,
      dt: float = 1.0,
11
      **kwargs
12
13 ) -> Iterator[torch.Tensor]:
      # language=rst
14
      0.0.0
15
      Lazily invokes ''bindsnet.encoding.bernoulli'' to iteratively
16
     encode a sequence of
      data.
17
18
      :param data: Tensor of shape ''[n_samples, n_1, ..., n_k]''.
19
      :param time: Length of Bernoulli spike train per input variable.
20
      :param dt: Simulation time step.
21
      :return: Tensors of shape ''[time, n_1, ..., n_k]'' of Bernoulli
     -distributed spikes.
      Keyword arguments:
24
25
      :param float max_prob: Maximum probability of spike per
26
     Bernoulli trial.
      .....
27
      # Setting kwargs.
28
      max_prob = kwargs.get("dt", 1.0)
29
30
      for i in range(len(data)):
31
          # Encode datum as Bernoulli spike trains.
32
          yield bernoulli(datum=data[i], time=time, dt=dt, max_prob=
33
     max_prob)
34
35
36 def poisson_loader(
      data: Union[torch.Tensor, Iterable[torch.Tensor]],
37
38
      time: int,
      dt: float = 1.0,
39
      **kwargs
40
41 ) -> Iterator[torch.Tensor]:
      # language=rst
42
      ......
43
      Lazily invokes ''bindsnet.encoding.poisson'' to iteratively
44
     encode a sequence of
      data.
45
46
      :param data: Tensor of shape '`[n_samples, n_1, ..., n_k]'`.
47
      :param time: Length of Poisson spike train per input variable.
48
      :param dt: Simulation time step.
49
      :return: Tensors of shape ''[time, n_1, ..., n_k]'' of Poisson-
50
     distributed spikes.
      0.0.0
51
      for i in range(len(data)):
52
          # Encode datum as Poisson spike trains.
53
          yield poisson(datum=data[i], time=time, dt=dt)
54
```

```
55
56
57 def rank_order_loader(
      data: Union[torch.Tensor, Iterable[torch.Tensor]],
58
      time: int,
59
      dt: float = 1.0,
60
      **kwargs
61
62 ) -> Iterator[torch.Tensor]:
      # language=rst
63
      ......
64
     Lazily invokes ''bindsnet.encoding.rank_order'' to iteratively
65
     encode a sequence of
      data.
66
67
     :param data: Tensor of shape ''[n_samples, n_1, ..., n_k]''.
68
      :param time: Length of rank order-encoded spike train per input
69
     variable.
      :param dt: Simulation time step.
70
      :return: Tensors of shape ''[time, n_1, ..., n_k]'' of rank
71
     order-encoded spikes.
      0.0.0
72
      for i in range(len(data)):
73
          # Encode datum as rank order-encoded spike trains.
74
          yield rank_order(datum=data[i], time=time, dt=dt)
75
```

Listing B.16: Loaders

```
1 from . import encodings
2
3
4 class Encoder:
      # language=rst
5
      .....
6
      Base class for spike encodings transforms.
7
8
      Calls ''self.enc'' from the subclass and passes whatever
9
     arguments were provided.
      ''self.enc'' must be callable with ''torch.Tensor'', ''*args'',
10
     ' **kwargs ''
      .....
11
      def __init__(self, *args, **kwargs) -> None:
13
          self.enc_args = args
14
          self.enc_kwargs = kwargs
15
16
      def __call__(self, img):
17
          return self.enc(img, *self.enc_args, **self.enc_kwargs)
18
19
20
21 class NullEncoder(Encoder):
     # language=rst
22
      0.0.0
23
      Pass through of the datum that was input.
24
25
```

```
.. note::
26
          This is not a real spike encoder. Be careful with the usage
27
     of this class.
      0.0.0
28
29
      def __init__(self):
30
          super().__init__()
31
32
      def __call__(self, img):
33
34
          return img
35
36
  class SingleEncoder(Encoder):
37
      def __init__(self, time: int, dt: float = 1.0, sparsity: float =
38
      0.5, **kwargs):
          # language=rst
39
          0.0.0
40
          Creates a callable SingleEncoder which encodes as defined in
41
           ''bindsnet.encoding.single''
42
43
          :param time: Length of single spike train per input variable
44
          :param dt: Simulation time step.
45
          :param sparsity: Sparsity of the input representation. O for
46
      no spikes and 1 for
               all spikes.
47
          .....
48
          super().__init__(time, dt=dt, sparsity=sparsity, **kwargs)
49
50
          self.enc = encodings.single
51
52
53
54 class RepeatEncoder(Encoder):
      def __init__(self, time: int, dt: float = 1.0, **kwargs):
55
          # language=rst
56
          .....
57
          Creates a callable ''RepeatEncoder'' which encodes as
58
     defined in
           ''bindsnet.encoding.repeat''
59
60
          :param time: Length of repeat spike train per input variable
61
          :param dt: Simulation time step.
62
          0.0.0
63
          super().__init__(time, dt=dt, **kwargs)
64
65
          self.enc = encodings.repeat
66
67
68
69 class BernoulliEncoder(Encoder):
      def __init__(self, time: int, dt: float = 1.0, **kwargs):
70
          # language=rst
71
          .....
72
          Creates a callable 'BernoulliEncoder' which encodes as
73
```

```
defined in
           :code: 'bindsnet.encoding.bernoulli '
74
75
           :param time: Length of Bernoulli spike train per input
76
      variable.
           :param dt: Simulation time step.
77
78
           Keyword arguments:
79
80
           :param float max_prob: Maximum probability of spike per time
81
       step.
           ......
82
           super().__init__(time, dt=dt, **kwargs)
83
84
           self.enc = encodings.bernoulli
85
86
87
88 class PoissonEncoder(Encoder):
       def __init__(self, time: int, dt: float = 1.0, **kwargs):
89
           # language=rst
90
           .....
91
           Creates a callable PoissonEncoder which encodes as defined
92
      in
           ''bindsnet.encoding.poisson'
93
94
           :param time: Length of Poisson spike train per input
95
      variable.
           :param dt: Simulation time step.
96
           0.0.0
97
           super().__init__(time, dt=dt, **kwargs)
98
99
           self.enc = encodings.poisson
100
101
102
  class RankOrderEncoder(Encoder):
103
       def __init__(self, time: int, dt: float = 1.0, **kwargs):
104
           # language=rst
105
           .....
106
           Creates a callable RankOrderEncoder which encodes as defined
107
       in
           :code:'bindsnet.encoding.rank_order'
108
109
           :param time: Length of RankOrder spike train per input
110
      variable.
           :param dt: Simulation time step.
111
           0.0.0
           super().__init__(time, dt=dt, **kwargs)
113
114
           self.enc = encodings.rank_order
115
```

Listing B.17: Encoders

1 from typing import Optional

```
3 import torch
4 import numpy as np
7 def single(
      datum: torch.Tensor, time: int, dt: float = 1.0, sparsity: float
8
      = 0.5, **kwargs
9) -> torch.Tensor:
      # language=rst
10
      0.0.0
11
      Generates timing based single-spike encoding. Spike occurs
12
     earlier if the
      intensity of the input feature is higher. Features whose value
13
     is lower than
     threshold is remain silent.
14
15
      :param datum: Tensor of shape '`[n_1, ..., n_k]''.
16
      :param time: Length of the input and output.
17
      :param dt: Simulation time step.
18
      :param sparsity: Sparsity of the input representation. 0 for no
19
     spikes and 1 for all
          spikes.
20
      :return: Tensor of shape ''[time, n_1, ..., n_k]''.
      .....
22
      time = int(time / dt)
23
      shape = list(datum.shape)
24
      datum = np.copy(datum)
25
      quantile = np.quantile(datum, 1 - sparsity)
26
      s = np.zeros([time, *shape])
27
      s[0] = np.where(datum > quantile, np.ones(shape), np.zeros(shape
28
     ))
      return torch.Tensor(s).byte()
29
30
31
32 def repeat(datum: torch.Tensor, time: int, dt: float = 1.0, **kwargs
     ) -> torch.Tensor:
      # language=rst
33
      0.0.0
34
      :param datum: Repeats a tensor along a new dimension in the Oth
35
     position for
          ''int(time / dt)'' timesteps.
36
37
      :param time: Tensor of shape '`[n_1, ..., n_k]''.
      :param dt: Simulation time step.
38
      :return: Tensor of shape ''[time, n_1, ..., n_k]'' of repeated
39
     data along the 0-th
          dimension.
40
      ......
41
      time = int(time / dt)
42
      return datum.repeat([time, *([1] * len(datum.shape))])
43
44
45
46 def bernoulli(
      datum: torch.Tensor, time: Optional[int] = None, dt: float =
47
     1.0, **kwargs
```

```
48 ) -> torch.Tensor:
      # language=rst
49
      .....
50
      Generates Bernoulli-distributed spike trains based on input
51
     intensity. Inputs must
      be non-negative. Spikes correspond to successful Bernoulli
52
     trials, with success
      probability equal to (normalized in [0, 1]) input value.
53
54
55
      :param datum: Tensor of shape ''[n_1, ..., n_k]''.
      :param time: Length of Bernoulli spike train per input variable.
56
      :param dt: Simulation time step.
57
      :return: Tensor of shape ''[time, n_1, ..., n_k]'' of Bernoulli-
58
     distributed spikes.
59
      Keyword arguments:
60
61
      :param float max_prob: Maximum probability of spike per
62
     Bernoulli trial.
      0.0.0
63
      # Setting kwargs.
64
      max_prob = kwargs.get("max_prob", 1.0)
65
66
      assert 0 <= max_prob <= 1, "Maximum firing probability must be</pre>
67
     in range [0, 1]"
      assert (datum >= 0).all(), "Inputs must be non-negative"
68
69
      shape, size = datum.shape, datum.numel()
70
      datum = datum.flatten()
71
72
      if time is not None:
73
          time = int(time / dt)
74
75
      # Normalize inputs and rescale (spike probability proportional
76
     to input intensity).
      if datum.max() > 1.0:
77
          datum /= datum.max()
78
79
      # Make spike data from Bernoulli sampling.
80
      if time is None:
81
          spikes = torch.bernoulli(max_prob * datum)
82
          spikes = spikes.view(*shape)
83
      else:
84
          spikes = torch.bernoulli(max_prob * datum.repeat([time, 1]))
85
          spikes = spikes.view(time, *shape)
86
87
      return spikes.byte()
88
89
90
91 def poisson(datum: torch.Tensor, time: int, dt: float = 1.0, **
     kwargs) -> torch.Tensor:
      # language=rst
92
      0.0.0
93
      Generates Poisson-distributed spike trains based on input
94
```

```
intensity. Inputs must be
      non-negative, and give the firing rate in Hz. Inter-spike
95
      intervals (ISIs) for
96
      non-negative data incremented by one to avoid zero intervals
      while maintaining ISI
      distributions.
97
98
      :param datum: Tensor of shape ''[n_1, ..., n_k]''.
99
       :param time: Length of Poisson spike train per input variable.
100
      :param dt: Simulation time step.
101
      :return: Tensor of shape ''[time, n_1, ..., n_k]'' of Poisson-
102
      distributed spikes.
       .....
103
      assert (datum >= 0).all(), "Inputs must be non-negative"
104
105
      # Get shape and size of data.
106
      shape, size = datum.shape, datum.numel()
107
      datum = datum.flatten()
108
      time = int(time / dt)
109
      # Compute firing rates in seconds as function of data intensity,
111
      # accounting for simulation time step.
112
      rate = torch.zeros(size)
      rate[datum != 0] = 1 / datum[datum != 0] * (1000 / dt)
114
      # Create Poisson distribution and sample inter-spike intervals
116
      # (incrementing by 1 to avoid zero intervals).
      dist = torch.distributions.Poisson(rate=rate)
118
      intervals = dist.sample(sample_shape=torch.Size([time + 1]))
119
      intervals[:, datum != 0] += (intervals[:, datum != 0] == 0).
120
      float()
      # Calculate spike times by cumulatively summing over time
122
      dimension.
      times = torch.cumsum(intervals, dim=0).long()
      times[times >= time + 1] = 0
124
      # Create tensor of spikes.
126
      spikes = torch.zeros(time + 1, size).byte()
      spikes[times, torch.arange(size)] = 1
128
      spikes = spikes[1:]
129
130
      return spikes.view(time, *shape)
134 def rank_order(
      datum: torch.Tensor, time: int, dt: float = 1.0, **kwargs
135
136 ) -> torch.Tensor:
      # language=rst
137
      0.0.0
138
      Encodes data via a rank order coding-like representation. One
139
     spike per neuron,
      temporally ordered by decreasing intensity. Inputs must be non-
140
     negative.
```

```
141
       :param datum: Tensor of shape ''[n_samples, n_1, ..., n_k]''.
142
       :param time: Length of rank order-encoded spike train per input
143
      variable.
       :param dt: Simulation time step.
144
       :return: Tensor of shape ''[time, n_1, ..., n_k]'' of rank order
145
      -encoded spikes.
       . . . .
146
       assert (datum >= 0).all(), "Inputs must be non-negative"
147
148
       shape, size = datum.shape, datum.numel()
149
       datum = datum.flatten()
150
       time = int(time / dt)
151
       # Create spike times in order of decreasing intensity.
153
       datum /= datum.max()
154
       times = torch.zeros(size)
155
       times[datum != 0] = 1 / datum[datum != 0]
156
       times *= time / times.max() # Extended through simulation time.
157
       times = torch.ceil(times).long()
158
159
       # Create spike times tensor.
160
       spikes = torch.zeros(time, size).byte()
161
       for i in range(size):
162
           if 0 < times[i] < time:</pre>
163
               spikes[times[i] - 1, i] = 1
164
165
       return spikes.reshape(time, *shape)
166
```

Listing B.18: Encodings

B.6 Conversion

```
1 from .conversion import (
      Permute,
2
      FeatureExtractor,
3
      SubtractiveResetIFNodes,
4
      PassThroughNodes,
5
      PermuteConnection,
6
      ConstantPad2dConnection,
7
      data_based_normalization,
8
      ann_to_snn,
9
10)
```

Listing B.19: Initialization

```
import torch
import numpy as np
import torch.nn as nn
import torch.nn.functional as F
form torch.nn.modules.utils import _pair
form copy import deepcopy
```

```
9 from typing import Union, Sequence, Optional, Tuple, Dict, Iterable
10
import bindsnet.network.nodes as nodes
12 import bindsnet.network.topology as topology
13
14 from bindsnet.network import Network
15
16
17 class Permute(nn.Module):
18
      # language=rst
      ......
19
      PyTorch module for the explicit permutation of a tensor's
20
     dimensions in a parent
      module's ''forward'' pass (as opposed to ''torch.permute'').
21
      0.0.0
22
      def __init__(self, dims):
24
          # language=rst
25
          .....
26
          Constructor for "Permute" module.
28
          :param dims: Ordering of dimensions for permutation.
29
          0.0.0
30
          super(Permute, self).__init__()
31
32
          self.dims = dims
33
34
      def forward(self, x):
35
          # language=rst
36
          0.0.0
37
          Forward pass of permutation module.
38
39
          :param x: Input tensor to permute.
40
          :return: Permuted input tensor.
41
          0.0.0
42
          return x.permute(*self.dims).contiguous()
43
44
45
46 class FeatureExtractor(nn.Module):
      # language=rst
47
      ......
48
      Special-purpose PyTorch module for the extraction of child
49
     module's activations.
      .....
50
51
      def __init__(self, submodule):
52
          # language=rst
53
          54
          Constructor for ''FeatureExtractor'' module.
55
56
          :param submodule: The module who's children modules are to
57
     be extracted.
          ......
58
          super(FeatureExtractor, self).__init__()
59
```

```
60
           self.submodule = submodule
61
62
63
      def forward(self, x: torch.Tensor) -> Dict[nn.Module, torch.
      Tensorl:
           # language=rst
64
           ......
65
           Forward pass of the feature extractor.
66
67
           :param x: Input data for the ''submodule''.
68
           :return: A dictionary mapping
69
           0.0.0
70
           activations = {"input": x}
71
           for name, module in self.submodule._modules.items():
               if isinstance(module, nn.Linear):
                    x = x.view(-1, module.in_features)
74
75
               x = module(x)
76
                activations[name] = x
77
78
           return activations
79
80
81
  class SubtractiveResetIFNodes(nodes.Nodes):
82
      # language=rst
83
       .....
84
      Layer of 'integrate-and-fire (IF) neurons
85
      <http://neuronaldynamics.epfl.ch/online/Ch1.S3.html>' using
86
      reset by subtraction.
       .....
87
88
      def __init__(
89
           self.
90
           n: Optional[int] = None,
91
           shape: Optional[Iterable[int]] = None,
92
           traces: bool = False,
93
           traces_additive: bool = False,
94
           tc_trace: Union[float, torch.Tensor] = 20.0,
95
           trace_scale: Union[float, torch.Tensor] = 1.0,
96
           sum_input: bool = False,
97
           thresh: Union[float, torch.Tensor] = -52.0,
98
           reset: Union[float, torch.Tensor] = -65.0,
99
           refrac: Union[int, torch.Tensor] = 5,
100
           lbound: float = None,
101
           **kwargs,
102
      ) -> None:
103
           # language=rst
104
           0.0.0
105
           Instantiates a layer of IF neurons with the subtractive
106
      reset mechanism from
           'this paper
107
           <https://www.frontiersin.org/articles/10.3389/fnins</pre>
108
      .2017.00682/full>'_.
109
```

:param n: The number of neurons in the layer. :param shape: The dimensionality of the layer. :param traces: Whether to record spike traces. :param traces_additive: Whether to record spike traces additively. :param tc_trace: Time constant of spike trace decay. 114 :param trace_scale: Scaling factor for spike trace. :param sum_input: Whether to sum all inputs. 116 :param thresh: Spike threshold voltage. :param reset: Post-spike reset voltage. 118 :param refrac: Refractory (non-firing) period of the neuron. 119 :param lbound: Lower bound of the voltage. 0.0.0 super().__init__(n=n, shape=shape, 124 traces=traces, traces_additive=traces_additive, 126 tc_trace=tc_trace, trace_scale=trace_scale, 128 sum_input=sum_input, 129) 130 self.register_buffer("reset", torch.tensor(reset, dtype=torch.float)) # Post-spike reset voltage. 134 self.register_buffer("thresh", torch.tensor(thresh, dtype=torch.float) 136) # Spike threshold voltage. self.register_buffer(138 "refrac", torch.tensor(refrac)) # Post-spike refractory period. 140 self.register_buffer("v", torch.FloatTensor()) # Neuron 141 voltages. self.register_buffer(142 "refrac_count", torch.FloatTensor() 143) # Refractory period counters. 144 145 self.lbound = lbound # Lower bound of voltage. 146 147 def forward(self, x: torch.Tensor) -> None: 148 # language=rst 149 0.0.0 150 Runs a single simulation step. 151 152 :param x: Inputs to the layer. 153 154 # Integrate input voltages. self.v += (self.refrac_count == 0).float() * x 156 157 # Decrement refractory counters. 158 self.refrac_count = (self.refrac_count > 0).float() * (159 self.refrac_count - self.dt 160

)

```
162
           # Check for spiking neurons.
163
           self.s = self.v >= self.thresh
164
165
           # Refractoriness and voltage reset.
166
           self.refrac_count.masked_fill_(self.s, self.refrac)
167
           self.v[self.s] = self.v[self.s] - self.thresh
168
169
           # Voltage clipping to lower bound.
170
           if self.lbound is not None:
                self.v.masked_fill_(self.v < self.lbound, self.lbound)</pre>
173
           super().forward(x)
174
       def reset_state_variables(self) -> None:
176
           # language=rst
           0.0.0
178
           Resets relevant state variables.
179
           .....
180
           super().reset_state_variables()
181
           self.v.fill_(self.reset) # Neuron voltages.
182
           self.refrac_count.zero_() # Refractory period counters.
183
184
       def set_batch_size(self, batch_size) -> None:
185
           # language=rst
186
           .....
187
           Sets mini-batch size. Called when layer is added to a
188
      network.
189
190
           :param batch_size: Mini-batch size.
           0.0.0
191
           super().set_batch_size(batch_size=batch_size)
192
           self.v = self.reset * torch.ones(batch_size, *self.shape,
193
      device=self.v.device)
           self.refrac_count = torch.zeros_like(self.v, device=self.
194
      refrac_count.device)
195
196
  class PassThroughNodes(nodes.Nodes):
197
       # language=rst
198
       .....
199
       Layer of 'integrate-and-fire (IF) neurons
200
       <http://neuronaldynamics.epfl.ch/online/Ch1.S3.html>'_ with
201
      using reset by
       subtraction.
202
       0.0.0
203
204
       def __init__(
205
           self,
206
           n: Optional[int] = None,
207
           shape: Optional[Sequence[int]] = None,
208
           traces: bool = False,
209
           traces_additive: bool = False,
210
           tc_trace: Union[float, torch.Tensor] = 20.0,
```

```
trace_scale: Union[float, torch.Tensor] = 1.0,
           sum_input: bool = False,
       ) \rightarrow None:
214
           # language=rst
           0.0.0
216
           Instantiates a layer of IF neurons.
218
            :param n: The number of neurons in the layer.
219
            :param shape: The dimensionality of the layer.
220
            :param traces: Whether to record spike traces.
221
           :param trace_tc: Time constant of spike trace decay.
            :param sum_input: Whether to sum all inputs.
223
            0.0.0
224
           super().__init__(
                n=n,
226
                shape=shape,
227
                traces=traces,
228
                traces_additive=traces_additive,
229
                tc_trace=tc_trace,
230
                trace_scale=trace_scale,
                sum_input=sum_input,
           )
           self.register_buffer("v", torch.zeros(self.shape))
234
       def forward(self, x: torch.Tensor) -> None:
236
           # language=rst
237
           0.0.0
238
           Runs a single simulation step.
239
240
           :param inputs: Inputs to the layer.
241
           :param dt: Simulation time step.
242
           0.0.0
243
           self.s = x
244
245
       def reset_state_variables(self) -> None:
246
247
           # language=rst
           0.0.0
248
           Resets relevant state variables.
249
           0.0.0
250
           self.s.zero_()
251
252
253
  class PermuteConnection(topology.AbstractConnection):
254
       # language=rst
255
       0.0.0
256
       Special-purpose connection for emulating the custom "Permute"
257
      module in spiking
       neural networks.
258
       .....
259
260
       def __init__(
261
           self,
262
           source: nodes.Nodes,
263
           target: nodes.Nodes,
264
```

```
dims: Sequence,
265
           nu: Optional[Union[float, Sequence[float]]] = None,
266
           weight_decay: float = 0.0,
267
268
           **kwargs,
       ) \rightarrow None:
269
           # language=rst
           .....
271
           Constructor for 'PermuteConnection'.
274
           :param source: A layer of nodes from which the connection
      originates.
           :param target: A layer of nodes to which the connection
      connects.
           :param dims: Order of dimensions to permute.
276
           :param nu: Learning rate for both pre- and post-synaptic
      events.
           :param weight_decay: Constant multiple to decay weights by
278
      on each iteration.
279
           Keyword arguments:
280
281
           :param function update_rule: Modifies connection parameters
282
      according to some
               rule.
283
           :param float wmin: The minimum value on the connection
284
      weights.
           :param float wmax: The maximum value on the connection
285
      weights.
           :param float norm: Total weight per target neuron
286
      normalization.
           0.0.0
287
           super().__init__(source, target, nu, weight_decay, **kwargs)
288
289
           self.dims = dims
290
291
       def compute(self, s: torch.Tensor) -> torch.Tensor:
292
           # language=rst
293
           0.0.0
294
           Permute input.
295
296
           :param s: Input.
297
           :return: Permuted input.
298
           0.0.0
299
           return s.permute(self.dims).float()
300
301
302
  class ConstantPad2dConnection(topology.AbstractConnection):
303
       # language=rst
304
305
       Special-purpose connection for emulating the ''ConstantPad2d''
306
      PyTorch module in
           spiking neural networks.
307
       .....
308
309
```

```
def __init__(
310
           self,
311
           source: nodes.Nodes,
312
313
           target: nodes.Nodes,
           padding: Tuple,
314
           nu: Optional[Union[float, Sequence[float]]] = None,
315
           weight_decay: float = 0.0,
316
           **kwargs,
317
       ) -> None:
318
           # language=rst
319
           .....
320
           Constructor for ''ConstantPad2dConnection''.
321
           :param source: A layer of nodes from which the connection
      originates.
           :param target: A layer of nodes to which the connection
324
      connects.
           :param padding: Padding of input tensors; passed to ''torch.
325
      nn.functional.pad''.
           :param nu: Learning rate for both pre- and post-synaptic
326
      events.
           :param weight_decay: Constant multiple to decay weights by
327
      on each iteration.
328
           Keyword arguments:
329
330
           :param function update_rule: Modifies connection parameters
331
      according to some
               rule.
           :param float wmin: The minimum value on the connection
      weights.
           :param float wmax: The maximum value on the connection
334
      weights.
           :param float norm: Total weight per target neuron
335
      normalization.
           .....
336
337
           super().__init__(source, target, nu, weight_decay, **kwargs)
338
339
           self.padding = padding
340
341
       def compute(self, s: torch.Tensor):
342
           # language=rst
343
           0.0.0
344
           Pad input.
345
346
           :param s: Input.
347
           :return: Padding input.
348
           0.0.0
349
           return F.pad(s, self.padding).float()
350
351
352
353 def data_based_normalization(
       ann: Union[nn.Module, str], data: torch.Tensor, percentile:
354
```

```
float = 99.9
355):
      # language=rst
356
      0.0.0
357
      Use a dataset to rescale ANN weights and biases such that that
358
      the max ReLU
      activation is less than 1.
359
360
      :param ann: Artificial neural network implemented in PyTorch.
361
      Accepts either
           "torch.nn.Module" or path to network saved using "torch.
362
      save() ``.
       :param data: Data to use to perform data-based weight
363
      normalization of shape
           ``[n_examples, ...]''.
364
      :param percentile: Percentile (in ''[0, 100]'') of activations
365
      to scale by in
           data-based normalization scheme.
366
      :return: Artificial neural network with rescaled weights and
367
      biases according to
           activations on the dataset.
368
       .....
369
      if isinstance(ann, str):
370
           ann = torch.load(ann)
371
372
      assert isinstance(ann, nn.Module)
373
374
      def set_requires_grad(module, value):
375
           for param in module.parameters():
376
               param.requires_grad = value
377
378
      set_requires_grad(ann, value=False)
379
       extractor = FeatureExtractor(ann)
380
      all_activations = extractor.forward(data)
381
382
383
      prev_module = None
      prev_factor = 1
384
      for name, module in ann._modules.items():
385
           if isinstance(module, nn.Sequential):
386
387
               extractor2 = FeatureExtractor(module)
388
               all_activations2 = extractor2.forward(data)
389
               for name2, module2 in module.named_children():
390
                    activations = all_activations2[name2]
391
392
                    if isinstance(module2, nn.ReLU):
393
                        if prev_module is not None:
394
                             scale_factor = np.percentile(activations.cpu
395
      (), percentile)
396
                             prev_module.weight *= prev_factor /
397
      scale_factor
                             prev_module.bias /= scale_factor
398
```

prev_factor = scale_factor 400 401 elif isinstance(module2, nn.Linear) or isinstance(402 module2, nn.Conv2d): prev_module = module2 403 404 else: 405 activations = all_activations[name] 406 if isinstance(module, nn.ReLU): 407 if prev_module is not None: 408 scale_factor = np.percentile(activations.cpu(), 409 percentile) 410 prev_module.weight *= prev_factor / scale_factor 411 prev_module.bias /= scale_factor 412 413 prev_factor = scale_factor 414 415 elif isinstance(module, nn.Linear) or isinstance(module, 416 nn.Conv2d): prev_module = module 417 418 return ann 419 420 421 422 def _ann_to_snn_helper(prev, current, node_type, last=False, ** kwargs): # language=rst 423 424 Helper function for main ''ann_to_snn'' method. 425 426 :param prev: Previous PyTorch module in artificial neural 427 network. :param current: Current PyTorch module in artificial neural 428 network. :param node_type: Type of ''bindsnet.network.nodes'' to use. 429 :param last: Whether this connection and layer is the last to be 430 converted. :return: Spiking neural network layer and connection 431 corresponding to ''prev'' and "current" PyTorch modules. 432 433 if isinstance(current, nn.Linear): 434 layer = node_type(435 n=current.out_features, 436 reset=0, 437 thresh=1, 438 refrac=0, 439 sum_input=last, 440 **kwargs, 441) 442 bias = current.bias if current.bias is not None else torch. 443 zeros(layer.n) connection = topology.Connection(444

```
source=prev, target=layer, w=current.weight.t(), b=bias
445
           )
446
447
448
       elif isinstance(current, nn.Conv2d):
           input_height, input_width = prev.shape[2], prev.shape[3]
110
           out_channels, output_height, output_width = (
450
                current.out_channels,
451
               prev.shape[2],
452
               prev.shape[3],
453
           )
454
455
           width = (
456
                input_height - current.kernel_size[0] + 2 * current.
457
      padding[0]
           ) / current.stride[0] + 1
458
           height = (
459
                input_width - current.kernel_size[1] + 2 * current.
460
      padding[1]
           ) / current.stride[1] + 1
461
           shape = (1, out_channels, int(width), int(height))
462
463
           layer = node_type(
464
                shape=shape, reset=0, thresh=1, refrac=0, sum_input=last
465
        **kwargs
           )
466
           bias = current.bias if current.bias is not None else torch.
467
      zeros(layer.shape[1])
           connection = topology.Conv2dConnection(
468
                source=prev,
469
470
               target=layer,
               kernel_size=current.kernel_size,
471
                stride=current.stride,
472
               padding=current.padding,
473
                dilation=current.dilation,
474
               w=current.weight,
475
               b=bias,
476
           )
477
478
       elif isinstance(current, nn.MaxPool2d):
479
           input_height, input_width = prev.shape[2], prev.shape[3]
480
           current.kernel_size = _pair(current.kernel_size)
481
           current.padding = _pair(current.padding)
482
           current.stride = _pair(current.stride)
483
484
           width = (
485
                input_height - current.kernel_size[0] + 2 * current.
486
      padding[0]
           ) / current.stride[0] + 1
487
           height = (
488
                input_width - current.kernel_size[1] + 2 * current.
489
      padding[1]
           ) / current.stride[1] + 1
490
           shape = (1, prev.shape[1], int(width), int(height))
491
492
```

```
layer = PassThroughNodes(shape=shape)
493
            connection = topology.MaxPool2dConnection(
494
                source=prev,
495
496
                target=layer,
                kernel_size=current.kernel_size,
497
                stride=current.stride,
498
                padding=current.padding,
499
                dilation=current.dilation,
500
501
                decay=1,
           )
502
503
       elif isinstance(current, Permute):
504
           layer = PassThroughNodes(
505
                shape=[
506
                    prev.shape[current.dims[0]],
507
                    prev.shape[current.dims[1]],
508
                    prev.shape[current.dims[2]],
509
                    prev.shape[current.dims[3]],
510
                ]
511
           )
512
513
            connection = PermuteConnection(source=prev, target=layer,
514
      dims=current.dims)
515
       elif isinstance(current, nn.ConstantPad2d):
516
           layer = PassThroughNodes(
517
                shape=[
518
                    prev.shape[0],
519
                    prev.shape[1],
520
                     current.padding[0] + current.padding[1] + prev.shape
521
      [2],
                     current.padding[2] + current.padding[3] + prev.shape
522
      [3],
                ]
523
           )
524
525
           connection = ConstantPad2dConnection(
526
                source=prev, target=layer, padding=current.padding
527
           )
528
529
       else:
530
           return None, None
531
532
       return layer, connection
533
534
535
  def ann_to_snn(
536
       ann: Union[nn.Module, str],
537
       input_shape: Sequence[int],
538
       data: Optional[torch.Tensor] = None,
539
       percentile: float = 99.9,
540
       node_type: Optional[nodes.Nodes] = SubtractiveResetIFNodes,
541
       **kwargs,
542
543) -> Network:
```

```
# language=rst
544
       .....
545
       Converts an artificial neural network (ANN) written as a ''torch
546
      .nn.Module'' into a
      near-equivalent spiking neural network.
547
548
       :param ann: Artificial neural network implemented in PyTorch.
549
      Accepts either
           "torch.nn.Module" or path to network saved using "torch.
550
      save() ``.
       :param input_shape: Shape of input data.
551
       :param data: Data to use to perform data-based weight
552
      normalization of shape
           '`[n_examples, ...]'`.
553
       :param percentile: Percentile (in ''[0, 100]'') of activations
554
      to scale by in
           data-based normalization scheme.
555
       :param node_type: Class of 'Nodes' to use in replacing 'torch
556
      .nn.Linear'' layers
           in original ANN.
557
       :return: Spiking neural network implemented in PyTorch.
558
       0.0.0
559
       if isinstance(ann, str):
560
           ann = torch.load(ann)
561
       else:
562
           ann = deepcopy(ann)
563
564
       assert isinstance(ann, nn.Module)
565
566
       if data is None:
567
           import warnings
568
569
           warnings.warn("Data is None. Weights will not be scaled.",
570
      RuntimeWarning)
       else:
571
           ann = data_based_normalization(
572
                ann=ann, data=data.detach(), percentile=percentile
573
           )
574
575
       snn = Network()
576
577
       input_layer = nodes.Input(shape=input_shape)
578
       snn.add_layer(input_layer, name="Input")
579
580
       children = []
581
       for c in ann.children():
582
           if isinstance(c, nn.Sequential):
583
               for c2 in list(c.children()):
584
                    children.append(c2)
585
           else:
586
                children.append(c)
587
588
       i = 0
589
       prev = input_layer
590
```

```
while i < len(children) - 1:</pre>
591
           current, nxt = children[i : i + 2]
592
           layer, connection = _ann_to_snn_helper(prev, current,
593
      node_type, **kwargs)
594
           i += 1
595
596
           if layer is None or connection is None:
597
598
                continue
599
           snn.add_layer(layer, name=str(i))
600
           snn.add_connection(connection, source=str(i - 1), target=str
601
      (i))
602
           prev = layer
603
604
       current = children[-1]
605
       layer, connection = _ann_to_snn_helper(
606
           prev, current, node_type, last=True, **kwargs
607
       )
608
609
       i += 1
610
611
       if layer is not None or connection is not None:
612
           snn.add_layer(layer, name=str(i))
613
           snn.add_connection(connection, source=str(i - 1), target=str
614
      (i))
615
      return snn
616
```

Listing B.20: Conversion

B.7 Model

```
1 from .models import (
2 TwoLayerNetwork,
3 DiehlAndCook2015,
4 DiehlAndCook2015v2,
5 IncreasingInhibitionNetwork,
6 LocallyConnectedNetwork,
7 )
```

Listing B.21: Initialization

```
1 from typing import Optional, Union, Tuple, List, Sequence, Iterable
2
3 import numpy as np
4 import torch
5 from scipy.spatial.distance import euclidean
6 from torch.nn.modules.utils import _pair
7 import torch.nn as nn
8 from torchvision import models
9
10 from ..learning import PostPre
```

```
11 from ...network import Network
12 from ..network.nodes import Input, LIFNodes, DiehlAndCookNodes
13 from .. network.topology import Connection, LocalConnection
14
15
16 class TwoLayerNetwork(Network):
      # language=rst
17
      .....
18
      Implements an ''Input'' instance connected to a ''LIFNodes''
19
     instance with a
      fully-connected ''Connection''.
20
      0.0.0
21
      def __init__(
          self,
24
          n_inpt: int,
25
          n_neurons: int = 100,
26
          dt: float = 1.0,
          wmin: float = 0.0,
28
          wmax: float = 1.0,
29
          nu: Optional[Union[float, Sequence[float]]] = (1e-4, 1e-2),
30
          reduction: Optional[callable] = None,
31
          norm: float = 78.4,
32
      ) -> None:
33
          # language=rst
34
          .....
35
          Constructor for class 'TwoLayerNetwork'.
36
37
          :param n_inpt: Number of input neurons. Matches the 1D size
38
     of the input data.
          :param n_neurons: Number of neurons in the ''LIFNodes''
39
     population.
          :param dt: Simulation time step.
40
          :param nu: Single or pair of learning rates for pre- and
41
     post-synaptic events,
42
               respectively.
          :param reduction: Method for reducing parameter updates
43
     along the minibatch
              dimension.
44
          :param wmin: Minimum allowed weight on ''Input'' to ''
45
     LIFNodes'' synapses.
          :param wmax: Maximum allowed weight on ''Input'' to ''
46
     LIFNodes'' synapses.
           :param norm: ''Input'' to ''LIFNodes'' layer connection
47
     weights normalization
              constant.
48
          .....
49
          super().__init__(dt=dt)
50
51
          self.n_inpt = n_inpt
52
          self.n_neurons = n_neurons
53
          self.dt = dt
54
55
          self.add_layer(Input(n=self.n_inpt, traces=True, tc_trace
56
```

```
=20.0), name="X")
            self.add_layer(
57
                LIFNodes(
58
59
                     n=self.n_neurons,
                     traces=True,
60
                     rest=-65.0,
61
                     reset = -65.0,
62
                     thresh = -52.0,
63
                     refrac=5,
64
                     tc_decay=100.0,
65
                     tc_trace=20.0,
66
                ),
67
                name = "Y",
68
           )
69
70
           w = 0.3 * torch.rand(self.n_inpt, self.n_neurons)
71
            self.add_connection(
72
                Connection(
                     source=self.layers["X"],
74
                     target=self.layers["Y"],
75
                     w = w,
76
                     update_rule=PostPre,
77
                     nu=nu,
78
                     reduction=reduction,
79
                     wmin=wmin,
80
                     wmax=wmax,
81
82
                     norm=norm,
                ),
83
                source="X",
84
                target="Y",
85
           )
86
87
88
  class DiehlAndCook2015(Network):
89
       # language=rst
90
       0.0.0
91
       Implements the spiking neural network architecture from '(Diehl
92
      & Cook 2015)
       <https://www.frontiersin.org/articles/10.3389/fncom.2015.00099/</pre>
93
      full>'_.
       0.0.0
94
95
       def __init__(
96
            self,
97
           n_inpt: int,
98
            n_neurons: int = 100,
99
            exc: float = 22.5,
100
            inh: float = 17.5,
101
           dt: float = 1.0,
102
           nu: Optional[Union[float, Sequence[float]]] = (1e-4, 1e-2),
103
            reduction: Optional[callable] = None,
104
            wmin: float = 0.0,
105
           wmax: float = 1.0,
106
           norm: float = 78.4,
107
```

```
theta_plus: float = 0.05,
108
           tc_theta_decay: float = 1e7,
109
           inpt_shape: Optional[Iterable[int]] = None,
111
      ) \rightarrow None:
           # language=rst
112
           .....
113
           Constructor for class ''DiehlAndCook2015''.
114
           :param n_inpt: Number of input neurons. Matches the 1D size
116
      of the input data.
           :param n_neurons: Number of excitatory, inhibitory neurons.
117
           :param exc: Strength of synapse weights from excitatory to
118
      inhibitory layer.
           :param inh: Strength of synapse weights from inhibitory to
119
      excitatory layer.
           :param dt: Simulation time step.
120
           :param nu: Single or pair of learning rates for pre- and
      post-synaptic events,
               respectively.
122
           :param reduction: Method for reducing parameter updates
      along the minibatch
               dimension.
124
           :param wmin: Minimum allowed weight on input to excitatory
125
      synapses.
           :param wmax: Maximum allowed weight on input to excitatory
126
      synapses.
           :param norm: Input to excitatory layer connection weights
127
      normalization
               constant.
128
           :param theta_plus: On-spike increment of 'DiehlAndCookNodes
129
      ' ' membrane
               threshold potential.
130
           :param tc_theta_decay: Time constant of 'DiehlAndCookNodes
      ' threshold
               potential decay.
           :param inpt_shape: The dimensionality of the input layer.
           0.0.0
134
           super().__init__(dt=dt)
135
136
           self.n_inpt = n_inpt
           self.inpt_shape = inpt_shape
138
           self.n_neurons = n_neurons
139
           self.exc = exc
140
           self.inh = inh
141
           self.dt = dt
142
143
           # Layers
144
           input_layer = Input(
145
               n=self.n_inpt, shape=self.inpt_shape, traces=True,
146
      tc_trace=20.0
           )
147
           exc_layer = DiehlAndCookNodes(
148
               n=self.n_neurons,
149
               traces=True,
150
```

```
rest=-65.0,
151
                reset = -60.0,
152
                thresh = -52.0,
153
154
                refrac=5,
                tc_decay = 100.0,
155
                tc_trace=20.0,
156
                theta_plus=theta_plus,
157
                tc_theta_decay=tc_theta_decay,
158
           )
159
           inh_layer = LIFNodes(
160
                n=self.n_neurons,
161
                traces=False,
162
                rest=-60.0,
163
                reset = -45.0
164
                thresh = -40.0,
165
                tc_decay=10.0,
166
                refrac=2,
167
                tc_trace=20.0,
168
           )
169
           # Connections
           w = 0.3 * torch.rand(self.n_inpt, self.n_neurons)
           input_exc_conn = Connection(
                source=input_layer,
174
                target=exc_layer,
                w = w,
176
177
                update_rule=PostPre,
                nu=nu,
178
                reduction=reduction,
179
180
                wmin=wmin,
                wmax=wmax,
181
                norm=norm,
182
           )
183
           w = self.exc * torch.diag(torch.ones(self.n_neurons))
184
            exc_inh_conn = Connection(
185
                source=exc_layer, target=inh_layer, w=w, wmin=0, wmax=
186
      self.exc
           )
187
           w = -self.inh * (
188
                torch.ones(self.n_neurons, self.n_neurons)
189
                - torch.diag(torch.ones(self.n_neurons))
190
           )
191
           inh_exc_conn = Connection(
192
                source=inh_layer, target=exc_layer, w=w, wmin=-self.inh,
193
       wmax=0
           )
194
195
           # Add to network
196
           self.add_layer(input_layer, name="X")
197
           self.add_layer(exc_layer, name="Ae")
198
            self.add_layer(inh_layer, name="Ai")
199
           self.add_connection(input_exc_conn, source="X", target="Ae")
200
           self.add_connection(exc_inh_conn, source="Ae", target="Ai")
201
           self.add_connection(inh_exc_conn, source="Ai", target="Ae")
202
```

```
203
204
  class DiehlAndCook2015v2(Network):
205
206
      # language=rst
      0.0.0
207
      Slightly modifies the spiking neural network architecture from
208
      '(Diehl & Cook 2015)
      <https://www.frontiersin.org/articles/10.3389/fncom.2015.00099/</pre>
209
      full>'_ by removing
      the inhibitory layer and replacing it with a recurrent
210
      inhibitory connection in the
      output layer (what used to be the excitatory layer).
       .....
      def __init__(
214
           self.
           n_inpt: int,
           n_neurons: int = 100,
           inh: float = 17.5,
218
          dt: float = 1.0,
219
           nu: Optional[Union[float, Sequence[float]]] = (1e-4, 1e-2),
220
           reduction: Optional[callable] = None,
221
           wmin: Optional[float] = 0.0,
222
           wmax: Optional[float] = 1.0,
           norm: float = 78.4,
           theta_plus: float = 0.05,
           tc_theta_decay: float = 1e7,
226
           inpt_shape: Optional[Iterable[int]] = None,
      ) -> None:
228
           # language=rst
229
           0.0.0
230
           Constructor for class ''DiehlAndCook2015v2''.
           :param n_inpt: Number of input neurons. Matches the 1D size
      of the input data.
           :param n_neurons: Number of excitatory, inhibitory neurons.
234
           :param inh: Strength of synapse weights from inhibitory to
      excitatory layer.
           :param dt: Simulation time step.
236
           :param nu: Single or pair of learning rates for pre- and
      post-synaptic events,
               respectively.
238
           :param reduction: Method for reducing parameter updates
239
      along the minibatch
               dimension.
240
           :param wmin: Minimum allowed weight on input to excitatory
241
      synapses.
           :param wmax: Maximum allowed weight on input to excitatory
242
      synapses.
           :param norm: Input to excitatory layer connection weights
243
      normalization
               constant.
244
           :param theta_plus: On-spike increment of 'DiehlAndCookNodes
245
```

' ' membrane

```
threshold potential.
246
           :param tc_theta_decay: Time constant of ''DiehlAndCookNodes
247
      ' threshold
248
                potential decay.
           :param inpt_shape: The dimensionality of the input layer.
249
            0.0.0
250
           super().__init__(dt=dt)
251
252
           self.n_inpt = n_inpt
253
           self.inpt_shape = inpt_shape
254
           self.n_neurons = n_neurons
255
           self.inh = inh
256
           self.dt = dt
257
258
259
           input_layer = Input(
                n=self.n_inpt, shape=self.inpt_shape, traces=True,
260
      tc_trace=20.0
           )
261
           self.add_layer(input_layer, name="X")
262
263
            output_layer = DiehlAndCookNodes(
264
265
                n=self.n_neurons,
                traces=True,
266
                rest=-65.0,
267
                reset = -60.0
268
                thresh = -52.0,
269
                refrac=5,
270
                tc_decay=100.0,
                tc_trace=20.0,
272
                theta_plus=theta_plus,
                tc_theta_decay=tc_theta_decay,
274
           )
           self.add_layer(output_layer, name="Y")
276
277
           w = 0.3 * torch.rand(self.n_inpt, self.n_neurons)
278
           input_connection = Connection(
279
                source=self.layers["X"],
280
                target=self.layers["Y"],
281
                w = w,
282
                update_rule=PostPre,
283
284
                nu=nu,
                reduction=reduction,
285
                wmin=wmin,
286
                wmax=wmax,
287
                norm=norm,
288
           )
289
           self.add_connection(input_connection, source="X", target="Y"
290
      )
291
           w = -self.inh * (
292
                torch.ones(self.n_neurons, self.n_neurons)
293
                - torch.diag(torch.ones(self.n_neurons))
294
           )
295
           recurrent_connection = Connection(
296
```

```
source=self.layers["Y"],
297
                target=self.layers["Y"],
298
                w = w,
299
300
                wmin=-self.inh,
                wmax=0,
301
           )
302
           self.add_connection(recurrent_connection, source="Y", target
303
      = "Y")
304
305
  class IncreasingInhibitionNetwork(Network):
306
      # language=rst
307
       .....
308
       Implements the inhibitory layer structure of the spiking neural
309
      network architecture
       from '(Hazan et al. 2018) <https://arxiv.org/abs/1807.09374>'_
       0.0.0
311
312
       def __init__(
313
           self,
314
           n_input: int,
315
           n_neurons: int = 100,
316
           start_inhib: float = 1.0,
317
           max_inhib: float = 100.0,
318
           dt: float = 1.0,
319
           nu: Optional[Union[float, Sequence[float]]] = (1e-4, 1e-2),
           reduction: Optional[callable] = None,
321
           wmin: float = 0.0,
           wmax: float = 1.0,
           norm: float = 78.4,
324
           theta_plus: float = 0.05,
           tc_theta_decay: float = 1e7,
326
       ) \rightarrow None:
327
           # language=rst
328
           0.0.0
329
           Constructor for class ''IncreasingInhibitionNetwork''.
330
331
           :param n_inpt: Number of input neurons. Matches the 1D size
      of the input data.
           :param n_neurons: Number of excitatory, inhibitory neurons.
333
           :param inh: Strength of synapse weights from inhibitory to
334
      excitatory layer.
           :param dt: Simulation time step.
           :param nu: Single or pair of learning rates for pre- and
336
      post-synaptic events,
               respectively.
337
           :param reduction: Method for reducing parameter updates
338
      along the minibatch
               dimension.
339
           :param wmin: Minimum allowed weight on input to excitatory
340
      synapses.
           :param wmax: Maximum allowed weight on input to excitatory
341
      synapses.
           :param norm: Input to excitatory layer connection weights
342
```

```
normalization
                constant.
343
           :param theta_plus: On-spike increment of 'DiehlAndCookNodes
344
      " membrane
                threshold potential.
345
            :param tc_theta_decay: Time constant of 'DiehlAndCookNodes
346
      '' threshold
                potential decay.
347
            .....
348
           super().__init__(dt=dt)
349
350
           self.n_input = n_input
351
           self.n_neurons = n_neurons
352
           self.n_sqrt = int(np.sqrt(n_neurons))
353
           self.start_inhib = start_inhib
354
           self.max_inhib = max_inhib
355
           self.dt = dt
356
357
           input_layer = Input(n=self.n_input, traces=True, tc_trace
358
      =20.0)
           self.add_layer(input_layer, name="X")
359
360
            output_layer = DiehlAndCookNodes(
361
                n=self.n_neurons,
362
                traces=True,
363
                rest=-65.0,
364
                reset = -60.0,
365
                thresh = -52.0,
366
                refrac=5,
367
                tc_decay = 100.0,
368
                tc_trace=20.0,
369
                theta_plus=theta_plus,
                tc_theta_decay=tc_theta_decay,
371
           )
372
           self.add_layer(output_layer, name="Y")
373
374
           w = 0.3 * torch.rand(self.n_input, self.n_neurons)
375
           input_output_conn = Connection(
376
                source=self.layers["X"],
377
                target=self.layers["Y"],
378
379
                w = w,
                update_rule=PostPre,
380
                nu=nu,
381
                reduction=reduction,
382
                wmin=wmin,
383
                wmax=wmax,
384
                norm=norm,
385
           )
386
           self.add_connection(input_output_conn, source="X", target="Y
387
      ")
388
           w = torch.zeros(self.n_neurons, self.n_neurons)
389
           for i in range(self.n_neurons):
390
                for j in range(self.n_neurons):
391
```

```
if i != j:
392
                         x1, y1 = i // self.n_sqrt, i % self.n_sqrt
393
                         x2, y2 = j // self.n_sqrt, j % self.n_sqrt
394
395
                         inhib = self.start_inhib * np.sqrt(euclidean([x1
396
      , y1], [x2, y2]))
                         w[i, j] = -min(self.max_inhib, inhib)
397
398
           recurrent_output_conn = Connection(
399
                source=self.layers["Y"],
400
                target=self.layers["Y"],
401
                w = w,
402
                wmin=-self.max_inhib,
403
                wmax=0,
404
           )
405
           self.add_connection(recurrent_output_conn, source="Y",
406
      target="Y")
407
408
  class LocallyConnectedNetwork(Network):
409
       # language=rst
410
       .....
411
       Defines a two-layer network in which the input layer is "locally
412
       connected" to the
       output layer, and the output layer is recurrently inhibited
413
      connected such that
       neurons with the same input receptive field inhibit each other.
414
       .....
415
416
       def __init__(
417
           self,
418
           n_inpt: int,
419
           input_shape: List[int],
420
           kernel_size: Union[int, Tuple[int, int]],
421
           stride: Union[int, Tuple[int, int]],
422
423
           n_filters: int,
           inh: float = 25.0,
424
           dt: float = 1.0,
425
           nu: Optional[Union[float, Sequence[float]]] = (1e-4, 1e-2),
426
           reduction: Optional[callable] = None,
427
           theta_plus: float = 0.05,
428
           tc_theta_decay: float = 1e7,
429
           wmin: float = 0.0,
430
           wmax: float = 1.0,
431
           norm: Optional[float] = 0.2,
432
       ) \rightarrow None:
433
           # language=rst
434
           .....
435
           Constructor for class 'LocallyConnectedNetwork''. Uses ''
436
      DiehlAndCookNodes'' to
           avoid multiple spikes per timestep in the output layer
437
      population.
438
           :param n_inpt: Number of input neurons. Matches the 1D size
439
```

```
of the input data.
           :param input_shape: Two-dimensional shape of input
440
      population.
441
           :param kernel_size: Size of input windows. Integer or two-
      tuple of integers.
           :param stride: Length of horizontal, vertical stride across
442
      input space. Integer
               or two-tuple of integers.
443
           :param n_filters: Number of locally connected filters per
444
      input region. Integer
               or two-tuple of integers.
445
           :param inh: Strength of synapse weights from output layer
446
      back onto itself.
           :param dt: Simulation time step.
447
           :param nu: Single or pair of learning rates for pre- and
448
      post-synaptic events,
               respectively.
449
           :param reduction: Method for reducing parameter updates
450
      along the minibatch
               dimension.
451
           :param wmin: Minimum allowed weight on ''Input'' to ''
452
      DiehlAndCookNodes''
               synapses.
453
           :param wmax: Maximum allowed weight on ''Input'' to ''
454
      DiehlAndCookNodes''
               synapses.
455
           :param theta_plus: On-spike increment of 'DiehlAndCookNodes
456
      " membrane
               threshold potential.
457
           :param tc_theta_decay: Time constant of 'DiehlAndCookNodes
458
      '' threshold
               potential decay.
459
           :param norm: ''Input'' to ''DiehlAndCookNodes'' layer
460
      connection weights
               normalization constant.
461
           ......
462
           super().__init__(dt=dt)
463
464
           kernel_size = _pair(kernel_size)
465
           stride = _pair(stride)
466
467
           self.n_inpt = n_inpt
468
           self.input_shape = input_shape
469
           self.kernel_size = kernel_size
470
           self.stride = stride
471
           self.n_filters = n_filters
472
           self.inh = inh
473
           self.dt = dt
474
           self.theta_plus = theta_plus
475
           self.tc_theta_decay = tc_theta_decay
476
           self.wmin = wmin
477
           self.wmax = wmax
478
           self.norm = norm
479
480
```

```
if kernel_size == input_shape:
481
                conv_size = [1, 1]
482
           else:
483
484
                conv_size = (
                     int((input_shape[0] - kernel_size[0]) / stride[0]) +
485
       1,
                    int((input_shape[1] - kernel_size[1]) / stride[1]) +
486
       1,
                )
487
488
           input_layer = Input(n=self.n_inpt, traces=True, tc_trace
489
      =20.0)
490
            output_layer = DiehlAndCookNodes(
491
                n=self.n_filters * conv_size[0] * conv_size[1],
492
                traces=True,
493
                rest=-65.0,
494
                reset = -60.0,
495
                thresh = -52.0,
496
                refrac=5,
497
                tc_decay=100.0,
498
                tc_trace=20.0,
499
                theta_plus=theta_plus,
500
                tc_theta_decay=tc_theta_decay,
501
           )
502
503
           input_output_conn = LocalConnection(
504
                input_layer,
                output_layer,
505
                kernel_size=kernel_size,
506
507
                stride=stride,
                n_filters=n_filters,
508
                nu=nu,
509
                reduction=reduction,
510
                update_rule=PostPre,
511
                wmin=wmin,
512
513
                wmax=wmax,
                norm=norm,
514
                input_shape=input_shape,
515
           )
516
517
           w = torch.zeros(n_filters, *conv_size, n_filters, *conv_size
518
      )
           for fltr1 in range(n_filters):
519
                for fltr2 in range(n_filters):
520
                     if fltr1 != fltr2:
521
                         for i in range(conv_size[0]):
522
                              for j in range(conv_size[1]):
523
                                  w[fltr1, i, j, fltr2, i, j] = -inh
524
525
           w = w.view(
526
                n_filters * conv_size[0] * conv_size[1],
527
                n_filters * conv_size[0] * conv_size[1],
528
           )
529
           recurrent_conn = Connection(output_layer, output_layer, w=w)
530
```

```
532 self.add_layer(input_layer, name="X")
533 self.add_layer(output_layer, name="Y")
534 self.add_connection(input_output_conn, source="X", target="Y")
535 self.add_connection(recurrent_conn, source="Y", target="Y")
```

Listing B.22: Models

B.8 Learning

531

```
1 from .learning import (
      LearningRule,
2
      NoOp,
3
      PostPre,
4
      WeightDependentPostPre,
5
      Hebbian,
6
      MSTDP,
7
      MSTDPET,
8
      Rmax,
9
10)
```

Listing B.23: Initialization

```
1 from abc import ABC
2 from typing import Union, Optional, Sequence
4 import torch
5 import numpy as np
6
7 from ...network.nodes import SRMONodes
8 from ..network.topology import (
      AbstractConnection,
9
      Connection,
10
      Conv2dConnection,
11
     LocalConnection,
12
13)
14 from ..utils import im2col_indices
15
16
17 class LearningRule(ABC):
18
      # language=rst
      0.0.0
19
20
      Abstract base class for learning rules.
      ......
21
22
      def __init__(
23
24
           self,
25
           connection: AbstractConnection,
          nu: Optional[Union[float, Sequence[float]]] = None,
26
          reduction: Optional[callable] = None,
27
           weight_decay: float = 0.0,
28
           **kwargs
29
      ) -> None:
30
```

```
# language=rst
31
          .....
32
          Abstract constructor for the ''LearningRule'' object.
34
          :param connection: An 'AbstractConnection' object.
35
           :param nu: Single or pair of learning rates for pre- and
36
     post-synaptic events.
          :param reduction: Method for reducing parameter updates
37
     along the batch
               dimension.
38
          :param weight_decay: Constant multiple to decay weights by
39
     on each iteration.
          .....
40
          # Connection parameters.
41
42
          self.connection = connection
          self.source = connection.source
43
          self.target = connection.target
44
45
          self.wmin = connection.wmin
46
          self.wmax = connection.wmax
47
48
          # Learning rate(s).
40
          if nu is None:
50
               nu = [0.0, 0.0]
51
          elif isinstance(nu, float) or isinstance(nu, int):
52
               nu = [nu, nu]
53
54
          self.nu = nu
55
56
          # Parameter update reduction across minibatch dimension.
57
          if reduction is None:
58
               reduction = torch.mean
59
60
          self.reduction = reduction
61
62
          # Weight decay.
63
          self.weight_decay = weight_decay
64
65
      def update(self) -> None:
66
          # language=rst
67
          ......
68
          Abstract method for a learning rule update.
69
          0.0.0
70
          # Implement weight decay.
71
          if self.weight_decay:
72
               self.connection.w -= self.weight_decay * self.connection
     . W
74
          # Bound weights.
75
          if (
76
               self.connection.wmin != -np.inf or self.connection.wmax
77
     != np.inf
          ) and not isinstance(self, NoOp):
78
               self.connection.w.clamp_(self.connection.wmin, self.
79
```

```
connection.wmax)
80
81
82 class NoOp(LearningRule):
       # language=rst
83
       .....
84
       Learning rule with no effect.
85
       .....
86
87
       def __init__(
88
           self,
89
           connection: AbstractConnection,
90
           nu: Optional[Union[float, Sequence[float]]] = None,
91
           reduction: Optional[callable] = None,
92
           weight_decay: float = 0.0,
93
           **kwargs
94
       ) \rightarrow None:
95
           # language=rst
96
           .....
97
           Abstract constructor for the ''LearningRule'' object.
98
99
           :param connection: An 'AbstractConnection' object.
100
           :param nu: Single or pair of learning rates for pre- and
101
      post-synaptic events.
           :param reduction: Method for reducing parameter updates
102
      along the batch
                dimension.
103
            :param weight_decay: Constant multiple to decay weights by
104
      on each iteration.
           0.0.0
105
           super().__init__(
106
                connection=connection,
107
                nu=nu.
108
                reduction=reduction,
109
                weight_decay=weight_decay,
                **kwargs
           )
113
       def update(self, **kwargs) -> None:
114
           # language=rst
115
           0.0.0
116
117
           Abstract method for a learning rule update.
           0.0.0
118
           super().update()
119
120
  class PostPre(LearningRule):
122
       # language=rst
123
       .....
124
       Simple STDP rule involving both pre- and post-synaptic spiking
      activity. By default,
       pre-synaptic update is negative and the post-synaptic update is
126
      positive.
       \mathbf{H} = \mathbf{H}
```

```
128
       def __init__(
129
           self,
130
131
           connection: AbstractConnection,
           nu: Optional[Union[float, Sequence[float]]] = None,
           reduction: Optional[callable] = None,
133
           weight_decay: float = 0.0,
134
           **kwargs
135
       ) -> None:
136
           # language=rst
           0.0.0
138
           Constructor for ''PostPre'' learning rule.
139
140
           :param connection: An ''AbstractConnection'' object whose
141
      weights the
                "PostPre" learning rule will modify.
142
           :param nu: Single or pair of learning rates for pre- and
143
      post-synaptic events.
           :param reduction: Method for reducing parameter updates
144
      along the batch
                dimension.
145
           :param weight_decay: Constant multiple to decay weights by
146
      on each iteration.
           .....
147
           super().__init__(
148
               connection=connection,
149
               nu=nu,
150
                reduction=reduction,
151
                weight_decay=weight_decay,
                **kwargs
153
           )
154
           assert (
156
               self.source.traces and self.target.traces
157
           ), "Both pre- and post-synaptic nodes must record spike
158
      traces."
159
           if isinstance(connection, (Connection, LocalConnection)):
160
                self.update = self._connection_update
161
           elif isinstance(connection, Conv2dConnection):
162
               self.update = self._conv2d_connection_update
163
           else:
164
               raise NotImplementedError(
165
                    "This learning rule is not supported for this
166
      Connection type."
               )
167
168
       def _connection_update(self, **kwargs) -> None:
169
           # language=rst
170
           0.0.0
171
           Post-pre learning rule for 'Connection' subclass of '
      AbstractConnection ''
           class.
173
           0.0.0
174
```

batch_size = self.source.batch_size 176 source_s = self.source.s.view(batch_size, -1).unsqueeze(2). 177 float() source_x = self.source.x.view(batch_size, -1).unsqueeze(2) 178 target_s = self.target.s.view(batch_size, -1).unsqueeze(1). 179 float() target_x = self.target.x.view(batch_size, -1).unsqueeze(1) 180 181 # Pre-synaptic update. 182 if self.nu[0]: 183 update = self.reduction(torch.bmm(source_s, target_x), 184 dim=0)self.connection.w -= self.nu[0] * update 185 186 # Post-synaptic update. 187 if self.nu[1]: 188 update = self.reduction(torch.bmm(source_x, target_s), 189 dim=0) self.connection.w += self.nu[1] * update 190 191 super().update() 192 193 def _conv2d_connection_update(self, **kwargs) -> None: 194 # language=rst 195 196 Post-pre learning rule for 'Conv2dConnection' subclass of 197 'AbstractConnection' class. 198 0.0.0 199 # Get convolutional layer parameters. 200 out_channels, _, kernel_height, kernel_width = self. 201 connection.w.size() padding, stride = self.connection.padding, self.connection. 202 stride batch_size = self.source.batch_size 203 204 # Reshaping spike traces and spike occurrences. 205 source_x = im2col_indices(206 self.source.x, kernel_height, kernel_width, padding= 207 padding, stride=stride 208) target_x = self.target.x.view(batch_size, out_channels, -1) 209 source_s = im2col_indices(self.source.s.float(), 211 kernel_height, kernel_width, padding=padding, 214 stride=stride,) 216 target_s = self.target.s.view(batch_size, out_channels, -1). 217 float() 218 # Pre-synaptic update. 219 if self.nu[0]: 220

```
pre = self.reduction(
221
                    torch.bmm(target_x, source_s.permute((0, 2, 1))),
      dim=0
223
               )
               self.connection.w -= self.nu[0] * pre.view(self.
224
      connection.w.size())
           # Post-synaptic update.
226
           if self.nu[1]:
               post = self.reduction(
228
                    torch.bmm(target_s, source_x.permute((0, 2, 1))),
229
      dim=0
               )
230
               self.connection.w += self.nu[1] * post.view(self.
      connection.w.size())
           super().update()
234
236 class WeightDependentPostPre(LearningRule):
      # language=rst
       .....
238
      STDP rule involving both pre- and post-synaptic spiking activity
239
      . The post-synaptic
      update is positive and the pre- synaptic update is negative, and
240
       both are dependent
      on the magnitude of the synaptic weights.
241
       0.0.0
242
243
      def __init__(
244
           self,
245
           connection: AbstractConnection,
246
           nu: Optional[Union[float, Sequence[float]]] = None,
247
           reduction: Optional[callable] = None,
248
           weight_decay: float = 0.0,
249
           **kwargs
250
      ) \rightarrow None:
251
           # language=rst
252
           0.0.0
253
           Constructor for 'WeightDependentPostPre' learning rule.
254
255
           :param connection: An 'AbstractConnection' object whose
256
      weights the
                "WeightDependentPostPre" learning rule will modify.
257
           :param nu: Single or pair of learning rates for pre- and
258
      post-synaptic events.
           :param reduction: Method for reducing parameter updates
259
      along the batch
               dimension.
260
           :param weight_decay: Constant multiple to decay weights by
261
      on each iteration.
           0.0.0
262
           super().__init__(
263
               connection=connection,
264
```

```
nu=nu,
265
               reduction=reduction,
266
               weight_decay=weight_decay,
267
268
               **kwargs
           )
269
270
           assert self.source.traces, "Pre-synaptic nodes must record
271
      spike traces."
           assert (
               connection.wmin != -np.inf and connection.wmax != np.inf
273
           ), "Connection must define finite wmin and wmax."
274
275
           self.wmin = connection.wmin
276
           self.wmax = connection.wmax
278
           if isinstance(connection, (Connection, LocalConnection)):
279
               self.update = self._connection_update
280
           elif isinstance(connection, Conv2dConnection):
281
               self.update = self._conv2d_connection_update
282
           else:
283
               raise NotImplementedError(
284
                    "This learning rule is not supported for this
285
      Connection type."
               )
286
287
      def _connection_update(self, **kwargs) -> None:
288
           # language=rst
289
           0.0.0
290
           Post-pre learning rule for "Connection" subclass of "
291
      AbstractConnection''
           class.
292
           .....
293
           batch_size = self.source.batch_size
294
295
           source_s = self.source.s.view(batch_size, -1).unsqueeze(2).
296
      float()
           source_x = self.source.x.view(batch_size, -1).unsqueeze(2)
297
           target_s = self.target.s.view(batch_size, -1).unsqueeze(1).
298
      float()
           target_x = self.target.x.view(batch_size, -1).unsqueeze(1)
299
300
           update = 0
301
302
           # Pre-synaptic update.
303
           if self.nu[0]:
304
               outer_product = self.reduction(torch.bmm(source_s,
305
      target_x), dim=0)
               update -= self.nu[0] * outer_product * (self.connection.
306
      w - self.wmin)
307
           # Post-synaptic update.
308
           if self.nu[1]:
309
               outer_product = self.reduction(torch.bmm(source_x,
310
      target_s), dim=0)
```

```
update += self.nu[1] * outer_product * (self.wmax - self
311
      .connection.w)
312
313
           self.connection.w += update
314
           super().update()
315
316
       def _conv2d_connection_update(self, **kwargs) -> None:
317
           # language=rst
318
           0.0.0
319
           Post-pre learning rule for 'Conv2dConnection' subclass of
320
           'AbstractConnection' class.
321
           0.0.0
           # Get convolutional layer parameters.
           (
324
                out_channels,
                in_channels,
326
                kernel_height,
327
               kernel_width,
328
           ) = self.connection.w.size()
329
           padding, stride = self.connection.padding, self.connection.
330
      stride
           batch_size = self.source.batch_size
331
           # Reshaping spike traces and spike occurrences.
           source_x = im2col_indices(
334
                self.source.x, kernel_height, kernel_width, padding=
335
      padding, stride=stride
           )
336
           target_x = self.target.x.view(batch_size, out_channels, -1)
337
           source_s = im2col_indices(
338
                self.source.s.float(),
339
                kernel_height,
340
                kernel_width,
341
                padding=padding,
342
343
                stride=stride,
           )
344
           target_s = self.target.s.view(batch_size, out_channels, -1).
345
      float()
346
           update = 0
347
348
           # Pre-synaptic update.
349
           if self.nu[0]:
350
               pre = self.reduction(
351
                    torch.bmm(target_x, source_s.permute((0, 2, 1))),
352
      dim=0
                )
353
                update -= (
354
                    self.nu[0]
355
                    * pre.view(self.connection.w.size())
356
                    * (self.connection.w - self.wmin)
357
                )
358
359
```

```
# Post-synaptic update.
360
           if self.nu[1]:
361
                post = self.reduction(
362
363
                     torch.bmm(target_s, source_x.permute((0, 2, 1))),
      dim=0
                )
364
                update += (
365
                    self.nu[1]
366
                    * post.view(self.connection.w.size())
367
                     * (self.wmax - self.connection.wmin)
368
                )
369
           self.connection.w += update
371
372
           super().update()
374
375
  class Hebbian(LearningRule):
376
       # language=rst
377
       0.0.0
378
       Simple Hebbian learning rule. Pre- and post-synaptic updates are
379
       both positive.
       .....
380
381
       def __init__(
382
           self,
383
           connection: AbstractConnection,
384
           nu: Optional[Union[float, Sequence[float]]] = None,
385
           reduction: Optional[callable] = None,
386
           weight_decay: float = 0.0,
387
           **kwargs
388
       ) \rightarrow None:
389
           # language=rst
390
            0.0.0
391
           Constructor for 'Hebbian' learning rule.
392
393
            :param connection: An 'AbstractConnection' object whose
394
      weights the
                "Hebbian" learning rule will modify.
395
           :param nu: Single or pair of learning rates for pre- and
396
      post-synaptic events.
           :param reduction: Method for reducing parameter updates
397
      along the batch
                dimension.
398
           :param weight_decay: Constant multiple to decay weights by
399
      on each iteration.
           .....
400
           super().__init__(
401
                connection=connection,
402
                nu=nu.
403
                reduction=reduction,
404
                weight_decay=weight_decay,
405
                **kwargs
406
           )
407
```

```
408
           assert (
409
               self.source.traces and self.target.traces
410
411
           ), "Both pre- and post-synaptic nodes must record spike
      traces."
412
           if isinstance(connection, (Connection, LocalConnection)):
413
               self.update = self._connection_update
414
           elif isinstance(connection, Conv2dConnection):
415
               self.update = self._conv2d_connection_update
416
           else:
417
               raise NotImplementedError(
418
                    "This learning rule is not supported for this
419
      Connection type."
               )
420
421
      def _connection_update(self, **kwargs) -> None:
422
           # language=rst
423
           .....
424
           Hebbian learning rule for "Connection" subclass of "
425
      AbstractConnection ''
           class.
426
           0.0.0
427
           batch_size = self.source.batch_size
428
429
430
           source_s = self.source.s.view(batch_size, -1).unsqueeze(2).
      float()
           source_x = self.source.x.view(batch_size, -1).unsqueeze(2)
431
           target_s = self.target.s.view(batch_size, -1).unsqueeze(1).
432
      float()
           target_x = self.target.x.view(batch_size, -1).unsqueeze(1)
433
434
           # Pre-synaptic update.
435
           update = self.reduction(torch.bmm(source_s, target_x), dim
436
      =0)
437
           self.connection.w += self.nu[0] * update
438
           # Post-synaptic update.
439
           update = self.reduction(torch.bmm(source_x, target_s), dim
440
      =0)
           self.connection.w += self.nu[1] * update
441
442
           super().update()
443
444
      def _conv2d_connection_update(self, **kwargs) -> None:
445
           # language=rst
446
           ......
447
           Hebbian learning rule for 'Conv2dConnection' subclass of
448
           'AbstractConnection' class.
449
           0.0.0
450
           out_channels, _, kernel_height, kernel_width = self.
451
      connection.w.size()
           padding, stride = self.connection.padding, self.connection.
452
      stride
```

```
batch_size = self.source.batch_size
453
454
           # Reshaping spike traces and spike occurrences.
455
456
           source_x = im2col_indices(
                self.source.x, kernel_height, kernel_width, padding=
457
      padding, stride=stride
           )
458
           target_x = self.target.x.view(batch_size, out_channels, -1)
459
           source_s = im2col_indices(
460
                self.source.s.float(),
461
                kernel_height,
462
                kernel_width,
463
                padding=padding,
464
                stride=stride,
465
           )
466
           target_s = self.target.s.view(batch_size, out_channels, -1).
467
      float()
468
           # Pre-synaptic update.
469
           pre = self.reduction(torch.bmm(target_x, source_s.permute
470
      ((0, 2, 1))), dim=0)
           self.connection.w += self.nu[0] * pre.view(self.connection.w
471
      .size())
472
           # Post-synaptic update.
473
           post = self.reduction(torch.bmm(target_s, source_x.permute
474
      ((0, 2, 1))), dim=0)
           self.connection.w += self.nu[1] * post.view(self.connection.
475
      w.size())
476
           super().update()
477
478
479
  class MSTDP(LearningRule):
480
      # language=rst
481
       .....
482
       Reward-modulated STDP. Adapted from '(Florian 2007)
483
       <https://florian.io/papers/2007_Florian_Modulated_STDP.pdf>'_.
484
       0.0.0
485
486
       def __init__(
487
           self,
488
           connection: AbstractConnection,
489
           nu: Optional[Union[float, Sequence[float]]] = None,
490
           reduction: Optional[callable] = None,
491
           weight_decay: float = 0.0,
492
           **kwargs
493
       ) -> None:
494
           # language=rst
495
           0.0.0
496
           Constructor for 'MSTDP'' learning rule.
497
498
           :param connection: An 'AbstractConnection' object whose
499
      weights the ''MSTDP''
```

```
learning rule will modify.
500
           :param nu: Single or pair of learning rates for pre- and
501
      post-synaptic events,
502
               respectively.
           :param reduction: Method for reducing parameter updates
503
      along the minibatch
                dimension.
504
           :param weight_decay: Constant multiple to decay weights by
505
      on each iteration.
506
           Keyword arguments:
507
508
           :param tc_plus: Time constant for pre-synaptic firing trace.
509
           :param tc_minus: Time constant for post-synaptic firing
510
      trace.
           0.0.0
511
           super().__init__(
512
               connection=connection,
513
               nu=nu,
514
               reduction=reduction,
515
                weight_decay=weight_decay,
516
                **kwargs
517
           )
518
519
           if isinstance(connection, (Connection, LocalConnection)):
                self.update = self._connection_update
521
           elif isinstance(connection, Conv2dConnection):
522
                self.update = self._conv2d_connection_update
523
           else:
524
                raise NotImplementedError(
525
                    "This learning rule is not supported for this
526
      Connection type."
               )
527
528
           self.tc_plus = torch.tensor(kwargs.get("tc_plus", 20.0))
529
           self.tc_minus = torch.tensor(kwargs.get("tc_minus", 20.0))
530
531
       def _connection_update(self, **kwargs) -> None:
532
           # language=rst
533
534
           MSTDP learning rule for ''Connection'' subclass of ''
535
      AbstractConnection '' class.
536
           Keyword arguments:
537
538
           :param Union[float, torch.Tensor] reward: Reward signal from
539
       reinforcement
               learning task.
540
           :param float a_plus: Learning rate (post-synaptic).
541
           :param float a_minus: Learning rate (pre-synaptic).
542
           0.0.0
543
           batch_size = self.source.batch_size
544
545
           # Initialize eligibility, P^+, and P^-.
546
```

```
if not hasattr(self, "p_plus"):
547
               self.p_plus = torch.zeros(batch_size, *self.source.shape
548
      )
549
           if not hasattr(self, "p_minus"):
               self.p_minus = torch.zeros(batch_size, *self.target.
550
      shape)
           if not hasattr(self, "eligibility"):
551
               self.eligibility = torch.zeros(batch_size, *self.
552
      connection.w.shape)
553
           # Reshape pre- and post-synaptic spikes.
554
           source_s = self.source.s.view(batch_size, -1).float()
555
           target_s = self.target.s.view(batch_size, -1).float()
556
557
           # Parse keyword arguments.
558
           reward = kwargs["reward"]
559
           a_plus = torch.tensor(kwargs.get("a_plus", 1.0))
560
           a_minus = torch.tensor(kwargs.get("a_minus", -1.0))
561
562
           # Compute weight update based on the eligibility value of
563
      the past timestep.
           update = reward * self.eligibility
564
           self.connection.w += self.nu[0] * self.reduction(update, dim
565
      =0)
566
           # Update P^+ and P^- values.
567
           self.p_plus *= torch.exp(-self.connection.dt / self.tc_plus)
568
           self.p_plus += a_plus * source_s
569
           self.p_minus *= torch.exp(-self.connection.dt / self.
570
      tc_minus)
           self.p_minus += a_minus * target_s
571
572
           # Calculate point eligibility value.
573
           self.eligibility = torch.bmm(
574
               self.p_plus.unsqueeze(2), target_s.unsqueeze(1)
575
           ) + torch.bmm(source_s.unsqueeze(2), self.p_minus.unsqueeze
576
      (1))
577
578
           super().update()
579
      def _conv2d_connection_update(self, **kwargs) -> None:
580
           # language=rst
581
           0.0.0
582
           MSTDP learning rule for 'Conv2dConnection' subclass of '
583
      AbstractConnection ''
           class.
584
585
           Keyword arguments:
586
587
           :param Union[float, torch.Tensor] reward: Reward signal from
588
       reinforcement
               learning task.
589
           :param float a_plus: Learning rate (post-synaptic).
590
           :param float a_minus: Learning rate (pre-synaptic).
591
```

```
11 11 11
592
           batch_size = self.source.batch_size
593
594
595
           # Initialize eligibility.
           if not hasattr(self, "eligibility"):
596
               self.eligibility = torch.zeros(batch_size, *self.
597
      connection.w.shape)
598
           # Parse keyword arguments.
599
           reward = kwargs["reward"]
600
           a_plus = torch.tensor(kwargs.get("a_plus", 1.0))
601
           a_minus = torch.tensor(kwargs.get("a_minus", -1.0))
602
603
           batch_size = self.source.batch_size
604
605
           # Compute weight update based on the eligibility value of
606
      the past timestep.
           update = reward * self.eligibility
607
           self.connection.w += self.nu[0] * torch.sum(update, dim=0)
608
609
           out_channels, _, kernel_height, kernel_width = self.
610
      connection.w.size()
           padding, stride = self.connection.padding, self.connection.
611
      stride
612
           # Initialize P^+ and P^-.
613
           if not hasattr(self, "p_plus"):
614
               self.p_plus = torch.zeros(batch_size, *self.source.shape
615
      )
               self.p_plus = im2col_indices(
616
                    self.p_plus, kernel_height, kernel_width, padding=
617
      padding, stride=stride
               )
618
           if not hasattr(self, "p_minus"):
619
               self.p_minus = torch.zeros(batch_size, *self.target.
620
      shape)
               self.p_minus = self.p_minus.view(batch_size,
621
      out_channels, -1).float()
622
           # Reshaping spike occurrences.
623
           source_s = im2col_indices(
624
               self.source.s.float(),
625
               kernel_height,
626
               kernel_width,
627
               padding=padding,
628
               stride=stride,
629
           )
630
           target_s = self.target.s.view(batch_size, out_channels, -1).
631
      float()
632
           # Update P^+ and P^- values.
633
           self.p_plus *= torch.exp(-self.connection.dt / self.tc_plus)
634
           self.p_plus += a_plus * source_s
635
           self.p_minus *= torch.exp(-self.connection.dt / self.
636
```

```
tc_minus)
           self.p_minus += a_minus * target_s
637
638
639
           # Calculate point eligibility value.
           self.eligibility = torch.bmm(
640
                target_s, self.p_plus.permute((0, 2, 1))
641
           ) + torch.bmm(self.p_minus, source_s.permute((0, 2, 1)))
642
           self.eligibility = self.eligibility.view(self.connection.w.
643
      size())
644
           super().update()
645
646
647
  class MSTDPET(LearningRule):
648
       # language=rst
649
       0.0.0
650
       Reward-modulated STDP with eligibility trace. Adapted from
651
       (Florian 2007) <https://florian.io/papers/2007
652
      _Florian_Modulated_STDP.pdf>'_.
       0.0.0
653
654
       def __init__(
655
           self,
656
           connection: AbstractConnection,
657
           nu: Optional[Union[float, Sequence[float]]] = None,
658
           reduction: Optional[callable] = None,
659
           weight_decay: float = 0.0,
660
           **kwargs
661
       ) -> None:
662
663
           # language=rst
           0.0.0
664
           Constructor for 'MSTDPET'' learning rule.
665
666
           :param connection: An ''AbstractConnection'' object whose
667
      weights the
                "MSTDPET" learning rule will modify.
668
           :param nu: Single or pair of learning rates for pre- and
669
      post-synaptic events,
               respectively.
670
           :param reduction: Method for reducing parameter updates
671
      along the minibatch
               dimension.
672
           :param weight_decay: Constant multiple to decay weights by
673
      on each iteration.
674
           Keyword arguments:
675
676
           :param float tc_plus: Time constant for pre-synaptic firing
677
      trace.
           :param float tc_minus: Time constant for post-synaptic
678
      firing trace.
           :param float tc_e_trace: Time constant for the eligibility
679
      trace.
           0.0.0
680
```

```
super().__init__(
681
               connection=connection,
682
               nu=nu.
683
684
               reduction=reduction,
               weight_decay=weight_decay,
685
               **kwargs
686
           )
687
688
           if isinstance(connection, (Connection, LocalConnection)):
689
               self.update = self._connection_update
690
           elif isinstance(connection, Conv2dConnection):
691
               self.update = self._conv2d_connection_update
692
           else:
693
               raise NotImplementedError(
694
                    "This learning rule is not supported for this
695
      Connection type."
               )
696
697
           self.tc_plus = torch.tensor(kwargs.get("tc_plus", 20.0))
698
           self.tc_minus = torch.tensor(kwargs.get("tc_minus", 20.0))
699
           self.tc_e_trace = torch.tensor(kwargs.get("tc_e_trace",
700
      25.0))
701
      def _connection_update(self, **kwargs) -> None:
702
           # language=rst
703
           704
           MSTDPET learning rule for 'Connection' subclass of '
705
      AbstractConnection ''
           class.
706
707
           Keyword arguments:
708
709
           :param Union[float, torch.Tensor] reward: Reward signal from
       reinforcement
               learning task.
           :param float a_plus: Learning rate (post-synaptic).
           :param float a_minus: Learning rate (pre-synaptic).
           0.0.0
714
           # Initialize eligibility, eligibility trace, P<sup>+</sup>, and P<sup>-</sup>-.
           if not hasattr(self, "p_plus"):
716
               self.p_plus = torch.zeros(self.source.n)
717
           if not hasattr(self, "p_minus"):
718
               self.p_minus = torch.zeros(self.target.n)
719
           if not hasattr(self, "eligibility"):
720
               self.eligibility = torch.zeros(*self.connection.w.shape)
           if not hasattr(self, "eligibility_trace"):
722
               self.eligibility_trace = torch.zeros(*self.connection.w.
      shape)
724
           # Reshape pre- and post-synaptic spikes.
           source_s = self.source.s.view(-1).float()
726
           target_s = self.target.s.view(-1).float()
728
           # Parse keyword arguments.
729
```

```
reward = kwargs["reward"]
730
           a_plus = torch.tensor(kwargs.get("a_plus", 1.0))
           a_minus = torch.tensor(kwargs.get("a_minus", -1.0))
           # Calculate value of eligibility trace based on the value
734
           # of the point eligibility value of the past timestep.
           self.eligibility_trace *= torch.exp(-self.connection.dt /
736
      self.tc_e_trace)
           self.eligibility_trace += self.eligibility / self.tc_e_trace
738
           # Compute weight update.
739
           self.connection.w += (
740
               self.nu[0] * self.connection.dt * reward * self.
741
      eligibility_trace
           )
742
743
           # Update P^+ and P^- values.
744
           self.p_plus *= torch.exp(-self.connection.dt / self.tc_plus)
745
           self.p_plus += a_plus * source_s
746
           self.p_minus *= torch.exp(-self.connection.dt / self.
747
      tc_minus)
           self.p_minus += a_minus * target_s
748
749
           # Calculate point eligibility value.
750
           self.eligibility = torch.ger(self.p_plus, target_s) + torch.
751
      ger(
752
               source_s, self.p_minus
           )
753
754
           super().update()
755
756
      def _conv2d_connection_update(self, **kwargs) -> None:
757
           # language=rst
758
           ......
759
           MSTDPET learning rule for 'Conv2dConnection' subclass of
760
           'AbstractConnection' class.
761
762
           Keyword arguments:
763
764
           :param Union[float, torch.Tensor] reward: Reward signal from
765
       reinforcement
               learning task.
766
           :param float a_plus: Learning rate (post-synaptic).
767
           :param float a_minus: Learning rate (pre-synaptic).
768
           .....
769
           batch_size = self.source.batch_size
771
           # Initialize eligibility and eligibility trace.
           if not hasattr(self, "eligibility"):
773
               self.eligibility = torch.zeros(batch_size, *self.
774
      connection.w.shape)
           if not hasattr(self, "eligibility_trace"):
               self.eligibility_trace = torch.zeros(batch_size, *self.
776
      connection.w.shape)
```

```
777
           # Parse keyword arguments.
778
           reward = kwargs["reward"]
779
780
           a_plus = torch.tensor(kwargs.get("a_plus", 1.0))
           a_minus = torch.tensor(kwargs.get("a_minus", -1.0))
781
782
           # Calculate value of eligibility trace based on the value
783
           # of the point eligibility value of the past timestep.
784
           self.eligibility_trace *= torch.exp(-self.connection.dt /
785
      self.tc_e_trace)
786
           # Compute weight update.
787
           update = reward * self.eligibility_trace
788
           self.connection.w += self.nu[0] * self.connection.dt * torch
789
      .sum(update, dim=0)
790
           out_channels, _, kernel_height, kernel_width = self.
791
      connection.w.size()
           padding, stride = self.connection.padding, self.connection.
792
      stride
793
           # Initialize P^+ and P^-.
794
           if not hasattr(self, "p_plus"):
795
               self.p_plus = torch.zeros(batch_size, *self.source.shape
796
      )
               self.p_plus = im2col_indices(
797
                    self.p_plus, kernel_height, kernel_width, padding=
798
      padding, stride=stride
799
           if not hasattr(self, "p_minus"):
800
               self.p_minus = torch.zeros(batch_size, *self.target.
801
      shape)
               self.p_minus = self.p_minus.view(batch_size,
802
      out_channels, -1).float()
803
           # Reshaping spike occurrences.
804
           source_s = im2col_indices(
805
               self.source.s.float(),
806
               kernel_height,
807
               kernel_width,
808
               padding=padding,
809
               stride=stride,
810
           )
811
           target_s = (
812
               self.target.s.permute(1, 2, 3, 0).view(batch_size,
813
      out_channels, -1).float()
           )
814
815
           # Update P^+ and P^- values.
816
           self.p_plus *= torch.exp(-self.connection.dt / self.tc_plus)
817
           self.p_plus += a_plus * source_s
818
           self.p_minus *= torch.exp(-self.connection.dt / self.
819
      tc_minus)
           self.p_minus += a_minus * target_s
820
```

```
821
           # Calculate point eligibility value.
822
           self.eligibility = torch.bmm(
823
824
                target_s, self.p_plus.permute((0, 2, 1))
           ) + torch.bmm(self.p_minus, source_s.permute((0, 2, 1)))
825
           self.eligibility = self.eligibility.view(self.connection.w.
826
      size())
827
           super().update()
828
829
830
  class Rmax(LearningRule):
831
       # language=rst
832
       .....
833
      Reward-modulated learning rule derived from reward maximization
834
      principles. Adapted
       from '(Vasilaki et al., 2009)
835
       <https://intranet.physio.unibe.ch/Publikationen/Dokumente/</pre>
836
      Vasilaki2009PloSComputBio_1.pdf>'_.
       .....
837
838
       def __init__(
839
           self,
840
           connection: AbstractConnection,
841
           nu: Optional[Union[float, Sequence[float]]] = None,
842
           reduction: Optional[callable] = None,
843
           weight_decay: float = 0.0,
844
           **kwargs
845
       ) -> None:
846
           # language=rst
847
           0.0.0
848
           Constructor for "R-max" learning rule.
849
850
           :param connection: An 'AbstractConnection' object whose
851
      weights the "R-max"
               learning rule will modify.
852
           :param nu: Single or pair of learning rates for pre- and
853
      post-synaptic events,
               respectively.
85/
           :param reduction: Method for reducing parameter updates
855
      along the minibatch
               dimension.
856
           :param weight_decay: Constant multiple to decay weights by
857
      on each iteration.
858
           Keyword arguments:
859
860
           :param float tc_c: Time constant for balancing naive Hebbian
861
       and policy gradient
               learning.
862
           :param float tc_e_trace: Time constant for the eligibility
863
      trace.
           .....
864
           super().__init__(
865
```

```
connection=connection,
866
               nu=nu,
867
               reduction=reduction,
868
869
                weight_decay=weight_decay,
                **kwargs
870
           )
871
872
           # Trace is needed for computing epsilon.
873
           assert (
874
               self.source.traces and self.source.traces_additive
875
           ), "Pre-synaptic nodes must use additive spike traces."
876
877
           # Derivation of R-max depends on stochastic SRM neurons!
878
           assert isinstance(
879
               self.target, SRMONodes
880
           ), "R-max needs stochastically firing neurons, use SRMONodes
881
      . "
882
           if isinstance(connection, (Connection, LocalConnection)):
883
               self.update = self._connection_update
884
           else:
885
               raise NotImplementedError(
886
                    "This learning rule is not supported for this
887
      Connection type."
               )
888
889
           self.tc_c = torch.tensor(
890
               kwargs.get("tc_c", 5.0)
891
           )
             # 0 for pure naive Hebbian, inf for pure policy gradient.
892
           self.tc_e_trace = torch.tensor(kwargs.get("tc_e_trace",
893
      25.0))
894
       def _connection_update(self, **kwargs) -> None:
895
           # language=rst
896
           0.0.0
897
           R-max learning rule for ''Connection'' subclass of ''
898
      AbstractConnection '' class.
899
           Keyword arguments:
000
901
           :param Union[float, torch.Tensor] reward: Reward signal from
902
       reinforcement
               learning task.
903
           .....
904
           # Initialize eligibility trace.
905
           if not hasattr(self, "eligibility_trace"):
906
                self.eligibility_trace = torch.zeros(*self.connection.w.
907
      shape)
908
           # Reshape variables.
909
           target_s = self.target.s.view(-1).float()
910
           target_s_prob = self.target.s_prob.view(-1)
911
           source_x = self.source.x.view(-1)
912
913
```

```
# Parse keyword arguments.
914
           reward = kwargs["reward"]
915
916
           # New eligibility trace.
917
           self.eligibility_trace *= 1 - self.connection.dt / self.
918
      tc_e_trace
           self.eligibility_trace += (
919
               target_s
920
                - (target_s_prob / (1.0 + self.tc_c / self.connection.dt
921
       * target_s_prob))
           ) * source_x[:, None]
922
923
           # Compute weight update.
924
           self.connection.w += self.nu[0] * reward * self.
925
      eligibility_trace
926
           super().update()
927
```

Listing B.24: Learning

```
1 from abc import ABC, abstractmethod
3 import torch
4
5
6 class AbstractReward(ABC):
       # language=rst
7
       0.0.0
8
       Abstract base class for reward computation.
9
       ......
10
11
       @abstractmethod
12
       def compute(self, **kwargs) -> None:
13
            # language=rst
14
            ......
15
            Computes/modifies reward.
16
            \mathbf{H}_{\mathbf{H}} = \mathbf{H}_{\mathbf{H}}
17
            pass
18
19
       @abstractmethod
20
       def update(self, **kwargs) -> None:
21
            # language=rst
22
             0.0.0
23
            Updates internal variables needed to modify reward. Usually
24
      called once per
            episode.
25
            \mathbf{H}_{\mathbf{H}} = \mathbf{H}_{\mathbf{H}}
26
            pass
27
28
29
30 class MovingAvgRPE(AbstractReward):
       # language=rst
31
       0.0.0
32
       Computes reward prediction error (RPE) based on an exponential
33
```

```
moving average (EMA)
      of past rewards.
34
      .....
35
36
      def __init__(self, **kwargs) -> None:
37
           # language=rst
38
          .....
39
          Constructor for EMA reward prediction error.
40
          0.0.0
41
42
          self.reward_predict = torch.tensor(0.0) # Predicted reward
     (per step).
          self.reward_predict_episode = torch.tensor(0.0) # Predicted
43
      reward per episode.
          self.rewards_predict_episode = (
44
45
               []
          )
             # List of predicted rewards per episode (used for
46
     plotting).
47
      def compute(self, **kwargs) -> torch.Tensor:
48
          # language=rst
49
           .....
50
          Computes the reward prediction error using EMA.
51
52
          Keyword arguments:
53
54
          :param Union[float, torch.Tensor] reward: Current reward.
55
          :return: Reward prediction error.
56
          0.0.0
57
          # Get keyword arguments.
58
          reward = kwargs["reward"]
59
60
          return reward - self.reward_predict
61
62
      def update(self, **kwargs) -> None:
63
          # language=rst
64
           .....
65
          Updates the EMAs. Called once per episode.
66
67
          Keyword arguments:
68
69
          :param Union[float, torch.Tensor] accumulated_reward: Reward
70
      accumulated over
               one episode.
71
           :param int steps: Steps in that episode.
72
          :param float ema_window: Width of the averaging window.
73
          0.0.0
74
          # Get keyword arguments.
75
          accumulated_reward = kwargs["accumulated_reward"]
76
          steps = torch.tensor(kwargs["steps"]).float()
77
          ema_window = torch.tensor(kwargs.get("ema_window", 10.0))
78
79
          # Compute average reward per step.
80
          reward = accumulated_reward / steps
81
82
```

```
# Update EMAs.
83
          self.reward_predict = (
84
              1 - 1 / ema_window
85
          ) * self.reward_predict + 1 / ema_window * reward
86
          self.reward_predict_episode = (
87
              1 - 1 / ema_window
88
          ) * self.reward_predict_episode + 1 / ema_window *
89
     accumulated_reward
          self.rewards_predict_episode.append(self.
90
     reward_predict_episode.item())
```

```
Listing B.25: Reward
```

B.9 Evaluation

```
1 from .evaluation import (
     assign_labels,
2
     logreg_fit,
3
      logreg_predict,
4
     all_activity,
5
     proportion_weighting,
6
7
     ngram,
      update_ngram_scores,
8
9)
```

Listing B.26: Initialization

```
1 from itertools import product
2 from typing import Optional, Tuple, Dict
4 import torch
5 from sklearn.linear_model import LogisticRegression
6
8 def assign_labels(
      spikes: torch.Tensor,
9
      labels: torch.Tensor,
10
     n_labels: int,
11
      rates: Optional[torch.Tensor] = None,
12
13
      alpha: float = 1.0,
14 ) -> Tuple[torch.Tensor, torch.Tensor, torch.Tensor]:
      # language=rst
15
      0.0.0
16
     Assign labels to the neurons based on highest average spiking
17
     activity.
18
     :param spikes: Binary tensor of shape ''(n_samples, time,
19
     n_neurons)'' of a single
          layer's spiking activity.
20
      :param labels: Vector of shape ''(n_samples,)'' with data labels
      corresponding to
          spiking activity.
22
      :param n_labels: The number of target labels in the data.
23
```

```
:param rates: If passed, these represent spike rates from a
24
     previous
          ''assign_labels()'' call.
25
26
      :param alpha: Rate of decay of label assignments.
      :return: Tuple of class assignments, per-class spike proportions
27
     , and per-class
          firing rates.
28
      . . . .
29
30
      n_neurons = spikes.size(2)
31
      if rates is None:
32
          rates = torch.zeros(n_neurons, n_labels)
33
34
      # Sum over time dimension (spike ordering doesn't matter).
      spikes = spikes.sum(1)
36
37
      for i in range(n_labels):
38
          # Count the number of samples with this label.
39
          n_labeled = torch.sum(labels == i).float()
40
41
          if n_labeled > 0:
42
              # Get indices of samples with this label.
43
              indices = torch.nonzero(labels == i).view(-1)
44
45
              # Compute average firing rates for this label.
46
              rates[:, i] = alpha * rates[:, i] + (
47
                   torch.sum(spikes[indices], 0) / n_labeled
48
              )
49
50
      # Compute proportions of spike activity per class.
51
      proportions = rates / rates.sum(1, keepdim=True)
52
      proportions [proportions != proportions] = 0 # Set NaNs to 0
53
54
      # Neuron assignments are the labels they fire most for.
55
      assignments = torch.max(proportions, 1)[1]
56
57
      return assignments, proportions, rates
58
59
60
61 def logreg_fit(
      spikes: torch.Tensor, labels: torch.Tensor, logreg:
62
     LogisticRegression
63 ) -> LogisticRegression:
      # language=rst
64
65
      (Re)fit logistic regression model to spike data summed over time
66
67
      :param spikes: Summed (over time) spikes of shape ''(n_examples,
68
      time, n_neurons) ''.
      :param labels: Vector of shape ''(n_samples,)'' with data labels
69
      corresponding to
          spiking activity.
70
      :param logreg: Logistic regression model from previous fits.
71
```

```
:return: (Re)fitted logistic regression model.
72
      .....
      # (Re)fit logistic regression model.
74
75
      logreg.fit(spikes, labels)
      return logreg
76
77
78
79 def logreg_predict(spikes: torch.Tensor, logreg: LogisticRegression)
       -> torch.Tensor:
      # language=rst
80
       .....
81
      Predicts classes according to spike data summed over time.
82
83
      :param spikes: Summed (over time) spikes of shape ''(n_examples,
84
       time, n_neurons) ''.
      :param logreg: Logistic regression model from previous fits.
85
       :return: Predictions per example.
86
       .....
87
      # Make class label predictions.
88
      if not hasattr(logreg, "coef_") or logreg.coef_ is None:
89
           return -1 * torch.ones(spikes.size(0)).long()
90
91
      predictions = logreg.predict(spikes)
92
      return torch.Tensor(predictions).long()
93
94
95
96 def all_activity(
      spikes: torch.Tensor, assignments: torch.Tensor, n_labels: int
97
    -> torch.Tensor:
98)
      # language=rst
99
       0.0.0
100
      Classify data with the label with highest average spiking
101
      activity over all neurons.
102
      :param spikes: Binary tensor of shape ''(n_samples, time,
103
      n_neurons)'' of a layer's
           spiking activity.
104
      :param assignments: A vector of shape '((n_neurons,)'' of neuron
105
       label assignments.
       :param n_labels: The number of target labels in the data.
106
       :return: Predictions tensor of shape '((n_samples,)'' resulting
107
      from the "all
           activity" classification scheme.
108
       . . . .
109
      n_samples = spikes.size(0)
110
      # Sum over time dimension (spike ordering doesn't matter).
      spikes = spikes.sum(1)
114
      rates = torch.zeros(n_samples, n_labels)
      for i in range(n_labels):
116
           # Count the number of neurons with this label assignment.
117
           n_assigns = torch.sum(assignments == i).float()
118
119
```

```
if n_assigns > 0:
120
               # Get indices of samples with this label.
               indices = torch.nonzero(assignments == i).view(-1)
               # Compute layer-wise firing rate for this label.
124
               rates[:, i] = torch.sum(spikes[:, indices], 1) /
      n_assigns
126
      # Predictions are arg-max of layer-wise firing rates.
      return torch.sort(rates, dim=1, descending=True)[1][:, 0]
128
129
130
  def proportion_weighting(
131
      spikes: torch.Tensor,
      assignments: torch.Tensor,
      proportions: torch.Tensor,
134
      n_labels: int,
135
136 ) -> torch.Tensor:
      # language=rst
      0.0.0
138
      Classify data with the label with highest average spiking
139
      activity over all neurons,
      weighted by class-wise proportion.
140
141
      :param spikes: Binary tensor of shape ''(n_samples, time,
142
      n_neurons)'' of a single
           layer's spiking activity.
143
      :param assignments: A vector of shape '((n_neurons,)'' of neuron
144
       label assignments.
      :param proportions: A matrix of shape '(n_neurons, n_labels)''
145
      giving the per-class
           proportions of neuron spiking activity.
146
      :param n_labels: The number of target labels in the data.
147
      :return: Predictions tensor of shape '((n_samples,)'' resulting
148
      from the "proportion
           weighting" classification scheme.
149
       .....
150
      n_samples = spikes.size(0)
151
152
      # Sum over time dimension (spike ordering doesn't matter).
153
      spikes = spikes.sum(1)
154
155
      rates = torch.zeros(n_samples, n_labels)
156
      for i in range(n_labels):
157
           # Count the number of neurons with this label assignment.
158
           n_assigns = torch.sum(assignments == i).float()
159
160
           if n_assigns > 0:
161
               # Get indices of samples with this label.
162
               indices = torch.nonzero(assignments == i).view(-1)
163
164
               # Compute layer-wise firing rate for this label.
165
               rates[:, i] += (
166
                   torch.sum((proportions[:, i] * spikes)[:, indices],
167
```

```
1) / n_assigns
                )
168
169
170
       # Predictions are arg-max of layer-wise firing rates.
       predictions = torch.sort(rates, dim=1, descending=True)[1][:, 0]
172
       return predictions
173
174
175
176 def ngram(
       spikes: torch.Tensor,
       ngram_scores: Dict[Tuple[int, ...], torch.Tensor],
178
       n_labels: int,
179
      n: int,
180
    -> torch.Tensor:
181
  )
       # language=rst
182
       0.0.0
183
       Predicts between ''n_labels'' using ''ngram_scores''.
184
185
       :param spikes: Spikes of shape '(n_examples, time, n_neurons)
186
      c c .
       :param ngram_scores: Previously recorded scores to update.
187
       :param n_labels: The number of target labels in the data.
188
       :param n: The max size of n-gram to use.
189
       :return: Predictions per example.
190
       .....
191
       predictions = []
192
       for activity in spikes:
193
           score = torch.zeros(n_labels)
194
195
           # Aggregate all of the firing neurons' indices
196
           fire_order = []
197
           for t in range(activity.size()[0]):
198
               ordering = torch.nonzero(activity[t].view(-1))
199
               if ordering.numel() > 0:
200
                    fire_order += ordering[:, 0].tolist()
201
202
           # Consider all n-gram sequences.
203
           for j in range(len(fire_order) - n):
204
                if tuple(fire_order[j : j + n]) in ngram_scores:
205
                    score += ngram_scores[tuple(fire_order[j : j + n])]
206
207
           predictions.append(torch.argmax(score))
208
209
       return torch.tensor(predictions).long()
210
211
213 def update_ngram_scores(
       spikes: torch.Tensor,
214
       labels: torch.Tensor,
      n_labels: int,
      n: int,
217
      ngram_scores: Dict[Tuple[int, ...], torch.Tensor],
218
219 ) -> Dict[Tuple[int, ...], torch.Tensor]:
```

```
# language=rst
      .....
      Updates ngram scores by adding the count of each spike sequence
222
      of length n from the
      past ''n_examples''.
223
224
      :param spikes: Spikes of shape ''(n_examples, time, n_neurons)
      c c .
      :param labels: The ground truth labels of shape ''(n_examples)
226
      c c .
      :param n_labels: The number of target labels in the data.
      :param n: The max size of n-gram to use.
228
      :param ngram_scores: Previously recorded scores to update.
229
      :return: Dictionary mapping n-grams to vectors of per-class
230
      spike counts.
      0.0.0
      for i, activity in enumerate(spikes):
           # Obtain firing order for spiking activity.
           fire_order = []
234
           # Aggregate all of the firing neurons' indices.
236
           for t in range(spikes.size(1)):
               # Gets the indices of the neurons which fired on this
238
      timestep.
               ordering = torch.nonzero(activity[t]).view(-1)
239
               if ordering.numel() > 0: # If there was more than one
240
      spike...
                   # Add the indices of spiked neurons to the fire
241
      ordering.
                   ordering = ordering.tolist()
242
                   fire_order.append(ordering)
243
244
           # Check every sequence of length n.
245
           for order in zip(*(fire_order[k:] for k in range(n))):
246
               for sequence in product(*order):
247
                   if sequence not in ngram_scores:
248
                        ngram_scores[sequence] = torch.zeros(n_labels)
249
250
                   ngram_scores[sequence][int(labels[i])] += 1
251
252
      return ngram_scores
253
```

```
Listing B.27: Evaluation
```

B.10 Analysis

from . import plotting, visualization, pipeline_analysis
Listing B.28: Initialization

```
1 from abc import ABC, abstractmethod
2 from typing import Dict, Optional
3
4 import matplotlib.pyplot as plt
```

```
5 import numpy as np
6 import pandas as pd
7 import torch
8 from tensorboardX import SummaryWriter
9 from torchvision.utils import make_grid
10
in from .plotting import plot_spikes, plot_voltages,
     plot_conv2d_weights
12 from ..utils import reshape_conv2d_weights
13
14
15 class PipelineAnalyzer(ABC):
      # language=rst
16
      ......
17
      Responsible for pipeline analysis. Subclasses maintain state
18
      information related to plotting or logging.
19
      0.0.0
20
21
      @abstractmethod
      def finalize_step(self) -> None:
           # language=rst
24
           0.0.0
25
           Flush the output from the current step.
26
           0.0.0
27
28
           pass
29
      @abstractmethod
30
      def plot_obs(self, obs: torch.Tensor, tag: str = "obs", step:
31
     int = None) -> None:
32
           # language=rst
           0.0.0
33
           Pulls the observation from PyTorch and sets up for
34
     Matplotlib
           plotting.
35
36
           :param obs: A 2D array of floats depicting an input image.
37
           :param tag: A unique tag to associate the data with.
38
           :param step: The step of the pipeline.
39
           \mathbf{H}_{\mathbf{H}} = \mathbf{H}_{\mathbf{H}}
40
           pass
41
42
      @abstractmethod
43
      def plot_reward(
44
           self,
45
           reward_list: list,
46
           reward_window: int = None,
47
           tag: str = "reward",
48
           step: int = None,
49
      ) \rightarrow None:
50
           # language=rst
51
           0.0.0
52
           Plot the accumulated reward for each episode.
53
54
           :param reward_list: The list of recent rewards to be plotted
55
```

```
:param reward_window: The length of the window to compute a
56
      moving average over.
57
           :param tag: A unique tag to associate the data with.
           :param step: The step of the pipeline.
58
           0.0.0
59
           pass
60
61
       @abstractmethod
62
      def plot_spikes(
63
           self,
64
           spike_record: Dict[str, torch.Tensor],
65
           tag: str = "spike",
66
           step: int = None,
67
      ) \rightarrow None:
68
           # language=rst
69
           0.0.0
70
           Plots all spike records inside of 'spike_record'. Keeps
      unique
           plots for all unique tags that are given.
73
           :param spike_record: Dictionary of spikes to be rasterized.
74
           :param tag: A unique tag to associate the data with.
75
           :param step: The step of the pipeline.
76
           0.0.0
77
           pass
78
79
       @abstractmethod
80
      def plot_voltages(
81
82
           self,
           voltage_record: Dict[str, torch.Tensor],
83
           thresholds: Optional[Dict[str, torch.Tensor]] = None,
84
           tag: str = "voltage",
85
           step: int = None,
86
      ) \rightarrow None:
87
           # language=rst
88
           0.0.0
89
           Plots all voltage records and given thresholds. Keeps unique
90
           plots for all unique tags that are given.
91
92
           :param voltage_record: Dictionary of voltages for neurons
93
      inside of networks
                                     organized by the layer they
94
      correspond to.
           :param thresholds: Optional dictionary of threshold values
95
      for neurons.
           :param tag: A unique tag to associate the data with.
96
           :param step: The step of the pipeline.
97
           0.0.0
98
           pass
99
100
       @abstractmethod
101
      def plot_conv2d_weights(
102
           self, weights: torch.Tensor, tag: str = "conv2d", step: int
103
```

= None) -> None: 104 # language=rst 105 0.0.0 106 Plot a connection weight matrix of a "Conv2dConnection". 107 108 :param weights: Weight matrix of 'Conv2dConnection' object 109 :param tag: A unique tag to associate the data with. 110 :param step: The step of the pipeline. 0.0.0 pass 114 class MatplotlibAnalyzer(PipelineAnalyzer): 116 # language=rst 117 0.0.0 118 Renders output using Matplotlib. 119 120 Matplotlib requires objects to be kept around over the full 121 lifetime of the plots; this is done through "self.plots". An 122 interactive session is needed so that we can continue processing and just update the plots. 126 def __init__(self, **kwargs) -> None: # language=rst 128 129 Initializes the analyzer. 130 Keyword arguments: :param str volts_type: Type of plotting for voltages (''" 134 color"'' or ''line"''). self.volts_type = kwargs.get("volts_type", "color") 136 plt.ion() self.plots = {} 138 139 def plot_obs(self, obs: torch.Tensor, tag: str = "obs", step: 140 int = None) -> None: # language=rst 141 0.0.0 142 Pulls the observation off of torch and sets up for 143 Matplotlib plotting. 144 145 :param obs: A 2D array of floats depicting an input image. 146 :param tag: A unique tag to associate the data with. 147 :param step: The step of the pipeline. 148 0.0.0 149 obs = obs.detach().cpu().numpy() 150

```
obs = np.transpose(obs, (1, 2, 0)).squeeze()
151
152
           if tag in self.plots:
153
154
                obs_ax, obs_im = self.plots[tag]
           else:
155
                obs_ax, obs_im = None, None
156
157
           if obs_im is None and obs_ax is None:
158
                fig, obs_ax = plt.subplots()
159
                obs_ax.set_title("Observation")
160
                obs_ax.set_xticks(())
161
                obs_ax.set_yticks(())
162
                obs_im = obs_ax.imshow(obs, cmap="gray")
163
164
                self.plots[tag] = obs_ax, obs_im
165
           else:
166
                obs_im.set_data(obs)
167
168
       def plot_reward(
169
           self,
           reward_list: list,
171
           reward_window: int = None,
           tag: str = "reward",
173
           step: int = None,
174
       ) -> None:
175
           # language=rst
176
           0.0.0
177
           Plot the accumulated reward for each episode.
178
179
           :param reward_list: The list of recent rewards to be plotted
180
           :param reward_window: The length of the window to compute a
181
      moving average over.
           :param tag: A unique tag to associate the data with.
182
           :param step: The step of the pipeline.
183
           0.0.0
184
           if tag in self.plots:
185
                reward_im, reward_ax, reward_plot = self.plots[tag]
186
           else:
187
                reward_im, reward_ax, reward_plot = None, None, None
188
189
           # Compute moving average.
190
           if reward_window is not None:
191
                # Ensure window size > 0 and < size of reward list.
192
                window = max(min(len(reward_list), reward_window), 0)
193
194
                # Fastest implementation of moving average.
195
                reward_list_ = (
196
                    pd.Series(reward_list)
197
                    .rolling(window=window, min_periods=1)
198
                    .mean()
199
                    .values
200
                )
201
           else:
202
```

```
reward_list_ = reward_list[:]
203
204
           if reward_im is None and reward_ax is None:
205
206
               reward_im, reward_ax = plt.subplots()
               reward_ax.set_title("Accumulated reward")
207
               reward_ax.set_xlabel("Episode")
208
               reward_ax.set_ylabel("Reward")
209
               (reward_plot,) = reward_ax.plot(reward_list_)
210
               self.plots[tag] = reward_im, reward_ax, reward_plot
212
           else:
               reward_plot.set_data(range(len(reward_list_)),
214
      reward_list_)
               reward_ax.relim()
               reward_ax.autoscale_view()
217
      def plot_spikes(
218
           self,
219
           spike_record: Dict[str, torch.Tensor],
220
           tag: str = "spike",
           step: int = None,
222
      ) \rightarrow None:
           # language=rst
224
           .....
           Plots all spike records inside of 'spike_record'. Keeps
226
      unique
           plots for all unique tags that are given.
227
228
           :param spike_record: Dictionary of spikes to be rasterized.
229
           :param tag: A unique tag to associate the data with.
230
           :param step: The step of the pipeline.
           0.0.0
           if tag not in self.plots:
               self.plots[tag] = plot_spikes(spike_record)
234
           else:
               s_im, s_ax = self.plots[tag]
236
               self.plots[tag] = plot_spikes(spike_record, ims=s_im,
      axes=s_ax)
238
      def plot_voltages(
239
240
           self,
           voltage_record: Dict[str, torch.Tensor],
241
           thresholds: Optional[Dict[str, torch.Tensor]] = None,
242
           tag: str = "voltage",
243
           step: int = None,
244
      ) -> None:
245
           # language=rst
246
           247
           Plots all voltage records and given thresholds. Keeps unique
248
           plots for all unique tags that are given.
249
250
           :param voltage_record: Dictionary of voltages for neurons
251
      inside of networks
                                    organized by the layer they
252
```

```
correspond to.
           :param thresholds: Optional dictionary of threshold values
253
      for neurons.
254
           :param tag: A unique tag to associate the data with.
           :param step: The step of the pipeline.
255
           0.0.0
256
           if tag not in self.plots:
257
                self.plots[tag] = plot_voltages(
258
                    voltage_record, plot_type=self.volts_type,
259
      thresholds=thresholds
                )
260
           else:
261
                v_im, v_ax = self.plots[tag]
262
                self.plots[tag] = plot_voltages(
263
                    voltage_record,
264
                    ims=v_im,
265
                    axes=v_ax,
266
                    plot_type=self.volts_type,
267
                    thresholds=thresholds,
268
                )
269
270
       def plot_conv2d_weights(
271
           self, weights: torch.Tensor, tag: str = "conv2d", step: int
272
      = None
       ) -> None:
           # language=rst
274
           0.0.0
275
           Plot a connection weight matrix of a 'Conv2dConnection'.
276
           :param weights: Weight matrix of 'Conv2dConnection' object
278
           :param tag: A unique tag to associate the data with.
279
           :param step: The step of the pipeline.
280
           0.0.0
281
           wmin = weights.min().item()
282
           wmax = weights.max().item()
283
284
           if tag not in self.plots:
285
                self.plots[tag] = plot_conv2d_weights(weights, wmin,
286
      wmax)
           else:
287
                im = self.plots[tag]
288
                plot_conv2d_weights(weights, wmin, wmax, im=im)
289
290
       def finalize_step(self) -> None:
291
           # language=rst
292
           ......
293
           Flush the output from the current step
294
           ......
295
           plt.draw()
296
           plt.pause(1e-8)
297
           plt.show()
298
299
```

300

```
301 class TensorboardAnalyzer(PipelineAnalyzer):
       def __init__(self, summary_directory: str = "./logs"):
302
           # language=rst
303
           0.0.0
304
           Initializes the analyzer.
305
306
           :param summary_directory: Directory to save log files.
307
           ......
308
           self.writer = SummaryWriter(summary_directory)
309
       def finalize_step(self) -> None:
311
           # language=rst
312
           0.0.0
313
           No-op for ''TensorboardAnalyzer''.
314
           0.0.0
           pass
316
317
       def plot_obs(self, obs: torch.Tensor, tag: str = "obs", step:
318
      int = None) -> None:
           # language=rst
319
           0.0.0
320
           Pulls the observation off of torch and sets up for
321
      Matplotlib
           plotting.
           :param obs: A 2D array of floats depicting an input image.
324
           :param tag: A unique tag to associate the data with.
325
           :param step: The step of the pipeline.
326
           0.0.0
327
           obs_grid = make_grid(obs.float(), nrow=4, normalize=True)
328
           self.writer.add_image(tag, obs_grid, step)
330
       def plot_reward(
331
           self,
           reward_list: list,
           reward_window: int = None,
334
           tag: str = "reward",
           step: int = None,
336
       ) \rightarrow None:
           # language=rst
338
           ......
339
           Plot the accumulated reward for each episode.
340
341
           :param reward_list: The list of recent rewards to be plotted
342
           :param reward_window: The length of the window to compute a
343
      moving average over.
           :param tag: A unique tag to associate the data with.
344
           :param step: The step of the pipeline.
345
           0.0.0
346
           self.writer.add_scalar(tag, reward_list[-1], step)
347
348
       def plot_spikes(
349
           self,
350
```

```
spike_record: Dict[str, torch.Tensor],
351
           tag: str = "spike",
352
           step: int = None,
353
      ) \rightarrow None:
354
           # language=rst
355
           0.0.0
356
           Plots all spike records inside of 'spike_record''. Keeps
357
      unique
           plots for all unique tags that are given.
358
359
           :param spike_record: Dictionary of spikes to be rasterized.
360
           :param tag: A unique tag to associate the data with.
361
           :param step: The step of the pipeline.
362
           0.0.0
363
           for k, spikes in spike_record.items():
364
               # shuffle spikes into 1x1x#NueronsxT
365
               spikes = spikes.view(1, 1, -1, spikes.shape[-1]).float()
366
               spike_grid_img = make_grid(spikes, nrow=1, pad_value
367
      =0.5)
368
               self.writer.add_image(tag + "_" + str(k), spike_grid_img
369
      , step)
370
      def plot_voltages(
371
           self,
           voltage_record: Dict[str, torch.Tensor],
           thresholds: Optional[Dict[str, torch.Tensor]] = None,
374
           tag: str = "voltage",
375
           step: int = None,
376
      ) -> None:
377
           # language=rst
378
           0.0.0
379
           Plots all voltage records and given thresholds. Keeps unique
380
           plots for all unique tags that are given.
381
382
           :param voltage_record: Dictionary of voltages for neurons
383
      inside of networks
                                    organized by the layer they
384
      correspond to.
           :param thresholds: Optional dictionary of threshold values
385
      for neurons.
           :param tag: A unique tag to associate the data with.
386
           :param step: The step of the pipeline.
387
           0.0.0
388
           for k, v in voltage_record.items():
389
               # Shuffle voltages into 1x1x#neuronsxT
390
               v = v.view(1, 1, -1, v.shape[-1])
391
               voltage_grid_img = make_grid(v, nrow=1, pad_value=0)
392
393
               self.writer.add_image(tag + "_" + str(k),
394
      voltage_grid_img, step)
395
      def plot_conv2d_weights(
396
           self, weights: torch.Tensor, tag: str = "conv2d", step: int
```

397

| | = None |
|-----|--|
| 398 |) -> None: |
| 399 | # language=rst |
| 400 | N N N |
| 401 | Plot a connection weight matrix of a ''Conv2dConnection''. |
| 402 | |
| 403 | :param weights: Weight matrix of ''Conv2dConnection'' object |
| | |
| 404 | :param tag: A unique tag to associate the data with. |
| 405 | :param step: The step of the pipeline. |
| 406 | 0.0.0 |
| 407 | reshaped = reshape_conv2d_weights(weights).unsqueeze(0) |
| 408 | |
| 409 | reshaped -= reshaped.min() |
| 410 | reshaped /= reshaped.max() |
| 411 | |
| 412 | <pre>self.writer.add_image(tag, reshaped, step)</pre> |
| | |

Listing B.29: Pipeline analysis

```
1 import torch
2 import numpy as np
3 import matplotlib.pyplot as plt
5 from matplotlib.axes import Axes
6 from matplotlib.image import AxesImage
7 from torch.nn.modules.utils import _pair
8 from matplotlib.collections import PathCollection
9 from mpl_toolkits.axes_grid1 import make_axes_locatable
10 from typing import Tuple, List, Optional, Sized, Dict, Union
11
12 from ..utils import reshape_locally_connected_weights,
     reshape_conv2d_weights
13
14 plt.ion()
15
16
17 def plot_input(
     image: torch.Tensor,
18
     inpt: torch.Tensor,
19
      label: Optional[int] = None,
20
      axes: List[Axes] = None,
21
     ims: List[AxesImage] = None,
22
     figsize: Tuple[int, int] = (8, 4),
23
24 ) -> Tuple[List[Axes], List[AxesImage]]:
      # language=rst
25
      ......
26
     Plots a two-dimensional image and its corresponding spike-train
27
     representation.
28
     :param image: A 2D array of floats depicting an input image.
29
      :param inpt: A 2D array of floats depicting an image's spike-
30
     train encoding.
    :param label: Class label of the input data.
31
```

```
:param axes: Used for re-drawing the input plots.
32
      :param ims: Used for re-drawing the input plots.
      :param figsize: Horizontal, vertical figure size in inches.
34
      :return: Tuple of '(axes, ims)'' used for re-drawing the input
35
     plots.
      .....
36
      local_image = image.detach().clone().cpu().numpy()
37
      local_inpy = inpt.detach().clone().cpu().numpy()
38
39
      if axes is None:
40
          fig, axes = plt.subplots(1, 2, figsize=figsize)
41
          ims = (
42
               axes[0].imshow(local_image, cmap="binary"),
43
               axes[1].imshow(local_inpy, cmap="binary"),
44
          )
45
46
          if label is None:
47
               axes[0].set_title("Current image")
48
          else:
49
               axes[0].set_title("Current image (label = %d)" % label)
50
51
          axes[1].set_title("Reconstruction")
52
53
          for ax in axes:
54
               ax.set_xticks(())
55
               ax.set_yticks(())
56
57
          fig.tight_layout()
58
      else:
59
          if label is not None:
60
               axes[0].set_title("Current image (label = %d)" % label)
61
62
          ims[0].set_data(local_image)
63
          ims[1].set_data(local_inpy)
64
65
66
      return axes, ims
67
68
69 def plot_spikes(
      spikes: Dict[str, torch.Tensor],
70
      time: Optional[Tuple[int, int]] = None,
71
72
      n_neurons: Optional[Dict[str, Tuple[int, int]]] = None,
      ims: Optional[List[PathCollection]] = None,
73
      axes: Optional[Union[Axes, List[Axes]]] = None,
74
      figsize: Tuple[float, float] = (8.0, 4.5),
75
   -> Tuple[List[AxesImage], List[Axes]]:
76
 )
      # language=rst
77
      .....
78
      Plot spikes for any group(s) of neurons.
79
80
      :param spikes: Mapping from layer names to spiking data. Spike
81
     data has shape
          ''[time, n_1, ..., n_k]'', where ''[n_1, ..., n_k]'' is the
82
     shape of the
```

```
recorded layer.
83
       :param time: Plot spiking activity of neurons in the given time
84
      range. Default is
85
           entire simulation time.
       :param n_neurons: Plot spiking activity of neurons in the given
86
      range of neurons.
           Default is all neurons.
87
       :param ims: Used for re-drawing the plots.
88
       :param axes: Used for re-drawing the plots.
89
       :param figsize: Horizontal, vertical figure size in inches.
90
       :return: ''ims, axes'': Used for re-drawing the plots.
91
       .....
92
       n_subplots = len(spikes.keys())
93
       if n_neurons is None:
94
           n_neurons = {}
95
96
       spikes = {k: v.view(v.size(0), -1) for (k, v) in spikes.items()}
97
       if time is None:
98
           # Set it for entire duration
99
           for key in spikes.keys():
100
               time = (0, spikes[key].shape[0])
101
               break
102
103
       # Use all neurons if no argument provided.
104
       for key, val in spikes.items():
105
           if key not in n_neurons.keys():
106
               n_neurons[key] = (0, val.shape[1])
107
108
       if ims is None:
109
           fig, axes = plt.subplots(n_subplots, 1, figsize=figsize)
110
           if n_subplots == 1:
               axes = [axes]
           ims = []
114
           for i, datum in enumerate(spikes.items()):
116
               spikes = (
                    datum[1][
                        time[0] : time[1], n_neurons[datum[0]][0] :
118
      n_neurons[datum[0]][1]
                    ]
119
                    .detach()
120
                    .clone()
                    .cpu()
                    .numpy()
123
               )
124
               ims.append(
                    axes[i].scatter(
126
                        x=np.array(spikes.nonzero()).T[:, 0],
                        y=np.array(spikes.nonzero()).T[:, 1],
128
                        s=1,
129
                    )
130
               )
131
               args = (
```

datum[0],

```
n_neurons[datum[0]][0],
134
                     n_neurons[datum[0]][1],
135
                     time[0],
136
                     time[1],
137
                )
138
                axes[i].set_title(
139
                     "%s spikes for neurons (%d - %d) from t = %d to %d "
140
       % args
                )
141
            for ax in axes:
142
                ax.set_aspect("auto")
143
144
           plt.setp(
145
                axes, xticks=[], yticks=[], xlabel="Simulation time",
146
      ylabel="Neuron index"
           )
147
           plt.tight_layout()
148
       else:
149
           for i, datum in enumerate(spikes.items()):
150
                spikes = (
151
                     datum[1][
152
                          time[0] : time[1], n_neurons[datum[0]][0] :
153
      n_neurons[datum[0]][1]
                     ٦
154
                     .detach()
155
                     .clone()
156
                     .cpu()
157
                     .numpy()
158
                )
159
                ims[i].set_offsets(np.array(spikes.nonzero()).T)
160
                args = (
161
                     datum[0],
162
                     n_neurons[datum[0]][0],
163
                     n_neurons[datum[0]][1],
164
                     time[0],
165
                     time[1],
166
                )
167
                axes[i].set_title(
168
                     "%s spikes for neurons (%d - %d) from t = %d to %d "
169
       % args
                )
170
171
       plt.draw()
173
       return ims, axes
174
175
176
  def plot_weights(
       weights: torch.Tensor,
178
       wmin: Optional[float] = 0,
179
       wmax: Optional[float] = 1,
180
       im: Optional[AxesImage] = None,
181
       figsize: Tuple[int, int] = (5, 5),
182
       cmap: str = "hot_r",
183
```

```
184 ) -> AxesImage:
      # language=rst
185
       0.0.0
186
187
      Plot a connection weight matrix.
188
       :param weights: Weight matrix of "Connection" object.
189
       :param wmin: Minimum allowed weight value.
190
       :param wmax: Maximum allowed weight value.
191
       :param im: Used for re-drawing the weights plot.
192
      :param figsize: Horizontal, vertical figure size in inches.
193
      :param cmap: Matplotlib colormap.
194
       :return: "AxesImage" for re-drawing the weights plot.
195
       .....
196
      local_weights = weights.detach().clone().cpu().numpy()
197
      if not im:
198
           fig, ax = plt.subplots(figsize=figsize)
199
200
           im = ax.imshow(local_weights, cmap=cmap, vmin=wmin, vmax=
201
      wmax)
           div = make_axes_locatable(ax)
202
           cax = div.append_axes("right", size="5%", pad=0.05)
203
204
           ax.set_xticks(())
205
           ax.set_yticks(())
206
           ax.set_aspect("auto")
207
208
           plt.colorbar(im, cax=cax)
209
           fig.tight_layout()
210
       else:
211
           im.set_data(local_weights)
      return im
214
216
217 def plot_conv2d_weights(
218
      weights: torch.Tensor,
      wmin: float = 0.0,
219
      wmax: float = 1.0,
220
      im: Optional[AxesImage] = None,
      figsize: Tuple[int, int] = (5, 5),
222
      cmap: str = "hot_r",
224 ) -> AxesImage:
      # language=rst
       .....
226
      Plot a connection weight matrix of a Conv2dConnection.
228
       :param weights: Weight matrix of Conv2dConnection object.
229
       :param wmin: Minimum allowed weight value.
230
       :param wmax: Maximum allowed weight value.
231
       :param im: Used for re-drawing the weights plot.
       :param figsize: Horizontal, vertical figure size in inches.
      :param cmap: Matplotlib colormap.
234
       :return: Used for re-drawing the weights plot.
       ппп
236
```

```
sqrt1 = int(np.ceil(np.sqrt(weights.size(0))))
238
       sqrt2 = int(np.ceil(np.sqrt(weights.size(1))))
239
240
       height, width = weights.size(2), weights.size(3)
       reshaped = reshape_conv2d_weights(weights)
241
242
       if not im:
243
           fig, ax = plt.subplots(figsize=figsize)
244
           im = ax.imshow(reshaped, cmap=cmap, vmin=wmin, vmax=wmax)
245
           div = make_axes_locatable(ax)
246
           cax = div.append_axes("right", size="5%", pad=0.05)
247
248
           for i in range(height, sqrt1 * sqrt2 * height, height):
249
                ax.axhline(i - 0.5, color="g", linestyle="--")
250
               if i % sqrt1 == 0:
251
                    ax.axhline(i - 0.5, color="g", linestyle="-")
252
253
           for i in range(width, sqrt1 * sqrt2 * width, width):
254
               ax.axvline(i - 0.5, color="g", linestyle="--")
255
                if i % sqrt1 == 0:
256
                    ax.axvline(i - 0.5, color="g", linestyle="-")
257
258
           ax.set_xticks(())
259
           ax.set_yticks(())
260
           ax.set_aspect("auto")
261
262
           plt.colorbar(im, cax=cax)
263
           fig.tight_layout()
264
       else:
265
266
           im.set_data(reshaped)
267
       return im
268
269
270
  def plot_locally_connected_weights(
271
       weights: torch.Tensor,
       n_filters: int,
       kernel_size: Union[int, Tuple[int, int]],
274
       conv_size: Union[int, Tuple[int, int]],
275
       locations: torch.Tensor,
276
       input_sqrt: Union[int, Tuple[int, int]],
277
       wmin: float = 0.0,
278
       wmax: float = 1.0,
279
       im: Optional[AxesImage] = None,
280
       lines: bool = True,
281
       figsize: Tuple[int, int] = (5, 5),
282
       cmap: str = "hot_r",
283
    -> AxesImage:
284
  )
       # language=rst
285
       0.0.0
286
       Plot a connection weight matrix of a :code: 'Connection' with '
287
      locally connected
       structure <http://yann.lecun.com/exdb/publis/pdf/gregor-nips-11.</pre>
288
      pdf>_.
```

```
289
       :param weights: Weight matrix of Conv2dConnection object.
290
       :param n_filters: No. of convolution kernels in use.
291
292
       :param kernel_size: Side length(s) of 2D convolution kernels.
       :param conv_size: Side length(s) of 2D convolution population.
293
      :param locations: Indices of input receptive fields for
294
      convolution population
           neurons.
295
       :param input_sqrt: Side length(s) of 2D input data.
296
       :param wmin: Minimum allowed weight value.
297
       :param wmax: Maximum allowed weight value.
298
       :param im: Used for re-drawing the weights plot.
299
       :param lines: Whether or not to draw horizontal and vertical
300
      lines separating input
           regions.
301
       :param figsize: Horizontal, vertical figure size in inches.
302
       :param cmap: Matplotlib colormap.
303
       :return: Used for re-drawing the weights plot.
304
       .....
305
      kernel_size = _pair(kernel_size)
306
       conv_size = _pair(conv_size)
307
      input_sqrt = _pair(input_sqrt)
308
309
      reshaped = reshape_locally_connected_weights(
310
           weights, n_filters, kernel_size, conv_size, locations,
311
      input_sqrt
312
      )
      n_sqrt = int(np.ceil(np.sqrt(n_filters)))
313
314
      if not im:
315
           fig, ax = plt.subplots(figsize=figsize)
           im = ax.imshow(reshaped.cpu(), cmap=cmap, vmin=wmin, vmax=
318
      wmax)
           div = make_axes_locatable(ax)
319
           cax = div.append_axes("right", size="5%", pad=0.05)
320
321
           if lines:
               for i in range(
323
                   n_sqrt * kernel_size[0],
324
                   n_sqrt * conv_size[0] * kernel_size[0],
325
                   n_sqrt * kernel_size[0],
326
               ):
                   ax.axhline(i - 0.5, color="g", linestyle="--")
328
329
               for i in range(
330
                    n_sqrt * kernel_size[1],
331
                   n_sqrt * conv_size[1] * kernel_size[1],
                   n_sqrt * kernel_size[1],
               ):
334
                   ax.axvline(i - 0.5, color="g", linestyle="--")
336
           ax.set_xticks(())
           ax.set_yticks(())
338
```

```
ax.set_aspect("auto")
339
340
           plt.colorbar(im, cax=cax)
341
342
           fig.tight_layout()
       else:
343
           im.set_data(reshaped)
344
345
       return im
346
347
348
  def plot_assignments(
349
       assignments: torch.Tensor,
350
       im: Optional[AxesImage] = None,
351
       figsize: Tuple[int, int] = (5, 5),
352
       classes: Optional[Sized] = None,
353
    -> AxesImage:
354
  )
       # language=rst
355
       .....
356
       Plot the two-dimensional neuron assignments.
357
358
       :param assignments: Vector of neuron label assignments.
359
360
       :param im: Used for re-drawing the assignments plot.
       :param figsize: Horizontal, vertical figure size in inches.
361
       :param classes: Iterable of labels for colorbar ticks
362
      corresponding to data labels.
       :return: Used for re-drawing the assignments plot.
363
       .....
364
       locals_assignments = assignments.detach().clone().cpu().numpy()
365
       if not im:
366
           fig, ax = plt.subplots(figsize=figsize)
367
           ax.set_title("Categorical assignments")
368
369
           if classes is None:
               color = plt.get_cmap("RdBu", 11)
371
               im = ax.matshow(locals_assignments, cmap=color, vmin
372
      =-1.5, vmax=9.5)
           else:
373
               color = plt.get_cmap("RdBu", len(classes) + 1)
374
               im = ax.matshow(
375
                    locals_assignments, cmap=color, vmin=-1.5, vmax=len(
376
      classes) - 0.5
               )
377
378
           div = make_axes_locatable(ax)
379
           cax = div.append_axes("right", size="5%", pad=0.05)
380
381
           if classes is None:
382
                cbar = plt.colorbar(im, cax=cax, ticks=list(range(-1,
383
      11)))
                cbar.ax.set_yticklabels(["none"] + list(range(10)))
384
           else:
385
                cbar = plt.colorbar(im, cax=cax, ticks=np.arange(-1, len
386
      (classes)))
               cbar.ax.set_yticklabels(["none"] + list(classes))
387
```

```
388
           ax.set_xticks(())
389
           ax.set_yticks(())
390
391
           fig.tight_layout()
       else:
392
           im.set_data(locals_assignments)
393
394
       return im
395
396
397
  def plot_performance(
398
       performances: Dict[str, List[float]],
399
       ax: Optional[Axes] = None,
400
       figsize: Tuple[int, int] = (7, 4),
401
    -> Axes:
402
  )
       # language=rst
403
       0.0.0
404
       Plot training accuracy curves.
405
406
       :param performances: Lists of training accuracy estimates per
407
      voting scheme.
       :param ax: Used for re-drawing the performance plot.
408
       :param figsize: Horizontal, vertical figure size in inches.
409
       :return: Used for re-drawing the performance plot.
410
       ....
411
       if not ax:
412
           _, ax = plt.subplots(figsize=figsize)
413
       else:
414
           ax.clear()
415
416
       for scheme in performances:
417
           ax.plot(
418
                range(len(performances[scheme])),
419
                [p for p in performances[scheme]],
420
                label=scheme,
421
           )
422
423
       ax.set_ylim([0, 100])
424
       ax.set_title("Estimated classification accuracy")
425
       ax.set_xlabel("No. of examples")
426
       ax.set_ylabel("Accuracy")
427
       ax.set_xticks(())
428
       ax.set_yticks(range(0, 110, 10))
429
       ax.legend()
430
431
       return ax
432
433
434
  def plot_voltages(
435
       voltages: Dict[str, torch.Tensor],
436
       ims: Optional[List[AxesImage]] = None,
437
       axes: Optional[List[Axes]] = None,
438
       time: Tuple[int, int] = None,
439
       n_neurons: Optional[Dict[str, Tuple[int, int]]] = None,
440
```

```
cmap: Optional[str] = "jet",
441
       plot_type: str = "color",
442
       thresholds: Dict[str, torch.Tensor] = None,
443
444
       figsize: Tuple[float, float] = (8.0, 4.5),
    -> Tuple[List[AxesImage], List[Axes]]:
445
  )
       # language=rst
446
       .....
447
       Plot voltages for any group(s) of neurons.
448
449
       :param voltages: Contains voltage data by neuron layers.
450
       :param ims: Used for re-drawing the plots.
451
       :param axes: Used for re-drawing the plots.
452
       :param time: Plot voltages of neurons in given time range.
453
      Default is entire
           simulation time.
454
       :param n_neurons: Plot voltages of neurons in given range of
455
      neurons. Default is all
           neurons.
456
       :param cmap: Matplotlib colormap to use.
457
       :param figsize: Horizontal, vertical figure size in inches.
458
       :param plot_type: The way how to draw graph. 'color' for
459
      pcolormesh, 'line' for
           curved lines.
460
       :param thresholds: Thresholds of the neurons in each layer.
461
       :return: ''ims, axes'': Used for re-drawing the plots.
462
       .....
463
       n_subplots = len(voltages.keys())
464
465
       for key in voltages.keys():
466
           voltages[key] = voltages[key].view(-1, voltages[key].size
467
      (-1))
468
       if time is None:
469
           for key in voltages.keys():
470
                time = (0, voltages[key].size(-1))
471
472
                break
473
       if n_neurons is None:
474
           n_neurons = {}
475
476
       for key, val in voltages.items():
477
           if key not in n_neurons.keys():
478
               n_neurons[key] = (0, val.size(0))
479
480
       if not ims:
481
           fig, axes = plt.subplots(n_subplots, 1, figsize=figsize)
482
           ims = []
483
           if n_subplots == 1: # Plotting only one image
484
               for v in voltages.items():
485
                    if plot_type == "line":
486
                        ims.append(
487
                             axes.plot(
488
                                 v[1]
489
                                 .detach()
```

490

.clone() 491 .cpu() 492 .numpy()[493 n_neurons[v[0]][0] : n_neurons[v 494 [0]][1], time[0] : time[1], 495] 496) 497) 498 499 if thresholds is not None and thresholds[v[0]]. 500 size() == torch.Size([] 501): 502 503 ims.append(axes.axhline(504 y=thresholds[v[0]].item(), c="r", 505 linestyle="--") 506) 507 else: 508 ims.append(509 axes.pcolormesh(510 v[1] 511 .cpu() 512 .numpy()[513 n_neurons[v[0]][0] : n_neurons[v 514 [0]][1], time[0] : time[1], 515] 516 .Т, 517 cmap=cmap, 518) 519) 520 521 args = (v[0], n_neurons[v[0]][0], n_neurons[v 522 [0]][1], time[0], time[1]) plt.title("%s voltages for neurons (%d - %d) from t 523 = %d to %d " % args) plt.xlabel("Time (ms)") 524 525 if plot_type == "line": 526 plt.ylabel("Voltage") 527 else: 528 plt.ylabel("Neuron index") 529 530 axes.set_aspect("auto") 531 532 else: # Plot each layer at a time 533 for i, v in enumerate(voltages.items()): 534 if plot_type == "line": 535 ims.append(536 axes[i].plot(537 v[1] 538

.cpu() 539 .numpy()[540 n_neurons[v[0]][0] : n_neurons[v 541 [0]][1], time[0] : time[1], 542] 543) 544) 545 if thresholds is not None and thresholds[v[0]]. 546 size() == torch.Size([] 547): 548 ims.append(549 axes[i].axhline(550 y=thresholds[v[0]].item(), c="r", 551 linestyle="--") 552) 553 else: 554 ims.append(555 axes[i].matshow(556 v[1] 557 .cpu() 558 .numpy()[559 n_neurons[v[0]][0] : n_neurons[v 560 [0]][1], time[0] : time[1], 561] 562 .Т, 563 cmap=cmap, 564) 565) 566 args = (v[0], n_neurons[v[0]][0], n_neurons[v 567 [0]][1], time[0], time[1]) axes[i].set_title(568 "%s voltages for neurons (%d - %d) from t = %d 569 to %d " % args) 570 571 for ax in axes: 572 ax.set_aspect("auto") 573 574 if plot_type == "color": 575 plt.setp(axes, xlabel="Simulation time", ylabel="Neuron 576 index") elif plot_type == "line": 577 plt.setp(axes, xlabel="Simulation time", ylabel="Voltage 578 ") 579 plt.tight_layout() 580 581 else: 582 # Plotting figure given 583 if n_subplots == 1: # Plotting only one image 584

for v in voltages.items(): 585 axes.clear() 586 if plot_type == "line": 587 588 axes.plot(v[1] 589 .cpu() 590 .numpy()[591 n_neurons[v[0]][0] : n_neurons[v[0]][1], 592 time[0] : time[1]] 593) 594 if thresholds is not None and thresholds[v[0]]. 595 size() == torch.Size([] 596): 597 axes.axhline(y=thresholds[v[0]].item(), c="r 598 ", linestyle="--") else: 599 axes.matshow(600 v[1] 601 .cpu() 602 .numpy()[603 n_neurons[v[0]][0] : n_neurons[v[0]][1], 604 time[0] : time[1]] 605 .Т, 606 cmap=cmap, 607) 608 args = (v[0], n_neurons[v[0]][0], n_neurons[v 609 [0]][1], time[0], time[1]) axes.set_title(610 "%s voltages for neurons (%d - %d) from t = %d 611 to %d " % args 612) axes.set_aspect("auto") 613 614 else: 615 # Plot each layer at a time 616 for i, v in enumerate(voltages.items()): 617 axes[i].clear() 618 if plot_type == "line": 619 axes[i].plot(620 v[1] 621 .cpu() 622 .numpy()[623 n_neurons[v[0]][0] : n_neurons[v[0]][1], 624 time[0] : time[1]] 625) 626 if thresholds is not None and thresholds [v[0]]. 627 size() == torch.Size([] 628): 629 axes[i].axhline(630

y=thresholds[v[0]].item(), c="r", 631 linestyle="--") 632 633 else: axes[i].matshow(634 v[1] 635 .cpu() 636 .numpy()[637 n_neurons[v[0]][0] : n_neurons[v[0]][1], 638 time[0] : time[1]] 639 .Т, 640 cmap=cmap , 641) 642 args = (v[0], n_neurons[v[0]][0], n_neurons[v 643 [0]][1], time[0], time[1]) axes[i].set_title(644 "%s voltages for neurons (%d - %d) from t = %d 645 to %d " % args) 646 647 for ax in axes: 648 ax.set_aspect("auto") 649 650 if plot_type == "color": 651 plt.setp(axes, xlabel="Simulation time", ylabel="Neuron 652 index") elif plot_type == "line": 653 plt.setp(axes, xlabel="Simulation time", ylabel="Voltage 654 ") 655 plt.tight_layout() 656 657 return ims, axes 658

Listing B.30: Plotting

1 import torch 2 import numpy as np 3 import matplotlib.pyplot as plt 4 import matplotlib.animation as animation 5 6 from typing import List, Tuple, Optional 9 def plot_weights_movie(ws: np.ndarray, sample_every: int = 1) -> None: # language=rst 10 11 Create and plot movie of weights. 12 13 :param ws: Array of shape ''[n_examples, source, target, time 14] ' ' . :param sample_every: Sub-sample using this parameter. 15

```
16
      weights = []
17
18
      # Obtain samples from the weights for every example.
19
      for i in range(ws.shape[0]):
20
          sub_sampled_weight = ws[i, :, :, range(0, ws[i].shape[2],
     sample_every)]
          weights.append(sub_sampled_weight)
23
      else:
24
          weights = np.concatenate(weights, axis=0)
25
      # Initialize plot.
26
      fig = plt.figure()
27
      im = plt.imshow(weights[0, :, :], cmap="hot_r", animated=True,
28
     vmin=0, vmax=1)
      plt.axis("off")
29
      plt.colorbar(im)
30
31
      # Update function for the animation.
32
      def update(j):
          im.set_data(weights[j, :, :])
34
          return [im]
35
36
      # Initialize animation.
37
      global ani
38
      ani = 0
39
      ani = animation.FuncAnimation(
40
          fig, update, frames=weights.shape[-1], interval=1000, blit=
41
     True
      )
42
      plt.show()
43
44
45
46 def plot_spike_trains_for_example(
      spikes: torch.Tensor,
47
      n_ex: Optional[int] = None,
48
      top_k: Optional[int] = None,
49
      indices: Optional[List[int]] = None,
50
   -> None:
 )
51
      # language=rst
52
      0.0.0
53
54
      Plot spike trains for top-k neurons or for specific indices.
55
      :param spikes: Spikes for one simulation run of shape
56
          ('(n_examples, n_neurons, time)''.
57
      :param n_ex: Allows user to pick which example to plot spikes
58
     for.
      :param top_k: Plot k neurons that spiked the most for n_ex
59
     example.
      :param indices: Plot specific neurons' spiking activity instead
60
     of top_k.
      .....
61
      assert n_ex is not None and 0 <= n_ex < spikes.shape[0]
62
63
```

0.0.0

```
plt.figure()
64
65
      if top_k is None and indices is None: # Plot all neurons'
66
      spiking activity
           spike_per_neuron = [np.argwhere(i == 1).flatten() for i in
67
      spikes[n_ex, :, :]]
           plt.title("Spiking activity for all %d neurons" % spikes.
68
      shape[1])
69
      elif top_k is None: # Plot based on indices parameter
70
           assert indices is not None
71
           spike_per_neuron = [
72
               np.argwhere(i == 1).flatten() for i in spikes[n_ex,
73
      indices, :]
          ٦
74
75
      elif indices is None: # Plot based on top_k parameter
76
           assert top_k is not None
77
           # Obtain the top k neurons that fired the most
78
           top_k_loc = np.argsort(np.sum(spikes[n_ex, :, :], axis=1),
79
      axis=0) [::-1]
           spike_per_neuron = [
80
               np.argwhere(i == 1).flatten() for i in spikes[n_ex,
81
      top_k_loc[0:top_k], :]
          ]
82
           plt.title("Spiking activity for top %d neurons" % top_k)
83
84
      else:
85
           raise ValueError('One of "top_k" or "indices" or both must
86
      be None')
87
      plt.eventplot(spike_per_neuron, linelengths=[0.5] * len(
88
      spike_per_neuron))
      plt.xlabel("Simulation Time")
89
      plt.ylabel("Neuron index")
90
91
      plt.show()
92
93
94 def plot_voltage(
      voltage: torch.Tensor,
95
      n_ex: int = 0,
96
      n_neuron: int = 0,
97
      time: Optional[Tuple[int, int]] = None,
98
      threshold: float = None,
99
    -> None:
100)
      # language=rst
101
      .....
102
      Plot voltage for a single neuron on a specific example.
103
104
      :param voltage: Tensor or array of shape ''[n_examples,
105
      n_neurons, time]''.
      :param n_ex: Allows user to pick which example to plot voltage
106
      for.
      :param n_neuron: Neuron index for which to plot voltages for.
107
```

```
:param time: Plot spiking activity of neurons between the given
108
      range of time.
      :param threshold: Neuron spiking threshold.
109
       0.0.0
110
      assert n_ex \ge 0 and n_euron \ge 0
111
      assert n_ex < voltage.shape[0] and n_neuron < voltage.shape[1]
112
      if time is None:
114
           time = (0, voltage.shape[-1])
115
      else:
116
           assert time[0] < time[1]
117
           assert time[1] <= voltage.shape[-1]</pre>
118
119
      timer = np.arange(time[0], time[1])
120
      time_ticks = np.arange(time[0], time[1] + 1, 10)
121
122
      plt.figure()
      plt.plot(voltage[n_ex, n_neuron, timer])
124
      plt.xlabel("Simulation Time")
125
      plt.ylabel("Voltage")
126
      plt.title("Membrane voltage of neuron %d for example %d" % (
127
      n_neuron, n_ex + 1)
      locs, labels = plt.xticks()
128
      locs = range(int(locs[1]), int(locs[-1]), 10)
129
      plt.xticks(locs, time_ticks)
130
131
      # Draw threshold line only if given
132
      if threshold is not None:
133
           plt.axhline(threshold, linestyle="--", color="black", zorder
134
      =0)
135
      plt.show()
136
```

Listing B.31: Visualization