

Fault Analysis of Injection Substation Using Symmetrical Component Method A Case Study of Mofor Injection Substation, Delta State, Nigeria.

Oladimeji J. Ayamolowo^{a,*}, Oladipo Folorunso^a, Elutunji Buraimoh^a

^aDepartment of Electrical Electronics & Computer Engineering, Afe Babalola University Ado-Ekiti, Nigeria.

Corresponding Author: Oladimeji J. Ayamolowo

ABSTRACT: This study centers on the fault analysis of 15MVA Mofor Injection Substation, which is an Injection Substation located in Warri, Delta state, Nigeria which gets its source from PTI transmission station. Mofor Injection substation has two outgoing feeders which are Orhuwhorun feeder and Eketete feeder. The analysis was carried out and deductions were made considering the various faults which occurred during the period of assessment and their associated fault current was calculated using symmetrical Component method of Fault analysis. A model of the distribution network was made using Electrical Transient Analyzer Program (ETAP); the value of real and reactive powers and voltage magnitudes in the whole network were observed. The data obtained from the injection substation indicates that Orhuwhorun feeder has a higher frequency of fault and from results obtained from Symmetrical method of fault analysis revealed that double Line to ground fault has the highest fault current and could cause adverse damages to equipments' and as such must be avoided. The fault current calculated from Symmetrical component method of Fault analysis was validated with computer program MATLAB as results agreed closely since error was below 0.1%. This paper analyzes several faults from an injection substation. The distribution network was modelled in ETAP, observing values for active and reactive power and voltage magnitudes

Keywords: Mofor Injection Substation, Fault analysis, Fault current.

Date of Submission: 27-09-2017

Date of acceptance: 10-10-2017

I. INTRODUCTION

One of the major problems industries in Nigeria face is to counter the sudden voltage fluctuations in the system which results in the deterioration of power quality and damages to equipment [1]. The consequences of power incidents show that industrial and digital firms are losing revenue per year due to power interruptions. The cost to replace equipment damaged because of voltage spikes is very high as these results to reduction in production. Electricity supply is also very important as it affects all sphere of life both social and economic development of any nation. Power supply to consumer must be reliable, adequate and of acceptable quality at a minimum cost, but this is not easily achievable as the reliability of supply and adequacy is being truncated by incessant faults along the line, which reduces the efficiency of the system.

The Manufacturers Association of Nigeria (MAN) and the National Association of Small Scale Industries (NASSI) estimated that their members spend an average of about N2billion (about \$12 million) per week on self-power generation [2].

A series of power sector polls conducted by NOI Polls Ltd for the second quarter of 2013 revealed that about 130 million, representing 81 per cent, out of the 160 million Nigerians generated their own electricity through alternative sources to make up for irregular power supply. Study also showed a combined average of 69 percent or 110 million of Nigerians experienced greater spending on alternative electricity supply [3].

Nigeria's electricity consumption on a per capita basis was among the lowest in the world when compared with the average per capita electricity usage in Libya which is 4,270KWH; India, 616KWH; China, 2,944KWH; South Africa, 4,803 KWH; Singapore, 8,307KWH; and the United States, 13,394KWH [1-3]. By Journal of Sustainable Development Studies, South Africa with a population of just 50 million, has an installed electricity generation capacity of over 52,000 MW [4].

The Electrical system is sub divided into generation, transmission and distribution sections. The subsystem that generates electrical energy is called generation subsystem or generating plants (stations). It

consists of generating units (consisting of turbine alternator Sets) including the necessary accessories. Speed governors for the prime Movers (turbines; exciters and voltage regulators for generators, and step-up transformers also form part of the generating plants. The subsystem that transmits the electrical energy over long distances (from generating Plants to main load centers) is called transmission subsystem. It consists of transmission Lines, regulating transformers and static/rotating VAR units (which are used to control Active/reactive powers)

The sub system that distributes energy from load centers to individual consumer points along with end energy converting devices such as motors, resistances etc is called Distribution Subsystems. It consists of feeders, step-down transformers, and individual Consumer connections along with the terminal energy converting electrical equipment Such as motors, resistors etc.

The electricity distribution network starts at the Injection substation, where power is delivered by overhead transmission lines and stepped down by Power transformer (15MVA) from 33KV to 11KV. But sadly, at each of these stages of power system, a vital obstacle called **FAULT** is encountered. A Fault in an electrical equipment is a defect in the electrical circuit due to which current is diverted from the intended path [5]. This fault is subdivided into **Transient and permanent faults**

Transient faults are faults, which do not damage the insulation permanently and allow the circuit to be safely re-energized after a short period, such as sudden loss of generation or an interconnecting line, or the sudden connection of additional load. The duration of the transient period is in the order of a second. System behavior in this interval is crucial in the design of power systems. Transient overvoltage occurring in our power system can cause operational breakdown and also cause failure in industrial and household equipment. These types of problems have been given serious consideration by engineers since most of the equipment that are used in the substation have a specific Basic Insulation Level (BIL) and if the overvoltage exceeds the safety or defined limit, insulation breaks down and failure of equipment occur. For that reason, several protective devices and schemes are applied to reduce the effect of transient overvoltage to control damage caused to the utility system and to avoid poor power quality.

Transient over voltages in power systems may be caused due to several reasons of which those occurring due to lightning strikes or switching operations of inductive or capacitive are the commonest [6].

Permanent faults result in permanent damage to the insulation. In this case, the equipment has to be repaired.

II. METHODOLOGY

The step by step methods involves the analysis are:

1. Data collection from the Injection Substation
2. Simulation of the Mofor injection Substation using ETAP
3. Calculation of Fault Current and Line Impedance using symmetrical method for fault analysis
4. Validation of Fault current using Matlab
5. Determination of the bus voltage, Real and reactive power from the load flow analysis.

2.1 Data Collected for 33KV Current Transformer

Product of C. T=ABB

C.T Ratio=400:1

RHSV 36KV

Type =outdoor

Frequency =50 Hz

Burden =50VA core

Core 1=400/1A=10P10

Core 2=10P10 400-1A

Core 3=10P10 400-1A

2.2 CT Ratio on the Secondary Side of 15MVA Transformer

Product Of C.T=ABB

C.T ratio=400:5

Calculation of Load Current

The 15MVA transformer is connected in Delta/Star.

$$\text{Primary Load Current} = \frac{15 * 10^6}{\sqrt{3} * 33 * 10^3} = 262.4A \dots (1)$$

C.T Ratio for the H.V side of the Transformer 400:1A

$$\text{Secondary load Current} = \frac{15 * 10^6}{\sqrt{3} * 11 * 10^3} = 787.3A \dots (2)$$

Name plate reading=780A

Secondary Full load current in Primary C.T

$$= \frac{262.4 * 1}{400} = 0.656A \dots\dots\dots(3)$$

Secondary full load in secondary

$$C.T = \frac{787.3 * 5}{400} = 9.841A \dots\dots\dots(4)$$

On the low voltage side of the main transformer winding are connected in star, so

$$\text{Phase voltage} = \frac{11}{\sqrt{3}} = 6.351kV \dots\dots\dots(5)$$

On the high voltage side of the transformer, the Main transformer windings are connected in Delta, so

Phase voltage = line voltage = 33kV

$$\text{Turn ratio of main Transformer} = \frac{33}{6.351} = 5turns \dots(6)$$

$$\text{Current transformer on 11kV side are connected in delta and the turn ratio} = \frac{400}{5} = 80 \dots\dots\dots(7)$$

$$\text{Apparent Power} = V_{rms} I_{rms} = I^2_{rms} Z = \frac{V_{rms}^2}{Z}$$

$$\text{Reactive Power} = V_{rms} I_{rms} = I_{rms}^2 X = \frac{V_{rms}^2}{X} \dots(8)$$

$$\text{Active Power} = \sqrt{3} VI \cos \phi \dots(9)$$

Instantaneous power is defined as:

$$P_{inst}(t) = V(t) * I(t) \dots\dots\dots(10)$$

Where V(t) and I(t) are the time varying voltage and current waveforms.

Table 1. Loading Distributions on Eketete Feeder

Substation	Apparent Power (kVA)	Reactive Power (kVAR)	Real Power kW	Rated capacity (kVA)	Power factor	Frequency (Hz)	ROUTE LENGTH (km)
Maternity substation	443	266.6	353.8	500	0.798	50	0.7
Catholic Substation	429	258.2	342.6	500	0.794	50	0.8
Express Junction Substation	431	259.4	344.2	500	0.793	50	0.9
Cross and stop substation	408	245.5	325.8	500		50	1.1
Old Eketete Road Substation	421.8	253.8	336.9	500	0.794	50	1.4

Table 2. Loading Distributions on Orhuwhorun Feeder

Substation	Power (kVA)	Power (kVAR)	Power (kW)	Power factor	Frequency (Hz)	Route length (km)	Rated capacity (kVA)
1 st orhuwhorun Road sub station	453	272.6	361.8	0.795	50	0.6	500
Oboh street substation	433	260.6	345.8	0.792	50	0.8	500
Udu market Substation	451	271.4	360.2	0.793	50	1.1	500
kotokoto substation	431	259.4	344.2	0.794	50	1.4	500
Newyork Substation	421.7	253.8	336.8	0.797	50	1.5	500

2.3 Calculation of Line Parameters for Mofor Injection Substation

For short transmission line: For short length, the shunt capacitance of this type of line is neglected and other parameters like Electrical resistance and inductor of these short lines are lumped [7], hence the vector diagram is given

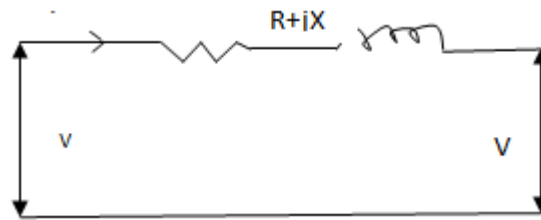


Fig.1 Representing a short transmission Line

RESISTANCE = $R = PL/A$ Where P is the resistivity of the conductor material

F=50Hz

$$Z = \sqrt{R^2 + (\omega L)^2} \quad (11)$$

Table 3. Shows the Impedance of the various node in the Injection Substation

Node	Resistivity (Ω/km)	Inductance(mH)	Length(km)	Area (mm ²)	R(Ω)	Reactance (Ω)	Z(Ω)	Y(S)
Node 3	0.00001	11.26	20	100	2	3.5	4.03	0.25
Node 5	0.00004	4.78	0.5	70	0.3	1.5	1.5	0.67
Node 8	0.00004	4.78	0.7	70	0.4	1.5	1.5	0.67
Node 11	0.00003	4.78	0.8	70	0.3	1.5	1.5	0.67
Node 12	0.00002	4.78	1.1	70	0.3	1.5	1.5	0.67
Node 13	0.00002	6.37	1.4	70	0.4	2	2	0.5
Node 19	0.00002	6.37	0.6	70	0.2	2	2	0.5
Node 20	0.00004	6.37	0.8	70	0.45	2	2	0.5
Node 21	0.00004	3.18	1.1	70	0.6	1	1	1
Node 22	0.00002	3.18	1.4	70	0.4	1	1	1
Node 23	0.00001	3.18	1.5	70	0.2	1	1	1

Table 4: Fault analysis of Mofor Injection substation feeders for 2015 [4].

Fault	SLG	LL	DLG	3-phase fault	Miscellaneous	Total	Monthly Total
January 2015							
Ekete feeder	14 times	10 times	2 times	Nil	Nil	26 times	44 Times
Orhuwhorun feeder	9 times	7 times	1 time	1 time	1time	18times	
FEBRUARY2015							
Ekete feeder	13 times	5 times	4 times	Nil	Nil	22 times	49 times
Orhuwhorun feeder	12 times	10 times	5 times	Nil	Nil	27 times	
MARCH 2015							
Ekete feeder	15 times	10 times	3 times	Nil	Nil	28 times	48 times
Orhuwhorun feeder	9 times	8 times	5 times	Nil	1time	23times	
APRIL 2015							
Ekete feeder	13 times	7 times	5 times	1time	Nil	26 times	44 times
Orhuwhorun Feeder	7 times	6 times	4 times	1time	Nil	18times	
MAY 2015							
Ekete feeder	9 times	7 times	6 times	Nil	Nil	22 times	41 times
Orhuwhorun feeder	8 times	6 times	5 times	Nil	Nil	19 times	
JUNE 2015							
Ekete feeder	11 times	9 times	2 times	Nil	Nil	22 times	48 times
Orhuwhorun feeder	10 times	7 times	3 times	Nil	Nil	23 times	
JULY 2015							
Ekete feeder	17 times	11 times	4 times	Nil	Nil	32 times	57 times
Orhuwhorun feeder	11 times	9 times	5 times	Nil	Nil	25 times	
AUGUST 2015							
Ekete feeder	10 times	8 times	5 times	Nil	Nil	23 times	44 times
Orhuwhorun feeder	10 times	7 times	4 times	Nil	Nil	21times	
SEPTEMBER 2015							
Ekete feeder	16 times	8 times	7 times	2times	1time	34 times	61 times
Orhuwhorun feeder	15 times	6 times	5 times	1time	Nil	27 times	
OCTOBER 2015							
Ekete feeder	13 times	7 times	7 times	Nil	Nil	27times	50 times

Orhuwhorun feeder	14 times	6 times	3 times	Nil	Nil	23 times	
NOVEMBER 2015							
Ekete feeder	17 times	11 times	3 times	Nil	Nil	31 times	63 times
Orhuwhorun feeder	19 times	5 times	7 times	Nil	1time	32 times	
DECEMBER 2015							
Ekete feeder	14 times	6 times	4 times	1 time	Nil	25	50 times
Orhuwhorun feeder	13 times	5 times	5 times	Nil	2 times	25	
Total	299	181	104	7 times	6times	597	
Total fault on Ekete feeder	296						
Total fault on Orhuwhorun feeder	301						

2.4 Analysis of Typical Single Line to Ground

Fault on the 11kV Line with Fault at Phase A. Fault currents throughbus M are independent offault distances and fault resistances [6-7].

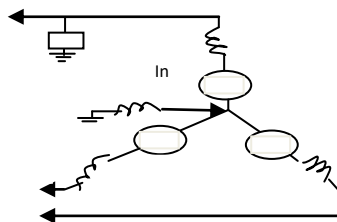


Fig.2 Representation of the Line to Ground Fault

$$\text{Base Current} = \frac{15 * 10^6}{\sqrt{3} * 11 * 10^3} = 787.3A \quad (12)$$

$$\text{Base Impedance} = \frac{(11 * 10^3)^2}{15 * 10^6} = 8.07\Omega \quad (13)$$

Line to Line Voltage= 11kV

$$\text{Base Voltage} = \frac{11kV}{\sqrt{3}}$$

The fault occurred between terminal “a” and ground.

Fault impedance $Z_f = 0$

The induced voltage of phase “a” be 1 per unit which is the reference phasor.

$$E_a = 1.0\angle 0^\circ pu$$

Neglecting the resistance since the reactance is much larger we have,

$$Z_1 = 2j, \quad Z_2 = 1.5j, \quad Z_0 = 1j, \quad Z_f = 0$$

Converting to per unit

$$Z_1 = \frac{2j}{8.07} = 0.25j \quad (14)$$

$$Z_2 = \frac{1.5j}{8.07} = 0.2j \quad (15)$$

$$I_{a0} = I_{a1} = I_{a2} = \frac{E_a}{Z_1 + Z_2 + Z_0 + 3Z_f} \quad (16)$$

$$= \frac{1.0\angle 0^\circ}{0.25j + 0.2j + 0.125j} \quad (17)$$

$$= \frac{1.0\angle 0^\circ}{0.575j} = -j1.739 pu$$

Fault Current, I_f

$$I_f = I_a = 3I_{a1} = -3 * j1.739 p.u = -j5.217 p.u \quad (18)$$

$$= 5.217 * 787.3 = 4107.3A$$

where , $I_b = 0$ and $I_c = 0$

Symmetrical components of voltages from terminals "a" to ground

$$V_{a1} = E_a - I_{a1}Z_1 \quad (19)$$

$$= (1 + j0) - (-j1.739) * j0.25 = 0.5653 p.u$$

$$V_{a0} = -I_{a0}Z_0 = -(-j1.739) * j0.125 = -0.2174 p.u$$

Line to ground Voltages,

$$V_a = V_{a1} + V_{a2} + V_{a0} \quad (20)$$

$$= 0.5653 - 0.3478 - 0.2174 = 0$$

$$V_b = a^2V_{a1} + aV_{a2} + V_{a0} \quad (21)$$

Where , $a = 0.5 + j0.8660$

$$= 0.5653(-0.5 - j0.866) -$$

$$0.3478(-0.5 + j0.866) - 0.2174$$

$$= -0.3262 - j0.7907 p.u$$

$$V_c = aV_{a1} + a^2V_{a2} + V_{a0} \quad (22)$$

Where $a = -0.5 + j0.866$

$$= 0.5653(-0.5 + j0.866) -$$

$$0.3478(-0.5 - j0.866) - 0.2174$$

$$= -0.3262 + j0.7907 p.u$$

Line to line voltages at fault points

$$V_{ab} = V_a - V_b = 0 - (-0.3262 - j0.7907)$$

$$= 0.3262 + j0.7907$$

$$= \frac{11}{\sqrt{3}} * 0.8553 \angle 67.6^\circ kV = 5.43 \angle 67.6^\circ kV$$

$$= V_{bc} = V_b - V_c = (-0.3262 - j0.7907) -$$

$$(-0.3262 + j0.7907) = -j1.5814$$

$$= 1.5814 \angle 270^\circ p.u$$

$$= \frac{11}{\sqrt{3}} * 1.5814 \angle 270^\circ kV = 10.04 \angle 270^\circ$$

$$V_{ca} = V_c - V_a = (-0.3262 + j0.7907) - 0$$

$$= -0.3262 + j0.7907$$

$$= 0.8553 \angle 112.4^\circ p.u = \frac{11}{\sqrt{3}} * 0.8553 \angle 112.4^\circ$$

$$= 5.43 \angle 112.4^\circ kV$$

It can be seen that when a fault occurs the post fault voltages and current are different from pre-fault voltage and current. While the voltage on the affected phase is reduced the current rises tremendously. Fault current = 4107.3A,

The secondary current in CTs on LV side will be

$$\frac{4107.3 * 5}{400} = 51.35A$$

The current in the pilot wires = $51.35 * \sqrt{3} = 88.93A$ since the CT on LV side is delta connected.

2.5 Line to Line Fault Analysis

Considering a line to line that occurred between phase b and c.

$$\text{Base Current} = \frac{15 * 10^6}{\sqrt{3} * 11 * 10^3} = 787.3A$$

$$\text{Base Impedance} = \frac{(11 * 10^3)^2}{15 * 10^6} = 8.07\Omega$$

Base Voltage= 11kV

The fault occurred between terminal "b" and c.

Fault impedance $Z_f = j0.01$

$Z_1 = j0.2$, $Z_2 = j0.2$, $Z_0 = j0.125$

The induced voltage of phase "a" line to neutral voltage be 1 per unit.

$$\text{So, } Ea = (1 + j0)p.u \quad (23)$$

$$Vb - Vc = I_b Z_f; I_a = -I_c$$

$$I_{a1} = \frac{Ea}{Z_1 + Z_2 + Z_f} = \frac{1 + j0}{(j0.20 + j0.2 + j0.01)}$$

$$= -j2.44 p.u$$

$$I_{a2} = -I_{a1} = j2.44 p.u$$

$$I_{a0} = 0$$

$$I_a = I_{a1} + I_{a2} + I_{a0} = -j2.44 + j2.44 + 0 = 0$$

$$I_b = a^2 I_{a1} + a I_{a2} + I_{a0} \quad (24)$$

$$= -j2.44(-0.5 - j0.866) + j2.44(-0.5 + j0.866) + 0$$

$$= -4.23 p.u$$

$$I_c = a I_{a1} + a^2 I_{a2} + I_{a0} \quad (25)$$

$$= -j2.44(-0.5 + j0.866) + j2.44(-0.5 - j0.866) + 0$$

$$= 4.23 p.u$$

Therefore $I_a = 0$

$$I_b = -4.23 * 787.3 = -3330.3A$$

$$I_c = 4.23 * 787.3 = 3330.3A$$

Symmetrical component of the voltages from terminal a to ground

$$Va_1 = Ea - I_{a1} Z_1 = (1.0 + j0) - (-j2.44) * j0.20 = 0.512 p.u$$

$$Va_2 = -I_{a2} Z_2 = -j2.44 * j0.20 = 0.488 p.u$$

$V_{a0} = 0$ since the transformer is grounded

Line to ground Voltages,

$$Va = Va_1 + Va_2 + Va_0 = 0.512 + 0.488 = 1 p.u$$

$$Vb = a^2 Va_1 + a Va_2 + Va_0 \quad (26)$$

$$= 0.512(-0.5 - j0.866) + 0.488(-0.5 + j0.866) + 0$$

$$= -0.5 - j0.021 p.u$$

$$Vc = a Va_1 + a^2 Va_2 + Va_0$$

$$= 0.512(-0.5 + j0.866) + 0.488(-0.5 - j0.866) + 0$$

$$= -0.5 + j0.021 p.u$$

$$Vb - Vc = I_b Z_f = -4.23 * j0.01 = -j0.0423$$

$$(27)$$

Line to line Voltages,

$$= \frac{11}{\sqrt{3}} * 1.5 \angle 0.8^\circ = 9.53 \angle 0.8^\circ kV$$

$$V_{bc} = V_b - V_c$$

$$= -0.5 - j0.021 - (-0.5 + j0.021) = -j0.042 p.u$$

$$= 0.042 \angle 90^\circ p.u$$

$$V_{ca} = V_c - V_a = -0.5 + j0.021 - 1$$

$$= \frac{11}{\sqrt{3}} * 0.042 \angle 90^\circ = 266.7 \angle 90^\circ V = -1.5 + j0.021 = 1.5 \angle 0.8^\circ p.u \quad (28)$$

$$= \frac{11}{\sqrt{3}} * 1.5 \angle 0.8^\circ = 9.53 \angle 0.8^\circ kV$$

It can be seen that when a fault occurs the post fault voltages and current are different from pre-fault voltage and current, while the voltage on the affected phase is reduced the current rises tremendously. For fault current = 3330.3A,

The secondary current in CTs on LV side will be $3330.3 * 5 / 400 = 41.6A$

The current in the pilot wires = $51.35 * \sqrt{3} = 72A$ since the CT on LV side is delta connected.

$$\text{Base Current} = \frac{15 * 10^6}{\sqrt{3} * 11 * 10^3} = 787.3A$$

$$\text{Base Impedance} = \frac{(11 * 10^3)^2}{15 * 10^6} = 8.07 \Omega$$

$$\text{Base Voltage} = 11kV$$

The fault occurred between terminal "b,c" and ground with Fault Impedance $Z_f = 0$

$$Z_1 = 0.25 p.u, Z_2 = j0.20 p.u, Z_0 = j0.125 p.u$$

The induced voltage of phase "a" line to neutral voltage is 1 per unit.

$$\text{So, } E_a = (1 + j0) p.u$$

$$I_{a1} = \frac{E_a}{Z_1 + \frac{Z_2 Z_0}{Z_2 + Z_0}} = \frac{1 + j0}{j0.25 + \frac{j0.20 + j0.125}{j0.20 + j0.125}}$$

$$= -j3.06 p.u \quad (29)$$

$$V_{a1} = V_{a2} = V_{a0}$$

$$V_{a1} = E_a - I_{a1} Z_1$$

$$V_{a0} = V_{a2} = V_{a1} = E_a - I_{a1} Z_1$$

$$= (1 + j0) - (-j3.06) * j0.25 = 0.235 p.u$$

$$I_{a2} = \frac{-V_{a2}}{Z_2} = \frac{-0.235}{j0.2} = j1.175 p.u$$

$$V_{ab} = V_a - V_b = 1 - (-0.5 - j0.021)$$

$$= 1.5 + j0.021 = 1.5 \angle 0.8^\circ p.u$$

2.6 Double Line to Ground Fault Analysis

Considering a double line to ground fault which occurred between terminal b and c to ground.

$$I_{a_0} = \frac{V_{a_0}}{Z_0} = \frac{-0.235}{j0.125} = j1.88 p.u \quad (30)$$

$$I_{a_0} + I_{a_1} + I_{a_2} = j1.88 - j3.06 + j1.175 = 0$$

$$\begin{aligned} I_b &= a^2 I_{a_1} + a I_{a_2} + I_{a_0} = \\ &- j3.06(-0.5 - j0.866) + \\ &j1.175(-0.5 + j0.866) + j1.88 \\ &= -3.67 + j2.82 p.u = 4.63 \angle 142.4^\circ p.u \\ &= 3645.2 A \angle 142.4^\circ \end{aligned} \quad (31)$$

$$\begin{aligned} I_c &= a I_{a_1} + a^2 I_{a_2} + I_{a_0} \\ &= -j3.06(-0.5 + j0.866) + \\ &j1.175(-0.5 - j0.866) + j1.88 = 3.67 + j2.82 p.u \\ &= 4.63 \angle 37.6^\circ p.u = 3645.2 A \angle 37.6^\circ \end{aligned} \quad (32)$$

$$\begin{aligned} \text{Fault current, } I_f \\ &= I_f = I_b + I_c = j5.64 p.u = 5.64 \angle 90^\circ p.u \\ &= 4440.4 \angle 90^\circ A \end{aligned}$$

$$V_{a_0} = V_{a_1} = V_{a_2} = 0.235 p.u, Z_f = 0 \quad (33)$$

$$V_b = V_c = 0$$

$$V_a = V_{a_0} + V_{a_1} + V_{a_2} = 3 * 0.235 = 0.705 p.u$$

Line to line voltages in p.u

$$V_{ab} = V_a - V_b = 0.705 \angle 0^\circ p.u$$

$$V_{bc} = V_b - V_c = 0 \quad (34)$$

$$V_{ca} = V_c - V_a = 0.705 \angle 180^\circ p.u$$

Line to line voltage in kV,

$$V_{ab} = 0.705 \angle 0^\circ * \frac{11}{\sqrt{3}} kV = 4.48 \angle 0^\circ kV \quad (35)$$

$$V_{bc} = 0$$

$$V_{ca} = 0.705 \angle 0^\circ * \frac{11}{\sqrt{3}} kV = 4.48 \angle 180^\circ kV \quad (36)$$

It can be seen that when a fault occurs the post fault voltages and current are different from pre-fault voltage and current, while the voltage on the affected phase is reduced the current rises tremendously.

For fault current = 4440.4A,

The secondary current in CTs on LV side will be

$$= 4440.4 * \frac{5}{400} = 55.5 A \quad (37)$$

The current in the pilot wires = 55.5 * √3 = 96.1A since the CT on LV side is delta connected

2.7 Fault Analysis for a 3 Phase Fault on the 11kv Line

$$I_{a_1} = \frac{E_a}{Z_1} \quad (38)$$

$$\text{Line current} = \frac{1.0^\circ}{j0.25} = 4 \angle -90^\circ \text{ p.u} \quad (39)$$

Actual value of the line current =
 $4 * 787.3 \angle -90^\circ$
 $= 3149.2 \angle -90^\circ$

Therefore, fault current = 3149.2A
 The secondary current in CTs on LV side will be

$$3149.2 * \frac{5}{400} = 39.4 \text{ A}$$

The current in the pilot wires = $68.2 * \sqrt{3} = 68.2 \text{ A}$ since the CT on LV side is delta connected.

2.8 Modeling of the Power Network Load flow studies are used to ensure that electrical power transfer from generators to consumers through the grid system is stable, reliable and economic [8].

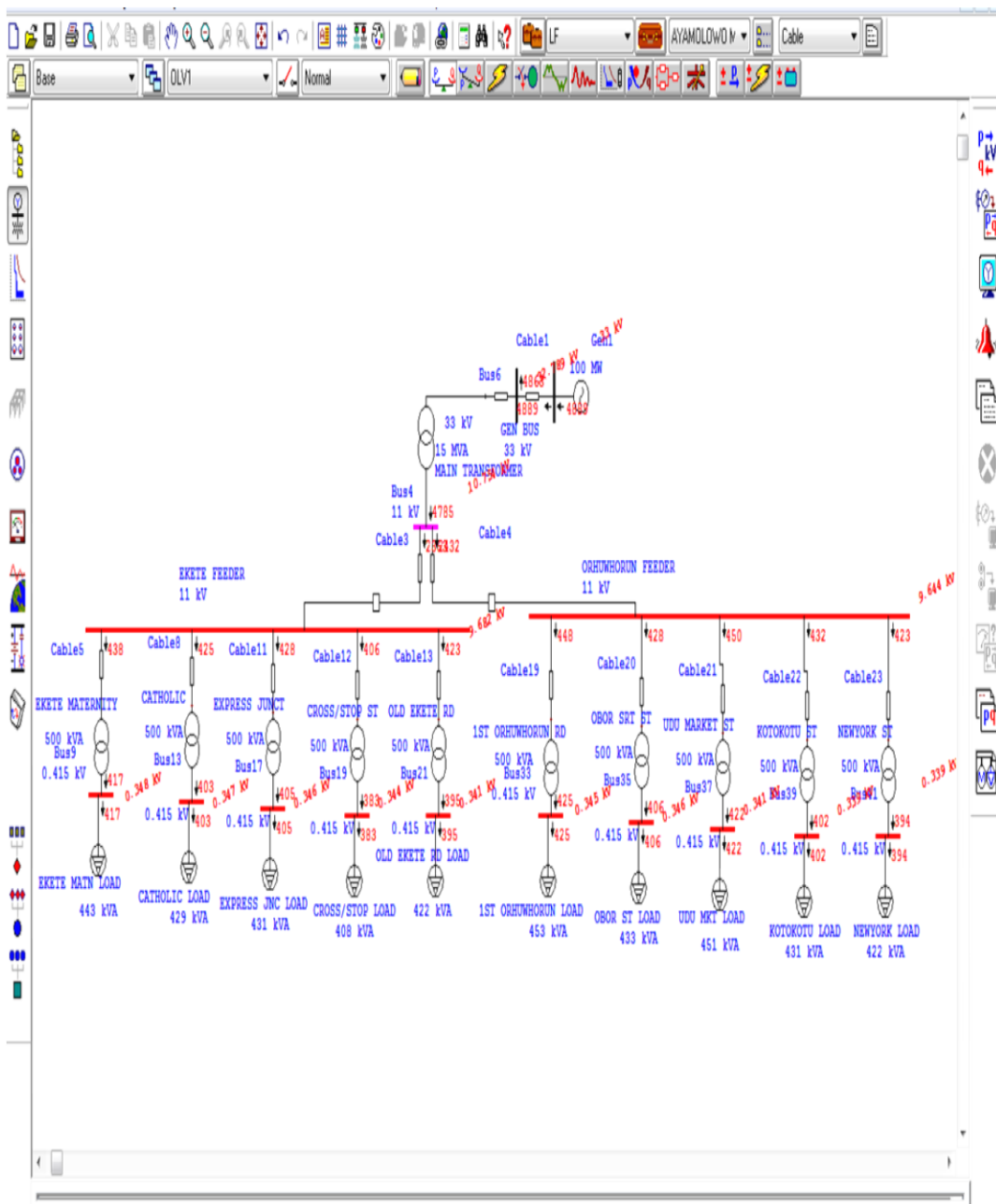


Fig 3: Simulated Power Network using ETAP 7.0

Table 5. Shows the Summary of fault analysis of various faults in Mofor Injection Substation with 11KV as base voltage and Base power MVA 15MVA.

Faults	Fault current(A)	Voltage Magnitude(kV) of line voltage Vab	Voltage Magnitude(kV) of line voltage Vbc	Voltage Magnitude(kV) of line voltage Vca
Single line to Ground	4107.3	5.43	10.04	5.43
Line to Line fault with fault at phase b,c	3330.3	9.53	0.227	9.53
Double Line to ground With fault at phase b,c to ground	4440.4	4.48	0	4.48
3 Phase fault	3149.2	0	0	0

III. RESULTS AND DISCUSSION

Simulated and calculated results obtained from 15MVA Mofor Injection Sub-station are analyzed. The study was carried out considering various faults in the Substation.

3.1 Input Data for Simulation of the Various Faults Using Matlab.

Table 6. Shows the input parameter for simulation using Matlab

FAULTS	$R_0(\Omega)$	$X_0(\Omega)$	$Z_0(P.U)$	$R_1(\Omega)$	$X_1(\Omega)$	$Z_1(P.U)$	$R_2(\Omega)$	$X_2(H)$	$Z_2(P.U)$	$Z_3(P.U)$
SLG	0	1	j0.125	0	2	j0.25	0	1.5	j0.2	0
LL	0	1	j0.125	0	1.5	j0.2	0	1.5	j0.2	0.01
DLG	0	1	J0.125	0	2	J0.25	0	1.5	J0.2	0
3PHASE	0	1	j0.125	0	2	j0.25	0	1.5	j0.2	0
BASE VOLTAGE=11/√3 KV										
BASE POWER (KVA)=15MVA										
BASE IMPEDANCE=8.07Ω										

Table 7: Comparing the Calculate and the Simulated results.

Fault	Line Voltage	Hand Calculations	Matlab
Single Line to Ground at	Vab (KV)	5.43	5.40
	Vbc (KV)	10.04	10.01
	Vca (KV)	5.43	5.40
	Fault Current(A)	4107.3	4107.1
Line to Line fault with fault at	Vab (KV)	9.53	9.49
	Vbc (KV)	0.227	0.225
	Vca (KV)	9.53	9.49
	Fault Current(A)	3330.3	3330.1
Double Line to ground With fault at phase b,c to	Vab (KV)	4.48	4.45
	Vbc (KV)	0	0
	Vca (KV)	4.48	4.45
	Fault Current(A)	4440.4	4440.1
3 Phase faults	Vab (KV)	0	0
	Vbc (KV)	0	0
	Vca (KV)	0	0
	Fault Current(A)	3149.2	3149.0

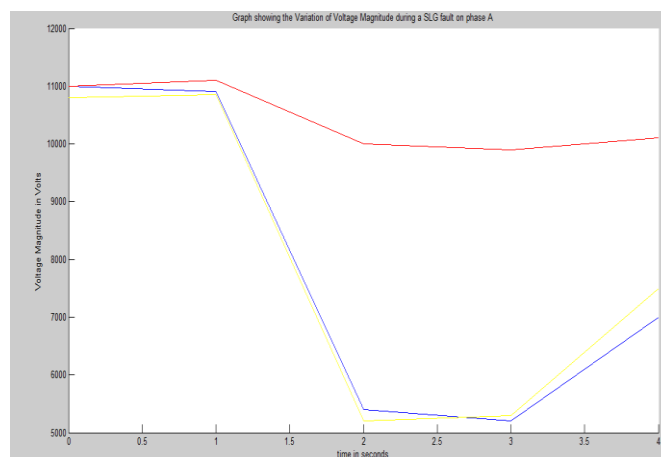


Figure 4: Graphical illustration of line to line voltage variation during a Single Line to Ground Fault using Matlab

The figure above shows the sharp decline in the Line to line voltage of Vab and Vca during a single line to ground fault at Phase A, while line voltage Vbc remains simply un affected.

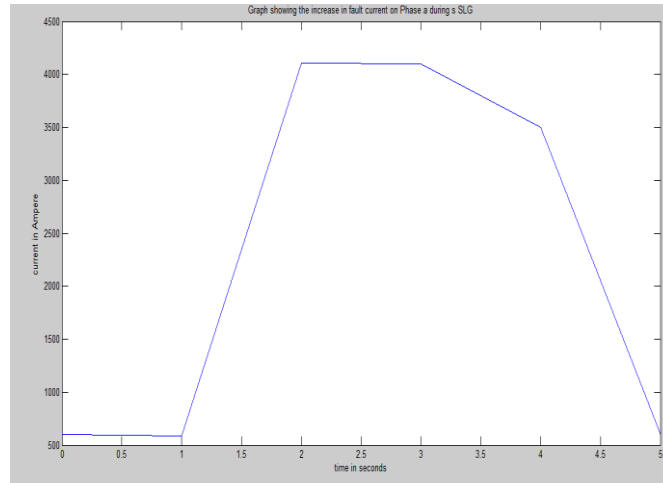


Figure 5: Graphical illustration of sharp increase in current during a Single Line to Ground Fault using Matlab. The figure above shows the increase in fault current due to the single line to ground fault at Phase A, this fault current is the second highest Fault current in power system and could cause severe damages if no proper protective device is in place.

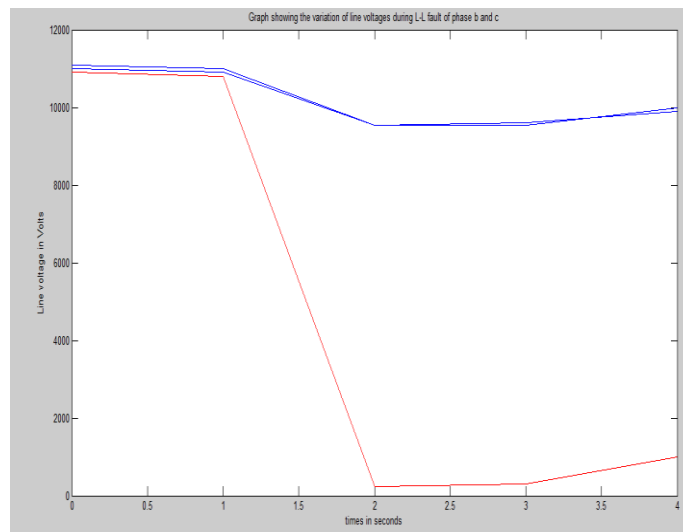


Figure 6: Graphical illustration of sharp decrease in phase voltage Vbc during a Line to Line fault between phase b and c using Matlab.

The figure above shows the decrease in line voltage Vbc due to the Line line fault between phase b and c, while line Vab and Vca have fairly steady voltages.

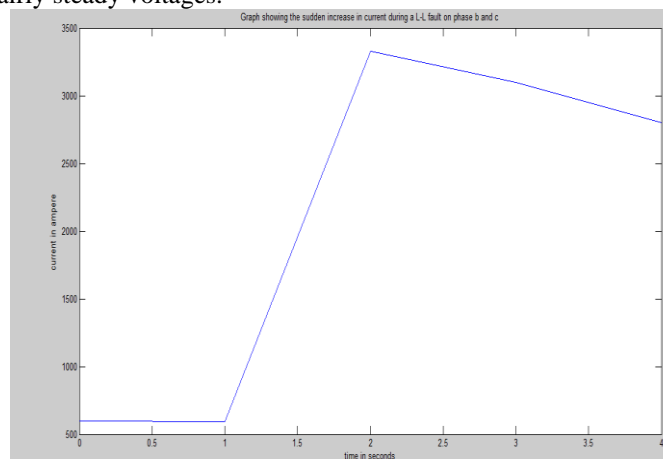


Figure 7: Graphical illustration of sharp increase in current during a Line to Line Fault using Matlab.

The figure above shows the increase in fault current due to the line to line fault at Phase b and c, the fault current could cause severe damages if no proper protective device in place.

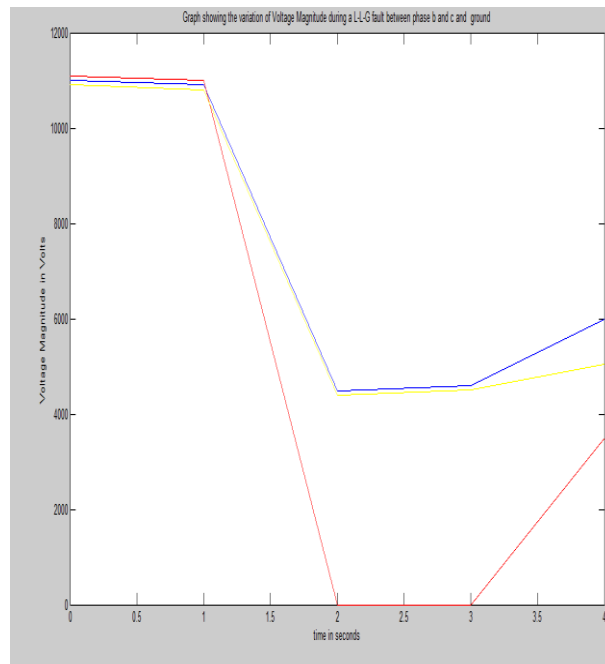


Figure 8: Graphical illustration of Voltage Magnitude variation during a DLG Fault between phase b and c using Matlab

The figure above shows the sharp decline in the Line to line voltage as Vbc drops to zero while Vab, Vca suffered a decline in voltage during the period of the fault.

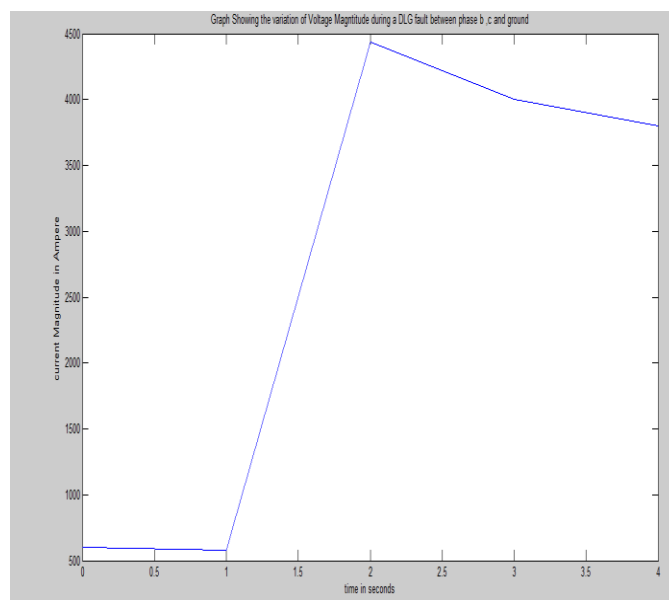


Figure 9: Graphical illustration of sharp increase in fault current during a Double Line to Ground Fault using Matlab

The figure above shows the increase in fault current due to the Double line to ground fault between phase b,c and ground, the fault current in the type of fault is the largest in power system and must be avoided. It was observed that this type of fault most times in Mofor Injection Substation causes the 33KV line to open.

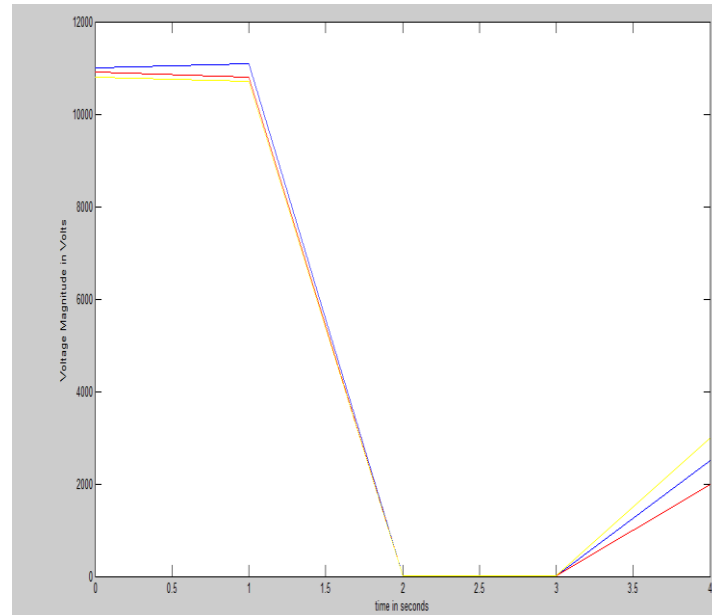


Figure 10: Graphical illustration of Voltage Magnitude variation during a 3 phase Fault between phase a, b and c using Matlab

The figure above shows the sharp decline in the Line to line voltage as V_{bc} , V_{ca} , V_{ab} all dropped to zero. The type of fault has the least possibility of occurrence in power system.

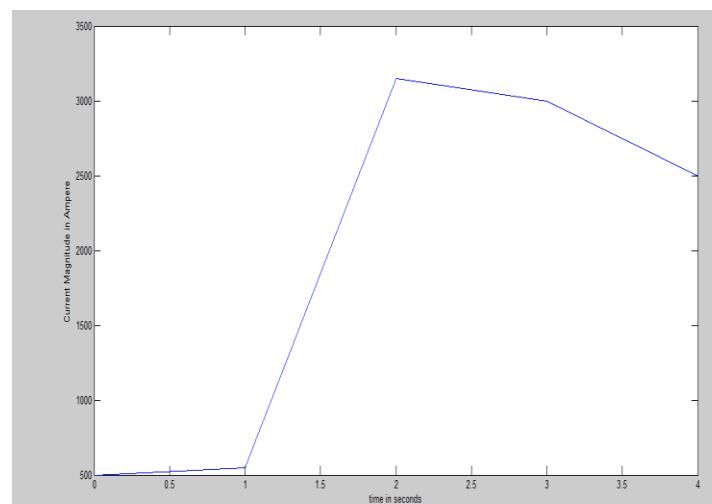


Figure 11: Graphical illustration of sharp increase in current during 3 phase using Matlab

The figure above shows the increase in fault current due to the short circuit involving all three phase. This fault current can cause severe damages in power system.

IV. CONCLUSION

In this paper, fault analysis was carried out on Mofor Injection Substation. The analysis was carried manually using symmetrical components method. The results were compared with software solutions obtained from 'MATLAB' to validate the hand calculations' accuracy. The error was between the acceptable limit of 0.1% for all type of fault. The following observations have been made based on the results obtained from the analysis.

1. In three-phase faults, the voltages at faulted bus phases dropped to zero during the fault. In the faulted bus, Phase, A, B and C has a zero-voltage potential.
2. In the single line-to-ground fault; however, only voltage at Phase A is equal to zero in. In addition, only Phase A has fault current since it is the faulted phase. The fault current in this is the second highest fault currents of in the system in consideration.
3. In line-to-line fault Phase B and Phase C, are in contact, the voltages at both phases are equal. The fault current passes from B to C. In Phase A, the current is equal to zero compared to the fault current.

4. In double line-to-ground fault, Phase B and C voltages are equal to zero. The faulted current is flowing through both phases only. In addition, this type of fault is the most severe fault on the system which can be seen from its current value has it has the highest value of fault current.

The analysis was carried out on Mofor Injection Sub-station a 15MVA network reveals that electrical power transfer from the Substation to consumers through the grid system is unstable, unreliable it was also observed that the Substation was been under-utilized as it is operating less than its rated capacity.

REFERENCES

- [1]. Zhang, L.D., Bollen, M.H.J. (1998) A method for characterizing unbalanced voltage dips (sags) with symmetrical components. IEEE Power Eng.
- [2]. B.L Theraja., A..K.,Theraja`A Textboobook of Electrical Technology', ,S.Chand Ltd 24th Edition 2008..
- [3]. Iseolorunkanmi, K.O.(2014) Journal of sustainable Development Studies,
- [4]. PHCN Plc Mofor Injection Substation, 2015, Control room data for the injection substations
- [5]. Asaduzzaman Nur, M. H. S., Muhit, M. S., and Md Khaled Hossain, M. D. (2014). Fault AnalysisElectrical Protection of Distribution Transformers. *Global Journal of Research In Engineering*, 14(3).
- [6]. Wanying Q. (2006) Simulation Study of Single Line-to-Ground Faults on Rural Teed Distribution Lines
- [7]. Fuchs, E.F.,(2011), M.A.S.: Power quality in power systems and electrical machines ISBN 978- 0-12-369536, Masoum.
- [8]. Gupta J.B (2008) Power systems, Kataria & sons ISO 9

Oladimeji J. Ayamolowo. "Fault Analysis of Injection Substation Using Symmetrical Component Method A Case Study of Mofor Injection Substation, Delta State, Nigeria." American Journal of Engineering Research (AJER), vol. 16, no. 10, 2017, pp. 83–97.