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So close, so different: characterization of the K2-36 planetary system with HARPS-N

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ABSTRACT

Context. K2-36 is a K dwarf orbited by two small ($R_b = 1.43 \pm 0.08 R_\oplus$ and $R_c = 3.2 \pm 0.3 R_\oplus$), close-in ($a_b=0.022$ AU and $a_c=0.054$ AU) transiting planets discovered by the Kepler/K2 space observatory. They are representatives of two distinct families of small planets ($R_p < 4 R_\oplus$) recently emerged from the analysis of Kepler data, with likely a different structure, composition and evolutionary pathways.

Aims. We revise the fundamental stellar parameters and the sizes of the planets, and provide the first measurement of their masses and bulk densities, which we use to infer their structure and composition.

Methods. We observed K2-36 with the HARPS-N spectrograph over ~ 3.5 years, collecting 81 useful radial velocity measurements. The star is active, with evidence for increasing levels of magnetic activity during the observing time span. The radial velocity scatter is ~ 17 ms^{-1} due to the stellar activity contribution, which is much larger than the semi-amplitudes of the planetary signals. We tested different methods for mitigating the stellar activity contribution to the radial velocity time variations and measuring the planet masses with good precision.

Results. We found that K2-36 is likely a ~ 1 Gyr old system, and by treating the stellar activity through a Gaussian process regression, we measured the planet masses $m_b=3.9 \pm 1.1 M_\oplus$ and $m_c=7.8 \pm 2.3 M_\oplus$. The derived planet bulk densities $\rho_b=7.2^{+2.5}_{-2.1}$ g cm^{-3} and $\rho_c=1.3^{+0.7}_{-0.5}$ g cm^{-3} point out that K2-36 b has a rocky, Earth-like composition, and K2-36 c is a low-density sub-Neptune.

Conclusions. Composed of two planets with similar orbital separations but different densities, K2-36 represents an optimal laboratory for testing the role of the atmospheric escape in driving the evolution of close-in, low-mass planets after ~ 1 Gyr from their formation. Due to their similarities, we performed a preliminary comparative analysis between the systems K2-36 and Kepler-36, which we deem worthy of a more detailed investigation.

Key words. Stars: individual: K2-36 (TYC 266-622-1, EPIC 201713348) - Planets and satellites: detection - Planets and satellites: composition - Techniques: radial velocities

1. Introduction

Launched in 2009, the Kepler space observatory has discovered thousands of transiting extrasolar planets, and unveiled the huge diversity that characterizes the exoplanetary systems. Such large numbers of new worlds has enabled statistical studies to shed light on the different observed architectures, forming an impor-

tant repository of data on the formation and evolutionary history of the planetary systems.

One striking feature that has emerged from observations is that the distribution of the radii of small ($R_p < 4 R_\oplus$), close-in planets is bi-modal (Owen & Wu 2013, and the following studies by Fulton et al. 2017; Zeng et al. 2017; Zeng et al. 2017b).

By refining the stellar and the planet radii using parallaxes from *Gaia*, Fulton & Petigura (2018) have better characterized these two quite distinct populations, identified as super-Earths and sub-Neptunes. They have determined that the centres of the two groups lie at $1.2\text{--}1.3 R_{\oplus}$ and $\sim 2.4 R_{\oplus}$, respectively, and were able to locate the radius gap that separates the two families as lying between $\sim 1.8\text{--}2 R_{\oplus}$ (as also confirmed by Berger et al. 2018). The bi-modality in the size distribution is likely indicative of existing differences in the bulk compositions of the two classes of planets, which in turn could also be related to the formation history and the mass loss mechanisms in action during the system evolution, such as photo evaporation (e.g. Lopez & Fortney 2013; Owen & Wu 2017; Van Eylen et al. 2018).

There is ambiguity in the compositions of the sub-Neptune family, since they may be either gas dwarfs, with a rocky core surrounded by an H_2/He gaseous envelope, or water-worlds mainly composed of H_2O -dominated ices or/and fluids, or a combination of an ice mantle and an H_2/He gaseous envelope. According to Zeng et al. (2018, submitted) many of the $2\text{--}4 R_{\oplus}$ planets could actually be water-worlds. Nonetheless, the key information that is still missing for the bulk of the small planets are their masses, which would allow for a determination of their average densities, necessary to constrain their compositions and internal structures. Therefore, the characterization of these small exoplanets through the measurement of their masses is fundamental to understanding the origins and diversity of planets in the Milky Way Galaxy.

Within this framework, we present a characterization study of the K2-36 planetary system (Sinukoff et al. 2016) based on radial velocities (RVs) extracted from spectra collected with the HARPS-N spectrograph. This system is of special interest in that the star K2-36 hosts two small, close-in transiting planets discovered by K2 that are exemplar members of the two planet families identified in the Kepler sample ($R_b = 1.43 \pm 0.08 R_{\oplus}$ and $R_c = 3.2 \pm 0.3 R_{\oplus}$). K2-36 offers the exciting opportunity to measure the mass of planets below and above the radius gap that belong to the same system, testing the hypothesis that the gap represents the transition between rocky planets and lower density bodies with enough volatiles to measurably change their bulk composition. K2-36 is a magnetically active star with an RV scatter of $\sim 17 \text{ m s}^{-1}$, which is much larger than the expected semi-amplitude of the planetary signals on the basis of the observed planet radii. Thus, it represents a very challenging case study concerning the characterization of small-size, low-mass planets, even with transit ephemeris known to high precision.

The paper is organized as follows. In Section 2 we describe the photometric and spectroscopic datasets used in this work. In Section 3 we provide a new determination of the fundamental stellar parameters for K2-36, making use of *Gaia* data, and in Section 4 we present refined planetary parameters from a reanalysis of the K2 light curve. We discuss in Section 5.2 the results of the stellar activity analysis, and present in Section 6 the measurements from RV data of the mass and bulk density of the two K2-36 planets. In Section 7 we discuss the implications of our results concerning the composition and bulk structure of the K2-36 planets. The main conclusions are outlined in Section 8.

2. Dataset

2.1. K2 photometry

K2-36 was observed by the K2 mission during Campaign 1 in 2014 (May 30-Aug 21). In our work we used the 30 minute

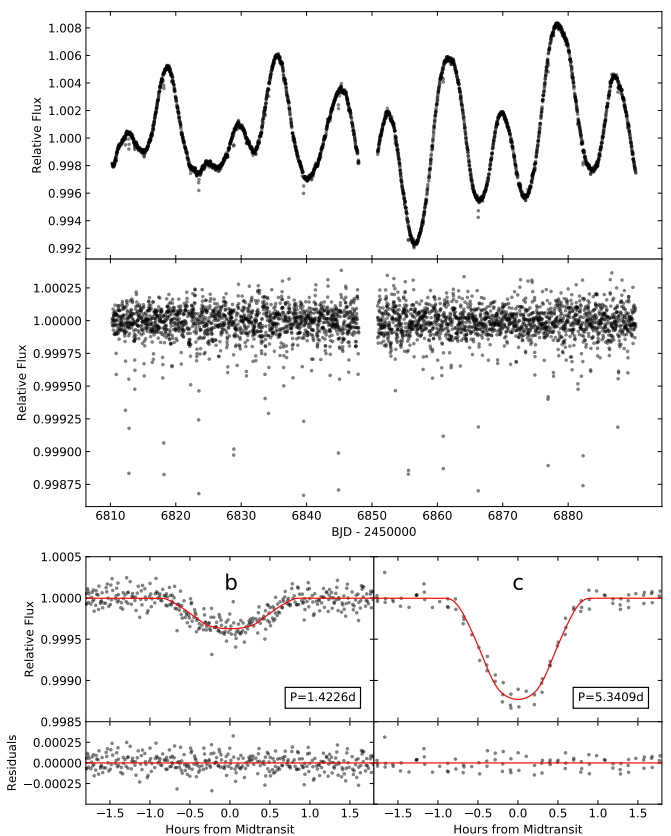


Fig. 1. *Upper panel:* K2-36 light curve observed by K2, showing the modulation induced by the stellar rotation. *Middle plot:* K2-36 flattened light curve, with the rotation modulation filtered-out. The observed dimming events correspond to the transits of the two planets. *Bottom panel:* transit light curves for K2-36b and K2-36c folded at their best-fit orbital periods (Table 2). The curves in red are our best-fit transit models, and the residuals are also shown.

cadence K2SFF¹ light curve processed as described by Vanderburg & Johnson (2014) and Vanderburg et al. (2016), and refined by simultaneously fitting for spacecraft systematics, stellar variability, and the planetary transits. The light curve is shown in the upper panel of Fig. 1. A gap is visible between epochs BJD 2456 848 and 2456 850.9, during which the observations were interrupted in order to downlink the data. During that time Kepler changed orientation, which also changed the heating due to the Sun and introduced an offset in the photometry. The middle panel in Fig. 1 shows the flattened light curve corrected for the modulation due to the stellar rotation, and it is that we used to model the planetary transit signals.

2.2. HARPS-N spectroscopy

We observed K2-36 over three seasons, between the end of January 2015 and the end of May 2018, with the high-resolution and stabilised spectrograph HARPS-N (Cosentino et al. 2014) at the Telescopio Nazionale Galileo (TNG) on the island of La Palma. A total of 83 echelle spectra have been secured on fiber A, all with an exposure time of 1800 seconds. Their average signal-to-noise ratio S/N per pixel is 34, as measured at wavelength $\lambda \sim 550 \text{ nm}$. Two of them have $S/N < 15$ (taken at epochs BJD 2457 810.586681 and 2457 890.464286), and they have been

¹<https://archive.stsci.edu/prepds/k2sff/>

discarded from further analysis due to their low quality. Fiber B was used to collect sky spectra. The spectra were reduced with version 3.7 of the HARPS-N Data Reduction Software (DRS).

We performed an analysis to identify the RV measurements potentially contaminated by moonlight. This check is particularly necessary for a target such as K2-36, which lies close to the ecliptic plane. The procedure adopted for this analysis is the same as the one described in Section 2.1 of Malavolta et al. (2017a). We have found one potentially contaminated spectrum at epoch BJD 2 457 054.632798, but since our analysis is not conclusive we have decided to include it in the final dataset, which thus consists of 81 spectra.

3. Stellar parameters

Adaptive optics imaging did not detect stellar companions near K2-36 (Sinukoff et al. 2016), and there is no evidence in the cross-correlation function (CCF) of the HARPS-N spectra for more than one component. We derived new values for the fundamental stellar parameters from the analysis of HARPS-N spectra and using data from the *Gaia* DR2 catalogue. The atmospheric parameters were first determined separately using three different algorithms.

Equivalent widths. In the classical curve-of-growth approach, we derive temperature T_{eff} and microturbulent velocity ξ_t by minimizing the trend of iron abundances (obtained from the equivalent width of each line) with respect to excitation potential and reduced equivalent width, respectively. The surface gravity $\log g$ is obtained by imposing the same average abundance from neutral and ionized iron lines. We used ARESv2² (Sousa et al. 2015) to measure the equivalent widths, and used MOOG³ (Snedden 1973) jointly with the ATLAS9 grid of stellar model atmospheres from Castelli & Kurucz (2004) to perform line analysis and spectrum synthesis, under the assumption of local thermodynamic equilibrium (LTE). We followed the prescription of Andreasen et al. (2017) and applied the gravity correction from Mortier et al. (2014). The analysis was performed on the resulting co-addition of individual spectra. We get $T_{\text{eff}} = 4800 \pm 59$ K, $\log g = 4.73 \pm 0.15$ (cgs), and $[\text{Fe}/\text{H}] = -0.15 \pm 0.03$ dex.

Atmospheric Stellar Parameters from Cross-Correlation Functions (CCFpams). This technique is described in Malavolta et al. (2017b), and the code is publicly available⁴. We get $T_{\text{eff}} = 4841 \pm 37$ K, $\log g = 4.60 \pm 0.10$ (cgs), and $[\text{Fe}/\text{H}] = -0.19 \pm 0.04$ dex. We report here the internal errors, which are likely underestimated.

Stellar Parameter Classification (SPC). The SPC technique (Buchhave et al. 2012, 2014) was applied to 55 spectra with high S/N, and the weighted average of the individual spectroscopic analyses yielded stellar parameters of $T_{\text{eff}} = 4862 \pm 50$ K, $\log g = 4.57 \pm 0.10$ (cgs), and $[\text{m}/\text{H}] = -0.05 \pm 0.08$ dex. For the projected rotational velocity we can reliably impose only the upper limit $v \sin i_{\star} < 2$ km s⁻¹.

3.1. The age of K2-36

Inferring the age of this planetary system is relevant for investigating its origin and evolution, but it is a difficult issue for a K dwarf when using only stellar evolution isochrones. Based on the rotational modulation observed in the K2 light curve (Sect.

5.1) and on a rotation-age relationship (Scott Engle, private communication), the age of K2-36 is found to be 1.5 ± 0.4 Gyr, which agrees with our measured average level of chromospheric activity ($\log R'_{\text{HK}} = -4.50$ dex).

Using the relation of Mamajek & Hillenbrand (2008) based on gyrochronology (eqs. [12]-[14]), and adopting $P_{\text{rot}} = 16.9 \pm 0.2$ as the rotation period of K2-36 (Sect. 5.1), we derive an age of 1.09 ± 0.13 Gyr, although the color index of K2-36 ($B - V = 0.96$, corrected for the extinction $E(B - V) = 0.03$ using the 3D Pan-STARRS 1 dust map of Green et al. 2018) is slightly out the range of validity for that calibration ($0.5 < B - V < 0.9$). This result is in agreement with the previous estimate.

We also carried out Galactic population assignment using the classification scheme by Bensby et al. (2003, 2005), the K2-36's systemic radial velocity from HARPS-N spectra, and *Gaia* DR2 proper motion and parallax. We obtain a thick disk-to-thin disk probability ratio *thick/thin* = 0.1, implying that K2-36 is significantly identified as a thin-disk object, presumably not very old.

Finally, we searched for evidence of the lithium absorption line at 6707.8 Å (Fig. 2). We compared the co-added spectrum with four models, each differing only in the assumed Li abundance. The lithium line is not detectable within the noise of the continuum, and we set an upper limit of $A(\text{Li}) < 0.0$. The lithium depletion in K2-36 is comparable to, or lower than, that observed for stars of the same temperature and spectral type in 600-800 Myr-old open clusters with similar metallicity (e.g., Soderblom et al. 1995; Sestito & Randich 2005; Somers & Pinsonneault 2014; Brandt & Huang 2015). We thus set an approximate lower limit for the age of K2-36 at $t = 0.6$ Gyr.

3.2. Age-constrained final set of stellar parameters

We used our estimated age of K2-36 to derive a final set of fundamental stellar parameters, including the stellar mass and radius. To this purpose we have constrained the stellar age to be in the range of 600 Myr to 2 Gyr. The parameters were obtained with the package *isochrone* (Morton 2015), following the prescriptions of Malavolta et al. (2018). The photospheric parameters of the star obtained with the three different techniques outlined earlier in this Section were used as priors together with the photometric magnitudes V, K, WISE1 and WISE2, and the parallax from *Gaia*, within a Bayesian framework. The stellar evolution models Dartmouth (Dotter et al. 2008) and MIST (Dotter 2016; Choi et al. 2016; Paxton et al. 2011) were used, thus a total of six different sets of posteriors for the fitted parameters have been derived. The final results are listed in Table 1 and represent the 50th, 15.86th and 84.14th percentiles (the last two used for defining the error bars) after combining all the posteriors together (32310 samples) to take into account the differences existing between the different stellar evolution models. Our model provides an estimate of the extinction A_V at the distance of the star, $A_V = 0.09^{+0.09}_{-0.07}$ mag. This value is consistent with zero and is in agreement with the results of the 3D dust mapping with Pan-STARRS 1.

4. Photometric transit analysis

The transit analysis was done in the same manner as described in Mayo et al. (2018). The two planets in the system were fit simultaneously using the *BATMAN* transit fitting package. The model consists of four global parameters (baseline flux level, a noise parameter, and a quadratic limb darkening law) as well as five

²Available at <http://www.astro.up.pt/~sousasag/ares/>

³Available at <http://www.as.utexas.edu/~chris/moog.html>

⁴<https://github.com/LucaMalavolta/CCFpams>

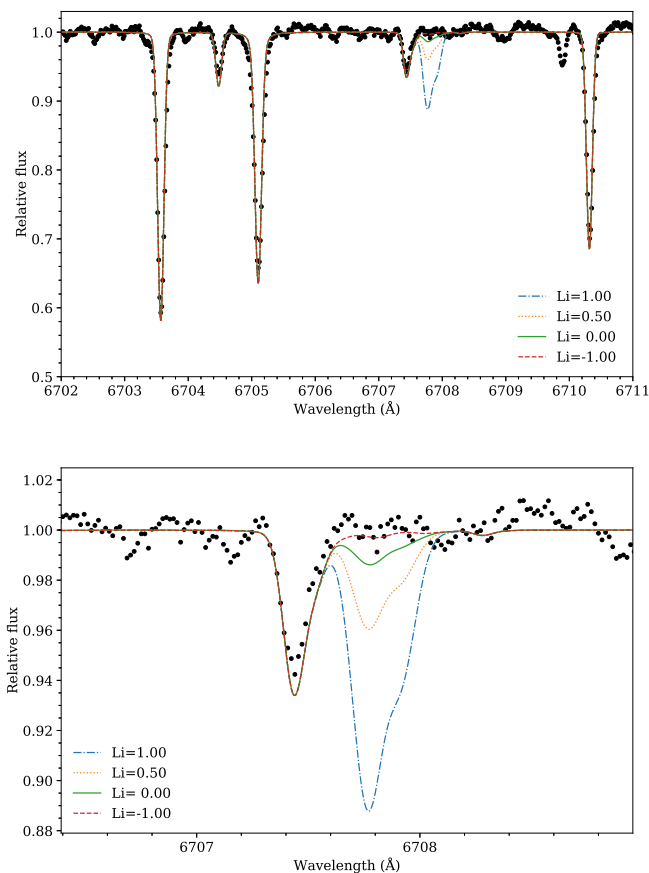


Fig. 2. *Top panel:* portion of the HARPS-N co-added spectrum of K2-36 containing the LiI line at 6707.8 Å, compared to four different syntheses (lines of various colors and styles), each differing only for the assumed lithium abundance. *Bottom panel:* zoom-in view of the region around 6707.8 Å to enable easier comparison between the observed data and model spectra for low Li abundances.”

parameters per planet (time of transit, period, R_p/R_* , semi-major axis, and inclination). Our model also assumes zero eccentricity and non-interacting planets. The parameters were estimated using *emcee* (Foreman-Mackey et al. 2013), a python package to perform Markov chain Monte Carlo (MCMC) analysis. Convergence was determined by requiring the Gelman-Rubin statistic (Gelman & Rubin 1992) to be less than 1.1 for all parameters. The only difference between our analysis and that of Mayo et al. (2018) is that we included a prior on the stellar density ρ_\odot in the light curve model fit. Specifically, at each step in the MCMC simulation we took the stellar density estimated from the transit fit at that step and applied a Gaussian prior to penalize values discrepant from our spectroscopic estimate of ρ_\odot . Table 2 summarizes the fit results. We see that, while our results are consistent with those in Mayo et al. (2018), the prior on the stellar density reduced the uncertainties in planetary radii, inclinations and transit durations. Planet radii are consistent within 1σ with those derived by Sinukoff et al. (2016), and have a similar precision.

Based on their radii, K2-36b and K2-36c are each representative of one of the two planet populations in the radius distribution, below $\sim 1.8 R_\oplus$ and above $\sim 2 R_\oplus$, as characterized by Fulton & Petigura (2018). We note that the mutual inclination between the orbital planes of the planets ($\Delta I \leq 3^\circ$) is in agreement with the results of Dai et al. (2018) based on the analysis of Kepler/K2 multi-planet systems (not including K2-36). They

Table 1. Summary of the fundamental stellar parameters of K2-36.

Parameter	Value	Ref.
RA [ICRS J2015]	11:17:47.78	(1)
DEC [ICRS J2015]	+03:51:59.00	(1)
μ_{α^*} [mas/year]	-20.521 ± 0.076	(1)
μ_δ [mas/year]	26.194 ± 0.058	(1)
Parallax [mas]	9.0832 ± 0.0504	(1)
V [mag]	11.803 ± 0.030	(2)
$B - V$	0.992 ± 0.064	(2)
K_s [mag]	9.454 ± 0.025	(3)
WISE/W1 [mag]	9.379 ± 0.023	(4)
WISE/W12 [mag]	9.442 ± 0.020	(4)
Radius [R_\odot]	$0.718^{+0.008}_{-0.006}$	(5a)
	0.74 ± 0.04	(6)
	0.75 ± 0.02	(7)
Mass [M_\odot]	0.79 ± 0.01	(5a)
	0.80 ± 0.04	(6)
	$0.80^{+0.02}_{-0.03}$	(7)
Density [ρ_\odot]	2.12 ± 0.04	(5a)
T_{eff} [K]	4916^{+35}_{-37}	(5)
	4924 ± 60	(6)
	4944 ± 50	(7)
$\log g$ [cgs]	$4.621^{+0.005}_{-0.004}$	(5b)
	4.65 ± 0.10	(6)
	4.70 ± 0.10	(7)
[Fe/H] [dex]	$-0.09^{+0.06}_{-0.04}$	(5)
	-0.03 ± 0.04	(6)
	-0.03 ± 0.08	(7)
Age [Gyr]	$1.4^{+0.4}_{-0.5}$	(5a)
	1.5 ± 0.4	(5c)
	1.1 ± 0.2	(5d)
$\log(L/L_\odot)$	-0.57 ± 0.01	(5a)
$u \sin i_*$ [km s $^{-1}$]	< 2	(5)
	2 ± 1	(6)
$\langle \log R'_{\text{HK}} \rangle$ [dex]	-4.50	(5)
P_{rot} [days]	16.9 ± 0.2	(5)

Notes. (1) *Gaia* DR2 (Gaia Collaboration et al. 2016, 2018); (2) APASS DR9 (Henden et al. 2015); (3) 2MASS Catalog (Skrutskie et al. 2006); (4) WISE Catalog; (5) this work; (5a) this work, derived from isochrones by imposing an age in the range 600 Myr–2 Gyr; (5b) derived from isochrones, and not from spectral analysis; (5c) based on a rotation-age relationship, and consistent with the measured $\langle \log R'_{\text{HK}} \rangle$; (5d) based on the activity-age calibration of Mamajek & Hillenbrand (2008); (6) Sinukoff et al. (2016); (7) Mayo et al. (2018).

found that when the innermost planet is closer to the host star than $a/R_* = 5$, ΔI can be likely greater than $\sim 5^\circ$, and this effect could also depend on the orbital period ratio, with pairs with $P_c/P_b \geq 5$ –6 showing larger ΔI . K2-36b has $a/R_* = 6.6$, the period ratio is $P_c/P_b \sim 3.8$, and the measured ΔI is very close to the dispersion of 2.0 ± 0.1 degrees they found for multi-planet systems where the innermost planet has $5 < a/R_* < 12$. This suggests that K2-36 likely belongs to a group of systems that evolved through a mechanism which did not excite the inclination of the innermost planet, therefore without resulting in different orbital architectures.

5. Stellar activity analysis

5.1. Stellar rotation from K2 light curve

Looking at the light curve of K2-36 (Fig. 1, upper panel), the modulation induced by the stellar rotation can be clearly seen. The data before the gap show a two-maxima pattern that repeats every ~ 17 days, suggesting that this could be the actual stellar rotation period P_{rot} . The scatter of the data before the gap is $\sigma_{\text{phot}}=2.4\%$, which increases to $\sigma_{\text{phot}}=3.9\%$ for data collected after the gap. A positive trend is seen in the second batch of data, that suggests that the active regions on the stellar photosphere are evolving with a timescale comparable with the stellar rotation period. However, we note that the light curve extracted with the alternative pipeline EVEREST (Luger et al. 2016) shows a weaker trend (light curve not shown here), implying that it could be not entirely astrophysical in origin. The highest increase in the relative flux of the light curve maxima is limited to $\sim 0.2\%$, and it is observed between the last two rotation cycles. To determine P_{rot} we computed the autocorrelation function (ACF) of the light curve using the DCF method by Edelson & Krolik (1988) (Fig. 3). The ACF has been explored up to the 80-day time span. The highest ACF peak occurs at ~ 16.7 days. We modelled this peak with a Gaussian profile⁵ in order to determine the error on P_{rot} , that we assume to be equal to the Gaussian RMS width. We get $P_{\text{rot}}=16.7\pm 1.9$ days.

Since the light curve shows evidence for quasi-periodic variations on a timescale of the order of P_{rot} , this makes it interesting to analyse the data using a Gaussian process (GP) regression as done, e.g., by Haywood et al. (2014), Cloutier et al. (2017), or Angus et al. (2018) to model space-based photometry, adopting a quasi-periodic kernel defined by the covariance matrix

$$K(t, t') = h^2 \cdot \exp \left[-\frac{(t-t')^2}{2\lambda^2} - \frac{\sin^2 \left(\frac{\pi(t-t')}{\theta} \right)}{2w^2} \right] + \sigma_{\text{phot}, \text{K2}}^2(t) \cdot \delta_{t, t'} \quad (1)$$

where t and t' represent two different epochs. The four hyperparameters are h , which represents the amplitude of the correlations; θ , which parametrizes the rotation period of the star; w , which describes the level of high-frequency variation within a complete stellar rotation; and λ , which represents the decay timescale of the correlations and can be physically related to the active region lifetimes. The flux error at time t is indicated by $\sigma_{\text{phot}, \text{K2}}(t)$, and $\delta_{t, t'}$ is the Kronecker delta. We introduced a free parameter to model the offset due to the gap in the K2 observations. Since the computing time for a GP regression scales as N^3 , where N is the number of data points, we analysed the 6-hr binned light curve instead of the full dataset.

All the GP analyses presented in this work (see also Sect. 5.2 and 6) were carried out using the publicly available Monte Carlo sampler and Bayesian inference tool MultiNestv3.10 (e.g. Feroz et al. 2013), through the pyMultiNest wrapper (Buchner et al. 2014), by adopting 800 live points and a sampling efficiency of 0.5. All the logarithms of the Bayesian evidence ($\ln \mathcal{Z}$) mentioned in our work were calculated by MultiNest. The GP component of our code is the publicly available GEORGEv0.2.1 python module (Ambikasaran et al. 2016). The results of the analysis are summarized in Table 3. The rotation period, that

⁵using LMFIT, a Non-Linear Least-Squares Minimization and Curve-Fitting for Python.

we left free to vary between 0 and 20 days, is consistent with, but more precise than, the ACF estimate ($P_{\text{rot}}=16.9\pm 0.2$ days). The best-fit value for the evolution timescale of the active regions is well constrained ($\lambda = 106_{-11}^{+14}$ days) and of the order of a few rotation periods. The best-fit value for the offset is 0.0036 ± 0.0004 , and Fig. 4 shows the light curve corrected for the offset. Within the framework of a quasi-periodic model, the corrected light curve shows that the active regions on one hemisphere are evolving faster than those on the opposite side of the stellar disk, because the relative height of one maximum has increased by $\sim 1.2\%$ over the observation time span.

Using our measure for the stellar radius and the upper limit for $v \sin i_*$ (which coincides with the best-fit value of Sinukoff et al. 2016), the expected maximum rotation period is $P_{\text{rot}} = 17.7$ days. This result implies that the projected inclination of the spin axis is $i_* \sim 90^\circ$.

Since the star is active, we searched for flares in the K2 light curve, without finding any clear evidence of large events.

5.2. Stellar activity spectroscopic diagnostics

We characterized the activity of K2-36 during the time span of the HARPS-N observations by analysing a set of standard spectroscopic indicators. We considered the full width at half maximum (FWHM) of the CCF, the bisector inverse slope (BIS) and V_{asy} indicators, that quantify the CCF line asymmetry (V_{asy} is defined by Figueira et al. 2013), the chromospheric activity index $\log R'_{\text{HK}}$, and the activity indicator based on the H_α line (derived following the method described in Gomes da Silva et al. 2011). The time series of all the indicators are listed in Table 4 and shown in Fig. 5. Extending to HARPS-N the results by Santerne et al. (2015) valid for the HARPS spectrograph, the uncertainties of the FWHM and BIS are fixed to $2\sigma_{\text{RV}}$, where σ_{RV} are the RV internal errors. Positive trends are clearly visible for the FWHM, $\log R'_{\text{HK}}$, and H_α index, pointing out that the level of activity of K2-36 increased during the time span of our observations. These trends could be part of a long-term activity cycle, but our time span of ~ 3.5 years is not extended enough to confirm this. We note that the dispersion in the FWHM, BIS, V_{asy} and H_α data increased with time, as a consequence of the increasing levels of activity. We calculated the frequency spectrum of these datasets using the Generalised Lomb-Scargle (GLS) algorithm (Zechmeister & Kürster 2009), after correcting the trends in the FWHM, $\log R'_{\text{HK}}$, and H_α data by subtracting from each seasonal data chunk the corresponding average value. The periodograms are shown in Fig. 5. For the FWHM, BIS, and V_{asy} we find the highest peak at 8.6 days; for $\log R'_{\text{HK}}$ the peak with the highest power occurs at 16.7 days, and for the H_α index the main peak is at 12.9 days, even though peaks of slightly lower power occur at P_{rot} and its first harmonic. In conclusion, these indicators appear modulated over P_{rot} or $P_{\text{rot}}/2$. We note that a strong correlation exists between $\log R'_{\text{HK}}$ and H_α ($\rho_{\text{Spear}}=0.8$).

We fitted all the indicators with a quasi-periodic GP model, as explained in Sect. 4. Since they have been extracted from the same spectra used to measure the RVs, the outcomes of such analysis are important to eventually set up the analysis of the RVs, in order to properly remove the stellar activity contribution. Results of the GP regression are listed in Table 3.

6. RV analysis

Predicting the amplitude of the RV variations due to the stellar contribution based on the photometric variability is a complex task, especially when photometric and spectroscopic data

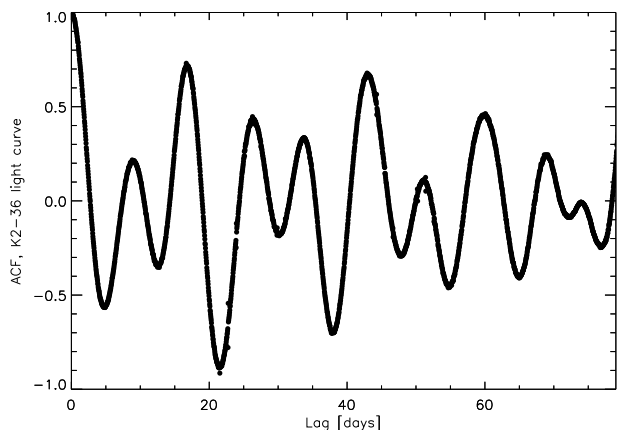


Fig. 3. Autocorrelation function of the K2-36 light curve shown in Fig. 1.

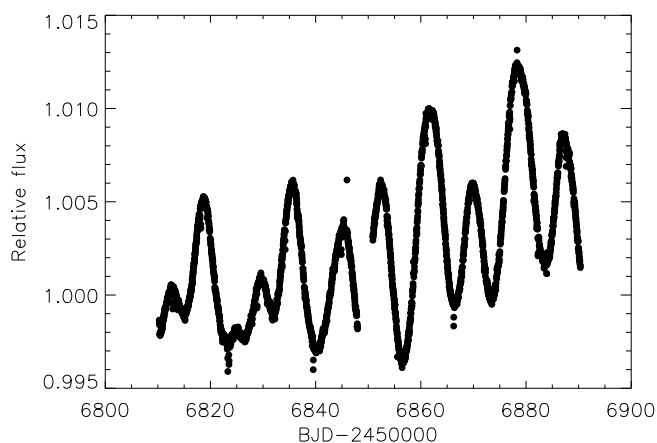


Fig. 4. K2-36 light curve corrected for the offset introduced by the gap in the K2 observations (see Fig. 1 for comparison). An offset of $\sim 0.36\%$ has been determined through a Gaussian process regression, as described in Section 4.

are not collected during the same seasons. Following Mann et al. (2018), a guess for the RV variability could be estimated as $\sim \sigma_{\text{phot}} \cdot v \sin i_*$, where σ_{phot} is the scatter observed in the K2 light curve. The expected RV variability for K2-36 due to stellar activity is therefore $\sim 2\text{-}5 \text{ m s}^{-1}$. According to the calibration for K-dwarfs derived by Santos et al. (2000), the expected radial velocity scatter for K2-36 is $\sim 9 \text{ m s}^{-1}$. We anticipate here that the signal due to the stellar activity largely dominates the observed RVs variations, and it is 5-8 times larger than the semi-amplitudes of the planetary signals, which are of the order of the average RV internal errors ($\sim 2\text{-}3 \text{ m s}^{-1}$). When dealing with such an active star it is interesting to compare the results obtained from RV extracted with two different procedures, that in principle could be sensitive to stellar activity in different ways for this specific case. Therefore, we have calculated the systemic RVs through the CCF-based recipe of the on-line DRS, using a mask suitable for stars with spectral type K5V, and relative RVs with the TERRA pipeline (Anglada-Escudé & Butler 2012), measured against a high S/N template spectrum. We corrected the TERRA RVs for the perspective acceleration using parallax and proper motion from *Gaia* DR2. The complete list of RVs

Table 2. Best-fit values obtained from modelling the transit light curve of the K2-36 planets. Data from literature are shown for comparison.

Parameter	Best-fit value	Reference
$P_{p,b}$ [days]	1.422614 ± 0.000038	(1)
	1.42266 ± 0.00005	(2)
	1.422619 ± 0.000039	(3)
$T_{0,b}$ [BJD-2 454 833]	1977.8916 ± 0.0013	(1)
	1977.8914 ± 0.0013	(3)
$T_{\text{dur},b}$ [days]	$0.05157^{+0.00046}_{-0.00034}$	(1)
$P_{p,c}$ [days]	5.340888 ± 0.000086	(1)
	5.34059 ± 0.00010	(2)
	$5.340883^{+0.000088}_{-0.000089}$	(3)
$T_{0,c}$ [BJD-2 454 833]	1979.84001 ± 0.00071	(1)
	$1979.84015^{+0.00072}_{-0.00073}$	(3)
$T_{\text{dur},c}$ [days]	$0.0564^{+0.0035}_{-0.0027}$	(1)
R_b/R_*	$0.01828^{+0.00072}_{-0.00099}$	(1)
	$0.0180^{+0.0026}_{-0.0013}$	(3)
R_c/R_*	$0.04119^{+0.0043}_{-0.0029}$	(1)
	$0.04^{+0.17}_{-0.01}$	(3)
$R_b (R_{\oplus})$	1.43 ± 0.08	(1)
	1.32 ± 0.09	(2)
$R_c (R_{\oplus})$	$1.47^{+0.22}_{-0.11}$	(3)
	3.2 ± 0.3	(1)
	$2.80^{+0.43}_{-0.31}$	(2)
i_b [deg]	$4.0^{+14.0}_{-1.0}$	(3)
	$84.45^{+0.78}_{-0.48}$	(1)
i_c [deg]	$86.3^{+2.7}_{-6.2}$	(3)
	$86.917^{+0.066}_{-0.056}$	(1)
b_b	$85.5^{+3.9}_{-3.3}$	(3)
	$0.66^{+0.06}_{-0.09}$	(1)
b_c	$0.89^{+0.01}_{-0.02}$	(1)
$a_b [R_*$	6.63 ± 0.11	(1)
a_b [AU]	0.0223 ± 0.0004	(1)
$a_c [R_*$	$16.01^{+0.26}_{-0.27}$	(1)
a_c [AU]	0.054 ± 0.001	(1)
$T_{\text{eq},b}$ [K]	1224 ± 13	(1a)
$T_{\text{eq},c}$ [K]	788 ± 9	(1a)
Insolation $S_b [S_{\oplus}]$	529 ± 23	(1)
Insolation $S_c [S_{\oplus}]$	90 ± 4	(1)

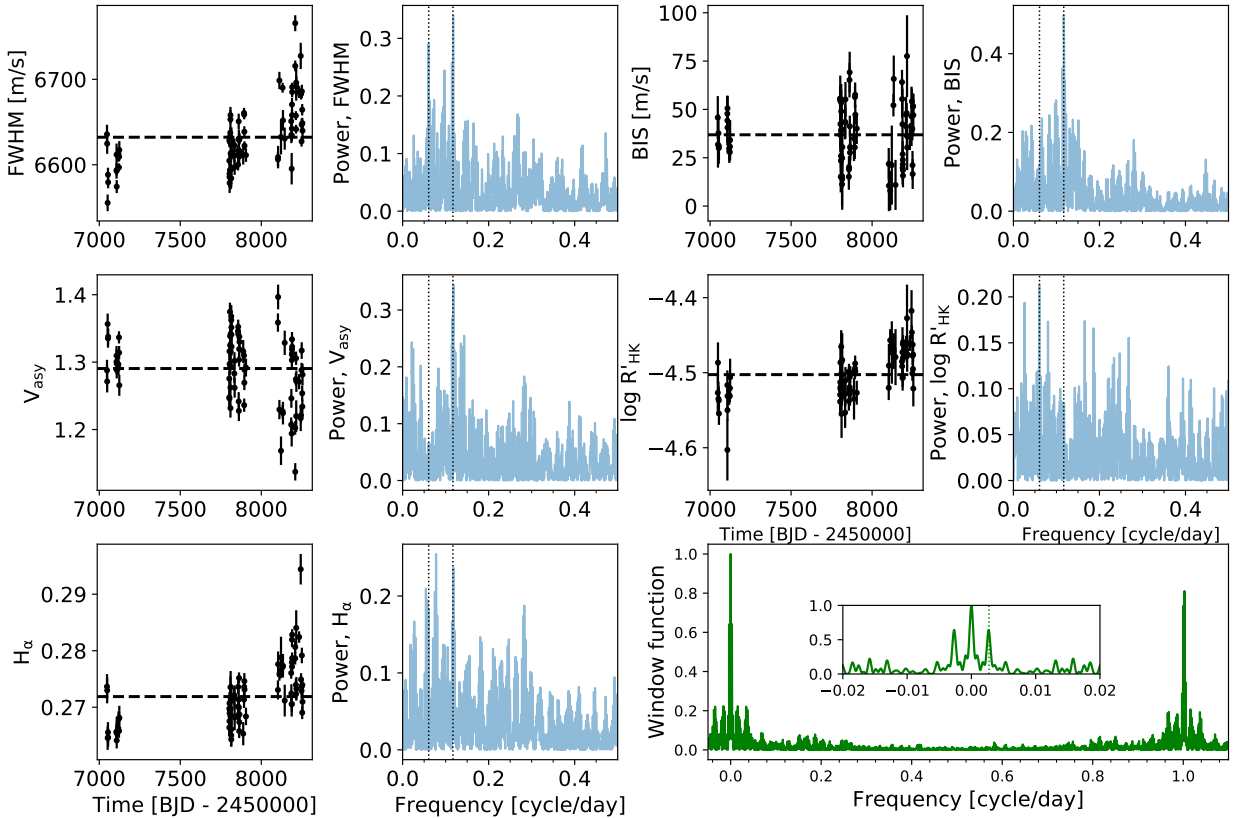
Notes. (1) This work. (1a) This work, assuming the Bond albedo $A_b=0.3$ (2) Sinukoff et al. (2016). (3) Mayo et al. (2018)

is presented in Table 5. We summarize general properties of the two RV datasets in Table 6, and show the time series in Fig. 6. One common feature is the increase of the scatter observed in the last two seasons with respect to the first. This is a consequence of the increasing stellar activity discussed in Sect. 5.2. The scatter over the time span is similar for all the methods, and the internal errors calculated with TERRA are on average lower than those of the DRS.

After a preliminary analysis of the RVs, in this Section we present, and compare, the results of different global models (combined fit of planet orbital equations and stellar signals). We used the results from the light curve analysis to fix the priors of

Table 3. GP hyper-parameters of a quasi-periodic model applied to the K2 light curve (6-hr bins), and to the asymmetry and activity index time series derived from HARPS-N spectra. Uncertainties are given as the 16th and 84th percentiles of the posterior distributions.

Jump parameter	Prior	K2 light curve	BIS span	FWHM ^a	V _{asy} ^a	log R' _{HK} ^a	H _α ^a
<i>h</i>	light curve: $\mathcal{U}(0,0.5)$ BIS-(<i>BIS</i>): $\mathcal{U}(0,100)$ [m s ⁻¹] FWHM-(<i>FWHM</i>): $\mathcal{U}(0,200)$ [m s ⁻¹] V _{asy} : $\mathcal{U}(0,2)$ [m s ⁻¹] log R' _{HK} - ⟨log R' _{HK} ⟩: $\mathcal{U}(0,1)$ [dex] H _α : $\mathcal{U}(0,0.5)$	0.31 ^{+0.06} _{-0.04}	15 ⁺⁴ ₋₃	40 ⁺⁸ ₋₆	0.7±0.1	0.025 ^{+0.009} _{-0.006}	0.11±0.02
<i>λ</i>	$\mathcal{U}(0,1500)$ [days]	106 ⁺¹⁴ ₋₁₁	144 ⁺¹⁰⁰ ₋₅₅	79 ⁺³⁴ ₋₂₄	161 ⁺⁸⁰ ₋₅₄	270 ⁺¹⁷⁵ ₋₁₁₁	1308 ⁺¹⁴² ₋₂₅₁
<i>w</i>	$\mathcal{U}(0,1)$	0.987 ^{+0.009} _{-0.02}	0.6±0.2	0.41 ^{+0.08} _{-0.06}	0.87±0.1	0.8 ^{+0.1} _{-0.2}	0.96 ^{+0.03} _{-0.06}
<i>θ</i>	$\mathcal{U}(0,20)$ [days]	16.9±0.2	8.56 ^{+0.07} _{-0.04}	17.2±0.1	17.24 ^{+0.07} _{-0.53}	16.7 ^{+0.3} _{-3.2}	16.90±0.01

^(a) Time series not corrected for the long-term trend.

Fig. 5. Time series of the FWHM, BIS and V_{asy} CCF line diagnostics, and the log(R'_{HK}) and H_α activity indexes, shown next to their corresponding GLS periodograms (after removing the trends in the FWHM, log(R'_{HK}) and H_α data as described in the text). The dashed horizontal lines mark the mean values, to highlight the increasing trend visible in the FWHM, log(R'_{HK}) and H_α data. Vertical dotted lines in the periodograms mark the locations of the stellar rotation period, as derived from K2 photometry, and its first harmonic. The panel in the bottom right corner shows the window function of the data. A zoomed view of the low-frequency part of the spectrum is shown in the inset plot, and a vertical dotted line marks the 1-year orbital frequency of the Earth.

the orbital periods and time of inferior conjunction for K2-36 b and K2-36 c. We assume independent Keplerian motions (i.e. ignoring mutual planetary perturbations, which would be significantly below 1 mm s⁻¹) in all the cases and, especially considering the short orbital period of K2-36 b, we did not bin the data on a nightly basis to make use of all the available information in each single data point.

6.1. Frequency content and correlation with activity indicators

We scrutinized the frequency content in the RV datasets with the GLS algorithm by fitting a single sinusoid to the data. Periodograms are shown in Fig. 6. All look very similar, with the main peak clearly located at ~8.5 days, that is the first harmonic of P_{rot} , and semi-amplitudes of ~16 m s⁻¹, which are equal to the measured RMS. This analysis shows that signals due to stellar activity dominate the RVs. The orbital frequency $f \sim 0.7$ d⁻¹ associated with K2-36 b appears with much less power, while the Doppler signal of K2-36 c is missing. We analysed the resid-

uals of the RVs with a GLS periodogram (using DRS data only because of the similarities with the periodogram of the TERRA RVs), after subtracting the best-fit sinusoid, and the periodogram shows the main peak at P_{rot} . An additional pre-whitening results in a peak at frequency $f \sim 0.17 \text{ d}^{-1}$, which likely corresponds to the second harmonic of P_{rot} . This analysis points out that the stellar activity component could be mitigated by a sum of at least three sinusoids with periods P_{rot} , $P_{\text{rot}}/2$ and $P_{\text{rot}}/3$. This simple pre-whitening procedure does not allow for the identification of significant power at the orbital planetary frequencies, pointing out that the detection of the two planets using only RVs, without the help from transits and an effective treatment of the stellar activity contribution, is very complicated. We have folded the RVs of each season taken separately at the period $P=8.5$ days, and we observe a change in the phase of the signal. This suggests that the stellar activity signal has been evolving on a timescale less than one year, and that a quasi-periodic fit of the stellar component could be more appropriate than a simple combination of sinusoids.

We checked the correlation between the RVs and the CCF line asymmetry and activity indicators discussed in Sect. 5.2 by calculating the Spearman's rank correlation coefficients. Results are shown in Fig. 7, where we used the RVs from DRS. Significant anti-correlation exists just between the DRS RVs and BIS⁶ ($\rho_{\text{Spear}} = -0.65$), which is not surprising since they have similar GLS periodograms. This anti-correlation is expected when the observed RV variations are due mainly to the presence of dark spots on the stellar photosphere, as shown by the light curve modulation (Boisse et al. 2011).

6.2. Joint modelling of planetary and stellar signals (1): sum of sinusoids

Based on the results of the GLS analysis, first we tested a model (hereafter model 1) with the activity component described by a sum of three sinusoids, each with periods sampled around P_{rot} , $P_{\text{rot}}/2$ and $P_{\text{rot}}/3$, using the priors indicated in Table 7. We modelled the planetary signals as circular orbits. In total, 17 free parameters were used, including the uncorrelated jitter and offset, that for the DRS RVs corresponds to the systemic velocity. Table 7 shows the results from the analysis of the DRS and TERRA datasets. The semi-amplitude K_b is fitted with a relative error of $\sim 50\%$, while that of the signal induced by K2-36 c is nearly twice K_b . We note that the required uncorrelated jitter σ_{jit} is more than twice the typical internal error $\sigma_{\text{RV}} \sim 2\text{-}3 \text{ m s}^{-1}$.

6.3. Joint modelling of planetary and stellar signals (2): de-trending using the BIS line asymmetry indicator

Since a significant anti-correlation is observed between the DRS RVs and the BIS asymmetry indicator, we modelled the stellar signal contribution by including a linear term $c_{\text{BIS}} \cdot \text{BIS}$ in the model (hereafter model 2). The planetary orbits were fixed to the circular case. For the semi-amplitudes of the planetary signals we get estimates that are nearly twice and nearly half those derived for model 1, for planet b and c respectively: $K_b = 4.8^{+1.8}_{-1.7} \text{ m s}^{-1}$ and $K_c = 2.8^{+1.7}_{-1.5} \text{ m s}^{-1}$. Since $\ln\left(\frac{\mathcal{Z}_{\text{model 1}}}{\mathcal{Z}_{\text{model 2}}}\right) \simeq +10$, which corresponds to a posterior odds ratio $\simeq 2 \times 10^4:1$, this model is very significantly disfavoured, according to the conventional scale adopted for model selection (see, e.g., Feroz et al. 2011).

⁶Since the BIS span indicator is extracted with the DRS pipeline, we limit this analysis to the DRS RVs only.

6.4. Joint modelling of planetary and stellar signals (3): Gaussian process regression analysis

We analysed the RV datasets with a GP regression using the quasi-periodic kernel (Eq. 1) to model the correlated signal introduced by the stellar activity contribution. Since both signals modulated on P_{rot} and $P_{\text{rot}}/2$ are present in the RV timeseries, we left the hyper-parameter θ free to explore uniformly the range between 0 and 20 days. In general, for the hyper-parameters θ , w , and λ we used the same priors as those in Table 3. We included the parameter σ_{jit} , which is summed in quadrature with σ_{RV} in Eq. 1, to take into account other sources of uncorrelated noise not included in $\sigma_{\text{RV}}(t)$.

We first considered the case of circular orbits, then we included the eccentricities e_b and e_c as free parameters. The results of the analyses are shown in Table 8. Concerning the circular model, looking at the best-fit values of the hyper-parameters, θ is determined with high precision and its value corresponds to P_{rot} , and the evolutionary timescale of the active regions λ is $\sim 5\text{-}8$ times P_{rot} , depending on the RV extraction algorithm. This is in very good agreement with the results of the analysis of the light curve and the FWHM activity diagnostic, while there is evidence for a slightly longer evolutionary timescale from the log R'_{HK} activity index. The Doppler semi-amplitude K_b is in agreement within the errors with that obtained from model 1, both for DRS ($K_b = 2.1 \pm 0.9 \text{ m s}^{-1}$) and TERRA ($K_b = 2.6 \pm 0.7 \text{ m s}^{-1}$), but more precise. The mass of K2-36 b is measured with a significance of $\sim 2.5\sigma$ (DRS, $m_b = 3.2^{+1.4}_{-1.3} M_{\oplus}$) and $\sim 3.6\sigma$ (TERRA, $m_b = 3.9 \pm 1.1 M_{\oplus}$), and there is agreement within 1σ between the two RV extraction pipelines. As for K2-36 c, the mass is measured at best with a significance of $\sim 3.5\sigma$ (TERRA, $m_c = 7.8 \pm 2.3 M_{\oplus}$), and all the values are in agreement within 1σ . When compared to model 1, the semi-amplitude of the K2-36 c signal is lower for both DRS and TERRA, and more precise.

Our analysis does not constrain the eccentricities of the two planets. In fact, for K2-36 b we get $e_{b, \text{DRS}} = 0.41^{+0.33}_{-0.30}$ (68.3th percentile=0.57) and $e_{b, \text{TERRA}} = 0.51^{+0.26}_{-0.37}$ (68.3th percentile=0.65), while for K2-36 c we get $e_{c, \text{DRS}} = 0.18^{+0.23}_{-0.12}$ (68.3th percentile=0.27) and $e_{c, \text{TERRA}} = 0.14^{+0.17}_{-0.10}$ (68.3th percentile=0.21). For both planets, the eccentricity differs from zero with a significance less than 1.5σ , and the peak of the posterior distribution of e_c occurs at zero. Therefore we conclude that our data do not allow us to constrain the eccentricities. Moreover, the eccentric model is statistically disfavoured with respect to the circular model for both the DRS ($\ln \mathcal{Z}_{\text{circular}} - \ln \mathcal{Z}_{\text{ecc}} = +2$) and TERRA ($\ln \mathcal{Z}_{\text{circular}} - \ln \mathcal{Z}_{\text{ecc}} = +2.5$) datasets.

Fig. 8 shows the RV signals due to the K2-36 planets, and the distribution of the HARPS-N measurements along the planetary orbits. In both cases, the orbit has been covered uniformly. We show in Fig. 9 the stellar component present in the RVs as fit by the GP quasi-periodic model (TERRA dataset). We note that the GLS periodogram of the stellar signal only is very similar to that obtained for the original RV dataset (Fig. 6), demonstrating that the quasi-periodic model gives a good representation of the activity component. Moreover, we folded the stellar component in the TERRA dataset, as fitted by the GP regression, at the stellar rotation period, and compared to the folded K2 light curve (Fig. 10). Interestingly the RV data, collected in 2017 and 2018 and with a good phase coverage at P_{rot} , have a similar phase pattern of the photometric data and appear only slightly shifted, despite more than 3 years separating the K2 observations from the HARPS-N observations.

Table 6. Properties of the two RV datasets analysed in this work.

Pipeline	RMS (all data) [m s ⁻¹]	RMS (1 st seas.) [m s ⁻¹]	RMS (2 nd seas.) [m s ⁻¹]	RMS (3 rd seas.) [m s ⁻¹]	Median internal error σ_{RV} [m s ⁻¹]
DRS	14.9	9.8	15.6	15.5	3.1
TERRA	14.7	9.4	14.8	16.2	2.3

Table 7. Results of the MC analysis performed on the RVs extracted with the DRS and TERRA recipes using a sum of three sinusoids to model the stellar activity component. Uncertainties are given as the 16th and 84th percentiles of the posterior distributions.

Jump parameter	Prior	Best-fit value	
		DRS	TERRA
γ [m s ⁻¹]	$\mathcal{U}(13550,13750)$ [DRS] $\mathcal{U}(-100,100)$ [TERRA]	13643.6 ^{+0.8} _{-0.9}	-0.09 ^{+0.84} _{-0.86}
σ_{jit} [m s ⁻¹]	$\mathcal{U}(0,20)$	6.4 ^{+0.8} _{-0.7}	6.8 ^{+0.7} _{-0.6}
Stellar activity signal			
P_{rot} [days]	$\mathcal{U}(15,18)$	16.65±0.02	16.68±0.02
$P_{rot}/2$ [days]	$\mathcal{U}(7,9.5)$	8.499 ^{+0.006} _{-0.005}	8.507±0.005
$P_{rot}/3$ [days]	$\mathcal{U}(4.5,6.5)$	5.754±0.003	5.755 ^{+0.004} _{-0.138}
$K_{act,P=P_{rot}}$ [m s ⁻¹]	$\mathcal{U}(0,30)$	7.8±1.2	7.9±1.2
$T_{0,act,P=P_{rot}}$ [BJD-2 450 000]	$\mathcal{U}(7800,7820)$	7811.5±0.4	7811.9 ^{+0.5} _{-0.4}
$K_{act,P=P_{rot}/2}$ [m s ⁻¹]	$\mathcal{U}(0,30)$	14.6±1.1	14.5±1.1
$T_{0,act,P=P_{rot}/2}$ [BJD-2 450 000]	$\mathcal{U}(7800,7810)$	7809.4±0.2	7809.1±0.2
$K_{act,P=P_{rot}/3}$ [m s ⁻¹]	$\mathcal{U}(0,20)$	7.4±1.4	6.7±1.3
$T_{0,act,P=P_{rot}/3}$ [BJD-2 450 000]	$\mathcal{U}(7800,7808)$	7802.9±0.2	7802.8 ^{+0.3} _{-0.2}
Planetary signals			
K_b [m s ⁻¹]	$\mathcal{U}(0,10)$	2.8±1.3	2.4±1.2
K_c [m s ⁻¹]	$\mathcal{U}(0,10)$	5.0±1.4	4.9±1.4
m_b [M_{\oplus}]	derived	4.2±1.8	3.7 ^{+1.8} _{-1.7}
m_c [M_{\oplus}]	derived	11.7 ^{+3.0} _{-3.4}	11.5±3.2
Bayesian evidence $\ln(\mathcal{Z})_{model 1}$		-310.5±0.06	-310.14±0.04

6.5. Adopted results

We tested three different models to derive the main planetary parameters. According to their Bayesian evidences the GP quasi-periodic and circular model is strongly favoured over all the other models (in particular $\ln(\frac{\mathcal{Z}_{model 3}}{\mathcal{Z}_{model 1}}) \simeq +14.5$ for the TERRA dataset, and $\ln(\frac{\mathcal{Z}_{model 3}}{\mathcal{Z}_{model 1}}) \simeq +9$ for the DRS dataset), therefore we adopt this as the best representation for the K2-36 system based on our data. Since the relative errors on the semi-amplitudes K_b and K_c are lower for the TERRA than for the DRS dataset, we adopt as our final solution the best-fit values obtained with the TERRA RVs. Based on that, K2-36 c has a mass ~ 2 times higher than that of K2-36 b ($m_b = 3.9 \pm 1.1 M_{\oplus}$, $m_c = 7.8 \pm 2.3 M_{\oplus}$), but its bulk density is $\sim 19\%$ that of the innermost planet ($\rho_b = 7.2^{+2.5}_{-2.1} \text{ g cm}^{-3}$, $\rho_c = 1.3^{+0.7}_{-0.5} \text{ g cm}^{-3}$). By using the relation $S/S_{\oplus} = (L/L_{\odot}) \times (AU/a)^2$, we derived the insolation fluxes $S_b = 529 \pm 23 S_{\oplus}$ and $S_c = 90 \pm 4 S_{\oplus}$: planet b is ~ 6 times more irradiated than K2-36 c. The derived planet equilibrium temperatures are $T_{eq,b} = 1224 \pm 13 \text{ K}$ and $T_{eq,c} = 788 \pm 9 \text{ K}$.

6.6. Robustness of the derived planet masses

We devised a test to assess how robust our results are. We simulated $N_{sim} = 100$ RV time series using the epochs of the HARPS-N spectra as time stamps, and assuming the TERRA dataset and the results of the GP global model to build the mock datasets.

We added two planetary signals (circular orbits) to the quasi-periodic stellar activity signal, with semi-amplitudes $K_b = 2.6$ and $K_c = 3.4 \text{ m s}^{-1}$. The orbital periods and epochs of inferior conjunction are those derived from K2 light curve. Each mock dataset has been obtained by randomly shifting each point of the exact solution within the error bar, assuming normal distributions centred to zero and with $\sigma = \sigma_{RV}(t)$. We use this set of simulated data to test our ability to retrieve the injected signals. We analysed the mock RV time series within the same MC framework used to model the original dataset, and for each free parameter we saved the 16th, 50th and 84th percentiles. Then, we analysed the posterior distributions of the N_{sim} median values, and for the planetary Doppler semi-amplitudes we get $K_b = 2.7^{+0.4}_{-0.5}$ and $K_c = 3.4^{+0.8}_{-0.6} \text{ m s}^{-1}$ (16th, 50th and 84th percentiles). Since these values are in very good agreement with those injected, that are equal to those we get from the GP analysis, this suggests that the best-fit values obtained for the original dataset are accurate.

6.7. Sensitivity of the planetary masses to an extended dataset

Through a different set of simulations we have investigated how much the precision of the planet masses would have improved with an additional season of RV data. We simulated $N_{sim} = 50$ RV datasets by randomly drawing 40 additional epochs (dif-

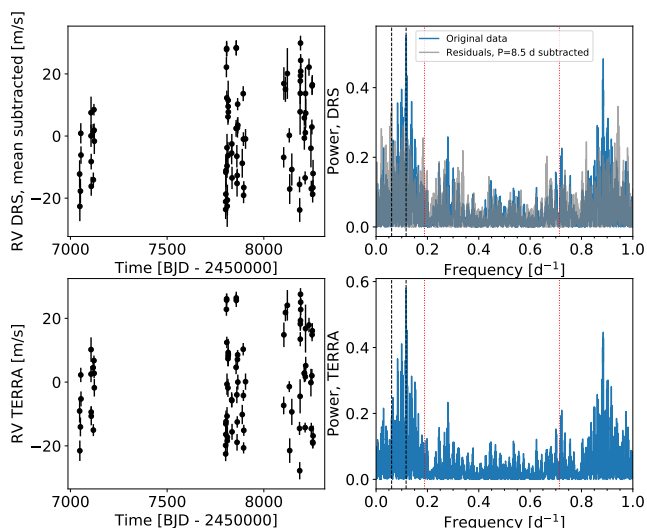


Fig. 6. *Left column.* Radial velocity time series extracted from HARPS-N spectra using the DRS (upper plot) and TERRA (lower plot) pipelines. *Right column.* GLS periodograms of the RV time series (blue line). Vertical dashed lines mark the location of the highest peak at ~ 8.5 days and the stellar rotation frequency, for all the datasets. Vertical dotted lines in red mark the orbital frequencies of the K2-36 planets. For the DRS dataset only, we show the periodogram of the residuals, after subtracting the signal with period of 8.5 days (gray line), with the main peak located at $P \sim 16.5$ days, which corresponds to the stellar rotation period. The window function of the data (not shown) is the same as in Fig. 5.

ferent for each mock dataset) within a 180-day timespan, six months after the end of the third observing season with HARPS-N (for a total of 121 RV measurements per dataset, including the original data). We assumed a sampling characterized by one RV measurement per night, and adopted the GP quasi-periodic best-fit solution to represent the stellar activity term. We used the `sample_conditional` module in the GEORGE package to draw samples from the predictive conditional distribution (different for each mock dataset) at the randomly selected epochs. Then, we have injected two planetary signals with semi-amplitudes $K_b=2.6$ and $K_c=3.4$ m s^{-1} and circular orbits, using the ephemeris derived from the K2 light curve. The internal errors σ_{RV} of the additional RVs have been randomly drawn from a normal distribution centred on the mean of the internal errors of the original RV dataset and with σ equal to the RMS of the real array σ_{RV} . In order to avoid the selection of σ_{RV} values that are too optimistic and never obtained for the original dataset, we have simulated only internal errors greater than 1 m s^{-1} . This analysis suggests that, on average, the significance of the retrieved semi-amplitudes of the planetary signals are expected to increase to 4.4σ for K2-36 b and to 5.6σ for K2-36 c, and the same result is obtained for the planet masses. Concerning the densities, their significance increases to 4σ (ρ_b) and to 2.6σ (ρ_c), thus only of a slight amount with respect to the original dataset. Our conclusion is that, under the hypothesis that the structure of the stellar activity signal is preserved several months after the last epoch of the actual observations, a set of 40 additional RVs (which is an affordable amount of measurements to be collected over one season) does not help in improving the precision of the derived planetary parameters enough to significantly improve the theoretical estimates of the planets' bulk composition based on theoretical models.

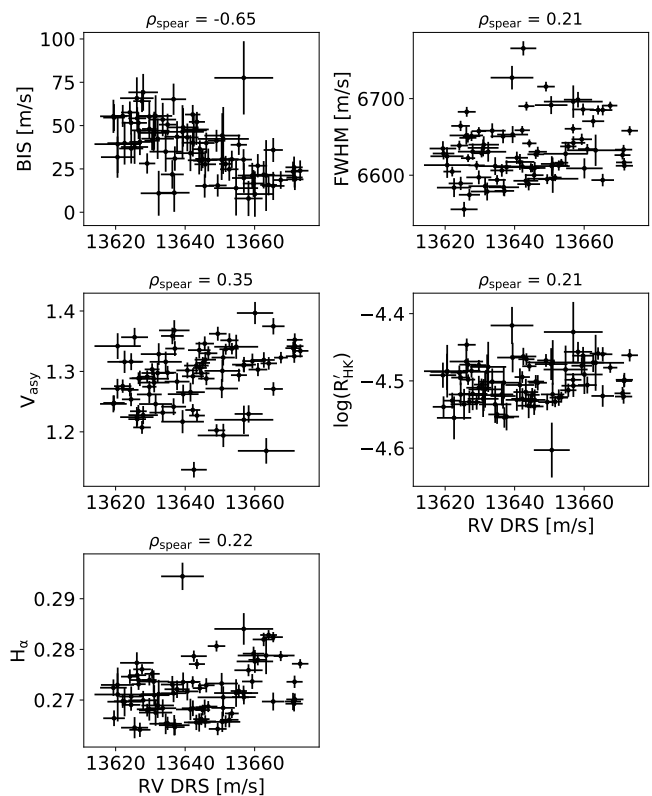


Fig. 7. Correlations between radial velocities (from DRS), the CCF line profile indicators, and activity diagnostics.

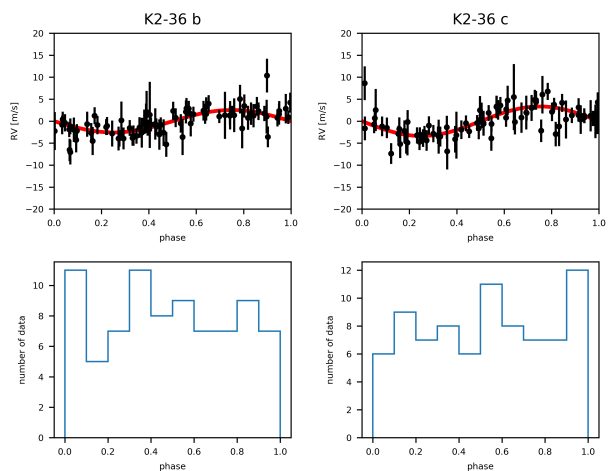


Fig. 8. Doppler signals due to the K2-36 planets (TERRA radial velocity dataset, after removing the GP quasi-periodic stellar activity term), folded according to their transit ephemeris (phase=0 corresponds to the time of inferior conjunction). The histograms show the distribution of the RV measurements along the planetary orbits.

7. Discussion

In this Section we first use our measurements of the planet parameters to investigate the bulk structure of K2-36 b and K2-36 c in the context of the photo-evaporation as the main driver of the evolution of these close-in, low-mass planets.

Table 8. Best-fit solutions for the model tested in this work (quasi-periodic GP model) applied to the HARPS-N RV time series extracted with the DRS and TERRA pipelines. Our global model includes two orbital equations (circular and eccentric case). Uncertainties are given as the 16th and 84th percentiles of the posterior distributions.

Jump parameter	Prior	Best-fit value	
		DRS	TERRA
Stellar activity GP model			
h [m s ⁻¹]	$\mathcal{U}(0,30)$	16.3 ^{+3.8} _{-2.7}	17.11 ^{+3.9} _{-2.8}
λ [days]	$\mathcal{U}(0,1500)$	131 ⁺⁵⁵ ₋₃₅	93 ⁺²² ₋₂₀
w	$\mathcal{U}(0,1)$	0.33 ^{+0.06} _{-0.05}	0.33±0.05
θ [days]	$\mathcal{U}(0,20)$	16.99 ^{+0.09} _{-0.07}	17.06±0.08
σ_{jit} [m s ⁻¹]	$\mathcal{U}(0,20)$	2.5±1.0	1.6 ^{+0.8} _{-0.9}
γ [m s ⁻¹]	$\mathcal{U}(13550,13750)$	13640.7 ^{+4.9} _{-5.2}	-1.7 ^{+5.1} _{-5.2}
K_b [m s ⁻¹]	$\mathcal{U}(0,10)$	2.1±0.9	2.6±0.7
K_c [m s ⁻¹]	$\mathcal{U}(0,10)$	2.9±1.1	3.4±1.0
Derived quantities ^(a)			
m_b (M_{\oplus})		3.2 ^{+1.4} _{-1.3}	3.9±1.1
m_c (M_{\oplus})		6.7 ^{+2.7} _{-2.6}	7.8±2.3
ρ_b [g cm ⁻³]		5.9 ^{+2.9} _{-2.5}	7.2 ^{+2.5} _{-2.1}
ρ_c [g cm ⁻³]		1.1 ^{+0.6} _{-0.5}	1.3 ^{+0.7} _{-0.5}
Bayesian Evidence $\ln \mathcal{Z}_{\text{model } 3}$		-301.45±0.02	-295.5±0.08

Notes. ^(a) Derived quantities from the posterior distributions. We used the following equations (assuming $M_s + m_p \cong M_s$): $m_p \sin i \cong (K_p \cdot M_s^{3/5} \cdot \sqrt{1 - e^2} \cdot P_p^{1/5}) / (2\pi G)^{1/5}$; $a \cong [(M_s \cdot G)^{1/3} \cdot P_p^{2/3}] / (2\pi)^{2/3}$, where G is the gravitational constant. We set $e=0$ for circular orbits.

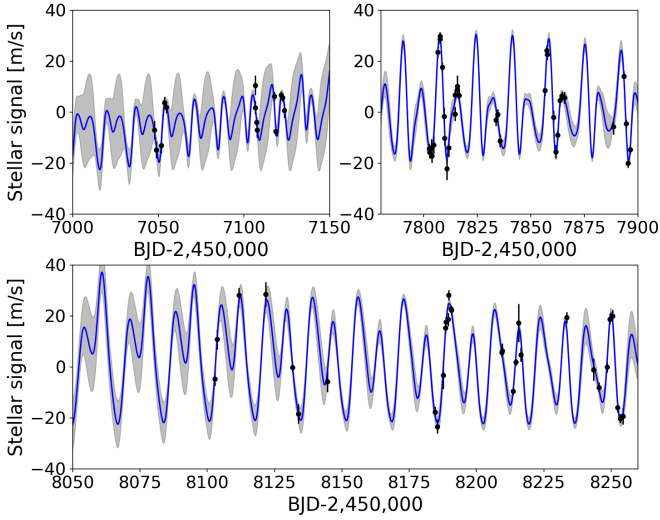


Fig. 9. Stellar activity component in the radial velocities (TERRA dataset) as fitted using a GP quasi-periodic model (circular case). Each panel shows one of the three observing seasons. The blue line represents the best-fit solution, and the grey area the 1 σ confidence interval.

7.1. Planets in the mass-radius diagram

The exoplanet mass-radius diagram is shown in Fig. 11, and it includes the masses of the K2-36 planets derived from the GP analysis of the TERRA dataset. K2-36 b is nicely located on the theoretical curve for planets with Earth-like rocky composition, while the Neptune/sub-Neptune size K2-36 c has a bulk structure compatible with having a H₂-dominated gas envelope of ~ 1 –2%

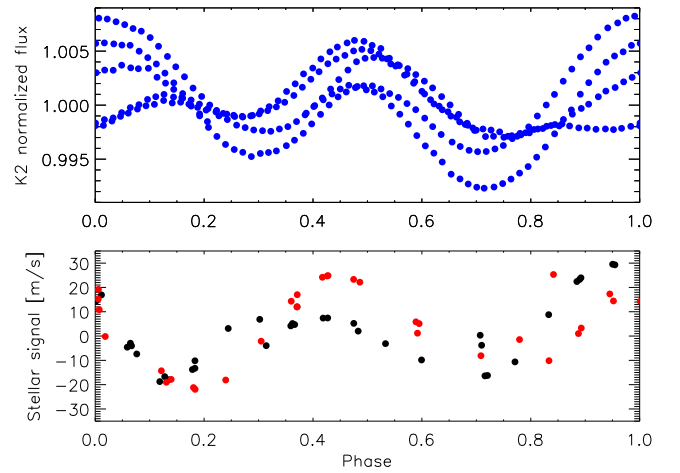


Fig. 10. K2 light curve (upper plot) and stellar activity component in the radial velocities (lower plot; TERRA data for the last two seasons). DRS data show a similar behaviour, folded at the stellar rotation period. The reference epoch corresponding to phase=0 is the same for both datasets. Light curve goes from May, 30th to Aug, 21th 2014 (K2 campaign C1). Spectroscopic data are distinguished according the observing season: black dots are used for data collected in 2017, red dots for those of 2018.

planet mass, or a higher mean-molecular-weight envelope with higher mass fraction. Both planets have escape velocity compatible with 20 km s⁻¹ within 1 σ , as marked in Fig. 11 by the dashed grey contour corresponding to $m_p/R_p=3$ (in Earth units). Within such a gravitational potential well and considering the young age (~ 1 Gyr) of the system, K2-36 c is consistent with

having 1-2% primordial H₂/He-dominated envelope at its corresponding equilibrium temperature (Fig. 12), or an even less massive H₂/He envelope if it has not cooled off from formation yet. Note the mass of K2-36 c is also less than 10 M_{\oplus} , the critical core mass required for run-away gas accretion (Rafikov 2006). This may explain why it did not acquire more gas and evolve into a gas giant.

Both methane CH₄ and ammonia NH₃ (Levi et al. 2013, 2014, 2017), and even H₂ itself (Soubiran & Militzer 2015), can be incorporated into the H₂O-reservoir during the initial formation stage, then out-gassed gradually to replenish a primary envelope, or form a secondary envelope, making K2-36 c a possible example of water-world (Zeng et al. *subm.*). It is possible that K2-36 b formed inside the snowline of the system (located at ~ 1.2 AU, see e.g. Mulders et al. 2015), and K2-36 c formed farther away beyond the snowline, building up a water-rich core and acquiring almost twice the mass of planet b. In fact, it is expected from cosmic element abundance that just beyond the snowline there is about equal mass available in solids from icy material (including methane clathrates and ammonia hydrates, which both contain H₂O) and from rocky material (including primarily Mg-silicates and (Fe,Ni)-metal-alloy), for planet to accrete from, while only rocky material would remain available in solids inside the snowline (Lewis 1972, 2004).

7.2. Comparing K2-36 to Kepler-36

An interesting comparison can be made between the K2-36 and Kepler-36 planetary systems. The two-planet system Kepler-36 was discussed by Carter et al. (2012), and then studied by Lopez & Fortney (2013), Quillen et al. (2013), Owen & Morton (2016), Bodenheimer et al. (2018). Kepler-36 is a 6.8 Gyr moderately-evolved Sun-like star, thus older than K2-36 and with very similar metallicity ([Fe/H]= -0.20 ± 0.6). Both Kepler-36 planets have very similar masses and radii compared to the corresponding K2-36 planets (see Fig. 11). The innermost planets b are consistent with Earth-like rocky composition (see Fig. 11). Kepler-36 c has a larger radius than that of K2-36 c, by adopting the more recent estimate of Fulton & Petigura (2018)⁷, and lower density. Kepler-36 planets have different densities and close orbits with periods near the 7:6 mean motion resonance. They both receive nearly half the insolation of K2-36 b, and have insolation difference much lower than that for K2-36 planets ($[S_b - S_c]_{\text{Kep-36}} \sim 45 S_{\oplus}$, and $[S_b - S_c]_{\text{K2-36}} \sim 440 S_{\oplus}$). They are both susceptible to H₂-He atmospheric escape considering their escape velocities and current equilibrium temperatures $T_{\text{eq}} \geq 900$ K. According to their measured densities, Kepler-36 b has lost any H₂-He gaseous envelope, while planet c still appears inflated and consistent with retaining an envelope of H₂/He with some percent in mass at the corresponding insolation. The near 7:6 mean motion resonance indicates that they have reached a stable orbital configuration. If photo evaporation has been driving atmospheric loss, its effects could have been steeply accelerated when the host star moved to the MS turn-off point, and it is still eroding the atmosphere of planet c. K2-36 and Kepler-36 planets could have formed in a similar environment, as suggested by the similar host star metallicity, and experienced a similar migration pathway.

⁷also Berger et al. (2018) provided a revised estimate for the radius of Kepler-36 c, $R = 3.689^{+0.165}_{-0.153}$, which is actually very similar to that of Carter et al. (2012). By adopting this value instead of that from Fulton & Petigura (2018), Kepler-36 c and K2-36 c have their radii compatible within one sigma.

7.3. Comparing K2-36 to WASP-107

Another interesting comparison is with WASP-107, a one-planet system characterized by a $0.9 R_{\text{Jup}}$ planet with a sub-Saturn mass, and with an orbital period very similar to that of K2-36 c (5.7 days), transiting a magnetic active K6V star with rotation period very similar to that of K2-36 (Anderson et al. 2017; Močnik et al. 2017). Transmission spectroscopy has recently enabled the detection of helium in a likely extended atmosphere of the planet, for which an erosion rate of 0.1-4% of the total mass per billion years has been calculated (Spake et al. 2018). WASP-107 b has an escape velocity ($\geq 20 \text{ km s}^{-1}$, or $m_p/R_p \sim 3.6$) and a surface equilibrium temperature ($T_{\text{eq}} \sim 740$ K) not very dissimilar to those of K2-36 c. If the sub-Neptune K2-36 c has H₂/He as components in its atmosphere, they could currently be escaping at a strong rate, despite intermediate-sized planets ($2-4 R_{\oplus}$) presumably having much less H₂/He volatiles than WASP-107 b, which would then be depleted faster. Based on this planet-to-planet comparison, K2-36 c may be considered suitable for future observations to search for evaporating helium. In fact, by assuming an atmosphere composed of 50% H₂ and 50% He, and the mass and radius estimated above for K2-36c, the atmospheric transmission spectrum signal of the planet can reach values up to about 160 ppm at five scale heights if it has a clear atmosphere. If the planet has a pure He atmosphere that extend 10 scale heights, it might present He absorption with an amplitude of 500 ppm.

8. Conclusions

We presented a characterization study of the K2-36 planetary system based on data collected with the HARPS-N spectrograph. According to their size, the planets K2-36 b and K2-36 c are located above and below the photo-evaporation valley, and their derived bulk densities ($\rho_b = 7.2^{+2.5}_{-2.1} \text{ g cm}^{-3}$, $\rho_c = 1.3^{+0.7}_{-0.5} \text{ g cm}^{-3}$) indicate that K2-36 b has an Earth-like rocky composition, while the Neptune/sub-Neptune size K2-36 c is likely surrounded by a significant gas envelope, not yet evaporated. K2-36 is an ideal laboratory to study the role of the photo-evaporation on the evolution of low-mass, close-in planets, especially for a relatively young (~ 1 Gyr) system, as we determined in this work, with the host star having high levels of magnetic activity.

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References

- Ambikasaran, S., Foreman-Mackey, D., Greengard, L., Hogg, D. W., & O’Neil, M. 2016, *IEEE Trans. Pattern Anal. Mach. Intell.*, 38, 252
- Anderson, D. R., Collier Cameron, A., Delrez, L., et al. 2017, *A&A*, 604, A110
- Andreasen, D. T., Sousa, S. G., Tsantaki, M., et al. 2017, *A&A*, 600, A69
- Anglada-Escudé, G. & Butler, R. P. 2012, *The Astrophysical Journal Supplement Series*, 200, 15
- Angus, R., Morton, T., Aigrain, S., Foreman-Mackey, D., & Rajpaul, V. 2018, *Monthly Notices of the Royal Astronomical Society*, 474, 2094
- Bensby, T., Feltzing, S., & Lundström, I. 2003, *A&A*, 410, 527
- Bensby, T., Feltzing, S., Lundström, I., & Ilyin, I. 2005, *A&A*, 433, 185
- Berger, T. A., Huber, D., Gaidos, E., & van Saders, J. L. 2018, *ApJ*, 866, 99
- Bodenheimer, P., Stevenson, D. J., Lissauer, J. J., & D’Angelo, G. 2018, *ApJ*, 868, 138
- Boisse, I., Bouchy, F., Hébrard, G., et al. 2011, *A&A*, 528, A4
- Brandt, T. D. & Huang, C. X. 2015, *The Astrophysical Journal*, 807, 24
- Buchhave, L. A., Bizzarro, M., Latham, D. W., et al. 2014, *Nature*, 509, 593
- Buchhave, L. A., Latham, D. W., Johansen, A., et al. 2012, *Nature*, 486, 375
- Buchner, J., Georgakakis, A., Nandra, K., et al. 2014, *A&A*, 564, A125
- Carter, J. A., Agol, E., Chaplin, W. J., et al. 2012, *Science*, 337, 556
- Castelli, F. & Kurucz, R. L. 2004, *ArXiv Astrophysics e-prints* [astro-ph/0405087]
- Choi, J., Dotter, A., Conroy, C., et al. 2016, *ApJ*, 823, 102
- Cloutier, R., Astudillo-Defru, N., Doyon, R., et al. 2017, *A&A*, 608, A35
- Cosentino, R., Lovis, C., Pepe, F., et al. 2014, in *Proc. SPIE*, Vol. 9147, Ground-based and Airborne Instrumentation for Astronomy V, 91478C
- Dai, F., Masuda, K., & Winn, J. N. 2018, *ApJ*, 864, L38
- Dotter, A. 2016, *ApJS*, 222, 8
- Dotter, A., Chaboyer, B., Jevremović, D., et al. 2008, *ApJS*, 178, 89
- Edelson, R. A. & Krolik, J. H. 1988, *ApJ*, 333, 646
- Feroz, F., Balan, S. T., & Hobson, M. P. 2011, *Monthly Notices of the Royal Astronomical Society*, 415, 3462
- Feroz, F., Hobson, M. P., Cameron, E., & Pettitt, A. N. 2013, *ArXiv e-prints* [arXiv:1306.2144]
- Figueira, P., Santos, N. C., Pepe, F., Lovis, C., & Nardetto, N. 2013, *A&A*, 557, A93
- Foreman-Mackey, D., Hogg, D. W., Lang, D., & Goodman, J. 2013, *PASP*, 125, 306
- Fulton, B. J. & Petigura, E. A. 2018, *AJ*, 156, 264
- Fulton, B. J., Petigura, E. A., Howard, A. W., et al. 2017, *AJ*, 154, 109
- Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2018, *A&A*, 616, A1
- Gaia Collaboration, Prusti, T., de Bruijne, J. H. J., et al. 2016, *A&A*, 595, A1
- Gelman, A. & Rubin, D. B. 1992, *Statistical Science*, 7, 457
- Gomes da Silva, J., Santos, N. C., Bonfils, X., et al. 2011, *A&A*, 534, A30
- Green, G. M., Schlafly, E. F., Finkbeiner, D., et al. 2018, *MNRAS*, 478, 651
- Haywood, R. D., Collier Cameron, A., Queloz, D., et al. 2014, *MNRAS*, 443, 2517
- Henden, A. A., Levine, S., Terrell, D., & Welch, D. L. 2015, in *American Astronomical Society Meeting Abstracts*, Vol. 225, *American Astronomical Society Meeting Abstracts*, 336.16
- Levi, A., Kenyon, S. J., Podolak, M., & Prialnik, D. 2017, *ApJ*, 839, 111
- Levi, A., Sasselov, D., & Podolak, M. 2013, *ApJ*, 769, 29
- Levi, A., Sasselov, D., & Podolak, M. 2014, *ApJ*, 792, 125
- Lewis, J. 2004, *Physics and Chemistry of the Solar System*, *International Geophysics* (Elsevier Science)
- Lewis, J. S. 1972, *Icarus*, 16, 241
- Lopez, E. D. & Fortney, J. J. 2013, *ApJ*, 776, 2
- Luger, R., Agol, E., Kruse, E., et al. 2016, *AJ*, 152, 100
- Malavolta, L., Borsato, L., Granata, V., et al. 2017a, *AJ*, 153, 224
- Malavolta, L., Lovis, C., Pepe, F., Sneden, C., & Udry, S. 2017b, *MNRAS*, 469, 3965
- Malavolta, L., Mayo, A. W., Loudon, T., et al. 2018, *AJ*, 155, 107
- Mamajek, E. E. & Hillenbrand, L. A. 2008, *ApJ*, 687, 1264
- Mann, A. W., Vanderburg, A., Rizzuto, A. C., et al. 2018, *The Astronomical Journal*, 155, 4
- Marcus, R. A., Stewart, S. T., Sasselov, D., & Hernquist, L. 2009, *The Astrophysical Journal Letters*, 700, L118
- Mayo, A. W., Vanderburg, A., Latham, D. W., et al. 2018, *AJ*, 155, 136
- Mortier, A., Sousa, S. G., Adibekyan, V. Z., Brandão, I. M., & Santos, N. C. 2014, *A&A*, 572, A95
- Morton, T. D. 2015, *isochrones: Stellar model grid package*, *Astrophysics Source Code Library*
- Močnik, T., Hellier, C., Anderson, D. R., Clark, B. J. M., & Southworth, J. 2017, *MNRAS*, 469, 1622
- Mulders, G. D., Ciesla, F. J., Min, M., & Pascucci, I. 2015, *The Astrophysical Journal*, 807, 9
- Owen, J. E. & Morton, T. D. 2016, *ApJ*, 819, L10
- Owen, J. E. & Wu, Y. 2013, *ApJ*, 775, 105
- Owen, J. E. & Wu, Y. 2017, *ApJ*, 847, 29
- Paxton, B., Bildsten, L., Dotter, A., et al. 2011, *ApJS*, 192, 3
- Quillen, A. C., Bodman, E., & Moore, A. 2013, *Monthly Notices of the Royal Astronomical Society*, 435, 2256
- Rafikov, R. R. 2006, *ApJ*, 648, 666
- Santerne, A., Díaz, R. F., Almenara, J.-M., et al. 2015, *MNRAS*, 451, 2337
- Santos, N. C., Mayor, M., Naef, D., et al. 2000, *A&A*, 361, 265
- Sestito, P. & Randich, S. 2005, *A&A*, 442, 615
- Sinukoff, E., Howard, A. W., Petigura, E. A., et al. 2016, *ApJ*, 827, 78
- Skrutskie, M. F., Cutri, R. M., Stiening, R., et al. 2006, *AJ*, 131, 1163
- Sneden, C. 1973, *ApJ*, 184, 839
- Soderblom, D. R., Jones, B. F., Stauffer, J. R., & Chaboyer, B. 1995, *AJ*, 110, 729
- Somers, G. & Pinsonneault, M. H. 2014, *ApJ*, 790, 72
- Soubiran, F. & Militzer, B. 2015, *ApJ*, 806, 228
- Sousa, S. G., Santos, N. C., Adibekyan, V., Delgado-Mena, E., & Israelian, G. 2015, *A&A*, 577, A67
- Spake, J. J., Sing, D. K., Evans, T. M., et al. 2018, *Nature*, 557, 68
- Van Eylen, V., Agentoft, C., Lundkvist, M. S., et al. 2018, *MNRAS*, 479, 4786
- Vanderburg, A. & Johnson, J. A. 2014, *PASP*, 126, 948
- Vanderburg, A., Latham, D. W., Buchhave, L. A., et al. 2016, *ApJS*, 222, 14
- Zechmeister, M. & Kürster, M. 2009, *A&A*, 496, 577
- Zeng, L., Jacobsen, S. B., Hyung, E., et al. 2017, in *Lunar and Planetary Science Conference*, Vol. 48, *Lunar and Planetary Science Conference*, 1576
- Zeng, L., Jacobsen, S. B., & Sasselov, D. D. 2017b, *Research Notes of the AAS*, 1, 32

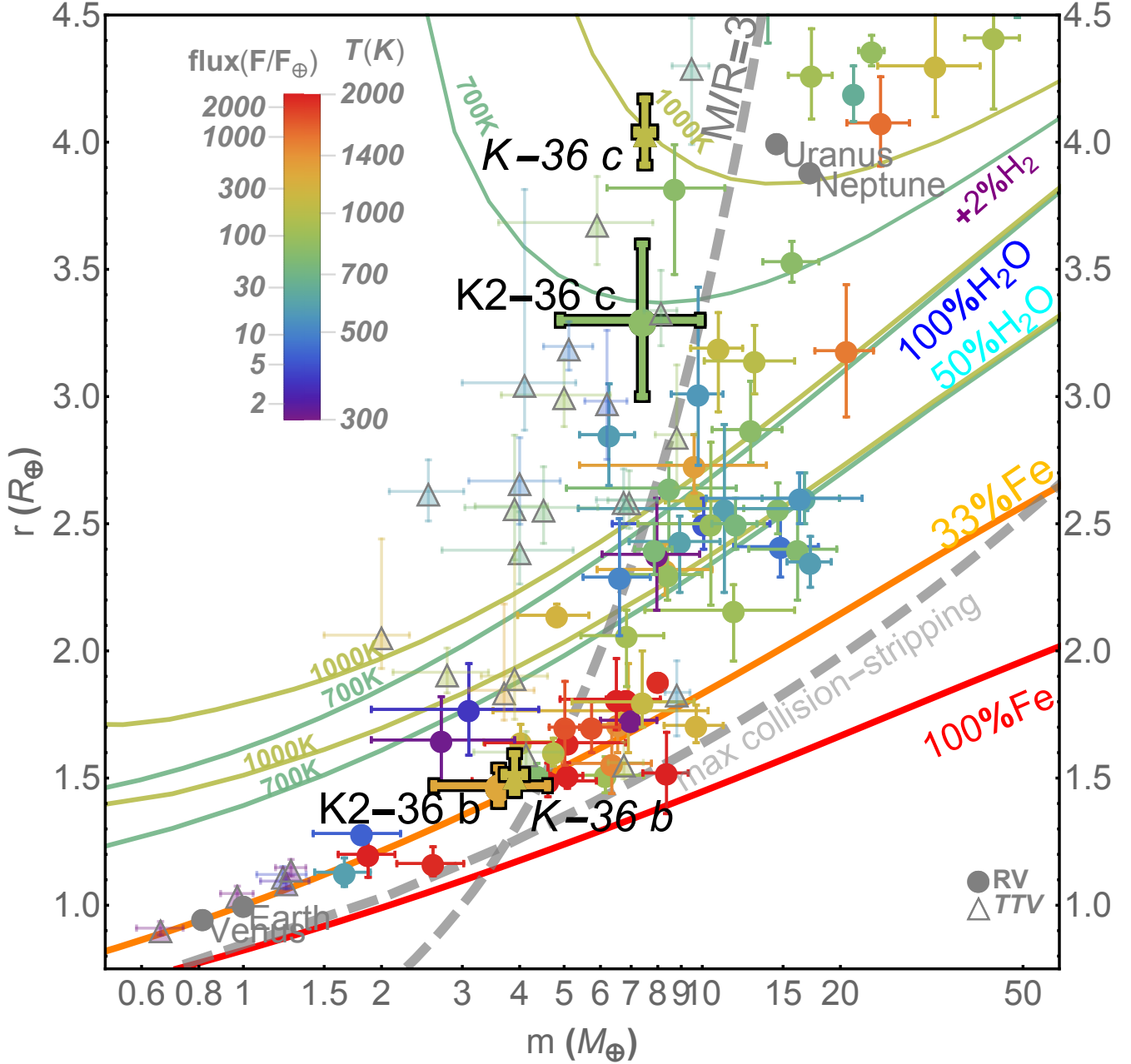


Fig. 11. Mass-radius diagram for exoplanets with densities derived with precision better than 35% (data updated up to 2018 09 14). The planets with masses determined by the radial-velocity method are labelled as circles, and the ones with masses determined by the transit-timing-variation method are labelled as triangles. The color of the data points denotes stellar insolation (see legend in the upper left corner) in the Earth units (expressed as either the amount of stellar bolometric radiation reaching a given area at their orbital distances, assuming negligible orbital eccentricities, normalized to the Earth’s value or surface equilibrium temperatures assuming Earth-like albedo). The plotted masses of the K2-36 planets are those derived from the GP analysis of the TERRA RV dataset. K2-36 planets are represented by filled circles in bold and explicitly labelled. Overplotted are the planets of the Kepler-36 system (filled triangles in bold labelled as K-36), showing an analogy with the K2-36 system as discussed in the text. Two sets of H_2O mass-radius theoretical curves (blue - 100 mass% H_2O , cyan - 50 mass% H_2O ; cores consist of rock and H_2O ice in 1:1 proportion by mass) are calculated for an isothermal fluid/steam envelope at temperatures 700 K and 1000 K, sitting on top of ice VII-layer at the appropriate melting pressure. A set of mass-radius curves (upper portion of the diagram) is calculated for the same temperatures assuming the addition of an isothermal H_2 -envelope (2% mass) to the top of the 50 % mass H_2O -rich cores. The dashed curve labelled *maximum collisional stripping* corresponds to the lower bound in radius or upper bound in density that a giant impact can yield for a given planet mass (Marcus et al. 2009). The dashed curve labelled $M/R=3$ corresponds to the contour on the mass-radius diagram where planet mass dividing by planet radius equals 3 in Earth units. It marks the equi-gravitational-potential for the surfaces of planets. Planets residing to the left of this curve are susceptible to atmospheric escape of H_2 and Helium over a billion years at their current equilibrium temperatures.

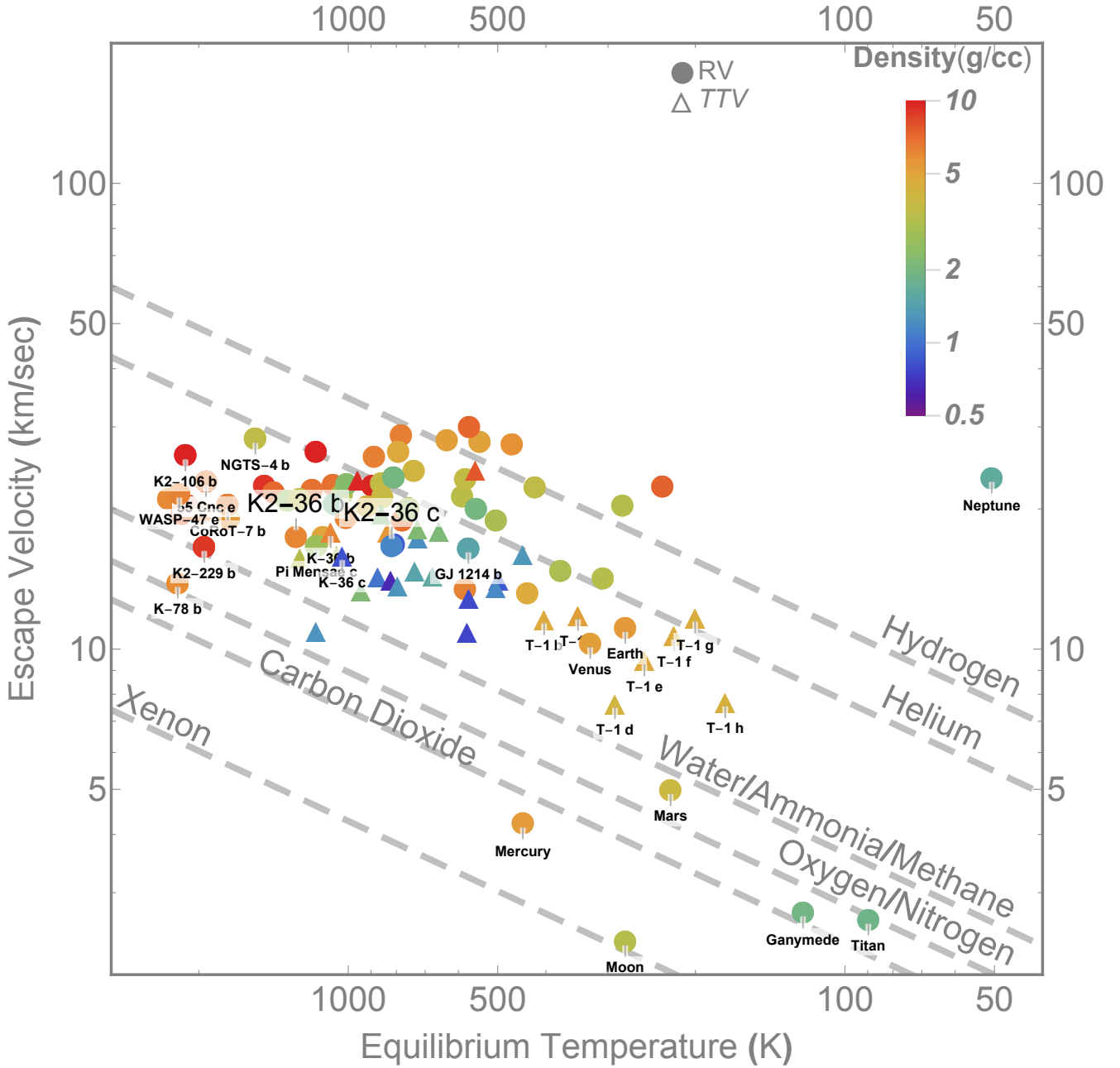


Fig. 12. Empirical relations that describe the dependence of the atmospheric composition in exoplanets from their escape velocities and equilibrium temperatures. The plot shows the location of the K2-36 planets in the context of some notable small-size exoplanets ($R < 4R_{\oplus}$) with measured masses (K :- Kepler planets; T -1: Trappist-1 planets). A color code is used to distinguish the planets on the basis of their bulk density.

Table 5. Radial velocities of K2-36 extracted from the 81 HARPS-N spectra analyzed in this work (the full dataset is available on-line via CDS).

Time (BJD _{TDB} -2 400000)	DRS		TERRA	
	Radial velocity (m s ⁻¹)	σ_{RV} (m s ⁻¹)	Radial velocity (m s ⁻¹)	σ_{RV} (m s ⁻¹)
57047.651272	13630.93	4.44	-9.07	3.55
57048.697294	13620.53	4.76	-21.54	3.20
...