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1 **Central-Eastern China persistent heat waves: Evaluation of the AMIP**

2 **models**

3 N. Freychet\*

4 *School of Geosciences, University of Edinburgh, Crew Building, The King's Buildings,*  
5 *Edinburgh EH9 3FF, UK*

6 S. F. B. Tett, G. C. Hegerl

7 *School of Geosciences, University of Edinburgh, Crew Building, The King's Buildings,*  
8 *Edinburgh EH9 3FF, UK*

9 J. Wang

10 *Institute of Atmospheric Physics, Chinese Academy of Sciences, Beijing, China*

11 \*Corresponding author address: Nicolas Freychet, Crew Building, The King's Buildings, Alexan-

12 der Crum Brown Road, Edinburgh EH9 3FF, UK

13 E-mail: nicolas.freychet@ed.ac.uk

## ABSTRACT

14 Large scale and persistent heat waves affecting Central-Eastern China are in-  
15 vestigated in 40 different simulations of sea surface temperature driven global  
16 atmospheric models. The different models are compared with results from  
17 reanalysis and ground station datasets. It is found that the dynamics of heat  
18 wave events is well reproduced by the models. However, they tend to pro-  
19 duce too persistent heat wave events (lasting more than 20 days) and several  
20 hypothesis were tested to explain this bias. The daily variability of the tem-  
21 peratures or the seasonal signal did not explain the persistence. However,  
22 interannual variability of the temperatures in the models, and especially the  
23 sharp transition in the mid-90s, has a large impact on the duration of heat  
24 waves. A filtering method was applied to select the models closest to the ob-  
25 servations in terms of events persistence. The selected models do not show  
26 significant difference with the other models for the long term trends. Thus,  
27 the bias on the duration of the events do not impact the reliability of the model  
28 positive trends, mainly controlled by the changes in mean temperatures.

## 1. Introduction

Large scale and persistent heat waves (HW) over East China have a large environmental and socio-economic impact (e.g. Luber and McGeehin 2008; Wang et al. 2015) and have been the focus of many studies (see for example Perkins (2015) and Lu and Chen (2016) for a review). During the past few decades, the frequency of these events have been found to increase (Wei and Chen 2011; Wang and Fu 2013; Ren et al. 2005, 2016; Zhou and Wang 2016). But this trend is not always consistent and can vary in some regions (Yan et al. 2011b; Ding and Qian 2011; Dong and Huang 2015). Freychet et al. (2017) showed that, for large scale heat waves, this trend is mainly due to increase in the mean temperature. This study also showed that HW are related to strong mid-troposphere positive anomaly and to an enhanced heat and moisture transport in the lower troposphere. On the other hand, Luo and Lau (2017) indicated dry conditions associated with HW over Southern China. Other works have also pointed out the role of the reduction in the snow cover over the western Tibetan Plateau (e.g. Wu et al. 2012; Sun et al. 2014) and of the Eurasian teleconnection pattern (Wang et al. 2016a). Thus, different processes are involved in the formation and magnitude of the HW events.

Adaptation to such events for the next few decades is important and was investigated by the Working group II of the IPCC5 Fifth Assessment (IPCC 2014, Kripalani et al. (2007)). Many studies, relying on global climate model projections such as the CMIP5 (Coupled Model Inter-comparison Project Phase 5) ensemble, indicate an increase in HW events for the future decades in terms of frequency, intensity and duration (e.g. Guo et al. 2017). As many different models are used for such ensemble experiments, the confidence on these projections can be questioned, especially for extreme or rare events (Freychet et al. 2015, 2016). The main objective of this study is to conduct an evaluation of the AMIP models for persistent and large scale heat waves over Central-

52 Eastern China (CEC) and use these evaluated models to estimate the changing risk of such events.  
53 The region is chosen to be close to Lin et al. (2015) definition. It is heavily populated and extreme  
54 temperature events can impact a large population. Urbanisation is also important and can locally  
55 impact the temperatures. However, this aspect is not included in the current global climate models  
56 and should not change the results of this study. It must also be noted that the results presented in  
57 this study are specific to the definition of the region. Other area could lead to different findings  
58 depending on the dynamics (e.g. Wang et al. 2016b). Even if using realistic SST forcing, AMIP  
59 simulations are not reanalyses, thus it is not expected that they can reproduce the same heat waves  
60 at the same dates. In this study only statistical approaches are considered, different from a case  
61 analysis such as Luo and Lau (2017) for instance.

62 Our focus is on the atmospheric component of the climate models and the evaluation is based  
63 on two different reference datasets, defined in Section 2. Another ensemble of 15 members of the  
64 Met Office HadGEM3-GA6-N216 model (Walters et al. 2017) is also used to examine the intra-  
65 variability of the models. The study investigates if the AMIP ensemble is consistent in terms of  
66 dynamics (Section 3) and if the models can reproduce HW signals in the observational datasets  
67 (Section 4). A major question is to verify that the models are consistent in terms of risk change.  
68 This point is addressed in section 5, before concluding in Section 6.

## 69 **2. Data and heat waves definition**

### 70 *a. Data*

#### 71 1) REANALYSIS AND OBSERVATIONS

72 Maximum and minimum temperatures (Tmax and Tmin) and atmospheric circulation variables  
73 from ERA Interim reanalysis (ERA-Interim, Dee et al. (2011)) are used as a reference for this study. Daily

74 data are extracted at 0.75 degree resolution, and the 1979-2010 period is used. Homogenized  
75 ground station observations of temperature (OBS, Li and Yan (2009)) are also used. OBS are first  
76 regridded on the ERAI grid (shown in Fig.1a-b for Tmax) by averaging, for each grid point, the  
77 corresponding available data from OBS. If no OBS data is available for a grid point, then it is  
78 masked.

79 A significant bias exists between ERAI and OBS (not show). ERAI is too cold, especially over  
80 the central and Southern China. Part of this bias may be related to the urban effect that can impact  
81 locally the ground station temperatures (Yan et al. 2011a). Another part of this bias may be due  
82 to elevation effect, that is directly recorded in OBS but could be missing in ERAI due to the  
83 resolution. A modification is applied to OBS so that it is more consistent with ERAI. To do so, a  
84 linear temperature gradient coefficient ( $C_Z = 0.6\text{K}/100\text{m}$ ) is combined with the difference between  
85 the elevation of each station ( $Z_{OBS}$ ) and the elevation of the co-located ERAI grid point ( $Z_{ERAI}$ )  
86 to obtain an adjustment term ( $dT$ ) equivalent to:  $dT = C_Z \times (Z_{OBS} - Z_{ERAI})$ . This term is then  
87 applied to the temperatures at the station. The station observations are then regridded on the ERAI  
88 grid. Also note that the choice of a fixed coefficient  $C_Z$  is arbitrary and can vary significantly  
89 according to the land type (Li et al. 2013). Thus the adjustment method employed here should not  
90 be considered as perfect.

91 After adjusting the elevation effect, the differences between ERAI and OBS are reduced (Fig.1c)  
92 compared to the raw data differences (not shown). This indicates that part of the differences  
93 between reanalysis and observation are due to the fact they represent temperatures at different  
94 elevations, stations being more often located in the valley while reanalysis grid point correspond  
95 to the mean elevation of the region. Other processes impacting temperatures at a very local scale  
96 such as aerosols or urban effect (e.g. Gong and Wang 2002; Heisler and Brazel 2010; Yan et al.  
97 2011a) could explain the remaining differences. Results for Tmin show lower biases compared to

98 Tmax, and the elevation correction also reduces the differences between ERAI and OBS (Fig.1f).  
99 Hereafter, OBS will refer to the regrided ground station observation, after elevation correction.  
100 Moreover, the term “observations” will be used to include both ERAI and OBS, when comparing  
101 the results with the models.

## 102 2) MODEL DATA

103 Daily data from 1979 to 2008 from an ensemble of 40 members of the AMIP multi-model  
104 ensemble (AMIP) is investigated. As some models have several members, the total of independent  
105 models is 21 (Table ??). AMIP models correspond to the same CMIP5 models but are forced by  
106 prescribed sea surface temperature (SST) during the historical period, removing uncertainties due  
107 to ocean models. The study does not investigate individual performance of each model. However,  
108 for each diagnostic performed, the list of the five models with the lowest and the highest scores is  
109 given in Table ?. The user may refer to this table to see individual model performances.

110 Another ensemble of 15 members from the Met Office HadGEM3-GA6-N216 atmospheric  
111 model is used (N216). It also follows an AMIP-like experiment, i.e. forced by prescribed SST  
112 during the historical period, and data are extracted for the same period. The N216 ensemble is  
113 mainly used to estimate the internal variability and uncertainties. It runs from 1960 to 2013, but  
114 the same period (1979-2008) as the AMIP is used for analysis.

### 115 *b. Heat waves definition and computation of the composites*

#### 116 1) HEAT WAVES DEFINITION

117 There are many ways to define HW events and trends can be different depending on the index  
118 definition (You et al. 2016). Here we focus on large scale and persistent events, and the definition  
119 of HW used in the study follows that of Freychet et al. (2017). Daily Tmax and Tmin are both

120 averaged over the Central-Eastern China (CEC) region (105E-125E, 30N-40N), and the 90<sup>th</sup> per-  
121 centile is computed for each temperature, using the extended summer period (May-September) of  
122 each year. A warm day is defined as when both Tmax and Tmin are above their respective 90%  
123 values on the same calendar day. A HW event is defined when at least 5 consecutive days are  
124 warm days. Note that this methodology is applied independently to each dataset (ERA-Interim, OBS, and  
125 each model member) to define their own 90<sup>th</sup> percentile removing mean temperature bias.

126 As the main objective of this study is to focus on the most threatening events for society, HW  
127 highlights the warmest events in an absolute way. As the temperatures are warmer during mid  
128 July, it is expected that most of the HW events will be identified during this period too. Thus,  
129 HW events can be seen as a phenomenon that amplifies the seasonal transition and increases the  
130 temperature during the warmest period. It also implies that HW events are related to the seasonal  
131 transition. This point will be further discussed in the Section 4.

## 132 2) COMPOSITES

133 To study the atmospheric circulation during the HW, a composite method is applied to an atmo-  
134 spheric variable labelled X. When a day d is identified as part of a HW event, the corresponding  
135 variable  $X_d$  at time d is extracted, and the climatology (as a 5-days running mean) of X at the same  
136 calendar day ( $X_{d-clim}$ ) is removed. To remove any long term trend and variability and to focus on  
137 anomalies due to the HW, the difference between the annual mean around the time d ( $X_{d-ann}$ ) and  
138 the mean 1979-2008 climatology of X ( $X_{clim}$ ) is also removed. Thus, only the anomaly ( $X_d$ ) due  
139 to the HW remains.

$$X_d = X_d - X_{d-clim} - (X_{d-ann} - X_{clim}) \quad (1)$$

140 The composite of X corresponds to the averaging of the anomalies from all the HW days during  
141 the studied period (see Appendix for a schematic view).



### 142 3. Heat Wave Dynamics

143 It is first important to verify if the model can reproduce the observed dynamics of events. For  
144 that, a composite analysis is used, as described in Section 2.

145 The dynamical processes correlated with persistent HW events have been described in details in  
146 Freychet et al. (2017). Here we verify that the models can reproduce the composite ERAI signals.  
147 The ensemble mean of the AMIP models can reproduce the observed dynamical patterns (Fig.2).  
148 A mid-troposphere high pressure (Z500) along with a subsidence anomaly (W500) and northward  
149 shift of the subtropical jet (U200) leads to an increase in surface solar radiation (SSR) and favour  
150 higher Tmax. The specific humidity (S.Hum.) is also higher than usual during these events and is  
151 important to reduce the night time cooling and keep Tmin higher. Finally, the low level circulation  
152 (SLP) pattern corresponds to the development of a meridional cell anomaly with an upward motion  
153 over the the North-East of the CEC region. This anomaly has been hypothesised to lead to return  
154 wind from the North and to increase the heat convergence over CEC during the HW (Freychet  
155 et al. 2017).

156 The individual member performances are tested (Fig.3a,b). Most of the models are close to the  
157 reference (ERAI) in terms of correlation (between 0.7 and 0.9). The scatter of the N216 members,  
158 especially for the SLP, indicates a high intra-model variability. Poor results may be due to a too  
159 strong control of the seasonal transition in some members instead of an anomaly of the circulation  
160 (i.e. HW events may be triggered by an overall large increase in temperature during the peak of the  
161 summer). The ensemble mean is overall consistent with ERAI in terms of patterns (correlation)  
162 but tend to have a weaker signal due to the ensemble averaging. The dynamical signal is tested  
163 furthermore with a lag-composite analysis (Freychet et al. 2017), from 10 days before to 10 days  
164 after the HW events. The anomalies are averaged over the [105E-125E, 30N-40N] region for Z500,

165 and over the [115E-140E, 40N-50N] region for the SLP. The evolutions of these anomalies are  
166 compared with ERAI results and displayed in Fig.3c,d. The ensemble mean is able to reproduce  
167 the signal with a good correlation (0.8 for Z500 and 0.9 for SLP), but individual results are more  
168 scattered. Interestingly, the ensemble is more consistent for the SLP, indicating that the low-level  
169 dynamical response in the models is a robust result. Other variables are also tested (surface solar  
170 radiation, 500hPa vertical wind and 850hPa specific humidity, not shown). Results are overall  
171 similar to findings in Fig.3: the ensemble mean is consistent with ERAI, but individual models  
172 can have weaker performances.

173 Overall the AMIP ensemble is able to reproduce the main spatial and temporal evolutions of the  
174 dynamical patterns of HW events, even if some individual members are less consistent.

#### 175 **4. Representation of heat waves in the AMIP models**

176 This section investigates if models can reproduce HW events compared to observations, in terms  
177 of number and duration during the historical period (Section a and b). Following this, the possi-  
178 ble reasons for the model differences are explored. Finally, Section d discusses the interannual  
179 variability of the events.

##### 180 *a. Estimation of heat waves events in models*

181 The difference between the reanalysis and observations shows that the estimated number of  
182 observed heat waves has considerable dataset uncertainty (Fig.4a). For example, Fig.4 of Luo and  
183 Lau (2017) shows another example of different heat wave number and intensity estimates (over  
184 South China) based on different datasets (reanalysis or weather station). High variability is also  
185 seen between the different models or even between different simulations of a same model. Indeed,  
186 when looking at the different members of the N216 ensemble, the number of days may vary from

187 30 to 60, and the standard deviation of N216 ensemble is about the same order as the observed  
188 uncertainty. Thus, the statistics on these events are very sensitive to the sampling processes and  
189 both modelled or observed events must be considered within a margin of error. The fact that these  
190 events are rare and the period is limited suggests that part of the difference may be simply due to  
191 the variability. Considering, the actual number of heat waves per year (Fig.4b), results are more  
192 consistent between observations but the AMIP models still tend to produce too many events and  
193 have a large scatter.

194 To verify that the differences between models and observations are not an artefact due to an  
195 incorrect seasonal signal, the seasonal climatology is corrected in each model and OBS, using  
196 the seasonal climatology of ERAI. To do so, the 31-day smoothed climatology is removed from  
197 the simulated temperatures (or OBS), and the 31-day smoothed climatology from ERAI is added.  
198 Then heat waves are computed using the corrected data (Fig.4c and d). The total number of heat  
199 wave days in the AMIP ensemble is not improved by such methodology. Interestingly, the number  
200 of events in OBS is enhanced, increasing the uncertainties in the observations. The seasonal  
201 signal may influence the production of heat waves, and with the same seasonal climatology the  
202 reanalysis or ground stations have a different estimation of the number of events. Consequently,  
203 the uncertainties on the true estimate is larger and models are more consistent with observations.  
204 As correcting the seasonal climatology does not improve the results, the actual temperatures are  
205 used from hereon.

#### 206 *b. Event Persistence*

207 To investigate in more detail the reasons for the overestimation of the number of heat wave days,  
208 the persistence of the warm events is displayed in Fig.5 (a warm event being a combination of  
209 both Tmin and Tmax above their respective threshold during a same day). As defined before, an

210 event is defined as a heat wave if it lasts at least 5 days, but in Fig.5 shorter events (1 to 4 days)  
211 are also plotted to obtain a full spectrum of the warm events persistence. For each models, results  
212 are displayed as a percentage relative to the total number of warm days in this same model (or  
213 observation). For instance, if a model has 12 warm events lasting for 2 days, and in total it has 300  
214 days of warm events (all length grouped), then it would have 8% of events with a persistence of  
215 2 days. The mean persistence of the events of more than 5 days is also displayed for OBS, ERAI  
216 each AMIP and N216 members.

217 ERAI is, overall, consistent with the station data (Fig.5), though there are more short events in  
218 ERAI (4 days), and less long lasting heat waves than in the gridded station observations. The max-  
219 imum heatwave length in ERAI is 9 days, while in OBS it can reach 12 days, and the percentage  
220 of long lasting events is larger in OBS than in ERAI. However, this differences are relatively small  
221 compared to the differences with the models, and could be due to local effects (e.g. urban effect)  
222 not resolved in ERAI. Many AMIP members produce very persistent events that can last for 20  
223 days or more. The mean duration is found to be 6 days in ERAI and 8 days in OBS, and ranges  
224 from 5 to 11 days in the models. Thus the mean duration may be considered as realistic in some  
225 models, but specific longer events could be problematic and some models are outside the range of  
226 the observational uncertainties. Possible reasons for such behaviour are explored below.

### 227 *c. Hypothesis for the over-persistent heat waves*

228 Three main hypothesis are investigated in this section: the variability of the models, the vari-  
229 ability of the temperatures in the models, and the influence of the seasonal signal.

## 230 1) INTERNAL VARIABILITY AND OBSERVATION ERROR

231 Even if long persistent HW events (more than 10 day events) are observed in many simulations,  
232 considerable internal variability exists in the models, illustrated in Fig.6 for the N216 simulations.  
233 Some members can simulate a reasonable ratio of long persistent events whereas other simulations  
234 produce mostly long lasting events. These differences are also observed in the AMIP ensemble  
235 (not shown). Thus, the persistence of the events cannot be attributed to a systematic bias of a  
236 model, but may be linked to the internal variability of the model.

237 A crude estimation of the realistic range of the maximum persistence is made, based on the  
238 observations mean ( $\mu_{obs}=10.5$  days) and differences ( $\sigma_{obs}=3$  days) and on the N216 standard devi-  
239 ation ( $\sigma_{N216}=5.1$  days). Considering that the uncertainties are simply independent and cumulative,  
240 the maximum realistic persistence could be considered as:

$$\mu_{obs} + \sqrt{(\sigma_{obs}^2 + \frac{\sigma_{N216}^2}{N})} \quad (2)$$

241 with N the number of members (for example 15 for the N216 ensemble mean). The result would  
242 be 14 days for the N216 ensemble mean and 16.5 days for a single member. It means that an event  
243 persistence of 16.5 days in a single member can be considered as reasonable, given the range  
244 of the intra-model variability and observation uncertainties. This explains part of the differences  
245 between the models and the observation, but not the most persistent events. It is still important to  
246 understand if a specific factor controls the variability of the persistence, or could be attributed to  
247 chaos. Thus, other factors are investigated below.

## 248 2) TEMPERATURE VARIABILITY

249 The daily variability of the temperatures is an important aspect that can explain over-persistent  
250 warm events. Indeed, if a model has a systematic too low daily variability of the temperature (thus

251 with temperatures more stable from one day to another), it may lead to more stable temperatures  
252 and thus longer events. This hypothesis is investigated in Fig.7 (a,b). The variability is computed  
253 by removing the 3-days running mean and taking the standard deviation of the anomaly (for Tmin  
254 and Tmax separately). No clear relationship can be found between the variability of Tmin and the  
255 HW persistence. But many models producing long HW events (red circles) tend to correspond  
256 to weaker variability of Tmax (with an overall correlation of -0.61). Thus, a too weak daily  
257 variability of the maximum temperature in the models could lead to more systematic long HW  
258 events. However, this signal is not observed for N216, and the models with a similar (or lower)  
259 observations variability have too many long heat waves. Thus the biases cannot be explained by  
260 variability alone, though it has an impact on the duration of the events in the models.

### 261 3) EFFECT OF THE SEASONAL CYCLE

262 The amplitude of the summer range (i.e. the difference between the coldest and warmest period  
263 of the summer based on the 5-day smoothed climatology) could also impact the HW persistence.  
264 Too large a summer range would lead to systematically too persistent heat waves, as the warmest  
265 period would be above the threshold used to detect HW. This hypothesis is tested in Fig.7 (c,d).  
266 The summer ranges for Tmax and Tmin correspond to the difference between their highest and  
267 their lowest magnitudes respectively (based on the daily climatology smoothed by a 5 days running  
268 mean). Again, no clear relationship is found between this signal and the persistence of HW,  
269 either in terms of inter- (AMIP ensemble) or intra-model (N216 ensemble) variability. However,  
270 it is noticeable that all the members (AMIP and N216) have a larger seasonal range for Tmax,  
271 compared to ERAI.

272 As the simulated summer range is generally larger than observations, persistence is analysed  
273 after correcting the seasonal climatology as explained in Section 4. It is clear that even after

274 correcting the seasonal climatology, differences in the persistence (Fig.8a.) are still noticeable for  
275 both AMIP and N216.

276 A last case is to consider heat waves events in terms of anomalies, by removing the seasonal  
277 climatology from the temperatures before computing HW events. This correspond to the method-  
278 ology described before to correct the climatology, except that the ERAI climatology is not added  
279 after removing the model climatology. In this case the events are independent from the seasonal  
280 signal. As expected, the events tend to be shorter (Fig.8b), because they are not amplified by the  
281 seasonal transition. There is a better agreement between EARI and OBS, but the models still tend  
282 to produce to many long lasting events.

283 Errors in the seasonal cycle cannot on their own explain the persistence of simulated events.  
284 However, the influence of the seasonal signal in the models is larger than in OBS or ERAI. For  
285 the models, the persistence of high temperatures may be partly due to an anomalous high seasonal  
286 range rather than by circulation anomalies, or a combination of both. There are also large uncer-  
287 tainties associated with both intra-model variability and differences between observations. These  
288 results also indicate that statistics on HW events are highly dependent on the choice of the index  
289 (absolute or anomalies), in accordance with You et al. (2016).

290 Next it will be investigated if the models can still reproduce the historical trends of the events  
291 despite their bias.

#### 292 *d. Evolution and trend of the heat waves*

293 ERAI and OBS have a good agreement in terms of inter-annual evolution of HW events (Fig.9).  
294 They both have a clear decadal oscillation and an overall positive trend. Models tend to reproduce  
295 the positive trend, but the decadal oscillation is less clear (though it is still visible), especially for  
296 the N216 ensemble. A major transition occurs between the mid-90s and 2000, with a peak just

297 after 2000. In the observations this transition is also visible, but in the models it is particularly  
298 sharp.

299 Fig.10 shows the same evolution but for long HW events only (more than 10 days). In the ob-  
300 servations, the two peaks (corresponding to the few long events in OBS) are concurrent with the  
301 higher phases of the decadal signal. This indicates that the persistence of the events can be influ-  
302 enced by the decadal variability of temperatures. In the models, the signal is mostly controlled by  
303 the mid-90s transition, with most of the long HW occurring after this transition. This is also visi-  
304 ble for the signal without running mean where the interannual variability is larger (Fig.10b). Two  
305 periods are clearly visible in the models (before 1995 and after 2000), with a transition between  
306 the two and a peak just after 2000. The influence of the interannual variations of the tempera-  
307 tures is tested furthermore. The HW events and their persistence are computed after removing the  
308 yearly summer mean temperatures from the signals without the seasonal climatology (as described  
309 in Section 3). Doing so, the persistence is reduced (not shown), though the impact is not as large  
310 as the seasonal signal. This indicates that the interannual variability of the temperatures can also  
311 influence the length of the HW events.

312 Finally, it is noticeable that both models and observations indicate a steady increase in the num-  
313 ber of HW (days or events per year), even if models reproduce less clearly the observed decadal  
314 oscillations. This is not surprising given the ensemble averaging that tend to reduce the variabil-  
315 ity. When computing HW events after removing both the interannual summer means, the signal  
316 is more constant (Fig.10c) in the models. This clearly indicates that the trend in the models is  
317 mainly controlled by the trends in the mean temperatures, which is consistent with Freychet et al.  
318 (2017). An interesting difference between observations and models is the clear decadal oscillation  
319 still visible in ERAI and OBS but not in the models (though their signal tends to oscillate too). It  
320 may indicate again some missing chaos in the model ensemble due to averaging.



## 5. Risk and confidence in the models trends

Fig.11a,b compares the AMIP ensemble probability distribution for the number of HW days or events between the first and the last decade (1980-1990 and 1998-2008 respectively) of the investigated period. Both distributions shift to a higher number of days or events between the two periods, indicating an increased risk of HW days, but the ensemble spread is also large. Similar results are found for the N216 ensemble (Fig.11c,d). Interestingly, the most recent period (2009-2013) does not show a significant difference. Thus the major increase in the heat waves events occurred during the mid-90s transition. It may be due to a change in aerosols emission and transport during these years (and a high sensitivity of the models to these changes), but this hypothesis could be investigated in future work.

In previous sections, it has been shown that the signals in the AMIP simulations is often biased, especially in terms of the length of the events they produce. Thus, the reliability of the trend of heat waves in the AMIP (and the long-term forecasts) can be questioned. An approach to improve the confidence of the ensemble (and its projection) is to filter the best models based on their consistency with observations and reanalysis results. In the following, a filtering method is applied, based on the statistics of heat wave events (number of events or days). Two sources of error are considered: the observational error (estimated from the difference between ERAI and OBS) and the internal variability of the models (estimated with the N216 ensemble spread). This gives a margin of uncertainties within which the differences between a model and the observations can be considered as reasonable.

As the biases are observed on the number and the duration of HW events, two variables are considered to evaluate the models performance: the total number of heat wave days per years ( $HW_{d/y}$ ) and the ratio of days included in long heat waves (more than 10 days) compared to the

344 total number of heat wave days ( $HWL_{rat}$ ). The reference values and associated uncertainties are  
 345 computed using both OBS and ERAI, using the following formula:

$$\mu_{obs} = \frac{OBS + ERAI}{2} \quad (3)$$

$$\sigma_{obs} = |OBS - ERAI| \quad (4)$$

347 with  $\mu_{obs}$  the mean,  $\sigma_{obs}$  the error and  $||$  symbols denoting the absolute value. In a similar way,  
 348 the mean of a model ( $\mu_{mod}$ ) is computed by averaging, if necessary, the results from each of its  
 349 members. The model error is estimated from the N216 ensemble ( $\sigma_{mod}$ ), as it has the largest  
 350 number of members, and corresponds to the standard deviation of the N216 ensemble. This error  
 351 is particularly important as it is common to have only one member for a model, and thus a large  
 352 uncertainty comes from the sampling process. As shown before, different members may have very  
 353 different results, and thus the model cannot be evaluated correctly with a single member. A model  
 354 results termed good when its difference with the observation is lower than the total error, i.e.:

$$Criteria : |\mu_{mod} - \mu_{obs}| \leq \sqrt{\sigma_{obs}^2 + \frac{\sigma_{mod}^2}{N}} \quad (5)$$

355 where  $N$  is the number of ensemble members. When several members are available for one  
 356 model, only the ensemble mean is evaluated (and all members are considered retained or excluded  
 357 based on the result on the ensemble mean). The criteria is verified for both variables ( $HW_{d/y}$   
 358 and  $HWL_{rat}$ ) and a model is termed good if it meets both criterion. The linear trends of the  
 359 models is displayed in Fig.12. Even if the selection criteria is sharp many models are considered  
 360 as good. However, the ensemble of good models does not show a significant difference compared  
 361 to the ensemble mean of other models. Both groups indicate a positive trend, either in terms  
 362 of events (about 0.25 events per decade) or days (about 2 HW days per decade). These results

363 are consistent with ERAI and OBS, when considering the margin of error (ensemble scatter and  
364 difference between ERAI and OBS), especially in terms of HW events. The weaker trend in the  
365 observation may be related to a stronger decadal variability while the models have a more steady  
366 increase (Figure 9). Selecting only the best models does not significantly affect the results in this  
367 case, thus the results from the overall ensemble (in terms of trends) can be considered as reliable.

## 368 **6. Concluding remarks**

369 The representation of persistent large-scale heat waves over Central-Eastern China have been  
370 investigated in 40 AMIP members and compared with the results from ground stations and ERA  
371 Interim reanalysis. An ensemble of 15 members of the HadGEM3-A-N216 model was used to  
372 estimate the intra-model variability.

373 It was found that models tend to overestimate the number of heat wave days during the historical  
374 period, mostly because the events are too persistent. In the observations and reanalysis, the length  
375 of the events reaches a maximum of 12 or 9 days respectively, while in the models it can be more  
376 than 20 days.

377 Possible reasons to explain this bias were investigated: the magnitude of the summer range  
378 between the coldest and warmest temperatures, the climatology and the daily variability of the  
379 temperatures. None of these possible factors showed a significant relationship with the persistence  
380 of the heat waves, though it seems that the models are particularly sensitive to the seasonal signal.  
381 When investigating the decadal variability of the signals, it was found that most of the long heat  
382 waves occurs during the warmest periods. Thus, a possible explanation is that the heat wave signal  
383 in the models is more impacted by interannual to long term variability of the temperatures, while  
384 in the observations it is more sensitive to short term variations. It was also noticed that the large  
385 internal variability of the models could explain part of the long heat waves.

386 The circulation signal during heatwave events was verified with a composite analysis. The AMIP  
387 ensemble mean was consistent with reanalysis though individual members were less consistent.  
388 It was also verified that the composites of short heat waves (5-10 days) were consistent with the  
389 composites of all events, i.e. that the too persistent heat waves were not related to an incorrect  
390 dynamics. Finally, models were selected based on their heat wave length agreement with obser-  
391 vations taking account of internal variability and observational error. These filtered models had  
392 similar trends in the number of heat waves and heat wave days as the other members of the ensem-  
393 ble. Thus the biases on the persistence of HW events do not affect significantly the trends, the later  
394 being mainly controlled by the interannual variability of the temperature. Thus, if a model can re-  
395 produce the mean change in the temperatures, it is expected that it can also reproduce the trends  
396 of the heat waves. Other dynamical factors (such as the jet streams, the Circumglobal teleconnec-  
397 tions, the Western North Pacific High or the South Asia High) have been shown to influence the  
398 summer temperatures in China (e.g. Wang et al. 2013). We haven't investigated these processes in  
399 this study, thus they should be considered in the future as possible factors impacting heat waves in  
400 the models and eventually leading to biases in the persistence of the events.

401 Based on this study, the AMIP models were found reliable in terms of dynamics for the heat  
402 waves over Central-East China. Despite their tendencies to produce too persistent events, most of  
403 the AMIP members are able to reproduce the positive trends observed in both ground stations and  
404 reanalysis, and all results indicate an increase in the risk of such events during the past decades  
405 (from 4 events during the first decade to 8 events during the last decade). However, the long term  
406 trends in the models should be considered carefully due to some missing signals in the models  
407 (the decadal oscillation observed in ERAI and OBS). The mid-90s transition, especially clear in  
408 the models, should also be investigated in future work, as it raises the question of possible large  
409 scale impact of aerosols emissions. Finally, it is also noticeable that some uncertainties come

410 from the difference between observation and reanalysis. Larger datasets, such an ensemble of  
411 reanalysis, could be used to improve the estimation of these uncertainties.

412 Using directly the raw temperature threshold is justified as it impacts human health. However  
413 the methodology used to define heat waves may lead to uncertain results. Indeed, the signal may  
414 result from a mix between the natural warming due to the seasonal transition and a warming due  
415 to weather type circulation anomaly. Thus the persistence of the event could be attributed to  
416 one or the other. Moreover, the use of a fixed threshold to identify the duration of an event can  
417 lead to sensitive statistics (as an event could be cut in too with one day in the middle just below  
418 the threshold for instance). Thus a final advise is that statistics on heat waves should always be  
419 carefully associated with a margin of error due to the methodology and definition, the data used  
420 and the sampling.

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425 Environmental Laboratory.

## 426 APPENDIX

### 427 *a. Computation of composites*

428 The composite of  $X$  at a day  $d$  ( $X_d$ ) of a specific year ( $ann$ ) is given by equation 1. The cor-  
429 responding daily climatology ( $X_{d-clim}$ ) of the variable is first removed (Fig.A1). The difference  
430 between the annual mean of the year  $ann$  and the climatology (annual mean,  $X_{clim}$ ) is also removed  
431 from the composite. This method removes any long term trend effect (for instance, an elevation

432 of the geopotential height due to a global temperature warming) and only highlight the differences  
433 due to short terms anomalies.

## 434 **References**

435 Dee, D. P., and Coauthors, 2011: The ERA-Interim reanalysis: Configuration and performance of  
436 the data assimilation system. *Quarterly J. of the Roy. Met. Soc.*, **137(656)**, 553–597.

437 Ding, T., and W.-H. Qian, 2011: Geographical patterns and temporal variations of regional dry  
438 and wet heatwave events in China during 1960-2008. *Adv. in Atm. Sc.*, **28**, 322–337.

439 Dong, D., and G. Huang, 2015: Relationship between altitude and variation characteristics of the  
440 maximum, minimum temperature and diurnal temperature range in China. *Chinese J. of Atm.  
441 Sc.*, **39**, 1011–1024.

442 Freychet, N., H.-H. Hsu, C. Chou, and C.-H. Wu, 2015: Asian summer monsoon in CMIP5 projec-  
443 tions: A link between the change in extreme precipitation and monsoon dynamics. *J. Climate*,  
444 **28**, 1477–1493.

445 Freychet, N., H. H. Hsu, and C.-H. Wu, 2016: Extreme precipitation events over East Asia: Evalu-  
446 ating the cmip5 model. *Atmospheric Hazards - Case Studies in Modeling, Communication, and  
447 Societal Impacts*, J. S. M. Coleman, Ed., InTech, Rijeka, chap. 05, doi:10.5772/62996, URL  
448 <http://dx.doi.org/10.5772/62996>.

449 Freychet, N., S. F. B. Tett, J. Wang, and G. C. Hegerl, 2017: Summer heat waves over Eastern  
450 China: dynamical processes and trend attribution. *Env. Res. Lett.*, **12**, 024 015.

451 Gong, D. Y., and S. W. Wang, 2002: Uncertainties in the global warming studies [in chinese].  
452 *Earth Sci. Front.*, **9(2)**, 371–376.

- 453 Guo, X., J. Huang, Y. Luo, Z. Zhao, and Y. Xu, 2017: Projection of heat waves over China for  
454 eight different global warming targets using 12 CMIP5 models. *Theor. and App. Clim.*, **128(3-4)**,  
455 507–522.
- 456 Heisler, G. M., and A. J. Brazel, 2010: *The urban physical environment: Temperature and urban*  
457 *heat islands*. Am. Soc. of Agron., Crop Sci. Soc. of Am., Soil Sci. Soc. of Am.
- 458 Kripalani, R. H., J.-H. Oh, and H. S. Chaudhari, 2007: Response of the East Asian summer  
459 monsoon to doubled atmospheric CO<sub>2</sub>: Coupled climate model simulations and projections  
460 under IPCC AR4. *Theor. Appl. Climatol.*, **87**, 1–28.
- 461 Li, X., L. Wang, K. Yang, B. Xue, and L. Sun, 2013: Near-surface air temperature lapse rates in  
462 the mainland China during 1962–2011. *J. Geophys. Res. Atmos.*, **118**, 7505–7515, doi:10.1002/  
463 jgrd.50553.
- 464 Li, Z., and Z.-W. Yan, 2009: Homogenized daily mean/maximum/minimum temperatures series  
465 for China from 1960–2008. *Atm. and Oc. Sc. Lett.*, **2(4)**, 237–243.
- 466 Lin, C., and Coauthors, 2015: Impact of wind stilling on solar radiation variability in China.  
467 *Nature Sc. Reports*, **5(15135)**, doi:10.1038/srep15135.
- 468 Lu, R.-Y., and R.-D. Chen, 2016: A review of recent studies on extreme heat in China. *Atm. and*  
469 *Ocean. Sc. Lett.*, **9(2)**, 114–121.
- 470 Luber, G., and M. McGeehin, 2008: Climate change and extreme heat events. *Am. J. of Prev. Med.*,  
471 **35**, 429–435.
- 472 Luo, M., and N.-G. Lau, 2017: Heat waves in southern china: Synoptic behavior, long-term  
473 change, and urbanisation effects. *J. of Clim.*, **30(2)**, 703–720.

- 474 Perkins, S. E., 2015: A review on the scientific understanding of heatwaves their measurement,  
475 driving mechanisms, and changes at the global scale. *Atmos. Res.*, **164**, 242–67.
- 476 Ren, G.-Y., M.-Z. Xu, Z.-Y. Chu, A.-Y. Zhang, J. Guo, H.-Z. Bai, and X.-F. Liu, 2005: Changes  
477 of surface air temperature in China during 1951-2004. *J. Geophys. Res.*, **10(4)**, 717–727.
- 478 Ren, Y.-Y., D. Parker, G.-Y. Ren, and R. Dunn, 2016: Tempo-spatial characteristics of sub-daily  
479 temperature trends in mainland China. *Clim. Dyn.*, **46**, 2737–2748.
- 480 Sun, Y., X. Zhang, F. W. Zwiers, L. Song, H. Wan, T. Hu, H. Yin, and G. Ren, 2014: Rapid increase  
481 in the risk of extreme summer heat in eastern china. *Nature Clim. Change*, **4(12)**, 1082–1085.
- 482 Walters, D., and Coauthors, 2017: The Met Office Unified Model Global Atmosphere 6.0/6.1 and  
483 JULES Global Land 6.0/6.1 configurations. *Geosci. Model Dev.*, **10**, 1487–1520, doi:10.5194/  
484 gmd-10-1487-2017.
- 485 Wang, A., and J. Fu, 2013: Changes in daily climate extremes of observed temperature and pre-  
486 cipitation in China. *Atm. and Oc. Sc. Lett.*, **6**, 312–319.
- 487 Wang, S., X. Yuan, and Y. Li, 2016a: Does a strong el nio imply a higher predictability of extreme  
488 drought? *Nat. Scient. Rep.*, **7**, 40 741.
- 489 Wang, W., W. Zhou, X. Li, X. Wang, and D. Wang, 2016b: Synoptic-scale characteristics and  
490 atmospheric controls of summer heat waves in China. *Clim. Dyn.*, **46(9-10)**, 2923–2941.
- 491 Wang, W., W. Zhou, Y. Li, X. Wang, and D. Wang, 2015: Statistical modeling and cmip5 simula-  
492 tions of hot spell changes in china. *Clim. Dyn.*, **44**, 28592872.
- 493 Wang, W. W., W. Zhou, X. Wang, S. K. Fong, and K. C. Leung, 2013: Summer high tempera-  
494 ture extremes in southeast China associated with the East Asian jet stream and circumglobal  
495 teleconnection. *J. Geophys. Res.*, **118**, 8306–8319.



- 496 Wei, K., and W. Chen, 2011: An abrupt increase in the summer high temperature extreme days  
497 across china in the mid-1990s. *Adv. Atmo. Sc.*, **28**, 1023–1029.
- 498 Wu, Z., Z. Jiang, J. Li, S. Zhong, and L. Wang, 2012: Possible association of the western Tibetan  
499 Plateau snow cover with the decadal to interdecadal variations of northern China heatwave fre-  
500 quency. *Clim. Dyn.*, **39**, 2393–2402.
- 501 Yan, X., Y. Hou, and B. Chen, 2011a: Observed surface warming induced by urbanization in East  
502 China. *J. of Geop. R.: Atm.*, **116**, 2156–2202, doi:10.1029/2010JD015452.
- 503 Yan, Z., J. Xia, C. Qian, and W. Zhou, 2011b: Changes in seasonal cycle and extremes in China  
504 during the period 1960-2008. *Adv. in Atm. Sc.*, **28(2)**, 269–283.
- 505 You, Q., Z. Jiang, L. Kong, Z. Wu, Y. Bao, S. Kang, and N. Pepin, 2016: A comparison of heat  
506 wave climatologies and trends in china based on multiple definitions. *Clim. Dyn.*, **48**, 39753989.
- 507 Zhou, C.-L., and K.-C. Wang, 2016: Coldest temperature extreme monotonically increased and  
508 hottest extreme oscillated over Northern hemisphere land during last 114 years. *Nature Scient.*  
509 *Report*, **6:24721**.

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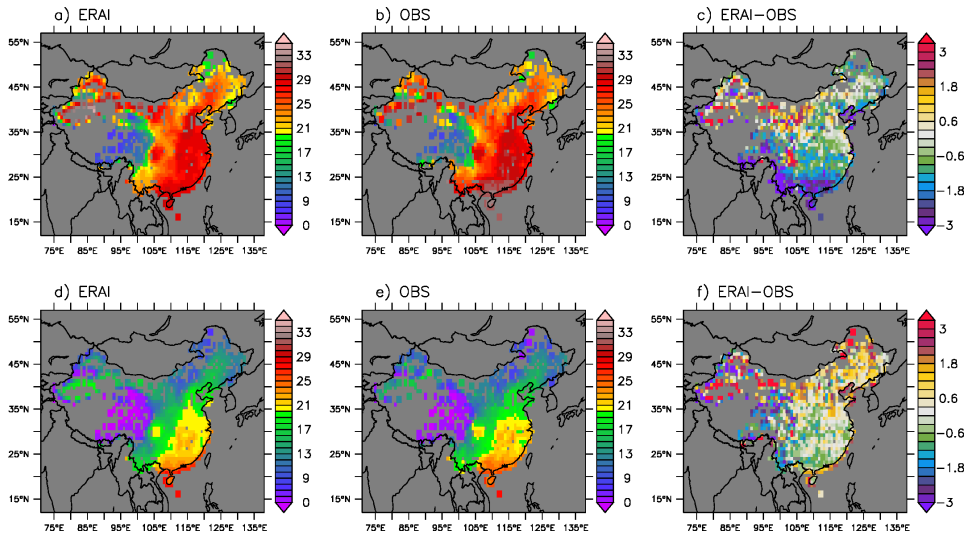
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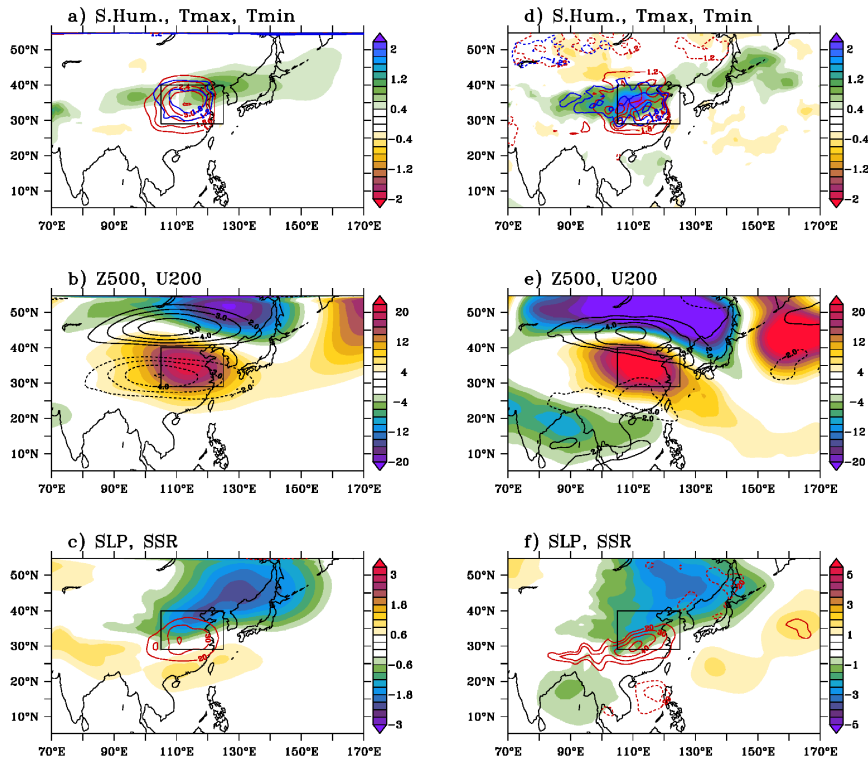
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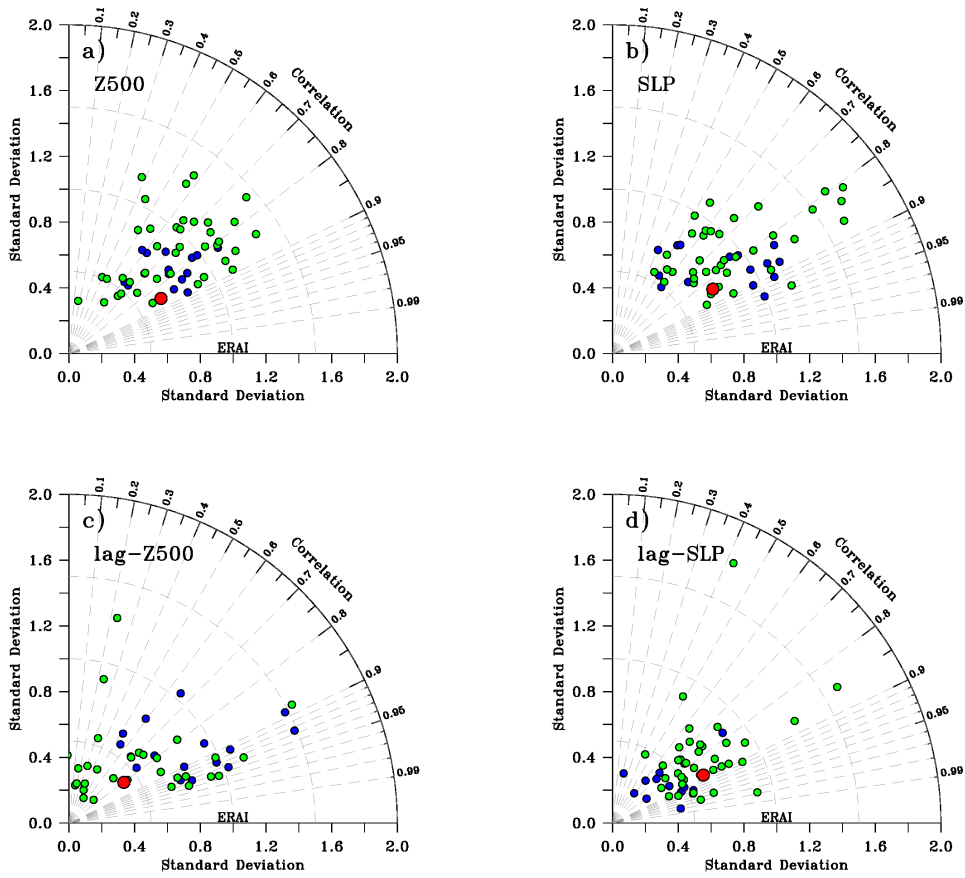
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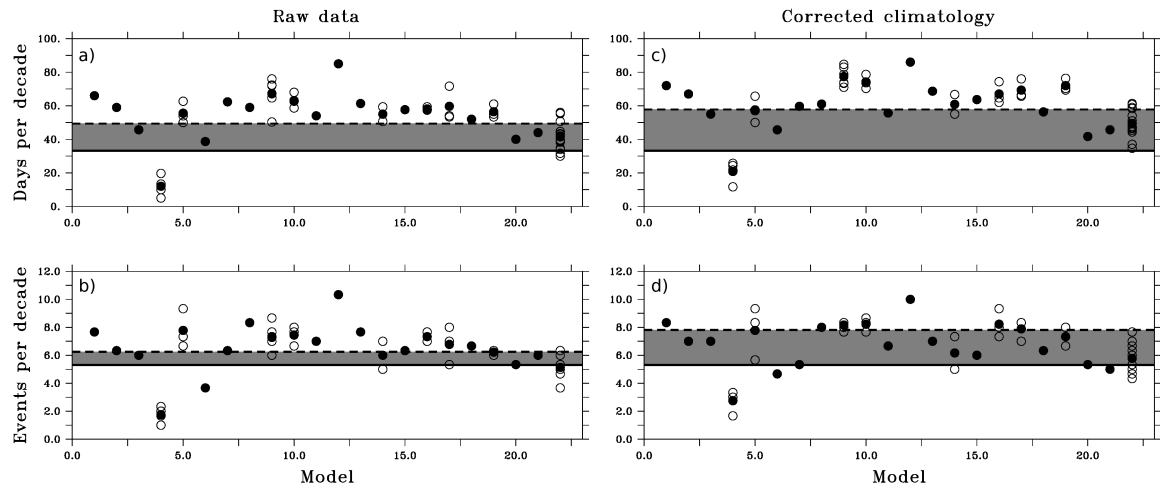
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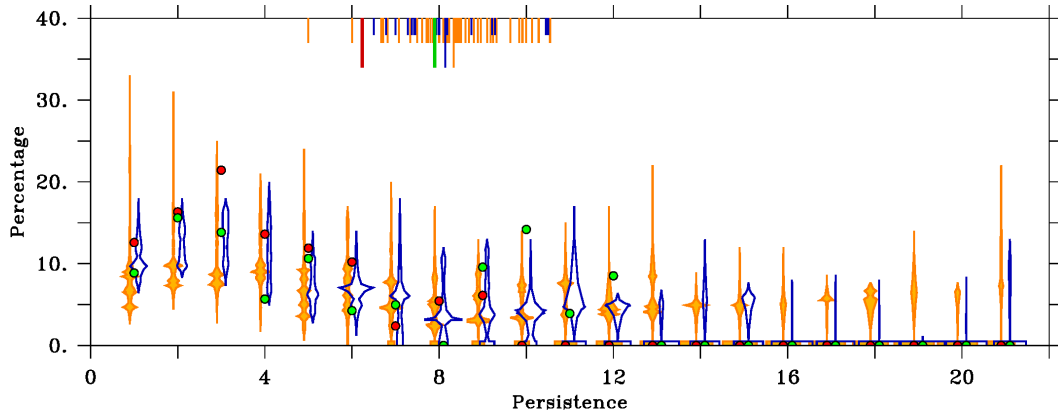


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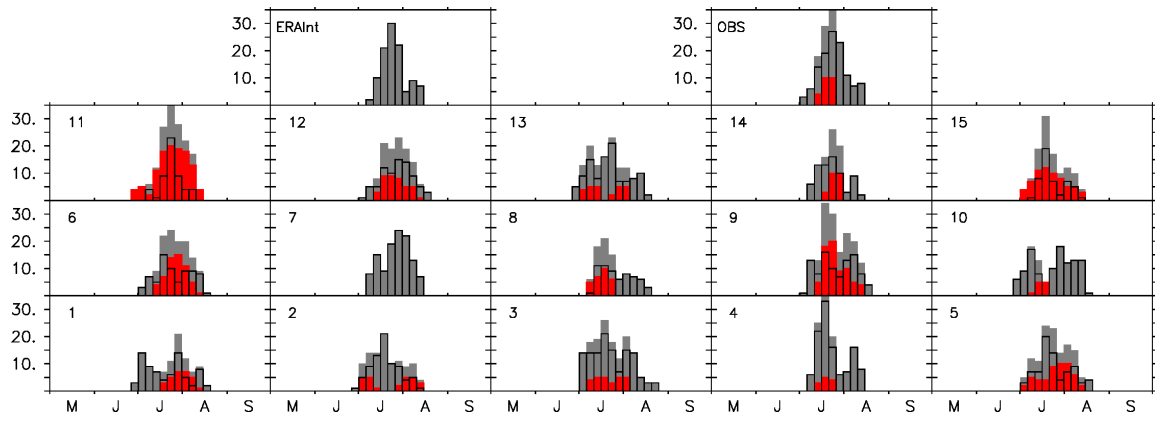


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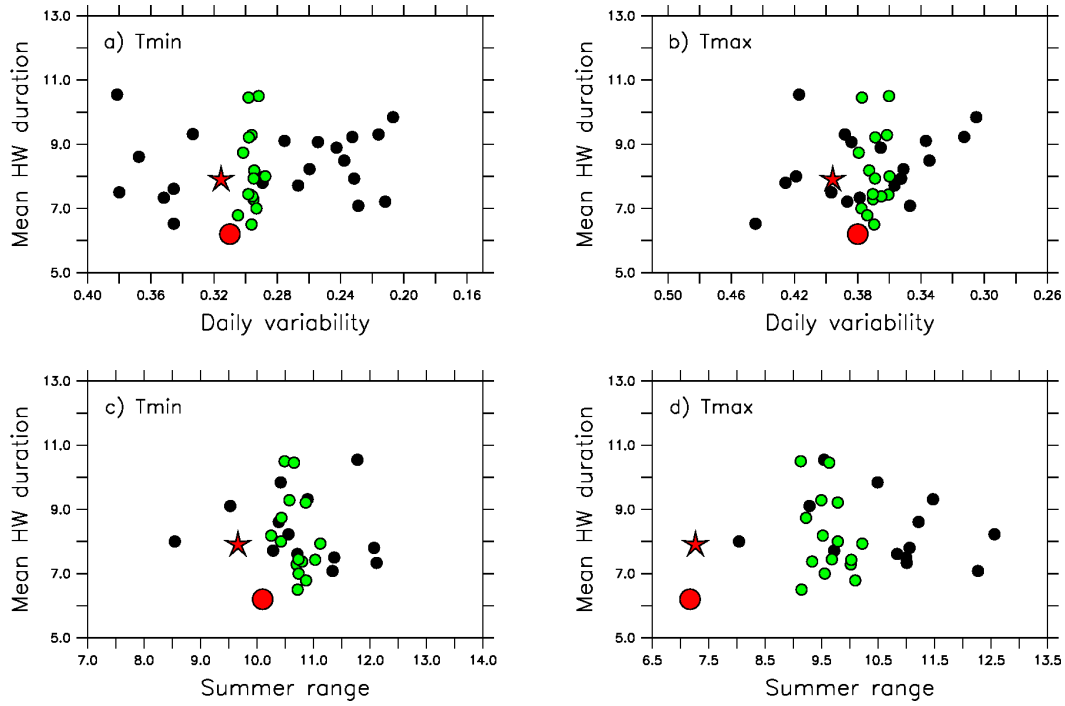




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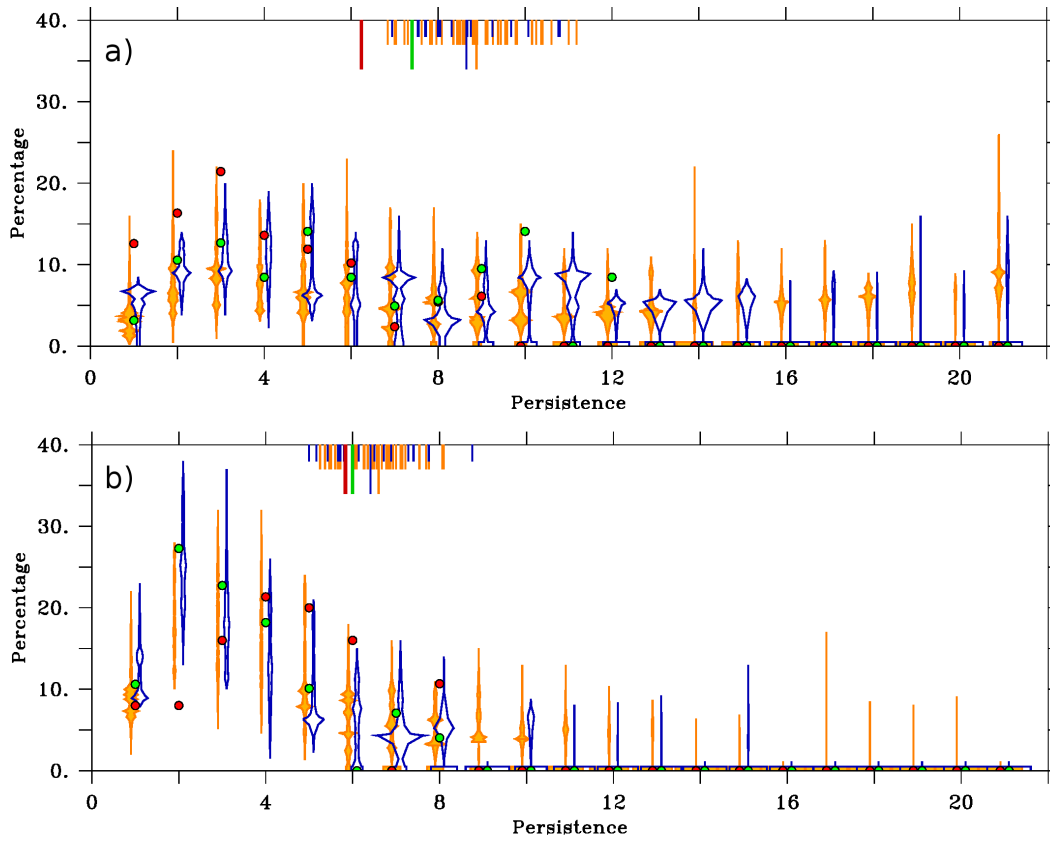
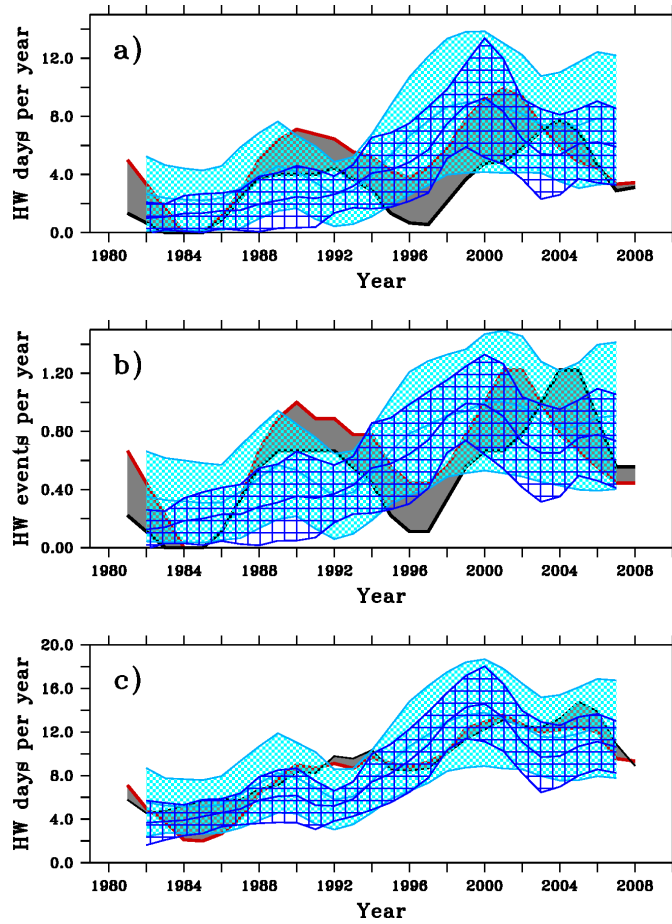
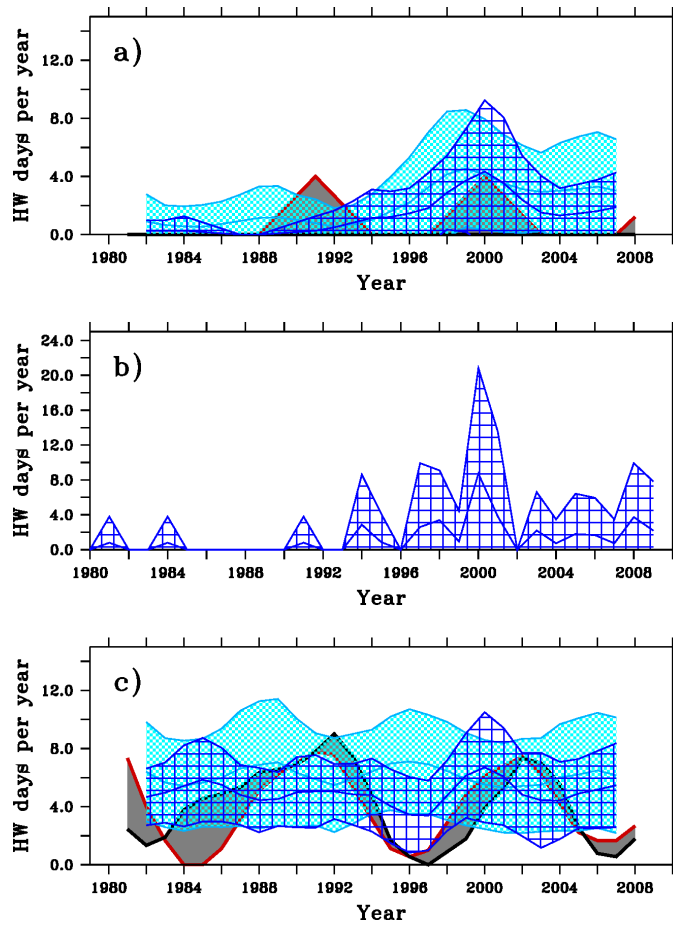


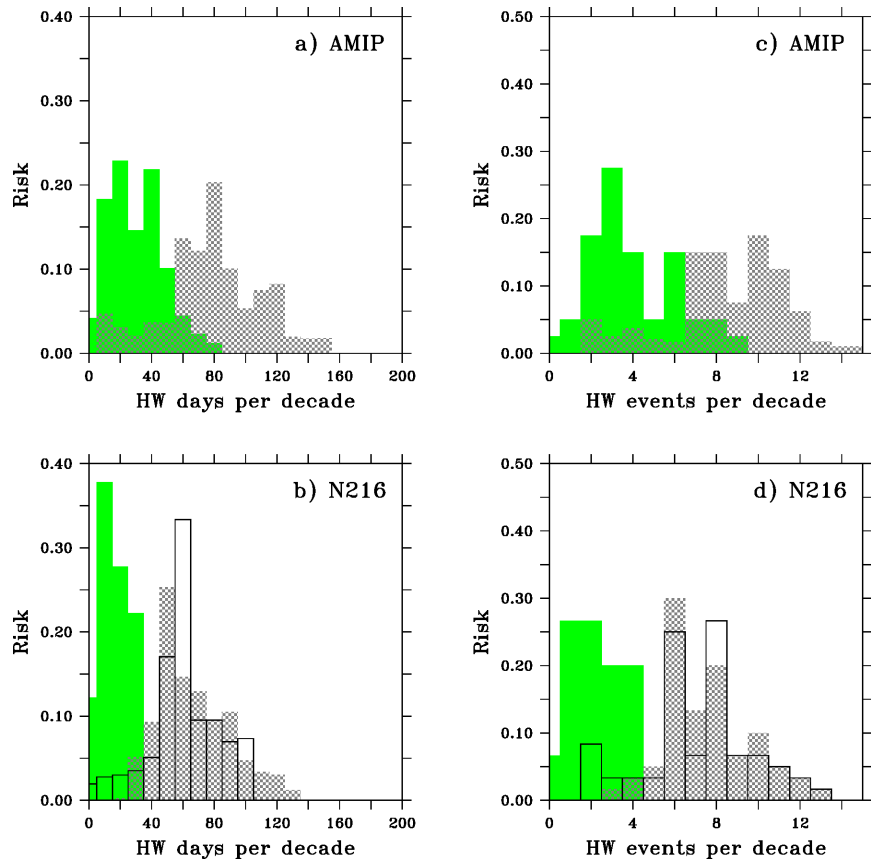
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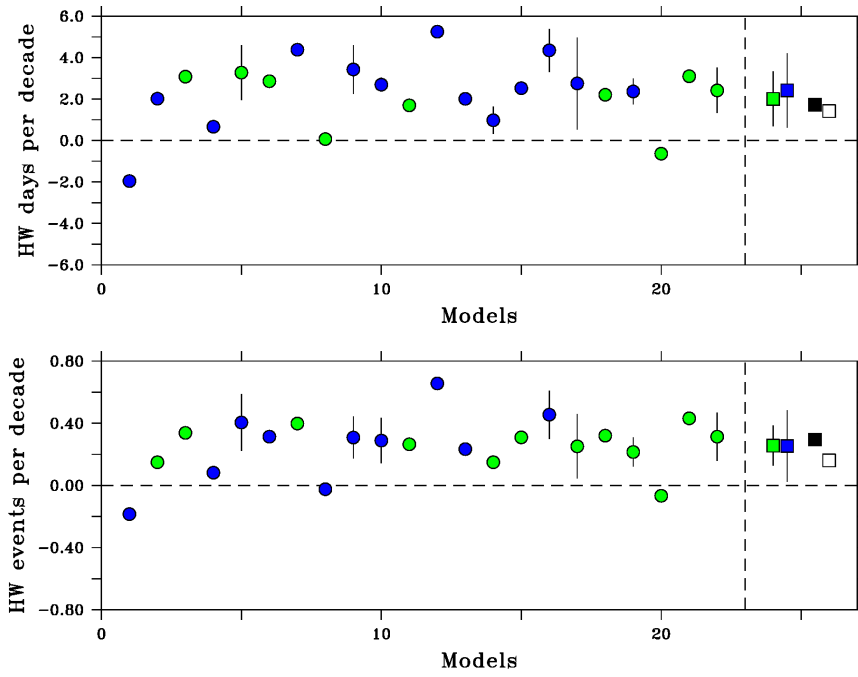
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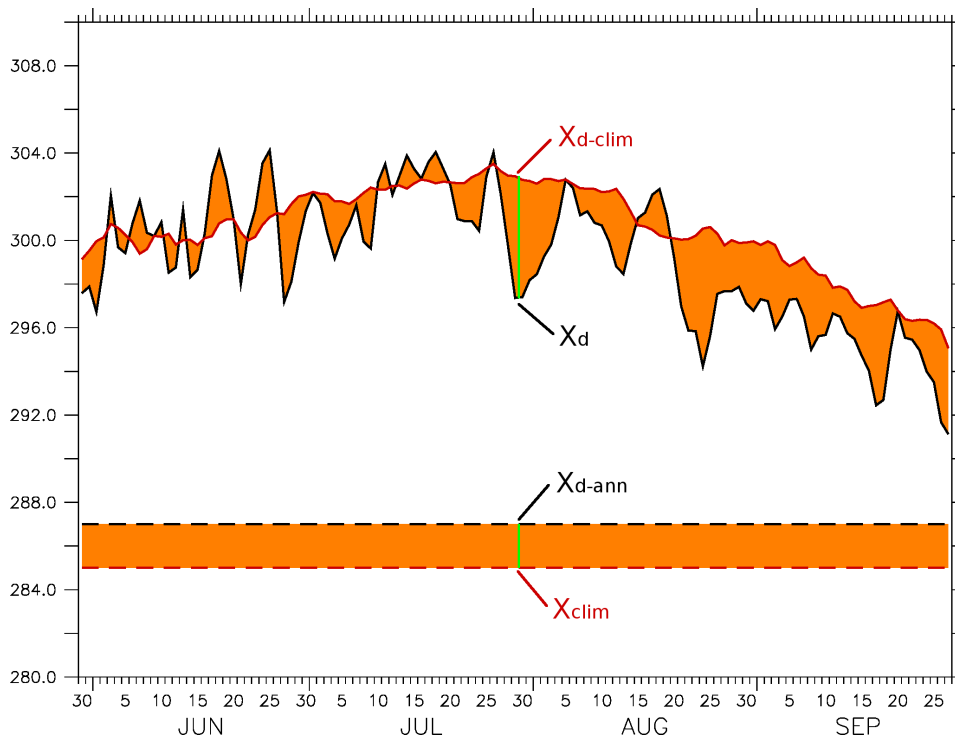


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