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Structural ordering in liquid gallium under extreme conditions

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The atomic-scale structure, melting curve, and equation of state of liquid gallium has been measured to high-pressure (p) and -temperature (T) up to 26 GPa and 900 K by *in situ* synchrotron x-ray diffraction. Ab *initio* molecular dynamics simulations up to 33.4 GPa and 1000 K are in excellent agreement with the experimental measurements, providing detailed insight at the level of pair distribution functions. The results reveal an absence of dimeric bonding in the liquid-state and a continuous increase in average coordination number \bar{n}_{Ga}^{Ga} from 10.4(2) at 0.1 GPa approaching ~ 12 by 25 GPa. Topological cluster analysis of the simulation trajectories finds increasing fractions of five-fold symmetric and crystalline motifs at high-*p*-*T*. Although the liquid progressively resembles a hard-sphere structure towards the melting curve, the deviation from this simple description remains large ($\geq 40\%$) across all *p*-*T*-space, with specific motifs of different geometries strongly correlating with low local two-body excess entropy at high-*p*-*T*.

Liquid metals and allows have exceptional properties that make them particularly attractive for applications: potential uses include electrical energy storage and generation as e.g. electrodes for all-liquid high capacity batteries [1] and efficient heat exchange fluids in concentrated solar power systems [2]. By virtue of their non-toxicity, low viscosity, and high thermal and electrical conductivity, low-melting point gallium-based liquid metals have applications from cooling integrated electronics to manufacturing flexible and reconfigurable electronic devices and soft robotics [3–6]. Such optimal thermo-physical properties are governed by the atomic-scale structure of these liquids. Knowledge of structural changes and solidification pathways in liquid metals at non-ambient pressure (p) and temperature (T) is essential for the development of new materials with novel physical properties and for operating under extreme conditions. Structural information of liquid metals is also key to understanding processes within deep terrestrial and exoplanetary interiors, including metallic core formation [7] and magnetic field generation [8]. While challenging, measuring liquid structure at elevated p-T conditions is a rapidly developing field [9–16].

Gallium is a remarkable metal, exhibiting a rich array of crystal structures at non-ambient p-T [17]. At ambient p-T, gallium exhibits an orthorhombic structure (Ga-I) with mixed metallic-covalent bonding featuring Ga₂ dimers [18, 19]. This mixed bonding gives rise to unusual characteristics including an anomalously low melting point ($T_{\rm m} = 302.9 \,\mathrm{K}$ [20]) and consequently one of the largest liquid ranges of any element, a 3.2 % volume contraction on melting, and a strong tendency for undercooling [20, 21]. At elevated-p the melting curve exhibits negative dT_m/dp up to the I-II-liquid triple point at 1.2 GPa [22] (Fig. 1). The existence of a first-order liquid-liquid phase transition (LLPT) has been postulated [23–26] on the basis that other candidate polyamorphic liquids exhibit similar anomalous behavior [27], notably water [28], silicon [29], sulphur [30], and phosphorous [9]. Previous in situ structural measurements of liquid gallium at highp are limited to ~ 6 GPa [26, 31–37] by synchrotron x-ray diffraction (SXRD) and 9 GPa by x-ray spectroscopy [38]. At ambient-p and $T_{\rm m}$ the average coordination number $\bar{n}_{\rm Ga}^{\rm Ga}$ increases from 7 in the solid Ga-I phase to $\sim~10$ [34], compared to a typical value of 11-12 in most liquid metals. A gradual increase in \bar{n}_{Ga}^{Ga} is observed with increasing p with a simple close-packed liquid predicted by $\sim 15 \,\mathrm{GPa}$ [34]. A similar evolution from a complex low-coordinated liquid to a simple liquid at high-p has been reported recently in shock compressed tin [39].

In this letter, we report the atomic-scale structure, melting curve, and equation of state of liquid gallium as measured by *in situ* SXRD up to 26 GPa, representing a > 4-fold increase in the *p*-range compared to previous experimental surveys. Complementary *ab initio* Molecular Dynamics (MD) simulations of the liquid atomistic structure were made to 33.4 GPa and 1000 K.

p-T conditions of up to 26 GPa and 900 K were achieved using a membrane driven diamond anvil cell (DAC) with Boehler-Almax anvils (\emptyset 500 μ m culet) surrounded by a Watlow coiled resistive heater within a vacuum vessel [40, 41]. Temperature was measured using a K-type thermocouple attached to one anvil, close to the gasket. To prevent alloying with the gasket, the liquid gallium droplet was loaded into an annulus of dry NaCl (130 μ m inner diameter) [42] within the \emptyset 165 μ m sam-



FIG. 1. Melting curve for gallium. SXRD acquisitions are denoted by open (liquid) or closed (solid) circles (run 1) or squares (run 2). Enlarged symbols represent locations of longer acquisitions for liquid structure determination. The diamonds are the mid-points of melting brackets fitted to the Simon Glatzel equation (solid line). The blue field represents 95% confidence bands. The + symbols denote the p-T conditions in the ab initio MD simulations. The previously reported low-p liquid (L) and crystalline (I, II, III) phase boundaries are also shown (black lines) [22]. The inset shows an example diffraction image in the liquid field.

ple chamber drilled in a pre-indented rhenium gasket. SXRD measurements were made at beamline I15, Diamond Light Source, UK using a Perkin-Elmer 1621 EN flat panel detector and a monochromatic 56 keV x-ray beam collimated by a 20 μ m tungsten pinhole to ensure a clean signal from the wholly liquid sample. This offers a significant advantage over laser-heated DAC or shock compression experiments which both suffer from contamination of the liquid signal by diffraction peaks arising from e.g. thermal insulation media or non-melted solid [13, 39]. Pressure was determined from additional SXRD measurements of the NaCl annulus at each step and the known p-T equation of state of NaCl [52]. We constrained the melting curve by observing either liquid diffuse scattering or Bragg peaks in regular 20s SXRD acquisitions along a stepped p-T path (Fig. 1.). The mid-points of the melting brackets were fitted to a Simon-Glatzel [53] equation

$$T_{\rm m} = 319 \left(\frac{p-3.03}{a}+1\right)^{1/c},$$
 (1)

modified to force the fit through the I-II-liquid triple point [22] using orthogonal distance regression and yielding a = 6.0(1) and c = 1.58(2). Longer, 20 minute acquisitions were made at ~2-3 GPa steps in the liquid field just above the melting curve. At the end of the experiment an SXRD measurement of the DAC containing the recovered empty gasket was made to characterize the dominant background component originating from Compton scattering from the diamond anvils. The single crystal diamond reflections were masked prior to integration of the two-dimensional diffraction images.

Density functional theory (DFT) electronic structure calculations were performed using the Vienna Ab Initio Software Package (VASP) [54, 55]. The electronic interactions were described by the projector-augmented wave (PAW) [56, 57] pseudopotentials with an [Ar] core and $3d^{10}4s^24p^1$ valence electrons. The Perdew-Burke-Ernzerhof (PBE) formulation of the generalized gradient approximation (GGA) exchange correlation functional [58] was used with an energy cut-off value of 500 eV, sampling the Brillouin zone at the Γ -point. Molecular dynamics trajectories were calculated in the canonical (NVT) ensemble with N = 600 Ga atoms. Smaller boxes did not accurately reproduce the low-q features observed by experiment. Simulations at various initial volumes (V), were heated at 6000 K for 2 ps, cooled to target temperatures of T = 400, 600, 800, or 1000 K over 2.5 ps, and equilibrated for 15 ps with a simulation timestep of 1 fs. An additional simulation at the ambient-p density at $T_{\rm m}$ of 0.0526 Å^{-3} (6.095 g cm³ [59]) yields p = 24.38 GPa via the computed stress tensor. This value was subtracted from the computed p at each V-T to correct for the inherent underbinding of the GGA functional. The compute time for a 5 ps simulation interval was approximately 7 days using the University of Bristol BlueCrystal Phase 4 supercomputer on 10 nodes with 28 central processing units (CPUs) per node.

The measured *p*-dependent structure factors $S_{\text{GaGa}}(Q)$ and pair distribution functions

$$g_{\text{GaGa}}(r) - 1 = \frac{1}{2\pi^2 r n_0} \int_0^\infty Q[S_{\text{GaGa}}(Q) - 1]\sin(Qr) dQ$$
(2)

shown in Fig. 2 (a) & (b), were obtained by normalizing the background-corrected diffraction patterns using the formalism of Eggert *et al.* [60], as implemented in our code LiquidDiffract [61]. This iterative procedure [42] exploits the simple behaviour of the reduced pair distribution function $G(r) = -4\pi n_0 r [g_{GaGa}(r) - 1)]$ prior to the first interatomic distance, to eliminate the Q-space manifestations of the un-physical low-r contributions and provide a converged solution for the liquid atomic number density n_0 (Å⁻³) (Fig. 3 (a)). The *ab initio* MD $g_{\text{GaGa}}(r)$ and corresponding $S_{\text{GaGa}}(Q)$ functions were computed from the final 5 ps of the simulation trajectories using the R.I.N.G.S. code [62]. The agreement between the $S_{\text{GaGa}}(Q)$ and $g_{\text{GaGa}}(r)$ functions as measured in the DAC at 0.1 GPa (the lowest p) and computed from the *ab initio* MD simulations at ambient-p and 303 K (this study) with previous ambient-p results from neutron and x-ray diffraction measurements [63], is excellent (Fig. 2. (a)). We find no evidence from the measured $g_{\text{GaGa}}(r)$ or *ab initio* MD trajectories for short (< 2.5 Å) Ga-Ga bonds under any p-T condition, indicating that dimeric bonding characteristic of the Ga-I structure does not per-



FIG. 2. (a) Structure factors $S_{\text{GaGa}}(Q)$ measured in the DAC by SXRD, and (b) corresponding pair distribution functions $g_{\text{GaGa}}(r)$ obtained by Fourier transformation (black curves). Previously reported ambient-*p* measurements [63] are represented by the open red circles. A selection of the S_{GaGa} and $g_{\text{GaGa}}(r)$ functions computed from the *ab initio* MD trajectories are also shown at comparable conditions just above the melting curve at (i) 303 K, (ii) 3.4 GPa, 400 K, (iii) 10.9 GPa, 600 K, (iv) 18.3 GPa, 800 K, and (v) 33.4 GPa, 1000 K (dashed blue curves).

sist in the liquid state. The *p*-evolution of the computed $S_{\text{GaGa}}(Q)$ and $g_{\text{GaGa}}(r)$ (Fig. 2) is in good general agreement with the experiment, although with increasing *p* the experimental reciprocal-space data suffer from increasing statistical uncertainty leading to poorer resolution and stronger Fourier transform artifacts in real-space.

The first peak in $S_{GaGa}(Q)$ features a pronounced high-Q should r that becomes less pronounced by $\sim 15 \,\mathrm{GPa}$ in the experimental measurements, matching the p at which liquid Ga is predicted to transform to a hard-sphere like liquid [34]. However, we note the first peak remains asymmetric in the experimental measurements and a distinct shoulder can be resolved in the simulation results. A Mie-Gruniesen-Debye thermal equation of state [64] determined from a fit to the high-p-T ab initio MD results, with parameters $V_0 = 19.043(13) \text{ Å}^3$, K = 50.3(6) GPa, $K' = 4.75(4), q = -0.09(21), D = 325 \text{ K}, g_0 = 2.07(4),$ and $g_{\infty} = 0$, agrees with the experimentally derived density within the limits of uncertainty (Fig. 3(a)). The first peak in $g_{\text{GaGa}}(r)$ shifts to smaller radii with increasing p, from $r_{\text{GaGa}} = 2.79(2)$ Å measured in the DAC at 0.1 GPa to $2.58(2)\,\mathrm{\AA}$ at 25.9 GPa and 891 K. The development of average coordination number \bar{n}_{Ga}^{Ga} with increasing p, as obtained by integrating over the measured $g_{\text{GaGa}}(r)$ or directly from the *ab initio* MD trajectories with a cut-off value $r_{\rm cut} = 3.5 \,\text{A}$, are shown in Fig. 3 (b). The experimental and simulation results are in good agreement



FIG. 3. (a) Mie-Gruniesen-Debye thermal equation of state isotherms from 300 K (blue) to 1000 K (red) in 100 K steps. (b) Average coordination number \bar{n}_{Ga}^{Ga} . Solid circles with error bars denote SXRD, open symbols denote *ab initio* MD. The dashed black curve indicates the density approximated to 6 GPa from ultrasonic measurements [34].

within the limits of uncertainty revealing a continuous increase in $\bar{n}_{\text{Ga}}^{\text{Ga}}$ on densification from ~ 10 at ambient-*p* towards close packed liquid values of ~ 12 by 26 GPa.

Recent studies of the local structure of gallium at elevated-p have employed Reverse Monte Carlo (RMC) modeling [33, 34, 36]. RMC is a fitting strategy to generate an atomistic model by minimizing the difference between experimental data (e.g. the pair distribution function) and an input configuration. However, we show that this naive RMC approach can be misleading by comparison with direct analysis of the local structure of the liquid *ab initio* MD trajectories. This is illustrated in Fig. 4 which compares the local structure obtained by analy-



FIG. 4. Comparison of structural features between *ab initio* MD and RMC for a selected state point and two distinct seeds for the RMC fitting: an ordered and a disordered configuration. (a) Voronoi spectrum. (b) TCC spectrum. The structural motifs are illustrated with rings indicated by colored bonds. (c) Pair distribution functions from *ab initio* MD (green background) and the two RMC fits (overlapping blue dots and red line).



FIG. 5. Fractional population of atoms detected in a given motif in the *ab initio* MD trajectories close to the melting curve, where 6A: octahedra, 6Z: tetrahedral tripyramids, 7A: pentagonal bipyramids, 10A: twisted double square pyramids, 10B: a partial icosahedron, 11F: a section of a hexagonal closed packed layer, and 12D: a complex combination of four pentagonal rings.

sis of the *ab initio* MD result at T = 1000 K, p = 3.2 GPa with new RMC results obtained using two different initial guesses: a disordered configuration (obtained via a linear compression algorithm) and an ordered fcc configuration at the relevant density, constrained by the *ab initio* MD $g_{\text{GaGa}}(r)$ function [42]. In our analysis of the simulation trajectories, we employ two descriptors of local structure: Voronoi indices and the Topological Cluster Classification (TCC) algorithm [65]. In the former case, we count the fraction of particles in polyhedra (non-uniquely) identified by a vector of integers representing the histogram of the number of edges on the faces. In the latter case, the local environment of the particles is compared to a pre-defined library of elementary motifs that are important in simple classical liquids, as they minimize the local energy.

For consistency with a recent RMC study of liquid gallium to 1.9 GPa interpreted by Voronoi tessellation [36], we first consider a selection of Voronoi motifs (Fig. 4(a)). These results show that naive RMC constrained solely to an input $g_{\text{GaGa}}(r)$ not only fails to reproduce the *ab initio* MD structure but also produces different results depending on the starting configuration. In particular, icosahedral motifs [0,0,12,0], which are marginal in the *ab initio* MD, are more highly represented in the disordered RMC but entirely absent in the ordered RMC. In fact, the ordered RMC has preserved strong signatures of crystalline order [42]. Similar behavior is observed in the TCC analysis (Fig. 4(b)). For simplicity, we present the results for a set $\{S\}$ of seven specific motifs which describe different types of local environments: tetrahedal ordering (6Z) which is a precursor to crystallization, motifs with fourmembered rings (6A,10A,11F), and five-fold symmetric ordering (7A, 10B, 12D). Pentagonal structures such as 7A and 10B are over-represented in the disordered RMC and absent in the ordered RMC, while crystal-like patterns such as 11F, which have small fractions in the abintio MD, are over-represented in the ordered RMC. All

these differences emerge despite the naive impression of a good convergence of pair correlations (Fig. 4(c)).

We continue the analysis focusing on the TCC motifs, due to their relative simplicity of interpretation compared to Voronoi indices. Fig. 5 shows how the structural features change as we move from low- to high-p-T along the melting curve. With increasing T and p the abundance of larger motifs increases. Among these, the five-fold symmetric 10B and the crystalline 11F units stand out, as their abundance almost doubles from low- to high-p-T. In order to understand to what extent such structural changes result from effective excluded-volume effects, we performed a mapping onto a system of hard spheres in the Percus-Yevick approximation and compare the TCC spectra of *ab initio* MD with event-driven molecular dynamics [66] for hard spheres [42]. We define a scoring function as a weighted average of the relative deviations of the fractions n_i ,

$$\Delta = \sum_{i \in \{S\}} w_i |n_i^{\text{Ga}} - n_i^{\text{HS}}| / n_i^{\text{Ga}}, \qquad (3)$$

where the weight $w_i = s_i / \sum_{j \in \{S\}} s_j$ is proportional to the number of particles s_i in the TCC motif *i*. Performing this calculation on all the *ab initio* MD results delivers a contour map of the deviation from hard-sphere behavior (Fig. 6). Although hard-sphere features become progressively more important towards the melting curve, the deviation is always $\Delta \geq 40\%$ such that they do not model a sizable part of the emerging structural correlations. Metastable hard sphere liquids show the formation of low configurational entropy regions [67]. These can be related to the so-called local two-body excess entropy

$$s_{2}^{i} = -2\pi n_{0} \int_{0}^{\infty} \left[\tilde{g}^{i}(r) \log \left(\tilde{g}^{i}(r) \right) - \tilde{g}^{i}(r) + 1 \right] r^{2} \mathrm{d}r,$$
(4)

which accounts for fluctuations in the (smoothed) local pair correlations $\tilde{g}^i(r)$ of particle *i* [42]. This measurement is not an entropy difference, but connects local structural variations to entropic contributions [68–70].



FIG. 6. (a) Deviation from hard-sphere structure Δ : evaluated state points (circles) and interpolated contour map. (b) Distribution (violin-plots) of locally averaged two-body excess entropy for particles in different local environments.

Utilising the *ab initio* MD configurations, we measure the local excess entropy and compare its distributions for atoms in different local environments. Fig. 6 shows that despite broad fluctuations, the 10B and 11F motifs, as well as fivefold symmetric 12D motifs, have significantly lower values of s_2 , suggesting that gallium at high-*p*-*T* forms regions of exceptionally low configurational entropy, which may help to stabilize the glassy phase beyond the melting curve.

From our combined SXRD experimental and *ab initio* MD simulation approach we have considerably extended the p-T conditions at which the melting curve, equation of state, and nature of local structural ordering in liquid gallium is known. The results reveal an increase in local coordination number $\bar{n}_{\rm Ga}^{\rm Ga}$ approaching \sim 12 with increasing densification. Analysis of the *ab initio* MD trajectories reveals the concomitant increase of the number of five-fold symmetric and crystalline motifs at highp-T. Both form regions of low local entropy, a behaviour that contrasts with purely repulsive hard spheres, which are dominated by five-fold symmetry. Previous studies predict the development of hard-sphere like behaviour in liquid gallium [34] and tin [39]. However, we find that although the local structure progressively resembles that of hard-spheres when approaching the melting curve, the deviation from this simple description is always $\geq 40\%$ across all p-T space. The presence of low configurational entropy motifs in the liquid provides a mechanism for the promotion of metastable polyamorphic phases beyond the high-p melting curve. The emergence of novel amorphous phases from supercooled regimes may be explored in future work using effective potentials checked by liquid structure measurements using heating elements inside the DAC [71] for rapid T quenching at high-p.

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