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A Time Series Analysis and Forecasting of Opening Stock Price of McDonald's Crop.

Rawiyah Muneer Alraddadi 2055 Napoleon Rd, Unit 8H, Bowling Green, OH 43402 rawiyah-2013@hotmail.com

Abstract

McDonald's Corp. is globally famous and is abounded in recent years. It is one of the major chain restaurants that offers a fast food. Basic foods that are served at McDonald's are different types and sizes of burgers, fries, some breakfast, sweets, ice cream and kid's meals.

McDonald's products have increased loyalty from customers, which has led to the rise of an uneven stock price. So the data is not stationary and makes the role of the analyst's ability to forecast the future condition of the organization important. The aim of this paper is to analyze and forecast the opening stock price of McDonald's Corp. over a period time.

Keywords

Price; forecast; stationary; stock; open

1. Data Description

The Time Series Analysis of the opening price of McDonald's Corp. from January 2006 to December 2014 is complete. Real time data of the opening stock price of McDonald's Corp. is collected from yahoo finance. Source Link:(http://finance.yahoo.com/q/hp?s=AAPL&a=11&b=12&c=1980&d=3&e=1&f=2016&g=d& z=66&y=0).

2. Time-Series Data Model

2.1. Original Data

Time Series Plot of Opening Stock Price of McDonald's Corp.

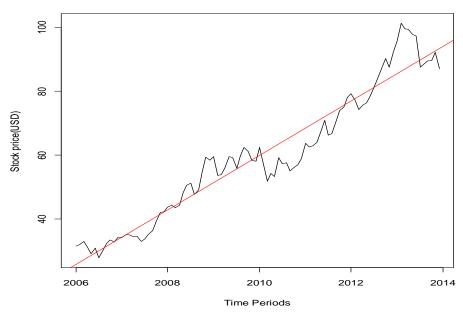


Table 1. Augmented Dickey-Fuller Test (ADF Test)

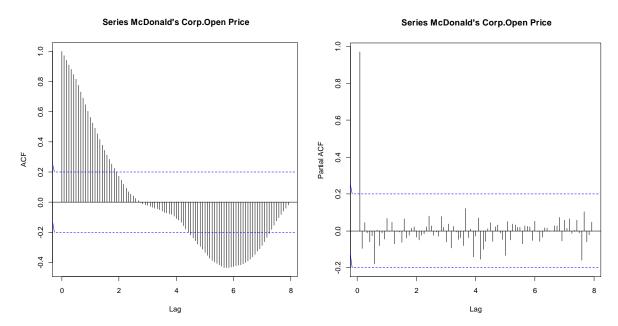
Dickey-Fuller	-2.2111
p-value	0.4892
Lag Order	4

The monthly stock open price of McDonald's Corp. from January 2006 to December 2014 was selected to build the model. In the time series plot, the observations from January 2006 to December 2013 indicate the data used



to fit the model, while the data from January 2014 to December 2014 indicate the last 12 observations used for comparison with the forecasts.

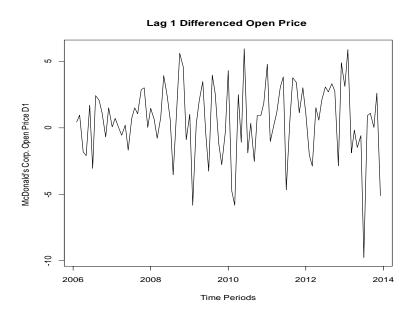
The first procedure is to check for stationarity in all-time series analysis. The obvious increasing trend showed in the time series plot indicates a non-stationarity. The ADF Test results a P-value of 0.4892, which also indicates as the original data is not stationary with a 5% level significance.



The slow decline in the Autocorrelation Function (ACF) plot indicates that the observations are correlated or not independent, and also the immediate cut in the Partial Autocorrelation Function (PACF) plot also confirms that. Thus, the original data is neither stationary nor does it indicate the existence of a trend in the data set.

Obviously the trend of McDonald's Corp. stock price indicates an upward parabola. This shows that a lag 1 differencing needs to be taken in order to stabilize and make the trend linear.

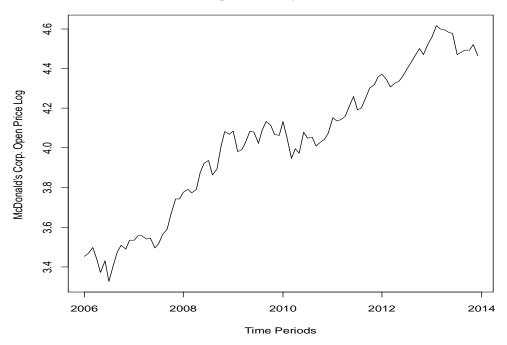
2.2. Making The Time Series Stationary



First, the lag 1 difference of the data is taken. The time series plot of lag 1 difference shows that it seems to be mean stationary, but the variance is non-stationary. The variance increases as time goes on. Therefore, logarithmic transformation needs to be taken into consideration.



Log of The Open Price



Take the log transformation on the original data, the time series plot of the transformed data looks better than that of the original data since the increase or drop isn't as severe as was before, which indicates log transformation performs well in eliminating the variance non-stationary.

Lag Difference of Log (Open Price)

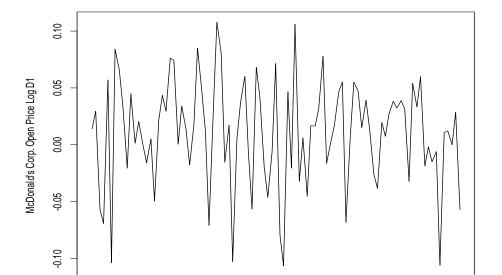


Table 2. Augmented Dickey-Fuller Test (ADF Test)

2010

Time Periods

2012

2008

2006

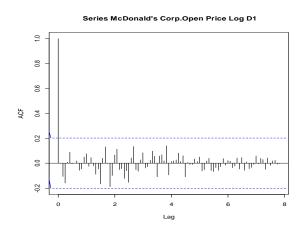
Dickey-Fuller	-4.4712
p-value	0.01
Lag Order	4

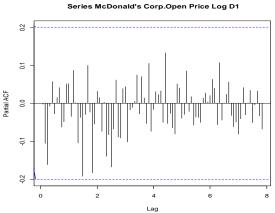
2014



Take the log transformation on the lag 1 difference of original data. The time series looks pretty good, both mean and variance seems to be stationary. The ADF Test results a P-value of 0.01, which indicates the lag 1 difference logarithmic transformed data is stationary with 5% level of significance.

2.3. Model Fitting

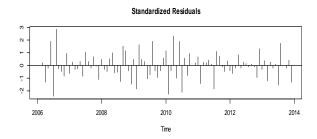




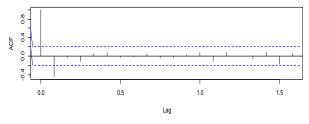
ACF and PACF plot confirms that the transformed data is stationary both in mean and variance. Also, from the ACF and PACF plot it is clear that the transformed data is White Noise.

Table 3. Model fitting

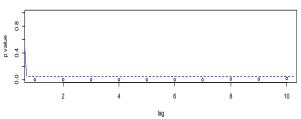
Description	ARIMA (0,1,0)
Sigma ²	0.004381
Log Likelihood	121.85
AIC	-241.71



ACF of Residuals



p values for Ljung-Box statistic



As seen in the time series diagram output, the model is valid or acceptable for the following reasons. The ACF of the residual confirms that the residuals are White Noise. In addition, all the P-values of the Ljung-box statistics are way above the boundary, which confirms the non-independence of the residuals.

2.4. Model Equation

$$log X_t - log X_{t-1} = Z_t$$

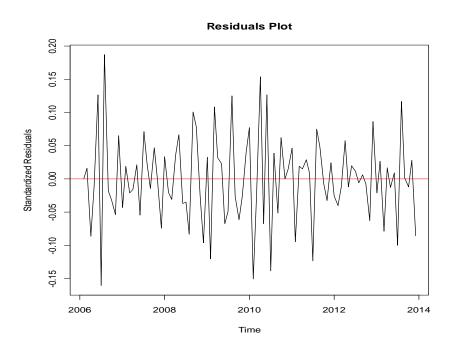
$$\log \frac{X_t}{X_{t-1}} = Z_t$$

$$\frac{X_t}{X_{t-1}} = e^{Z_t}$$

$$X_t = X_{t-1} e^{Z_t}$$

The last equation is the final model.

2.5. Residual Assessment





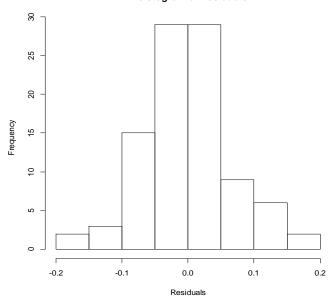
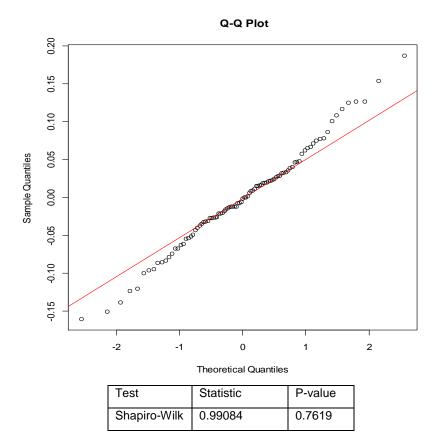


Table 4. Test for

Normality





The sequence plot of the standardized residuals looks random, which shows the independent assumption holds. In the normal probability plot, there is some minor curvature to the plot with possible outliers, but the Shapiro-Wilk Test indicates that normality of the error terms in the ARIMA (0,1,0) model cannot be rejected. In summary, the time series seems to be well-represented by the ARIMA (0,1,0) model.

3. Forecasting and Summary

We fitted an ARIMA (0,1,0) model on the log transformed data, which indicates the algorithm of the original data is an AR (1) model. The forecast values of the next twelve months are showed below, with a 95% confidence interval:





Table 5. Forecasting

Date	Actual Data	Forecast	Lo 95	Hi 95
Jan 2014	96.81	88.40030	80.39722	96.40337
Feb 2014	94.54	89.02635	78.43016	99.62253
Mar 2014	94.24	89.65240	76.95305	102.35175
Apr 2014	98.10	90.27845	75.75129	104.80562
May 2014	100.68	90.90451	74.73106	107.07795
Jun 2014	101.39	91.53056	73.84144	109.21967
Jul 2014	100.43	92.15661	73.05116	111.26207
Aug 2014	94.30	92.78266	72.33940	113.22593
Sep 2014	93.24	93.40872	71.69151	115.12593
Oct 2014	94.37	94.03477	71.09670	116.97284
Nov 2014	93.78	94.66082	70.54680	118.77485
Dec 2014	96.15	95.28688	70.03539	120.53836

There is no big gap between the actual values and forecasts, which indicates that the model is good. In addition, the 95% confidence interval increases as time goes on, so that a more accurate prediction for recent observations can be given, while less accurate predictions for further observations are given.

In this model, the data series are monthly stock prices, in which one month is not considered short term to stock market. Therefore, it's reasonable that the model is some kind of White Noise since monthly data can be regarded as long term data series. That is to say, in a long term, stock price is hard to predict or even unpredictable just based on the past observations.

Many other forms of research also present the potential of ARIMA models in predicting stock prices in a short term basis, which could benefit the investment decision making. In a short term, as a backward looking statistical method, time series model which was built to outperform the way of randomly guessing the fluctuation of future stock price. However, since the model doesn't consider the events and information that would influence the stock price, one can hardly say in a long term that stock prices can be forecasted accurately.

REFERENCES

I. Cryer, Jonathan, D., Chan, and Kung, 2008. Time series Analysis.